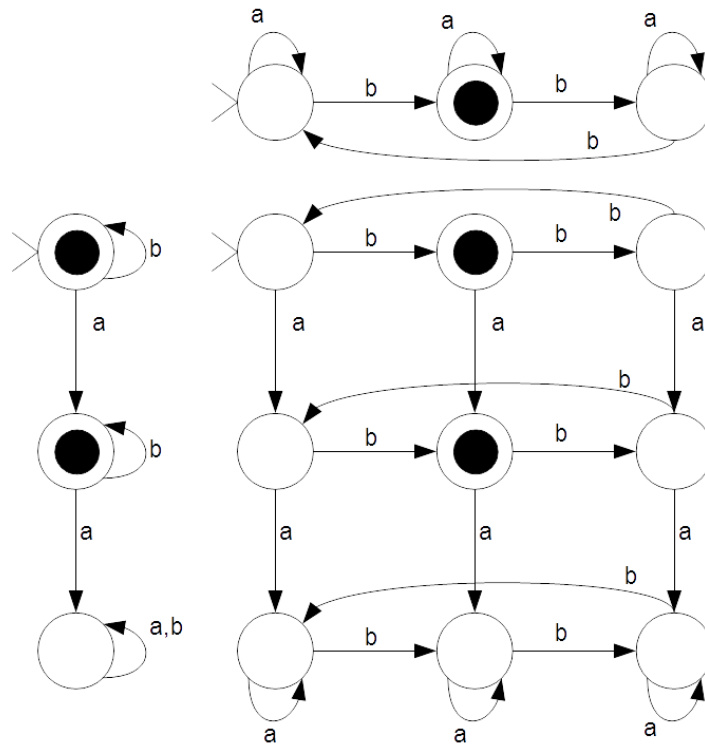


The theory of computation

1. Give DFA M with $L(M) = \{w \in \{a, b\}^* \mid \#a < 2 \text{ and } \#b \bmod 3 = 1\}$!

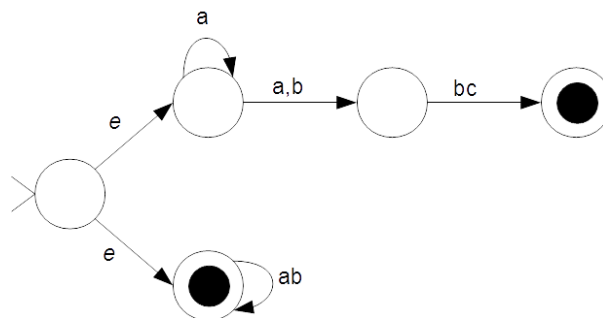
(4p)



2. Give NFA M with equivalent with the following RE:

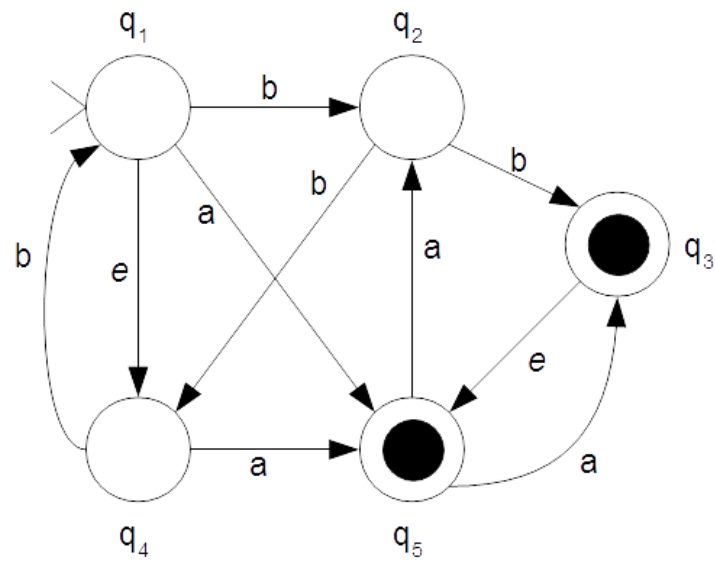
(3p)

$a^*(a \cup b)bc \cup (ab)^*$



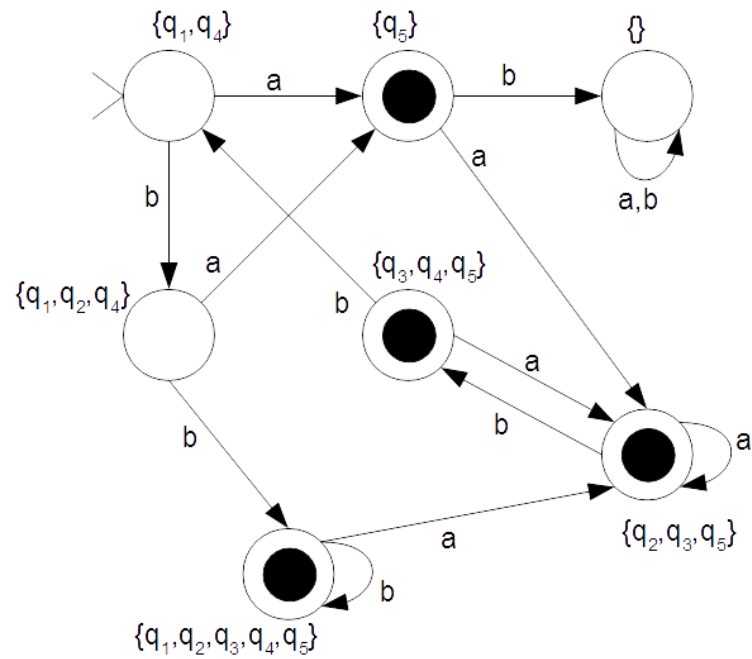
3. Give DFA M' such that $L(M') = L(M)$!

(6p)



$E(q_1) = \{q_1, q_4\}$

$E(q_3) = \{q_3, q_5\}$



4. Give CFG G such that $L(G) = \{a(bc)^{n+1}adb^mc^p cd^{2m}a^nd \mid m, n, p \geq 0\}$? (3p)

$V = \{a, b, c, d, S, N, M, P\}$

$\Sigma = \{a, b, c, d\}$

$R = \{S \rightarrow aNd, N \rightarrow bcNa \mid bcadM, M \rightarrow bMdd \mid Pc, P \rightarrow cP \mid e\}$

$S = S$

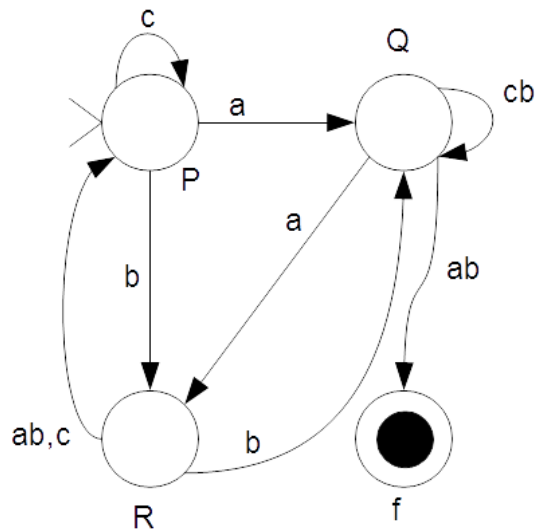
5. Construct such NFA M which is equivalent with the given RG! (3p)

$V = \{a, b, c, P, Q, R\}$

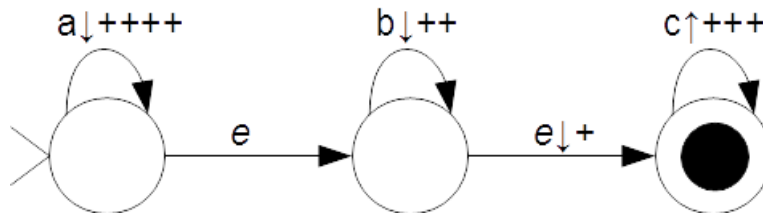
$\Sigma = \{a, b, c\}$

$R = \{P \rightarrow aQ \mid cP \mid bR, Q \rightarrow ab \mid cbQ \mid aR, R \rightarrow abP \mid cP \mid bQ\}$

$S = P$



6. Give the state diagram of PDA M for which $L(M) = \{w \in \{a, b, c\}^* \mid w = a^n b^m c^p, 4n+2m+1=3p\}$! (4p)



7. Give the definition of NFA! (3p)

NFA M is an ordered five-tuple $(K, \Sigma, \Delta, s, F)$, where:

K is the set of states

Σ is the alphabet

$\Delta \subseteq K \times \Sigma \times K$ is the state transition relation

$s \in K$ is the starting state

$F \subset K$ is the set of final states

8. Prove that the set of languages accepted by finite automata are closed under intersection! (4p)

We already know that languages accepted by finite automata are closed under union and complementation.

Perform:

- NFA \rightarrow DFA twice
- complementation theorem twice
- union once
- NFA \rightarrow DFA
- complementation theorem once again

De'Morgan identity: $L(M) = L(M_1) \cap L(M_2) = (L(M_1)^c \cup L(M_2)^c)^c$