1. Memcheck

a. Invalid write of size 4

```
==7844== Invalid write of size 4
==7844== at 0x1091C0: main (memleak.c:49)
==7844== Address 0x4a7d068 is 0 bytes after a block of size 40 alloc'd
==7844== at 0x484684F: malloc (vg_replace_malloc.c:393)
==7844== by 0x10919E: main (memleak.c:46)
==7844==
```

Explanation:

The program allocates 40 bytes of memory using the malloc() function, which is enough space to store 10 integers (i.e., malloc(10 * sizeof(int)) gives access to arr[0] - arr[9] in the heap). However, it writes an additional 4 bytes (the size of an int) just after the allocated memory block. Accessing arr[10], which is one element beyond the valid range of arr[0] to arr[9]. This kind of error results in a heap buffer overflow, where memory outside the allocated region is being incorrectly modified. So, occur invalid write of size 4.

The possible loop used in this test:

```
int *arr = (int *)malloc(10 * sizeof(int));

for (int i = 0; i <= 10; i++) {

    arr[i] = 0; // Error when i = 10 \rightarrow out-of-bounds write

}
```

To slove the error we need to adjust our loop like below:

```
int *arr = (int *)malloc(10 * sizeof(int));
for (int i = 0; i < 10; i++) {
          arr[i] = 0;
}</pre>
```

b. Invalid read of size 4

```
==7844== Invalid read of size 4
==7844== at 0x1091ED: main (memleak.c:54)
==7844== Address 0x4a7d068 is 0 bytes after a block of size 40 alloc'd
==7844== at 0x484684F: malloc (vg_replace_malloc.c:393)
==7844== by 0x10919E: main (memleak.c:46)
==7844==
```

Explanation:

This error occurs when the program attempts to read 4 bytes (the size of an int) from memory just beyond the allocated buffer. Just like the invalid write error, this happens because the program accesses an out-of-bounds index, like arr[10], when only arr[0] through arr[9] are valid. This time, the program is trying to read from that invalid memory location. So, occur invalid read of size 4.

The possible loop used in this test:

```
int sum = 0; for (int i = 0; i \le 10; i++) { sum += arr[i]; // Error when i = 10 \rightarrow \text{out-of-bounds read} }
```

To slove the error we need to adjust our loop like below:

```
int sum = 0;
for (int i = 0; i < 10; i++) {
    sum += arr[i];
}</pre>
```

```
==7844== Conditional jump or move depends on uninitialised value(s)
            at 0x48D2OCB: __printf_buffer (vfprintf-process-arg.c:58)
==7844==
            by 0x48D373A: vfprintf internal (vfprintf-internal.c:1544)
==7844==
==7844==
            by 0x48C81B2: printf (printf.c:33)
==7844==
            by 0x109214: main (memleak.c:57)
==7844==
==7844== Use of uninitialised value of size 8
            at 0x48C70BB: _itoa_word (_itoa.c:183)
==7844==
            by 0x48D1C9B: __printf_buffer (vfprintf-process-arg.c:155)
==7844==
            by 0x48D373A: vfprintf internal (vfprintf-internal.c:1544)
==7844==
==7844==
            by 0x48C81B2: printf (printf.c:33)
==7844==
            by 0x109214: main (memleak.c:57)
==7844==
==7844== Conditional jump or move depends on uninitialised value(s)
            at 0x48C70CC: _itoa_word (_itoa.c:183)
==7844==
==7844==
            by 0x48D1C9B: __printf_buffer (vfprintf-process-arg.c:155)
==7844==
            by 0x48D373A: vfprintf internal (vfprintf-internal.c:1544)
            by 0x48C81B2: printf (printf.c:33)
==7844==
==7844==
            by 0x109214: main (memleak.c:57)
==7844==
==7844== Conditional jump or move depends on uninitialised value(s)
            at 0x48D1D85: __printf_buffer (vfprintf-process-arg.c:186)
==7844==
==7844==
            by 0x48D373A: vfprintf internal (vfprintf-internal.c:1544)
==7844==
            by 0x48C81B2: printf (printf.c:33)
==7844==
            by 0x109214: main (memleak.c:57)
==7844==
```

Explanation:

This error means that the program is using a function such as printf based on a value that was never initialized. Typically, this happens when a variable (such as an integer or pointer) is declared but not assigned any value before being used in output or computation. In C, variables are not automatically initialized to zero. Instead, they contain whatever random data is already present at that memory location. This is known as a "garbage value" and using it can cause unpredictable behavior, like:

- Use of uninitialized value of size 8:
 - A value is used (e.g., printed) before being set.
- Conditional jump or move depends on uninitialized value(s):
 - The program makes a decision (e.g., an if-condition or printf's formatting logic) using that garbage value.

The possible program used in this test:

To slove the error we need to adjust our program like below:

d. Argument 'size' of malloc has a fishy (possibly negative) value

```
==7844== Argument 'size' of function malloc has a fishy (possibly negative) value: -40 ==7844== at 0x484684F: malloc (vg_replace_malloc.c:393) ==7844== by 0x109220: main (memleak.c:61)
```

Explanation:

This error means the program is calling malloc() with an invalid size, specifically a negative number (e.g., -40). In C, the argument passed to malloc() must be a non-negative value of type size_t. However, when a negative integer is implicitly converted to size_t, it wraps around into a very large positive number, causing unexpected behavior or allocation failures. This usually happens when the size passed to malloc is incorrect values, such as:

The possible program used in this test:

```
int size = -10;
int *arr = (int *)malloc(size * sizeof(int)); // results in malloc(-40)
```

To slove the error we need to adjust our program like below:

```
int size = 10;
int *arr = (int *)malloc(size * sizeof(int)); // malloc(40), OK
```

e. Invalid free() / delete / delete[] / realloc()

```
==7844== Invalid free() / delete / delete[] / realloc()
==7844==
            at 0x48490C4: free (vg replace malloc.c:884)
==7844==
            by 0x10924A: main (memleak.c:65)
==7844==
          Address 0x4a7d4f0 is 0 bytes inside a block of size 40 free'd
==7844==
            at 0x48490C4: free (vg_replace_malloc.c:884)
==7844==
            by 0x10923E: main (memleak.c:64)
          Block was alloc'd at
==7844==
            at 0x484684F: malloc (vg replace malloc.c:393)
==7844==
==7844==
            by 0x10922E: main (memleak.c:63)
```

Explanation:

This error means the program attempted to free a memory block that was already freed earlier. In C, calling free() on the same pointer more than once leads to undefined behavior, such as crashing or corrupting the heap. In the log, we can see Address $0 \times 4a7d4f0$ is 0 bytes inside a block of size 40, This indicates that the program is trying to free the exact same block of memory that was already released. The first call to free() was valid, but the second call to free() on the same pointer caused the error. So, occur invalid free() / delete / delete[] / realloc()

The possible program used in this test:

```
int *arr = malloc(40);
free(arr);
free(arr); // Error: double free
```

To slove the error we need to adjust our program like below:

```
int *arr = malloc(40);
free(arr);
arr = NULL; // Clears the pointer
free(arr); // Safe: free(NULL) does nothing
```

f. Memory leak

```
==7844== 40 bytes in 1 blocks are definitely lost in loss record 1 of 1
            at 0x484684F: malloc (vg replace malloc.c:393)
==7844==
==7844==
            by 0x10919E: main (memleak.c:46)
==7844==
==7844== LEAK SUMMARY:
==7844==
            definitely lost: 40 bytes in 1 blocks
            indirectly lost: 0 bytes in 0 blocks
==7844==
              possibly lost: 0 bytes in 0 blocks
==7844==
            still reachable: 0 bytes in 0 blocks
==7844==
==7844==
                 suppressed: 0 bytes in 0 blocks
```

Explanation:

This error means the program allocated memory on the heap using malloc(), but never released it using free(). More specifically, the pointer to the allocated memory was either lost, went out of scope, or was simply never freed, making it impossible to reclaim that memory during the program's execution. We can see in log, 40 bytes in 1 blocks are definitely lost. This means 40 bytes of memory were allocated but no corresponding free() was found. The tag "definitely lost" mean that no pointer still points to that memory, it is permanently unreachable. So, occur memory leaked.

The possible program used in this test:

```
int *arr = (int *)malloc(40);
// ... some code
// forgot to call free(arr); before program ends
```

To slove the error we need to adjust our program like below:

```
int *arr = (int *)malloc(40);
// use arr ...
free(arr); // explicitly free the allocated memory
```

2. Cachegrind

```
$ cat 312551002_bad_loc
                          $ cat 312551002 good lo
=15714== Cachegrind, a cache and branch-prediction profiler
=15714== Copyright (C) 2002-2017, and GNU GPL'd, by Nicholas Nethercote et al.
=15714== Using Valgrind-3.20.0 and LibVEX; rerun with -h for copyright info
                                                                                          ==15715== Cachegrind, a cache and branch-prediction profiler
==15715== Copyright (C) 2002-2017, and GNU GPL'd, by Nicholas Nethercote et al
                                                                                           =15715== Using Valgrind-3.20.0 and LibVEX; rerun with -h for copyright info
=15714== Command: ./good
                                                                                           =15715== Command: ./bad
=15714== Parent PID: 7540
                                                                                          ==15715== Parent PID: 7540
=15714==
                                                                                           =15715==
 -15714-- warning: L3 cache found, using its data for the LL simulation.
                                                                                           -15715-- warning: L3 cache found, using its data for the LL simulation.
=15714==
                                                                                           =15715==
=15714== I
              refs:
                           30,158,770
                                                                                           =15715== I
                                                                                                         refs:
                                                                                                                      30,158,770
 =15714== I1 misses:
                                 1,063
                                                                                           =15715== I1 misses:
                                                                                                                           1,065
=15714== LLi misses:
                                 1,042
                                                                                           ==15715== LLi misses:
                                                                                                                           1,044
=15714== I1 miss rate:
                                  0.00%
                                                                                           ==15715== I1 miss rate:
                                                                                                                            0.00%
 =15714== LLi miss rate:
                                                                                           =15715== LLi miss rate:
                                  0.00%
                                                                                                                            0.00%
 =15714==
                                                                                           =15715==
=15714== D refs:
                           14,052,656 (12,039,322 rd + 2,013,334 wr)
                                                                                           =15715== D refs:
                                                                                                                      14,052,656 (12,039,322 rd + 2,013,334 wr)
=15714== D1 misses:
                              126,516 ( 63,684 rd + 62,832 wr)
                                                                                          ==15715== D1 misses:
                                                                                                                        203,632 ( 102,995 rd + 100,637 wr)
==15714== LLd misses:
                                                                                          ==15715== LLd misses:
                                63,811 (
                                               1,000 rd +
                                                                 62,811 wr)
                                                                                                                          63,810 (
                                                                                                                                            999 rd +
                                                                                                                                                           62,811 wr)
==15714== D1  miss rate:
                                   0.9% (
                                                 0.5%
                                                                     3.1% )
                                                                                          ==15715== D1 miss rate:
                                                                                                                             1.4% (
                                                                                                                                            0.9%
                                                                                                                                                               5.0% )
 =15714== LLd miss rate:
                                                                                           =15715== LLd miss rate:
                                                                                                                              0.5% (
 =15714==
                                                                                          ==15715==
==15714== LL refs:
                               127,579 (
                                              64,747 rd
                                                           +
                                                                 62,832 wr)
                                                                                          ==15715== LL refs:
                                                                                                                         204,697 (
                                                                                                                                       104,060 rd
                                                                                                                                                     +
                                                                                                                                                          100,637 wr)
                                                                                           =15715== LL misses:
 :15714== LL misses:
                                               2,042 rd
                                                                                                                          64,854
                                                                                                                                          2,043 rd
                                64,853
                                                                 62,811 Wr
                                                                                                                                                            62,811 Wr
 =15714== LL miss rate:
                                   0.1%
                                                 0.0%
                                                                                           =15715== LL miss rate:
                                                                                                                             0.1%
                                                                                                                                            0.0%
```

Explanation:

Metric	./good	./bad	Explanation
D1 misses (data cache)	126,516	203,632	bad has 77,116 more cache misses
D1 miss rate	0.9% (0.5% + 3.1%)	1.4% (0.9% + 5.0%)	bad shows much higher write miss rate
LL references (LL refs)	127,579	204,697	More frequent access to last-level cache in bad

Although both programs execute the same number of instructions and data accesses, their cache behaviors are very different. This difference is caused by how the programs access memory in loops. In C, arrays are stored in row-major order, meaning that elements in the same row are stored next to each other in memory. good accesses adjacent memory addresses, so better cache hit rate, bad jumps between distant memory addresses, so more cache misses.

This explains:

- D1 (data cache) miss rate is higher in ./bad (1.4%) than in ./good (0.9%)
- Write miss rate in ./bad is 5.0%, compared to ./good's 3.1%
- LL (last-level cache) accesses are higher in ./bad due to more frequent cache evictions

The possible program used in good test:

```
for (int i = 0; i < rows; i++)
  for (int j = 0; j < cols; j++)
    matrix[i][j]++; // good locality</pre>
```

The possible program used in bad test:

```
for (int j = 0; j < cols; j++)
    for (int i = 0; i < rows; i++)
        matrix[i][j]++; // poor locality</pre>
```

The performance gap between good and bad is caused by inefficient memory access in bad. Although both programs do the same amount of work, bad accesses memory in a way that leads to poor cache utilization (likely column-wise), while good uses a more cache-friendly (row-wise) access pattern. This demonstrates how data locality can have a significant impact on performance.

3. Massif

a. Please observe the relationship between time and memory allocation throughout the **entire** program execution, and provide **one** screenshot of the output file containing relevant information. (You must clearly display the total number of **snapshots** each time the system records the information **in intervals**).

```
ben@ben-server:~/Desktop$ ms_print massif.out.20416
Command:
Massif arguments: --time-unit=B
ms_print arguments: massif.out.20416
234.0^
                                          :::#:@
                                        @@::: #:@
                                      ::::@ ::: #:@
                                    :::::: @ ::: #:@
                                  @:
                                   :: ::: @ ::: #:@
                              :::::::@: :::: @ :::: #:@
                                        @ ::: #:@
                                 @: :::::
                                         ::: #:@
                                 @:
                                        0
                        ::0:: ::::::
                                 @:
                                        0
                                            #:0
                     @:
                                        0
                                         ::: #:@
                    @ ::: #:@
                                 @:
                 @ ::: #:@
                                 @:
                ::::0:: :::::::
                                 @: :::::
                                        @ ::: #:@
              @: :: ::: @ ::: #:@
       ::::::::
     0: :: ::: 0 ::: #:0
 0
                                            -->KB
                                           243.9
  0
Number of snapshots: 76
Detailed snapshots: [9, 19, 29, 39, 49, 59, 65 (peak), 75]
```

Explanation:

The output reveals a steadily increasing trend in heap memory usage throughout the program's execution. This pattern reflects continuous memory allocation without corresponding deallocation, due to the absence of free() calls in the source code.

No significant memory release is observed, suggesting that all allocated memory is retained until the program terminates. A total of 76 snapshots were recorded by Massif, 75 at regular intervals and 1 final snapshot at the program's end. The massif graph clearly illustrates a gradual and consistent growth in heap memory, driven by nested function calls and persistent allocations.

b. Then, point out how many bytes are allocated and used at peak respectively.

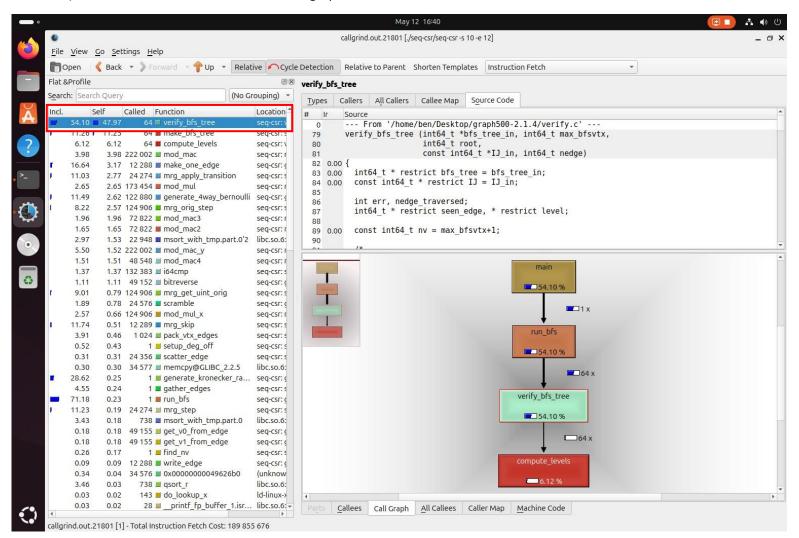
n	time(B)	total(B)	useful-heap(B) ext	a-heap(B)	stacks(B)				
60	225,568	225,568	225,000	568	0				
61	229,576	229,576	229,000	576	0				
62	231,584	231,584	231,000	584	0				
63	235,592	235,592	235,000	592	0				
64	239,600	239,600	239,000	600	0				
65	239,600	239,600	239,000	600	0				
99.75% (239,000B) (heap allocation functions) malloc/new/new[],alloc-fns, etc.									
->48.4	1% (116,000B) 0x1	0919A: a (in /	home/ben/Desktop/hea	ap)					
->26	.71% (64,000B) 0x	1091B4: b (in	/home/ben/Desktop/he	eap)					
->	10.02% (24,000B)	0x1091CE: c (i	n /home/ben/Desktop,	/heap)					
	->03.34% (8,000B)	0x1091F7: d (in /home/ben/Desktop	/heap)					
	->01.67% (4,000	B) 0x109234: e	(in /home/ben/Deskt	top/heap)					
	->01.67% (4,000	B) 0x1092C3: m	ain (in /home/ben/De	esktop/heap)					

Explanation:

- Overall Trend: Heap memory usage continuously increases, indicating sustained allocation without deallocation.
- **Peak Usage**: The peak heap memory usage occurs at snapshot 65, reaching 239600 bytes, of which 239000 bytes are useful heap and 600 bytes are extra heap (heap management overhead).
- Primary Allocation Sources:
 - a () is the top contributor, allocating approximately **116,000 bytes (48.41%** of total heap).
 - a () is repeatedly called via b () \rightarrow c () \rightarrow c () \rightarrow e (), forming a recursive call chain that leads to layered memory allocations.
 - All function calls ultimately originate from main (), making it the root cause of heap memory growth.
- **Potential Memory Leak**: Since no free() operations are observed, the memory is never deallocated during execution. This behavior strongly suggests a memory leak, where memory is allocated repeatedly but not released, resulting in a cumulative increase in usage.

4. Callgrind

a. Please use kcachegrind GUI to indicate which function is most expensive in terms of time (**excluding the time of their callee functions**). Please include a screenshot of the call graph.



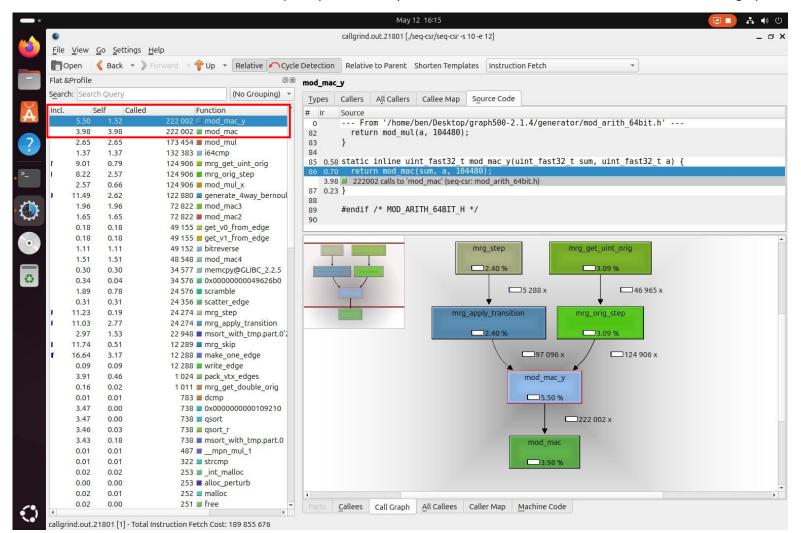
Explanation:

To determine which function is most expensive in terms of execution time (excluding time spent in its callees), we refer to the "Self" column in kcachegrind GUI. This value reflects the number of instructions executed directly within the function itself.

According to the kcachegrind GUI, the function verify_bfs_tree has the highest Self cost of 47.97%, making it the most time-consuming function in terms of its own operations. This indicates that nearly half of all instruction fetches during execution occurred within this function alone. It was invoked 64 times, each from the run_bfs() function.

The call graph shows the hierarchy: main() \rightarrow run_bfs() \rightarrow verify_bfs_tree() \rightarrow compute_levels().

b. Point out which function is called most frequently, and identify its caller as well. Please include a screenshot of the call graph.



Explanation:

The most frequently called function is mod_mac_y, which was called 222002 times directly by its callers. Although mod_mac is also called 222002 times, it is only called internally within mod_mac_y.

From the call graph, mod_mac_y is called 222002 time by:

- mrg_apply_transition: 97,096 times
- mrg_orig_step: 124,906 times

5. Pytorch profiler

a. Please follow the tutorial to get the columns shown in the picture below. Please provide a screenshot of the analysis result, ensuring that the username and machinename are visible in the first line. Then, identify the top three functions in terms of CPU time excluding the time of their callee functions, **except for the model label** (e.g. model_inference in tutorials).

Name	C-16 CDU W	C-16 CDII	CDU +-+-1 W	CDU +-+-1	CDU time	CDII Man	C-16 CDU M	4 -5 0
Name	Self CPU %	Self CPU	CPU total %	CPU total	CPU time avg	CPU Mem	Self CPU Mem	# of Ca
aten::addmm	52.10%	8.510ms	56.10%	9.163ms	186.993us	3.66 Mb	3.66 Mb	
aten::bernoulli	10.01%	1.635ms	10.01%	1.635ms	96.154us	0 b	0 b	
model inference	9.36%	1.529ms	100.00%	16.333ms	16.333ms	6.09 Mb	-5.63 Mb	
aten::copy	7.06%	1.154ms	7.06%	1.154ms	8.807us	0 b	0 Ь	
aten::bmm	2.05%	335.458us	2.07%	337.504us	18.750us	673.88 Kb	673.88 Kb	
aten::clamp min	1.85%	302.395us	1.85%	302.395us	50.399us	1.27 Mb	1.27 Mb	
aten::mul	1.42%	232.024us	1.42%	232.024us	13.648us	900.00 Kb	900.00 Kb	
aten::add	1.34%	218.978us	1.34%	218.978us	12.881us	900.00 Kb	900.00 Kb	
aten::einsum	1.19%	194.623us	7.93%	1.294ms	71.912us	2.10 Mb	0 b	
ten::native_layer_norm	1.12%	182.561us	1.34%	219.010us	14.601us	798.19 Kb	768 b	
aten::_softmax	1.05%	171.399us	1.05%	171.399us	19.044us	205.88 Kb	205.88 Kb	
aten::view	0.90%	146.264us	0.90%	146.264us	0.710us	0 b	0 b	
aten::tril	0.86%	140.302us	0.86%	140.302us	140.302us	576 b	576 b	
aten::empty	0.77%	125.341us	0.77%	125.341us	1.266us	2.88 Mb	2.88 Mb	
aten::div_	0.73%	119.502us	1.14%	185.556us	10.915us	8 b	-60 b	
aten::reshape	0.61%	99.454us	5.24%	856.204us	6.850us	1.90 Mb	0 b	
aten::linear	0.60%	97.645us	58.06%	9.483ms	193.521us	3.66 Mb	0 b	
aten::permute	0.55%	90.178us	0.67%	110.028us	1.223us	0 Ь	0 b	
aten::unsqueeze	0.52%	84.698us	0.59%	96.300us	2.534us	0 Ь	0 b	
aten::index_select	0.46%	74.819us	0.55%	90.630us	22.658us	216.00 Kb	216.00 Kb	

Explanation:

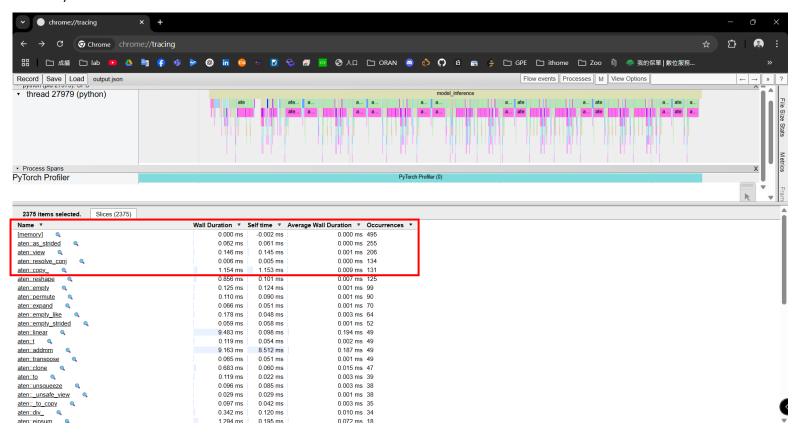
The top three functions can be find based on the "Self CPU %" or "Self CPU" columns.

1. aten::addmm (Self CPU %: 52.10%, Self CPU total: 8.510ms)

2. aten::bernoulli_ (Self CPU %: 10.01%, Self CPU total: 1.635ms)

3. aten::copy_ (Self CPU %: 7.06%, Self CPU total: 1.154ms)

b. Output the profiling results to <output>.json and analyze in Chrome trace viewer. Take a screenshot of the visualization and point out **which two functions (colors)** appear the most (in terms of time), **except for the model label** (e.g. model_inference in tutorials).



Name	Self CPU %	Self CPU	CPU total %	CPU total	CPU time avg	CPU Mem	Self CPU Mem	# of Cal
aten::addmm	52.10%	8.510ms	56.10%	9.163ms	186.993us	3.66 Mb	3.66 Mb	
aten::bernoulli	10.01%	1.635ms	10.01%	1.635ms	96.154us	0 b	0 b	
model_inference	9.36%	1.529ms	100.00%	16.333ms	16.333ms	6.09 Mb	-5.63 Mb	
aten::copy	7.06%	1.154ms	7.06%	1.154ms	8.807us	0 b	0 b	1
aten::bmm	2.05%	335.458us	2.07%	337.504us	18.750us	673.88 Kb	673.88 Kb	
aten::clamp min	1.85%	302.395us	1.85%	302.395us	50.399us	1.27 Mb	1.27 Mb	
aten::mul	1.42%	232.024us	1.42%	232.024us	13.648us	900.00 Kb	900.00 Kb	
aten::add	1.34%	218.978us	1.34%	218.978us	12.881us	900.00 Kb	900.00 Kb	
aten::einsum	1.19%	194.623us	7.93%	1.294ms	71.912us	2.10 Mb	0 b	
ten::native_layer_norm	1.12%	182.561us	1.34%	219.010us	14.601us	798.19 Kb	768 b	
aten::_softmax	1.05%	171.399us	1.05%	171.399us	19.044us	205.88 Kb	205.88 Kb	
aten::view	0.90%	146.264us	0.90%	146.264us	0.710us	0 b	0 b	2
aten::tril	0.86%	140.302us	0.86%	140.302us	140.302us	576 b	576 b	
aten::empty	0.77%	125.341us	0.77%	125.341us	1.266us	2.88 Mb	2.88 Mb	
aten::div_	0.73%	119.502us	1.14%	185.556us	10.915us	8 b	-60 b	
aten::reshape	0.61%	99.454us	5.24%	856.204us	6.850us	1.90 Mb	0 b	1
aten::linear	0.60%	97.645us	58.06%	9.483ms	193.521us	3.66 Mb	0 Ь	
aten::permute	0.55%	90.178us	0.67%	110.028us	1.223us	0 Ь	0 Ь	
aten::unsqueeze	0.52%	84.698us	0.59%	96.300us	2.534us	0 Ь	0 b	
aten::index select	0.46%	74.819us	0.55%	90.630us	22.658us	216.00 Kb	216.00 Kb	

Explanation:

Chrome Trace Viewer shows the two functions that appear the most, which we can see the "Occurrences" (corresponding to the "# of Calls" column in the 5-1 results). We ignore memory-related events and PyTorch functions.

- 1. aten::view (# of Calls: 206)
- 2. aten::copy_ (# of Calls: 131)