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1 |----- MODULE GCD -----|
2 | EXTENDS Integers, FiniteSets, TLAPS, NaturalsInduction
3 |-----|
4 | Divides(p, n)  $\triangleq \exists q \in \textit{Int} : n = p * q$ 
5 | DivisorsOf(n)  $\triangleq \{p \in \textit{Int} : \textit{Divides}(p, n)\}$ 
6 |
7 | SetMax(S)  $\triangleq \text{CHOOSE } i \in S : \forall j \in S : i \geq j$ 
8 |
9 | GCD(m, n)  $\triangleq \textit{SetMax}(\textit{DivisorsOf}(m) \cap \textit{DivisorsOf}(n))$ 
10 |
11 | THEOREM GCD1  $\triangleq \forall m \in \textit{Nat} \setminus \{0\} : \textit{GCD}(m, m) = m$ 
12 | THEOREM GCD2  $\triangleq \forall m, n \in \textit{Nat} \setminus \{0\} : \textit{GCD}(m, n) = \textit{GCD}(n, m)$ 
13 | THEOREM GCD3  $\triangleq \forall m, n \in \textit{Nat} \setminus \{0\} : (n > m) \Rightarrow (\textit{GCD}(m, n) = \textit{GCD}(m, n - m))$ 
14 |-----|

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