ident, $x, y, y_p, y_f, -$, abbrev, r, α subscripts: p for pointers, f for functions

n, i, j index variables

 $impl_const$ implementation-defined constant member C struct/union member name

Ott-hack, ignore (annotations)

nat OCaml arbitrary-width natural number

mem_ptr abstract pointer value
mem_val abstract memory value

Ott-hack, ignore (locations)

mem_iv_c OCaml type for memory constraints on integer values

 UB_name undefined behaviour

string OCaml string

Ott-hack, ignore (OCaml type variable TY)
Ott-hack, ignore (OCaml Symbol.prefix)

mem_order, _ OCaml type for memory order

linux_mem_order OCaml type for Linux memory order

Ott-hack, ignore (OCaml type variable bt)

```
Sctypes_{-}t, \tau
                                               C type
                                                  pointer to type \tau
                                               OCaml type for struct/union tag
tag
                    ::=
                          ident
β, _
                                               base types
                    ::=
                                                  unit
                          unit
                          bool
                                                  boolean
                                                  integer
                          integer
                                                  rational numbers?
                          real
                                                  location
                          loc
                          \operatorname{array} \beta
                                                  array
                          \mathtt{list}\, eta
                                                  list
                                                  tuple
                          \mathtt{struct}\,tag
                                                  struct
                          \operatorname{\mathfrak{set}} \beta
                                                  \operatorname{set}
                          opt(\beta)
                                                  option
                          \beta \to \beta'
                                                  parameter types
                                          Μ
                                                  of a C type
binop
                                               binary operators
                                                  addition
                                                  subtraction
                                                  multiplication
                                                  division
                                                  modulus
                          rem_t
                                                  remainder
                          rem_f
                                                  exponentiation
                                                  equality, defined both for integer and C types
                                                  inequality, similarly defined
                           !=
```

```
greater than, similarly defined
                                   less than, similarly defined
                                   greater than or equal to, similarly defined
                                   less than or equal to, similarly defined
                                   conjucttion
                                   disjunction
binop_{arith}
                                 arithmentic binary operators
                    rem_t
                    rem_f
binop_{rel}
                                relational binary operators
binop_{bool}
                                boolean binary operators
mem\_int
                                memory integer value
                            Μ
                            М
```

$object_value$::= 	$\begin{split} & mem_int \\ & mem_ptr \\ & \texttt{array} \left(\overline{loaded_value_i}^i \right) \\ & (\texttt{struct} ident) \{ \overline{.member_i : \tau_i = mem_val_i}^i \} \\ & (\texttt{union} ident) \{ .member = mem_val \} \end{split}$	C object values (inhabitants of object types), which can be read/stored integer value pointer value C array value C struct value C union value
$loaded_value$::=		potentially unspecified C object values
		$\verb specified object_value $	specified loaded value
value	::=		Core values
		$object_value$	C object value
	ĺ	$loaded_value$	loaded C object value
	ĺ	Unit	unit
		True	boolean true
		False	boolean false
		$eta[\overline{value_i}^i]$	list
		$(\overline{value_i}^i)$	tuple
$bool_value$::=		Core booleans
		True	boolean true
		False	boolean false
$ctor_val$::=		data constructors
		$\mathtt{Nil}\beta$	empty list
		Cons	list cons
		Tuple	tuple
		Array	C array
		Specified	non-unspecified loaded value
$ctor_expr$::=		data constructors

		Ivmax Ivmin Ivsizeof Ivalignof IvCOMPL IvAND IvOR IvXOR Fvfromint		max integer value min integer value sizeof value alignof value bitwise complement bitwise AND bitwise OR bitwise XOR cast integer to floating value
		Ivfromfloat		cast floating to integer value
name	::= 	$ident \\ impl_const$		Core identifier implementation-defined constant
pval	::= 	$ident \\ impl_const \\ value \\ \texttt{constrained}\left(\overline{mem_iv_c_i, pval_i}^i\right) \\ \texttt{error}\left(string, pval\right) \\ ctor_val\left(\overline{pval_i}^i\right) \\ (\texttt{struct}ident)\{\overline{.member_i = pval_i}^i\} \\ (\texttt{union}ident)\{.member = pval\}$		pure values Core identifier implementation-defined constant Core values constrained value impl-defined static error data constructor application C struct expression C union expression
tpval	::=	$\begin{array}{l} \text{undef} \ \ UB_name \\ \text{done} \ pval \end{array}$		top-level pure values undefined behaviour pure done
$ident_opt_\beta$::=	<i>∴</i> ;β	$binders = \{\}$	type annotated optional identifier

```
ident:\beta
                                                          binders = ident
pattern
                                ident\_opt\_\beta
                                                          binders = binders(ident\_opt\_\beta)
                               ctor\_val(\overline{pattern_i}^i)
                                                          binders = binders(\overline{pattern_i}^i)
                                                                                                  OCaml arbitrary-width integer
z
                         ::=
                                                           Μ
                                                                                                     literal integer
                                mem\_int
                                                           Μ
                               size\_of(\tau)
                                                           Μ
                                                                                                     size of a C type
                                offset_of_{tag}(member)
                                                          Μ
                                                                                                     offset of a struct member
                               ptr_size
                                                           Μ
                                                                                                     size of a pointer
                               \max_{-int_{\tau}}
                                                           Μ
                                                                                                     maximum value of int of type \tau
                                                          Μ
                                                                                                     minimum value of int of type \tau
                                \min_{-int_{\tau}}
\mathbb{Q},\ q,\ _{-}
                                                                                                  OCaml type for rational numbers
                                \frac{int_1}{int_2}
lit
                         ::=
                                ident
                                unit
                                bool
                                z
                                \mathbb{Q}
ident\_or\_pattern
                                ident
                                                           binders = ident
                                                           binders = binders(pattern)
                                pattern
bool\_op
                                \neg term
```

```
term_1 = term_2
                       term_1 \rightarrow term_2
                       \bigwedge(\overline{term_i}^i)
                       \bigvee (\overline{term_i}^i)
                       term_1 \ binop_{bool} \ term_2
                                                                  M
                       if term_1 then term_2 else term_3
arith\_op
                       term_1 + term_2
                       term_1 - term_2
                       term_1 \times term_2
                       term_1/term_2
                       term_1 \, {\tt rem\_t} \, term_2
                       term_1 \, {\tt rem\_f} \, term_2
                       term_1 \hat{} term_2
                                                                   Μ
                       term_1 \ binop_{arith} \ term_2
cmp\_op
                       term_1 < term_2
                                                                           less than
                       term_1 \le term_2
                                                                           less than or equal
                       term_1 \ binop_{rel} \ term_2
                                                                  Μ
list\_op
                       nil
                       term_1 :: term_2
                       {\tt tl}\, term
                       term^{(int)}
tuple\_op
```

```
pointer\_op
                        mem\_ptr
                        term_1 +_{ptr} term_2
                        {\tt cast\_int\_to\_ptr}\, term
                        {\tt cast\_ptr\_to\_int}\, term
array\_op
                  ::=
                        [\mid \overline{term_i}^i \mid]
                        term_1[term_2]
param\_op
                        ident:\beta.\ term
                        term(term_1, ..., term_n)
struct\_op
                  ::=
                        term.member
ct\_pred
                  ::=
                        \texttt{representable}\left(\tau, term\right)
                        aligned(\tau, term)
                        alignedI(term_1, term_2)
term, _{-}
                  ::=
                        lit
                         arith\_op
                        bool\_op
                        cmp\_op
                        tuple\_op
                        struct\_op
                        pointer\_op
                        list\_op
```

	$ array_op \ ct_pred$		
	param_op		
	(term)	S	parentheses
	$\sigma(term)$	M	simul-sub σ in $term$
	$pval$	M	
pexpr	::=		pure expressions
	$\mid pval$		pure values
	$ ctor_expr(\overline{pval_i}^i)$		data constructor application
	$ \texttt{array_shift}\left(pval_1, \tau, pval_2\right)$		pointer array shift
	$ \verb member_shift (pval, ident, member)$		pointer struct/union memb
	$ \mathtt{not} (pval)$		boolean not
	$ pval_1 \ binop \ pval_2$		binary operations
	$ \mathtt{memberof} \ (ident, member, pval)$		C struct/union member acc
	$ name(\overline{pval_i}^i) $		pure function call
	$ \texttt{assert_undef} \ (pval, \ UB_name)$		
	$ \verb bool_to_integer (pval)$		
	$ \mathtt{conv_int} \ (\tau, pval)$		
	$ \mathtt{wrapI} \ (\tau, pval)$		
tpexpr	::=		top-level pure expressions
	tpval		top-level pure values
	\mid case $pval$ of $\overline{\mid tpexpr_case_branch_i}^i$ end		pattern matching
	$ \hspace{.1cm} \texttt{let} \hspace{.04cm} ident_or_pattern = pexpr \hspace{.04cm} \texttt{in} \hspace{.04cm} tpexpr$	bind binders(ident_or_patte	•
	$ \text{let } ident_or_pattern:(y_1:\beta_1.\ term_1) = tperconstant term_1 = tperconstant t$	$expr_1$ in $tpexpr_2$ bind binders $(ident_or_patt)$ bind y_1 in $term_1$	$ern)$ in $tpexpr_2$ annoted pure let
	\mid if $pval$ then $tpexpr_1$ else $tpexpr_2$, and the second	pure if
	$\sigma(tpexpr)$	M	simul-sub σ in $tpexpr$

pure top-level case expression

 $tpexpr_case_branch$

```
pattern \Rightarrow tpexpr
                                                                                    bind binders(pattern) in tpexpr
                                                                                                                           top-level case expression branch
m_kill_kind
                        dynamic
                         \mathtt{static}\,	au
                                                                                                                         OCaml booleans
bool, _
                         true
                         false
int, \, \, \_
                                                                                                                         OCaml fixed-width integer
                                                                                                                            literal integer
res\_term
                                                                                                                         resource terms
                                                                                                                            empty heap
                         emp
                                                                                                                           single-cell heap
                        points\_to
                        ident
                                                                                                                            variable
                         \langle res\_term_1, res\_term_2 \rangle
                                                                                                                            seperating-conjunction pair
                        pack(pval, res\_term)
                                                                                                                            packing for existentials
                        fold(res_term)
                                                                                                                           fold into recursive res. pred.
                        \sigma(res\_term)
                                                                                     Μ
                                                                                                                            substitution for resource terms
mem\_action
                                                                                                                         memory actions
                        create(pval, \tau)
                        create\_readonly(pval_1, \tau, pval_2)
                        alloc(pval_1, pval_2)
                        kill(m_kill_kind, pval, pt)
                        store(bool, \tau, pval_1, pval_2, mem\_order, pt)
                                                                                                                            true means store is locking
                        load(\tau, pval, mem\_order, pt)
                        rmw(\tau, pval_1, pval_2, pval_3, mem\_order_1, mem\_order_2)
                        fence (mem\_order)
```

```
cmp\_exch\_strong(\tau, pval_1, pval_2, pval_3, mem\_order_1, mem\_order_2)
                            cmp\_exch\_weak(\tau, pval_1, pval_2, pval_3, mem\_order_1, mem\_order_2)
                            linux_fence(linux_mem_order)
                            linux\_load(\tau, pval, linux\_mem\_order)
                            linux\_store(\tau, pval_1, pval_2, linux\_mem\_order)
                            linux_rmw(\tau, pval_1, pval_2, linux_mem_order)
polarity
                                                                                                         polarities for memory actions
                                                                                                           (pos) sequenced by let weak and let strong
                                                                                                           only sequenced by let strong
                            neg
pol\_mem\_action
                                                                                                        memory actions with polarity
                            polarity\ mem\_action
                                                                                                        operations involving the memory state
mem\_op
                            pval_1 \ binop_{rel} \ pval_2
                                                                                                           pointer relational binary operations
                            pval_1 -_{\tau} pval_2
                                                                                                           pointer subtraction
                                                                                                           cast of pointer value to integer value
                            intFromPtr(	au_1, 	au_2, pval)
                            ptrFromInt (\tau_1, \tau_2, pval)
                                                                                                           cast of integer value to pointer value
                            ptrValidForDeref(\tau, pval, pt)
                                                                                                           dereferencing validity predicate
                            ptrWellAligned(\tau, pval)
                            ptrArrayShift (pval_1, \tau, pval_2)
                            memcpy (pval_1, pval_2, pval_3)
                            memcmp(pval_1, pval_2, pval_3)
                            realloc(pval_1, pval_2, pval_3)
                            va\_start(pval_1, pval_2)
                            va\_copy(pval)
                            va\_arg(pval, \tau)
                            va_{-}end(pval)
spine\_elem
                                                                                                        spine element
                      ::=
```

	 	$egin{aligned} pval \ res_term \ \sigma(spine_elem) \end{aligned}$	M	pure or logical value resource value substitution for spine elements / return values
spine	::= 	$\overline{spine_elem_i}^{\ i}$		spine
tval	::= 	$\begin{array}{c} \texttt{done} \ spine \\ \texttt{undef} \ \ UB_name \end{array}$		(effectful) top-level values end of top-level expression undefined behaviour
$res_pattern$::=	emp $ident$ fold $(res_pattern)$ $\langle res_pattern_1, res_pattern_2 \rangle$ pack $(ident, res_pattern)$	$\begin{aligned} & \text{binders} = \{\} \\ & \text{binders} = ident \\ & \text{binders} = \{\} \\ & \text{binders} = & \text{binders}(res_pattern_1) \cup & \text{binders}(res_pattern_2) \\ & \text{binders} = & ident \cup & \text{binders}(res_pattern) \end{aligned}$	resource terms empty heap variable unfold (recursive) predicate seperating-conjunction pair packing for existentials
$ret_pattern$::= 	$ ext{comp} ident_or_pattern \ ext{log} ident \ ext{res} res_pattern$	$\begin{aligned} & \text{binders} = \text{binders}(ident_or_pattern) \\ & \text{binders} = ident \\ & \text{binders} = \text{binders}(res_pattern) \end{aligned}$	return pattern computational variable logical variable resource variable
init,	::= 	✓ ×		initialisation status initialised uninitalised
$points_to, pt$::=	$term_1 \stackrel{init}{\mapsto}_{\tau} term_2$		points-to separation logic predicate
res	::=			resources

		emp $points_to$ $res_1 * res_2$ $\exists ident: \beta. res$ $term \land res$ if $term$ then res_1 else res_2 $\alpha(\overrightarrow{pval_i}^i)$ $\sigma(res)$	M	empty heap points-top heap pred. seperating conjunction existential logical conjuction ordered disjuction predicate simul-sub σ in res
$ret, _$::=	$\Sigma ident: \beta. \ ret$ $\exists ident: \beta. \ ret$ $res \otimes ret$ $term \wedge ret$ I $\sigma(ret)$	M	return types return a computational value return a logical value return a resource value return a predicate (post-condition) end return list simul-sub σ in ret
seq_expr	::=	$\begin{aligned} & \texttt{ccall}\left(\tau, ident, spine\right) \\ & \texttt{pcall}\left(name, spine\right) \end{aligned}$		sequential (effectful) expressions C function call procedure call
seq_texpr	::= 	$tval$ $run ident \overline{pval_i}^i$ $let ident_or_pattern = pexpr in texpr$ $let ident_or_pattern:(y_1:eta_1. term_1) = tpexpr in texpr$	bind binders($ident_or_pattern$) in $texpr$ bind binders($ident_or_pattern$) in $texpr$ bind y_1 in $term_1$	sequential top-level (effectful) expressions (effectful) top-level values run from label pure let annotated pure let
		$\begin{array}{l} \operatorname{let} \overline{\mathit{ret_pattern}_i}^i = \mathit{seq_expr} \operatorname{in} \mathit{texpr} \\ \operatorname{let} \overline{\mathit{ret_pattern}_i}^i : \mathit{ret} = \mathit{texpr}_1 \operatorname{in} \mathit{texpr}_2 \\ \operatorname{case} \mathit{pval} \operatorname{of} \overline{\mid \mathit{texpr_case_branch}_i}^i \operatorname{end} \\ \operatorname{if} \mathit{pval} \operatorname{then} \mathit{texpr}_1 \operatorname{else} \mathit{texpr}_2 \end{array}$	bind binders $(\overline{ret_pattern_i}^i)$ in $texpr$ bind binders $(\overline{ret_pattern_i}^i)$ in $texpr_2$	bind return patterns annotated bind return patterns pattern matching conditional

		$\verb bound [int](is_texpr) $		limit scope of indet seq behaviour, absent at ru
$texpr_case_branch$::=	$pattern \Rightarrow texpr$	bind $binders(pattern)$ in $texpr$	top-level case expression branch top-level case expression branch
is_expr	::= 	$tval$ $memop(mem_op)$ pol_mem_action		indet seq (effectful) expressions (effectful) top-level values pointer op involving memory memory action
is_texpr	::= 	$\begin{array}{l} {\tt letweak}\overline{ret_pattern_i}^{i} = is_expr{\tt in}texpr\\ {\tt letstrong}\overline{ret_pattern_i}^{i} = is_expr{\tt in}texpr \end{array}$	bind binders $(\overline{ret_pattern_i}^i)$ in $texpr$ bind binders $(\overline{ret_pattern_i}^i)$ in $texpr$	indet seq top-level (effectful) expressions weak sequencing strong sequencing
texpr	::= 	seq_texpr is_texpr $\sigma(texpr)$	M	top-level (effectful) expressions sequential (effectful) expressions indet seq (effectful) expressions simul-sub σ in $texpr$
arg	::=	$\Pi ident: \beta. \ arg$ $\forall ident: \beta. \ arg$ $res \multimap arg$ $term \supset arg$ ret		argument/function types
		$\sigma(arg)$	М	simul-sub σ in arg
$pure_arg$::= 	$\Pi ident:\beta. \ pure_arg$ $term \supset pure_arg$ $pure_ret$		pure argument/function types

```
pure\_ret
                                                                                  pure return types
                                 \Sigma ident:\beta. pure\_ret
                                 term \land pure\_ret
\mathcal{C}
                                                                                 computational var env
                                 \mathcal{C}, ident: \beta
\mathcal{L}
                                                                                  logical var env
                                egin{aligned} & \cdot & \ \overline{\mathcal{L}_i}^i & \ \mathcal{L}, ident: eta \end{aligned}
Φ
                                                                                  constraints env
                                 \frac{\Phi, term}{\Phi_i}{}^i
\mathcal{R}
                                                                                  resources env
                                 \frac{\mathcal{R}, ident:res}{\mathcal{R}_i}^i
\sigma, \psi
                                                                                 substitutions
                         |spine\_elem/ident, \sigma
                                term/ident, \sigma
\overline{\sigma_i}^i
                                 \sigma(\psi)
                                                                                     apply \sigma to all elements in \psi
```

```
typing
                                                \mathtt{smt}\left(\Phi\Rightarrow term\right)
                                      |\begin{array}{c} ident:\beta\in\mathcal{C}\\ |\begin{array}{c} ident:\beta\in\mathcal{C}\\ |\end{array}\\ |\begin{array}{c} ident:\beta\in\mathcal{L}\\ |\end{array}\\ |\begin{array}{c} struct\ tag\ \&\ \overline{member_i:\tau_i}^i\in\texttt{Globals}\\ |\begin{array}{c} \alpha\equiv\overline{x_i:\beta_i}^i\mapsto res\in\texttt{Globals}\\ |\overline{\mathcal{C}_i;\mathcal{L}_i;\Phi_i\vdash mem\_val_i\Rightarrow mem\,\beta_i}^i\\ |\end{array}
                                                                                                                                                                     recursive resource predicate
                                                                                                                                                                     dependent on memory object model
 opsem
                                              \forall i < j. \ \mathsf{not} \ (pattern_i = pval \leadsto \sigma_i)
                                                {	t fresh}(mem\_ptr)
                                                term
                                                pval:\beta
formula
                                                judgement
                                                typing
                                       opsem
                                        term \equiv term'
                                              name:pure\_arg \equiv \overline{x_i}^i \mapsto tpexpr \in 	exttt{Globals}
                                              name:arg \equiv \overline{x_i}^i \mapsto texpr \in Globals
heap, h, f
                                                                                                                                                          heaps
                                                                                                                                                          [O] convenient for the soundness proof
lemma\_jtype
```

```
res\_jtype
                                                        \Phi \vdash res \equiv res'
                                                        C; \mathcal{L}; \Phi; \mathcal{R} \vdash res\_term \Leftarrow res
object\_value\_jtype
                                                       \mathcal{C}; \mathcal{L}; \Phi \vdash object\_value \Rightarrow \ \mathtt{obj} \ \beta
pval\_jtype
                                                        C; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta
spine\_jtype
                                              ::=
                                                       C; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{x_i = spine\_elem_i}^i :: arg \gg \sigma; ret
pexpr\_jtype
                                              ::=
                                                        C; \mathcal{L}; \Phi \vdash pexpr \Rightarrow ident: \beta. term
comp\_pattern\_jtype
                                              ::=
                                                        pattern: \beta \leadsto \mathcal{C} \text{ with } term
                                                        ident\_or\_pattern: \beta \leadsto \mathcal{C} \ \text{with} \ term
res\_pattern\_jtype
                                                        \Phi \vdash res' = \mathtt{strip\_ifs}(res)
                                                        \Phi \vdash res \text{ as } res\_pattern \leadsto \mathcal{L}'; \Phi'; \mathcal{R}'
                                                        \Phi \vdash res\_pattern:res \leadsto \mathcal{L}'; \Phi'; \mathcal{R}'
ret\_pattern\_jtype
                                              ::=
                                                        \Phi \vdash \overline{ret\_pattern_i}^i : ret \leadsto \mathcal{C}'; \mathcal{L}'; \Phi'; \mathcal{R}'
tpval\_jtype
                                              ::=
                                                        C; \mathcal{L}; \Phi \vdash tpval \Leftarrow ident: \beta. term
```

$$| \quad \mathcal{C}; \mathcal{L}; \Phi \vdash tpexpr \Leftarrow ident: \beta. term \\ | \quad \mathcal{C}; \mathcal{L}; \Phi \vdash tpexpr \Leftarrow ident: \beta. term \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem_action \Rightarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem_op \Rightarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem_op \Rightarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash tval \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash tval \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash seq_expr \Rightarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_expr \Rightarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_expr \Rightarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_expr \Leftrightarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftrightarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftrightarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftrightarrow ret \\ | \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{L}; \Phi$$

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 $pure_opsem_jtype$

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 \begin{array}{c|c} & \langle pexpr \rangle \longrightarrow \langle pexpr' \rangle \\ & \langle pexpr \rangle \longrightarrow \langle tpexpr: (y:\beta.\ term) \rangle \\ & \langle tpexpr \rangle \longrightarrow \langle tpexpr' \rangle \\ \\ & opsem\_jtype \end{array} \\ ::= \\ & \begin{vmatrix} \langle h; seq\_expr \rangle \longrightarrow \langle h'; texpr: ret \rangle \\ & \langle h; seq\_texpr \rangle \longrightarrow \langle h'; texpr \rangle \\ & | \langle h; mem\_op \rangle \longrightarrow \langle h'; tval \rangle \\ & | \langle h; mem\_action \rangle \longrightarrow \langle h'; tval \rangle \\ & | \langle h; is\_expr \rangle \longrightarrow \langle h'; is\_expr' \rangle \\ & | \langle h; is\_texpr \rangle \longrightarrow \langle h'; texpr \rangle \\ & | \langle h; texpr \rangle \longrightarrow \langle h'; texpr' \rangle \\ \end{array}
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 $\overline{x_i}^i :: arg \leadsto \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \mid ret$

$$\frac{}{::ret \leadsto :; :; : | ret} \quad Arg_Env_Ret$$

$$\frac{\overline{x_i}^i :: arg \leadsto \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \mid ret}{x, \overline{x_i}^i :: \Pi \, x: \beta. \, arg \leadsto \mathcal{C}, x: \beta; \mathcal{L}; \Phi; \mathcal{R} \mid ret} \quad \text{Arg_Env_Comp}$$

$$\frac{\overline{x_i}^i :: arg \leadsto \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \mid ret}{x, \overline{x_i}^i :: \forall x : \beta. arg \leadsto \mathcal{C}; \mathcal{L}, x : \beta; \Phi; \mathcal{R} \mid ret} \quad \text{Arg_Env_Log}$$

$$\frac{\overline{x_i}^{\;i}\,:: arg \leadsto \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \mid ret}{\overline{x_i}^{\;i}\,:: term \supset arg \leadsto \mathcal{C}; \mathcal{L}; \Phi, term; \mathcal{R} \mid ret} \quad \text{Arg_Env_Phi}$$

$$\frac{\overline{x_i}^i :: arg \leadsto \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \mid ret}{x, \overline{x_i}^i :: res \multimap arg \leadsto \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}, x: res \mid ret} \quad \text{Arg_Env_Res}$$

 $\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \sqsubseteq \mathcal{C}'; \mathcal{L}'; \Phi'; \mathcal{R}'$

$$\frac{}{\cdot;\cdot;\cdot;\cdot\sqsubseteq\cdot;\cdot;\cdot;}\quad \text{Weak_Empty}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \sqsubseteq \mathcal{C}'; \mathcal{L}'; \Phi'; \mathcal{R}'}{\mathcal{C}, x : \beta; \mathcal{L}; \Phi; \mathcal{R} \sqsubseteq \mathcal{C}', x : \beta; \mathcal{L}'; \Phi'; \mathcal{R}'} \quad \text{Weak_Cons_Comp}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \sqsubseteq \mathcal{C}'; \mathcal{L}'; \Phi'; \mathcal{R}'}{\mathcal{C}; \mathcal{L}, x:\beta; \Phi; \mathcal{R} \sqsubseteq \mathcal{C}'; \mathcal{L}', x:\beta; \Phi'; \mathcal{R}'} \quad \text{Weak_Cons_Log}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \sqsubseteq \mathcal{C}'; \mathcal{L}'; \Phi'; \mathcal{R}'}{\mathcal{C}; \mathcal{L}; \Phi, term; \mathcal{R} \sqsubseteq \mathcal{C}'; \mathcal{L}'; \Phi', term; \mathcal{R}'} \quad \text{Weak_Cons_Phi}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \sqsubseteq \mathcal{C}'; \mathcal{L}'; \Phi'; \mathcal{R}'}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}, x : res \sqsubseteq \mathcal{C}'; \mathcal{L}'; \Phi'; \mathcal{R}', x : res} \quad \text{Weak_Cons_Res}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \sqsubseteq \mathcal{C}'; \mathcal{L}'; \Phi'; \mathcal{R}'}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \sqsubseteq \mathcal{C}', x:\beta; \mathcal{L}'; \Phi'; \mathcal{R}'} \quad \text{Weak_Skip_Comp}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \sqsubseteq \mathcal{C}'; \mathcal{L}'; \Phi'; \mathcal{R}'}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \sqsubseteq \mathcal{C}'; \mathcal{L}', x : \beta; \Phi'; \mathcal{R}'} \quad \text{Weak_Skip_Log}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \sqsubseteq \mathcal{C}'; \mathcal{L}'; \Phi'; \mathcal{R}'}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \sqsubseteq \mathcal{C}'; \mathcal{L}'; \Phi', term; \mathcal{R}'} \quad \text{Weak_Skip_Phi}$$

$$C; \mathcal{L}; \Phi; \mathcal{R} \vdash (\sigma): (C'; \mathcal{L}'; \Phi'; \mathcal{R}')$$

$$\overline{\mathcal{C};\mathcal{L};\Phi;\cdot\vdash(\cdot):(\cdot;\cdot;\cdot;\cdot)} \quad \text{Ty_Subs_Empty}$$

$$\begin{array}{ll} \mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash(\sigma):(\mathcal{C}';\mathcal{L}';\Phi';\mathcal{R}') \\ \hline \mathcal{C};\mathcal{L};\Phi\vdash pval\Rightarrow\beta \\ \hline \mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash (pval/x,\sigma):(\mathcal{C}',x:\beta;\mathcal{L}';\Phi';\mathcal{R}') \end{array} & \text{Ty_Subs_Cons_Comp} \\ \hline \\ \mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash (\sigma):(\mathcal{C}';\mathcal{L}';\Phi';\mathcal{R}') \\ \hline \\ \mathcal{C};\mathcal{L};\Phi\vdash pval\Rightarrow\beta \\ \hline \mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash (pval/x,\sigma):(\mathcal{C}';\mathcal{L}',x:\beta;\Phi';\mathcal{R}') \end{array} & \text{Ty_Subs_Cons_Log} \\ \hline \\ \mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash (\sigma):(\mathcal{C}';\mathcal{L}';\Phi';\mathcal{R}') \\ \hline \\ \frac{smt}{\mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash (\sigma):(\mathcal{C}';\mathcal{L}';\Phi';\mathcal{R}')} \\ \hline \\ \mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash (\sigma):(\mathcal{C}';\mathcal{L}';\Phi';\mathcal{R}') \end{array} & \text{Ty_Subs_Cons_Phi} \\ \hline \\ \mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash (\sigma):(\mathcal{C}';\mathcal{L}';\Phi';\mathcal{R}') \\ \hline \\ \mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash (\sigma):(\mathcal{C}';\mathcal{L}';\Phi';\mathcal{R}') \\ \hline \\ \mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash (\sigma):(\mathcal{C}';\mathcal{L}';\Phi';\mathcal{R}') \end{array} & \text{Ty_Subs_Cons_Res} \\ \hline \\ \mathcal{C};\mathcal{L};\Phi;\mathcal{R},\mathcal{R}\vdash (\sigma):(\mathcal{C}';\mathcal{L}';\Phi';\mathcal{R}') \\ \hline \\ \mathcal{C};\mathcal{L};\Phi;\mathcal{R},\mathcal{R}\vdash (\sigma):(\mathcal{C}';\mathcal{L}';\Phi';\mathcal{R}') \\ \hline \\ \mathcal{C};\mathcal{L};\Phi;\mathcal{R},\mathcal{R}\vdash (res_term/x,\sigma):(\mathcal{C}';\mathcal{L}';\Phi';\mathcal{R}',x:res) \end{array} & \text{Ty_Subs_Cons_Res} \\ \hline \end{array}$$

 $\Phi \vdash res \equiv res'$

$$\overline{\Phi \vdash \mathtt{emp} \ \equiv \ \mathtt{emp}} \quad \mathrm{TY_RES_EQ_EMP}$$

$$\frac{\operatorname{smt}\left(\Phi\Rightarrow\left(term_{1}=term_{1}'\right)\wedge\left(term_{2}=term_{2}'\right)\right)}{\Phi\vdash term_{1}\overset{init}{\mapsto}_{\tau}term_{2}\equiv term_{1}'\overset{init}{\mapsto}_{\tau}term_{2}'}$$
 TY_RES_EQ_POINTSTO

$$\begin{array}{ccc} \Phi \vdash res_1 \equiv res_1' \\ \Phi \vdash res_2 \equiv res_2' \\ \hline \Phi \vdash res_1 * res_2 \equiv res_1' * res_2' \end{array} \quad \text{TY_RES_EQ_SEPCONJ}$$

$$\frac{\Phi \vdash res \equiv res'}{\Phi \vdash \exists ident: \beta. \ res \equiv \exists ident: \beta. \ res'} \quad \text{TY_RES_EQ_EXISTS}$$

$$\frac{\operatorname{smt}\left(\Phi\Rightarrow\left(\operatorname{term}\rightarrow\operatorname{term}'\right)\wedge\left(\operatorname{term}'\rightarrow\operatorname{term}\right)\right)}{\Phi\vdash\operatorname{ters}\equiv\operatorname{res}'}$$

$$\Phi\vdash\operatorname{term}\wedge\operatorname{res}\equiv\operatorname{term}'\wedge\operatorname{res}'$$

$$\operatorname{Ty.Res.Eq.Term}$$

$$\frac{\operatorname{smt}\left(\Phi\Rightarrow\left(\operatorname{term}_{1}\rightarrow\operatorname{term}_{2}\right)\wedge\left(\operatorname{term}_{2}\rightarrow\operatorname{term}_{1}\right)\right)}{\Phi\vdash\operatorname{res}_{11}\equiv\operatorname{res}_{21}}$$

$$\Phi\vdash\operatorname{res}_{21}\equiv\operatorname{res}_{22}$$

$$\overline{\Phi\vdash\operatorname{if}\operatorname{term}_{1}\operatorname{then}\operatorname{res}_{11}\operatorname{else}\operatorname{res}_{12}}\equiv\operatorname{if}\operatorname{term}_{2}\operatorname{then}\operatorname{res}_{21}\operatorname{else}\operatorname{res}_{22}$$

$$\overline{\Phi\vdash\operatorname{if}\operatorname{term}_{1}\operatorname{then}\operatorname{res}_{11}\operatorname{else}\operatorname{res}_{12}}\equiv\operatorname{if}\operatorname{term}_{2}\operatorname{then}\operatorname{res}_{21}\operatorname{else}\operatorname{res}_{22}$$

$$\overline{\Phi\vdash\operatorname{if}\operatorname{term}_{1}\operatorname{then}\operatorname{res}_{11}\operatorname{else}\operatorname{res}_{12}}\equiv\operatorname{if}\operatorname{term}_{2}\operatorname{then}\operatorname{res}_{21}\operatorname{else}\operatorname{res}_{22}$$

$$\overline{\Phi\vdash\operatorname{if}\operatorname{term}_{1}\operatorname{then}\operatorname{res}_{11}}=\operatorname{if}\operatorname{term}_{2}\operatorname{then}\operatorname{res}_{21}\operatorname{else}\operatorname{res}_{22}$$

$$\overline{\Phi\vdash\operatorname{if}\operatorname{term}_{2}\operatorname{then}\operatorname{res}_{21}}$$

$$\overline{\Phi\vdash\operatorname{if}\operatorname{term}_{2}\operatorname{then}\operatorname{res}_{21}\operatorname{term}_$$

$$\begin{split} & \text{smt} \; (\Phi \Rightarrow term) \\ & \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash res_term \Leftarrow res \\ & \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash res_term \Leftarrow term \land res \end{split} \quad \text{Ty_Res_Conj}$$

$$\begin{split} & \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta \\ & \frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash res_term \Leftarrow pval/y, \cdot (res)}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \operatorname{pack} (pval, res_term) \Leftarrow \exists \, y : \beta. \, res} \end{split} \quad \text{TY_RES_PACK} \end{split}$$

$$\begin{split} \alpha &\equiv \overline{x_i {:} \beta_i}^i \mapsto res \in \mathtt{Globals} \\ \overline{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_i \Rightarrow \beta_i}^i \\ \Phi \vdash res' &= \mathtt{strip_ifs}\left(\overline{pval_i/x_i, \cdot}^i(res)\right) \\ \overline{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash res_term \Leftarrow res'} \\ \overline{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \mathtt{fold}\left(res_term\right) \Leftarrow \alpha(\overline{pval_i}^i)} \end{split} \quad \mathtt{TY_RES_FOLD} \end{split}$$

 $h:\mathcal{R}$

$$\frac{h:\mathcal{R}}{\vdots:::\mathcal{R}' \vdash pt \Leftarrow pt}$$

$$\frac{h:\mathcal{R}}{h + \{pt\}:\mathcal{R},\mathcal{R}'}$$

$$\text{TY_HEAP_POINTSTO}$$

 $\mathcal{C}; \mathcal{L}; \Phi \vdash object_value \Rightarrow \mathtt{obj}\,\beta$

$$\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash mem_int \Rightarrow \mathtt{objinteger}} \quad \mathrm{TY_PVAL_OBJ_INT}$$

$$\overline{\mathcal{C};\mathcal{L};\Phi \vdash mem_ptr \Rightarrow \mathtt{objloc}} \quad \mathsf{TY_PVAL_OBJ_PTR}$$

$$\frac{\overline{\mathcal{C};\mathcal{L};\Phi \vdash loaded_value_i \Rightarrow \beta}^i}{\mathcal{C};\mathcal{L};\Phi \vdash \mathtt{array}\left(\overline{loaded_value_i}^i\right) \Rightarrow \mathtt{obj}\,\mathtt{array}\,\beta} \quad \mathsf{TY_PVAL_OBJ_ARR}$$

$$\frac{\texttt{struct} \, tag \, \& \, \overline{member_i : \tau_i}^{\, i} \, \in \, \texttt{Globals}}{\overline{\mathcal{C}}; \mathcal{L}; \Phi \vdash mem_val_i \, \Rightarrow \, \texttt{mem} \, \beta_{\tau_i}^{\, i}}}{\mathcal{C}; \mathcal{L}; \Phi \vdash (\, \texttt{struct} \, tag) \{\, \overline{.member_i : \tau_i = mem_val_i}^{\, i} \, \} \, \Rightarrow \, \texttt{obj} \, \texttt{struct} \, tag} \quad \text{Ty_Pval_Obj_Struct}$$

 $C; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta$

$$\frac{x:\beta \in \mathcal{C}}{\mathcal{C}:\mathcal{L};\Phi \vdash x \Rightarrow \beta} \quad \text{Ty_Pval_Var_Comp}$$

$$\frac{x:\beta \in \mathcal{L}}{\mathcal{C}; \mathcal{L}; \Phi \vdash x \Rightarrow \beta} \quad \text{Ty_Pval_Var_Log}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash object_value \Rightarrow \mathsf{obj} \beta}{\mathcal{C}; \mathcal{L}; \Phi \vdash object_value \Rightarrow \beta} \quad \text{Ty_Pval_Obj}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash object_value \Rightarrow \mathtt{obj}\,\beta}{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathtt{specified}\,object_value \Rightarrow \beta} \quad \mathsf{TY_PVAL_LOADED}$$

$$\overline{\mathcal{C};\mathcal{L};\Phi \vdash \mathtt{Unit} \Rightarrow \mathtt{unit}} \quad \mathtt{TY_PVAL_UNIT}$$

$$\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathtt{True} \Rightarrow \mathtt{bool}} \quad \mathtt{TY_PVAL_TRUE}$$

$$\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathtt{False} \Rightarrow \mathtt{bool}} \quad \mathtt{TY_PVAL_FALSE}$$

$$\frac{\overline{C}; \mathcal{L}; \Phi \vdash value_i \Rightarrow \beta^i}{C; \mathcal{L}; \Phi \vdash \beta[value_i^{\ i}] \Rightarrow \mathbf{list} \beta} \quad \text{Ty_PVAL_LIST}$$

$$\frac{\overline{C}; \mathcal{L}; \Phi \vdash value_i \Rightarrow \beta_i^{\ i}}{C; \mathcal{L}; \Phi \vdash (value_i^{\ i}) \Rightarrow \overline{\beta_i}^i} \quad \text{Ty_PVAL_TUPLE}$$

$$\frac{\text{smt} (\Phi \Rightarrow \mathbf{false})}{C; \mathcal{L}; \Phi \vdash \text{error} (string, pval) \Rightarrow \beta} \quad \text{Ty_PVAL_ERROR}$$

$$\overline{C}; \mathcal{L}; \Phi \vdash \text{Nil} \beta() \Rightarrow \mathbf{list} \beta \quad \text{Ty_PVAL_CTOR_NIL}$$

$$\frac{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \beta \quad \text{Ty_PVAL_CTOR_CONS}$$

$$\frac{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \mathbf{list} \beta \quad \text{Ty_PVAL_CTOR_CONS}$$

$$\frac{\overline{C}; \mathcal{L}; \Phi \vdash pval_i \Rightarrow \overline{\beta_i}^i}{C; \mathcal{L}; \Phi \vdash \text{Tuple} (\overline{pval_i}^i) \Rightarrow \overline{\beta_i}^i} \quad \text{Ty_PVAL_CTOR_TUPLE}$$

$$\frac{\overline{C}; \mathcal{L}; \Phi \vdash pval_i \Rightarrow \overline{\beta_i}^i}{C; \mathcal{L}; \Phi \vdash \text{Array} (\overline{pval_i}^i) \Rightarrow \text{array} \beta} \quad \text{Ty_PVAL_CTOR_ARRAY}$$

$$\frac{C; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta}{C; \mathcal{L}; \Phi \vdash \text{pval} \Rightarrow \beta} \quad \text{Ty_PVAL_CTOR_SPECIFIED}$$

$$\text{struct} \ tag \ \& \overline{member_i : \tau_i}^i \in \text{Globals}$$

$$\overline{C}; \mathcal{L}; \Phi \vdash pval_i \Rightarrow \beta_{\tau_i}^i$$

$$\overline{C}; \mathcal{L}; \Phi \vdash \text{pval}_i \Rightarrow \beta_{\tau_i}^i \Rightarrow \text{Struct} \ tag \ \& \overline{member_i : \tau_i}^i \in \text{Globals}$$

$$\overline{C}; \mathcal{L}; \Phi \vdash \text{pval}_i \Rightarrow \beta_{\tau_i}^i \Rightarrow \text{Struct} \ tag \ \& \overline{member_i : \tau_i}^i \in \text{Globals}$$

$$\overline{C}; \mathcal{L}; \Phi \vdash \text{pval}_i \Rightarrow \beta_{\tau_i}^i \Rightarrow \text{Struct} \ tag \ \& \overline{member_i : \tau_i}^i \in \text{Globals}$$

$$\overline{C}; \mathcal{L}; \Phi \vdash \text{pval}_i \Rightarrow \beta_{\tau_i}^i \Rightarrow \text{Struct} \ tag \ \& \overline{member_i : \tau_i}^i \in \text{Globals}$$

$$\overline{C}; \mathcal{L}; \Phi \vdash \text{pval}_i \Rightarrow \beta_{\tau_i}^i \Rightarrow \text{Struct} \ tag \ \& \overline{member_i : \tau_i}^i \in \text{Globals}$$

$$C; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{x_i = spine_elem_i}^i :: arg \gg \sigma; ret$$

$$\overline{\mathcal{C};\mathcal{L};\Phi;\cdot\vdash :: ret \gg \cdot; ret} \quad \text{TY_Spine_Empty}$$

$$\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{x_i = spine_elem_i}^i :: arg \gg \sigma; ret \\ \hline \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash x = pval, \overline{x_i = spine_elem_i}^i :: \Pi x: \beta. arg \gg pval/x, \sigma; ret \end{array} \quad \text{TY_SPINE_COMP}$$

$$\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{x_i = spine_elem_i}^i :: arg \gg \sigma; ret \\ \hline \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash x = pval, \overline{x_i = spine_elem_i}^i :: \forall \, x : \beta. \, arg \gg pval/x, \sigma; ret \end{array} \quad \text{TY_Spine_Log}$$

$$\begin{aligned} & \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_1 \vdash \underbrace{\mathit{res_term} \Leftarrow \mathit{res}}_{i} \\ & \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_2 \vdash \underbrace{\overline{x_i = \mathit{spine_elem}_i}^i :: \mathit{arg} \gg \sigma; \mathit{ret}}_{i} \\ & \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_1, \mathcal{R}_2 \vdash x = \mathit{res_term}, \underbrace{\overline{x_i = \mathit{spine_elem}_i}^i :: \mathit{res} \multimap \mathit{arg} \gg \mathit{res_term}/x, \sigma; \mathit{ret}} \end{aligned}$$
 Ty_Spine_Res

$$\frac{\operatorname{smt}\left(\Phi\Rightarrow term\right)}{\mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash \overline{x_{i}=spine_elem_{i}}^{i}::arg\gg\sigma;ret} \frac{\mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash \overline{x_{i}=spine_elem_{i}}^{i}::arg\gg\sigma;ret}{\mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash \overline{x_{i}=spine_elem_{i}}^{i}::term\supset arg\gg\sigma;ret}$$
 TY_SPINE_PHI

 $C; \mathcal{L}; \Phi \vdash pexpr \Rightarrow ident: \beta. term$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta}{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow y : \beta. \ y = pval} \quad \text{TY_PE_VAL}$$

$$\begin{split} \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{loc} \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \text{integer} \\ \hline \mathcal{C}; \mathcal{L}; \Phi \vdash \text{array_shift} \left(pval_1, \tau, pval_2\right) \Rightarrow y : \text{loc.} \ y = pval_1 +_{\text{ptr}} \left(pval_2 \times \text{size_of}(\tau)\right) \end{split} \quad \text{TY_PE_ARRAY_SHIFT}$$

$$\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \mathtt{loc}$$
 $\mathtt{struct} \ tag \ \& \overline{member_i {:} au_i}^i \in \mathtt{Globals}$

Ty_PE_Member_Shift

 $\overline{\mathcal{C};\mathcal{L};\Phi} \vdash \mathtt{member_shift}(pval,tag,member_i) \Rightarrow y:\mathtt{loc}.\ y = pval +_{\mathtt{ptr}} \mathtt{offset_of}_{tag}(member_i)$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \texttt{bool}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \texttt{not} \, (pval) \Rightarrow y \texttt{:bool}. \, y = \neg \, pval} \quad \texttt{TY_PE_NOT}$$

$$\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \mathtt{integer}$$

$$\mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \mathtt{integer}$$

 $\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \ binop_{arith} \ pval_2} \Rightarrow y : \mathtt{integer}. \ y = (pval_1 \ binop_{arith} \ pval_2)$

TY_PE_ARITH_BINOP

$$\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \mathtt{integer}$$

 $\mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \mathtt{integer}$

TY_PE_REL_BINOP

$$C$$
; \mathcal{L} ; $\Phi \vdash pval_1 \Rightarrow bool$
 C ; \mathcal{L} ; $\Phi \vdash pval_2 \Rightarrow bool$

$$\mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \texttt{bool}$$

 $\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \ binop_{bool} \ pval_2 \Rightarrow y : bool. \ y = (pval_1 \ binop_{bool} \ pval_2)}{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \ binop_{bool} \ pval_2 \Rightarrow y : bool. \ y = (pval_1 \ binop_{bool} \ pval_2)}$

TY_PE_BOOL_BINOP

$$\begin{array}{l} \textit{name:pure_arg} \equiv \overline{x_i}^i \mapsto \textit{tpexpr} \in \texttt{Globals} \\ \underline{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \overline{x_i = pval_i}^i :: pure_arg \gg \sigma; \Sigma \ y : \beta. \ term \land \mathtt{I}} \\ \underline{\mathcal{C}; \mathcal{L}; \Phi \vdash name(\overline{pval_i}^i) \Rightarrow y : \beta. \ \sigma(term)} \end{array} \quad \text{TY_PE_CALL}$$

$$\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \texttt{bool}$$
 smt $(\Phi \Rightarrow pval)$

 $\frac{\texttt{smt} \ (\Psi \Rightarrow pval)}{\mathcal{C}; \mathcal{L}; \Phi \vdash \texttt{assert_undef} \ (pval, \ UB_name) \Rightarrow y \text{:unit.} \ y = \texttt{unit}} \quad \texttt{Ty_PE_Assert_UNDEF}$

$$C; \mathcal{L}; \Phi \vdash pval \Rightarrow bool$$

 $\overline{\mathcal{C};\mathcal{L};\Phi\vdash\mathtt{bool_to_integer}\,(pval)\Rightarrow y\mathtt{:integer}.\,\,y=\mathtt{if}\,pval\,\mathtt{then}\,1\,\mathtt{else}\,0}$

Ty_PE_Bool_To_Integer

$$\begin{split} \mathcal{C}; \mathcal{L}; \Phi \vdash pval &\Rightarrow \mathtt{integer} \\ abbrev_1 &\equiv \mathtt{max_int}_\tau - \mathtt{min_int}_\tau + 1 \\ abbrev_2 &\equiv pval\,\mathtt{rem_f}\,\,abbrev_1 \\ \hline \mathcal{C}; \mathcal{L}; \Phi \vdash \mathtt{wrapI}\,(\tau, pval) \Rightarrow y : \beta.\,\, y = \mathtt{if}\,\,abbrev_2 \leq \mathtt{max_int}_\tau\,\mathtt{then}\,\,abbrev_2\,\mathtt{else}\,\,abbrev_2 - abbrev_1 \end{split}$$

Ty_PE_WrapI

 $pattern:eta\leadsto\mathcal{C}$ with term

$$\underline{\hspace{1cm}}$$
: $\beta:\beta \leadsto \cdot \text{with}$ TY_PAT_COMP_NO_SYM_ANNOT

$$\overline{x{:}\beta{:}\beta \leadsto \cdot, x{:}\beta \, \text{with} \, x} \quad \text{Ty_Pat_Comp_Sym_Annot}$$

$$\frac{1}{\text{Nil }\beta(\cdot): \text{list }\beta \leadsto \cdot \text{with nil}} \quad \text{TY_PAT_COMP_NIL}$$

$$\frac{pattern_1:\beta \leadsto \mathcal{C}_1 \text{ with } term_1}{pattern_2: \texttt{list} \, \beta \leadsto \mathcal{C}_2 \text{ with } term_2} \\ \frac{Cons(pattern_1, pattern_2): \texttt{list} \, \beta \leadsto \mathcal{C}_1, \mathcal{C}_2 \text{ with } term_1}{\mathsf{Cons}(pattern_1, pattern_2): \mathsf{list} \, \beta \leadsto \mathcal{C}_1, \mathcal{C}_2 \text{ with } term_1 :: term_2} \\ \text{TY_PAT_COMP_CONS}$$

$$\frac{\overline{pattern_i: \beta_i \leadsto \mathcal{C}_i \, \text{with} \, term_i}^i}{\text{Tuple}(\overline{pattern_i}^i): \overline{\beta_i}^i \leadsto \overline{\mathcal{C}_i}^i \, \text{with} \, (\overline{term_i}^i)} \quad \text{TY_PAT_COMP_TUPLE}$$

$$\frac{\overline{pattern_i:\beta \leadsto \mathcal{C}_i \, \mathtt{with} \, term_i}^i}{\operatorname{Array}(\, \overline{pattern_i}^i\,) : \operatorname{array}\beta \leadsto \overline{\mathcal{C}_i}^i \, \mathtt{with} \, [|\,\, \overline{term_i}^i\,|]} \quad \text{Ty_Pat_Comp_Array}$$

$$\frac{pattern: \beta \leadsto \mathcal{C} \, \mathtt{with} \, term}{\mathtt{Specified}(pattern): \beta \leadsto \mathcal{C} \, \mathtt{with} \, term} \quad \mathsf{TY_PAT_COMP_SPECIFIED}$$

 $ident_or_pattern{:}\beta \leadsto \mathcal{C} \, \mathtt{with} \, term$

$$\frac{pattern:\beta \leadsto \mathcal{C} \text{ with } term}{pattern:\beta \leadsto \mathcal{C} \text{ with } term} \quad \text{Ty_Pat_Sym_Or_Pattern_Pattern}$$

$$\Phi \vdash res' = \mathtt{strip_ifs}(res)$$

$$\overline{\Phi \vdash \mathtt{emp} = \mathtt{strip_ifs}\,(\mathtt{emp})} \quad \mathrm{TY_PAT_RES_STRIPIFS_EMPTY}$$

$$\overline{\Phi \vdash pt = \mathtt{strip_ifs}\left(pt\right)} \quad \text{TY_PAT_RES_STRIPIFS_POINTSTO}$$

$$\frac{}{\Phi \vdash res_1 * res_2 = \mathtt{strip_ifs}(res_1 * res_2)} \quad \text{TY_PAT_RES_STRIPIFS_SEPCONJ}$$

$$\overline{\Phi \vdash \exists x : \beta. \ res = \text{strip_ifs} (\exists x : \beta. \ res)} \quad \text{TY_PAT_RES_STRIPIFS_EXISTS}$$

$$\frac{}{\Phi \vdash term \land res = \mathtt{strip_ifs} (term \land res)} \quad \text{TY_PAT_RES_STRIPIFS_TERMCONJ}$$

$$\frac{\texttt{smt}\,(\Phi\Rightarrow term)}{\Phi\vdash res_1'=\,\texttt{strip_ifs}\,(res_1')} \\ \frac{\Phi\vdash res_1'=\,\texttt{strip_ifs}\,(\texttt{if}\,term\,\texttt{then}\,res_1\,\texttt{else}\,res_2)}{\Phi\vdash res_1'=\,\texttt{strip_ifs}\,(\texttt{if}\,term\,\texttt{then}\,res_1\,\texttt{else}\,res_2)}$$

$$\frac{\texttt{smt}\,(\Phi \Rightarrow \neg \textit{term})}{\Phi \vdash \textit{res}_2' = \,\texttt{strip_ifs}\,(\textit{res}_2)} \\ \frac{\Phi \vdash \textit{res}_2' = \,\texttt{strip_ifs}\,(\textit{if}\,\textit{term}\,\texttt{then}\,\textit{res}_1\,\texttt{else}\,\textit{res}_2)}{\Phi \vdash \textit{res}_2' = \,\texttt{strip_ifs}\,(\textit{if}\,\textit{term}\,\texttt{then}\,\textit{res}_1\,\texttt{else}\,\textit{res}_2)}$$

 $\overline{\Phi \vdash \text{if } term \text{ then } res_1 \text{ else } res_2 = \text{strip_ifs} (\text{if } term \text{ then } res_1 \text{ else } res_2)}$

Ty_Pat_Res_StripIfs_UnderDet

 $\frac{}{\Phi \vdash \alpha(\overline{\textit{pval}_i}^i) = \mathsf{strip_ifs}(\alpha(\overline{\textit{pval}_i}^i))} \quad \text{Ty_Pat_Res_StripIfs_Pred}$

 $\Phi \vdash \mathit{res} \ \mathsf{as} \ \mathit{res_pattern} \leadsto \mathcal{L}'; \Phi'; \mathcal{R}'$

 $\overline{\Phi \vdash \mathtt{emp \, as \, emp \, \leadsto \, \cdot; \cdot; \cdot}} \quad \text{TY_PAT_RES_MATCH_EMPTY}$

 $\overline{\Phi \vdash \mathit{res} \; \mathsf{as} \; r \leadsto \cdot; \cdot; \cdot, r {:} \mathit{res}} \quad \mathsf{TY_PAT_RES_MATCH_VAR}$

 $\Phi \vdash res_pattern_1:res_1 \leadsto \mathcal{L}_1; \Phi_1; \mathcal{R}_1$

 $\Phi \vdash res_pattern_2 : res_2 \leadsto \mathcal{L}_2; \Phi_2; \mathcal{R}_2$

 $\frac{\Psi \vdash \mathit{res_pattern}_2 : \mathit{res}_2 \leadsto \mathcal{L}_2; \Psi_2; \mathcal{K}_2}{\Phi \vdash \mathit{res}_1 * \mathit{res}_2 \mathsf{as} \left\langle \mathit{res_pattern}_1, \mathit{res_pattern}_2 \right\rangle \leadsto \mathcal{L}_1, \mathcal{L}_2; \Phi_1, \Phi_2; \mathcal{R}_1, \mathcal{R}_2} \quad \text{TY_PAT_RES_MATCH_SEPCONJ}$

 $\frac{1}{\Phi \vdash term \land res \text{ as } res_pattern \leadsto \mathcal{L}'; \Phi', term; \mathcal{R}'} \quad \text{Ty_Pat_Res_Match_Conj}$ $\Phi \vdash res_pattern:res \leadsto \mathcal{L}'; \Phi'; \mathcal{R}'$

 $\frac{\Phi \vdash \mathit{res_pattern} : x/y, \cdot (\mathit{res}) \leadsto \mathcal{L}'; \Phi'; \mathcal{R}'}{\Phi \vdash \exists \, y : \beta. \, \mathit{res} \, \mathsf{as} \, \mathsf{pack} \, (x, \mathit{res_pattern}) \leadsto \mathcal{L}', \, x : \beta; \Phi'; \mathcal{R}'}$ Ty_Pat_Res_Match_Pack

$$\begin{array}{l} \alpha \equiv \overline{x_{i}:}\overline{\beta_{i}}^{i} \mapsto res \in \texttt{Globals} \\ \frac{\Phi \vdash res_pattern:}{\overline{pval_{i}/x_{i}, \cdot}^{i}(res) \leadsto \mathcal{L}'; \Phi'; \mathcal{R}'} \\ \overline{\Phi \vdash \alpha(\overline{pval_{i}}^{i}) \texttt{ as fold } (res_pattern) \leadsto \mathcal{L}'; \Phi'; \mathcal{R}'} \end{array} \quad \text{Ty_Pat_Res_Match_Fold}$$

 $\Phi \vdash \mathit{res_pattern} : \mathit{res} \leadsto \mathcal{L}' ; \Phi' ; \mathcal{R}'$

$$\frac{\Phi \vdash \mathit{res'} = \mathsf{strip_ifs}\,(\mathit{res})}{\Phi \vdash \mathit{res_pattern} : \mathit{res} \leadsto \mathcal{L'}; \Phi'; \mathcal{R'}} \quad \text{TY_PAT_RES_STRIP_IFS}$$

 $\Phi \vdash \overline{\mathit{ret_pattern}_i}^i : \! \mathit{ret} \leadsto \mathcal{C}'; \mathcal{L}'; \Phi'; \mathcal{R}'$

$$\frac{}{\Phi \vdash : \texttt{I} \leadsto \cdot ; \cdot ; \cdot ; \cdot } \cdot \quad \text{TY_PAT_RET_EMPTY}$$

$$\frac{ident_or_pattern:\beta \leadsto \mathcal{C}_1 \, \text{with} \, term_1}{\Phi \vdash \overline{ret_pattern_i}^i : term_1/y, \cdot (ret) \leadsto \mathcal{C}_2; \mathcal{L}_2; \Phi_2; \mathcal{R}_2} {\Phi \vdash \mathsf{comp} \, ident_or_pattern, \, \overline{ret_pattern_i}^i : \Sigma \, y : \beta. \, ret \leadsto \mathcal{C}_1, \mathcal{C}_2; \mathcal{L}_2; \Phi_2; \mathcal{R}_2} \quad \text{TY_PAT_RET_COMP}$$

$$\frac{\Phi \vdash \overline{\mathit{ret_pattern}_i}^i : \mathit{ret} \leadsto \mathcal{C}'; \mathcal{L}'; \Phi'; \mathcal{R}'}{\Phi \vdash \log y, \, \overline{\mathit{ret_pattern}_i}^i : \exists \, y : \beta. \, \mathit{ret} \leadsto \mathcal{C}'; \mathcal{L}', y : \beta; \Phi'; \mathcal{R}'} \quad \text{Ty_Pat_Ret_Log}$$

$$\frac{\Phi \vdash \mathit{res_pattern} : \mathit{res} \leadsto \mathcal{L}_1; \Phi_1; \mathcal{R}_1}{\Phi \vdash \overline{\mathit{ret_pattern}_i}^i : \mathit{ret} \leadsto \mathcal{C}_2; \mathcal{L}_2; \Phi_2; \mathcal{R}_2} \\ \frac{\Phi \vdash \mathit{res_pattern}, \overline{\mathit{ret_pattern}_i}^i : \mathit{res} \otimes \mathit{ret} \leadsto \mathcal{C}_2; \mathcal{L}_1, \mathcal{L}_2; \Phi_1, \Phi_2; \mathcal{R}_1, \mathcal{R}_2}}{\Phi \vdash \mathit{res_pattern}, \overline{\mathit{ret_pattern}_i}^i : \mathit{res} \otimes \mathit{ret} \leadsto \mathcal{C}_2; \mathcal{L}_1, \mathcal{L}_2; \Phi_1, \Phi_2; \mathcal{R}_1, \mathcal{R}_2}}$$

$$\frac{\Phi \vdash \overline{\mathit{ret_pattern}_i}^i : \mathit{ret} \leadsto \mathcal{C}'; \mathcal{L}'; \Phi'; \mathcal{R}'}{\Phi \vdash \overline{\mathit{ret_pattern}_i}^i : \mathit{term} \land \mathit{ret} \leadsto \mathcal{C}'; \mathcal{L}'; \Phi', \mathit{term}; \mathcal{R}'} \quad \mathsf{TY_PAT_RET_PHI}$$

 $C; \mathcal{L}; \Phi \vdash tpval \Leftarrow ident: \beta. \overline{term}$

$$\frac{\mathtt{smt}\,(\Phi\Rightarrow\mathtt{false})}{\mathcal{C};\mathcal{L};\Phi\vdash\mathtt{undef}\ \mathit{UB_name}\Leftarrow\mathit{y}{:}\beta.\mathit{term}}\quad \mathsf{TY_TPVAL_UNDEF}$$

$$\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta \\ \underline{\text{smt} \left(\Phi \Rightarrow pval/y, \cdot (term)\right)} \\ \overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{done } pval \Leftarrow y:\beta. \ term} \end{array} \quad \text{Ty_TPVal_Done}$$

 $C; \mathcal{L}; \Phi \vdash tpexpr \Leftarrow ident: \beta. term$

$$\begin{split} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \mathsf{bool} \\ \mathcal{C}; \mathcal{L}; \Phi, pval &= \mathsf{true} \vdash tpexpr_1 \Leftarrow y : \beta. \ term \\ \mathcal{C}; \mathcal{L}; \Phi, pval &= \mathsf{false} \vdash tpexpr_2 \Leftarrow y : \beta. \ term \\ \hline \mathcal{C}; \mathcal{L}; \Phi \vdash \mathsf{if} \ pval \ \mathsf{then} \ tpexpr_1 \ \mathsf{else} \ tpexpr_2 \Leftarrow y : \beta. \ term \end{split}$$
 TY_TPE_IF

$$\begin{split} & \mathcal{C}; \mathcal{L}; \Phi \vdash pexpr \Rightarrow y_1 {:} \beta_1. \ term_1 \\ & ident_or_pattern {:} \beta_1 \leadsto \mathcal{C}_1 \ \text{with} \ term \\ & \frac{\mathcal{C}, \mathcal{C}_1; \mathcal{L}; \Phi, term/y_1, \cdot (term_1) \vdash tpexpr \Leftarrow y_2 {:} \beta_2. \ term_2}{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathtt{let} \ ident_or_pattern = pexpr \ \mathtt{in} \ tpexpr \Leftarrow y_2 {:} \beta_2. \ term_2} \end{split} \quad \mathtt{TY_TPE_LET} \end{split}$$

$$\begin{split} \mathcal{C}; \mathcal{L}; \Phi \vdash tpexpr_1 &\Leftarrow y_1 : \beta_1. \ term_1 \\ ident_or_pattern : \beta_1 &\leadsto \mathcal{C}_1 \ \mathtt{with} \ term \\ \mathcal{C}, \mathcal{C}_1; \mathcal{L}; \Phi, term/y_1, \cdot (term_1) \vdash tpexpr &\Leftarrow y_2 : \beta_2. \ term_2 \\ \hline \mathcal{C}; \mathcal{L}; \Phi \vdash \mathtt{let} \ ident_or_pattern : (y_1 : \beta_1. \ term_1) &= tpexpr_1 \ \mathtt{in} \ tpexpr_2 &\Leftarrow y_2 : \beta_2. \ term_2 \end{split} \quad \texttt{TY_TPE_LETT}$$

$$\begin{split} & \frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta_1}{pattern_i : \beta_1 \leadsto \mathcal{C}_i \text{ with } term_i}{}^i} \\ & \frac{\overline{\mathcal{C}, \mathcal{C}_i; \mathcal{L}; \Phi, term_i = pval \vdash tpexpr_i \Leftarrow y_2 : \beta_2. \ term_2}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathsf{case} \ pval \ \mathsf{of} \ \boxed{pattern_i \Rightarrow tpexpr_i}}^i \ \mathsf{end} \ \Leftarrow y_2 : \beta_2. \ term_2} \end{split} \quad \mathsf{TY_TPE_CASE} \end{split}$$

 $C; \mathcal{L}; \Phi; \mathcal{R} \vdash mem_action \Rightarrow ret$

$$\frac{\mathcal{C};\mathcal{L};\Phi\vdash pval\Rightarrow \mathtt{integer}}{\mathcal{C};\mathcal{L};\Phi;\cdot\vdash \mathtt{create}\,(pval,\tau)\Rightarrow \Sigma\,y_p\mathtt{:loc.\,representable}\,(\tau*,y_p)\land \mathtt{alignedI}\,(pval,y_p)\land \exists\,y\mathtt{:}\beta_\tau.\,y_p\overset{\times}{\mapsto}_\tau\,y\otimes\mathtt{I}}\quad \mathtt{TY_ACTION_CREATE}$$

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\mathcal{C}: \mathcal{L}: \Phi \vdash pval_0 \Rightarrow \mathsf{loc}
                                                                                                       \operatorname{smt} (\Phi \Rightarrow pval_0 = pval_1)
                                                \frac{\mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash pval_1\overset{\checkmark}{\mapsto}_{\tau}\;pval_2 \Leftarrow pval_1\overset{\checkmark}{\mapsto}_{\tau}\;pval_2}{\mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash \mathsf{load}\left(\tau,pval_0, \_,pval_1\overset{\checkmark}{\mapsto}_{\tau}\;pval_2\right)\Rightarrow \Sigma\;y:\beta_{\tau}.\;y=pval_2\wedge pval_1\overset{\checkmark}{\mapsto}_{\tau}\;pval_2\otimes \mathtt{I}}
                                                                                                                                                                                                                                                                    TY_ACTION_LOAD
                                                                                                                \mathcal{C}; \mathcal{L}; \Phi \vdash pval_0 \Rightarrow \mathsf{loc}
                                                                                                                \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \beta_{\tau}
                                                                                                                 \operatorname{smt}(\Phi \Rightarrow \operatorname{representable}(\tau, pval_1))
                                                                                                                \operatorname{smt}(\Phi \Rightarrow pval_2 = pval_0)
                                                                                                                \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash pval_2 \mapsto_{\tau} \bot \Leftarrow pval_2 \mapsto_{\tau} \bot
                                                      \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \mathtt{store} \xrightarrow{(\neg, \tau, pval_0, pval_1, \neg, pval_2 \mapsto_{\tau} \neg)} \Rightarrow \Sigma \neg \mathtt{:unit.} \ pval_2 \xrightarrow{\checkmark} pval_1 \otimes \mathtt{I}
                                                                                                                                                                                                                                                                                Ty_Action_Store
                                                                                                        C; \mathcal{L}; \Phi \vdash pval_0 \Rightarrow \mathsf{loc}
                                                                                                        \operatorname{smt} (\Phi \Rightarrow pval_0 = pval_1)
                                                                          \frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash pval_1 \mapsto_{\tau_-} \Leftarrow pval_1 \mapsto_{\tau_-}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{kill} \left( \text{static} \ \tau, pval_0, pval_1 \mapsto_{\tau_-} \right) \Rightarrow \Sigma_-: \text{unit. I}} \quad \text{TY\_ACTION\_KILL\_STATIC}
C; \mathcal{L}; \Phi; \mathcal{R} \vdash mem\_op \Rightarrow ret
                                                                                                                              \mathcal{C}: \mathcal{L}: \Phi \vdash pval_1 \Rightarrow \mathsf{loc}
                                                                                                                              C; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \mathsf{loc}
                                                                                                                                                                                                                                                                 TY_MEMOP_REL_BINOP
                                                          \overline{\mathcal{C};\mathcal{L};\Phi;\cdot\vdash pval_1\ binop_{rel}\ pval_2\Rightarrow\Sigma\ y\text{:bool}.\ y=(pval_1\ binop_{rel}\ pval_2)\wedge\mathtt{I}}
                                                                                                                           C; \mathcal{L}; \Phi \vdash pval \Rightarrow loc
                                                                                                                                                                                                                                                                          TY_MEMOP_INTFROMPTR
                                            \overline{\mathcal{C};\mathcal{L};\Phi;\cdot\vdash \mathtt{intFromPtr}\left(\tau_{1},\tau_{2},pval\right)}\Rightarrow \Sigma \ y\mathtt{:integer}. \ y=\mathtt{cast\_ptr\_to\_int} \ pval\wedge \mathtt{I}
                                                                                                                     \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \mathtt{integer}
                                                                                                                                                                                                                                                                   TY_MEMOP_PTRFROMINT
                                                 \overline{\mathcal{C};\mathcal{L};\Phi;\cdot\vdash \mathsf{ptrFromInt}\left(\tau_1,\tau_2,pval\right)}\Rightarrow \Sigma\,y\mathtt{:loc}.\,\,y=\mathtt{cast\_int\_to\_ptr}\,pval\wedge\mathtt{I}
```

$$\begin{aligned} &\mathcal{C}; \mathcal{L}; \Phi \vdash pval_0 \Rightarrow \texttt{loc} \\ &\texttt{smt} \ (\Phi \Rightarrow pval_1 = pval_0) \\ &\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash pval_1 \overset{\checkmark}{\mapsto}_{\tau} \ _ \Leftarrow pval_1 \overset{\checkmark}{\mapsto}_{\tau} \ _ \end{aligned}$$

Ty_Memop_PtrValidForDeref

 $\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash pval_1 \overset{\checkmark}{\mapsto}_{\tau -} \Leftarrow pval_1 \overset{\checkmark}{\mapsto}_{\tau -}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{ptrValidForDeref}\left(\tau, pval_0, pval_1 \overset{\checkmark}{\mapsto}_{\tau -}\right) \Rightarrow \Sigma \ y \text{:bool.} \ y = \text{aligned}\left(\tau, pval_1\right) \land pval_1 \overset{\checkmark}{\mapsto}_{\tau -} \otimes \mathbf{I} }$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \mathtt{loc}}{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \mathtt{ptrWellAligned}\left(\tau, pval\right) \Rightarrow \Sigma \ y : \mathtt{bool}. \ y = \mathtt{aligned}\left(\tau, pval\right) \wedge \mathtt{I}} \quad \mathsf{TY_MEMOP_PTRWellAligneD}$$

$$\begin{split} \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \texttt{loc} \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \texttt{integer} \\ \hline \mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \texttt{ptrArrayShift} (pval_1, \tau, pval_2) \Rightarrow \Sigma \ y : \texttt{loc.} \ y = pval_1 +_{\texttt{ptr}} (pval_2 \times \texttt{size_of}(\tau)) \land \texttt{I} \end{split} \qquad \texttt{Ty_Memop_PtrArrayShift}$$

 $\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash tval \Leftarrow ret$

$$\overline{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \mathtt{done} \ \Leftarrow \mathtt{I}} \quad \mathrm{TY_TVAL_I}$$

$$\begin{split} & \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta \\ & \frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \mathsf{done} \ \overline{spine_elem_i}^{\ i} \Leftarrow pval/y, \cdot (ret)}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \mathsf{done} \ pval, \ \overline{spine_elem_i}^{\ i} \Leftarrow \Sigma \ y : \beta. \ ret} \end{split} \qquad \text{TY_TVAL_COMP}$$

$$\begin{split} & \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta \\ & \frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \mathsf{done} \ \overline{spine_elem_i}^{\ i} \Leftarrow pval/y, \cdot (ret)}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \mathsf{done} \ pval, \ \overline{spine_elem_i}^{\ i} \Leftarrow \exists \ y : \beta. \ ret} \end{split} \quad \mathsf{TY_TVAL_LOG}$$

$$\begin{split} & \text{smt} \ (\Phi \Rightarrow term) \\ & \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{done} \ spine \Leftarrow ret \\ & \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{done} \ spine \Leftarrow term \land ret \end{split} \quad \text{TY_TVAL_PHI}$$

$$\begin{split} & \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_1 \vdash \mathit{res_term} \Leftarrow \mathit{res} \\ & \frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_2 \vdash \mathsf{done} \, \overline{\mathit{spine_elem}_i}^i \Leftarrow \mathit{ret} }{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_1, \mathcal{R}_2 \vdash \mathsf{done} \, \mathit{res_term}, \, \overline{\mathit{spine_elem}}^i \Leftarrow \mathit{res} \otimes \mathit{ret} } \end{split} \quad \text{Ty_TVAL_RES}$$

$$\frac{\mathtt{smt}\,(\Phi\Rightarrow\mathtt{false})}{\mathcal{C};\mathcal{L};\Phi;\cdot\vdash\mathtt{undef}\ \mathit{UB_name} \Leftarrow\mathit{ret}}\quad \mathtt{TY_TVAL_UNDEF}$$

 $|\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash seq_expr \Rightarrow ret$

$$\begin{split} ident: & arg \equiv \overline{x_i}^i \mapsto texpr \in \texttt{Globals} \\ & \underbrace{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{x_i = spine_elem_i}^i :: arg \gg \sigma; ret}_{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \texttt{ccall}\left(\tau, ident, \overline{spine_elem_i}^i\right) \Rightarrow \sigma(ret)} \end{split} \text{TY_SEQ_E_CCALL}$$

$$\begin{array}{l} \mathit{name} : \mathit{arg} \; \equiv \; \overline{x_i}^{\; i} \; \mapsto \mathit{texpr} \; \in \; \mathsf{Globals} \\ \frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \; \overline{x_i = \mathit{spine_elem}_i}^{\; i} \; :: \mathit{arg} \gg \sigma; \mathit{ret}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \mathsf{pcall} \left(\mathit{name}, \overline{\mathit{spine_elem}_i}^{\; i} \right) \Rightarrow \sigma(\mathit{ret})} \end{array} \quad \mathsf{TY_Seq_E_PROC}$$

 $C; \mathcal{L}; \Phi; \mathcal{R} \vdash is_expr \Rightarrow ret$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem_op \Rightarrow ret}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash memop \ (mem_op) \Rightarrow ret} \quad \text{Ty_Is_E_MEMOP}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem_action \Rightarrow ret}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem_action \Rightarrow ret} \quad \text{Ty_Is_E_Action}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem_action \Rightarrow ret}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash neg \ mem_action \Rightarrow ret} \quad \text{Ty_Is_E_Neg_Action}$$

 $|\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash seq_texpr \Leftarrow ret$

$$\frac{\mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash tval\Leftarrow ret}{\mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash tval\Leftarrow ret} \quad \text{Ty_Seq_TE_TVal}$$

$$\frac{\mathcal{C};\mathcal{L};\Phi\vdash pexpr\Rightarrow y:\beta.\ term}{ident_or_pattern:\beta\rightsquigarrow\mathcal{C}_1\text{ with } term_1}$$

$$\frac{\mathcal{C},\mathcal{C}_1;\mathcal{L};\Phi, term_1/y, \cdot (term);\mathcal{R}\vdash texpr\Leftarrow ret}{\mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash \text{let } ident_or_pattern=pexpr \text{ in } texpr\Leftarrow ret} \quad \text{Ty_Seq_TE_LetP}$$

$$\frac{\mathcal{C};\mathcal{L};\Phi\vdash tpexpr\Leftarrow y:\beta.\ term}{ident_or_pattern:\beta\rightsquigarrow\mathcal{C}_1\text{ with } term_1}$$

$$\frac{\mathcal{C},\mathcal{C}_1;\mathcal{L};\Phi, term_1/y, \cdot (term);\mathcal{R}\vdash texpr\Leftarrow ret}{\mathcal{C};\mathcal{L};\Phi;\mathcal{R}\vdash \text{let } ident_or_pattern:(y:\beta.\ term)=tpexpr \text{ in } texpr\Leftarrow ret} \quad \text{Ty_Seq_Te_LetPT}$$

$$\frac{\mathcal{C};\mathcal{L};\Phi;\mathcal{R}'\vdash \text{seq_expr}\Rightarrow ret_1}{\mathcal{C};\mathcal{L};\Phi,\mathcal{R}';\mathcal{R}\vdash \text{let } ident_or_pattern_i^i: ret_1\rightsquigarrow\mathcal{C}_1;\mathcal{L}_1;\Phi_1;\mathcal{R}_1}$$

$$\frac{\mathcal{C},\mathcal{C}_1;\mathcal{L},\mathcal{L}_1;\Phi,\Phi_1;\mathcal{R},\mathcal{R}_1\vdash texpr\Leftarrow ret_2}{\mathcal{C};\mathcal{L};\Phi;\mathcal{R}',\mathcal{R}\vdash \text{let } ret_pattern_i^i: \text{seq_expr} \text{ in } texpr\Leftarrow ret_2} \quad \text{Ty_Seq_Te_Let}$$

$$\frac{\mathcal{C};\mathcal{L};\Phi;\mathcal{R}',\mathcal{R}\vdash \text{let } ret_pattern_i^i: \text{ret}_1 \rightsquigarrow \mathcal{C}_1;\mathcal{L}_1;\Phi_1;\mathcal{R}_1}{\mathcal{C},\mathcal{C}_1;\mathcal{L},\mathcal{L}_1;\Phi,\Phi_1;\mathcal{R},\mathcal{R}_1\vdash \text{texpr}_2\Leftarrow ret_2} \quad \text{Ty_Seq_Te_LetT}$$

$$\frac{\mathcal{C};\mathcal{L};\Phi;\mathcal{R}',\mathcal{R}\vdash \text{let } ret_pattern_i^i: \text{ret}_1 \Rightarrow \mathcal{C}_1;\mathcal{L}_1;\Phi_1;\mathcal{R}_1}{\mathcal{C},\mathcal{C}_1;\mathcal{L},\mathcal{L}_1;\Phi,\Phi_1;\mathcal{R},\mathcal{R}_1\vdash \text{texpr}_2\Leftarrow ret_2} \quad \text{Ty_Seq_Te_LetT}$$

$$\frac{\mathcal{C};\mathcal{L};\Phi\vdash pval\Rightarrow\beta_1}{\mathcal{C};\mathcal{L};\Phi,\mathcal{R}',\mathcal{R}\vdash \text{let } ret_pattern_i^i: \text{ret}_1 \Rightarrow \text{texpr}_1\text{ in } \text{texpr}_2\Leftarrow ret_2} \quad \text{Ty_Seq_Te_LetT}$$

$$\frac{\mathcal{C};\mathcal{L};\Phi\vdash pval\Rightarrow\beta_1}{pattern_i;\beta_1\rightsquigarrow\mathcal{C}_i\text{ with } \text{term}_i^i: \text{ret}_1 \Rightarrow \text{texpr}_1\text{ in } \text{texpr}_2\Leftarrow ret_2} \quad \text{Ty_Seq_Te_LetT}$$

$$\frac{\mathcal{C};\mathcal{L};\Phi\vdash pval\Rightarrow\beta_1}{\mathcal{C};\mathcal{L};\Phi,\Phi,\text{term}_i = pval;\mathcal{R}\vdash \text{texpr}_i\Leftarrow ret} \quad \text{Ty_Seq_Te_Case}$$

$$\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \texttt{bool} \\ \mathcal{C}; \mathcal{L}; \Phi, pval = \texttt{true}; \mathcal{R} \vdash texpr_1 \Leftarrow ret \\ \mathcal{C}; \mathcal{L}; \Phi, pval = \texttt{false}; \mathcal{R} \vdash texpr_2 \Leftarrow ret \\ \hline \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \texttt{if} pval \texttt{then} texpr_1 \texttt{else} texpr_2 \Leftarrow ret \end{array} \quad \text{TY_SEQ_TE_IF}$$

$$\begin{array}{c} \mathit{ident} : \mathit{arg} \; \equiv \; \overline{x_i}^i \; \mapsto \mathit{texpr} \; \in \; \mathsf{Globals} \\ \mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \; \overline{x_i = \mathit{pval}_i}^i \; :: \; \mathit{arg} \gg \sigma; \mathsf{false} \wedge \mathsf{I} \\ \hline \mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \mathsf{run} \, \mathit{ident} \, \overline{\mathit{pval}_i}^i \; \Leftarrow \; \mathsf{false} \wedge \mathsf{I} \end{array} \quad \text{TY_SEQ_TE_RUN}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_texpr \Leftarrow ret}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \mathsf{bound}\left[int\right](is_texpr) \Leftarrow ret} \quad \mathsf{TY_SeQ_TE_BOUND}$$

 $C; \mathcal{L}; \Phi; \mathcal{R} \vdash is_texpr \Leftarrow ret$

$$\begin{split} \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}' \vdash is_expr \Rightarrow ret_1 \\ \Phi \vdash \overline{ret_pattern_i}^i : ret_1 \leadsto \mathcal{C}_1; \mathcal{L}_1; \Phi_1; \mathcal{R}_1 \\ \mathcal{C}, \mathcal{C}_1; \mathcal{L}, \mathcal{L}_1; \Phi, \Phi_1; \mathcal{R}, \mathcal{R}_1 \vdash texpr \Leftarrow ret_2 \\ \hline \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}', \mathcal{R} \vdash \mathtt{let\,strong} \, \overline{ret_pattern_i}^i = is_expr \, \mathtt{in} \, texpr \Leftarrow ret_2 \end{split} \qquad \text{TY_IS_TE_LETS}$$

 $\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret}$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_texpr \Leftarrow ret}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_texpr \Leftarrow ret} \quad \text{TY_TE_IS}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash seq_texpr \Leftarrow ret}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash seq_texpr \Leftarrow ret} \quad \text{TY_TE_SEQ}$$

 $pattern = pval \leadsto \sigma$

$$\underline{} := pval \leadsto \cdot$$
 Subs_Decons_Value_No_Sym_Annot

$$\overline{x:_=pval \leadsto pval/x,\cdot} \quad \text{Subs_Decons_Value_Sym_Annot}$$

$$\begin{aligned} & pattern_1 = pval_1 \leadsto \sigma_1 \\ & pattern_2 = pval_2 \leadsto \sigma_2 \\ & \overline{\text{Cons}(pattern_1, pattern_2) = \text{Cons}(pval_1, pval_2) \leadsto \sigma_1, \sigma_2} \end{aligned} \quad \text{SUBS_DECONS_VALUE_CONS}$$

$$\frac{\overline{pattern_i} = pval_i \leadsto \overline{\sigma_i}^i}{\text{Tuple}(\overline{pattern_i}^i) = \text{Tuple}(\overline{pval_i}^i) \leadsto \overline{\sigma_i}^i} \quad \text{Subs_Decons_Value_Tuple}$$

$$\frac{\overline{pattern_i = pval_i \leadsto \sigma_i}^i}{\operatorname{Array}(\overline{pattern_i}^i) = \operatorname{Array}(\overline{pval_i}^i) \leadsto \overline{\sigma_i}^i} \quad \text{Subs_Decons_Value_Array}$$

$$\frac{pattern = pval \leadsto \sigma}{\texttt{Specified}(pattern) = pval \leadsto \sigma} \quad \texttt{Subs_Decons_Value_Specified}$$

 $ident_or_pattern = pval \leadsto \sigma$

$$x = pval \leadsto pval/x$$
, Subs_Decons_Value'_Sym

$$\frac{pattern = pval \leadsto \sigma}{pattern = pval \leadsto \sigma} \quad \text{Subs_Decons_Value'_Pattern}$$

 $res_pattern = res_term \leadsto \sigma$

$$\frac{}{\texttt{emp} = \texttt{emp} \leadsto \cdot} \quad \text{Subs_Decons_Res_Emp}$$

 $\overline{ident = res_term \leadsto res_term/ident}, \quad \text{Subs_Decons_Res_Var}$ $res_pattern_1 = res_term_1 \leadsto \sigma_1$ $\mathit{res_pattern}_2 = \mathit{res_term}_2 \leadsto \sigma_2$ $\frac{\textit{res_pattern}_1 \sim \sigma_2}{\langle \textit{res_pattern}_1, \textit{res_pattern}_2 \rangle = \langle \textit{res_term}_1, \textit{res_term}_2 \rangle \leadsto \sigma_1, \sigma_2} \quad \text{Subs_Decons_Res_Pair}$ $\frac{res_pattern = res_term \leadsto \sigma}{\texttt{pack} \, (ident, res_pattern) = \texttt{pack} \, (pval, res_term) \leadsto pval/ident, \sigma} \quad \texttt{Subs_Decons_Res_Pack}$ $\frac{\mathit{res_pattern} = \mathit{res_term} \leadsto \sigma}{\mathtt{fold}\,(\mathit{res_pattern}) = \mathit{res_term} \leadsto \sigma} \quad \mathsf{Subs_Decons_Res_Fold}$ $\overline{ret_pattern_i = spine_elem_i}^i \leadsto \sigma$ \longrightarrow Subs_Decons_Ret_Empty $ident_or_pattern = pval \leadsto \sigma$ $\frac{\overline{ret_pattern_i = spine_elem_i}^i \leadsto \psi}{\operatorname{comp} ident_or_pattern = pval, \ \overline{ret_pattern_i = spine_elem_i}^i \leadsto \sigma, \psi}$ Subs_Decons_Ret_Comp $\frac{\overline{ret_pattern_i = spine_elem_i}^i \leadsto \psi}{\log ident = pval, \ \overline{ret_pattern_i = spine_elem_i}^i \leadsto pval/ident, \psi} \quad \text{Subs_Decons_Ret_Log}$

$$\frac{res_pattern = res_term \leadsto \sigma}{ret_pattern_i = spine_elem_i{}^i \leadsto \psi}$$

$$\frac{res_pattern = res_term, \overline{ret_pattern_i = spine_elem_i{}^i} \leadsto \phi}{res_res_pattern = res_term, \overline{ret_pattern_i = spine_elem_i{}^i} \leadsto \sigma, \psi}$$
 Subs_Decons_Ret_Res

$$\overline{x_i = spine_elem_i}^i :: arg \gg \sigma; ret$$

$$\frac{}{::ret \gg \cdot; ret} \quad \text{Subs_Decons_Arg_Empty}$$

$$\frac{\overline{x_i = spine_elem_i}^i :: arg \gg \sigma; ret}{x = pval, \overline{x_i = spine_elem_i}^i :: \Pi x:\beta. arg \gg pval/x, \sigma; ret} \quad \text{Subs_Decons_Arg_Comp}$$

$$\frac{\overline{x_i = spine_elem_i}^i :: arg \gg \sigma; ret}{x = pval, \overline{x_i = spine_elem_i}^i :: \forall x : \beta. arg \gg pval/x, \sigma; ret}$$
 Subs_Decons_Arg_Log

$$\frac{\overline{x_i = spine_elem_i}^i :: arg \gg \sigma; ret}{x = res_term, \ \overline{x_i = spine_elem_i}^i :: res \multimap arg \gg res_term/x, \sigma; ret}$$
 Subs_Decons_Arg_Res

$$\frac{\overline{x_i = spine_elem_i}^i :: arg \gg \sigma; ret}{\overline{x_i = spine_elem_i}^i :: term \supset arg \gg \sigma; ret} \quad \text{Subs_Decons_Arg_Phi}$$

$$\langle pexpr \rangle \longrightarrow \langle pexpr' \rangle$$

$$\frac{mem_ptr' \equiv mem_ptr +_{ptr} mem_int \times size_of(\tau)}{\langle array_shift (mem_ptr, \tau, mem_int) \rangle \longrightarrow \langle mem_ptr' \rangle} \quad Op_PE_PE_ArrayShift$$

$$\frac{mem_ptr' \equiv mem_ptr +_{\text{ptr}} \text{ offset_of}_{tag}(member)}{\langle \text{member_shift} (mem_ptr, tag, member) \rangle \longrightarrow \langle mem_ptr' \rangle} \quad \text{Op_PE_PE_MEMBERSHIFT}$$

$$\overline{\langle \mathtt{not}\,(\mathtt{True})\rangle \longrightarrow \langle \mathtt{False}\rangle} \quad \mathrm{OP_PE_PE_NOT_TRUE}$$

 $\langle tpexpr \rangle \longrightarrow \langle tpexpr' \rangle$

$$\frac{pattern_{j} = pval \leadsto \sigma_{j}}{\forall i < j. \ \text{not}(pattern_{i} = pval \leadsto \sigma_{i})}}{\langle \text{case} \ pval \ \text{of} \ | \ pattern_{i} \Rightarrow tpexpr_{i}^{-1} \ \text{end} \rangle \longrightarrow \langle \sigma_{j}(tpexpr_{j}) \rangle}} \quad \text{Op.TPE.TPE.Case}$$

$$\frac{ident.or.pattern}{\langle \text{let} \ ident.or.pattern} = pval \leadsto \sigma}{\langle \text{let} \ ident.or.pattern} = pval \ \text{in} \ tpexpr \rangle \longrightarrow \langle \sigma(tpexpr) \rangle} \quad \text{Op.TPE.TPE.Let.SuB}$$

$$\frac{\langle pexpr \rangle \longrightarrow \langle pexpr' \rangle}{\langle \text{let} \ ident.or. pattern} = pexpr \ \text{in} \ tpexpr \rangle \longrightarrow \langle \text{let} \ ident.or. pattern} = pexpr' \ \text{in} \ tpexpr \rangle} \quad \text{Op.TPE.TPE.Let.Let.}$$

$$\frac{\langle pexpr \rangle \longrightarrow \langle tpexpr_{1} : (y : \beta. \ term) \rangle}{\langle \text{let} \ ident.or. pattern} = pexpr \ \text{in} \ tpexpr_{2} \rangle \longrightarrow \langle \text{let} \ ident.or. pattern; (y : \beta. \ term) = tpexpr_{1} \ \text{in} \ tpexpr_{2} \rangle} \quad \text{Op.TPE.TPE.Let.Let.T.SuB}$$

$$\frac{ident.or. pattern}{\langle \text{let} \ ident.or. pattern:}(y : \beta. \ term) = tpexpr_{1} \ \text{in} \ tpexpr_{2} \rangle} \quad \text{Op.TPE.TPE.Let.T.SuB}$$

$$\frac{\langle tpexpr_{1} \rangle \longrightarrow \langle tpexpr_{1} \rangle}{\langle \text{let} \ ident.or. pattern:}(y : \beta. \ term) = tpexpr_{1} \ \text{in} \ tpexpr_{2} \rangle} \quad \text{Op.TPE.TPE.Let.T.Let.T.}$$

$$\frac{\langle tpexpr_{1} \rangle \longrightarrow \langle tpexpr_{2} \rangle}{\langle \text{let} \ ident.or. pattern:}(y : \beta. \ term) = tpexpr_{1} \ \text{in} \ tpexpr_{2} \rangle} \quad \text{Op.TPE.TPE.Let.T.Let.T.}$$

$$\frac{\langle tpexpr_{1} \rangle \longrightarrow \langle tpexpr_{2} \rangle}{\langle \text{let} \ ident.or. pattern:}(y : \beta. \ term) = tpexpr_{1} \ \text{in} \ tpexpr_{2} \rangle} \quad \text{Op.TPE.TPE.Let.T.Let.T.}$$

$$\frac{\langle tpexpr_{1} \rangle \longrightarrow \langle tpexpr_{2} \rangle \longrightarrow \langle tpexpr_{2} \rangle}{\langle tpexpr_{2} \rangle \longrightarrow \langle tpexpr_{2} \rangle} \quad \text{Op.TPE.TPE.Let.T.Let.T.}$$

$$\frac{\langle tpexpr_{1} \rangle \longrightarrow \langle tpexpr_{2} \rangle}{\langle tpexpr_{2} \rangle \longrightarrow \langle tpexpr_{2} \rangle} \quad \text{Op.TPE.TPE.Let.F.Alse}}$$

$$\frac{\langle tpexpr_{2} \rangle \longrightarrow \langle tpexpr_{2} \rangle}{\langle tpexpr_{2} \rangle \longrightarrow \langle tpexpr_{2} \rangle} \quad \text{Op.TPE.TPE.Let.F.Alse}}$$

$$\frac{ident:arg \equiv \overline{x_i}^i \rightarrow texpr \in \texttt{Globals}}{z_i = spine.clem_i}^i : arg \gg \sigma_i ret} \qquad \texttt{OP_SE_TE_CCALL}$$

$$\frac{name:arg \equiv \overline{x_i}^i \rightarrow texpr \in \texttt{Globals}}{z_i = spine.elem_i}^i : arg \gg \sigma_i ret} \qquad \texttt{OP_SE_TE_CCALL}$$

$$\frac{name:arg \equiv \overline{x_i}^i \rightarrow texpr \in \texttt{Globals}}{z_i = spine.elem_i}^i : arg \gg \sigma_i ret} \qquad \texttt{OP_SE_TE_PCALL}$$

$$\frac{ident:arg \equiv \overline{x_i}^i \rightarrow texpr \in \texttt{Globals}}{z_i = pval_i}^i : arg \gg \sigma_i false \land 1} \qquad \texttt{OP_STE_TE_RUN}$$

$$\frac{ident:arg \equiv \overline{x_i}^i \rightarrow texpr \in \texttt{Globals}}{z_i = pval_i}^i : arg \gg \sigma_i false \land 1} \qquad \texttt{OP_STE_TE_RUN}$$

$$\frac{pattern_j = pval \leadsto \sigma_j}{\langle h; run \, ident \, \overline{pval_i}^i \rangle \rightarrow \langle h; \sigma(texpr) \rangle} \qquad \texttt{OP_STE_TE_CASE}$$

$$\frac{pattern_j = pval \leadsto \sigma_j}{\langle h; case \, pval \, of \, [\, pattern_i \Rightarrow texpr_i^i \, end \rangle \rightarrow \langle h; \sigma_j(texpr_j) \rangle} \qquad \texttt{OP_STE_TE_CASE}$$

$$\frac{ident.or_pattern = pval \leadsto \sigma}{\langle h; let \, ident.or_pattern = pval \, in \, texpr_i^i \, end \rangle \rightarrow \langle h; \sigma(texpr_j) \rangle} \qquad \texttt{OP_STE_TE_LETP_SUB}$$

$$\frac{(pexpr) \longrightarrow \langle pexpr' \rangle}{\langle h; let \, ident.or_pattern = pexpr \, in \, texpr' \rangle \rightarrow \langle h; let \, ident.or_pattern = pexpr' \, in \, texpr}} \qquad \texttt{OP_STE_TE_LETP_LETP}$$

$$\frac{\langle pexpr \rangle \longrightarrow \langle pexpr' \rangle}{\langle h; let \, ident.or_pattern = pexpr \, in \, texpr \rangle \rightarrow \langle h; let \, ident.or_pattern = texpr \rangle} \qquad \texttt{OP_STE_TE_LETP_LETP}$$

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\frac{ident\_or\_pattern = pval \leadsto \sigma}{\langle h; \texttt{let} ident\_or\_pattern: (y:\beta. \ term) = \texttt{done} \ pval \ \texttt{in} \ texpr \rangle \longrightarrow \langle h; \sigma(texpr) \rangle} \quad \text{Op\_STE\_TE\_LetTP\_Sub}
\frac{\langle tpexpr\rangle \longrightarrow \langle tpexpr'\rangle}{\langle h; \mathtt{let}\, ident\_or\_pattern: (y:\beta.\,\, term) = tpexpr\, \mathtt{in}\, texpr\rangle \longrightarrow \langle h; \mathtt{let}\, ident\_or\_pattern: (y:\beta.\,\, term) = tpexpr'\, \mathtt{in}\, texpr\rangle} \quad \text{Op\_STE\_TE\_LetTP\_LetTP}
                                                          \frac{\overline{ret\_pattern_i = spine\_elem_i}^i \leadsto \sigma}{\langle h; \mathtt{let}\, \overline{ret\_pattern_i}^i : ret = \mathtt{done}\, \overline{spine\_elem_i}^i \, \mathtt{in}\, texpr \rangle \longrightarrow \langle h; \sigma(texpr) \rangle} \quad \mathsf{OP\_STE\_TE\_LETT\_SUB}
                                   \frac{\langle h; seq\_expr \rangle \longrightarrow \langle h; texpr_1 : ret \rangle}{\langle h; \mathsf{let} \ \overline{ret\_pattern_i}^i = seq\_expr \ \mathsf{in} \ texpr_2 \rangle \longrightarrow \langle h; \mathsf{let} \ \overline{ret\_pattern_i}^i : ret = texpr_1 \ \mathsf{in} \ texpr_2 \rangle} \quad \mathsf{OP\_STE\_TE\_LET\_LETT}
                               \frac{\langle h; texpr_1 \rangle \longrightarrow \langle h'; texpr_1' \rangle}{\langle h; \mathsf{let} \, \overline{ret\_pattern_i}^{\,\, i} : ret = texpr_1 \, \mathsf{in} \, texpr_2 \rangle \longrightarrow \langle h'; \mathsf{let} \, \overline{ret\_pattern_i}^{\,\, i} : ret = texpr_1' \, \mathsf{in} \, texpr_2 \rangle} \quad \mathsf{OP\_STE\_TE\_LETT\_LETT}
                                                                                       \overline{\langle h; \text{if True then } texpr_1 \text{ else } texpr_2 \rangle \longrightarrow \langle h; texpr_1 \rangle} OP_STE_TE_IF_TRUE
                                                                                    \overline{\langle h; \text{if False then } texpr_1 \text{ else } texpr_2 \rangle \longrightarrow \langle h; texpr_2 \rangle}
                                                                                                                                                                                                                         OP_STE_TE_IF_FALSE
                                                                                                   \frac{}{\langle h; \mathtt{bound} \, [int] (is\_texpr) \rangle \longrightarrow \langle h; is\_texpr \rangle} \quad \mathsf{OP\_STE\_TE\_BOUND}
 \langle h; mem\_op \rangle \longrightarrow \langle h'; tval \rangle
                                                                    \frac{bool\_value \equiv mem\_int_1 \ binop_{rel} \ mem\_int_2}{\langle h; mem\_int_1 \ binop_{rel} \ mem\_int_2 \rangle \longrightarrow \langle h; \texttt{done} \ bool\_value \rangle}
                                                                                                                                                                                                                      Op_Memop_TVal_Rel_Binop
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mem\_int \equiv \texttt{cast\_ptr\_to\_int} \ mem\_ptr
                                                                                                                                                                                            Op_Memop_TVal_IntFromPtr
                                                             \overline{\langle h; \mathtt{intFromPtr} \left(\tau_1, \tau_2, mem\_ptr\right)\rangle \longrightarrow \langle h; \mathtt{done} \ mem\_int\rangle}
                                                             \frac{mem\_ptr \equiv \texttt{cast\_ptr\_to\_int} \ mem\_int}{\langle h; \texttt{ptrFromInt} \ (\tau_1, \tau_2, mem\_int) \rangle \longrightarrow \langle h; \texttt{done} \ mem\_ptr \rangle}
                                                                                                                                                                                            OP_MEMOP_TVAL_PTRFROMINT
                                                                                                     bool\_value \equiv aligned(\tau, mem\_ptr)
\frac{\textit{bool\_value} = \texttt{aligned}\left(\tau, \textit{mem\_ptr}\right)}{\langle h + \{\textit{mem\_ptr} \overset{\checkmark}{\mapsto}_{\tau -} \}; \texttt{ptrValidForDeref}\left(\tau, \textit{mem\_ptr}, \textit{mem\_ptr} \overset{\checkmark}{\mapsto}_{\tau -} \right) \rangle \longrightarrow \langle h + \{\textit{mem\_ptr} \overset{\checkmark}{\mapsto}_{\tau -} \}; \texttt{done}\, \textit{bool\_value}, \textit{mem\_ptr} \overset{\checkmark}{\mapsto}_{\tau -} \rangle}
                                                                                                                                                                                                                                                                                              OP_MEMOP_TVAL_PTRVALID
                                                                            bool\_value \equiv \mathtt{aligned}\left(\tau, mem\_ptr\right)
                                                    \overline{\langle h; \mathtt{ptrWellAligned} \left(\tau, mem\_ptr\right) \rangle \longrightarrow \langle h; \mathtt{done} \, bool\_value \rangle}
                                                                                                                                                                                      Op_Memop_TVal_PtrWellAligned
                                              \frac{mem\_ptr' \equiv mem\_ptr +_{ptr} (mem\_int \times size\_of(\tau))}{\langle h; ptrArrayShift (mem\_ptr, \tau, mem\_int) \rangle \longrightarrow \langle h; done mem\_ptr' \rangle}
                                                                                                                                                                                                  Op_Memop_TVal_PtrArrayShift
   \langle h; mem\_action \rangle \longrightarrow \langle h'; tval \rangle
                                                                                               fresh(mem_ptr)
                                                                                               \texttt{representable} \ (\tau*, mem\_ptr)
                                                                                               alignedI (mem_int, mem_ptr)
                                                                                                                                                                                                                                          OP_ACTION_TVAL_CREATE
                           \overline{\langle h; \mathtt{create}\,(mem\_int,\tau)\rangle \longrightarrow \langle h + \{mem\_ptr \overset{\times}{\mapsto}_{\tau}\,pval\}; \mathtt{done}\,mem\_ptr,pval,mem\_ptr \overset{\times}{\mapsto}_{\tau}\,pval\rangle}
                                                                                                                                                                                                                                                                                    OP_ACTION_TVAL_LOAD
\frac{}{\langle h + \{mem\_ptr \overset{\checkmark}{\mapsto}_{\tau} \ pval\}; \texttt{load} \ (\tau, mem\_ptr, \_, mem\_ptr \overset{\checkmark}{\mapsto}_{\tau} \ pval) \rangle} \longrightarrow \langle h + \{mem\_ptr \overset{\checkmark}{\mapsto}_{\tau} \ pval\}; \texttt{done} \ pval, mem\_ptr \overset{\checkmark}{\mapsto}_{\tau} \ pval \rangle}
                                                                                                                                                                                                                                                                                        OP_ACTION_TVAL_STORE
\frac{}{\langle h + \{mem\_ptr \overset{\checkmark}{\mapsto}_{\tau} \_\}; \mathtt{store} \left( \_, \tau, mem\_ptr, pval, \_, mem\_ptr \overset{\checkmark}{\mapsto}_{\tau} \_ \right) \rangle} \longrightarrow \langle h + \{mem\_ptr \overset{\checkmark}{\mapsto}_{\tau} \ pval\}; \mathtt{done} \ \mathtt{Unit}, mem\_ptr \overset{\checkmark}{\mapsto}_{\tau} \ pval \rangle}
```

 $\frac{}{\langle h + \{mem_ptr \mapsto_{\tau_-}\}; \texttt{kill} (\texttt{static} \, \tau, mem_ptr, mem_ptr \mapsto_{\tau_-}) \rangle \longrightarrow \langle h; \texttt{done} \, \texttt{Unit} \rangle} \quad \text{OP_ACTION_TVAL_KILL_STATIC}$

 $\langle h; is_expr \rangle \longrightarrow \langle h'; is_expr' \rangle$

$$\frac{\langle h; mem_op \rangle \longrightarrow \langle h; tval \rangle}{\langle h; memop (mem_op) \rangle \longrightarrow \langle h; tval \rangle} \quad \text{Op_ISE_ISE_MEMOP}$$

$$\frac{\langle h; mem_action \rangle \longrightarrow \langle h'; tval \rangle}{\langle h; mem_action \rangle \longrightarrow \langle h'; tval \rangle} \quad \text{Op_IsE_IsE_Action}$$

$$\frac{\langle h; mem_action \rangle \longrightarrow \langle h'; tval \rangle}{\langle h; \mathsf{neg}\, mem_action \rangle \longrightarrow \langle h'; tval \rangle} \quad \mathsf{OP_ISE_ISE_NEG_ACTION}$$

 $\langle h; is_texpr \rangle \longrightarrow \langle h'; texpr \rangle$

$$\frac{\overline{ret_pattern_i = spine_elem_i}^i \leadsto \sigma}{\langle h; \mathtt{let strong} \, \overline{ret_pattern_i}^i = \mathtt{done} \, \overline{spine_elem_i}^i \, \mathtt{in} \, texpr \rangle \longrightarrow \langle h; \sigma(texpr) \rangle} \quad \mathsf{OP_ISTE_ISTE_LETS_SUB}$$

$$\frac{\langle h; is_expr\rangle \longrightarrow \langle h'; is_expr'\rangle}{\langle h; \mathsf{let} \, \mathsf{strong} \, \overline{ret_pattern_i}^{\,\, i} \, = is_expr \, \mathsf{in} \, texpr\rangle \longrightarrow \langle h'; \mathsf{let} \, \mathsf{strong} \, \overline{ret_pattern_i}^{\,\, i} \, = is_expr' \, \mathsf{in} \, texpr\rangle} \quad \mathsf{OP_ISTE_ISTE_LETS_LETS}$$

 $\overline{\langle h; texpr \rangle} \longrightarrow \langle h'; texpr' \rangle$

$$\frac{\langle h; seq_texpr \rangle \longrightarrow \langle h; texpr \rangle}{\langle h; seq_texpr \rangle \longrightarrow \langle h; texpr \rangle} \quad \text{Op_TE_TE_SeQ}$$

$$\frac{\langle h; is_texpr\rangle \longrightarrow \langle h'; texpr\rangle}{\langle h; is_texpr\rangle \longrightarrow \langle h'; texpr\rangle} \quad \text{Op_TE_TE_IS}$$

Definition rules: 213 good 0 bad Definition rule clauses: 476 good 0 bad