

# The SAFE Specification

*Working Draft*

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Sukyoung Ryu  
Jaejun Choi  
Woongsik Choi  
Yoonseok Ko  
Hongki Lee  
Changhee Park

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# Chapter 1

## Overview

The prevalent uses of JavaScript in web programming have revealed security vulnerability issues of JavaScript applications, which emphasizes the need for JavaScript analyzers to detect such issues. Recently, researchers have proposed several analyzers of JavaScript programs and some web service companies have developed various JavaScript engines. However, unfortunately, most of the tools are not documented well, thus it is very hard to understand and modify them. Or, such tools are often not open to the public.

In this specification, we present formal specification and implementation of **SAFE**, a scalable analysis framework for ECMAScript, developed for the JavaScript research community. This is the very first attempt to provide both formal specification and its open-source implementation for JavaScript, compared to the existing approaches focused on only one of them. To make it more amenable for other researchers to use our framework, we formally define three kinds of intermediate representations for JavaScript used in the framework, and we provide formal specifications of translations between them. To be adaptable for adventurous future research including modifications in the original JavaScript syntax, we actively use open-source tools to automatically generate parsers and some intermediate representations. To support a variety of program analyses in various compilation phases, we design the framework to be as flexible, scalable, and pluggable as possible. Finally, our framework is publicly available, and some collaborative research using the framework are in progress.

# Chapter 2

## AST

$p$	$::=$	$fd^* vd^* s^*$	<code>Program(TopLevel body)</code>
$fd$	$::=$	<code>function <math>f((x,)^*) \{fd^* vd^* s^*\}</math></code>	<code>TopLevel(List&lt;FunDecl&gt; fds, List&lt;VarDecl&gt; vds, List&lt;SourceElement&gt; stmts)</code>
$vd$	$::=$	<code>var <math>x</math></code>	<code>FunDecl(Id name, Functional ftn)</code>
$s$	$::=$	<code>{<math>s^*</math>}</code>	<code>Functional(List&lt;FunDecl&gt; fds, List&lt;VarDecl&gt; vds, List&lt;SourceElement&gt; stmts, List&lt;Id&gt; params)</code>
		<code>var <math>vd(, vd)^*</math>;</code>	<code>VarDecl(Id name, Option&lt;Expr&gt; expr)</code>
		<code>;</code>	<code>Block(List&lt;Stmt&gt; stmts, boolean internal = false)</code>
		<code><math>e</math>;</code>	<code>VarStmt(List&lt;VarDecl&gt; vds)</code>
		<code>if (<math>e</math>) <math>s</math> (else <math>s</math>)<sup>?</sup></code>	<code>EmptyStmt()</code>
			<code>ExprStmt(Expr expr)</code>
		<code>switch (<math>e</math>) {<math>cc^*(default:s^*)^? cc^*</math>}</code>	<code>If(Expr cond, Stmt trueBranch, Option&lt;Stmt&gt; falseBranch)</code>
			<code>Switch(Expr cond, List&lt;Case&gt; frontCases, Option&lt;List&lt;Stmt&gt;&gt; def, List&lt;Case&gt; backCases)</code>
		<code>do <math>s</math> while (<math>e</math>);</code>	<code>DoWhile(Stmt body, Expr cond)</code>
		<code>while (<math>e</math>) <math>s</math></code>	<code>While(Expr cond, Stmt body)</code>
		<code>for (<math>e^?; e^?; e^?</math>) <math>s</math></code>	<code>For(Option&lt;Expr&gt; init, Option&lt;Expr&gt; cond, Option&lt;Expr&gt; action, Stmt body)</code>
			<code>ForIn(LHS lhs, Expr expr, Stmt body)</code>
		<code>for (var <math>vd(, vd)^*; e^?; e^?</math>) <math>s</math></code>	<code>ForVar(List&lt;VarDecl&gt; vars, Option&lt;Expr&gt; cond, Option&lt;Expr&gt; action, Stmt body)</code>
			<code>ForVarIn(VarDecl var, Expr expr, Stmt body)</code>
		<code>for (var <math>vd</math> in <math>e</math>) <math>s</math></code>	<code>Continue(Option&lt;Label&gt; target)</code>
		<code>continue <math>x^?</math>;</code>	<code>Break(Option&lt;Label&gt; target)</code>
		<code>break <math>x^?</math>;</code>	<code>Return(Option&lt;Expr&gt; expr)</code>
		<code>return <math>e^?</math>;</code>	<code>With(Expr expr, Stmt stmt)</code>
		<code>with (<math>e</math>) <math>s</math></code>	<code>LabelStmt(Label label, Stmt stmt)</code>
		<code><math>l : s</math></code>	<code>Throw(Expr expr)</code>
		<code>throw <math>e</math>;</code>	<code>Try(Block body, Option&lt;Catch&gt; catchBlock, Option&lt;Block&gt; fin)</code>
		<code>try{<math>s^*</math>}(catch(<math>x</math>) {<math>s^*</math>})<sup>?</sup>(finally{<math>s^*</math>})<sup>?</sup></code>	<code>Catch(Id id, Block body)</code>
			<code>Debugger()</code>
		<code>debugger;</code>	<code>Case(Expr cond, Block body)</code>
$cc$	$::=$	<code>case <math>e : s^*</math></code>	<code>Debugger()</code>
$e$	$::=$	<code><math>e, e</math></code>	<code>Case(Expr cond, Block body)</code>
		<code><math>e ? e : e</math></code>	<code>ExprList(List&lt;Expr&gt; exprs)</code>
		<code><math>e \otimes e</math></code>	<code>Cond(Expr cond, Expr trueBranch, Expr falseBranch)</code>
		<code><math>\ominus e</math></code>	<code>InfixOpApp(Expr left, Op op, Expr right)</code>
		<code><math>lhs \oslash</math></code>	<code>PrefixOpApp(Op op, Expr right)</code>
		<code><math>lhs \odot e</math></code>	<code>UnaryAssignOpApp(LHS lhs, Op op)</code>
		<code><math>lhs</math></code>	<code>AssignOpApp(LHS lhs, Op op, Expr right)</code>
			<code>LHS()</code>

<i>lhs</i>	::=	<i>lit</i>	Literal()
		<i>x</i>	VarRef(Id id)
		$[(e^?,)^*]$	ArrayExpr(List<Option<Expr>> elements)
		$\{ (m,)^* \}$	ObjectExpr(List<Member> members)
		$(e)$	Parenthesized(Expr expr)
		<b>function</b> $x^? ((x,)^*) \{fd^* vd^* s^*\}$	FunExpr(Option<Id> name, Functional ftn)
		<i>lhs</i> [ <i>e</i> ]	Bracket(LHS obj, Expr index)
		<i>lhs</i> . <i>x</i>	Dot(LHS obj, Id member)
		<b>new</b> <i>lhs</i>	New(LHS lhs)
		<i>lhs</i> $((e,)^*)$	FunApp(LHS fun, List<Expr> args)
<i>lit</i>	::=	<b>this</b>	This()
		<b>null</b>	Null()
		<b>true</b>	Bool(boolean bool)
		<b>false</b>	Bool(boolean bool)
		<i>num</i>	DoubleLiteral(ignoreForEquals String text, Double num)
		<i>str</i>	IntLiteral(BigInteger intVal, int radix)
		<i>reg</i>	StringLiteral(String str, String quote)
			RegularExpression(String reg)
<i>m</i>	::=	<i>pr</i> : <i>e</i>	Field(Property prop, Expr expr)
		<b>get</b> <i>pr</i> () $\{fd^* vd^* s^*\}$	GetProp(Property prop, Functional ftn)
		<b>set</b> <i>pr</i> ( <i>x</i> ) $\{fd^* vd^* s^*\}$	SetProp(Property prop, Functional ftn)
<i>pr</i>	::=	<i>x</i>	PropId(Id id)
		<i>str</i>	PropStr(String str)
		<i>num</i>	PropNum(NumberLiteral num)

$\odot ::= = \mid * \mid / \mid \% \mid + \mid - \mid < < = \mid > > = \mid > > > = \mid \& \mid ^ \mid \mid =$   
 $\otimes ::= \& \& \mid \mid \mid \mid \mid \& \mid ^ \mid < < \mid > > \mid > > > \mid + \mid - \mid * \mid / \mid \% \mid = \mid ! = \mid == \mid != \mid < \mid > \mid < = \mid > =$   
 $\mid \text{instanceof} \mid \text{in}$   
 $\ominus ::= ++ \mid -- \mid \sim \mid ! \mid + \mid - \mid \text{delete} \mid \text{void} \mid \text{typeof}$   
 $\oslash ::= ++ \mid --$

- **VarDecl: The expr field is None after Hoister.**
- **VarStmt, ForVar, ForVarIn: Removed by Hoister.**
- **RegularExpression: Not yet supported.**
- **StmtUnit: Internally generated statement unit by Hoister.**

# Chapter 3

## IR

$\underline{p} ::= \underline{s}^*$	IRRoot
$\underline{s} ::= \underline{x} = \underline{e}$	IRExprStmt(IRId lhs, IRExpr right, boolean ref = false)
$\underline{x} = \text{delete } \underline{x}$	IRDelete(IRId lhs, IRId id)
$\underline{x} = \text{delete } \underline{x}[\underline{x}]$	IRDeleteProp(IRId lhs, IRId obj, IRId index)
$\underline{x}[\underline{x}] = \underline{e}$	IRStore(IRId obj, IRId index, IRExpr rhs)
$\underline{x} = \{(\underline{m},)^*\}$	IRObjekt(IRId lhs, List<IRMember> members,
	Option<IRId> proto)
$\underline{x} = [(\underline{e},)^*]$	IRArray(IRId lhs, List<Option<IRExpr>> elements)
	IRArgs(IRId lhs, List<Option<IRExpr>> elements)
$\underline{x} = \underline{x}(\underline{x}, \underline{x})$	IRCall(IRId lhs, IRId fun, IRId thisB, IRId args)
$\underline{x} = \underline{x}(\underline{x}, \underline{x})^?$	IRInternalCall(IRId lhs, IRId fun, IRExpr first,
	Option<IRId> second)
	toObject, toNumber, isObject, getBase, iteratorInit,
	iteratorHasNext, iteratorKey
$\underline{x} = \text{new } \underline{x}((\underline{x},)^*)$	IRNew(IRId lhs, IRId fun, List<IRId> args)
$\underline{x} = \text{function } \underline{f}(\underline{x}, \underline{x}) \{ \underline{s}^* \}$	IRFunExpr(IRId lhs, IRFunctional ftn)
	IRFunctional(IRId name, List<IRId> params,
	List<IRStmt> args, List<IRFunDecl> fds,
	List<IRVarStmt> vds, List<IRStmt> body)
	IRFunDecl(IRFunctional ftn)
$\underline{x} = \text{eval } (\underline{e})$	IREval(IRId lhs, IRExpr arg)
$\text{break } \underline{x}$	IRBreak(IRId label)
$\text{return } \underline{e}^?$	IRReturn(Option<IRExpr> expr)
$\text{with } (\underline{x}) \underline{s}$	IRWith(IRId id, IRStmt stmt)
$\underline{l} : \{ \underline{s} \}$	IRLabelStmt(IRId label, IRStmt stmt)
$\text{var } \underline{x}$	IRVarStmt(IRId lhs)
$\text{throw } \underline{e}$	IRThrow(IRExpr expr)
$\underline{s}^*$	IRSeq(List<IRStmt> stmts)
$\text{if } (\underline{e}) \text{ then } \underline{s} \text{ (else } \underline{s})^?$	IRIf(IRExpr expr, IRStmt trueB, Option<IRStmt> falseB)
$\text{while } (\underline{e}) \underline{s}$	IRWhile(IRExpr cond, IRStmt body)
$\text{try } \{ \underline{s} \} \text{ (catch } (\underline{x}) \{ \underline{s} \})^? \text{ (finally } \{ \underline{s} \})^?$	IRTry(IRStmt body, Option<IRId> name,
	Option<IRStmt> catchB, Option<IRStmt> finallyB)
$\langle \underline{s}^* \rangle$	IRStmtUnit(List<IRStmt> stmts)
$\underline{e} ::= \underline{e} \otimes \underline{e}$	IRBin(IRExpr first, IROp op, IRExpr second)
$\ominus \underline{e}$	IRUn(IROp op, IRExpr expr)
$\underline{x}[\underline{e}]$	IRLoad(IRId obj, IRExpr index)
$\underline{x}$	IRUserId(String text)
$\otimes \underline{x}$	IRImpId(String text)
$\underline{num}$	IRNumber(ignoreForEquals String text, Double num)
$\underline{str}$	IRString(String str)
$\text{true}$	IRBool(boolean bool)
$\text{false}$	IRBool(boolean bool)
$\text{undefined}$	IRUndef()
$\text{null}$	IRNull()
$\text{this}$	IRThis()

$\underline{m}$	$::=$	$\underline{x} : \underline{e}$	$\text{IRField}(\text{IRId prop}, \text{IRExpr expr})$
		$\text{get } \underline{f}(\underline{x}, \underline{x}) \{ \underline{s}^* \}$	$\text{IRGetProp}(\text{IRFunctional ftn})$
		$\text{set } \underline{f}(\underline{x}, \underline{x}) \{ \underline{s}^* \}$	$\text{IRSetProp}(\text{IRFunctional ftn})$

Assumptions and notations:

- Functions and variables are hoisted to their closest enclosing functions or the top level via `Hoister`.
- Identifiers and labels that exist in the source program, except when they appear at top level or within the `with` statement, are already disambiguated via `Disambiguator`, so that they have unique names.
- We use  $\Sigma$  to disambiguate the generated labels and temporary variables in the AST to IR translation. For the presentation brevity, we simply add the newly generated names to  $\Sigma$ .
  - In the actual implementation, we need to create a unique id for each generated name and add the binding information from the general name to the unique id to  $\Sigma$ . For example, when we say “ $\Sigma; \diamond\text{break}$ ”, we actually create a unique id for  $\diamond\text{break}$ , say  $\diamond\text{break}_{42}$ , and add it to  $\Sigma$  as  $\Sigma; \diamond\text{break} \mapsto \diamond\text{break}_{42}$ . When we look up the environment by  $\Sigma(\diamond\text{break})$ , the unique  $\diamond\text{break}_{42}$  is returned.
  - In the scope when the generated name is created, we don’t add it to the environment but use the unique id instead of the general name. For example, when we say “ $\diamond\text{eq} = \Sigma(\diamond\text{val}) == \diamond\text{break}$ ”, we create a unique id for  $\diamond\text{eq}$ , say  $\diamond\text{eq}_{910157}$ , and it is actually “ $\diamond\text{eq}_{910157} = \Sigma(\diamond\text{val}) == \diamond\text{break}_{42}$ ”.
  - To be clear, we use blue for the binding sites of such names and red for the use sites of such names.
- We denote a list as a possibly empty, semicolon-separated sequence, enclosed by  $\langle$  and  $\rangle$ .
- We denote a series of list appends as superscripted  $*$  such as  $s^*$ .
- We denote a fresh variable name as  $\diamond$  and its variants.
- We abuse our notations by mixing semicolon-separated sequences and lists.
- We use the following:
  - `==`, `toObject`, `toNumber`, `isObject`, `iteratorInit`, `iteratorHasNext`, `iteratorNext`, `global`, `getBase`
- To denote an AST-level statement granularity in the translated IR statements, we use `IRStmtUnit` which is represented as green angle brackets  $\langle \rangle$  in this document. To reduce the number of temporary variables, we use global variables to denote constants such as 1 and `true` which is represented in green 1 and `true` in this document.
- We wrap a possibly identical assignment with a box so that the actual implementation, `Translator`, can eliminate identical assignments.



## Chapter 4

# AST to IR

```
 $\Sigma$       : Env
ast2irp  : Program -> IRRoot
ast2irfd : FunDecl -> Env -> IRFunDecl
ast2irvd : VarDecl -> Env -> IRVarStmt
ast2irs  : Stmt -> Env -> IRStmtUnit
ast2ircase : List[Case] * Option[List[Stmt]] * List[Case] -> Env ->
              List[Option[Expr] * IRId] -> IRStmt
ast2irscond : List[Option[Expr] * IRId] -> Env -> IRStmt
ast2irival : Expr -> Env -> List[IRStmt] -> IRExpr -> boolean -> List[IRStmt] * IRExpr
ast2ire    : Expr -> Env -> IRId -> List[IRStmt] * IRExpr
ast2irlhs  : LHS -> Env -> IRId -> List[IRStmt] * IRExpr
ast2irlit  : LIT -> Env -> IRId -> List[IRStmt] * IRExpr
ast2irm    : Member -> Env -> IRId -> List[IRStmt] * IRMember
ast2irpr   : Property -> IRId
```

$$\begin{aligned}
ast2ir_p \llbracket fd^* \quad vd^* \quad s^* \rrbracket &= \langle (ast2ir_{fd} \llbracket fd \rrbracket (\langle \rangle))^* (ast2ir_{vd} \llbracket vd \rrbracket (\langle \rangle))^* (ast2ir_s \llbracket s \rrbracket (\langle \rangle))^* \rangle \\
ast2ir_{fd} \llbracket \text{function } f((x,)^*) \{fd^* vd^* s^*\} \rrbracket (\Sigma) &= \text{function } f(\diamond \text{this}, \diamond \text{arguments}) \{ \\
&\quad (ast2ir_{fd} \llbracket fd \rrbracket (\Sigma))^* \\
&\quad (\text{var } x_i)^* \\
&\quad (ast2ir_{vd} \llbracket vd \rrbracket (\Sigma))^* \\
&\quad (\underline{x_i} = \diamond \text{arguments}["i"])^* \quad \text{where } x_i \text{ is not the name of any of } fd \\
&\quad (ast2ir_s \llbracket s \rrbracket (\Sigma; \diamond \text{this}; \diamond \text{arguments}))^* \}
\end{aligned}$$

A function always receives explicit “this” and “arguments” arguments so that the desugaring of this and arguments is correct. Currently, “arguments” denotes copies of the arguments instead of their aliases. An early exit from a function using return statements is rewritten as a non-local jump to the label  $\diamond \text{return}$ .

$$\begin{aligned}
ast2ir_{vd} \llbracket \text{var } x \rrbracket (\Sigma) &= \text{var } \underline{x} \\
ast2ir_s \llbracket \{s^*\} \rrbracket (\Sigma) &= \langle (ast2ir_s \llbracket s \rrbracket (\Sigma))^* \rangle \\
ast2ir_s \llbracket ; \rrbracket (\Sigma) &= \langle \rangle \\
ast2ir_s \llbracket e; \rrbracket (\Sigma) &= \text{LET } (\underline{s^*}, \underline{e}) = ast2ir_e \llbracket e \rrbracket (\Sigma)(\diamond \_) \\
&\quad \text{IN } \langle \underline{s^*}; \boxed{\underline{\_} = \underline{e}} \rangle
\end{aligned}$$

*Candidate for optimization*

$$\begin{aligned}
ast2ir_s \llbracket \text{if } (e_1 \&\& e_2) \ s_1 \ (\text{else } s_2)^? \rrbracket (\Sigma) &= \text{LET } (\underline{s_1^*}, \underline{e_1}) = ast2ir_e \llbracket e_1 \rrbracket (\Sigma)(\diamond \text{new}_1) \\
&\quad (\underline{s_2^*}, \underline{e_2}) = ast2ir_e \llbracket e_2 \rrbracket (\Sigma)(\diamond \text{new}_2) \\
&\quad \text{IN } \langle \underline{s_1^*}; \\
&\quad \quad \diamond \text{label} : \{ \\
&\quad \quad \quad \text{if } (\underline{e_1}) \\
&\quad \quad \quad \text{then } \langle \underline{s_2^*}; \text{ if } (\underline{e_2}) \text{ then } \{ ast2ir_s \llbracket s_1 \rrbracket (\Sigma); \text{ break } \diamond \text{label} \} \rangle; \\
&\quad \quad \quad (\underline{ast2ir_s \llbracket s_2 \rrbracket (\Sigma)})^? \rangle \}
\end{aligned}$$

*Candidate for optimization*

$$\begin{aligned}
ast2ir_s \llbracket \text{if } (e_1 \mid e_2) \ s_1 \ (\text{else } s_2)^? \rrbracket (\Sigma) &= \text{LET } (\underline{s_1^*}, \underline{e_1}) = ast2ir_e \llbracket e_1 \rrbracket (\Sigma)(\diamond \text{new}_1) \\
&\quad (\underline{s_2^*}, \underline{e_2}) = ast2ir_e \llbracket e_2 \rrbracket (\Sigma)(\diamond \text{new}_2) \\
&\quad \text{IN } \langle \underline{s_1^*}; \\
&\quad \quad \diamond \text{label}_2 : \{ \\
&\quad \quad \quad \diamond \text{label}_1 : \{ \\
&\quad \quad \quad \quad \text{if } (\underline{e_1}) \\
&\quad \quad \quad \quad \text{then break } \diamond \text{label}_1; \underline{s_2^*}; \\
&\quad \quad \quad \quad \text{if } (\underline{e_2}) \text{ then break } \diamond \text{label}_1; \\
&\quad \quad \quad \quad (\underline{ast2ir_s \llbracket s_2 \rrbracket (\Sigma)})^? \diamond \text{label}_2 \\
&\quad \quad \quad \} ; ast2ir_s \llbracket s_1 \rrbracket (\Sigma) \} \rangle
\end{aligned}$$

$$\begin{aligned}
& ast2ir_s \llbracket \text{if } (e) \ s_1 \ (\text{else } s_2)^? \rrbracket (\Sigma) &= \text{LET } (\underline{s}^*, \underline{e}) = ast2ir_e \llbracket e \rrbracket (\Sigma) (\diamond_{\text{new}}) \\
& & \text{IN } \langle \underline{s}^*; \text{if } (\underline{e}) \text{ then } ast2ir_s \llbracket s_1 \rrbracket (\Sigma) \ (\text{else } ast2ir_s \llbracket s_2 \rrbracket (\Sigma))^? \rangle \\
& ast2ir_s \llbracket \text{switch } (e) \ \{ cc_1^* (\text{default} : s^*)^? \ cc_2^* \} \rrbracket (\Sigma) &= \text{LET } (\underline{s}^*, \underline{e}) = ast2ir_e \llbracket e \rrbracket (\Sigma) (\diamond_{\text{val}}) \\
& & \text{IN } \langle \diamond_{\text{break}} : \{ \\
& \quad \underline{s}^*; \ \boxed{\diamond_{\text{val}} = \underline{e};} \\
& \quad ast2ir_{case} \llbracket (\text{rev } cc_2^*) (\underline{s}^*)^? (\text{rev } cc_1^*) \rrbracket (\Sigma; \diamond_{\text{break}}; \diamond_{\text{val}}) \} \rangle \\
& ast2ir_{case} \llbracket (\text{case } e : s_1^* :: cc_2^* (s_2^*)^? \ cc_1^*) \rrbracket (\Sigma) (c^*) &= \langle \diamond_{\text{label}} : \{ ast2ir_{case} \llbracket cc_2^* (s_2^*)^? \ cc_1^* \rrbracket (\Sigma) ((\underline{e}, \diamond_{\text{label}}) :: c^*) \} ; \\
& \quad (ast2ir_s \llbracket s_1 \rrbracket (\Sigma))^* \rangle \\
& ast2ir_{case} \llbracket () \ (s^*)^? \ cc_1^* \rrbracket (\Sigma) (c^*) &= \langle \diamond_{\text{label}} : \{ ast2ir_{case} \llbracket () \ () \ cc_1^* \rrbracket (\Sigma) (c^* @ ((\underline{e}, \diamond_{\text{label}}))) \} ; \\
& \quad ((ast2ir_s \llbracket s \rrbracket (\Sigma))^*)^? \rangle \\
& ast2ir_{case} \llbracket () \ () \ (\text{case } e : s^* :: cc_1^*) \rrbracket (\Sigma) (c^*) &= \langle \diamond_{\text{label}} : \{ ast2ir_{case} \llbracket () \ () \ cc_1^* \rrbracket (\Sigma) ((\underline{e}, \diamond_{\text{label}}) :: c^*) \} ; \\
& \quad (ast2ir_s \llbracket s \rrbracket (\Sigma))^* \rangle \\
& ast2ir_{case} \llbracket () \ () \ () \rrbracket (\Sigma) ((\underline{e}, \underline{l})^*) &= \langle ast2ir_{scond} \llbracket (\underline{e}, \underline{l})^* \rrbracket (\Sigma); \\
& \quad \text{break } \Sigma (\diamond_{\text{break}}) \rangle \\
& ast2ir_{scond} \llbracket (\underline{e}, \underline{l}) :: (c^*) \rrbracket (\Sigma) &= \text{LET } (\underline{s}^*, \underline{e}) = ast2ir_e \llbracket e \rrbracket (\Sigma) (\diamond_{\text{cond}}) \\
& & \text{IN } \langle \underline{s}^*; \\
& \quad \text{if } (\Sigma (\diamond_{\text{val}}) === \underline{e}) \text{ then break } \underline{l} \text{ else } ast2ir_{scond} \llbracket c^* \rrbracket (\Sigma) \rangle \\
& ast2ir_{scond} \llbracket [(), \underline{l}] \rrbracket (\Sigma) &= \langle \text{break } \underline{l} \rangle \\
& ast2ir_{scond} \llbracket () \rrbracket (\Sigma) &= \langle \rangle \\
& \quad \text{Where } c \text{ is either } (\underline{e}, \underline{l}) \text{ or } (), \underline{l}. \\
& ast2ir_s \llbracket \text{do } s \text{ while } (e); \rrbracket (\Sigma) &= \text{LET } (\underline{s}^*, \underline{e}) = ast2ir_e \llbracket e \rrbracket (\Sigma) (\diamond_{\text{new}_1}) \\
& & \text{IN } \langle \diamond_{\text{break}} : \{ \\
& \quad \diamond_{\text{continue}} : \{ ast2ir_s \llbracket s \rrbracket (\Sigma; \diamond_{\text{break}}; \diamond_{\text{continue}}) \} ; \\
& \quad \underline{s}^*; \\
& \quad \text{while } (\underline{e}) \{ \\
& \quad \quad \diamond_{\text{continue}} : \{ ast2ir_s \llbracket s \rrbracket (\Sigma; \diamond_{\text{break}}; \diamond_{\text{continue}}) \} ; \\
& \quad \quad \underline{s}^*; \\
& \quad \} \\
& \} \rangle \\
& ast2ir_s \llbracket \text{while } (e) \ s \rrbracket (\Sigma) &= \text{LET } (\underline{s}^*, \underline{e}) = ast2ir_e \llbracket e \rrbracket (\Sigma) (\diamond_{\text{new}_1}) \\
& & \text{IN } \langle \diamond_{\text{break}} : \{ \\
& \quad \underline{s}^*; \\
& \quad \text{while } (\underline{e}) \{ \\
& \quad \quad \diamond_{\text{continue}} : \{ ast2ir_s \llbracket s \rrbracket (\Sigma; \diamond_{\text{break}}; \diamond_{\text{continue}}) \} ; \\
& \quad \quad \underline{s}^*; \\
& \quad \} \\
& \} \rangle \\
& ast2ir_s \llbracket \text{for } (e_1^?; e_2^?; e_3^?) \ s \rrbracket (\Sigma) &= \text{LET } ((\underline{s}_1^*, \underline{e}_1) = ast2ir_e \llbracket e_1 \rrbracket (\Sigma) (\diamond_{\text{new}_1}))^? \\
& & ((\underline{s}_3^*, \underline{e}_3) = ast2ir_e \llbracket e_3 \rrbracket (\Sigma) (\diamond_{\text{new}_1}))^? \\
& & \text{IN } \langle \diamond_{\text{break}} : \{ \\
& \quad (\underline{s}_1^*; \ \boxed{\underline{e}_1 = \underline{e}_1})^? \\
& \quad \text{while } (\text{true}) \{ \\
& \quad \quad \diamond_{\text{continue}} : \{ ast2ir_s \llbracket s \rrbracket (\Sigma; \diamond_{\text{break}}; \diamond_{\text{continue}}) \} ; \\
& \quad \quad (\underline{s}_3^*; \ \boxed{\underline{e}_3 = \underline{e}_3})^? \\
& \quad \} \\
& \} \rangle \\
& ast2ir_s \llbracket \text{for } (e_1^?; e_2; e_3^?) \ s \rrbracket (\Sigma) &= \text{LET } ((\underline{s}_1^*, \underline{e}_1) = ast2ir_e \llbracket e_1 \rrbracket (\Sigma) (\diamond_{\text{new}_1}))^? \\
& & (\underline{s}_2^*, \underline{e}_2) = ast2ir_e \llbracket e_2 \rrbracket (\Sigma) (\diamond_{\text{new}_2}) \\
& & ((\underline{s}_3^*, \underline{e}_3) = ast2ir_e \llbracket e_3 \rrbracket (\Sigma) (\diamond_{\text{new}_1}))^? \\
& & \text{IN } \langle \diamond_{\text{break}} : \{ \\
& \quad (\underline{s}_1^*; \ \boxed{\underline{e}_1 = \underline{e}_1})^? \\
& \quad \underline{s}_2^*; \\
& \quad \text{while } (\underline{e}_2) \{ \\
& \quad \quad \diamond_{\text{continue}} : \{ ast2ir_s \llbracket s \rrbracket (\Sigma; \diamond_{\text{break}}; \diamond_{\text{continue}}) \} ; \\
& \quad \quad (\underline{s}_3^*; \ \boxed{\underline{e}_3 = \underline{e}_3})^? \\
& \quad \quad \underline{s}_2^*; \\
& \quad \} \\
& \} \rangle
\end{aligned}$$

$ast2ir_s \llbracket \text{for } (lhs \text{ in } e) \ s \rrbracket (\Sigma)$

$ast2ir_s \llbracket \text{continue}; \rrbracket (\Sigma)$   
 $ast2ir_s \llbracket \text{continue } l; \rrbracket (\Sigma)$   
 $ast2ir_s \llbracket \text{break}; \rrbracket (\Sigma)$   
 $ast2ir_s \llbracket \text{break } l; \rrbracket (\Sigma)$   
 $ast2ir_s \llbracket \text{return}; \rrbracket (\Sigma)$   
 $ast2ir_s \llbracket \text{return } e; \rrbracket (\Sigma)$

$ast2ir_s \llbracket \text{with } (e) \ s \rrbracket (\Sigma)$

$ast2ir_s \llbracket l : s \rrbracket (\Sigma)$   
 $ast2ir_s \llbracket \text{throw } e; \rrbracket (\Sigma)$

$ast2ir_s \llbracket \text{try } \{s_1^*\} \{ \text{catch } (x) \{s_2^*\} \}^? (\text{finally } \{s_3^*\}^?) \rrbracket (\Sigma) =$

$ast2ir_s \llbracket \text{debugger}; \rrbracket (\Sigma)$

$ast2ir_{lval} \llbracket (e) \rrbracket (\Sigma)(\underline{s}^*; \underline{e}')(\text{keepOld})$   
 $ast2ir_{lval} \llbracket x \rrbracket (\Sigma)(\underline{s}^*; \underline{e})(\text{keepOld})$

$ast2ir_{lval} \llbracket lhs.x \rrbracket (\Sigma)(\underline{s}^*; \underline{e})(\text{keepOld})$   
 $ast2ir_{lval} \llbracket lhs[e] \rrbracket (\Sigma)(\underline{s}^*; \underline{e}')(\text{keepOld})$

$ast2ir_{lval} \llbracket e \rrbracket (\Sigma)(\underline{s}^*; \underline{e})(\text{keepOld})$

$ast2ir_e \llbracket e_1, e_2 \rrbracket (\Sigma)(\underline{x})$

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$ast2ir_e \llbracket e_a \&\&e_b ? e_2 : e_3 \rrbracket (\Sigma)(\underline{x})$

$= \text{LET } (\underline{s}^*, \underline{e}) = ast2ir_e \llbracket e \rrbracket (\Sigma)(\underline{\diamond new_1})$   
 $\text{IN } \langle \underline{\diamond break} : \{$   
 $\quad \underline{s}^* ;$   
 $\quad \underline{\diamond obj} = \diamond \text{toObject}(\underline{e}) ;$   
 $\quad \underline{\diamond iterator} = \diamond \text{iteratorInit}(\underline{\diamond obj}) ;$   
 $\quad \underline{\diamond cond_1} = \diamond \text{iteratorHasNext}(\underline{\diamond obj}, \underline{\diamond iterator}) ;$   
 $\quad \text{while } (\underline{\diamond cond_1}) \{$   
 $\quad \quad \underline{\diamond key} = \diamond \text{iteratorNext}(\underline{\diamond obj}, \underline{\diamond iterator}) ;$   
 $\quad \quad ast2ir_{lval} \llbracket lhs \rrbracket (\Sigma)(\underline{\diamond key})(\text{false}).1 ;$   
 $\quad \quad \underline{\diamond continue} : \{ ast2ir_s \llbracket s \rrbracket (\Sigma)(\underline{\diamond break}; \underline{\diamond continue}) \} ;$   
 $\quad \quad \underline{\diamond cond_1} = \diamond \text{iteratorHasNext}(\underline{\diamond obj}, \underline{\diamond iterator}) ;$   
 $\quad \quad \}$   
 $\quad \}$   
 $= \langle \text{break } \Sigma(\underline{\diamond continue}) \rangle$   
 $= \langle \text{break } l \rangle$   
 $= \langle \text{break } \Sigma(\underline{\diamond break}) \rangle$   
 $= \langle \text{break } l \rangle$   
 $= \langle \text{return} \rangle$   
 $= \text{LET } (\underline{s}^*, \underline{e}) = ast2ir_e \llbracket e \rrbracket (\Sigma)(\underline{\diamond new_1})$   
 $\text{IN } \langle \underline{s}^* ; \text{return } \underline{e} \rangle$   
 $= \text{LET } (\underline{s}^*, \underline{e}) = ast2ir_e \llbracket e \rrbracket (\Sigma)(\underline{\diamond new_1})$   
 $\text{IN } \langle \underline{s}^* ;$   
 $\quad \underline{\diamond new_2} = \diamond \text{toObject}(\underline{e}) ;$   
 $\quad \text{with } (\underline{\diamond new_2}) \ ast2ir_s \llbracket s \rrbracket (\Sigma) \rangle$   
 $= \langle l : \{ ast2ir_s \llbracket s \rrbracket (\Sigma) \} \rangle$   
 $= \text{LET } (\underline{s}^*, \underline{e}) = ast2ir_e \llbracket e \rrbracket (\Sigma)(\underline{\diamond new_1})$   
 $\text{IN } \langle \underline{s}^* ; \text{throw } \underline{e} \rangle$   
 $= \langle \text{try } \{ (ast2ir_s \llbracket s_1 \rrbracket (\Sigma))^* \}$   
 $\quad (\text{catch } (x) \{ (ast2ir_s \llbracket s_2 \rrbracket (\Sigma))^* \})^?$   
 $\quad (\text{finally } \{ (ast2ir_s \llbracket s_3 \rrbracket (\Sigma))^* \})^? \rangle$   
 $= \langle \rangle$   
 $= ast2ir_{lval} \llbracket e \rrbracket (\Sigma)(\underline{s}^*; \underline{e}')(\text{keepOld})$   
 $= \text{IF keepOld THEN } (\langle \underline{\diamond old} = \underline{x} ; \underline{s}^* ; \underline{x} = \underline{e} \rangle, \underline{x})$   
 $\quad \text{ELSE } \langle \underline{s}^* ; \underline{x} = \underline{e} \rangle$   
 $= ast2ir_{lval} \llbracket lhs["x"] \rrbracket (\Sigma)(\underline{s}^*; \underline{e})(\text{keepOld})$   
 $= \text{LET } (\underline{s}_1^*, \underline{e}_1) = ast2ir_{lval} \llbracket lhs \rrbracket (\Sigma)(\underline{\diamond obj_1})$   
 $\quad (\underline{s}_2^*, \underline{e}_2) = ast2ir_e \llbracket e \rrbracket (\Sigma)(\underline{\diamond field_1})$   
 $\text{IN IF keepOld}$   
 $\quad \text{THEN } (\langle \underline{s}_1^* ; \underline{\diamond obj} = \diamond \text{toObject}(\underline{e}_1) ; \underline{s}_2^* ;$   
 $\quad \quad \underline{\diamond old} = \underline{\diamond obj}[\underline{e}_2] ; \underline{s}^* ; \underline{\diamond obj}[\underline{e}_2] = \underline{e}' \rangle,$   
 $\quad \quad \underline{\diamond obj}[\underline{e}_2])$   
 $\quad \text{ELSE } (\langle \underline{s}_1^* ; \underline{\diamond obj} = \diamond \text{toObject}(\underline{e}_1) ; \underline{s}_2^* ;$   
 $\quad \quad \underline{s}^* ; \underline{\diamond obj}[\underline{e}_2] = \underline{e}' \rangle, \underline{\diamond obj}[\underline{e}_2])$   
 $= \text{Warning: ReferenceError!}$   
 $= \text{LET } (\underline{s}_1^*, \underline{e}_1) = ast2ir_e \llbracket e_1 \rrbracket (\Sigma)(\underline{\diamond y})$   
 $\quad (\underline{s}_2^*, \underline{e}_2) = ast2ir_e \llbracket e_2 \rrbracket (\Sigma)(\underline{x})$   
 $\text{IN } (\underline{s}_1^* ; \underline{\diamond y} = \underline{e}_1 ; \underline{s}_2^*, \underline{e}_2)$   
 $= \text{LET } (\underline{s}_a^*, \underline{e}_a) = ast2ir_e \llbracket e_a \rrbracket (\Sigma)(\underline{\diamond new_a})$   
 $\quad (\underline{s}_b^*, \underline{e}_b) = ast2ir_e \llbracket e_b \rrbracket (\Sigma)(\underline{\diamond new_b})$   
 $\quad (\underline{s}_2^*, \underline{e}_2) = ast2ir_e \llbracket e_2 \rrbracket (\Sigma)(\underline{x})$   
 $\quad (\underline{s}_3^*, \underline{e}_3) = ast2ir_e \llbracket e_3 \rrbracket (\Sigma)(\underline{x})$   
 $\text{IN } (\underline{s}_a^* ;$   
 $\quad \underline{\diamond label} : \{$   
 $\quad \quad \text{if } (\underline{e}_a)$   
 $\quad \quad \text{then } \langle \underline{s}_b^* ; \text{if } (\underline{e}_b) \text{ then } \{ \underline{s}_2^* ; \underline{x} = \underline{e}_2 \} ; \text{break } \underline{\diamond label} \} \rangle ;$   
 $\quad \underline{s}_3^* ; \underline{x} = \underline{e}_3 \rangle, \underline{x})$

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$$\begin{aligned}
ast2ir_e[e_a \mid e_b ? e_2 : e_3](\Sigma)(\underline{x}) &= \text{LET } (\underline{s}_a^*, \underline{e}_a) = ast2ir_e[e_a](\Sigma)(\diamond new_a) \\
&\quad (\underline{s}_b^*, \underline{e}_b) = ast2ir_e[e_b](\Sigma)(\diamond new_b) \\
&\quad (\underline{s}_2^*, \underline{e}_2) = ast2ir_e[e_2](\Sigma)(\underline{x}) \\
&\quad (\underline{s}_3^*, \underline{e}_3) = ast2ir_e[e_3](\Sigma)(\underline{x}) \\
&\quad \text{IN } (\underline{s}_a^*; \\
&\quad \quad \diamond label_2 : \{ \\
&\quad \quad \quad \diamond label_1 : \{ \\
&\quad \quad \quad \quad \text{if } (\underline{e}_a) \\
&\quad \quad \quad \quad \text{then break } \diamond label_1; \underline{s}_b^*; \\
&\quad \quad \quad \quad \text{if } (\underline{e}_b) \text{ then break } \diamond label_1; \\
&\quad \quad \quad \quad \underline{s}_3^*; \underline{x} = \underline{e}_3; \text{ break } \diamond label_2 \\
&\quad \quad \quad \quad \} ; \underline{s}_2^*; \underline{x} = \underline{e}_2 \}, \underline{x}) \\
ast2ir_e[e_1 ? e_2 : e_3](\Sigma)(\underline{x}) &= \text{LET } (\underline{s}_1^*, \underline{e}_1) = ast2ir_e[e_1](\Sigma)(\diamond new_1) \\
&\quad (\underline{s}_2^*, \underline{e}_2) = ast2ir_e[e_2](\Sigma)(\underline{x}) \\
&\quad (\underline{s}_3^*, \underline{e}_3) = ast2ir_e[e_3](\Sigma)(\underline{x}) \\
&\quad \text{IN } (\underline{s}_1^*; \text{if } (\underline{e}_1) \text{ then } \{ \underline{s}_2^*; \underline{x} = \underline{e}_2 \} \text{ else } \{ \underline{s}_3^*; \underline{x} = \underline{e}_3 \}, \underline{x}) \\
ast2ir_e[lhs = e](\Sigma)(\underline{x}) &= \text{LET } (\underline{s}^*, \underline{e}) = ast2ir_e[e](\Sigma)(\underline{x}) \\
&\quad \text{IN } \text{IF } \underline{e} \text{ contains } lhs \\
&\quad \quad \text{THEN } ast2ir_{lval}[lhs](\Sigma)(\underline{s}^*; \underline{e})(\text{false}) \\
&\quad \quad \text{ELSE } (ast2ir_{lval}[lhs](\Sigma)(\underline{s}^*; \underline{e})(\text{false}).1, \underline{e}) \\
ast2ir_e[lhs \odot = e](\Sigma)(\underline{x}) &= \text{LET } (\underline{s}^*, \underline{e}) = ast2ir_e[e](\Sigma)(\diamond y) \\
&\quad \text{IN } (ast2ir_{lval}[lhs](\Sigma)(\underline{s}^*; \diamond old \odot \underline{e})(\text{true}).1, \diamond old \odot \underline{e}) \\
ast2ir_e[++e](\Sigma)(\underline{x}) &= (ast2ir_{lval}[e](\Sigma)(\diamond new = \diamond toNumber(\diamond old); \diamond new + 1)(\text{true}).1, \diamond new + 1) \\
ast2ir_e[--e](\Sigma)(\underline{x}) &= (ast2ir_{lval}[e](\Sigma)(\diamond new = \diamond toNumber(\diamond old); \diamond new - 1)(\text{true}).1, \diamond new - 1) \\
ast2ir_e[delete x](\Sigma)(\underline{y}) &= (\underline{y} = \text{delete } x, \underline{y}) \\
ast2ir_e[delete (x)](\Sigma)(\underline{y}) &= (\underline{y} = \text{delete } x, \underline{y}) \\
ast2ir_e[delete lhs.x](\Sigma)(\underline{y}) &= ast2ir_e[\text{delete } lhs["x"]](\Sigma)(\underline{y}) \\
ast2ir_e[delete lhs[e]](\Sigma)(\underline{x}) &= \text{LET } (\underline{s}_1^*, \underline{e}_1) = ast2ir_{lhs}[lhs](\Sigma)(\diamond obj_1) \\
&\quad (\underline{s}_2^*, \underline{e}_2) = ast2ir_e[e](\Sigma)(\diamond field_1) \\
&\quad \text{IN } (\underline{s}_1^*; \diamond obj = \diamond toObject(\underline{e}_1); \underline{s}_2^*; \\
&\quad \quad \underline{x} = \text{delete } \diamond obj[\underline{e}_2], \underline{x}) \\
ast2ir_e[delete e](\Sigma)(\underline{x}) &= \text{LET } (\underline{s}^*, \underline{e}) = ast2ir_e[e](\Sigma)(\diamond y) \\
&\quad \text{IN } (\underline{s}^*; \diamond \_ = \underline{e}, \text{true}) \\
ast2ir_e[\ominus e](\Sigma)(\underline{x}) &= \text{LET } (\underline{s}^*, \underline{e}) = ast2ir_e[e](\Sigma)(\diamond y) \\
&\quad \text{IN } (\underline{s}^*, \ominus \underline{e}) \\
ast2ir_e[lhs++](\Sigma)(\underline{x}) &= (ast2ir_{lval}[lhs](\Sigma)(\diamond new = \diamond toNumber(\diamond old); \diamond new + 1)(\text{true}).1, \diamond new) \\
ast2ir_e[lhs--](\Sigma)(\underline{x}) &= (ast2ir_{lval}[lhs](\Sigma)(\diamond new = \diamond toNumber(\diamond old); \diamond new - 1)(\text{true}).1, \diamond new)
\end{aligned}$$

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$$\begin{aligned}
ast2ir_e[e_1 \&\& e_2](\Sigma)(\underline{x}) &= \text{LET } (\underline{s}_1^*, \underline{e}_1) = ast2ir_e[e_1](\Sigma)(\diamond y) \\
&\quad (\underline{s}_2^*, \underline{e}_2) = ast2ir_e[e_2](\Sigma)(\diamond z) \\
&\quad \text{IN } (\underline{s}_1^*; \text{if } (\underline{e}_1) \text{ then } \underline{s}_2^*; \underline{x} = \underline{e}_2 \text{ else } \underline{x} = \underline{e}_1, \underline{x})
\end{aligned}$$

*Candidate for optimization*

$$\begin{aligned}
ast2ir_e[e_1 \mid e_2](\Sigma)(\underline{x}) &= \text{LET } (\underline{s}_1^*, \underline{e}_1) = ast2ir_e[e_1](\Sigma)(\diamond y) \\
&\quad (\underline{s}_2^*, \underline{e}_2) = ast2ir_e[e_2](\Sigma)(\diamond z) \\
&\quad \text{IN } (\underline{s}_1^*; \text{if } (\underline{e}_1) \text{ then } \underline{x} = \underline{e}_1 \text{ else } \underline{s}_2^*; \underline{x} = \underline{e}_2, \underline{x})
\end{aligned}$$

*In order to preserve the semantics when the evaluation of  $e_1$  throws an exception, we force to evaluate  $e_1$  before evaluating  $\underline{s}_2^*$  by introducing an assignment " $\diamond new_1 = \underline{e}_1$ " to avoid any side effects by  $\underline{s}_2^*$ . Note that we add the assignment only when  $\underline{s}_2^*$  is not empty for a simple optimization.*

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$$\begin{aligned}
ast2ir_e[e_1 \otimes e_2](\Sigma)(\underline{x}) &= \text{LET } (\underline{s}_1^*, \underline{e}_1) = ast2ir_e[e_1](\Sigma)(\diamond y) \\
&\quad (\underline{s}_2^*, \underline{e}_2) = ast2ir_e[e_2](\Sigma)(\diamond z) \\
&\quad \text{IN } \text{IF } \underline{s}_2^* \text{ is empty} \\
&\quad \quad \text{THEN } (\underline{s}_1^*, \underline{e}_1 \otimes \underline{e}_2) \\
&\quad \quad \text{ELSE } (\underline{s}_1^*; \diamond y = \underline{e}_1; \underline{s}_2^*, \diamond y \otimes \underline{e}_2) \\
ast2ir_e[lhs](\Sigma)(\underline{x}) &= ast2ir_{lhs}[lhs](\Sigma)(\underline{x})
\end{aligned}$$

$$\begin{aligned}
& ast2ir_{lhs} \llbracket lit \rrbracket (\Sigma)(\underline{x}) &= ast2ir_{lit} \llbracket lit \rrbracket (\Sigma)(\underline{x}) \\
& ast2ir_{lhs} \llbracket arguments \rrbracket (\Sigma)(\underline{x}) &= (\langle \rangle, \Sigma(\diamond arguments)) \\
& ast2ir_{lhs} \llbracket x \rrbracket (\Sigma)(\underline{y}) &= (\langle \rangle, \underline{x}) \\
& \text{Candidate for optimization} \\
& ast2ir_{lhs} \llbracket [(e^?, *)^*] \rrbracket (\Sigma)(\underline{x}) &= \text{LET } ((s^*, e) = ast2ir_e \llbracket e \rrbracket (\Sigma)(\diamond elem))^* \\
& & \quad \text{IN } ((s^*; \diamond elem = e)^*; \underline{x} = [( \diamond elem, )^*], \underline{x}) \\
& ast2ir_{lhs} \llbracket [(m,)^*] \rrbracket (\Sigma)(\underline{x}) &= \text{LET } ((s^*, mem) = ast2ir_m \llbracket m \rrbracket (\Sigma)(\diamond member))^* \\
& & \quad \text{IN } ((s^*)^*; \underline{x} = [(mem,)^*], \underline{x}) \\
& ast2ir_{lhs} \llbracket (e) \rrbracket (\Sigma)(\underline{x}) &= ast2ir_e \llbracket e \rrbracket (\Sigma)(\underline{x}) \\
& ast2ir_{lhs} \llbracket function f^? ((x,)^*) \{fd^* vd^* s^*\} \rrbracket (\Sigma)(\underline{y}) &= (\langle \underline{y} = \text{function } f^? (\diamond this, \diamond arguments) \{ \\
& & \quad (ast2ir_{fd} \llbracket fd \rrbracket (\Sigma))^* \\
& & \quad (\text{var } x_i)^* \\
& & \quad (ast2ir_{vd} \llbracket vd \rrbracket (\Sigma))^* \\
& & \quad (\underline{x}_i = \diamond arguments["i"])^* \quad \text{where } x_i \text{ is not the name of any of fd} \\
& & \quad (ast2ir_s \llbracket s \rrbracket (\Sigma; \diamond this; \diamond arguments))^* \} \rangle, \underline{y}) \\
& ast2ir_{lhs} \llbracket lhs.x \rrbracket (\Sigma)(\underline{y}) &= ast2ir_{lhs} \llbracket lhs["x"] \rrbracket (\Sigma)(\underline{y}) \\
& ast2ir_{lhs} \llbracket lhs["x"] \rrbracket (\Sigma)(\underline{y}) &= \text{LET } (s_1^*, e_1) = ast2ir_{lhs} \llbracket lhs \rrbracket (\Sigma)(\diamond obj_1) \\
& & \quad \text{IN } (s_1^*; \diamond obj = \diamond toObject(e_1), \diamond obj["x"]) \\
& ast2ir_{lhs} \llbracket lhs[e] \rrbracket (\Sigma)(\underline{x}) &= \text{LET } (s_1^*, e_1) = ast2ir_{lhs} \llbracket lhs \rrbracket (\Sigma)(\diamond obj_1) \\
& & \quad (s_2^*, e_2) = ast2ir_e \llbracket e \rrbracket (\Sigma)(\diamond field_1) \\
& & \quad \text{IN } (s_1^*; \diamond obj = \diamond toObject(e_1); s_2^*, \diamond obj[e_2]) \\
& \text{Candidate for optimization} \\
& ast2ir_{lhs} \llbracket new lhs((e,)^*) \rrbracket (\Sigma)(\underline{x}) &= \text{LET } (s_l^*, e_l) = ast2ir_{lhs} \llbracket lhs \rrbracket (\Sigma)(\diamond fun_1) \\
& & \quad ((s^*, e) = ast2ir_e \llbracket e \rrbracket (\Sigma)(\diamond y))^* \\
& & \quad \text{IN } (s_l^*; \diamond fun = \diamond toObject(e_l); (s^*; \diamond y = e)^*; \\
& & \quad \quad \diamond arguments = [(\diamond y_i,)^*]; \\
& & \quad \quad \diamond proto = \diamond fun["prototype"]; \\
& & \quad \quad \diamond obj = \{ [ [Prototype]] = \diamond proto \}; \\
& & \quad \quad \diamond newObj = \text{new } \diamond fun(\diamond obj, \diamond arguments); \\
& & \quad \quad \diamond cond = \diamond isObject(\diamond newObj); \\
& & \quad \quad \text{if } (\diamond cond) \text{ then } \underline{x} = \diamond newObj \text{ else } \underline{x} = \diamond obj, \underline{x}) \\
& ast2ir_{lhs} \llbracket new lhs \rrbracket (\Sigma)(\underline{x}) &= \text{LET } (s^*, e) = ast2ir_{lhs} \llbracket lhs \rrbracket (\Sigma)(\diamond fun_1) \\
& & \quad \text{IN } (s^*; \diamond fun = \diamond toObject(e); \\
& & \quad \quad \diamond arguments = []; \\
& & \quad \quad \diamond proto = \diamond fun["prototype"]; \\
& & \quad \quad \diamond obj = \{ [ [Prototype]] = \diamond proto \}; \\
& & \quad \quad \diamond newObj = \text{new } \diamond fun(\diamond obj, \diamond arguments); \\
& & \quad \quad \diamond cond = \diamond isObject(\diamond newObj); \\
& & \quad \quad \text{if } (\diamond cond) \text{ then } \underline{x} = \diamond newObj \text{ else } \underline{x} = \diamond obj, \underline{x})
\end{aligned}$$

$\odot ::= * \mid / \mid \% \mid + \mid - \mid << \mid >> \mid >>> \mid \& \mid ^ \mid |$   
 $\ominus ::= \sim \mid ! \mid + \mid - \mid \text{delete} \mid \text{void} \mid \text{typeof}$   
 $\otimes ::= | \mid \& \mid ^ \mid << \mid >> \mid >>> \mid + \mid - \mid * \mid / \mid \% \mid == \mid != \mid === \mid !== \mid < \mid > \mid <= \mid >= \mid \text{instanceof} \mid \text{in}$

$$\begin{aligned}
& \text{ast2ir}_{lts} \llbracket \text{eval } (e) \rrbracket (\Sigma)(\underline{x}) &= \text{LET } (\underline{s}^*, \underline{e}) = \text{ast2ir}_e \llbracket e \rrbracket (\Sigma)(\diamond \text{new}_1) \\
& \text{ast2ir}_{lts} \llbracket (f) ((e,)^*) \rrbracket (\Sigma)(\underline{x}) &= \text{ast2ir}_{lts} \llbracket f ((e,)^*) \rrbracket (\Sigma)(\underline{x}) \\
& \text{Candidate for optimization} \\
& \text{ast2ir}_{lts} \llbracket f ((e,)^*) \rrbracket (\Sigma)(\underline{x}) &= \text{LET } ((\underline{s}^*, \underline{e}) = \text{ast2ir}_e \llbracket e \rrbracket (\Sigma)(\diamond \underline{y}))^* \\
& & \text{IN } (\diamond \text{obj} = \diamond \text{toObject}(f); (\underline{s}^*; \diamond \underline{y} = \underline{e})^*; \\
& & \quad \diamond \text{arguments} = [(\diamond \underline{y}_i)^*]; \\
& & \quad \diamond \text{fun} = \diamond \text{getBase}(f); \\
& & \quad \underline{x} = \diamond \text{obj}(\diamond \text{fun}, \diamond \text{arguments}), \underline{x}) \\
& \text{ast2ir}_{lts} \llbracket (lhs . x) ((e,)^*) \rrbracket (\Sigma)(\underline{y}) &= \text{ast2ir}_{lts} \llbracket lhs [ "x" ] ((e,)^*) \rrbracket (\Sigma)(\underline{y}) \\
& \text{ast2ir}_{lts} \llbracket lhs . x ((e,)^*) \rrbracket (\Sigma)(\underline{y}) &= \text{ast2ir}_{lts} \llbracket lhs [ "x" ] ((e,)^*) \rrbracket (\Sigma)(\underline{y}) \\
& \text{ast2ir}_{lts} \llbracket (lhs [ e' ] ((e,)^*) \rrbracket (\Sigma)(\underline{x}) &= \text{ast2ir}_{lts} \llbracket lhs [ e' ] ((e,)^*) \rrbracket (\Sigma)(\underline{x}) \\
& \text{Candidate for optimization} \\
& \text{ast2ir}_{lts} \llbracket lhs [ e' ] ((e,)^*) \rrbracket (\Sigma)(\underline{x}) &= \text{LET } (\underline{s}_l^*, \underline{e}_l) = \text{ast2ir}_{lts} \llbracket lhs \rrbracket (\Sigma)(\diamond \text{obj}_1) \\
& & (\underline{s}'^*, \underline{e}') = \text{ast2ir}_e \llbracket e' \rrbracket (\Sigma)(\diamond \text{field}_1) \\
& & ((\underline{s}^*, \underline{e}) = \text{ast2ir}_e \llbracket e \rrbracket (\Sigma)(\diamond \underline{y}))^* \\
& & \text{IN } (\underline{s}_l^*; \diamond \text{obj} = \diamond \text{toObject}(\underline{e}_l); \underline{s}'^*; \\
& & \quad (\underline{s}^*; \diamond \underline{y} = \underline{e})^*; \\
& & \quad \diamond \text{arguments} = [(\diamond \underline{y}_i)^*]; \\
& & \quad \diamond \text{fun} = \diamond \text{toObject}(\diamond \text{obj} [ \underline{e}' ]); \\
& & \quad \underline{x} = \diamond \text{fun}(\diamond \text{obj}, \diamond \text{arguments}), \underline{x}) \\
& \text{Candidate for optimization} \\
& \text{ast2ir}_{lts} \llbracket lhs ((e,)^*) \rrbracket (\Sigma)(\underline{x}) &= \text{LET } (\underline{s}_l^*, \underline{e}_l) = \text{ast2ir}_{lts} \llbracket lhs \rrbracket (\Sigma)(\diamond \text{obj}_1) \\
& & ((\underline{s}^*, \underline{e}) = \text{ast2ir}_e \llbracket e \rrbracket (\Sigma)(\diamond \underline{y}))^* \\
& & \text{IN } (\underline{s}_l^*; \diamond \text{obj} = \diamond \text{toObject}(\underline{e}_l); (\underline{s}^*; \diamond \underline{y} = \underline{e})^*; \\
& & \quad \diamond \text{arguments} = [(\diamond \underline{y}_i)^*]; \\
& & \quad \underline{x} = \diamond \text{obj}(\diamond \text{global}, \diamond \text{arguments}), \underline{x}) \\
& \text{ast2ir}_{lit} \llbracket \text{this} \rrbracket (\Sigma)(\underline{x}) &= (\langle \rangle, \Sigma(\diamond \text{this})) \\
& \text{ast2ir}_{lit} \llbracket \text{null} \rrbracket (\Sigma)(\underline{x}) &= (\langle \rangle, \text{null}) \\
& \text{ast2ir}_{lit} \llbracket \text{true} \rrbracket (\Sigma)(\underline{x}) &= (\langle \rangle, \text{true}) \\
& \text{ast2ir}_{lit} \llbracket \text{false} \rrbracket (\Sigma)(\underline{x}) &= (\langle \rangle, \text{false}) \\
& \text{ast2ir}_{lit} \llbracket \text{num} \rrbracket (\Sigma)(\underline{x}) &= (\langle \rangle, \text{num}) \\
& \text{ast2ir}_{lit} \llbracket \text{str} \rrbracket (\Sigma)(\underline{x}) &= (\langle \rangle, \text{str}) \\
& \text{ast2ir}_{lit} \llbracket \text{reg} \rrbracket (\Sigma) &= \\
& \text{ast2ir}_m \llbracket pr : e \rrbracket (\Sigma)(\underline{y}) &= \text{LET } (\underline{s}^*, \underline{e}) = \text{ast2ir}_e \llbracket e \rrbracket (\Sigma)(\underline{y}) \\
& & \text{IN } (\underline{s}^*, \text{ast2ir}_{pr} \llbracket pr \rrbracket : \underline{e}) \\
& \text{ast2ir}_m \llbracket \text{get } pr () \{ fd^* vd^* s^* \} \rrbracket (\Sigma)(\underline{x}) &= (\langle \rangle, \text{get } \text{ast2ir}_{pr} \llbracket pr \rrbracket (\diamond \text{this}, \diamond \text{arguments}) \{ \\
& & \quad (\text{ast2ir}_{fd} \llbracket fd \rrbracket (\Sigma))^* \\
& & \quad (\text{ast2ir}_{vd} \llbracket vd \rrbracket (\Sigma))^* \\
& & \quad (\text{ast2ir}_s \llbracket s \rrbracket (\Sigma; \diamond \text{this}; \diamond \text{arguments}))^* \}) \\
& \text{ast2ir}_m \llbracket \text{set } pr (x) \{ fd^* vd^* s^* \} \rrbracket (\Sigma)(\underline{y}) &= (\langle \rangle, \text{set } \text{ast2ir}_{pr} \llbracket pr \rrbracket (\diamond \text{this}, \diamond \text{arguments}) \{ \\
& & \quad (\text{ast2ir}_{fd} \llbracket fd \rrbracket (\Sigma))^* \\
& & \quad \text{var } \underline{x} \\
& & \quad (\text{ast2ir}_{vd} \llbracket vd \rrbracket (\Sigma))^* \\
& & \quad \underline{x} = \diamond \text{arguments} [ "0" ]; \quad \text{where } \underline{x} \text{ is not the name of any of } fd \\
& & \quad (\text{ast2ir}_s \llbracket s \rrbracket (\Sigma; \diamond \text{this}; \diamond \text{arguments}))^* \})
\end{aligned}$$

# Chapter 5

## IR Semantics

- Environments in the semantics are references.

### 5.1 Domains

$b \in$	$Bool$	$::=$	$true \mid false$
$n \in$	$Num$	$::=$	$NaN \mid Infinity \mid 0 \mid 1 \mid \dots$
$s \in$	$Str$	$::=$	$"foo" \mid "bar" \mid \dots$
$x, y, z \in$	$Var$	$::=$	$this \mid foo \mid bar \mid \dots$
$p \in$	$PName$	$=$	$Str \cup Var$
$pv \in$	$PVal$	$=$	$\{undefined, null\} \cup Bool \cup Num \cup Str$
$l \in$	$Loc$	$::=$	$\#Global \mid \#ObjProto \mid \#FtnProto \mid \#ArrProto \mid \#StrProto \mid \#BoolProto \mid \#NumProto$ $\mid \#Null \mid l_1 \mid \dots$
$v \in$	$Val$	$=$	$Loc \cup PVal$
$fv \in$	$FVal$	$::=$	$function \underline{f}(\underline{this}, \underline{arguments}) \{ \underline{s} \} \mid get \underline{f}(\underline{this}, \underline{arguments})\{ \underline{s} \} \mid set \underline{f}(\underline{this}, \underline{arguments})\{ \underline{s} \}$

4.2 Language Overview: [Error](#), [EvalError](#), [RangeError](#), [ReferenceError](#), [SyntaxError](#), [TypeError](#) and [URIError](#)

$err \in$	$Error$	$=$	$\{Error, EvalError, RangeError, ReferenceError, SyntaxError, TypeError, URIError\}$
$ve \in$	$ValError$	$=$	$Val \cup Error$

8.6.2 Object Internal Properties and Methods: [Table 8–Internal Properties Common to All Objects](#)

[\[\[Prototype\]\]](#), [\[\[Class\]\]](#), [\[\[Extensible\]\]](#), [\[\[Get\]\]](#), [\[\[GetOwnProperty\]\]](#), [\[\[GetProperty\]\]](#), [\[\[Put\]\]](#), [\[\[CanPut\]\]](#), [\[\[HasProperty\]\]](#), [\[\[Delete\]\]](#), [\[\[DefaultValue\]\]](#), [\[\[DefineOwnProperty\]\]](#)

$o \in$	$Object$	$::=$	$\{[[Class]] : Str,$ $[[Extensible]] : Bool,$ $[[Prototype]] : Loc,$ $@property : PName \mapsto ObjectValue$ $(, [[Code]] : FVal,$ $[[Scope]] : Env)^?\}$
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8.6.1 Property Attributes

$ov \in$	$ObjectValue$	$=$	$DataProp \cup AccessorProp$
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[Table 5–Attributes of a Named Data Property](#): [\[\[Value\]\]](#), [\[\[Writable\]\]](#), [\[\[Enumerable\]\]](#), [\[\[Configurable\]\]](#)

$dp \in$	$DataProp$	$::=$	$\{[[Value]] : Val,$ $[[Writable]] : Bool,$ $[[Enumerable]] : Bool,$ $[[Configurable]] : Bool\}$
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[Table 6–Attributes of a Named Accessor Property](#): [\[\[Get\]\]](#), [\[\[Set\]\]](#), [\[\[Enumerable\]\]](#), [\[\[Configurable\]\]](#)

$ap \in$	$AccessorProp$	$::=$	$\{[[Get]] : Val,$ $[[Set]] : Val,$ $[[Enumerable]] : Bool,$ $[[Configurable]] : Bool\}$
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$sv \in$	$StoreValue$	$::=$	$\{[[Value]] : ValError \cup \{\perp\}, [[Mutable]] : Bool, [[Configurable]] : Bool\}$
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$H, K \in$	$Heap$	$=$	$Loc \xrightarrow{\text{fin}} Object$ $\#Null \notin Dom(H)$
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10.2 Lexical Environments: A Lexical Environment consists of an Environment Record and a possibly null reference to an outer Lexical Environment.

$$A, B \in Env ::= \#Global \mid er :: A$$

10.2.1 Environment Records: An environment record is either a declarative environment record or an object environment record.

$$er \in EnvRec = DeclEnvRec \cup ObjEnvRec$$

10.2.1.1 Declarative Environment Records: A declarative environment record binds the set of identifiers defined by the declarations contained within its scope.

$$\sigma \in DeclEnvRec = Var \xrightarrow{\text{fin}} StoreValue$$

10.2.1.2 Object Environment Records: Each object environment record is associated with an object called its binding object.

$$l \in ObjEnvRec = Loc$$

$$bs \in EnvRec \cup Loc$$

$$bv \in BindingValue = StoreValue \cup ObjectValue$$

$$tb \in ThisBinding = Loc$$

$$(H, A, tb) \in State = Heap \times Env \times ThisBinding$$

### 8.9 The Completion Specification Type

$$ct \in Completion ::= nc \mid ac$$

$$vt \in Val \cup \{\text{empty}\}$$

$$nc \in NormalCompletion ::= Normal(vt)$$

The term “abrupt completion” refers to any completion with a type other than normal.

$$ac \in AbruptCompletion ::= Break(vt, x) \mid Return(vt) \mid Throw(ve)$$

## 5.2 Our Own Helpers

$$UndefVB = (\{[[Value]] : \text{undefined}, [[Writable]] : \text{false}, [[Enumerable]] : \text{false}, [[Configurable]] : \text{false}\}, \#Null)$$

$$isIndex : Str \rightarrow Bool$$

$$isIndex(s) = \begin{cases} \text{false} & \text{if } s \neq ToString(ToUint32(s)) \\ \text{true} & \text{if } s = ToString(ToUint32(s)) \end{cases}$$

$$NewLoc : () \rightarrow Loc$$

$$NewLoc() = l_{new}$$

$$Inherit : Heap \times Loc \times Loc \rightarrow Bool$$

$$Inherit(H, l_1, l_2) = \begin{cases} \text{false} & \text{if } l_1 = \#Null \\ \text{true} & \text{if } l_1 \neq \#Null \wedge l_1 = l_2 \\ Inherit(H, H(l_1).[[Prototype]], l_2) & \text{if } l_1 \neq \#Null \wedge l_1 \neq l_2 \end{cases}$$

### 11.4.3 The typeof Operator

$$TypeTag : Heap \times Val \rightarrow Str$$

$$TypeTag(H, v) = \begin{cases} \text{"undefined"} & \text{if } v = \text{undefined} \\ \text{"object"} & \text{if } v = \text{null} \\ \text{"boolean"} & \text{if } v \in Bool \\ \text{"number"} & \text{if } v \in Num \\ \text{"string"} & \text{if } v \in Str \\ \text{"object"} & \text{if } v \in Loc \wedge \neg IsCallable(H, v) \\ \text{"function"} & \text{if } v \in Loc \wedge IsCallable(H, v) \end{cases}$$

### 10.4.3 Entering Function Code

$$GetThis : Heap \times Val \rightarrow Heap \times Loc$$

$$GetThis(H, v) = \begin{cases} (H, \#Global) & \text{if } v = \text{undefined} \vee v = \text{null} \\ ToObject(H, v) & \text{if } v \in Bool \cup Num \cup Str \\ (H, v) & \text{if } v \in Loc \end{cases}$$

$$ParamsSize : FVal \rightarrow Num$$

$$ParamsSize(fv) = |s_{params}| \quad \text{where } fv = \_ f(\underline{this}, \underline{arguments}) \quad \{s_{params} \ s_{vds} \ s_{fds} \ s_{stmts}\}$$

$$GetBody : FVal \rightarrow Stmt$$

$$GetBody(fv) = \underline{s} \quad \text{where } fv = \_ f(\underline{this}, \underline{arguments}) \quad \{s\}$$

### 15.4 Array Objects

$IsArrayIndex : Val \rightarrow Bool$

$$IsArrayIndex(v) = \begin{cases} \text{true} & \text{if } ToString(ToUnit32(ToString(v))) = ToString(v) \wedge ToUnit32(ToString(v)) \neq 2^{32} - 1 \\ \text{false} & \text{otherwise} \end{cases}$$

### 15.9 Date Objects

$IsDate : Heap \times Val \rightarrow Bool$

$$IsDate(H, v) = \begin{cases} \text{true} & \text{if } v \in Loc \wedge H(v).[[\text{Class}]] = \text{"Date"} \\ \text{false} & \text{otherwise} \end{cases}$$

### 12.6.4 The for-in Statement

$IteratorInit : \wp(PName) \rightarrow Object$

$$IteratorInit(P) = NewObj().@property["length" \mapsto n, "@i" \mapsto 0, "0" \mapsto pn_0, \dots, "n-1" \mapsto pn_{n-1}] \\ \text{where } P = \{pn_0, \dots, pn_{n-1}\}$$

$$CollectProps(H, l) = \begin{cases} Dom(H(l).@property) \cup CollectProps(H, H(l).[[Prototype]]) & \text{if } l \in Dom(H) \\ \{\} & \text{if } l \notin Dom(H) \end{cases}$$

$IsEnumerable : Heap \times Loc \times PName \rightarrow Bool$

$$IsEnumerable(H, l, x) = \begin{cases} H(l).@property(x).[[Enumerable]] & \text{if } l \in Dom(H) \wedge x \in Dom(H(l)) \\ IsEnumerable(H, H(l).[[Prototype]], x) & \text{if } l \in Dom(H) \wedge x \notin Dom(H(l)) \\ \text{false} & \text{if } l \notin Dom(H) \end{cases}$$

$Next : Heap \times Object \times Num \times Loc \rightarrow Num$

$$Next(H, o, n, l) = \begin{cases} n & \text{if } n \notin Dom(o) \wedge n \geq o.@property("length") \\ Next(H, o, n+1, l) & \text{if } n \notin Dom(o) \wedge n < o.@property("length") \\ n & \text{if } n \in Dom(o) \wedge IsEnumerable(H, l, o.@property(n)) \\ Next(H, o, n+1, l) & \text{if } n \in Dom(o) \wedge \neg IsEnumerable(H, l, o.@property(n)) \end{cases}$$

$Negate : Num \rightarrow Num$

$$Negate(n) = \begin{cases} NaN & \text{if } n = NaN \\ 0 - n & \text{otherwise} \end{cases}$$

$Negate : Bool \rightarrow Bool$

$$Negate(b) = \begin{cases} \text{false} & \text{if } b = \text{true} \\ \text{true} & \text{otherwise} \end{cases}$$

$ExnLoc : ValError \rightarrow Val$

$$ExnLoc(ve) = \begin{cases} \#Error & \text{if } ve = Error \\ \#EvalError & \text{if } ve = EvalError \\ \#RangeError & \text{if } ve = RangeError \\ \#ReferenceError & \text{if } ve = ReferenceError \\ \#SyntaxError & \text{if } ve = SyntaxError \\ \#TypeError & \text{if } ve = TypeError \\ \#URIError & \text{if } ve = URIError \\ v & \text{if } ve \in Val \end{cases}$$

## 5.3 Helpers from the Specification

### 8.7 The Reference Specification Type

#### 8.7.2 PutValue(V, W)

$PutValue : Heap \times Env \times Var \times Val \times \text{strict} \rightarrow Heap \times Env \times ValError$

$$PutValue(H, A, x, v, b) = \begin{cases} (H, A, ReferenceError) & \text{if } Lookup(H, A, x, \text{strict}) = l \wedge l = \#Null \wedge b \\ Put(H, A, \#Global, x, v, \text{false}) & \text{if } Lookup(H, A, x, \text{strict}) = l \wedge l = \#Null \wedge \neg b \\ Put(H, A, l, x, v, b) & \text{if } Lookup(H, A, x, \text{strict}) = l \wedge l \neq \#Null \\ SetBindingDER(H, A, x, v, b) & \text{if } Lookup(H, A, x, \text{strict}) = \sigma \end{cases}$$

For primitive base values, see 8.7.2.

8.12.1  $[[\text{GetOwnProperty}]](P) : \text{Let } X \text{ be } O\text{'s own property named } P. x \in \text{Dom}(H(l))$

$$\text{Dom}(o) = \{ x \mid x \mapsto ov \in o.\text{@property} \}$$

8.12.1  $[[\text{GetOwnProperty}]](P) : \text{A String object has a more elaborate } [[\text{GetOwnProperty}]] \text{ internal method (15.5.5.2).}$

$\text{GetOwnProperty} : \text{Heap} \times \text{Loc} \times \text{PName} \rightarrow \text{ObjectValue} \times \text{Loc}$

$$\text{GetOwnProperty}(H, l, x) = \begin{cases} \text{UndefVB} & \text{if } l \notin \text{Dom}(H) \\ \text{UndefVB} & \text{if } l \in \text{Dom}(H) \wedge x \notin \text{Dom}(H(l)) \\ (\text{copy}(H(l).\text{@property}(x)), l) & \text{if } l \in \text{Dom}(H) \wedge x \in \text{Dom}(H(l)) \end{cases}$$

## 8.12 Algorithms for Object Internal Methods

8.12.2  $[[\text{GetProperty}]](P)$

$\text{GetProperty} : \text{Heap} \times \text{Loc} \times \text{PName} \rightarrow \text{ObjectValue} \times \text{Loc}$

$$\text{GetProperty}(H, l, x) = \begin{cases} \text{UndefVB} & \text{if } l \notin \text{Dom}(H) \\ \text{UndefVB} & \text{if } l \in \text{Dom}(H) \wedge x \notin \text{Dom}(H(l)) \wedge H(l).[[\text{Prototype}]] = \# \text{Null} \\ \text{GetProperty}(H, H(l).[[\text{Prototype}]], x) & \text{if } l \in \text{Dom}(H) \wedge x \notin \text{Dom}(H(l)) \wedge H(l).[[\text{Prototype}]] \neq \# \text{Null} \\ \text{GetOwnProperty}(H, l, x) & \text{if } l \in \text{Dom}(H) \wedge x \in \text{Dom}(H(l)) \end{cases}$$

8.12.3  $[[\text{Get}]](P) \ H(l).[[\text{Get}]](P)$

$\text{Get} : \text{Heap} \times \text{Loc} \times \text{PName} \rightarrow \text{Val}$

$$\text{Get}(H, l, x) = \begin{cases} \text{undefined} & \text{if } \text{GetProperty}(H, l, x) = \text{UndefVB} \\ dp. [[\text{Value}]] & \text{if } \text{GetProperty}(H, l, x) = (dp, \_) \\ \text{undefined} & \text{if } \text{GetProperty}(H, l, x) = (ap, \_) \wedge ap. [[\text{Get}]] = \text{undefined} \\ ap. [[\text{Get}]]. [[\text{Call}]](H(l), []) & \text{if } \text{GetProperty}(H, l, x) = (ap, \_) \wedge ap. [[\text{Get}]] \neq \text{undefined} \end{cases}$$

8.12.4  $[[\text{CanPut}]](P)$

$\text{CanPut} : \text{Heap} \times \text{Loc} \times \text{PName} \rightarrow \text{Bool}$

$$\text{CanPut}(H, l, x) = \begin{cases} \text{false} & \text{if } \text{GetOwnProperty}(H, l, x) = (ap, \_) \wedge ap. [[\text{Set}]] = \text{undefined} \\ \text{true} & \text{if } \text{GetOwnProperty}(H, l, x) = (ap, \_) \wedge ap. [[\text{Set}]] \neq \text{undefined} \\ dp. [[\text{Writable}]] & \text{if } \text{GetOwnProperty}(H, l, x) = (dp, \_) \\ H(l). [[\text{Extensible}]] & \text{if } \text{GetOwnProperty}(H, l, x) = \text{UndefVB} \wedge H(l). [[\text{Prototype}]] = \# \text{Null} \\ H(l). [[\text{Extensible}]] & \text{if } \text{GetOwnProperty}(H, l, x) = \text{UndefVB} \wedge H(l). [[\text{Prototype}]] \neq \# \text{Null} \wedge \\ & \text{GetProperty}(H, l, x) = \text{UndefVB} \\ \text{false} & \text{if } \text{GetOwnProperty}(H, l, x) = \text{UndefVB} \wedge H(l). [[\text{Prototype}]] \neq \# \text{Null} \wedge \\ & \text{GetProperty}(H, l, x) = (ap, \_) \wedge ap. [[\text{Set}]] = \text{undefined} \\ \text{true} & \text{if } \text{GetOwnProperty}(H, l, x) = \text{UndefVB} \wedge H(l). [[\text{Prototype}]] \neq \# \text{Null} \wedge \\ & \text{GetProperty}(H, l, x) = (ap, \_) \wedge ap. [[\text{Set}]] \neq \text{undefined} \\ \text{false} & \text{if } \text{GetOwnProperty}(H, l, x) = \text{UndefVB} \wedge H(l). [[\text{Prototype}]] \neq \# \text{Null} \wedge \\ & \text{GetProperty}(H, l, x) = (dp, \_) \wedge \neg H(l). [[\text{Extensible}]] \\ dp. [[\text{Writable}]] & \text{if } \text{GetOwnProperty}(H, l, x) = \text{UndefVB} \wedge H(l). [[\text{Prototype}]] \neq \# \text{Null} \wedge \\ & \text{GetProperty}(H, l, x) = (dp, \_) \wedge H(l). [[\text{Extensible}]] \end{cases}$$

8.12.5  $[[\text{Put}]](P, V, \text{Throw})$

$\text{Put} : \text{Heap} \times \text{Env} \times \text{Loc} \times \text{PName} \times \text{Val} \times \text{Bool} \rightarrow \text{Heap} \times \text{Env} \times \text{ValError}$

$$\text{Put}(H, A, l, x, v, b) = \begin{cases} (H, A, \text{TypeError}) & \text{if } \neg \text{CanPut}(H, l, x) \wedge b \\ (H, A, v) & \text{if } \neg \text{CanPut}(H, l, x) \wedge \neg b \\ \text{DefineOwnProperty}(H, A, l, x, dp', b) & \text{if } \text{CanPut}(H, l, x) \wedge \\ & \text{GetOwnProperty}(H, l, x) = (dp, \_) \neq \text{UndefVB} \wedge \\ & dp' = \{ [[\text{Value}]] : v \} \\ ap. [[\text{Set}]]. [[\text{Call}]](H(l), v) & \text{if } \text{CanPut}(H, l, x) \wedge \text{GetOwnProperty}(H, l, x) \neq (dp, \_) \wedge \\ & \text{GetProperty}(H, l, x) = (ap, \_) \\ \text{DefineOwnProperty}(H, A, l, x, dp', b) & \text{if } \text{CanPut}(H, l, x) \wedge \text{GetOwnProperty}(H, l, x) \neq (dp, \_) \wedge \\ & \text{GetProperty}(H, l, x) = (dp, \_) \wedge \\ & dp' = \{ [[\text{Value}]] : v, [[\text{Writable}]] : \text{true}, \\ & \quad [[\text{Enumerable}]] : \text{true}, [[\text{Configurable}]] : \text{true} \} \end{cases}$$

### 8.12.6 [[HasProperty]] (P)

$HasProperty : Heap \times Loc \times PName \rightarrow Bool$   
 $HasProperty(H, l, x) = \begin{cases} false & \text{if } GetProperty(H, l, x) = Undefined \\ true & \text{if } GetProperty(H, l, x) \neq Undefined \end{cases}$

### 10.2.1.1.5 DeleteBinding (N)

### 10.2.1.2.5 DeleteBinding (N)

$DeleteBinding : Heap \times Env \times Str \times strict \rightarrow Heap \times Env \times (Bool \cup Error)$   
 $DeleteBinding(H, A, s, b) = \begin{cases} (H, A, true) & \text{if } A = \#Global \wedge s \notin Dom(H(\#Global)) \\ Delete(H, A, \#Global, s, b) & \text{if } A = \#Global \wedge s \in Dom(H(\#Global)) \\ (H, (\sigma - s) :: A', true) & \text{if } A = \sigma :: A' \wedge s \in Dom(\sigma) \wedge \sigma(s).[[Configurable]] \\ (H, A, false) & \text{if } A = \sigma :: A' \wedge s \in Dom(\sigma) \wedge \neg \sigma(s).[[Configurable]] \\ (H', \sigma :: A'', ve) & \text{if } A = \sigma :: A' \wedge s \notin Dom(\sigma) \wedge \\ & DeleteBinding(H, A', s, b) = (H', A'', ve) \\ Delete(H, A, l, s, b) & \text{if } A = l :: A' \wedge s \in Dom(H(l)) \\ (H', l :: A'', ve) & \text{if } A = l :: A' \wedge s \notin Dom(H(l)) \wedge \\ & DeleteBinding(H, A', s, b) = (H', A'', ve) \end{cases}$

### 8.12.7 [[Delete]] (P, Throw)

$Delete : Heap \times Env \times Loc \times Str \times Bool \rightarrow Heap \times Env \times ValError$   
 $Delete(H, A, l, s, b) = \begin{cases} (H, A, true) & \text{if } GetOwnProperty(H, l, s) = Undefined \\ (H', A, true) & \text{if } GetOwnProperty(H, l, s) = (ov, -) \wedge \\ & ov. [[Configurable]] \wedge \\ & H' = H[l \mapsto H(l) - s] \\ (H, A, TypeError) & \text{if } GetOwnProperty(H, l, s) = (ov, -) \wedge \neg ov. [[Configurable]] \wedge b \\ (H, A, false) & \text{otherwise} \end{cases}$

Less precise but simpler!

### 8.12.8 [[DefaultValue]] (hint)

$DefaultValue : Heap \times Loc \times Str \rightarrow PVal \cup Error$   
 $DefaultValue(H, l, String) = \begin{cases} s & \text{if } "H(l)" = s \wedge s \in PVal \\ v & \text{if } "H(l)" \notin PVal \wedge valueOf(H(l)) = v \wedge v \in PVal \\ TypeError & \text{otherwise} \end{cases}$   
 $DefaultValue(H, l, Number) = \begin{cases} v & \text{if } valueOf(H(l)) = v \wedge v \in PVal \\ s & \text{if } valueOf(H(l)) \notin PVal \wedge "H(l)" = s \wedge s \in PVal \\ TypeError & \text{otherwise} \end{cases}$

Precise but too complicated!

### 8.12.8 [[DefaultValue]] (hint)

$DefaultValue : Heap \times Loc \times Str \rightarrow PVal \cup Error$   
 $DefaultValue(H, l, String) = \begin{cases} s & \text{if } Get(H, l, toString) = v \wedge IsCallable(H, v) \wedge v. [[Call]](H(l), []) = s \wedge s \in PVal \\ v'' & \text{if } Get(H, l, toString) = v \wedge (\neg IsCallable(H, v) \vee v. [[Call]](H(l), []) \notin PVal) \wedge \\ & Get(H, l, valueOf) = v' \wedge IsCallable(H, v') \wedge v'. [[Call]](H(l), []) = v'' \wedge v'' \in PVal \\ TypeError & \text{if } Get(H, l, toString) = v \wedge (\neg IsCallable(H, v) \vee v. [[Call]](H(l), []) \notin PVal) \wedge \\ & Get(H, l, valueOf) = v' \wedge (\neg IsCallable(H, v') \vee v'. [[Call]](H(l), []) \notin PVal) \end{cases}$   
 $DefaultValue(H, l, Number) = \begin{cases} v' & \text{if } Get(H, l, valueOf) = v \wedge IsCallable(H, v) \wedge v. [[Call]](H(l), []) = v' \wedge v' \in PVal \\ s & \text{if } Get(H, l, valueOf) = v \wedge (\neg IsCallable(H, v) \vee v. [[Call]](H(l), []) \notin PVal) \wedge \\ & Get(H, l, toString) = v' \wedge IsCallable(H, v') \wedge v'. [[Call]](H(l), []) = s \wedge s \in PVal \\ TypeError & \text{if } Get(H, l, valueOf) = v \wedge (\neg IsCallable(H, v) \vee v. [[Call]](H(l), []) \notin PVal) \wedge \\ & Get(H, l, toString) = v' \wedge (\neg IsCallable(H, v') \vee v'. [[Call]](H(l), []) \notin PVal) \end{cases}$

### 8.12.9 [[DefineOwnProperty]] (P, Desc, Throw)

*DefineOwnProperty* :  $\text{Heap} \times \text{Env} \times \text{Loc} \times \text{Var} \times \text{ObjectValue} \times \text{Bool} \rightarrow \text{Heap} \times \text{Env} \times \text{ValError}$

*DefineOwnProperty*( $H, A, l, x, ov, b$ )=

<b>Step 3</b>	
( $H, A, \text{TypeError}$ )	if $\text{GetOwnProperty}(H, l, x) = \text{UndefVB} \wedge \neg H(l).[[\text{Extensible}]] \wedge b$
( $H, A, \text{false}$ )	if $\text{GetOwnProperty}(H, l, x) = \text{UndefVB} \wedge \neg H(l).[[\text{Extensible}]] \wedge \neg b$
<b>Step 4</b>	
( $H[l \mapsto H(l).@property[x \mapsto \text{copy}(ov)]]$ , $A, \text{true}$ )	if $\text{GetOwnProperty}(H, l, x) = \text{UndefVB} \wedge H(l).[[\text{Extensible}]]$
<b>Steps 5&amp;6</b>	
( $H, A, \text{true}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge (ov = \emptyset \vee ov \subseteq ov')$
<b>Step 7-a</b>	
( $H, A, \text{TypeError}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge \neg ov'.[[\text{Configurable}]] \wedge$ $ov. [[\text{Configurable}]] \wedge b$
( $H, A, \text{false}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge \neg ov'. [[\text{Configurable}]] \wedge$ $ov. [[\text{Configurable}]] \wedge \neg b$
<b>Step 7-b</b>	
( $H, A, \text{TypeError}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge \neg ov'. [[\text{Configurable}]] \wedge$ $ov. [[\text{Enumerable}]] \neq ov'. [[\text{Enumerable}]] \wedge b$
( $H, A, \text{false}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge \neg ov'. [[\text{Configurable}]] \wedge$ $ov. [[\text{Enumerable}]] \neq ov'. [[\text{Enumerable}]] \wedge \neg b$
<b>Step 9-a</b>	
( $H, A, \text{TypeError}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge ov \in \text{DataProp} \wedge ov' \in \text{AccProp} \wedge$ $\neg ov'. [[\text{Configurable}]] \wedge b$
( $H, A, \text{false}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge ov \in \text{DataProp} \wedge ov' \in \text{AccProp} \wedge$ $\neg ov'. [[\text{Configurable}]] \wedge \neg b$
( $H, A, \text{TypeError}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge ov \in \text{AccProp} \wedge ov' \in \text{DataProp} \wedge$ $\neg ov'. [[\text{Configurable}]] \wedge b$
( $H, A, \text{false}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge ov \in \text{AccProp} \wedge ov' \in \text{DataProp} \wedge$ $\neg ov'. [[\text{Configurable}]] \wedge \neg b$
<b>Step 9-b-i</b>	
( $H[l \mapsto H(l).@property[x \mapsto \text{copy}(ov)]]$ , $A, \text{true}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge ov \in \text{AccProp} \wedge ov' \in \text{DataProp}$
<b>Step 9-c-i</b>	
( $H[l \mapsto H(l).@property[x \mapsto \text{copy}(ov)]]$ , $A, \text{true}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge ov \in \text{DataProp} \wedge ov' \in \text{AccProp}$
<b>Step 10-a-i</b>	
( $H, A, \text{TypeError}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge ov \in \text{DataProp} \wedge ov' \in \text{DataProp} \wedge$ $\neg ov'. [[\text{Configurable}]] \wedge \neg ov'. [[\text{Writable}]] \wedge ov. [[\text{Writable}]] \wedge b$
( $H, A, \text{false}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge ov \in \text{DataProp} \wedge ov' \in \text{DataProp} \wedge$ $\neg ov'. [[\text{Configurable}]] \wedge \neg ov'. [[\text{Writable}]] \wedge ov. [[\text{Writable}]] \wedge \neg b$
<b>Step 10-a-ii</b>	
( $H, A, \text{TypeError}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge ov \in \text{DataProp} \wedge ov' \in \text{DataProp} \wedge$ $\neg ov'. [[\text{Configurable}]] \wedge \neg ov'. [[\text{Writable}]] \wedge ov. [[\text{Value}]] \neq ov'. [[\text{Value}]] \wedge b$
( $H, A, \text{false}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge ov \in \text{DataProp} \wedge ov' \in \text{DataProp} \wedge$ $\neg ov'. [[\text{Configurable}]] \wedge \neg ov'. [[\text{Writable}]] \wedge ov. [[\text{Value}]] \neq ov'. [[\text{Value}]] \wedge \neg b$
<b>Step 10-b</b>	
( $H[l \mapsto H(l).@property[x \mapsto \text{copy}(ov)]]$ , $A, \text{true}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge ov \in \text{DataProp} \wedge ov' \in \text{DataProp} \wedge$ $ov'. [[\text{Configurable}]]$
<b>Step 11-a-i</b>	
( $H, A, \text{TypeError}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge ov \in \text{AccProp} \wedge ov' \in \text{AccProp} \wedge$ $\neg ov'. [[\text{Configurable}]] \wedge ov'. [[\text{Set}]] \neq ov. [[\text{Set}]] \wedge b$
( $H, A, \text{false}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge ov \in \text{AccProp} \wedge ov' \in \text{AccProp} \wedge$ $\neg ov'. [[\text{Configurable}]] \wedge ov'. [[\text{Set}]] \neq ov. [[\text{Set}]] \wedge \neg b$
<b>Step 11-a-ii</b>	
( $H, A, \text{TypeError}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge ov \in \text{AccProp} \wedge ov' \in \text{AccProp} \wedge$ $\neg ov'. [[\text{Configurable}]] \wedge ov'. [[\text{Get}]] \neq ov. [[\text{Get}]] \wedge b$
( $H, A, \text{false}$ )	if $\text{GetOwnProperty}(H, l, x) = (ov', -) \wedge ov \in \text{AccProp} \wedge ov' \in \text{AccProp} \wedge$ $\neg ov'. [[\text{Configurable}]] \wedge ov'. [[\text{Get}]] \neq ov. [[\text{Get}]] \wedge \neg b$
<b>Step 12</b>	
( $H[l \mapsto H(l).@property[x \mapsto \text{copy}(ov)]]$ , $A, \text{true}$ )	otherwise

For Array objects, see 15.4.5.1.

$DeleteArray : Heap \times Env \times Loc \times Num \times Num \times ObjectValue \times Bool \times Bool \rightarrow Heap \times Env \times (Bool \cup Error)$

$ov' = ov. \{ [[Value]] \mapsto oldLen \}$

$ov'' = ov'. \{ [[Writable]] \mapsto false \}$

$DeleteArray(H, A, l, newLen, oldLen, ov, b, b') =$

$\left\{ \begin{array}{ll} \text{Step 3.l} & (H, A, true) \quad \text{if } newLen \geq oldLen \\ \text{Step 3.l.ii} & (H, A, err) \quad \text{if } newLen < oldLen \wedge DeleteBinding(H, A, ToString(H, oldLen - 1), false) = (H', A', err) \\ \text{Step 3.l.iii / writable = true / DefineOwnProperty = err} & (H, A, err) \quad \text{if } newLen < oldLen \wedge DeleteBinding(H, A, ToString(H, oldLen - 1), false) = (H', A', false) \\ & \quad \wedge b = true \wedge DefineOwnProperty(H', A', l, "length", ov', false) = (H'', A'', err) \\ \text{Step 3.l.iii / writable = true / DefineOwnProperty} \neq err & (H, A, \text{if } b' \text{ TypeError else false}) \quad \text{if } newLen < oldLen \wedge DeleteBinding(H, A, ToString(H, oldLen - 1), false) = (H', A', false) \\ & \quad \wedge b = true \wedge DefineOwnProperty(H', A', l, "length", ov', false) = (H'', A'', v) \\ \text{Step 3.l.iii / writable = false / DefineOwnProperty = err} & (H, A, err) \quad \text{if } newLen < oldLen \wedge DeleteBinding(H, A, ToString(H, oldLen - 1), false) = (H', A', false) \\ & \quad \wedge b = false \wedge DefineOwnProperty(H', A', l, "length", ov'', false) = (H'', A'', err) \\ \text{Step 3.l.iii / writable = false / DefineOwnProperty} \neq err & (H, A, \text{if } b' \text{ TypeError else false}) \quad \text{if } newLen < oldLen \wedge DeleteBinding(H, A, ToString(H, oldLen - 1), false) = (H', A', false) \\ & \quad \wedge b = false \wedge DefineOwnProperty(H', A', l, "length", ov'', false) = (H'', A'', v) \\ \text{Step 3.l.ii} & DeleteArray(H', A', l, newLen, \quad \text{if } newLen < oldLen \wedge DeleteBinding(H, A, ToString(H, oldLen - 1), false) = (H', A', true) \\ & \quad oldLen - 1, ov, b) \end{array} \right.$

#### 15.4.5.1 [[DefineOwnProperty]] (P, Desc, Throw) for Array

$DefineOwnPropertyArray : Heap \times Env \times Loc \times Var \times ObjectValue \times Bool \rightarrow Heap \times Env \times (Bool \cup Error)$

$DefineOwnPropertyArray(H, A, l, x, ov, b) =$

where

$index = ToUint32(H, x)$   
 $newLenDesc = copy(ov)$   
 $newLen = ToUint32(ov. [[Value]])$   
 $newLenDesc' = newLenDesc \{ [[Value]] \mapsto newLen \}$   
 $newLenDesc'' = newLenDesc' \{ [[Writable]] \mapsto true \}$   
 $newLenNum = ToNumber(H, ov. [[Value]])$   
 $oldLenDesc = GetOwnProperty(H, l, "length")$   
 $oldLen = oldLenDesc. [[Value]]$   
 $oldLenDesc' = oldLenDesc \{ [[Value]] \mapsto index + 1 \}$

$\left\{ \begin{array}{ll} \text{Step 3.a} & DefineOwnProperty(H, A, l, "length", ov, b) \quad \text{if } ToString(H, x) = "length" \wedge [[Value]] \notin ov \\ \text{Step 3.d} & (H, A, RangeError) \quad \text{if } ToString(H, x) = "length" \wedge [[Value]] \in ov \wedge newLen \neq newLenNum \\ \text{Step 3.f.i} & DefineOwnProperty(H, A, l, "length", \quad \text{if } ToString(H, x) = "length" \wedge [[Value]] \in ov \wedge newLen = newLenNum \\ & \quad newLenDesc', b) \quad \quad \quad \wedge newLen \geq oldLen \\ \text{Step 3.g} & (H, A, \text{if } b \text{ TypeError else false}) \quad \text{if } ToString(H, x) = "length" \wedge [[Value]] \in ov \wedge newLen = newLenNum \\ & \quad \quad \quad \wedge newLen < oldLen \wedge \neg oldLenDesc. [[Writable]] \\ \text{Step 3.h : set newWritable = true \& 3.j} & (H', A', err) \quad \text{if } ToString(H, x) = "length" \wedge [[Value]] \in ov \wedge newLen = newLenNum \\ & \quad \quad \quad \wedge newLen < oldLen \wedge oldLenDesc. [[Writable]] \\ & \quad \quad \quad \wedge ([[Writable]] \notin newLenDesc \vee newLenDesc. [[Writable]]) \\ & \quad \quad \quad \wedge DefineOwnProperty(H, A, l, "length", newLenDesc', b) = (H', A', err) \\ \text{Step 3.h : set newWritable = true \& 3.k} & (H', A', false) \quad \text{if } ToString(H, x) = "length" \wedge [[Value]] \in ov \wedge newLen = newLenNum \\ & \quad \quad \quad \wedge newLen < oldLen \wedge oldLenDesc. [[Writable]] \\ & \quad \quad \quad \wedge ([[Writable]] \notin newLenDesc \vee newLenDesc. [[Writable]]) \\ & \quad \quad \quad \wedge DefineOwnProperty(H, A, l, "length", newLenDesc', b) = (H', A', false) \end{array} \right.$

<p>Step 3.h : set newWritable = true &amp; 3.l (H'', A'', err)</p>	<p>if ToString(H, x) = "length" <math>\wedge</math> [[Value]] <math>\in</math> ov <math>\wedge</math> newLen = newLenNum  <math>\wedge</math> newLen &lt; oldLen <math>\wedge</math> oldLenDesc.[[Writable]]  <math>\wedge</math> ([[Writable]] <math>\notin</math> newLenDesc <math>\vee</math> newLenDesc.[[Writable]])  <math>\wedge</math> DefineOwnProperty(H, A, l, "length", newLenDesc', b) = (H', A', true)  <math>\wedge</math> DeleteArray(H', A', l, newLen, oldLen, newLenDesc', true, b) = (H'', A'', err)</p>
<p>Step 3.h : set newWritable = true &amp; 3.l (H'', A'', if b TypeError else false)</p>	<p>if ToString(H, x) = "length" <math>\wedge</math> [[Value]] <math>\in</math> ov <math>\wedge</math> newLen = newLenNum  <math>\wedge</math> newLen &lt; oldLen <math>\wedge</math> oldLenDesc.[[Writable]]  <math>\wedge</math> ([[Writable]] <math>\notin</math> newLenDesc <math>\vee</math> newLenDesc.[[Writable]])  <math>\wedge</math> DefineOwnProperty(H, A, l, "length", newLenDesc', b) = (H', A', true)  <math>\wedge</math> DeleteArray(H', A', l, newLen, oldLen, newLenDesc', true, b) = (H'', A'', false)</p>
<p>Step 3.h : set newWritable = true &amp; 3.l (H'', A'', true)</p>	<p>if ToString(H, x) = "length" <math>\wedge</math> [[Value]] <math>\in</math> ov <math>\wedge</math> newLen = newLenNum  <math>\wedge</math> newLen &lt; oldLen <math>\wedge</math> oldLenDesc.[[Writable]]  <math>\wedge</math> ([[Writable]] <math>\notin</math> newLenDesc <math>\vee</math> newLenDesc.[[Writable]])  <math>\wedge</math> DefineOwnProperty(H, A, l, "length", newLenDesc', b) = (H', A', true)  <math>\wedge</math> DeleteArray(H', A', l, newLen, oldLen, newLenDesc', true, b) = (H'', A'', true)</p>
<p>Step 3.h : set newWritable = false &amp; 3.j (H', A', err)</p>	<p>if ToString(H, x) = "length" <math>\wedge</math> [[Value]] <math>\in</math> ov <math>\wedge</math> newLen = newLenNum  <math>\wedge</math> newLen &lt; oldLen <math>\wedge</math> oldLenDesc.[[Writable]] <math>\wedge</math> <math>\neg</math> newLenDesc.[[Writable]]  <math>\wedge</math> DefineOwnProperty(H, A, l, "length", newLenDesc'', b) = (H', A', err)</p>
<p>Step 3.h : set newWritable = false &amp; 3.k (H', A', false)</p>	<p>if ToString(H, x) = "length" <math>\wedge</math> [[Value]] <math>\in</math> ov <math>\wedge</math> newLen = newLenNum  <math>\wedge</math> newLen &lt; oldLen <math>\wedge</math> oldLenDesc.[[Writable]] <math>\wedge</math> <math>\neg</math> newLenDesc.[[Writable]]  <math>\wedge</math> DefineOwnProperty(H, A, l, "length", newLenDesc'', b) = (H', A', false)</p>
<p>Step 3.h : set newWritable = false &amp; 3.l (H'', A'', err)</p>	<p>if ToString(H, x) = "length" <math>\wedge</math> [[Value]] <math>\in</math> ov <math>\wedge</math> newLen = newLenNum  <math>\wedge</math> newLen &lt; oldLen <math>\wedge</math> oldLenDesc.[[Writable]] <math>\wedge</math> <math>\neg</math> newLenDesc.[[Writable]]  <math>\wedge</math> DefineOwnProperty(H, A, l, "length", newLenDesc'', b) = (H', A', true)  <math>\wedge</math> DeleteArray(H', A', l, newLen, oldLen, newLenDesc'', false, b) = (H'', A'', err)</p>
<p>Step 3.h : set newWritable = false &amp; 3.l (H'', A'', if b TypeError else false)</p>	<p>if ToString(H, x) = "length" <math>\wedge</math> [[Value]] <math>\in</math> ov <math>\wedge</math> newLen = newLenNum  <math>\wedge</math> newLen &lt; oldLen <math>\wedge</math> oldLenDesc.[[Writable]] <math>\wedge</math> <math>\neg</math> newLenDesc.[[Writable]]  <math>\wedge</math> DefineOwnProperty(H, A, l, "length", newLenDesc'', b) = (H', A', true)  <math>\wedge</math> DeleteArray(H', A', l, newLen, oldLen, newLenDesc'', false, b) = (H'', A'', false)</p>
<p>Step 3.h : set newWritable = false &amp; 3.m (H<sup>r</sup>, A<sup>r</sup>, ve)</p>	<p>if ToString(H, x) = "length" <math>\wedge</math> [[Value]] <math>\in</math> ov <math>\wedge</math> newLen = newLenNum  <math>\wedge</math> newLen &lt; oldLen <math>\wedge</math> oldLenDesc.[[Writable]] <math>\wedge</math> <math>\neg</math> newLenDesc.[[Writable]]  <math>\wedge</math> DefineOwnProperty(H, A, l, "length", newLenDesc'', b) = (H', A', true)  <math>\wedge</math> DeleteArray(H', A', l, newLen, oldLen, newLenDesc'', false, b) = (H'', A'', true)  <math>\wedge</math> DefineOwnProperty(H'', A'', l, "length", {[[Writable]] : false}, false) =  (H<sup>r</sup>, A<sup>r</sup>, ve)</p>
<p>Step 4.b (H, A, if b TypeError else false)</p>	<p>if isIndex(ToString(H, x)) <math>\wedge</math> index <math>\geq</math> oldLen <math>\wedge</math> <math>\neg</math> oldLenDesc.[[Writable]]</p>
<p>Step 4.c (H', A', err)</p>	<p>if isIndex(ToString(H, x)) <math>\wedge</math> (index &lt; oldLen <math>\vee</math> oldLenDesc.[[Writable]])  <math>\wedge</math> DefineOwnProperty(H, A, l, x, ov, false) = (H', A', err)</p>
<p>Step 4.d (H', A', if b TypeError else false)</p>	<p>if isIndex(ToString(H, x)) <math>\wedge</math> (index &lt; oldLen <math>\vee</math> oldLenDesc.[[Writable]])  <math>\wedge</math> DefineOwnProperty(H, A, l, x, ov, false) = (H', A', false)</p>
<p>Step 4.e.ii (H', A', err)</p>	<p>if isIndex(ToString(H, x)) <math>\wedge</math> (index &lt; oldLen <math>\vee</math> oldLenDesc.[[Writable]])  <math>\wedge</math> DefineOwnProperty(H, A, l, x, ov, false) = (H', A', true) <math>\wedge</math> index <math>\geq</math> oldLen  <math>\wedge</math> DefineOwnProperty(H', A', l, "length", oldLenDesc', false) = (H'', A'', err)</p>
<p>Step 4.e.ii (H', A', true)</p>	<p>if isIndex(ToString(H, x)) <math>\wedge</math> (index &lt; oldLen <math>\vee</math> oldLenDesc.[[Writable]])  <math>\wedge</math> DefineOwnProperty(H, A, l, x, ov, false) = (H', A', true) <math>\wedge</math> index <math>\geq</math> oldLen  <math>\wedge</math> DefineOwnProperty(H', A', l, "length", oldLenDesc', false) = (H'', A'', v)</p>
<p>Step 4.f (H', A', true)</p>	<p>if isIndex(ToString(H, x)) <math>\wedge</math> (index &lt; oldLen <math>\vee</math> oldLenDesc.[[Writable]])  <math>\wedge</math> DefineOwnProperty(H, A, l, x, ov, false) = (H', A', true) <math>\wedge</math> index &lt; oldLen</p>
<p>Step 5 DefinOwnProperty(H, A, l, x, ov, b)</p>	<p>if <math>\neg</math> ToString(H, x) = "length" <math>\wedge</math> <math>\neg</math> isIndex(ToString(H, x))</p>



## 9 Type Conversion and Testing

### 9.1 ToPrimitive

$ToPrimitive : Heap \times Val \times Str \rightarrow PVal$   
 $ToPrimitive(H, v, s) = \begin{cases} DefaultValue(H, v, s) & \text{if } v \in Loc \\ v & \text{otherwise} \end{cases}$

### 9.2 ToBoolean

$ToBoolean : Val \rightarrow Bool$   
 $ToBoolean(v) = \begin{cases} false & \text{if } v = undefined \\ false & \text{if } v = null \\ v & \text{if } v \in Bool \\ false & \text{if } v \in \{+0, -0, NaN\} \\ true & \text{if } v \in Num \setminus \{+0, -0, NaN\} \\ false & \text{if } v = "" \\ true & \text{if } v \in Str \setminus \{""\} \\ true & \text{if } v \in Loc \end{cases}$

### 9.3 ToNumber

$ToNumber : Heap \times Val \rightarrow Num$   
 $ToNumber(H, v) = \begin{cases} NaN & \text{if } v = undefined \\ +0 & \text{if } v = null \vee v = false \\ 1 & \text{if } v = true \\ v & \text{if } v \in Num \\ v.toString & \text{if } v \in Str \text{ See 9.3.1.} \\ ToNumber(H, ToPrimitive(H, v, Number)) & \text{if } v \in Loc \end{cases}$

### 9.5 ToInt32

### 9.6 ToUint32

*SKIP!*

### 9.8 ToString

$ToString : Heap \times Val \rightarrow Str$   
 $ToString(H, v) = \begin{cases} "undefined" & \text{if } v = undefined \\ "null" & \text{if } v = null \\ "v" & \text{if } v \in Bool \\ "v" & \text{if } v \in Num \text{ See 9.8.1.} \\ v & \text{if } v \in Str \\ ToString(H, ToPrimitive(H, v, String)) & \text{if } v \in Loc \end{cases}$

### 9.9 ToObject

$ToObject : Heap \times Val \rightarrow Heap \times (Loc \cup Error)$   
 $ToObject(H, v) = \begin{cases} (H, TypeError) & \text{if } v = undefined \vee v = null \\ (H[l \mapsto NewBoolObject(v)], l) & \text{if } v \in Bool \wedge l = NewLoc() \\ (H[l \mapsto NewNumObject(v)], l) & \text{if } v \in Num \wedge l = NewLoc() \\ (H[l \mapsto NewStrObject(v)], l) & \text{if } v \in Str \wedge l = NewLoc() \\ (H, v) & \text{if } v \in Loc \end{cases}$

### 9.10 CheckObjectCoercible

$CheckObjectCoercible : Val \rightarrow ValError$   
 $CheckObjectCoercible(v) = \begin{cases} TypeError & \text{if } v = undefined \vee v = null \\ v & \text{if } v \neq undefined \wedge v \neq null \end{cases}$

### 9.11 IsCallable

$IsCallable : Heap \times Val \rightarrow Bool$   
 $IsCallable(H, v) = v \in Dom(H) \wedge [[Code]] \in Dom(H(l))$

## 10.2.1 Environment Records

### 10.2.1.1 Declarative Environment Records

#### 10.2.1.1.1 HasBinding(N) $x \in Dom(\sigma)$

$HasBinding : Env \times Var \rightarrow Bool$   
 $HasBinding(A, x) = \begin{cases} false & \text{if } A = \#Global \\ x \in Dom(\sigma) & \text{if } A = \sigma :: A' \\ HasBinding(A', x) & \text{if } A = l :: A' \end{cases}$   
 $Dom(\sigma) = \{ x \mid x \mapsto sv \in \sigma \}$



### 10.2.1.2 Object Environment Records

#### 10.2.1.2.1 HasBinding (N) 8.12.6 [ [HasProperty] ] (P) *HasProperty*(H, l, x)

$$\text{Dom}(H) = \{ l \mid l \mapsto o \in H \}$$

#### 10.2.1.1.2 CreateMutableBinding (N, D) Assert: $x \notin \text{Dom}(\sigma)$

$$\text{CreateBinding} : \text{Heap} \times \text{Env} \times \text{Var} \times \text{eval} \rightarrow \text{Heap} \times \text{Env}$$

$$\text{CreateBinding}(H, A, x, b) = \begin{cases} (H[\#Global \mapsto H(\#Global).@property[x \mapsto \{[[\text{Value}]] : \text{undefined}, & \text{if } A = \#Global \\ [[\text{Writable}]] : \text{true}, \\ [[\text{Enumerable}]] : \text{true}, \\ [[\text{Configurable}]] : b\}]], A) \\ \text{InterpreterError} & \text{if } A = \sigma :: A' \wedge x \in \text{Dom}(\sigma) \\ (H, \sigma[x \mapsto \{[[\text{Value}]] : \text{undefined}, [[\text{Mutable}]] : \text{true}, & \text{if } A = \sigma :: A' \wedge x \notin \text{Dom}(\sigma) \\ [[\text{Configurable}]] : b\} :: A') & \text{if } A = l :: A' \wedge \\ (H', l :: A'') & \text{CreateBinding}(H, A', x, b) = (H', A'') \end{cases}$$

#### 10.2.1.1.3 SetMutableBinding (N, V, S)

$$\text{SetBinding} : \text{Heap} \times \text{Env} \times \text{Var} \times \text{Val} \times \text{strict} \rightarrow \text{Heap} \times \text{Env} \times \text{ValError}$$

$$\text{SetBinding}(H, A, x, v, b) = \begin{cases} (H[\#Global \mapsto H(\#Global).@property[x \mapsto v]], A, v) & \text{if } A = \#Global \\ (H, \sigma[x \mapsto \{[[\text{Value}]] : v, [[\text{Mutable}]] : \text{true}, & \text{if } A = \sigma :: A' \wedge x \in \text{Dom}(\sigma) \wedge \\ [[\text{Configurable}]] : b\} :: A', v) & \sigma(x).[[\text{Mutable}]] \\ (H, A, \text{TypeError}) & \text{if } A = \sigma :: A' \wedge x \in \text{Dom}(\sigma) \wedge \\ & \neg \sigma(x).[[\text{Mutable}]] \wedge b \\ (H, A, v) & \text{if } A = \sigma :: A' \wedge x \in \text{Dom}(\sigma) \wedge \\ & \neg \sigma(x).[[\text{Mutable}]] \wedge \neg b \\ \text{SetBinding}(H', A', x, v, b) & \text{if } A = \sigma :: A' \wedge x \notin \text{Dom}(\sigma) \wedge \\ (H', l :: A'', ve) & \text{CreateBinding}(H, A', x, b) = (H', A') \\ & \text{SetBinding}(H, A', x, v, b) = (H', A'', ve) \end{cases}$$

$$\text{SetBindingDER} : \text{Heap} \times \text{Env} \times \text{Var} \times \text{Val} \times \text{strict} \rightarrow \text{Heap} \times \text{Env} \times \text{ValError}$$

$$\text{SetBindingDER}(H, A, x, v, b) = \begin{cases} \text{InterpreterError} & \text{if } A = \#Global \\ (H, \sigma[x \mapsto \{[[\text{Value}]] : v, [[\text{Mutable}]] : \text{true}, & \text{if } A = \sigma :: A' \wedge x \in \text{Dom}(\sigma) \wedge \\ [[\text{Configurable}]] : b\} :: A', v) & \sigma(x).[[\text{Mutable}]] \\ (H, A, \text{TypeError}) & \text{if } A = \sigma :: A' \wedge x \in \text{Dom}(\sigma) \wedge \\ & \neg \sigma(x).[[\text{Mutable}]] \wedge b \\ (H, A, v) & \text{if } A = \sigma :: A' \wedge x \in \text{Dom}(\sigma) \wedge \\ & \neg \sigma(x).[[\text{Mutable}]] \wedge \neg b \\ (H', \sigma :: A'', ve) & \text{if } A = \sigma :: A' \wedge x \notin \text{Dom}(\sigma) \wedge \\ & \text{SetBindingDER}(H, A', x, v, b) = (H', A'', ve) \\ (H', l :: A'', ve) & \text{if } A = l :: A' \\ & \text{SetBindingDER}(H, A', x, v, b) = (H', A'', ve) \end{cases}$$

#### 10.2.1.1.4 GetBindingValue (N, S) Assert: $x \in \text{Dom}(\sigma)$

$$\text{GetBindingValue} : \text{Heap} \times \text{DeclEnvRec} \times \text{Var} \times \text{Bool} \rightarrow \text{ValError}$$

$$\text{GetBindingValue}(H, \sigma, x, b) = \begin{cases} \text{undefined} & \text{if } \sigma(x).[[\text{Value}]] = \perp \wedge \neg \sigma(x).[[\text{Mutable}]] \wedge \neg b \\ \text{ReferenceError} & \text{if } \sigma(x).[[\text{Value}]] = \perp \wedge \neg \sigma(x).[[\text{Mutable}]] \wedge b \\ \sigma(x).[[\text{Value}]] & \text{if } \sigma(x).[[\text{Value}]] \neq \perp \vee \sigma(x).[[\text{Mutable}]] \end{cases}$$

#### 10.2.1.1.7 CreateImmutableBinding (N) Assert: $x \notin \text{Dom}(\sigma)$

$$\text{CreateImmutableBinding} : \text{Heap} \times \text{Env} \times \text{Var} \times \text{eval} \rightarrow \text{Heap} \times \text{Env}$$

$$\text{CreateImmutableBinding}(H, A, x, b) = \begin{cases} (H, \sigma[x \mapsto \{[[\text{Value}]] : \text{undefined}, [[\text{Mutable}]] : \text{false}, [[\text{Configurable}]] : b\} :: A') & \text{if } A = \sigma :: A' \wedge x \notin \text{Dom}(\sigma) \\ \text{InterpreterError} & \text{otherwise} \end{cases}$$

#### 10.2.1.1.8 InitializeImmutableBinding(N, V) *Assert: $x \in \text{Dom}(\sigma)$*

*InitializeImmutableBinding* :  $\text{Heap} \times \text{Env} \times \text{Var} \times \text{Val} \times \text{strict} \rightarrow \text{Heap} \times \text{Env} \times \text{ValError}$

*InitializeImmutableBinding*( $H, A, x, v, b$ ) =

$$\begin{cases} (H, \sigma[x \mapsto \{[[\text{Value}]] : v, [[\text{Mutable}]] : \text{false}, [[\text{Configurable}]] : b\}] :: A', v) & \text{if } A = \sigma :: A' \wedge x \in \text{Dom}(\sigma) \\ \text{InterpreterError} & \text{otherwise} \end{cases}$$

#### 10.2.1.2.4 GetBindingValue(N, S)

*GetBindingValue* :  $\text{Heap} \times \text{ObjEnvRec} \times \text{Var} \times \text{Bool} \rightarrow \text{ValError}$

$$\text{GetBindingValue}(H, l, x, b) = \begin{cases} \text{ReferenceError} & \text{if } l = \# \text{Null} \\ \text{undefined} & \text{if } \neg \text{HasProperty}(H, l, x) \wedge \neg b \\ \text{ReferenceError} & \text{if } \neg \text{HasProperty}(H, l, x) \wedge b \\ \text{Get}(H, l, x) & \text{if } \text{HasProperty}(H, l, x) \end{cases}$$

#### 10.2.2.1 GetIdentifierReference(lex, name, strict)

*Lookup* :  $\text{Heap} \times \text{Env} \times \text{PName} \times \text{strict} \rightarrow \text{EnvRec}$

$$\text{Lookup}(H, A, x, \text{strict}) = \begin{cases} \# \text{Null} & \text{if } A = \# \text{Global} \wedge \neg \text{HasProperty}(H, \# \text{Global}, x) \\ l & \text{if } A = \# \text{Global} \wedge \text{HasProperty}(H, \# \text{Global}, x) \wedge \text{GetProperty}(H, \# \text{Global}, x) = (-, l) \\ \sigma & \text{if } A = \sigma :: A' \wedge x \in \text{Dom}(\sigma) \\ \text{Lookup}(H, A', x, \text{strict}) & \text{if } A = \sigma :: A' \wedge x \notin \text{Dom}(\sigma) \\ l' & \text{if } A = l :: A' \wedge \text{HasProperty}(H, l, x) \wedge \text{GetProperty}(H, l, x) = (-, l') \\ \text{Lookup}(H, A', x, \text{strict}) & \text{if } A = l :: A' \wedge \neg \text{HasProperty}(H, l, x) \end{cases}$$

## 15 Standard Built-in ECMAScript Objects

*InitHeap* = {

#### 15.1 The Global Object

$\# \text{Global} \mapsto \{\},$

#### 15.2.3.1 Object.prototype

#### 15.2.4 Properties of the Object Prototype Object

$\# \text{ObjProto} \mapsto \{[[\text{Class}]] : \text{"Object"}, [[\text{Extensible}]] : \text{true}, [[\text{Prototype}]] : \text{null}\},$

#### 15.3.3.1 Function.prototype

#### 15.3.4 Properties of the Function Prototype Object

$\# \text{FtnProto} \mapsto \{[[\text{Class}]] : \text{"Function"}, [[\text{Extensible}]] : \text{true}, [[\text{Prototype}]] : \# \text{ObjProto}, [[\text{Code}]] : \text{function } \_(\text{this}, \text{arguments}) \{ \text{return undefined} \}, \text{length} : 0\},$

#### 15.4.3.1 Array.prototype

#### 15.4.4 Properties of the Array Prototype Object

$\# \text{ArrProto} \mapsto \{[[\text{Class}]] : \text{"Array"}, [[\text{Extensible}]] : \text{true}, [[\text{Prototype}]] : \# \text{ObjProto}, \text{length} : 0\},$

#### 15.5.3.1 String.prototype

#### 15.5.4 Properties of the String Prototype Object

$\# \text{StrProto} \mapsto \{[[\text{Class}]] : \text{"String"}, [[\text{Extensible}]] : \text{true}, [[\text{Prototype}]] : \# \text{ObjProto}, [[\text{PrimitiveValue}]] : \text{""}\},$

#### 15.6.3.1 Boolean.prototype

#### 15.6.4 Properties of the Boolean Prototype Object

$\# \text{BoolProto} \mapsto \{[[\text{Class}]] : \text{"Boolean"}, [[\text{Extensible}]] : \text{true}, [[\text{Prototype}]] : \# \text{ObjProto}, [[\text{PrimitiveValue}]] : \text{false}\},$

#### 15.7.3.1 Number.prototype

#### 15.7.4 Properties of the Number Prototype Object

$\# \text{NumProto} \mapsto \{[[\text{Class}]] : \text{"Number"}, [[\text{Extensible}]] : \text{true}, [[\text{Prototype}]] : \# \text{ObjProto}, [[\text{PrimitiveValue}]] : +0\},$

#### 15.11.3.1 Error.prototype

#### 15.11.4 Properties of the Error Prototype Object

$\# \text{ErrProto} \mapsto \{[[\text{Class}]] : \text{"Error"}, [[\text{Extensible}]] : \text{true}, [[\text{Prototype}]] : \# \text{ObjProto}\},$

#### 15.11 Error Objects

#### 15.11.1 Error(message)

$\# \text{Error} \mapsto \{[[\text{Class}]] : \text{"Error"}, [[\text{Extensible}]] : \text{true}, [[\text{Prototype}]] : \# \text{ErrProto}\},$

#### 15.11.6 Native Error Types Used in This Standard

#### 15.11.7 NativeError Object Structure

##### 15.11.7.5 Properties of the NativeError

```
#EvalError ↦ {[Class]: "Error", [[Extensible]] : true, [[Prototype]] : #ErrProto},
#RangeError ↦ {[Class]: "Error", [[Extensible]] : true, [[Prototype]] : #ErrProto},
#ReferenceError ↦ {[Class]: "Error", [[Extensible]] : true, [[Prototype]] : #ErrProto},
#SyntaxError ↦ {[Class]: "Error", [[Extensible]] : true, [[Prototype]] : #ErrProto},
#TypeError ↦ {[Class]: "Error", [[Extensible]] : true, [[Prototype]] : #ErrProto},
#URIError ↦ {[Class]: "Error", [[Extensible]] : true, [[Prototype]] : #ErrProto}
}
```

#### 15.4 Array Objects

##### 15.4.2.1 new Array([item0[, item1[, ...]])

```
NewArrObject : Num → Object
NewArrObject(n) = {[Class]: "Array", [[Extensible]] : true, [[Prototype]] : #ArrProto,
  @property : { "length" ↦ {[Value] : n, [[Writable]] : true,
    [[Enumerable]] : false, [[Configurable]] : false }}
```

#### 15.5 String Objects

##### 15.5.2.1 new String([value])

```
NewStrObject : Str → Object
NewStrObject(s) = {[Class]: "String", [[Extensible]] : true, [[Prototype]] : #StrProto, [[PrimitiveValue]] : s}
```

#### 15.6 Boolean Objects

##### 15.6.2.1 new Boolean(value)

```
NewBoolObject : Bool → Object
NewBoolObject(b) = {[Class]: "Boolean", [[Extensible]] : true, [[Prototype]] : #BoolProto, [[PrimitiveValue]] : b}
```

#### 15.7 Number Objects

##### 15.7.2.1 new Number([value])

```
NewNumObject : Num → Object
NewNumObject(n) = {[Class]: "Number", [[Extensible]] : true, [[Prototype]] : #NumProto, [[PrimitiveValue]] : n}
```

#### 13.2 Creating Function Objects: The following properties are omitted for now:

```
[[Get]]: 15.3.5.4 [[Get]] (P)
[[Call]]: 13.2.1 [[Call]]
[[Construct]]: 13.2.2 [[Construct]]
[[HasInstance]]: 15.3.5.3 [[HasInstance]] (V)
[[FormalParameters]]
```

```
NewFtnObject : Heap × Env × FVal → Heap × Loc
NewFtnObject(H, A, fv) = (H[l ↦ NewFtnObj(fv, A, l', strict), l' ↦ o], l)
  where l = NewLoc()    l' = NewLoc()
         o = NewObj().@property["constructor" ↦ {[Value] : l, [[Writable]] : true,
           [[Enumerable]] : false, [[Configurable]] : true}]
```

```
NewFtnObj : FVal × Env × Loc × strict → Object
NewFtnObj(fv, A, l, b) = {[Class]: "Function",
  [[Extensible]] : true,
  [[Prototype]] : #FtnProto,
  @property : { "prototype" ↦ {[Value] : l, [[Writable]] : true,
    [[Enumerable]] : false, [[Configurable]] : false},
    "length" ↦ {[Value] : ParamsSize(fv), [[Writable]] : false,
    [[Enumerable]] : false, [[Configurable]] : false}},
  [[Code]] : fv,
  [[Scope]] : A}
```

### 15.2.2.1 new Object([value])

$$\begin{aligned} \text{NewObj} &: () \rightarrow \text{Object} \\ \text{NewObj}() &= \{[\text{Class}] : \text{"Object"}, \\ &\quad [\text{Extensible}] : \text{true}, \\ &\quad [\text{Prototype}] : \# \text{ObjProto}, \\ &\quad @\text{property} : \{\}\} \end{aligned}$$

### 10.6 Arguments Object

$$\begin{aligned} \text{NewArgObject} &: \text{Loc} \times \text{Num} \times \text{Object} \times \text{strict} \rightarrow \text{Object} \\ \text{NewArgObject}(l_f, n_p, o, b) &= \begin{cases} \text{NewArgObj}(l_f, n_p, o).@\text{property}[\text{"callee"}] \mapsto \{[\text{Value}] : l_f, [\text{Writable}] : \text{true}, & \text{if } b \\ & [\text{Enumerable}] : \text{false}, \\ & [\text{Configurable}] : \text{true}\} \\ \text{NewArgObj}(l_f, n_p, o) & \text{if } \neg b \end{cases} \\ \\ \text{NewArgObj} &: \text{Loc} \times \text{Num} \times \text{Object} \rightarrow \text{Object} \\ \text{NewArgObj}(l_f, n_p, o) &= \{[\text{Class}] : \text{"Arguments"}, \\ &\quad [\text{Extensible}] : \text{true}, \\ &\quad [\text{Prototype}] : \# \text{ObjProto}, \\ &\quad @\text{property} : \{ \\ &\quad \quad \text{"0"} \mapsto \{[\text{Value}] : v_0, [\text{Writable}] : \text{true}, [\text{Enumerable}] : \text{true}, [\text{Configurable}] : \text{true}\}, \\ &\quad \dots \\ &\quad \text{"n-1"} \mapsto \{[\text{Value}] : v_{n-1}, [\text{Writable}] : \text{true}, [\text{Enumerable}] : \text{true}, [\text{Configurable}] : \text{true}\}, \\ &\quad \text{"length"} \mapsto \{[\text{Value}] : n_a, [\text{Writable}] : \text{true}, [\text{Enumerable}] : \text{false}, [\text{Configurable}] : \text{true}\} \\ &\quad \text{where } n_a = o.@\text{property}(\text{"length"}) \quad n = \text{Max}(n_a, n_p) \quad v_i = \text{GetArg}(o, i, n_a, n_p) \\ \\ \text{Max} &: \text{Num} \times \text{Num} \rightarrow \text{Num} \\ \text{Max}(n_1, n_2) &= \begin{cases} n_1 & \text{if } n_1 \geq n_2 \\ n_2 & \text{if } n_1 < n_2 \end{cases} \\ \\ \text{GetArg} &: \text{Object} \times \text{Num} \times \text{Num} \times \text{Num} \rightarrow \text{Val} \\ \text{GetArg}(o, i, n_a, n_p) &= \begin{cases} o.@\text{property}(\text{"i"}) & \text{if } n_a \geq n_p \\ o.@\text{property}(\text{"i"}) & \text{if } n_a < n_p \wedge 0 \leq i < n_a \\ \text{undefined} & \text{if } n_a < n_p \wedge n_a \leq i < n_p \end{cases} \end{aligned}$$

## 5.4 Evaluation Rules

### 5.4.1 Program

$$\boxed{p \rightarrow_p (H, A), ct}$$

IRRoot(List<IRFunDecl> fds, List<IRVarStmt> vds, List<IRStmt> irs)

14 Program

10.4.1.1 Initial Global Execution Context

$$\frac{(InitHeap, \#Global, \#Global), p \rightarrow_s (H, A), ct}{p \rightarrow_p (H, A), ct}$$

### 5.4.2 Statements

$$\boxed{(H, A, tb), s \rightarrow_s (H, A), ct}$$

IRExprStmt(IRId lhs, IRExpr right, boolean ref = false)

12.4 Expression Statement

11.13 Assignment Operators: PutValue(lref, rval)

$$\frac{(H, A, tb), e \rightarrow_e err}{(H, A, tb), \underline{x} = \underline{e} \rightarrow_s (H, A), Throw(err)}$$

$$\frac{(H, A, tb), e \rightarrow_e v \quad PutValue(H, A, \underline{x}, v, \text{strict}) = (H', A', err)}{(H, A, tb), \underline{x} = \underline{e} \rightarrow_s (H', A'), Throw(err)}$$

$$\frac{(H, A, tb), e \rightarrow_e v \quad PutValue(H, A, \underline{x}, v, \text{strict}) = (H', A', v')}{(H, A, tb), \underline{x} = \underline{e} \rightarrow_s (H', A'), Normal(v')}$$

11.4.1 The delete Operator

IRDelete(IRId lhs, IRId id)

$$\frac{(H, A, tb), y \rightarrow_e err}{(H, A, tb), \underline{x} = \text{delete } y \rightarrow_s (H, A), Throw(err)}$$

$$\frac{(H, A, tb), y \rightarrow_e v \quad DeleteBinding(H, A, ToString(H, y), \text{strict}) = (H', A', err)}{(H, A, tb), \underline{x} = \text{delete } y \rightarrow_s (H', A'), Throw(err)}$$

$$\frac{(H, A, tb), y \rightarrow_e v \quad DeleteBinding(H, A, ToString(H, y), \text{strict}) = (H', A', b) \quad (H', A', tb), \underline{x} = b \rightarrow_s (H'', A''), ct}{(H, A, tb), \underline{x} = \text{delete } y \rightarrow_s (H'', A''), ct}$$

IRDeleteProp(IRId lhs, IRId obj, IRId index)

$$\frac{(H, A, tb), y \rightarrow_e err}{(H, A, tb), \underline{x} = \text{delete } y[\underline{z}] \rightarrow_s (H, A), Throw(err)}$$

$$\frac{(H, A, tb), y \rightarrow_e v \quad (H, A, tb), \underline{z} \rightarrow_e err}{(H, A, tb), \underline{x} = \text{delete } y[\underline{z}] \rightarrow_s (H, A), Throw(err)}$$

$$\frac{(H, A, tb), y \rightarrow_e v_1 \quad (H, A, tb), \underline{z} \rightarrow_e v_2 \quad CheckObjectCoercible(v_1) = err}{(H, A, tb), \underline{x} = \text{delete } y[\underline{z}] \rightarrow_s (H, A), Throw(err)}$$

$$\frac{(H, A, tb), y \rightarrow_e v_1 \quad (H, A, tb), \underline{z} \rightarrow_e v_2 \quad CheckObjectCoercible(v_1) \neq err \quad ToObject(H, v_1) = (H', l) \quad Delete(H', A, l, ToString(H', v_2), \text{strict}) = (H'', A', err)}{(H, A, tb), \underline{x} = \text{delete } y[\underline{z}] \rightarrow_s (H'', A'), Throw(err)}$$

$$\frac{(H, A, tb), y \rightarrow_e v_1 \quad (H, A, tb), \underline{z} \rightarrow_e v_2 \quad CheckObjectCoercible(v_1) \neq err \quad ToObject(H, v_1) = (H', l) \quad Delete(H', A, l, ToString(H', v_2), \text{strict}) = (H'', A', b) \quad (H'', A', tb), \underline{x} = b \rightarrow_s (H''', A''), ct}{(H, A, tb), \underline{x} = \text{delete } y[\underline{z}] \rightarrow_s (H''', A''), ct}$$

IRStore(IRId obj, IRId index, IRExpr rhs)

11.2.1 Property Accessors: IRStore

11.13 Assignment Operators

8.7.2 PutValue(V, W)

8.7.2 [[Put]](P, V, Throw)

$$\frac{(H, A, tb), \underline{x} \rightarrow_e err}{(H, A, tb), \underline{x}[\underline{y}] = \underline{e} \rightarrow_s (H, A), \text{Throw}(err)}$$

$$\frac{(H, A, tb), \underline{x} \rightarrow_e v \quad (H, A, tb), \underline{y} \rightarrow_e err}{(H, A, tb), \underline{x}[\underline{y}] = \underline{e} \rightarrow_s (H, A), \text{Throw}(err)}$$

$$\frac{(H, A, tb), \underline{x} \rightarrow_e v_1 \quad (H, A, tb), \underline{y} \rightarrow_e v_2 \quad \text{CheckObjectCoercible}(v_1) = err}{(H, A, tb), \underline{x}[\underline{y}] = \underline{e} \rightarrow_s (H, A), \text{Throw}(err)}$$

$$\frac{(H, A, tb), \underline{x} \rightarrow_e v_1 \quad (H, A, tb), \underline{y} \rightarrow_e v_2 \quad \text{CheckObjectCoercible}(v_1) \neq err \quad \text{ToObject}(H, v_1) = (H', l) \quad (H', A, tb), \underline{e} \rightarrow_e err}{(H, A, tb), \underline{x}[\underline{y}] = \underline{e} \rightarrow_s (H', A), \text{Throw}(err)}$$

[[Put]] 2.

$$\frac{(H, A, tb), \underline{x} \rightarrow_e v_1 \quad (H, A, tb), \underline{y} \rightarrow_e v_2 \quad \text{CheckObjectCoercible}(v_1) \neq err \quad \text{ToObject}(H, v_1) = (H', l) \quad (H', A, tb), \underline{e} \rightarrow_e v_3 \quad v_1 \in \{\text{Boolean}, \text{String}, \text{Number}\} \quad \text{CanPut}(H', l, \text{ToString}(H', v_2)) = \text{false}}{(H, A, tb), \underline{x}[\underline{y}] = \underline{e} \rightarrow_s (H', A), \text{if strict Throw(TypeError) else Normal}(v_3)}$$

[[Put]] 4.

$$\frac{(H, A, tb), \underline{x} \rightarrow_e v_1 \quad (H, A, tb), \underline{y} \rightarrow_e v_2 \quad \text{CheckObjectCoercible}(v_1) \neq err \quad \text{ToObject}(H, v_1) = (H', l) \quad (H', A, tb), \underline{e} \rightarrow_e v_3 \quad v_1 \in \{\text{Boolean}, \text{String}, \text{Number}\} \quad \text{CanPut}(H', l, \text{ToString}(H', v_2)) = \text{true} \quad \text{GetOwnPropety}(H', l, \text{ToString}(H', v_2)) = (dp, -)}{(H, A, tb), \underline{x}[\underline{y}] = \underline{e} \rightarrow_s (H', A), \text{if strict Throw(TypeError) else Normal}(v_3)}$$

[[Put]] 6.

$$\frac{(H, A, tb), \underline{x} \rightarrow_e v_1 \quad (H, A, tb), \underline{y} \rightarrow_e v_2 \quad \text{CheckObjectCoercible}(v_1) \neq err \quad \text{ToObject}(H, v_1) = (H', l) \quad (H', A, tb), \underline{e} \rightarrow_e v_3 \quad v_1 \in \{\text{Boolean}, \text{String}, \text{Number}\} \quad \text{CanPut}(H', l, \text{ToString}(H', v_2)) = \text{true} \quad \text{GetOwnPropety}(H', l, \text{ToString}(H', v_2)) \neq (dp, -) \quad \text{GetPropety}(H', l, \text{ToString}(H', v_2)) = (ap, -) \quad ap.[\text{Set}].[\text{Call}](v_1, [v_3]) = (H'', A', err)}{(H, A, tb), \underline{x}[\underline{y}] = \underline{e} \rightarrow_s (H'', A'), \text{Throw}(err)}$$

[[Put]] 6.

$$\frac{(H, A, tb), \underline{x} \rightarrow_e v_1 \quad (H, A, tb), \underline{y} \rightarrow_e v_2 \quad \text{CheckObjectCoercible}(v_1) \neq err \quad \text{ToObject}(H, v_1) = (H', l) \quad (H', A, tb), \underline{e} \rightarrow_e v_3 \quad v_1 \in \{\text{Boolean}, \text{String}, \text{Number}\} \quad \text{CanPut}(H', l, \text{ToString}(H', v_2)) = \text{true} \quad \text{GetOwnPropety}(H', l, \text{ToString}(H', v_2)) \neq (dp, -) \quad \text{GetPropety}(H', l, \text{ToString}(H', v_2)) = (ap, -) \quad ap.[\text{Set}].[\text{Call}](v_1, [v_3]) = (H'', A', v)}{(H, A, tb), \underline{x}[\underline{y}] = \underline{e} \rightarrow_s (H'', A'), \text{Normal}(v_3)}$$

[[Put]] 7.

$$\frac{(H, A, tb), \underline{x} \rightarrow_e v_1 \quad (H, A, tb), \underline{y} \rightarrow_e v_2 \quad \text{CheckObjectCoercible}(v_1) \neq err \quad \text{ToObject}(H, v_1) = (H', l) \quad (H', A, tb), \underline{e} \rightarrow_e v_3 \quad v_1 \in \{\text{Boolean}, \text{String}, \text{Number}\} \quad \text{CanPut}(H', l, \text{ToString}(H', v_2)) = \text{true} \quad \text{GetOwnPropety}(H', l, \text{ToString}(H', v_2)) \neq (dp, -) \quad \text{GetPropety}(H', l, \text{ToString}(H', v_2)) \neq (ap, -)}{(H, A, tb), \underline{x}[\underline{y}] = \underline{e} \rightarrow_s (H', A), \text{if strict Throw(TypeError) else Normal}(v_3)}$$

$(H, A, tb), \underline{x} \rightarrow_e v_1$	$(H, A, tb), \underline{y} \rightarrow_e v_2$	$CheckObjectCoercible(v_1) \neq err$	$ToObject(H, v_1) = (H', l)$
$(H', A, tb), \underline{e} \rightarrow_e v_3$	$v_1 \notin \{\text{Boolean}, \text{String}, \text{Number}\}$	$H'(l).[[\text{Class}]] \neq \text{"Array"}$	
$Put(H', A, l, ToString(H', v_2), v_3, \text{strict}) = (H'', A', err)$			
$(H, A, tb), \underline{x}[y] = \underline{e} \rightarrow_s (H'', A'), Throw(err)$			
$(H, A, tb), \underline{x} \rightarrow_e v_1$	$(H, A, tb), \underline{y} \rightarrow_e v_2$	$CheckObjectCoercible(v_1) \neq err$	$ToObject(H, v_1) = (H', l)$
$(H', A, tb), \underline{e} \rightarrow_e v_3$	$v_1 \notin \{\text{Boolean}, \text{String}, \text{Number}\}$	$H'(l).[[\text{Class}]] \neq \text{"Array"}$	
$Put(H', A, l, ToString(H', v_2), v_3, \text{strict}) = (H'', A', v)$			
$(H, A, tb), \underline{x}[y] = \underline{e} \rightarrow_s (H'', A'), Normal(v_3)$			
$(H, A, tb), \underline{x} \rightarrow_e v_1$	$(H, A, tb), \underline{y} \rightarrow_e v_2$	$CheckObjectCoercible(v_1) \neq err$	$ToObject(H, v_1) = (H', l)$
$(H', A, tb), \underline{e} \rightarrow_e v_3$	$v_1 \notin \{\text{Boolean}, \text{String}, \text{Number}\}$	$H'(l).[[\text{Class}]] = \text{"Array"}$	
$CanPut(H', l, ToString(H', v_2)) = false$			
$(H, A, tb), \underline{x}[y] = \underline{e} \rightarrow_s (H', A), if \text{strict } Throw(TypeError) \text{ else } Normal(v_3)$			
$(H, A, tb), \underline{x} \rightarrow_e v_1$	$(H, A, tb), \underline{y} \rightarrow_e v_2$	$CheckObjectCoercible(v_1) \neq err$	$ToObject(H, v_1) = (H', l)$
$(H', A, tb), \underline{e} \rightarrow_e v_3$	$v_1 \notin \{\text{Boolean}, \text{String}, \text{Number}\}$	$H'(l).[[\text{Class}]] = \text{"Array"}$	
$CanPut(H', l, ToString(H', v_2)) = true$			
$GetOwnProperty(H', l, ToString(H', v_2)) = (dp, -)$			
$valueDesc = \{[[Value]] : v_3\}$			
$DefineOwnProperty(H', A, l, ToString(H', v_2), valueDesc, \text{strict}) = (H'', A', err)$			
$(H, A, tb), \underline{x}[y] = \underline{e} \rightarrow_s (H'', A'), Throw(err)$			
$(H, A, tb), \underline{x} \rightarrow_e v_1$	$(H, A, tb), \underline{y} \rightarrow_e v_2$	$CheckObjectCoercible(v_1) \neq err$	$ToObject(H, v_1) = (H', l)$
$(H', A, tb), \underline{e} \rightarrow_e v_3$	$v_1 \notin \{\text{Boolean}, \text{String}, \text{Number}\}$	$H'(l).[[\text{Class}]] = \text{"Array"}$	
$CanPut(H', l, ToString(H', v_2)) = true$			
$GetOwnProperty(H', l, ToString(H', v_2)) = (dp, -)$			
$valueDesc = \{[[Value]] : v_3\}$			
$DefineOwnProperty(H', A, l, ToString(H', v_2), valueDesc, \text{strict}) = (H'', A', v)$			
$(H, A, tb), \underline{x}[y] = \underline{e} \rightarrow_s (H'', A'), Normal(v_3)$			
$(H, A, tb), \underline{x} \rightarrow_e v_1$	$(H, A, tb), \underline{y} \rightarrow_e v_2$	$CheckObjectCoercible(v_1) \neq err$	$ToObject(H, v_1) = (H', l)$
$(H', A, tb), \underline{e} \rightarrow_e v_3$	$v_1 \notin \{\text{Boolean}, \text{String}, \text{Number}\}$	$H'(l).[[\text{Class}]] = \text{"Array"}$	
$CanPut(H', l, ToString(H', v_2)) = true$			
$GetOwnProperty(H', l, ToString(H', v_2)) \neq (dp, -)$			
$GetProperty(H', l, ToString(H', v_2)) = (ap, -)$			
$ap.[[Set]].[[Call]](H'(l), v_3) = (H'', A', err)$			
$(H, A, tb), \underline{x}[y] = \underline{e} \rightarrow_s (H'', A'), Throw(err)$			
$(H, A, tb), \underline{x} \rightarrow_e v_1$	$(H, A, tb), \underline{y} \rightarrow_e v_2$	$CheckObjectCoercible(v_1) \neq err$	$ToObject(H, v_1) = (H', l)$
$(H', A, tb), \underline{e} \rightarrow_e v_3$	$v_1 \notin \{\text{Boolean}, \text{String}, \text{Number}\}$	$H'(l).[[\text{Class}]] = \text{"Array"}$	
$CanPut(H', l, ToString(H', v_2)) = true$			
$GetOwnProperty(H', l, ToString(H', v_2)) \neq (dp, -)$			
$GetProperty(H', l, ToString(H', v_2)) = (ap, -)$			
$ap.[[Set]].[[Call]](H'(l), v_3) = (H'', A', v)$			
$(H, A, tb), \underline{x}[y] = \underline{e} \rightarrow_s (H'', A'), Normal(v_3)$			
$(H, A, tb), \underline{x} \rightarrow_e v_1$	$(H, A, tb), \underline{y} \rightarrow_e v_2$	$CheckObjectCoercible(v_1) \neq err$	$ToObject(H, v_1) = (H', l)$
$(H', A, tb), \underline{e} \rightarrow_e v_3$	$v_1 \notin \{\text{Boolean}, \text{String}, \text{Number}\}$	$H'(l).[[\text{Class}]] = \text{"Array"}$	
$CanPut(H', l, ToString(H', v_2)) = true$			
$GetOwnProperty(H', l, ToString(H', v_2)) \neq (dp, -)$			
$newDesc = \{[[Value]] : v_3, [[Writable]] : true, [[Enumerable]] : true, [[Configurable]] : true\}$			
$DefineOwnProperty(H', A, l, ToString(H', v_2), newDesc, \text{strict}) = (H'', A', err)$			
$(H, A, tb), \underline{x}[y] = \underline{e} \rightarrow_s (H'', A'), Throw(err)$			
$(H, A, tb), \underline{x} \rightarrow_e v_1$	$(H, A, tb), \underline{y} \rightarrow_e v_2$	$CheckObjectCoercible(v_1) \neq err$	$ToObject(H, v_1) = (H', l)$
$(H', A, tb), \underline{e} \rightarrow_e v_3$	$v_1 \notin \{\text{Boolean}, \text{String}, \text{Number}\}$	$H'(l).[[\text{Class}]] = \text{"Array"}$	
$CanPut(H', l, ToString(H', v_2)) = true$			
$GetOwnProperty(H', l, ToString(H', v_2)) \neq (dp, -)$			

`IRObject (IRId lhs, List<IRMember> members, Option<IRId> proto)`

#### 11.1.5 Object Initialiser

$$\frac{\text{NewLoc}() = l \quad H' = H[l \mapsto \text{NewObj}()] \quad (H', A, tb), \underline{x} = l \rightarrow_{\underline{s}} (H'', A'), ct}{(H, A, tb), \underline{x} = \{\} \rightarrow_{\underline{s}} (H'', A'), ct}$$

$$\frac{\text{NewLoc}() = l \quad H_1 = H[l \mapsto \text{NewObj}()] \quad (H_i, A, tb), \underline{m}_i \rightarrow_{\underline{m}} (H_{i+1}, \underline{y}_i, ov_i) \quad 1 \leq i < j \leq |m^*|}{(H_j, A, tb), \underline{m}_j \rightarrow_{\underline{m}} err} \\ (H, A, tb), \underline{x} = \{(\underline{m},)^*\} \rightarrow_{\underline{s}} (H, A), \text{Throw}(err)$$

$$\frac{\text{NewLoc}() = l \quad H_1 = H[l \mapsto \text{NewObj}()] \quad A_1 = A \quad (H_i, A_i, tb), \underline{m}_i \rightarrow_{\underline{m}} (H'_{i+1}, \underline{y}_i, ov_i) \quad 1 \leq i \leq |m^*| = n}{\text{DefineOwnProperty}(H'_{i+1}, A_i, l, \text{ToString}(H'_{i+1}, \underline{y}_i, ov_i, \text{false}) = (H_{i+1}, A_{i+1}, v) \quad (H_{n+1}, A_{n+1}, tb), \underline{x} = l \rightarrow_{\underline{s}} (H', A'), ct)} \\ (H, A, tb), \underline{x} = \{(\underline{m},)^*\} \rightarrow_{\underline{s}} (H', A'), ct$$

`IRArray (IRId lhs, List<Option<IRExpr>> elements)`

#### 11.1.4 Array Initialiser

$$\frac{\text{NewLoc}() = l \quad |(\underline{e})^*| = n \quad H' = H[l \mapsto \text{NewArrObject}(n)] \quad (H', A, tb), \underline{e}_i \rightarrow_{\underline{e}} v_i \quad 0 \leq i < j < n}{(H', A, tb), \underline{e}_j \rightarrow_{\underline{e}} err} \\ (H, A, tb), \underline{x} = [(\underline{e},)^*] \rightarrow_{\underline{s}} (H, A), \text{Throw}(err)$$

$$\frac{\text{NewLoc}() = l \quad |(\underline{y})^*| = n \quad H' = H[l \mapsto \text{NewArrObject}(n)] \quad (H', A, tb), \underline{y}_i \rightarrow_{\underline{e}} v_i \quad 0 \leq i < n}{\{[[\text{Value}]] : v_i, [[\text{Writable}]] : \text{true}, [[\text{Enumerable}]] : \text{true}, [[\text{Configurable}]] : \text{true}\} = dp_i} \\ H'_0 = H' \quad A_0 = A \quad \text{DefineOwnProperty}(H'_i, A_i, l, \text{ToString}(i, dp_i, \text{false}) = (H'_{i+1}, A_{i+1}, v) \quad H'' = H'_n \quad A' = A_n \\ (H'', A', tb), \underline{x} = l \rightarrow_{\underline{s}} (H''', A''), ct \\ (H, A, tb), \underline{x} = [(\underline{e},)^*] \rightarrow_{\underline{s}} (H''', A''), ct$$

`IRArgs (IRId lhs, List<Option<IRExpr>> elements)`



IRCall(IRId lhs, IRId fun, IRId thisB, IRId args)

### 11.2.3 Function Calls

#### 11.2.4 Argument Lists

$$\frac{(H, A, tb), y \rightarrow_e err}{(H, A, tb), x = y(z_1, z_2) \rightarrow_s (H, A), \text{Throw}(err)}$$

$$\frac{(H, A, tb), y \rightarrow_e v \quad (H, A, tb), z_1 \rightarrow_e err}{(H, A, tb), x = y(z_1, z_2) \rightarrow_s (H, A), \text{Throw}(err)}$$

$$\frac{(H, A, tb), y \rightarrow_e v \quad (H, A, tb), z_1 \rightarrow_e v_1 \quad (H, A, tb), z_2 \rightarrow_e err}{(H, A, tb), x = y(z_1, z_2) \rightarrow_s (H, A), \text{Throw}(err)}$$

$$\frac{(H, A, tb), y \rightarrow_e v \quad (H, A, tb), z_1 \rightarrow_e v_1 \quad (H, A, tb), z_2 \rightarrow_e v_2 \quad v \notin Loc}{(H, A, tb), x = y(z_1, z_2) \rightarrow_s (H, A), \text{Throw}(\text{TypeError})}$$

$$\frac{(H, A, tb), y \rightarrow_e v \quad (H, A, tb), z_1 \rightarrow_e v_1 \quad (H, A, tb), z_2 \rightarrow_e v_2 \quad v \in Loc \quad \neg \text{IsCallable}(H, v)}{(H, A, tb), x = y(z_1, z_2) \rightarrow_s (H, A), \text{Throw}(\text{TypeError})}$$

$$\frac{(H, A, tb), y \rightarrow_e v \quad (H, A, tb), z_1 \rightarrow_e v_1 \quad (H, A, tb), z_2 \rightarrow_e v_2 \quad v \in Loc \quad \text{IsCallable}(H, v) \quad v_2 \notin Loc}{(H, A, tb), x = y(z_1, z_2) \rightarrow_s (H, A), \text{Throw}(\text{TypeError})}$$

#### 10.4.3 Entering Function Code

$$\frac{\begin{array}{l} (H, A, tb), y \rightarrow_e v \quad (H, A, tb), z_1 \rightarrow_e v_1 \quad (H, A, tb), z_2 \rightarrow_e v_2 \quad v \in Loc \quad \text{IsCallable}(H, v) \quad v_2 \in Loc \\ H(v).[[\text{Code}]] = fv \quad \{\} :: H(v).[[\text{Scope}]] = A' \\ \text{NewLoc}() = l \quad H' = H[l \mapsto \text{NewArgObj}(v, \text{ParamsSize}(fv), H(v_2))] \\ \text{CreateBinding}(H', A', \text{arguments}, \text{eval}) = (H'', A'') \quad \text{SetBinding}(H'', A'', \text{arguments}, l, \text{strict}) = (H^f, A^f, err) \end{array}}{(H, A, tb), x = y(z_1, z_2) \rightarrow_s (H^f, A), \text{Throw}(err)}$$

$$\frac{\begin{array}{l} (H, A, tb), y \rightarrow_e v \quad (H, A, tb), z_1 \rightarrow_e v_1 \quad (H, A, tb), z_2 \rightarrow_e v_2 \quad v \in Loc \quad \text{IsCallable}(H, v) \quad v_2 \in Loc \\ H(v).[[\text{Code}]] = fv \quad \{\} :: H(v).[[\text{Scope}]] = A' \\ \text{NewLoc}() = l \quad H' = H[l \mapsto \text{NewArgObj}(v, \text{ParamsSize}(fv), H(v_2))] \\ \text{CreateBinding}(H', A', \text{arguments}, \text{eval}) = (H'', A'') \quad \text{SetBinding}(H'', A'', \text{arguments}, l, \text{strict}) = (H^f, A^f, v^f) \\ \text{GetThis}(H^f, v_1) = (H^t, l^t) \quad (H^t, A^f, l^t), \text{GetBody}(fv) \rightarrow_s (H^b, A^b), \text{Throw}(ve) \end{array}}{(H, A, tb), x = y(z_1, z_2) \rightarrow_s (H^b, A), \text{Throw}(ve)}$$

$$\frac{\begin{array}{l} (H, A, tb), y \rightarrow_e v \quad (H, A, tb), z_1 \rightarrow_e v_1 \quad (H, A, tb), z_2 \rightarrow_e v_2 \quad v \in Loc \quad \text{IsCallable}(H, v) \quad v_2 \in Loc \\ H(v).[[\text{Code}]] = fv \quad \{\} :: H(v).[[\text{Scope}]] = A' \\ \text{NewLoc}() = l \quad H' = H[l \mapsto \text{NewArgObj}(v, \text{ParamsSize}(fv), H(v_2))] \\ \text{CreateBinding}(H', A', \text{arguments}, \text{eval}) = (H'', A'') \quad \text{SetBinding}(H'', A'', \text{arguments}, l, \text{strict}) = (H^f, A^f, v^f) \\ \text{GetThis}(H^f, v_1) = (H^t, l^t) \quad (H^t, A^f, l^t), \text{GetBody}(fv) \rightarrow_s (H^b, A^b), \text{Return}(\text{empty}) \\ (H^b, A, tb), x = \text{undefined} \rightarrow_s (H^r, A^r), ct \end{array}}{(H, A, tb), x = y(z_1, z_2) \rightarrow_s (H^r, A^r), ct}$$

$$\frac{\begin{array}{l} (H, A, tb), y \rightarrow_e v \quad (H, A, tb), z_1 \rightarrow_e v_1 \quad (H, A, tb), z_2 \rightarrow_e v_2 \quad v \in Loc \quad \text{IsCallable}(H, v) \quad v_2 \in Loc \\ H(v).[[\text{Code}]] = fv \quad \{\} :: H(v).[[\text{Scope}]] = A' \\ \text{NewLoc}() = l \quad H' = H[l \mapsto \text{NewArgObj}(v, \text{ParamsSize}(fv), H(v_2))] \\ \text{CreateBinding}(H', A', \text{arguments}, \text{eval}) = (H'', A'') \quad \text{SetBinding}(H'', A'', \text{arguments}, l, \text{strict}) = (H^f, A^f, v^f) \\ \text{GetThis}(H^f, v_1) = (H^t, l^t) \quad (H^t, A^f, l^t), \text{GetBody}(fv) \rightarrow_s (H^b, A^b), \text{Return}(v^b) \\ (H^b, A, tb), x = v^b \rightarrow_s (H^r, A^r), ct \end{array}}{(H, A, tb), x = y(z_1, z_2) \rightarrow_s (H^r, A^r), ct}$$

$$\frac{\begin{array}{l} (H, A, tb), y \rightarrow_e v \quad (H, A, tb), z_1 \rightarrow_e v_1 \quad (H, A, tb), z_2 \rightarrow_e v_2 \quad v \in Loc \quad \text{IsCallable}(H, v) \quad v_2 \in Loc \\ H(v).[[\text{Code}]] = fv \quad \{\} :: H(v).[[\text{Scope}]] = A' \\ \text{NewLoc}() = l \quad H' = H[l \mapsto \text{NewArgObj}(v, \text{ParamsSize}(fv), H(v_2))] \\ \text{CreateBinding}(H', A', \text{arguments}, \text{eval}) = (H'', A'') \quad \text{SetBinding}(H'', A'', \text{arguments}, l, \text{strict}) = (H^f, A^f, v^f) \\ \text{GetThis}(H^f, v_1) = (H^t, l^t) \quad (H^t, A^f, l^t), \text{GetBody}(fv) \rightarrow_s (H^b, A^b), \text{Normal}(-) \\ (H^b, A, tb), x = \text{undefined} \rightarrow_s (H^r, A^r), ct \end{array}}{(H, A, tb), x = y(z_1, z_2) \rightarrow_s (H^r, A^r), ct}$$

IRInternalCall(IRId lhs, IRId fun, IRExpr first, Option<IRId> second)

$$\begin{array}{c}
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} err}{(H, A, tb), \underline{x} = \diamond \text{toObject}(e) \rightarrow_{\underline{s}} (H, A), \text{Throw}(err)} \\
\\
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v \quad \text{ToObject}(H, v) = (H', err)}{(H, A, tb), \underline{x} = \diamond \text{toObject}(e) \rightarrow_{\underline{s}} (H, A), \text{Throw}(err)} \\
\\
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v \quad \text{ToObject}(H, v) = (H', l) \quad (H', A, tb), \underline{x} = l \rightarrow_{\underline{s}} (H'', A'), ct}{(H, A, tb), \underline{x} = \diamond \text{toObject}(e) \rightarrow_{\underline{s}} (H'', A'), ct} \\
\\
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} err}{(H, A, tb), \underline{x} = \diamond \text{isObject}(e) \rightarrow_{\underline{s}} (H, A), \text{Throw}(err)} \\
\\
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v \quad v \in \text{Loc} \quad (H, A, tb), \underline{x} = \text{true} \rightarrow_{\underline{s}} (H', A'), ct}{(H, A, tb), \underline{x} = \diamond \text{isObject}(e) \rightarrow_{\underline{s}} (H', A'), ct} \\
\\
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v \quad v \notin \text{Loc} \quad (H, A, tb), \underline{x} = \text{false} \rightarrow_{\underline{s}} (H', A'), ct}{(H, A, tb), \underline{x} = \diamond \text{isObject}(e) \rightarrow_{\underline{s}} (H', A'), ct} \\
\\
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} err}{(H, A, tb), \underline{x} = \diamond \text{toString}(e) \rightarrow_{\underline{s}} (H, A), \text{Throw}(err)} \\
\\
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v \quad (H, A, tb), \underline{x} = \text{ToString}(H, v) \rightarrow_{\underline{s}} (H', A'), ct}{(H, A, tb), \underline{x} = \diamond \text{toString}(e) \rightarrow_{\underline{s}} (H', A'), ct} \\
\\
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} err}{(H, A, tb), \underline{x} = \diamond \text{toNumber}(e) \rightarrow_{\underline{s}} (H, A), \text{Throw}(err)} \\
\\
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v \quad (H, A, tb), \underline{x} = \text{ToNumber}(H, v) \rightarrow_{\underline{s}} (H', A'), ct}{(H, A, tb), \underline{x} = \diamond \text{toNumber}(e) \rightarrow_{\underline{s}} (H', A'), ct} \\
\\
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} err}{(H, A, tb), \underline{x} = \diamond \text{toBoolean}(e) \rightarrow_{\underline{s}} (H, A), \text{Throw}(err)} \\
\\
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v \quad (H, A, tb), \underline{x} = \text{ToBoolean}(v) \rightarrow_{\underline{s}} (H', A'), ct}{(H, A, tb), \underline{x} = \diamond \text{toBoolean}(e) \rightarrow_{\underline{s}} (H', A'), ct} \\
\\
\frac{\text{Lookup}(H, A, y, \text{strict}) = l \quad (H, A, tb), \underline{x} = l \rightarrow_{\underline{s}} (H', A'), ct}{(H, A, tb), \underline{x} = \diamond \text{getBase}(y) \rightarrow_{\underline{s}} (H', A'), ct} \\
\\
\frac{\text{Lookup}(H, A, y, \text{strict}) = \sigma \quad (H, A, tb), \underline{x} = \# \text{Global} \rightarrow_{\underline{s}} (H', A'), ct}{(H, A, tb), \underline{x} = \diamond \text{getBase}(y) \rightarrow_{\underline{s}} (H', A'), ct} \\
\\
\frac{(H, A, tb), y \rightarrow_{\underline{e}} err}{(H, A, tb), \underline{x} = \diamond \text{iteratorInit}(y) \rightarrow_{\underline{s}} (H, A), \text{Throw}(err)} \\
\\
\frac{(H, A, tb), y \rightarrow_{\underline{e}} v \quad v \notin \text{Loc}}{(H, A, tb), \underline{x} = \diamond \text{iteratorInit}(y) \rightarrow_{\underline{s}} (H, A), \text{Throw}(\text{TypeError})} \\
\\
\frac{(H, A, tb), y \rightarrow_{\underline{e}} v \quad v \in \text{Loc} \quad \text{NewLoc}() = l \quad H' = H[l \mapsto \text{IteratorInit}(\text{CollectProps}(H, v))] \quad (H', A, tb), \underline{x} = l \rightarrow_{\underline{s}} (H'', A'), ct}{(H, A, tb), \underline{x} = \diamond \text{iteratorInit}(y) \rightarrow_{\underline{s}} (H'', A'), ct} \\
\\
\frac{(H, A, tb), y \rightarrow_{\underline{e}} err}{(H, A, tb), \underline{x} = \diamond \text{iteratorHasNext}(y, z) \rightarrow_{\underline{s}} (H, A), \text{Throw}(err)} \\
\\
\frac{(H, A, tb), y \rightarrow_{\underline{e}} v_1 \quad v_1 \notin \text{Loc}}{(H, A, tb), \underline{x} = \diamond \text{iteratorHasNext}(y, z) \rightarrow_{\underline{s}} (H, A), \text{Throw}(\text{TypeError})}
\end{array}$$

$$\begin{array}{c}
\frac{(H, A, tb), \underline{y} \rightarrow_e v \quad v \in Loc \quad (H, A, tb), \underline{z} \rightarrow_e err}{(H, A, tb), \underline{x} = \diamond \text{iteratorHasNext}(\underline{y}, \underline{z}) \rightarrow_s (H, A), \text{Throw}(err)} \\
\\
\frac{(H, A, tb), \underline{y} \rightarrow_e v_1 \quad v_1 \in Loc \quad (H, A, tb), \underline{z} \rightarrow_e v_2 \quad v_2 \notin Loc}{(H, A, tb), \underline{x} = \diamond \text{iteratorHasNext}(\underline{y}, \underline{z}) \rightarrow_s (H, A), \text{Throw}(\text{TypeError})} \\
\\
\frac{\text{Next}(H, H(v_2), H(v_2).\text{@property}("@i"), v_1) \in \text{Dom}(H(v_2)) \quad (H, A, tb), \underline{x} = \text{true} \rightarrow_s (H', A'), ct}{(H, A, tb), \underline{x} = \diamond \text{iteratorHasNext}(\underline{y}, \underline{z}) \rightarrow_s (H', A'), ct} \\
\\
\frac{\text{Next}(H, H(v_2), H(v_2).\text{@property}("@i"), v_1) \notin \text{Dom}(H(v_2)) \quad (H, A, tb), \underline{x} = \text{false} \rightarrow_s (H', A'), ct}{(H, A, tb), \underline{x} = \diamond \text{iteratorHasNext}(\underline{y}, \underline{z}) \rightarrow_s (H', A'), ct} \\
\\
\frac{(H, A, tb), \underline{y} \rightarrow_e err}{(H, A, tb), \underline{x} = \diamond \text{iteratorNext}(\underline{y}, \underline{z}) \rightarrow_s (H, A), \text{Throw}(err)} \\
\\
\frac{(H, A, tb), \underline{y} \rightarrow_e v_1 \quad v_1 \notin Loc}{(H, A, tb), \underline{x} = \diamond \text{iteratorNext}(\underline{y}, \underline{z}) \rightarrow_s (H, A), \text{Throw}(\text{TypeError})} \\
\\
\frac{(H, A, tb), \underline{y} \rightarrow_e v \quad v \in Loc \quad (H, A, tb), \underline{z} \rightarrow_e err}{(H, A, tb), \underline{x} = \diamond \text{iteratorNext}(\underline{y}, \underline{z}) \rightarrow_s (H, A), \text{Throw}(err)} \\
\\
\frac{(H, A, tb), \underline{y} \rightarrow_e v_1 \quad v_1 \in Loc \quad (H, A, tb), \underline{z} \rightarrow_e v_2 \quad v_2 \notin Loc}{(H, A, tb), \underline{x} = \diamond \text{iteratorNext}(\underline{y}, \underline{z}) \rightarrow_s (H, A), \text{Throw}(\text{TypeError})} \\
\\
\frac{\begin{array}{l} (H, A, tb), \underline{y} \rightarrow_e v_1 \quad (H, A, tb), \underline{z} \rightarrow_e v_2 \quad v_1 \in Loc \quad v_2 \in Loc \quad \text{Next}(H, H(v_2), H(v_2).\text{@property}("@i"), v_1) = i \\ H' = H[v_2 \mapsto H(v_2)[\text{@property} \mapsto H(v_2).\text{@property}["@i" \mapsto i + 1]] \quad (H', A, tb), \underline{x} = H(v_2).\text{@property}("i") \rightarrow_s (H'', A') \end{array}}{(H, A, tb), \underline{x} = \diamond \text{iteratorNext}(\underline{y}, \underline{z}) \rightarrow_s (H'', A'), ct}
\end{array}$$

**IRNew**(IRId lhs, IRId fun, List<IRId> args)

### 11.2.2 The new Operator

$$\frac{(H, A, tb), \underline{e} \rightarrow_e err}{(H, A, tb), \underline{x} = \text{new } \underline{e}(\underline{e}_1, \underline{e}_2) \rightarrow_s (H, A), \text{Throw}(err)}$$

$$\frac{(H, A, tb), \underline{e} \rightarrow_e v}{(H, A, tb), \underline{x} = \text{new } \underline{e} \rightarrow_s (H, A), \text{Throw}(err)}$$

$$\frac{(H, A, tb), \underline{e} \rightarrow_e err}{(H, A, tb), \underline{x} = \text{new } \underline{e} \rightarrow_s (H, A), \text{Throw}(err)}$$

$$\frac{(H, A, tb), \underline{e} \rightarrow_e v}{(H, A, tb), \underline{x} = \text{new } \underline{e} \rightarrow_s (H, A), \text{Throw}(err)}$$

**IRFunExpr**(IRId lhs, IRFunctional ftn)

### 11.2.5 Function Expressions

$$\frac{\begin{array}{l} \text{CreateImmutableBinding}(H, \{\} :: A, f, \text{eval}) = (H', A') \quad \text{NewFtnObject}(H', A', \text{function } \underline{f}(\underline{this}, \underline{arguments})\{\underline{s}\}) = (H'', l) \\ \text{InitializeImmutableBinding}(H'', A', f, l, \text{strict}) = (H^f, A^{f'}, err) \quad er :: A^f = A^{f'} \end{array}}{(H, A, tb), \underline{x} = \text{function } \underline{f}(\underline{this}, \underline{arguments})\{\underline{s}\} \rightarrow_s (H^f, A^{f'}), \text{Throw}(err)}$$

$$\frac{\begin{array}{l} \text{CreateImmutableBinding}(H, \{\} :: A, f, \text{eval}) = (H', A') \quad \text{NewFtnObject}(H', A', \text{function } \underline{f}(\underline{this}, \underline{arguments})\{\underline{s}\}) = (H'', l) \\ \text{InitializeImmutableBinding}(H'', A', f, l, \text{strict}) = (H^f, A^{f'}, v^f) \quad er :: A^f = A^{f'} \quad (H^f, A^f, tb), \underline{x} = l \rightarrow_s (H''', A''), ct \end{array}}{(H, A, tb), \underline{x} = \text{function } \underline{f}(\underline{this}, \underline{arguments})\{\underline{s}\} \rightarrow_s (H''', A''), ct}$$

```

IRFunDecl(IRFunctional ftn)
IRFunctional(IRId name, List<IRId> params, List<IRStmt> args,
            List<IRFunDecl> fds, List<IRVarStmt> vds, List<IRStmt> body)

```

### 13 Function Definition

#### 10.5 Declaration Binding Instantiation–Step 5

$$\begin{array}{c}
\text{NewFtnObject}(H, A, \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\}) = (H^f, l) \quad \neg \text{HasBinding}(A, \underline{f}) \\
\text{CreateBinding}(H^f, A, \underline{f}, \text{eval}) = (H', A') \quad \text{SetBinding}(H', A', \underline{f}, l, \text{strict}) = (H'', A'', \text{err}) \\
\hline
(H, A, tb), \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\} \rightarrow_{\underline{s}} (H'', A''), \text{Throw}(\text{err})
\end{array}$$

$$\begin{array}{c}
\text{NewFtnObject}(H, A, \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\}) = (H^f, l) \quad \neg \text{HasBinding}(A, \underline{f}) \\
\text{CreateBinding}(H^f, A, \underline{f}, \text{eval}) = (H', A') \quad \text{SetBinding}(H', A', \underline{f}, l, \text{strict}) = (H'', A'', v) \\
\hline
(H, A, tb), \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\} \rightarrow_{\underline{s}} (H'', A''), \text{Normal}(\text{empty})
\end{array}$$

$$\begin{array}{c}
\text{NewFtnObject}(H, A, \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\}) = (H^f, l) \quad \text{HasBinding}(A, \underline{f}) \quad A = \#Global \\
\text{GetProperty}(H, \#Global, \underline{f}) = (p, -) \quad p.[\text{Configurable}] \\
\{[\text{Value}] : \text{undefined}, [\text{Writable}] : \text{true}, [\text{Enumerable}] : \text{true}, [\text{Configurable}] : \text{eval}\} = dp \\
\text{DefineOwnProperty}(H^f, A, \#Global, \underline{f}, dp, \text{true}) = (H', A', \text{err}) \\
\hline
(H, A, tb), \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\} \rightarrow_{\underline{s}} (H', A'), \text{Throw}(\text{err})
\end{array}$$

$$\begin{array}{c}
\text{NewFtnObject}(H, A, \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\}) = (H^f, l) \quad \text{HasBinding}(A, \underline{f}) \quad A = \#Global \\
\text{GetProperty}(H, \#Global, \underline{f}) = (p, -) \quad p.[\text{Configurable}] \\
\{[\text{Value}] : \text{undefined}, [\text{Writable}] : \text{true}, [\text{Enumerable}] : \text{true}, [\text{Configurable}] : \text{eval}\} = dp \\
\text{DefineOwnProperty}(H^f, A, \#Global, \underline{f}, dp, \text{true}) = (H', A', v) \\
\text{SetBinding}(H', A', \underline{f}, l, \text{strict}) = (H'', A'', \text{err}) \\
\hline
(H, A, tb), \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\} \rightarrow_{\underline{s}} (H'', A''), \text{Throw}(\text{err})
\end{array}$$

$$\begin{array}{c}
\text{NewFtnObject}(H, A, \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\}) = (H^f, l) \quad \text{HasBinding}(A, \underline{f}) \quad A = \#Global \\
\text{GetProperty}(H, \#Global, \underline{f}) = (p, -) \quad p.[\text{Configurable}] \\
\{[\text{Value}] : \text{undefined}, [\text{Writable}] : \text{true}, [\text{Enumerable}] : \text{true}, [\text{Configurable}] : \text{eval}\} = dp \\
\text{DefineOwnProperty}(H^f, A, \#Global, \underline{f}, dp, \text{true}) = (H', A', v) \\
\text{SetBinding}(H', A', \underline{f}, l, \text{strict}) = (H'', A'', v') \\
\hline
(H, A, tb), \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\} \rightarrow_{\underline{s}} (H'', A''), \text{Normal}(\text{empty})
\end{array}$$

$$\begin{array}{c}
\text{NewFtnObject}(H, A, \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\}) = (H^f, l) \quad \text{HasBinding}(A, \underline{f}) \quad A = \#Global \\
\text{GetProperty}(H, \#Global, \underline{f}) = (p, -) \quad \neg p.[\text{Configurable}] \wedge (p \in \text{AccessorProp} \vee (\neg p.[\text{Writable}] \vee \neg p.[\text{Enumerable}]))) \\
\hline
(H, A, tb), \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\} \rightarrow_{\underline{s}} (H^f, A), \text{Throw}(\text{TypeError})
\end{array}$$

$$\begin{array}{c}
\text{NewFtnObject}(H, A, \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\}) = (H^f, l) \quad \text{HasBinding}(A, \underline{f}) \quad A = \#Global \\
\text{GetProperty}(H, \#Global, \underline{f}) = (p, -) \quad \neg p.[\text{Configurable}] \wedge \neg (p \in \text{AccessorProp} \vee (\neg p.[\text{Writable}] \vee \neg p.[\text{Enumerable}]))) \\
\text{SetBinding}(H^f, A, \underline{f}, l, \text{strict}) = (H', A', \text{err}) \\
\hline
(H, A, tb), \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\} \rightarrow_{\underline{s}} (H', A'), \text{Throw}(\text{err})
\end{array}$$

$$\begin{array}{c}
\text{NewFtnObject}(H, A, \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\}) = (H^f, l) \quad \text{HasBinding}(A, \underline{f}) \quad A = \#Global \\
\text{GetProperty}(H, \#Global, \underline{f}) = (p, -) \quad \neg p.[\text{Configurable}] \wedge \neg (p \in \text{AccessorProp} \vee (\neg p.[\text{Writable}] \vee \neg p.[\text{Enumerable}]))) \\
\text{SetBinding}(H^f, A, \underline{f}, l, \text{strict}) = (H', A', v) \\
\hline
(H, A, tb), \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\} \rightarrow_{\underline{s}} (H', A'), \text{Normal}(\text{empty})
\end{array}$$

$$\begin{array}{c}
\text{NewFtnObject}(H, A, \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\}) = (H^f, l) \\
\text{HasBinding}(A, \underline{f}) \quad A \neq \#Global \quad \text{SetBinding}(H^f, A, \underline{f}, l, \text{strict}) = (H', A', \text{err}) \\
\hline
(H, A, tb), \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\} \rightarrow_{\underline{s}} (H', A'), \text{Throw}(\text{err})
\end{array}$$

$$\begin{array}{c}
\text{NewFtnObject}(H, A, \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\}) = (H^f, l) \\
\text{HasBinding}(A, \underline{f}) \quad A \neq \#Global \quad \text{SetBinding}(H^f, A, \underline{f}, l, \text{strict}) = (H', A', v) \\
\hline
(H, A, tb), \text{function } \underline{f}(\underline{\text{this}}, \underline{\text{arguments}})\{\underline{s}\} \rightarrow_{\underline{s}} (H', A'), \text{Normal}(\text{empty})
\end{array}$$

IREval(IRId lhs, IRExpr arg)

IRBreak(IRId label)

#### 12.8 The break Statement

$(H, A, tb), \text{break } \underline{x} \rightarrow_{\underline{s}} (H, A), \text{Break}(\text{empty}, \underline{x})$

IRReturn(Option<IRExpr> expr)

#### 12.9 The return Statement

$(H, A, tb), \text{return } \rightarrow_{\underline{s}} (H, A), \text{Return}(\text{undefined})$

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} \text{err}}{(H, A, tb), \text{return } \underline{e} \rightarrow_{\underline{s}} (H, A), \text{Throw}(\text{err})}$$

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v}{(H, A, tb), \text{return } \underline{e} \rightarrow_{\underline{s}} (H, A), \text{Return}(v)}$$

IRWith(IRId id, IRStmt stmt)

#### 12.10 The with Statement

$$\frac{(H, A, tb), \underline{x} \rightarrow_{\underline{e}} \text{err}}{(H, A, tb), \text{with } (\underline{x}) \rightarrow_{\underline{s}} (H, A), \text{Throw}(\text{err})}$$

$$\frac{(H, A, tb), \underline{x} \rightarrow_{\underline{e}} v \quad \text{ToObject}(H, v) = (H', \text{err})}{(H, A, tb), \text{with } (\underline{x}) \rightarrow_{\underline{s}} (H', A), \text{Throw}(\text{err})}$$

$$\frac{(H, A, tb), \underline{x} \rightarrow_{\underline{e}} v \quad \text{ToObject}(H, v) = (H', l) \quad (H', l :: A, tb), \rightarrow_{\underline{s}} (H'', A'), ct}{(H, A, tb), \text{with } (\underline{x}) \rightarrow_{\underline{s}} (H'', A), ct}$$

IRLabelStmt(IRId label, IRStmt stmt)

#### 12.12 Labelled Statements

$$\frac{(H, A, tb), \rightarrow_{\underline{s}} (H', A'), \text{Break}(v, \underline{x})}{(H, A, tb), \underline{x}: \{\underline{s}\} \rightarrow_{\underline{s}} (H', A'), \text{Normal}(v)}$$

$$\frac{(H, A, tb), \rightarrow_{\underline{s}} (H', A'), ct \quad ct \neq \text{Break}(v, \underline{x})}{(H, A, tb), \underline{x}: \{\underline{s}\} \rightarrow_{\underline{s}} (H', A'), ct}$$

IRVarStmt(IRId lhs)

10.5 Declaration Binding Instantiation–Step 8: CreateMutableBinding( $N, D$ )  
SetMutableBinding( $N, V, S$ )

#### 12.2 Variable Statement

$$\frac{\text{CreateBinding}(H, A, \underline{x}, \text{eval}) = (H', A') \quad \text{SetBinding}(H', A', \underline{x}, \text{undefined}, \text{strict}) = (H'', A'', \text{err})}{(H, A, tb), \text{var } \underline{x} \rightarrow_{\underline{s}} (H'', A''), \text{Throw}(\text{err})}$$

$$\frac{\text{CreateBinding}(H, A, \underline{x}, \text{eval}) = (H', A') \quad \text{SetBinding}(H', A', \underline{x}, \text{undefined}, \text{strict}) = (H'', A'', v)}{(H, A, tb), \text{var } \underline{x} \rightarrow_{\underline{s}} (H'', A''), \text{Normal}(\text{empty})}$$

IRThrow (IRExpr expr)

12.13 The throw Statement

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} ve}{(H, A, tb), \text{throw } \underline{e} \rightarrow_{\underline{s}} (H, A), \text{Throw}(ve)}$$

IRSeq (List<IRStmt> stmts)

12.1 Block

$$(H, A, tb), \epsilon \rightarrow_{\underline{s}} (H, A), \text{Normal}(\text{empty})$$

$$\frac{(H, A, tb), \underline{s} \rightarrow_{\underline{s}} (H', A'), ac}{(H, A, tb), \underline{s} \underline{s}^* \rightarrow_{\underline{s}} (H', A'), ac}$$

$$\frac{(H, A, tb), \underline{s} \rightarrow_{\underline{s}} (H', A'), nc \quad (H', A', tb), \underline{s}^* \rightarrow_{\underline{s}} (H'', A''), \text{Throw}(ve)}{(H, A, tb), \underline{s} \underline{s}^* \rightarrow_{\underline{s}} (H'', A''), \text{Throw}(ve)}$$

$$\frac{(H, A, tb), \underline{s} \rightarrow_{\underline{s}} (H', A'), \text{Normal}(vt) \quad (H', A', tb), \underline{s}^* \rightarrow_{\underline{s}} (H'', A''), \text{Break}(\text{empty}, x)}{(H, A, tb), \underline{s} \underline{s}^* \rightarrow_{\underline{s}} (H'', A''), \text{Break}(vt, x)}$$

$$\frac{(H, A, tb), \underline{s} \rightarrow_{\underline{s}} (H', A'), nc \quad (H', A', tb), \underline{s}^* \rightarrow_{\underline{s}} (H'', A''), \text{Break}(v, x)}{(H, A, tb), \underline{s} \underline{s}^* \rightarrow_{\underline{s}} (H'', A''), \text{Break}(v, x)}$$

$$\frac{(H, A, tb), \underline{s} \rightarrow_{\underline{s}} (H', A'), nc \quad (H', A', tb), \underline{s}^* \rightarrow_{\underline{s}} (H'', A''), \text{Normal}(\text{empty})}{(H, A, tb), \underline{s} \underline{s}^* \rightarrow_{\underline{s}} (H'', A''), nc}$$

$$\frac{(H, A, tb), \underline{s} \rightarrow_{\underline{s}} (H', A'), nc \quad (H', A', tb), \underline{s}^* \rightarrow_{\underline{s}} (H'', A''), \text{Normal}(v)}{(H, A, tb), \underline{s} \underline{s}^* \rightarrow_{\underline{s}} (H'', A''), \text{Normal}(v)}$$

$$\frac{(H, A, tb), \underline{s} \rightarrow_{\underline{s}} (H', A'), \text{Normal}(vt) \quad (H', A', tb), \underline{s}^* \rightarrow_{\underline{s}} (H'', A''), \text{Return}(\text{empty})}{(H, A, tb), \underline{s} \underline{s}^* \rightarrow_{\underline{s}} (H'', A''), \text{Return}(vt)}$$

$$\frac{(H, A, tb), \underline{s} \rightarrow_{\underline{s}} (H', A'), nc \quad (H', A', tb), \underline{s}^* \rightarrow_{\underline{s}} (H'', A''), \text{Return}(v)}{(H, A, tb), \underline{s} \underline{s}^* \rightarrow_{\underline{s}} (H'', A''), \text{Return}(v)}$$

IRIf (IRExpr expr, IRStmt trueB, Option<IRStmt> falseB)

12.5 The if Statement

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} err}{(H, A, tb), \text{if } (\underline{e}) \text{ then } \underline{s}_1 \text{ (else } \underline{s}_2) \rightarrow_{\underline{s}} (H, A), \text{Throw}(err)}$$

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v \quad \text{ToBoolean}(v) = \text{true} \quad (H, A, tb), \underline{s}_1 \rightarrow_{\underline{s}} (H', A'), ct}{(H, A, tb), \text{if } (\underline{e}) \text{ then } \underline{s}_1 \text{ (else } \underline{s}_2) \rightarrow_{\underline{s}} (H', A'), ct}$$

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v \quad \text{ToBoolean}(v) = \text{false}}{(H, A, tb), \text{if } (\underline{e}) \text{ then } \underline{s}_1 \rightarrow_{\underline{s}} (H, A), \text{Normal}(\text{empty})}$$

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v \quad \text{ToBoolean}(v) = \text{false} \quad (H, A, tb), \underline{s}_2 \rightarrow_{\underline{s}} (H', A'), ct}{(H, A, tb), \text{if } (\underline{e}) \text{ then } \underline{s}_1 \text{ else } \underline{s}_2 \rightarrow_{\underline{s}} (H', A'), ct}$$

IRWhile(IRExpr cond, IRStmt body)

### 12.6.2 The while Statement

$$\begin{array}{c}
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} err}{(H, A, tb), \text{while } (\underline{e}) \xrightarrow{\underline{s}} (H, A), \text{Throw}(err)} \\
\\
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v \quad \text{ToBoolean}(v) = \text{false}}{(H, A, tb), \text{while } (\underline{e}) \xrightarrow{\underline{s}} (H, A), \text{Normal}(\text{empty})} \\
\\
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v \quad \text{ToBoolean}(v) = \text{true} \quad (H, A, tb), \underline{s} \rightarrow_{\underline{s}} (H', A'), ac}{(H, A, tb), \text{while } (\underline{e}) \xrightarrow{\underline{s}} (H', A'), ac} \\
\\
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v \quad \text{ToBoolean}(v) = \text{true} \quad (H, A, tb), \underline{s} \rightarrow_{\underline{s}} (H', A'), nc \quad (H', A', tb), \text{while } (\underline{e}) \xrightarrow{\underline{s}} (H'', A''), ac}{(H, A, tb), \text{while } (\underline{e}) \xrightarrow{\underline{s}} (H'', A''), ac} \\
\\
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v \quad \text{ToBoolean}(v) = \text{true} \quad (H, A, tb), \underline{s} \rightarrow_{\underline{s}} (H', A'), nc \quad (H', A', tb), \text{while } (\underline{e}) \xrightarrow{\underline{s}} (H'', A''), \text{Normal}(\text{empty})}{(H, A, tb), \text{while } (\underline{e}) \xrightarrow{\underline{s}} (H'', A''), nc} \\
\\
\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v \quad \text{ToBoolean}(v) = \text{true} \quad (H, A, tb), \underline{s} \rightarrow_{\underline{s}} (H', A'), nc \quad (H', A', tb), \text{while } (\underline{e}) \xrightarrow{\underline{s}} (H'', A''), \text{Normal}(v)}{(H, A, tb), \text{while } (\underline{e}) \xrightarrow{\underline{s}} (H'', A''), \text{Normal}(v)}
\end{array}$$

IRTry(IRStmt body, Option<IRId> name, Option<IRStmt> catchB, Option<IRStmt> finallyB)

### 12.14 The try Statement

$$\begin{array}{c}
\frac{(H, A, tb), \underline{s}_1 \rightarrow_{\underline{s}} (H', A'), \text{Throw}(ve) \quad \text{CreateBinding}(H', \{ \} :: A', x, \text{eval}) = (H'', A'') \quad \text{SetBinding}(H'', A'', x, \text{ExnLoc}(ve), \text{false}) = (H^x, A^x, err') \quad A^x = er :: A^f}{(H, A, tb), \text{try } \{ \underline{s}_1 \} \text{ catch } (\underline{x}) \{ \underline{s}_2 \} \rightarrow_{\underline{s}} (H^x, A^f), \text{Throw}(err')} \\
\\
\frac{(H, A, tb), \underline{s}_1 \rightarrow_{\underline{s}} (H', A'), \text{Throw}(ve) \quad \text{CreateBinding}(H', \{ \} :: A', x, \text{eval}) = (H'', A'') \quad \text{SetBinding}(H'', A'', x, \text{ExnLoc}(ve), \text{false}) = (H^x, A^x, v) \quad (H^x, A^x, tb), \underline{s}_2 \rightarrow_{\underline{s}} (H^c, A^c), ct \quad A^c = er :: A^f}{(H, A, tb), \text{try } \{ \underline{s}_1 \} \text{ catch } (\underline{x}) \{ \underline{s}_2 \} \rightarrow_{\underline{s}} (H^c, A^f), ct} \\
\\
\frac{(H, A, tb), \underline{s}_1 \rightarrow_{\underline{s}} (H', A'), ct \quad ct \neq \text{Throw}(ve)}{(H, A, tb), \text{try } \{ \underline{s}_1 \} \text{ catch } (\underline{x}) \{ \underline{s}_2 \} \rightarrow_{\underline{s}} (H', A'), ct} \\
\\
\frac{(H, A, tb), \underline{s}_1 \rightarrow_{\underline{s}} (H', A'), ct \quad (H', A', tb), \underline{s}_2 \rightarrow_{\underline{s}} (H'', A''), nc}{(H, A, tb), \text{try } \{ \underline{s}_1 \} \text{ finally } \{ \underline{s}_2 \} \rightarrow_{\underline{s}} (H'', A''), ct} \\
\\
\frac{(H, A, tb), \underline{s}_1 \rightarrow_{\underline{s}} (H', A'), ct \quad (H', A', tb), \underline{s}_2 \rightarrow_{\underline{s}} (H'', A''), ac}{(H, A, tb), \text{try } \{ \underline{s}_1 \} \text{ finally } \{ \underline{s}_2 \} \rightarrow_{\underline{s}} (H'', A''), ac} \\
\\
\frac{(H, A, tb), \underline{s}_1 \rightarrow_{\underline{s}} (H', A'), \text{Throw}(ve) \quad \text{CreateBinding}(H', \{ \} :: A', x, \text{eval}) = (H'', A'') \quad \text{SetBinding}(H'', A'', x, \text{ExnLoc}(ve), \text{false}) = (H^x, A^x, err') \quad A^x = er :: A^f}{(H, A, tb), \text{try } \{ \underline{s}_1 \} \text{ catch } (\underline{x}) \{ \underline{s}_2 \} \text{ finally } \{ \underline{s}_3 \} \rightarrow_{\underline{s}} (H^x, A^f), \text{Throw}(err')} \\
\\
\frac{(H, A, tb), \underline{s}_1 \rightarrow_{\underline{s}} (H', A'), \text{Throw}(ve) \quad \text{CreateBinding}(H', \{ \} :: A', x, \text{eval}) = (H'', A'') \quad \text{SetBinding}(H'', A'', x, \text{ExnLoc}(ve), \text{false}) = (H^x, A^x, v) \quad (H^x, A^x, tb), \underline{s}_2 \rightarrow_{\underline{s}} (H^c, A^c), ct \quad A^c = er :: A^{c'} \quad (H^c, A^{c'}, tb), \underline{s}_3 \rightarrow_{\underline{s}} (H^f, A^f), nc}{(H, A, tb), \text{try } \{ \underline{s}_1 \} \text{ catch } (\underline{x}) \{ \underline{s}_2 \} \text{ finally } \{ \underline{s}_3 \} \rightarrow_{\underline{s}} (H^f, A^f), ct} \\
\\
\frac{(H, A, tb), \underline{s}_1 \rightarrow_{\underline{s}} (H', A'), \text{Throw}(ve) \quad \text{CreateBinding}(H', \{ \} :: A', x, \text{eval}) = (H'', A'') \quad \text{SetBinding}(H'', A'', x, \text{ExnLoc}(ve), \text{false}) = (H^x, A^x, v) \quad (H^x, A^x, tb), \underline{s}_2 \rightarrow_{\underline{s}} (H^c, A^c), ct \quad A^c = er :: A^{c'} \quad (H^c, A^{c'}, tb), \underline{s}_3 \rightarrow_{\underline{s}} (H^f, A^f), ac}{(H, A, tb), \text{try } \{ \underline{s}_1 \} \text{ catch } (\underline{x}) \{ \underline{s}_2 \} \text{ finally } \{ \underline{s}_3 \} \rightarrow_{\underline{s}} (H^f, A^f), ac}
\end{array}$$

$$\frac{(H, A, tb), \underline{s_1} \rightarrow_s (H', A'), ct \quad ct \neq \text{Throw}(ve) \quad (H', A', tb), \underline{s_3} \rightarrow_s (H'', A''), nc}{(H, A, tb), \text{try } \{\underline{s_1}\} \text{ catch } (\underline{x})\{\underline{s_2}\} \text{ finally } \{\underline{s_3}\} \rightarrow_s (H'', A''), ct}$$

$$\frac{(H, A, tb), \underline{s_1} \rightarrow_s (H', A'), ct \quad ct \neq \text{Throw}(ve) \quad (H', A', tb), \underline{s_3} \rightarrow_s (H'', A''), ac}{(H, A, tb), \text{try } \{\underline{s_1}\} \text{ catch } (\underline{x})\{\underline{s_2}\} \text{ finally } \{\underline{s_3}\} \rightarrow_s (H'', A''), ac}$$

`IRStmtUnit(List<IRStmt> stmts)`

### 5.4.3 Expressions

$$\boxed{(H, A, tb), \underline{e} \rightarrow_e ve}$$

`IRBin(IRExpr first, IROp op, IRExpr second)`

#### 11.8.6 The instanceof operator

$$\frac{(H, A, tb), \underline{e_1} \rightarrow_e err}{(H, A, tb), \underline{e_1} \text{ instanceof } \underline{e_2} \rightarrow_e err}$$

$$\frac{(H, A, tb), \underline{e_1} \rightarrow_e v \quad (H, A, tb), \underline{e_2} \rightarrow_e err}{(H, A, tb), \underline{e_1} \text{ instanceof } \underline{e_2} \rightarrow_e err}$$

$$\frac{(H, A, tb), \underline{e_1} \rightarrow_e v_1 \quad (H, A, tb), \underline{e_2} \rightarrow_e v_2 \quad v_2 \notin Loc}{(H, A, tb), \underline{e_1} \text{ instanceof } \underline{e_2} \rightarrow_e \text{TypeError}}$$

#### 15.3.5.3 [[HasInstance]] (V)

Instead of checking whether  $v_2$  has a `[[HasInstance]]` internal method, we check whether  $v_2$  is a function object.

$$\frac{(H, A, tb), \underline{e_1} \rightarrow_e v_1 \quad (H, A, tb), \underline{e_2} \rightarrow_e v_2 \quad v_2 \in Loc \quad \neg \text{IsCallable}(H, v_2)}{(H, A, tb), \underline{e_1} \text{ instanceof } \underline{e_2} \rightarrow_e \text{TypeError}}$$

$$\frac{(H, A, tb), \underline{e_1} \rightarrow_e v_1 \quad (H, A, tb), \underline{e_2} \rightarrow_e v_2 \quad v_2 \in Loc \quad \text{IsCallable}(H, v_2) \quad v_1 \notin Loc}{(H, A, tb), \underline{e_1} \text{ instanceof } \underline{e_2} \rightarrow_e \text{false}}$$

$$\frac{(H, A, tb), \underline{e_1} \rightarrow_e v_1 \quad (H, A, tb), \underline{e_2} \rightarrow_e v_2 \quad v_2 \in Loc \quad \text{IsCallable}(H, v_2) \quad v_1 \in Loc}{(H, A, tb), \underline{e_1} \text{ instanceof } \underline{e_2} \rightarrow_e \text{Inherit}(H, v_1, v_2)}$$

#### 11.8.7 The in operator

$$\frac{(H, A, tb), \underline{e_1} \rightarrow_e err}{(H, A, tb), \underline{e_1} \text{ in } \underline{e_2} \rightarrow_e err}$$

$$\frac{(H, A, tb), \underline{e_1} \rightarrow_e v \quad (H, A, tb), \underline{e_2} \rightarrow_e err}{(H, A, tb), \underline{e_1} \text{ in } \underline{e_2} \rightarrow_e err}$$

$$\frac{(H, A, tb), \underline{e_1} \rightarrow_e v_1 \quad (H, A, tb), \underline{e_2} \rightarrow_e v_2 \quad v_2 \notin Loc}{(H, A, tb), \underline{e_1} \text{ in } \underline{e_2} \rightarrow_e \text{TypeError}}$$

$$\frac{(H, A, tb), \underline{e_1} \rightarrow_e v_1 \quad (H, A, tb), \underline{e_2} \rightarrow_e v_2 \quad v_2 \in Loc}{(H, A, tb), \underline{e_1} \text{ in } \underline{e_2} \rightarrow_e \text{HasProperty}(H, v_2, \text{ToString}(H, v_1))}$$



`IRUn(IROp op, IRExpr expr)`

#### 11.4.2 The `void` Operator

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} err}{(H, A, tb), \text{void } \underline{e} \rightarrow_{\underline{e}} err}$$

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v}{(H, A, tb), \text{void } \underline{e} \rightarrow_{\underline{e}} \text{undefined}}$$

#### 11.4.3 The `typeof` Operator

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} err}{(H, A, tb), \text{typeof } \underline{e} \rightarrow_{\underline{e}} \text{undefined}}$$

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v}{(H, A, tb), \text{typeof } \underline{e} \rightarrow_{\underline{e}} \text{TypeTag}(H, v)}$$

#### 11.4.6 Unary `+` Operator

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} err}{(H, A, tb), + \underline{e} \rightarrow_{\underline{e}} err}$$

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v}{(H, A, tb), + \underline{e} \rightarrow_{\underline{e}} \text{ToNumber}(H, v)}$$

#### 11.4.7 Unary `-` Operator

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} err}{(H, A, tb), - \underline{e} \rightarrow_{\underline{e}} err}$$

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v}{(H, A, tb), - \underline{e} \rightarrow_{\underline{e}} \text{Negate}(\text{ToNumber}(H, v))}$$

#### 11.4.8 Bitwise NOT Operator (`~`)

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} err}{(H, A, tb), \sim \underline{e} \rightarrow_{\underline{e}} err}$$

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v}{(H, A, tb), \sim \underline{e} \rightarrow_{\underline{e}} \sim (\text{ToInt32}(H, v))}$$

#### 11.4.9 Logical NOT Operator (`!`)

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} err}{(H, A, tb), ! \underline{e} \rightarrow_{\underline{e}} err}$$

$$\frac{(H, A, tb), \underline{e} \rightarrow_{\underline{e}} v}{(H, A, tb), ! \underline{e} \rightarrow_{\underline{e}} \text{Negate}(\text{ToBoolean}(v))}$$

IRLoad(IRId obj, IRExpr index)

#### 11.2.1 Property Accessors: IRLoad

$$\frac{(H, A, tb), \underline{x} \rightarrow_{\underline{e}} err}{(H, A, tb), \underline{x}[\underline{e}] \rightarrow_{\underline{e}} err}$$
$$\frac{(H, A, tb), \underline{x} \rightarrow_{\underline{e}} v \quad (H, A, tb), \underline{e} \rightarrow_{\underline{e}} err}{(H, A, tb), \underline{x}[\underline{e}] \rightarrow_{\underline{e}} err}$$
$$\frac{(H, A, tb), \underline{x} \rightarrow_{\underline{e}} v_1 \quad (H, A, tb), \underline{e} \rightarrow_{\underline{e}} v_2 \quad CheckObjectCoercible(v_1) = err}{(H, A, tb), \underline{x}[\underline{e}] \rightarrow_{\underline{e}} err}$$
$$\frac{(H, A, tb), \underline{x} \rightarrow_{\underline{e}} v_1 \quad (H, A, tb), \underline{e} \rightarrow_{\underline{e}} v_2 \quad CheckObjectCoercible(v_1) \neq err \quad ToObject(H, v_1) = (H', l)}{(H, A, tb), \underline{x}[\underline{e}] \rightarrow_{\underline{e}} Get(H', l, ToString(H', v_2))}$$

IRUserId(String text)

IRTmpId(String text)

#### 11.1.2 Identifier Reference

#### 10.3.1 Identifier Resolution

#### 10.2.2.1 GetIdentifierReference(lex, name, strict)

$$(H, A, tb), \underline{x} \rightarrow_{\underline{e}} GetBindingValue(H, Lookup(H, A, \underline{x}, \text{strict}), \underline{x}, \text{strict})$$

IRNumber(ignoreForEquals String text, Double num)

#### 11.1.3 Literal Reference

#### 7.8 Literals

$$(H, A, tb), n \rightarrow_{\underline{e}} n$$

IRString(String str)

$$(H, A, tb), s \rightarrow_{\underline{e}} s$$

IRBool(boolean bool)

$$(H, A, tb), \text{true} \rightarrow_{\underline{e}} \text{true}$$
$$(H, A, tb), \text{false} \rightarrow_{\underline{e}} \text{false}$$

IRUndef()

$$(H, A, tb), \text{undefined} \rightarrow_{\underline{e}} \text{undefined}$$

IRNull()

$$(H, A, tb), \text{null} \rightarrow_{\underline{e}} \text{null}$$

IRThis()

#### 11.1.1 The this Keyword

$$(H, A, tb), \text{this} \rightarrow_{\underline{e}} tb$$

## 5.4.4 Members

$(H, A, tb), \underline{m} \rightarrow_{\underline{m}} (H, \underline{x}, ov) \text{ or } err$

**IRField**(IRId prop, IRExpr expr)

11.1.5 Object Initialiser

$$\frac{(H, A, tb), y \rightarrow_e err}{(H, A, tb), \underline{x} : y \rightarrow_{\underline{m}} err}$$

$$\frac{(H, A, tb), y \rightarrow_e v \quad \{[[\text{Value}]] : v, [[\text{Writable}]] : \text{true}, [[\text{Enumerable}]] : \text{true}, [[\text{Configurable}]] : \text{true}\} = dp}{(H, A, tb), \underline{x} : y \rightarrow_{\underline{m}} (H, \underline{x}, dp)}$$

**IRGetProp**(IRFunctional ftn)

$$\frac{NewFtnObject(H, A, \text{get } \underline{f}(\underline{this}, \underline{arguments})\{\underline{s}\}) = (H', l) \quad \{[[\text{Get}]] : l, [[\text{Enumerable}]] : \text{true}, [[\text{Configurable}]] : \text{true}\} = ap}{(H, A, tb), \text{get } \underline{f}(\underline{this}, \underline{arguments})\{\underline{s}\} \rightarrow_{\underline{m}} (H', \underline{f}, ap)}$$

**IRSetProp**(IRFunctional ftn)

$$\frac{NewFtnObject(H, A, \text{set } \underline{f}(\underline{this}, \underline{arguments})\{\underline{s}\}) = (H', l) \quad \{[[\text{Set}]] : l, [[\text{Enumerable}]] : \text{true}, [[\text{Configurable}]] : \text{true}\} = ap}{(H, A, tb), \text{set } \underline{f}(\underline{this}, \underline{arguments})\{\underline{s}\} \rightarrow_{\underline{m}} (H', \underline{f}, ap)}$$

# Chapter 6

## CFG

### 6.1 Settings

```
.../jsaf/analysis/cfg/{package, CFG, CFGId}.scala
```

$P$	$\in$	Program	=	$\wp(\text{FunctionId} \times \text{ArgumentsName} \times \text{ArgVars} \times \text{LocalVars}) \times \text{Graph}$
$fid$	$\in$	FunctionId	::=	$fid_{global} \mid fid_1 \mid \dots$
		VarKind	::=	GlobalVar $\mid$ PureLocalVar $\mid$ CapturedVar $\mid$ CapturedCatchVar
		ArgVars, LocalVars	::=	$x^*$
		ArgumentsName	=	String
$G, \langle C, \hookrightarrow, \overset{\text{exc}}{\hookrightarrow}, \mathbb{A} \rangle$	$\in$	Graph	=	$\wp(\text{Node}) \times \wp(\text{Edge}) \times \wp(\text{Edge}) \times \wp(\text{Call})$
$n$	$\in$	Node	=	FunctionId $\times$ Label
		Edge, Call	=	Node $\times$ Node
		Label	::=	ENTRY $\mid$ EXIT $\mid$ EXIT-EXC $\mid$ $c_1 \mid \dots$
		Label	=	LEntry $\mid$ LExit $\mid$ LExitExc $\mid$ LBlock(id : BlockId)

A call expression splits into a pair of call and after-call nodes in this flow graph, and there is no edge between the pair. In order to treat them as a call-site and a return-site of the call, the pair  $(cp_{call}, cp_{after-call})$  must be recorded in  $\mathbb{A}$  as an element.

### 6.2 Helper Functions

```
.../jsaf/analysis/cfg/CFG.scala
```

$\underline{\text{getCmd}}_P$	:	Node $\rightarrow$ Command
$\underline{\text{getArgVars}}_P$	:	FunctionId $\rightarrow$ ArgVars
$\underline{\text{getLocalVars}}_P$	:	FunctionId $\rightarrow$ LocalVars
$\underline{\text{getCallFromAftercall}}_P$	:	Node $\rightarrow$ Node
$\underline{\text{getAftercallFromCall}}_P$	:	Node $\rightarrow$ Node
$\underline{\text{getExcSucc}}_P$	:	Node $\rightarrow$ Node
$\underline{\text{getArgumentsName}}_P$	:	FunctionId $\rightarrow$ String
$\underline{\text{getReturnVar}}_P$	:	Node $\rightarrow$ String
$\underline{\text{getVarKind}}_P$	:	String $\rightarrow$ VarKind
$\underline{\text{isUserFunction}}_P$	:	FunctionId $\rightarrow$ Boolean

### 6.3 Syntax of Command

```
.../jsaf/analysis/cfg/{CFG, CFGInst, CFGExpr}.scala
```

$c \in \text{Command} ::=$	entry	Entry	entry node
	exit	Exit	exit node
	exit-exc	ExitExc	exit node for exception
	$i^+$	Block	basic block
$i \in \text{Instruction} ::=$	$x := \text{alloc}(e^?)$	CFGAlloc	
	$x := \text{allocArray}(n)$	CFGAllocArray	
	$x := \text{allocArg}(n)$	CFGAllocArg	
	$x := e$	CFGExprStmt	
	$x := \text{delete}(e)$	CFGDelete	
	$x := \text{delete}(e_1, e_2)$	CFGDeleteProp	
	$e[e] := e$	CFGStore	
	$x_1 := \text{function } x_2^? (fid)$	CFGFunExpr	
	$\text{construct}(e_1, e_2, e_3)$	CFGConstruct	
	$\text{call}(e_1, e_2, e_3)$	CFGCall	
	$\text{assert}(e \otimes e)$	CFGAssert	
	$\text{catch}(x)$	CFGCatch	
	$\text{return}(e^?)$	CFGReturn	
	$\text{throw}(e)$	CFGThrow	
	$x := \diamond x(x^*)$	CFGInternalCall	
	noop	CFGNoOp	
$e \in \text{Expression} ::=$	$x$	CFGVarRef	
	$e \otimes e$	CFGBin	
	$\ominus e$	CFGUn	
	$e[e]$	CFGLoad	
	$n$	CFGNumber	Number, double
	$"s"$	CFGString	String
	true, false	CFGBool	Boolean
	null	CFGNull	
	this	CFGThis	
$\ominus ::=$	void   typeof   +   -   ~   !		
$\otimes ::=$	instanceof   in     &   ^   <<   >>   >>>   +   -   *   /   %   ==   !=   ===		
	!=   <   >   <=   >=		

# Chapter 7

## IR to CFG

### 7.1 Constraints

- There is no instruction after `call` or `return` in a node. There is no instruction before `catch` in a node.
  - $\forall n \in \text{nodes}. (i_k \in n \wedge (i_k = \text{call} \vee i_k = \text{return})) \rightarrow \neg(\exists i_{k'} \in n. k < k')$
  - $\forall n \in \text{nodes}. (i_k \in n \wedge (i_k = \text{catch})) \rightarrow \neg(\exists i_{k'} \in n. k > k')$
- An `entry` node has no predecessor, `exit` and `exit-exc` nodes have no successor.
  - $\forall (n_1, n_2) \in \hookrightarrow. n_1 \neq \text{exit} \wedge n_1 \neq \text{exit-exc} \wedge n_2 \neq \text{entry}$
- A call expression splits into a pair of call and after-call nodes in this flow graph, and there is no edge between the pair. In order to treat them as a call-site and a return-site of the call, the pair  $(cp_{\text{call}}, cp_{\text{after-call}})$  must be recorded in  $\mathbb{A}$  as an element.
  - $\forall n \in \mathbb{C}. ((\text{LastInstOf}(n) = \text{call}) \rightarrow \exists n' \in \mathbb{C}. ((n, n') \in \mathbb{A} \wedge n \not\hookrightarrow n'))$
  - $\forall (n_1, n_2), (n'_1, n'_2) \in \mathbb{A}. n_1 = n'_1 \Leftrightarrow n_2 = n'_2$

### 7.2 Translation

.../jsaf/analysis/cfg/CFG.scala

## 7.2.1 Data Type

$G \in \text{CFG}$	:	$\left\{ \begin{array}{ll} \text{nodes} & : \text{Node list} \\ \text{succMap} & : \text{Node} \mapsto \text{Node set} \\ \text{predMap} & : \text{Node} \mapsto \text{Node set} \\ \text{excSuccMap} & : \text{Node} \mapsto \text{Node} \\ \text{excPredMap} & : \text{Node} \mapsto \text{Node set} \\ \text{callFromAftercallMap} & : \text{Node} \mapsto \text{Node} \\ \text{aftercallFromCallMap} & : \text{Node} \mapsto \text{Node} \\ \text{callFromAftercatchMap} & : \text{Node} \mapsto \text{Node} \\ \text{aftercatchFromCallMap} & : \text{Node} \mapsto \text{Node} \\ \text{cmdMap} & : \text{Node} \mapsto \text{Cmd} \\ \text{funcMap} & : \text{FunctionId} \mapsto \text{ArgumentsName} \times \text{ArgVars} \times \text{LocalVars} \\ \text{returnVarMap} & : \text{Node} \mapsto \text{CFGId} \end{array} \right\}$
		$\left\{ \begin{array}{ll} \text{NewFunction} & : \text{ArgumentsName} \times \text{ArgVars} \times \text{LocalVars} \rightarrow \text{FunctionId} \\ \text{NewBlock} & : \text{FunctionId} \rightarrow \text{BlockNode} \\ \text{NewAfterCallBlock} & : \text{FunctionId} \times \text{CFGId} \rightarrow \text{BlockNode} \\ \text{NewAfterCatchBlock} & : \text{FunctionId} \rightarrow \text{BlockNode} \\ \text{AddInst} & : \text{BlockNode} \times \text{CFGInst} \rightarrow \text{Unit} \\ \text{AddEdge} & : \text{Node} \times \text{Node} \rightarrow \text{Unit} \\ \text{AddEdge} & : \text{Node list} \times \text{Node} \rightarrow \text{Unit} \\ \text{AddExcEdge} & : \text{Node} \times \text{Node} \rightarrow \text{Unit} \\ \text{AddExcEdge} & : \text{Node list} \times \text{Node} \rightarrow \text{Unit} \\ \text{AddCall} & : \text{Node} \times \text{Node} \times \text{Node} \rightarrow \text{Unit} \end{array} \right\}$

Node	=	FunctionId $\times$ Label
$fid \in \text{FunctionId}$	=	Int
$\#name \in \text{Label}$	=	{LEntry, LExit, LExitExc} $\cup$ LabelBlock
BlockNode	=	FunctionId $\times$ LabelBlock
LabelBlock	=	Int
Cmd	=	{Entry, Exit, ExitExc} $\cup$ Block
Block	=	CFGInst list
ArgumentsName	=	String
ArgVars	=	CFGId list
LocalVars	=	CFGId list

## 7.2.2 CFG Methods

$\text{NewFunction}(\text{argsName}, \text{argVars}, \text{localVars}) = fid \stackrel{\text{let}}{=} \text{newFunctionId}()$   
 $\text{funcMap} \leftarrow \text{funcMap}[fid \mapsto (\text{argsName}, \text{argVars}, \text{localVars})]$   
 $\text{nodes} \leftarrow (fid, \text{LEntry}) :: \text{nodes}$   
 $\text{cmdMap} \leftarrow \text{cmdMap}[(fid, \text{LEntry}) \mapsto \text{Entry}]$   
 $\text{nodes} \leftarrow (fid, \text{LExit}) :: \text{nodes}$   
 $\text{cmdMap} \leftarrow \text{cmdMap}[(fid, \text{LExit}) \mapsto \text{Exit}]$   
 $\text{nodes} \leftarrow (fid, \text{LExitExc}) :: \text{nodes}$   
 $\text{cmdMap} \leftarrow \text{cmdMap}[(fid, \text{LExitExc}) \mapsto \text{ExitExc}]$   
 $fid$   
  
 $\text{SetGlobalFId}(fid) = \text{globalFId} \leftarrow fid$

```

NewBlock(fid)      = bid  $\stackrel{\text{let}}{=}$  newBlockId()
                   blockNode  $\stackrel{\text{let}}{=}$  (fid, bid)
                   nodes  $\leftarrow$  blockNode :: nodes
                   cmdMap  $\leftarrow$  cmdMap[blockNode  $\mapsto$  []]
                   blockNode

NewAfterCallBlock(fid, x) = blockNode  $\stackrel{\text{let}}{=}$  NewBlock(fid)
                           returnVarMap  $\leftarrow$  returnVarMap[blockNode  $\mapsto$  x]
                           blockNode

NewAfterCatchBlock(fid) = NewBlock(fid)

AddInst(blockNode, inst) = block  $\stackrel{\text{let}}{=}$  cmdMap(blockNode)
                           cmdMap  $\leftarrow$  cmdMap[blockNode  $\mapsto$  block@[inst]]

AddEdge(n1, n2)      = if (succMap(n1)  $\neq$  null) then
                           succMap  $\leftarrow$  succMap[n1  $\mapsto$  {n2}  $\cup$  succMap(n1)]
                           predMap  $\leftarrow$  predMap[n2  $\mapsto$  {n1}  $\cup$  predMap(n2)]
                           else succMap  $\leftarrow$  succMap[n1  $\mapsto$  {n2}]
                           predMap  $\leftarrow$  predMap[n2  $\mapsto$  {n1}]
AddEdge(N, n2)      = Iter(N)( $\lambda$  n  $\Rightarrow$  AddEdge(n, n2))

AddExcEdge(n1, n2)    = if (excSuccMap(n1)  $\neq$  null) then
                           excSuccMap  $\leftarrow$  excSuccMap[n1  $\mapsto$  {n2}  $\cup$  excSuccMap(n1)]
                           excPredMap  $\leftarrow$  excPredMap[n2  $\mapsto$  {n1}  $\cup$  excPredMap(n2)]
                           else excSuccMap  $\leftarrow$  excSuccMap[n1  $\mapsto$  {n2}]
                           excPredMap  $\leftarrow$  excPredMap[n2  $\mapsto$  {n1}]
AddExcEdge(N, n2)    = Iter(N)( $\lambda$  n  $\Rightarrow$  AddExcEdge(n, n2))

AddCall(n1, n2)      = if (aftercallFromCallMap(n1)  $\neq$  null) then
                           aftercallFromCallMap  $\leftarrow$  aftercallFromCallMap[n1  $\mapsto$  {n2}  $\cup$  aftercallFromCallMap(n1)]
                           callFromAftercallMap  $\leftarrow$  callFromAftercallMap[n1  $\mapsto$  {n2}  $\cup$  callFromAftercallMap(n1)]
                           if (aftercatchFromCallMap(n1)  $\neq$  null) then
                               aftercatchFromCallMap  $\leftarrow$  aftercatchFromCallMap[n1  $\mapsto$  {n3}  $\cup$  aftercatchFromCallMap(n1)]
                               callFromAftercatchMap  $\leftarrow$  callFromAftercatchMap[n1  $\mapsto$  {n3}  $\cup$  callFromAftercatchMap(n1)]

```



### 7.2.3 Helper Functions

$Fold(A)(b)(f) : \text{Any list} \times \text{Any}' \times (\text{Any} \times \text{Any}' \rightarrow \text{Any}') \rightarrow \text{Any}'$   
 $= \text{if } (Length(A) = 0) \text{ then } b$   
 $\quad \text{else } Fold(TailOf(A))(f(HeadOf(A), b))(f)$

$Iter(A)(f) : \text{Any list} \times (\text{Any} \rightarrow \text{Unit}) \rightarrow \text{Unit}$   
 $= \text{if } (Length(A) = 0) \text{ then unit}$   
 $\quad \text{else } f(HeadOf(A))$   
 $\quad \quad Iter(TailOf(A))(f)$

$GetTail(G, N)(fid) : \text{CFG} \times \text{Node list} \times \text{FunctionId} \rightarrow \text{BlockNode}$   
 $= \text{if } (Length(N) = 1) \text{ then}$   
 $\quad HeadOf(N)$   
 $\quad \text{else if } (Length(N) = 0) \text{ then}$   
 $\quad \quad n \stackrel{let}{=} G.NewBlock(fid)$   
 $\quad \quad n$   
 $\quad \text{else } n \stackrel{let}{=} G.NewBlock(fid)$   
 $\quad \quad G.AddEdge(N, n)$   
 $\quad \quad n$

$ToString(l) : \text{Label} \rightarrow \text{String}$   
 $= l.getId().getText()$

### 7.2.4 Translation Rules

$L \in \text{LabelMap} : \text{String} \mapsto \text{Node set}$   
 $\llbracket - \rrbracket_{root} : \text{IRRoot} \rightarrow \text{CFG}$   
 $\llbracket - \rrbracket_{fdvars} : \text{IRFunDecl list} \rightarrow \text{LocalVars}$   
 $\llbracket - \rrbracket_{vds} : \text{IRVarStmt list} \rightarrow \text{LocalVars}$   
 $\llbracket - \rrbracket_{args} : \text{IRStmt list} \rightarrow \text{ArgVars}$   
 $\llbracket - \rrbracket_{fd} : \text{IRFunDecl} \times \text{CFG} \times \text{Node list} \times \text{FunctionId} \rightarrow \text{Node list}$   
 $\llbracket - \rrbracket_{stmt} : \text{IRStmt} \times \text{CFG} \times \text{Node list} \times \text{LabelMap} \times \text{FunctionId} \rightarrow \text{Node list} \times \text{LabelMap}$   
 $\llbracket - \rrbracket_{mem} : \text{IRField} \times \text{CFG} \times \text{Node} \times \text{IRId} \rightarrow \text{Unit}$   
 $\llbracket - \rrbracket_{elem} : \text{IRExpr} \times \text{CFG} \times \text{Node} \times \text{IRId} \times \text{Int} \rightarrow \text{Int}$

$$\begin{aligned}
\llbracket \text{IRRoot}(fd^*, vd^*, stmt^*) \rrbracket_{root} &= G \leftarrow \text{new CFG}() \\
&\quad argVars \stackrel{let}{=} [] \\
&\quad localVars \stackrel{let}{=} \llbracket fd^* \rrbracket_{fdvars} @ \llbracket vd^* \rrbracket_{vds} \\
&\quad fid_{global} \stackrel{let}{=} G.NewFunction(“”, argVars, localVars) \\
&\quad G.SetGlobalFid(fid_{global}) \\
&\quad n_{start} \stackrel{let}{=} G.NewBlock(fid_{global}) \\
&\quad G.AddEdge((fid_{global}, LEntry), n_{start}) \\
&\quad N_1 \stackrel{let}{=} \llbracket fd^* \rrbracket_{fd^*}(G, [n_{start}]) (fid_{global}) \\
&\quad L \stackrel{let}{=} [ \#return \mapsto [], \#throw \mapsto [], \#throw\_end \mapsto [], \#after\_catch \mapsto [] ] \\
&\quad (N_2, L_1) \stackrel{let}{=} \llbracket stmt^* \rrbracket_{stmt^*}(G, N_1, L) (fid_{global}) \\
&\quad G.AddEdge(N_2, (fid_{global}, LExit)) \\
&\quad G.AddEdge(L_1(\#return), (fid_{global}, LExit)) \\
&\quad G.AddExcEdge(L_1(\#throw), (fid_{global}, LExitExc)) \\
&\quad G.AddEdge(L_1(\#throw\_end), (fid_{global}, LExitExc)) \\
&\quad G.AddEdge(L_1(\#after\_catch), (fid_{global}, LExitExc)) \\
&\quad G \\
\\
\llbracket arg^* \rrbracket_{args} &= Fold(arg^*)([]) (\lambda(args, x = arguments[i]) \Rightarrow args @ [x]) \\
\\
\llbracket fd^* \rrbracket_{fdvars} &= Fold(fd^*)([]) (\lambda(vars, \text{function } f(this, args) \{ s_{arg}^* fd^*, vd^*, s_{body}^* \}) \Rightarrow vars @ [f]) \\
\\
\llbracket vd^* \rrbracket_{vds} &= Fold(vd^*)([]) (\lambda(vars, \text{var } x) \Rightarrow vars @ [x]) \\
\\
\llbracket fd^* \rrbracket_{fd^*}(G, N)(fid) &= \text{if } (Length(fd^*) = 0) \text{ then } N \\
&\quad \text{else } \llbracket TailOf(fd^*) \rrbracket_{fd^*}(G, \llbracket HeadOf(fd^*) \rrbracket_{fd}(G, N)(fid))(fid) \\
\\
\llbracket \text{function } f(this, args) \{ s_{arg}^* fd^*, vd^*, s_{body}^* \} \rrbracket_{fd}(G, N)(fid) &= argVars \stackrel{let}{=} \llbracket s_{arg}^* \rrbracket_{args} \\
&\quad localVars \stackrel{let}{=} \llbracket fd^* \rrbracket_{fdvars} @ \llbracket vd^* \rrbracket_{vds} - argVars \\
&\quad fid_{new} \stackrel{let}{=} G.NewFunction(args, argVars, localVars) \\
&\quad n_{start} \stackrel{let}{=} G.NewBlock(fid_{new}) \\
&\quad G.AddEdge((fid_{new}, LEntry), n_{start}) \\
&\quad L \stackrel{let}{=} [ \#return \mapsto [], \#throw \mapsto [], \#throw\_end \mapsto [], \#after\_catch \mapsto [] ] \\
&\quad N_1 \stackrel{let}{=} \llbracket fd^* \rrbracket_{fd^*}(G, [n_{start}]) (fid_{new}) \\
&\quad (N_2, L_1) \stackrel{let}{=} \llbracket stmt^* \rrbracket_{stmt^*}(G, N_1, L) (fid_{new}) \\
&\quad G.AddEdge(N_2, (fid_{new}, LExit)) \\
&\quad G.AddEdge(L_1(\#return), (fid_{new}, LExit)) \\
&\quad G.AddExcEdge(L_1(\#throw), (fid_{new}, LExitExc)) \\
&\quad G.AddEdge(L_1(\#throw\_end), (fid_{new}, LExitExc)) \\
&\quad G.AddEdge(L_1(\#after\_catch), (fid_{new}, LExitExc)) \\
&\quad n_{tail} \stackrel{let}{=} GetTail(G, N)(fid) \\
&\quad G.AddInst(n_{tail}, f := \text{function } (fid_{new})_{loc_1, loc_2} [n_{tail}]
\end{aligned}$$

$$\begin{aligned}
\llbracket stmt^* \rrbracket_{stmt^*}(G, N, L)(fid) &= \text{if } (Length(stmt^*) = 0) \text{ then } (N, L) \\
&\quad \text{else } (N_1, L_1) \stackrel{let}{=} \llbracket HeadOf(stmt^*) \rrbracket_{stmt}(G, N, L)(fid) \\
&\quad \llbracket TailOf(stmt^*) \rrbracket_{stmt^*}(G, N_1, L_1)(fid) \\
\llbracket IRSeq(stmt^*) \rrbracket_{stmt}(G, N, L)(fid) &= \llbracket stmt^* \rrbracket_{stmt^*}(G, N, L)(fid) \\
\llbracket IRStmtUnit(stmt^*) \rrbracket_{stmt}(G, N, L)(fid) &= \llbracket stmt^* \rrbracket_{stmt^*}(G, N, L)(fid) \\
\llbracket x = \text{function } f(this, args) \{ s_{arg}^*, fd^*, vd^*, s_{body}^* \} \rrbracket_{stmt}(G, N, L)(fid) &= argVars \stackrel{let}{=} \llbracket s_{arg}^* \rrbracket_{args} \\
&\quad localVars \stackrel{let}{=} \llbracket fd^* \rrbracket_{fdvars} @ \llbracket vd^* \rrbracket_{vds} - argVars \\
&\quad fid_{new} \stackrel{let}{=} G.NewFunction(args, argVars, localVars) \\
&\quad n_{start} \stackrel{let}{=} G.NewBlock(fid_{new}) \\
&\quad G.AddEdge((fid_{new}, LEntry), n_{start}) \\
&\quad L_{new} \stackrel{let}{=} [ \#return \mapsto [], \#throw \mapsto [], \#throw\_end \mapsto [], \#after\_catch \mapsto [] ] \\
&\quad N_1 \stackrel{let}{=} \llbracket fd^* \rrbracket_{fd^*}(G, [n_{start}]) (fid_{new}) \\
&\quad (N_2, L_1) \stackrel{let}{=} \llbracket stmt^* \rrbracket_{stmt^*}(G, N_1, L_{new})(fid_{new}) \\
&\quad G.AddEdge(N_2, (fid_{new}, LExit)) \\
&\quad G.AddEdge(L_1(\#return), (fid_{new}, LExit)) \\
&\quad G.AddExcEdge(L_1(\#throw), (fid_{new}, LExitExc)) \\
&\quad G.AddEdge(L_1(\#throw\_end), (fid_{new}, LExitExc)) \\
&\quad G.AddEdge(L_1(\#after\_catch), (fid_{new}, LExitExc)) \\
&\quad n_{tail} \stackrel{let}{=} GetTail(G, N)(fid) \\
&\quad \text{if } (getVarKind_P(f) = \text{CapturedVar}) \\
&\quad \quad G.AddInst(n_{tail}, x := \text{function } f(fid_{new})_{loc1, loc2, loc3}) \\
&\quad \text{else} \\
&\quad \quad G.AddInst(n_{tail}, x := \text{function } (fid_{new})_{loc1, loc2}) \\
&\quad ([n_{tail}], L) \\
\llbracket x = \{member^*, proto^?\} \rrbracket_{stmt}(G, N, L)(fid) &= n_{tail} \stackrel{let}{=} GetTail(G, N)(fid) \\
&\quad G.AddInst(n_{tail}, x := \text{alloc}(proto^?)_{loc}) \\
&\quad Iter(memeber^*)(\lambda(m) \Rightarrow \llbracket m \rrbracket_{mem}(G, n_{tail})(x)) \\
&\quad ([n_{tail}], L[\#throw \mapsto n_{tail} :: L(\#throw)]) \\
\llbracket y : z \rrbracket_{mem}(G, n)(x) &= G.AddInst(n, x["y"] := z) \\
\llbracket x = [elem^*] \rrbracket_{stmt}(G, N, L)(fid) &= n_{tail} \stackrel{let}{=} GetTail(G, N)(fid) \\
&\quad G.AddInst(n_{tail}, x := \text{allocArray}(Length(elem^*))_{loc}) \\
&\quad \stackrel{let}{=} Fold(elem^*)(0)(\lambda(e, k) \Rightarrow \llbracket y \rrbracket_{elem}(G, n_{tail})(x, k)) \\
&\quad ([n_{tail}], L[\#throw \mapsto n_{tail} :: L(\#throw)]) \\
\llbracket x = [elem^*] \rrbracket_{stmt}(G, N, L)(fid) &= n_{tail} \stackrel{let}{=} GetTail(G, N)(fid) \\
\text{(arguments)} &\quad G.AddInst(n_{tail}, x := \text{allocArg}(Length(elem^*))_{loc}) \\
&\quad \stackrel{let}{=} Fold(elem^*)(0)(\lambda(e, k) \Rightarrow \llbracket y \rrbracket_{elem}(G, n_{tail})(x, k)) \\
&\quad ([n_{tail}], L[\#throw \mapsto n_{tail} :: L(\#throw)]) \\
\llbracket y \rrbracket_{elem}(G, n)(x, k) &= G.AddInst(n, x["k"] := y) \\
&\quad k + 1
\end{aligned}$$

$$\begin{aligned}
\llbracket x = f(\text{this}, \text{args}^?) \rrbracket_{\text{stmt}}(G, N, L)(fid) &= n_1 \stackrel{\text{let}}{=} \text{GetTail}(G, N)(fid) \\
&\quad \text{if } (f = \diamond \text{toObject}) \\
&\quad \quad G.\text{AddInst}(n_1, x = \diamond f_1([this, \text{args}])_{loc}) \\
&\quad \quad ([n_1], L[\#throw \mapsto n_1 :: L(\#throw)]) \\
&\quad \text{else if } (f = \diamond \text{toBoolean} \vee f = \diamond \text{toNumber} \\
&\quad \quad \vee f = \diamond \text{toString} \vee f = \diamond \text{isObject} \vee f = \diamond \text{iteratorInit} \\
&\quad \quad \vee f = \diamond \text{iteratorHasNext} \vee f = \diamond \text{iteratorNext} \vee f = \diamond \text{getBase}) \\
&\quad \quad G.\text{AddInst}(n_1, x = \diamond f_1([this, \text{args}])) \\
&\quad \quad ([n_1], L) \\
&\quad \text{else} \\
&\quad \quad G.\text{AddInst}(n_1, \text{call}(f, \text{this}, \text{args})_{loc}) \\
&\quad \quad n_2 \stackrel{\text{let}}{=} G.\text{NewAfterCallBlock}(fid, x) \\
&\quad \quad n_3 \stackrel{\text{let}}{=} G.\text{NewAfterCatchBlock}(fid) \\
&\quad \quad G.\text{AddCall}(n_1, n_2, n_3) \\
&\quad \quad ([n_2], L[\#throw \mapsto n_1 :: L(\#throw), \#after\_catch \mapsto n_3 :: L(\#after\_catch)]) \\
\\
\llbracket x = c(\text{args}) \rrbracket_{\text{stmt}}(G, N, L)(fid) &= n_1 \stackrel{\text{let}}{=} \text{GetTail}(G, N)(fid) \\
(\text{irnew}) &\quad G.\text{AddInst}(n_1, \text{construct}(c, \text{args.hd}, \text{args.tl.hd})_{loc}) \\
&\quad n_2 \stackrel{\text{let}}{=} G.\text{NewAfterCallBlock}(fid, x) \\
&\quad n_3 \stackrel{\text{let}}{=} G.\text{NewAfterCatchBlock}(fid) \\
&\quad G.\text{AddCall}(n_1, n_2, n_3) \\
&\quad ([n_2], (L[\#throw \mapsto n_1 :: L(\#throw), \#after\_catch \mapsto n_3 :: L(\#after\_catch)])) \\
\\
\llbracket \text{with}(x) \ s \rrbracket_{\text{stmt}}(G, N, L)(fid) &= ??? \\
\\
\llbracket l : \{s\} \rrbracket_{\text{stmt}}(G, N, L)(fid) &= n \stackrel{\text{let}}{=} G.\text{NewBlock}(fid) \\
&\quad (N_1, L_1) \stackrel{\text{let}}{=} \llbracket s \rrbracket_{\text{stmt}}(G, N, L[l \mapsto []])(fid) \\
&\quad G.\text{AddEdge}(N_1, n) \\
&\quad G.\text{AddEdge}(L_1(l), n) \\
&\quad L_2 \stackrel{\text{let}}{=} L_1 - l \\
&\quad ([n], L_2) \\
\\
\llbracket \text{if}(e) \ s_{\text{true}} \ \text{else} \ s_{\text{false}} \rrbracket_{\text{stmt}}(G, N, L)(fid) &= n_1 \stackrel{\text{let}}{=} G.\text{NewBlock}(fid) \\
&\quad n_2 \stackrel{\text{let}}{=} G.\text{NewBlock}(fid) \\
&\quad G.\text{AddEdge}(N, n_1) \\
&\quad G.\text{AddEdge}(N, n_2) \\
&\quad G.\text{AddInst}(n_1, \text{assert}(e)) \\
&\quad G.\text{AddInst}(n_2, \text{assert}(\neg e)) \\
&\quad (N_1, L_1) \stackrel{\text{let}}{=} \llbracket s_{\text{true}} \rrbracket_{\text{stmt}}(G, [n_1], L)(fid) \\
&\quad (N_2, L_2) \stackrel{\text{let}}{=} \llbracket s_{\text{false}} \rrbracket_{\text{stmt}}(G, [n_2], L_1)(fid) \\
&\quad (N_1 @ N_2, L_2[\#throw \mapsto n_1 :: n_2 :: L_2(\#throw)]) \\
\\
\llbracket \text{if}(e) \ s_{\text{true}} \rrbracket_{\text{stmt}}(G, N, L)(fid) &= n_1 \stackrel{\text{let}}{=} G.\text{NewBlock}(fid) \\
&\quad n_2 \stackrel{\text{let}}{=} G.\text{NewBlock}(fid) \\
&\quad G.\text{AddEdge}(N, n_1) \\
&\quad G.\text{AddEdge}(N, n_2) \\
&\quad G.\text{AddInst}(n_1, \text{assert}(e)) \\
&\quad G.\text{AddInst}(n_2, \text{assert}(\neg e)) \\
&\quad (N_1, L_1) \stackrel{\text{let}}{=} \llbracket s_{\text{true}} \rrbracket_{\text{stmt}}(G, [n_1], L)(fid) \\
&\quad (N_1 @ [n_2], L_1[\#throw \mapsto n_1 :: n_2 :: L_1(\#throw)])
\end{aligned}$$

$$\begin{aligned}
\llbracket \text{while}(e) \ s \rrbracket_{\text{stmt}}(G, N, L)(fid) &= n_1 \stackrel{\text{let}}{=} \text{GetTail}(G, N)(fid) \\
&\quad n_{\text{head}} \stackrel{\text{let}}{=} G.\text{NewBlock}(fid) \\
&\quad n_2 \stackrel{\text{let}}{=} G.\text{NewBlock}(fid) \\
&\quad n_3 \stackrel{\text{let}}{=} G.\text{NewBlock}(fid) \\
&\quad G.\text{AddEdge}(n_1, n_{\text{head}}) \\
&\quad G.\text{AddEdge}(n_{\text{head}}, n_2) \\
&\quad G.\text{AddEdge}(n_{\text{head}}, n_3) \\
&\quad G.\text{AddInst}(n_2, \text{assert}(e)) \\
&\quad G.\text{AddInst}(n_3, \text{assert}(\neg e)) \\
&\quad (N_1, L_1) \stackrel{\text{let}}{=} \llbracket s \rrbracket_{\text{stmt}}(G, [n_2], L)(fid) \\
&\quad G.\text{AddEdge}(N_1, n_{\text{head}}) \\
&\quad ([n_3], L_1[\#throw \mapsto n_2 :: n_3 :: L_1(\#throw)]) \\
\\
\llbracket \text{throw } x \rrbracket_{\text{stmt}}(G, N, L)(fid) &= n \stackrel{\text{let}}{=} \text{GetTail}(G, N)(fid) \\
&\quad G.\text{AddInst}(n, \text{throw}(x)) \\
&\quad ([], L[\#throw \mapsto n :: L(\#throw)]) \\
\\
\llbracket \text{return } x \rrbracket_{\text{stmt}}(G, N, L)(fid) &= n \stackrel{\text{let}}{=} \text{GetTail}(G, N)(fid) \\
&\quad G.\text{AddInst}(n, \text{return}(x)) \\
&\quad ([], L[\#return \mapsto n :: L(\#return)]) \\
\\
\llbracket \text{return } \underline{x}^? \rrbracket_{\text{stmt}}(G, N, L)(fid) &= n \stackrel{\text{let}}{=} \text{GetTail}(G, N)(fid) \\
&\quad ([], L[\#return \mapsto n :: L(\#return)]) \\
\\
\llbracket x = e \rrbracket_{\text{stmt}}(G, N, L)(fid) &= n \stackrel{\text{let}}{=} \text{GetTail}(G, N)(fid) \\
&\quad G.\text{AddInst}(n, x := e) \\
&\quad \text{if } (e = \text{IRId}) \\
&\quad \quad ([n], L[\#throw \mapsto n :: L(\#throw)]) \\
&\quad \text{else} \\
&\quad \quad ([n], L) \\
\\
\llbracket x = \text{delete } y \rrbracket_{\text{stmt}}(G, N, L)(fid) &= n \stackrel{\text{let}}{=} \text{GetTail}(G, N)(fid) \\
&\quad G.\text{AddInst}(n, x := \text{delete}(y)) \\
&\quad ([n], L[\#throw \mapsto n :: L(\#throw)]) \\
\\
\llbracket x = \text{delete } y[z] \rrbracket_{\text{stmt}}(G, N, L)(fid) &= n \stackrel{\text{let}}{=} \text{GetTail}(G, N)(fid) \\
&\quad G.\text{AddInst}(n, x := \text{delete}(y, z)) \\
&\quad ([n], L[\#throw \mapsto n :: L(\#throw)]) \\
\\
\llbracket x = \ominus y \rrbracket_{\text{stmt}}(G, N, L)(fid) &= n \stackrel{\text{let}}{=} \text{GetTail}(G, N)(fid) \\
&\quad G.\text{AddInst}(n, x := \ominus y) \\
&\quad ([n], L[\#throw \mapsto n :: L(\#throw)]) \\
\\
\llbracket x = y \otimes z \rrbracket_{\text{stmt}}(G, N, L)(fid) &= n \stackrel{\text{let}}{=} \text{GetTail}(G, N)(fid) \\
&\quad G.\text{AddInst}(n, x := y \otimes z) \\
&\quad ([n], L[\#throw \mapsto n :: L(\#throw)]) \\
\\
\llbracket x[y] = z \rrbracket_{\text{stmt}}(G, N, L)(fid) &= n \stackrel{\text{let}}{=} \text{GetTail}(G, N)(fid) \\
&\quad G.\text{AddInst}(n, x[y] := z) \\
&\quad ([n], L[\#throw \mapsto n :: L(\#throw)]) \\
\\
\llbracket x = y[e] \rrbracket_{\text{stmt}}(G, N, L)(fid) &= n \stackrel{\text{let}}{=} \text{GetTail}(G, N)(fid) \\
&\quad G.\text{AddInst}(n, x := y[e]) \\
&\quad ([n], L[\#throw \mapsto n :: L(\#throw)])
\end{aligned}$$

$$\begin{aligned}
\llbracket \text{try}\{s\} \text{ catch}(x) \{s_c\} \rrbracket_{stm}(G, N, L)(fid) &= n_1 \stackrel{let}{=} G.NewBlock(fid) \\
&G.AddEdge(N, n_1) \\
n_3 &\stackrel{let}{=} G.NewBlock(fid) \\
&G.AddInst(n_3, \text{catch}(x)) \\
L_{try} &\stackrel{let}{=} [ \#return \mapsto [], \#throw \mapsto [], \#throw\_end \mapsto [], \#after\_catch \mapsto [] ] \\
(N_1, L_1) &= \llbracket s \rrbracket_{stm}(G, [n_2], L_{try})(fid) \\
&G.AddExcEdge(L_1(\#throw), n_2) \\
&G.AddEdge(L_1(\#throw\_end), n_2) \\
&G.AddEdge(L_1(\#catch), n_2) \\
(N_2, L_2) &= \llbracket s_c \rrbracket_{stm}(G, [n_2], L_1[\#throw \mapsto [], \#throw\_end \mapsto [], \#after\_catch \mapsto []])(fid) \\
L_3 &\stackrel{let}{=} Fold(L_2)(L)(\lambda((l, N'), L') \Rightarrow \\
&\quad \text{if } (L'.contains(l)) \\
&\quad \quad L'[l \mapsto L'(l) @ N'] \\
&\quad \text{else} \\
&\quad \quad L'[l \mapsto N'] \\
&(N_1 @ N_2, L_3)
\end{aligned}$$
  

$$\begin{aligned}
\llbracket \text{try}\{s\} \text{ finally } \{s_f\} \rrbracket_{stm}(G, N, L)(fid) &= n_1 \stackrel{let}{=} G.NewBlock(fid) \\
&G.AddEdge(N, n_1) \\
n_2 &\stackrel{let}{=} G.NewBlock(fid) \\
L_{try} &\stackrel{let}{=} [ \#return \mapsto [], \#throw \mapsto [], \#throw\_end \mapsto [], \#after\_catch \mapsto [] ] \\
(N_1, L_1) &\stackrel{let}{=} \llbracket s \rrbracket_{stm}(G, [n_1], L_{try})(fid) \\
(N_2, L_2) &\stackrel{let}{=} \llbracket s_f \rrbracket_{stm}(G, [n_2], L)(fid) \\
&G.AddEdge(N_1, n_2) \\
L_3 &\stackrel{let}{=} Fold(L_1[ \#after\_catch \mapsto [] ])(L_2)(\lambda((l, N'), L') \Rightarrow \\
&\quad \text{if } (N' \neq Nil) \\
&\quad \quad n_{dup} \stackrel{let}{=} G.NewBlock(fid) \\
&\quad \quad (N'', L'') \stackrel{let}{=} \llbracket s_f \rrbracket_{stm}(G, [n_{dup}], L')(fid) \\
&\quad \quad \text{if } (l = \#throw) \\
&\quad \quad \quad G.AddEdge(L_1(\#after\_catch), n_{dup}) \\
&\quad \quad \quad G.AddExcEdge(N', n_{dup}); L''[\#throw\_end \mapsto L''(\#throw\_end) @ N''] \\
&\quad \quad \text{else} \\
&\quad \quad \quad G.AddEdge(N', n_{dup}); L''[l \mapsto L''(l) @ N''] \\
&(N_2, L_3)
\end{aligned}$$

$$\begin{aligned}
& \llbracket \text{try}\{s\} \text{ catch}(x) \{s_c\} \text{ finally } \{s_f\} \rrbracket_{\text{stmt}}(G, N, L)(fid) = n_1 \stackrel{\text{let}}{=} G.\text{NewBlock}(fid) \\
& \quad G.\text{AddEdge}(N, n_1) \\
& \quad n_2 \stackrel{\text{let}}{=} G.\text{NewBlock}(fid) \\
& \quad G.\text{AddInst}(n_2, \text{catch}(x)) \\
& \quad n_3 \stackrel{\text{let}}{=} G.\text{NewBlock}(fid) \\
& \quad L_{\text{try}} \stackrel{\text{let}}{=} [\#return \mapsto [], \#throw \mapsto [], \#throw\_end \mapsto [], \#after\_catch \mapsto []] \\
& \quad (N_1, L_1) \stackrel{\text{let}}{=} \llbracket s \rrbracket_{\text{stmt}}(G, [n_1], L_{\text{try}})(fid) \\
& \quad G.\text{AddExcEdge}(L_1(\#throw), n_2) \\
& \quad G.\text{AddEdge}(L_1(\#throw\_end), n_2) \\
& \quad G.\text{AddEdge}(L_1(\#after\_catch), n_2) \\
& \quad (N_2, L_2) \stackrel{\text{let}}{=} \llbracket s_c \rrbracket_{\text{stmt}}(G, [n_2], L_1[\#throw \mapsto [], \#throw\_end \mapsto [], \\
& \quad \quad \quad \#after\_catch \mapsto []])(fid) \\
& \quad (N_3, L_3) \stackrel{\text{let}}{=} \llbracket s_f \rrbracket_{\text{stmt}}(G, [n_3], L)(fid) \\
& \quad G.\text{AddEdge}(N_1 @ N_2, n_3) \\
& \quad L_4 \stackrel{\text{let}}{=} \text{Fold}(L_2[\#after\_catch \mapsto []])(L_3)(\lambda((l, N'), L') \Rightarrow \\
& \quad \quad \text{if } (N' \neq \text{Nil}) \\
& \quad \quad \quad n_{\text{dup}} \stackrel{\text{let}}{=} G.\text{NewBlock}(fid) \\
& \quad \quad \quad (N'', L'') \stackrel{\text{let}}{=} \llbracket s_f \rrbracket_{\text{stmt}}(G, [n_{\text{dup}}], L')(fid) \\
& \quad \quad \quad \text{if } (l = \#throw) \\
& \quad \quad \quad \quad G.\text{AddEdge}(L_2(\#after\_catch), n_{\text{dup}}) \\
& \quad \quad \quad \quad G.\text{AddExcEdge}(N', n_{\text{dup}}); L''[\#throw\_end \mapsto L''(\#throw\_end) @ N''] \\
& \quad \quad \quad \text{else} \\
& \quad \quad \quad \quad G.\text{AddEdge}(N', n_{\text{dup}}); L''[l \mapsto L''(l) @ N''] \\
& \quad (N_3, L_4)
\end{aligned}$$

## Chapter 8

# CFG Collecting Semantics

Assumptions and limitations are as follows:

- All the variables declared by ‘var’ are included in the set LocalVars.
- Followings are not yet supported: regular expression, with, getter, setter, eval.
- Runtime exception is omitted. throw is the only way to make an exception.
- Semantics of operators are omitted.
- Semantics for helper functions is not written using denotational semantics(they are not compositional).
- Try-catch clause in a finally block can disturb a flow of a previous throwed value.

### 8.1 Settings

$x \in \text{Prop}$	=	$\text{String} \cup \left\{ \begin{array}{l} @return, @exception, @exception\_all, @this, @up, @outer \\ @proto, @scope, @class, @function, @extensible, @construct \end{array} \right\}$
$l \in \text{Loc}$	::=	$\#Global \mid \#ObjProto \mid \#ArrayProto \mid \#RefErrProto$ $\mid \#RangeErrProto \mid \#TypeErrProto$ $\mid l_1 \mid \dots$
$cp \in \text{ControlPoint}$	=	Node
$H \in \text{Heap}$	=	$\text{Loc} \xrightarrow{\text{fin}} \text{Obj}$
$o \in \text{Obj}$	=	$\text{Prop} \xrightarrow{\text{fin}} \text{PropValue}$
$A \in \text{Env}$	=	Loc list
$(H, A), \text{stuck} \in \text{State}$	=	Heap $\times$ Env
$\text{PropValue}$	=	ObjectValue $\cup$ Value $\cup$ FunctionId $\cup$ Env <i>‘Value <math>\cup</math> FunctionId <math>\cup</math> Env’ is for internal property.</i>
$v \in \text{Value}$	=	Loc $\cup$ PValue
$ov \in \text{ObjectValue}$	=	$\left\{ \begin{array}{l} value : \text{Value}; \\ writable : \text{Bool}; \\ enumerable : \text{Bool}; \\ configurable : \text{Bool}; \end{array} \right\}$
$pv \in \text{PValue}$	=	Number $\cup$ String $\cup$ Bool $\cup$ { undefined, null }
$n \in \text{Number}$	::=	NaN $\mid$ Inf $\mid$ - Inf $\mid$ 0 $\mid$ 1 $\mid$ - 1 $\mid$ 2 $\mid$ ...
$s \in \text{String}$		
$b \in \text{Bool}$		
$exc \in \text{Exception}$	::=	ReferenceError $\mid$ RangeError $\mid$ TypeError



## 8.2 Helper Functions

$$\begin{aligned}\text{PushStack}(l_o^*, l_n) &= l_n :: l_o^* \\ \text{TopStack}(l_n :: l_o^*) &= l_n\end{aligned}$$

$$\begin{aligned}\text{Dom}(H) &= \{ l \mid l \mapsto o \in H \} \\ \text{Dom}(o) &= \{ x \mid x \mapsto v \in o \}\end{aligned}$$

$$\begin{aligned}\text{IsArray}(H, l) &= \begin{cases} \text{true} & \text{if } H(l)(\text{@class}) = \text{"Array"} \\ \text{false} & \text{otherwise} \end{cases} \\ \text{IsObject}(H, l) &= \begin{cases} \text{true} & \text{if } H(l)(\text{@class}) = \text{"Object"} \vee H(l)(\text{@class}) = \text{"Function"} \\ \text{false} & \text{otherwise} \end{cases}\end{aligned}$$

IsArrayIndex : Value  $\rightarrow$  Bool

$$\text{IsArrayIndex}(v) = \begin{cases} \text{true} & \text{if } \text{toString}(\text{ToUint32}(\text{toString}(v))) = \text{toString}(v) \\ & \wedge \text{ToUint32}(\text{toString}(v)) \neq 2^{32} - 1 \\ \text{false} & \text{otherwise} \end{cases}$$

VarStore : Heap  $\times$  Env  $\times$  Prop  $\times$  Value  $\times$  Bool  $\rightarrow$  Heap

$$\text{VarStore}(H, [\#Global], x, v, b) = \text{PropStore}(H, \#Global, x, v)$$

if  $x \notin \text{Dom}(H(\#Global))$

$$\text{VarStore}(H, l_{hd} :: l_{tl}^*, x, v, b) = H[l_{hd} \mapsto H(l_{hd})[x \mapsto \{ H(l_{hd})(x) \text{ with value} = v; \text{writable} = b \}]]$$

if  $x \in \text{Dom}(H(l_{hd}))$

$$\text{VarStore}(H, l_{hd} :: l_{tl}^*, x, v, b) = \text{VarStore}(H, l_{tl}^*, x, v, b)$$

if  $x \notin \text{Dom}(H(l_{hd}))$

VarStoreE : Heap  $\times$  Env  $\times$  Prop  $\times$  Value  $\times$  Bool  $\rightarrow$  Heap

$$\text{VarStoreE}(H, A, t, v, b) = \text{VarStore}(H, A, t, v, b)$$

$$\text{VarStoreE}(H, A, x, v, b) = \begin{cases} \text{VarStore}(H, A, x, v, b) & \text{if } \text{CanPutVar}(H, A, x) \\ H & \text{otherwise} \end{cases}$$

PropStore : Heap  $\times$  Loc  $\times$  Prop  $\times$  Value  $\rightarrow$  Heap

$$\text{PropStore}(H, l, x, v) = H \left[ l \mapsto H(l) \left[ x \mapsto \begin{cases} \text{value} = v; \\ \text{enumerable} = \text{true}; \\ \text{configurable} = \text{true}; \\ \text{writable} = \text{true} \end{cases} \right] \right]$$

if  $x \notin \text{Dom}(H(l))$

$$\text{PropStore}(H, l, x, v) = H \left[ l \mapsto H(l) \left[ x \mapsto \{ H(l)(x) \text{ with value} = v \} \right] \right]$$

if  $x \in \text{Dom}(H(l))$

Delete : Heap  $\times$  Loc  $\times$  Prop  $\rightarrow$  Heap  $\times$  Bool

$$\text{Delete}(H, l, x) = (H, \text{true})$$

if  $\neg \text{HasOwnProperty}(H, l, x)$

$$\text{Delete}(H, l, x) = (H, \text{false})$$

if  $\text{HasOwnProperty}(H, l, x) \wedge H(l)(x).configurable = \text{false}$

$$\text{Delete}(H, l, x) = (H[l \mapsto H(l) - x], \text{true})$$

if  $\text{HasOwnProperty}(H, l, x) \wedge H(l)(x).configurable = \text{true}$

Lookup : Heap  $\times$  Env  $\times$  Prop  $\rightarrow$  Value  $\cup$  Exception

$$\text{Lookup}(H, [\#Global], x) = \text{ReferenceError}$$

if  $\neg \text{HasProperty}(H, \#Global, x)$

$$\text{Lookup}(H, [\#Global], x) = \text{Proto}(H, \#Global, x)$$

if  $\text{HasProperty}(H, \#Global, x)$

$$\text{Lookup}(H, l_{hd} :: l_{tl}^*, x) = H(l_{hd})(x).value$$

if  $x \in \text{Dom}(H(l_{hd}))$

$$\text{Lookup}(H, l_{hd} :: l_{tl}^*, x) = \text{Lookup}(H, l_{tl}^*, x)$$

if  $x \notin \text{Dom}(H(l_{hd}))$

<u>TypeTag</u>	$: \text{Heap} \times \text{Value} \rightarrow \begin{cases} \text{"number"}, \text{"string"}, \text{"boolean"}, \text{"object"}, \\ \text{"function"}, \text{"null"}, \text{"undefined"} \end{cases}$ $\text{TypeTag}(H, v) = \begin{cases} \text{"number"} & \text{if } v \in \text{Number} \\ \text{"boolean"} & \text{if } v \in \text{Boolean} \\ \text{"string"} & \text{if } v \in \text{String} \\ \text{"object"} & \text{if } v \in \text{Loc} \wedge \neg \text{IsCallable}(H, v) \\ \text{"function"} & \text{if } v \in \text{Loc} \wedge \text{IsCallable}(H, v) \\ \text{"object"} & \text{if } v = \text{null} \\ \text{"undefined"} & \text{if } v = \text{undefined} \end{cases}$
<u>CanPut</u>	$: \text{Heap} \times \text{Loc} \times \text{Prop} \rightarrow \text{Bool}$ $\text{CanPut}(H, l, x) = \text{CanPutHelp}(H, l, x, l)$
<u>CanPutHelp</u>	$: \text{Heap} \times \text{Loc} \times \text{Prop} \times \text{Loc} \rightarrow \text{Bool}$ $\text{CanPutHelp}(H, l_1, x, l_2) = \text{CanPutHelp}(H, H(l_1)(\text{@proto}).\text{value}, x, l_2)$ $\text{if } x \notin \text{Dom}(H(l_1)) \wedge H(l_1)(\text{@proto}).\text{value} \neq \text{null}$ $\text{CanPutHelp}(H, l_1, x, l_2) = H(l_1)(\text{@extensible})$ $\text{if } x \notin \text{Dom}(H(l_1)) \wedge H(l_1)(\text{@proto}).\text{value} = \text{null}$ $\text{CanPutHelp}(H, l_1, x, l_2) = H(l_1)(x).\text{writable}$ $\text{if } x \in \text{Dom}(H(l_1))$
<u>CanPutVar</u>	$: \text{Heap} \times \text{Env} \times \text{Prop} \rightarrow \text{Bool}$ $\text{CanPutVar}(H, [\#Global], x) = \text{CanPut}(H, \#Global, x)$ $\text{CanPutVar}(H, l_{hd} :: l_{tl}^*, x) = H(l_{hd})(x).\text{writable} \quad \text{if } x \in \text{Dom}(H(l_{hd}))$ $\text{CanPutVar}(H, l_{hd} :: l_{tl}^*, x) = \text{CanPutVar}(H, l_{tl}^*, x) \quad \text{if } x \notin \text{Dom}(H(l_{hd}))$
<u>HasProperty</u>	$: \text{Heap} \times \text{Loc} \times \text{Prop} \rightarrow \text{Bool}$ $\text{HasProperty}(H, l, x) = \text{true}$ $\text{if } \text{HasOwnProperty}(H, l, x)$ $\text{HasProperty}(H, l, x) = \text{false}$ $\text{if } \neg \text{HasOwnProperty}(H, l, x) \wedge H(l_1)(\text{@proto}).\text{value} = \text{null}$ $\text{HasProperty}(H, l, x) = \text{HasProperty}(H, H(l_1)(\text{@proto}).\text{value}, x)$ $\text{if } \neg \text{HasOwnProperty}(H, l, x) \wedge H(l_1)(\text{@proto}).\text{value} \neq \text{null}$
<u>HasOwnProperty</u>	$: \text{Heap} \times \text{Loc} \times \text{Prop} \rightarrow \text{Bool}$ $\text{HasOwnProperty}(H, l, x) = \text{false} \quad \text{if } x \notin \text{Dom}(H(l))$ $\text{HasOwnProperty}(H, l, x) = \text{true} \quad \text{if } x \in \text{Dom}(H(l))$
<u>LookupBase</u>	$: \text{Heap} \times \text{Env} \times \text{Prop} \rightarrow \text{Loc}$ $\text{LookupBase}(H, [\#Global], x) = \text{ProtoBase}(H, \#Global, x)$ $\text{LookupBase}(H, l_{hd} :: l_{tl}^*, x) = l_{hd} \quad \text{if } x \in \text{Dom}(H(l_{hd}))$ $\text{LookupBase}(H, l_{hd} :: l_{tl}^*, x) = \text{LookupBase}(H, l_{tl}^*, x) \quad \text{if } x \notin \text{Dom}(H(l_{hd}))$

ProtoBase

:  $\text{Heap} \times \text{Loc} \times \text{Prop} \rightarrow \text{Loc}$   
 $\text{ProtoBase}(H, l, x) = l$   
if  $x \in \text{Dom}(H(l))$   
 $\text{ProtoBase}(H, l, x) = \{\}$   
if  $x \notin \text{Dom}(H(l)) \wedge H(l)(\text{@proto}).\text{value} = \text{null}$   
 $\text{ProtoBase}(H, l, x) = \text{ProtoBase}(H, H(l)(\text{@proto}).\text{value}, x)$   
if  $x \notin \text{Dom}(H(l)) \wedge H(l)(\text{@proto}).\text{value} \neq \text{null}$

Proto

:  $\text{Heap} \times \text{Loc} \times \text{Prop} \rightarrow \text{Value}$   
 $\text{Proto}(H, l, x) = H(l)(x).\text{value}$   
if  $x \in \text{Dom}(H(l))$   
 $\text{Proto}(H, l, x) = \text{Proto}(H, H(l)(\text{@proto}).\text{value}, x)$   
if  $x \notin \text{Dom}(H(l)) \wedge H(l)(\text{@proto}).\text{value} \neq \text{null}$   
 $\text{Proto}(H, l, x) = \text{undefined}$   
if  $x \notin \text{Dom}(H(l)) \wedge H(l)(\text{@proto}).\text{value} = \text{null}$

NewObject

:  $\text{Loc} \rightarrow \text{Obj}$

$$\text{NewObject}(l) = \left\{ \begin{array}{l} \text{@class} \mapsto \text{"Object"}, \\ \text{@proto} \mapsto \left\{ \begin{array}{l} \text{value} = l; \\ \text{writable} = \text{false}; \\ \text{enumerable} = \text{false}; \\ \text{configurable} = \text{false} \end{array} \right\}, \\ \text{@extensible} \mapsto \text{true} \end{array} \right\}$$

NewFunctionObject

:  $\text{FunctionId} \times \text{Env} \times \text{Loc} \times \text{Number} \rightarrow \text{Obj}$

$$\text{NewFunctionObject}(fid, A, l, n) = \left\{ \begin{array}{l} \text{@class} \mapsto \text{"Function"}, \\ \text{@function} \mapsto fid, \\ \text{@construct} \mapsto fid, \\ \text{@scope} \mapsto A, \\ \text{@proto} \mapsto \left\{ \begin{array}{l} \text{value} = \#FunctionProto; \\ \text{writable} = \text{false}; \\ \text{enumerable} = \text{false}; \\ \text{configurable} = \text{false} \end{array} \right\}, \\ \text{"prototype"} \mapsto \left\{ \begin{array}{l} \text{value} : l; \\ \text{writable} : \text{true}; \\ \text{enumerable} : \text{false}; \\ \text{configurable} : \text{false} \end{array} \right\}, \\ \text{"length"} \mapsto \left\{ \begin{array}{l} \text{value} : n; \\ \text{writable} : \text{false}; \\ \text{enumerable} : \text{false}; \\ \text{configurable} : \text{false} \end{array} \right\}, \\ \text{@extensible} \mapsto \text{true} \end{array} \right\}$$

NewArrayObject

:  $\text{Number} \rightarrow \text{Obj}$

$$\text{NewArrayObject}(n) = \left\{ \begin{array}{l} \text{@class} \mapsto \text{"Array"}, \\ \text{@proto} \mapsto \left\{ \begin{array}{l} \text{value} = \#ArrayProto; \\ \text{writable} = \text{false}; \\ \text{enumerable} = \text{false}; \\ \text{configurable} = \text{false} \end{array} \right\}, \\ \text{"length"} \mapsto \left\{ \begin{array}{l} \text{value} : n; \\ \text{writable} : \text{true}; \\ \text{enumerable} : \text{false}; \\ \text{configurable} : \text{false} \end{array} \right\}, \\ \text{@extensible} \mapsto \text{true} \end{array} \right\}$$

NewArgObject : Number  $\rightarrow$  Obj

$$\text{NewArgObject}(n) = \left\{ \begin{array}{l} @class \mapsto \text{"Arguments"}, \\ @proto \mapsto \left\{ \begin{array}{l} value = \#ObjProto; \\ writable = \text{false}; \\ enumerable = \text{false}; \\ configurable = \text{false} \end{array} \right\}, \\ \text{"length"} \mapsto \left\{ \begin{array}{l} value : n; \\ writable : \text{true}; \\ enumerable : \text{false}; \\ configurable : \text{true} \end{array} \right\}, \\ @extensible \mapsto \text{true} \end{array} \right\}$$

NewBoolean : Bool  $\rightarrow$  Obj

$$\text{NewBoolean}(v) = \left\{ \begin{array}{l} @class \mapsto \text{"Boolean"}, \\ @proto \mapsto \left\{ \begin{array}{l} value = \#BoolProto; \\ writable = \text{false}; \\ enumerable = \text{false}; \\ configurable = \text{false} \end{array} \right\}, \\ @extensible \mapsto \text{true}, \\ @primitive \mapsto v \end{array} \right\}$$

NewNumber : Number  $\rightarrow$  Obj

$$\text{NewNumber}(v) = \left\{ \begin{array}{l} @class \mapsto \text{"Number"}, \\ @proto \mapsto \left\{ \begin{array}{l} value = \#NumProto; \\ writable = \text{false}; \\ enumerable = \text{false}; \\ configurable = \text{false} \end{array} \right\}, \\ @extensible \mapsto \text{true}, \\ @primitive \mapsto v \end{array} \right\}$$

NewString : String  $\rightarrow$  Obj

NewString(s) =  $o_1 \cup o_2$

where  $v_{len} = \text{length}(s)$

$$\begin{aligned} \wedge o_1 &= \left\{ \begin{array}{l} @class \mapsto \text{"String"}, \\ @proto \mapsto \left\{ \begin{array}{l} value = \#StrProto; \\ writable = \text{false}; \\ enumerable = \text{false}; \\ configurable = \text{false} \end{array} \right\}, \\ @extensible \mapsto \text{true}, \\ @primitive \mapsto s, \\ \text{"length"} \mapsto \left\{ \begin{array}{l} value = v_{len}; \\ writable = \text{false}; \\ enumerable = \text{false}; \\ configurable = \text{false} \end{array} \right\} \end{array} \right\} \\ \wedge o_2 &= \left\{ \begin{array}{l} \text{"i"} \mapsto \left\{ \begin{array}{l} value = v_{char}; \\ writable = \text{false}; \\ enumerable = \text{true}; \\ configurable = \text{false} \end{array} \right\} \end{array} \right\} \Bigg| 0 \leq i < v_{len} \wedge v_{char} = \text{charAt}(s, i) \end{aligned}$$

IsCallable : Heap  $\times$  Loc  $\rightarrow$  Bool

$$\text{IsCallable}(H, l) = \begin{cases} \text{true} & \text{if } @function \in \text{Dom}(H(l)) \\ \text{false} & \text{otherwise} \end{cases}$$

$\underline{\text{HasConstruct}} : \text{Heap} \times \text{Loc} \rightarrow \text{Bool}$   
 $\underline{\text{HasConstruct}}(H, l) = \begin{cases} \text{true} & \text{if } @construct \in \underline{\text{Dom}}(H(l)) \\ \text{false} & \text{otherwise} \end{cases}$

$\underline{\text{newLocation}} : \text{Unit} \rightarrow \text{Loc}$   
 $\underline{\text{newLocation}}() = l_{\text{new}}$

$\underline{\text{toNumber}} : \text{PValue} \rightarrow \text{Number}$   
 $\underline{\text{toNumber}}(pv) = \begin{cases} \text{NaN} & \text{if } pv = \text{undefined} \\ 0 & \text{if } pv = \text{null} \vee pv = \text{false} \\ 1 & \text{if } pv = \text{true} \\ pv & \text{if } pv \in \text{Number} \\ \text{Str2Num}(pv) & \text{if } pv \in \text{String} \end{cases}$

$\underline{\text{toString}} : \text{PValue} \rightarrow \text{String}$   
 $\underline{\text{toString}}(pv) = \begin{cases} \text{"undefined"} & \text{if } pv = \text{undefined} \\ \text{"null"} & \text{if } pv = \text{null} \\ \text{"pv"} & \text{if } pv \in \text{Boolean} \\ \text{"pv"} & \text{if } pv \in \text{Number} \\ pv & \text{if } pv \in \text{String} \end{cases}$

$\underline{\text{toBoolean}} : \text{Value} \rightarrow \text{Bool}$   
 $\underline{\text{toBoolean}}(v) = \begin{cases} \text{false} & \text{if } v = \text{undefined} \\ \text{false} & \text{if } v = \text{null} \\ v & \text{if } v \in \text{Boolean} \\ \text{false} & \text{if } v \in \text{Number} \wedge v \in \{0, \text{NaN}\} \\ \text{true} & \text{if } v \in \text{Number} \wedge v \notin \{0, \text{NaN}\} \\ \text{false} & \text{if } v \in \text{String} \wedge v = \text{""} \\ \text{true} & \text{if } v \in \text{String} \wedge v \neq \text{""} \\ \text{true} & \text{if } v \in \text{Loc} \end{cases}$

$\underline{\text{toPrimitive}} : \text{Value} \rightarrow \text{PValue}$   
 $\underline{\text{toPrimitive}}(v) = \begin{cases} v & \text{if } v \notin \text{Loc} \\ \text{Obj2Str}(v) & \text{if } v \in \text{Loc} \end{cases}$

$\underline{\text{toObject}} : \text{Heap} \times \text{Value} \rightarrow \text{Heap} \times \text{Value} \cup \text{Exception}$   
 $\underline{\text{toObject}}(H, l) = (H, l)$   
 $\underline{\text{toObject}}(H, v) = (H, \text{TypeError}) \quad \text{if } v \in \{ \text{undefined}, \text{null} \}$   
 $\underline{\text{toObject}}(H, v) = (H_1, l_{\text{new}})$   
 where  $o = \begin{cases} \underline{\text{NewString}}(v) & \text{if } v \in \text{String} \\ \underline{\text{NewNumber}}(v) & \text{if } v \in \text{Number} \\ \underline{\text{NewBoolean}}(v) & \text{if } v \in \text{Bool} \end{cases}$   
 $H_1 = H[l_{\text{new}} \mapsto o]$   
 $l_{\text{new}} = \underline{\text{newLocation}}()$

<u>getThis</u>	: Value $\rightarrow$ Loc
<u>getThis</u> ( $v$ )	$= \begin{cases} \#Global & \text{if } v = \text{undefined} \\ \#Global & \text{if } v = \text{null} \\ \#Global & \text{if } v \in \text{Loc} \wedge \neg \text{IsObject}(v) \\ v & \text{if } v \in \text{Loc} \wedge \text{IsObject}(v) \end{cases}$
<u>inherit</u>	: Heap $\times$ Loc $\times$ Loc $\rightarrow$ Value
<u>inherit</u> ( $H, l_1, l_2$ )	$= \begin{cases} \text{true} & \text{if } l_1 = l_2 \\ \text{false} & \text{if } l_1 \neq l_2 \wedge H(l_1)(\text{@proto}).value = \text{null} \\ \text{inherit}(H, H(l_1)(\text{@proto}).value, l_2) & \text{if } l_1 \neq l_2 \wedge H(l_1)(\text{@proto}).value \neq \text{null} \end{cases}$
<u>iteratorInit</u>	: Obj $\times$ $\wp$ (Prop) $\times$ Number $\rightarrow$ Obj
<u>iteratorInit</u> ( $o, P, n$ )	$= \begin{cases} \{\text{@i} \mapsto 0\} & \text{if } P = \emptyset \\ \text{iteratorInit}(o, P - x, n + 1)[n \mapsto x] & \text{if } x \in P \end{cases}$
<u>collectProps</u>	: Heap $\times$ Loc $\rightarrow$ $\wp$ (Loc)
<u>collectProps</u> ( $H, l$ )	$= \begin{cases} \text{Dom}(H(l)) \cup \text{CollectProps}(H, H(l)(\text{@proto}).value) & \text{if } H(l)(\text{@proto}).value \neq \text{null} \\ \{\} & \text{if } H(l)(\text{@proto}).value = \text{null} \end{cases}$
<u>isEnumerable</u>	: Heap $\times$ Loc $\times$ Prop $\rightarrow$ Bool
<u>isEnumerable</u> ( $H, l, x$ )	$= \begin{cases} H(l)(x).enumerable & \text{if } x \in \text{Dom}(H(l)) \\ \text{isEnumerable}(H, H(l)(\text{@proto}).value, x) & \text{if } x \notin \text{Dom}(H(l)) \wedge H(l)(\text{@proto}).value \neq \text{null} \\ \text{false} & \text{if } x \notin \text{Dom}(H(l)) \wedge H(l)(\text{@proto}).value = \text{null} \end{cases}$
<u>next</u>	: Heap $\times$ Obj $\times$ Number $\times$ Loc $\rightarrow$ Number
<u>next</u> ( $H, o_{iter}, n, l$ )	$= \begin{cases} n & \text{if } n \notin \text{Dom}(o_{iter}) \\ n & \text{if } n \in \text{Dom}(o_{iter}) \wedge \text{isEnumerable}(H, l, o_{iter}(n)) \\ \text{next}(H, o_{iter}, n + 1, l) & \text{otherwise} \end{cases}$
<u>NewExceptionObject</u>	: Exception $\rightarrow$ Obj
<u>NewExceptionObject</u> ( $exc$ )	$= \text{NewObject}(l)$
where $l =$	$\begin{cases} \#RefErrProto & \text{if } exc = \text{ReferenceError} \\ \#RangeErrProto & \text{if } exc = \text{RangeError} \\ \#TypeErrProto & \text{if } exc = \text{TypeError} \end{cases}$
<u>RaiseException</u>	: Heap $\times$ Exception $\cup$ Value $\rightarrow$ Heap
<u>RaiseException</u> ( $H, v$ )	$= H_1$
where $H_1 =$	$H[\#temp \mapsto H(\#temp)[\text{@exception} \mapsto v]]$
<u>RaiseException</u> ( $H, exc$ )	$= H_2$
where $l_e =$	$\text{newLocation}()$
$H_1 =$	$H[l_e \mapsto \text{NewExceptionObject}(exc)]$
$H_2 =$	$H_1[\#temp \mapsto H_1(\#temp)[\text{@exception} \mapsto l_e]]$

### 8.3 Semantics

$$\begin{aligned}
\mathcal{C} &\in \text{ControlPoint} \rightarrow \text{Command} \rightarrow \wp(\text{State}) \rightarrow \wp(\text{State}) \\
\mathcal{I} &\in \text{ControlPoint} \rightarrow \text{Instruction} \rightarrow \text{State} \rightarrow \text{State} \\
\mathcal{V} &\in \text{Expression} \rightarrow \text{State} \rightarrow \text{Value} \cup \text{Exception} \\
\mathcal{B} &\in \text{Expression} \rightarrow \text{State} \rightarrow \text{State}
\end{aligned}$$

$$\begin{aligned}
\mathcal{C}_{cp}[\text{entry}]S &= \bigcup \{ (H_1, A) \mid (H, A) \in S \} \\
\text{where } (fid_{this}, \text{ENTRY}) &= cp \wedge l = \text{TopStack}(A) \\
&\wedge x_{argvar}^* = \text{getArgVars}_P(fid_{this}) \wedge x_{localvar}^* = \text{getLocalVars}_P(fid_{this}) \\
&\wedge H_1 = H \left[ l \mapsto H(l) \left[ \begin{array}{l} \left( x_{argvar} \mapsto \left\{ \begin{array}{l} value = \text{undefined}; writable = \text{true}; \\ enumerable = \text{false}; configurable = \text{false} \end{array} \right\} \right)^* \\ \left( x_{localvar} \mapsto \left\{ \begin{array}{l} value = \text{undefined}; writable = \text{true}; \\ enumerable = \text{true}; configurable = \text{false} \end{array} \right\} \right)^* \end{array} \right] \right]
\end{aligned}$$

$$\mathcal{C}_{cp}[\text{exit}]S = S$$

$$\mathcal{C}_{cp}[\text{exit-exc}]S = S$$

$$\mathcal{C}_{cp}[i^+]S = \bigcup \{ (\mathcal{I}_{cp}[i](H, A))^+ \mid (H, A) \in S \}$$

$$\mathcal{I}_{cp}[i](H, A) = (H, A) \quad \text{if } \text{HasProperty}(H, \#temp, @exception) \vee (H, A) = \text{stuck}$$

*\* if e is None, v is considered like a value which is not an element of Loc.*

$$\begin{aligned}
\mathcal{I}_{cp}[x := \text{alloc}(e^?)](H, A) &= (H_2, A) \quad \text{if } v = \mathcal{V}[e](H, A) \\
\text{where } l_{new} &= \text{newLocation}() \\
l_p &= \begin{cases} v & \text{if } v \in \text{Loc} \\ \#ObjProto & \text{otherwise} \end{cases} \\
H_1 &= H[l_{new} \mapsto \text{NewObject}(l_p)] \\
H_2 &= \text{VarStoreE}(H_1, A, x, l_{new}, \text{true}) \\
\mathcal{I}_{cp}[x := \text{alloc}(e^?)](H, A) &= (H_1, A) \quad \text{if } exc = \mathcal{V}[e](H, A) \\
\text{where } H_1 &= \text{RaiseException}(H, exc)
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[x := \text{allocArray}(n)](H, A) &= (H_2, A) \\
\text{where } l_{new} &= \text{newLocation}() \\
n &= \mathcal{V}[n](H, A) \\
H_1 &= H[l_{new} \mapsto \text{NewArrayObject}(n)] \\
H_2 &= \text{VarStoreE}(H_1, A, x, l_{new}, \text{true})
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[x := \text{allocArg}(n)](H, A) &= (H_2, A) \\
\text{where } l_{new} &= \text{newLocation}() \\
n &= \mathcal{V}[n](H, A) \\
H_1 &= H[l_{new} \mapsto \text{NewArgObject}(n)] \\
H_2 &= \text{VarStoreE}(H_1, A, x, l_{new}, \text{true})
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[x := e](H, A) &= (H_1, A) \quad \text{if } v = \mathcal{V}[e](H, A) \\
\text{where } H_1 &= \text{VarStoreE}(H, A, x, v, \text{true}) \\
\mathcal{I}_{cp}[x := e](H, A) &= (H_1, A) \quad \text{if } exc = \mathcal{V}[e](H, A) \\
\text{where } H_1 &= \text{RaiseException}(H, exc)
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[x_1 := \text{delete}(x_2)](H, A) &= (H_2, A) \\
\text{where } l_{base} &= \text{LookupBase}(H, A, x_2) \\
(H_1, b) &= \text{Delete}(H, l_{base}, x_2) \\
H_2 &= \text{VarStoreE}(H_1, A, x_1, b, \text{true}) \\
\mathcal{I}_{cp}[x := \text{delete}(e)](H, A) &= (H_1, A) \quad \text{if } v = \mathcal{V}[e](H, A) \\
\text{where } H_1 &= \text{VarStoreE}(H, A, x, \text{true}, \text{true}) \\
\mathcal{I}_{cp}[x := \text{delete}(e)](H, A) &= (H_1, A) \quad \text{if } exc = \mathcal{V}[e](H, A) \\
\text{where } H_1 &= \text{RaiseException}(H, exc)
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[x := \text{delete}(e_1, e_2)](H, A) &= (H_2, A) \\
\text{where } l &= \mathcal{V}[e_1](H, A) \wedge s = \mathcal{V}[e_2](H, A) \\
(H_1, b) &= \text{Delete}(H, l, s) \\
H_2 &= \text{VarStoreE}(H_1, A, x, b, \text{true})
\end{aligned}$$

$$\mathcal{I}_{cp} \llbracket e_1 [e_2] = e_3 \rrbracket (H, A) = (H_1, A) \quad \text{if } exc = \mathcal{V} \llbracket e_3 \rrbracket (H, A) \\ \text{where } H_1 = \underline{\text{RaiseException}}(H, exc)$$

$$\mathcal{I}_{cp} \llbracket e_1 [e_2] = e_3 \rrbracket (H, A) = (H_1, A) \quad \text{if } \neg \text{IsArray}(H, l) \wedge \underline{\text{CanPut}}(H, l, x) \\ \text{where } l = \mathcal{V} \llbracket e_1 \rrbracket (H, A) \\ x = \mathcal{V} \llbracket e_2 \rrbracket (H, A) \\ v = \mathcal{V} \llbracket e_3 \rrbracket (H, A) \\ H_1 = \text{PropStore}(H, l, x, v) \\ \mathcal{I}_{cp} \llbracket e_1 [e_2] = e_3 \rrbracket (H, A) = (H_2, A) \quad \text{if } \text{IsArray}(H, l) \wedge \underline{\text{CanPut}}(H, l, v_{idx}) \wedge \underline{\text{IsArrayIndex}}(v_{idx}) \\ \text{where } l = \mathcal{V} \llbracket e_1 \rrbracket (H, A) \\ v_{idx} = \mathcal{V} \llbracket e_2 \rrbracket (H, A) \\ v = \mathcal{V} \llbracket e_3 \rrbracket (H, A) \\ n_{oldLen} = \text{Proto}(H, l, \text{"length"}) \\ H_1 = H[l \mapsto H(l)[v_{idx} \mapsto \{ \text{value} = v; \text{writable} = \text{true}; \text{enumerable} = \text{true}; \text{configurable} = \text{true} \}]] \\ H_2 = \begin{cases} H_1[l \mapsto H_1(l)[\text{"length"} \mapsto H(l)(\text{"length"}) \text{ with } \text{value} = v_{idx} + 1]] & \text{if } n_{oldLen} \leq v_{idx} \\ H_1 & \text{otherwise} \end{cases}$$

$$\mathcal{I}_{cp} \llbracket e_1 [\text{"length"}] = e_2 \rrbracket (H, A) = (H_2, A) \quad \text{if } \text{IsArray}(H, l) \wedge \underline{\text{CanPut}}(H, l, \text{"length"}) \wedge n_{newLen} \geq 0 \\ \text{where } l = \mathcal{V} \llbracket e_1 \rrbracket (H, A) \\ n_{oldLen} = \text{Proto}(H, l, \text{"length"}) \\ n_{newLen} = \text{toNumber}(\mathcal{V} \llbracket e_2 \rrbracket (H, A)) \\ H_1 = H[l \mapsto H(l)[\text{"length"} \mapsto H(l)(\text{"length"}) \text{ with } \text{value} = n_{newLen}]] \\ H_2 = \begin{cases} \bigsqcup_{x=n_{oldLen}-1 \text{ to } n_{newLen}} \underline{\text{Delete}}(H_1, l, x) & \text{if } n_{newLen} < n_{oldLen} \\ H_1 & \text{otherwise} \end{cases}$$

$$\mathcal{I}_{cp} \llbracket e_1 [\text{"length"}] = e_2 \rrbracket (H, A) = (H_1, A) \quad \text{if } \text{IsArray}(H, l) \\ \wedge (n_{newLen} < 0 \vee n_{newLen} \in \{ \text{NaN}, \text{Inf}, -\text{Inf} \}) \\ \text{where } l = \mathcal{V} \llbracket e_1 \rrbracket (H, A) \\ n_{newLen} = \text{toNumber}(\mathcal{V} \llbracket e_2 \rrbracket (H, A)) \\ H_1 = \underline{\text{RaiseException}}(H, \text{RangeError})$$

$$\mathcal{I}_{cp} \llbracket e_1 [e_2] = e_3 \rrbracket (H, A) = (H, A) \quad \text{if } \neg \underline{\text{CanPut}}(H, l, x) \wedge v = \mathcal{V} \llbracket e_3 \rrbracket (H, A) \\ \text{where } l = \mathcal{V} \llbracket e_1 \rrbracket (H, A) \\ x = \mathcal{V} \llbracket e_2 \rrbracket (H, A)$$

$$\mathcal{I}_{cp} \llbracket x_1 := \text{function } x_2^? (fid) \rrbracket (H, A) = \left( H_1 \left[ \begin{array}{l} l_{new1} \mapsto \underline{\text{NewFunctionObject}}(fid, A_1, l_{new2}, n), \\ l_{new2} \mapsto o_{new} \left[ \begin{array}{l} \text{"constructor"} \mapsto \left\{ \begin{array}{l} \text{value} = l_{new1}; \\ \text{writable} = \text{true}; \\ \text{enumerable} = \text{false}; \\ \text{configurable} = \text{true} \end{array} \right\} \end{array} \right] \end{array} \right], A_1 \right) \\ \text{where } l = \underline{\text{TopStack}}(A) \wedge l_{new1} = \underline{\text{newLocation}}() \wedge l_{new2} = \underline{\text{newLocation}}() \wedge l_{new3} = \underline{\text{newLocation}}() \\ H_1 = \underline{\text{VarStoreE}}(H, A, x_1, l_{new1}, \text{true}) \\ \wedge o_{new} = \underline{\text{NewObject}}(\#ObjProto) \\ \wedge l_{new3} = \{ x_2 \mapsto \{ \text{value} = l_{new1}; \text{writable} = \text{false}; \text{enumerable} = \text{false}; \text{configurable} = \text{false} \} \} \\ \wedge A_1 = \underline{\text{PushStack}}(A, l_{new3}) \\ \wedge n = |\underline{\text{getArgVars}}_P(fid)|$$



$$\mathcal{I}_{cp} \llbracket \text{construct } (e_1, e_2, e_3) \rrbracket (H, A) = \left( H \left[ \begin{array}{l} l_{arg} \mapsto H(l_{arg}) \left[ \begin{array}{l} callee \mapsto \left\{ \begin{array}{l} value = l_{fun}; \\ writable = \text{true}; \\ enumerable = \text{false}; \\ configurable = \text{true} \end{array} \right\} \\ arguments \mapsto \left\{ \begin{array}{l} value = v_{arg}; \\ writable = \text{true}; \\ enumerable = \text{false}; \\ configurable = \text{false} \end{array} \right\} \\ @this \mapsto value = l_{this}, \\ @up \mapsto A, \\ @return \mapsto H(\#temp)(@return), \end{array} \right] \end{array} \right], A_1 \right)$$

where  $\text{HasConstruct}(H, \mathcal{V}[e_1](H, A)) \wedge A_1 = \text{PushStack}(\mathcal{V}[e_1][@scope])(H, A, l_{new})$

$\wedge l = \mathcal{V}[e_1](H, A)$

$\wedge arguments = \text{getArgumentsName}_P(fid_{callee})$

$\wedge v_{arg} = \mathcal{V}[e_3](H, A)$

$\wedge l_{this} = \text{getThis}(\mathcal{V}[e_2](H, A))$

$\wedge l_{new} = \text{newLocation}() \wedge fid_{callee} = \mathcal{V}[e_1][@construct](H, A)$

$\wedge cp_{after-call} = \text{getAftercallFromCall}_P(cp)$

$\wedge \xrightarrow{\text{blue}} := \xrightarrow{\text{blue}} \cup \{ (cp, (fid_{callee}, \text{ENTRY})), ((fid_{callee}, \text{EXIT}), cp_{after-call}) \}$

$\wedge \xrightarrow{\text{exc}} := \xrightarrow{\text{exc}} \cup \{ ((fid_{callee}, \text{EXIT-EXC}), cp_{after-call}) \}$

$\wedge \text{BelongsTo} := \text{BelongsTo} \cup \{ (l_{new}, cp) \}$

$\mathcal{I}_{cp} \llbracket \text{construct } (e_1, e_2, e_3) \rrbracket (H, A) = (H_1, A) \quad \text{if } \neg \text{HasConstruct}(H, v) \vee v \notin \text{Loc}$

where  $v = \mathcal{V}[e_1](H, A)$

$H_1 = \text{RaiseException}(H, \text{TypeError})$

$\mathcal{I}_{cp} \llbracket \text{construct } (e_1, e_2, e_3) \rrbracket (H, A) = (H_1, A) \quad \text{if } exc = \mathcal{V}[e_1](H, A)$

where  $H_1 = \text{RaiseException}(H, exc)$

$$\mathcal{I}_{cp} \llbracket \text{call } (e_1, e_2, e_3) \rrbracket (H, A) = \left( H \left[ \begin{array}{l} l_{arg} \mapsto H(l_{arg}) \left[ \begin{array}{l} callee \mapsto \left\{ \begin{array}{l} value = l_{fun}; \\ writable = \text{true}; \\ enumerable = \text{false}; \\ configurable = \text{true} \end{array} \right\} \\ arguments \mapsto \left\{ \begin{array}{l} value = l_{arg}; \\ writable = \text{true}; \\ enumerable = \text{false}; \\ configurable = \text{false} \end{array} \right\} \\ @this \mapsto value = l_{this}, \\ @up \mapsto A, \\ @return \mapsto H(\#temp)(@return), \end{array} \right] \end{array} \right], A_1 \right)$$

where  $l_{fun} = \mathcal{V}[e_1](H, A) \wedge \text{IsCallable}(H, l_{fun}) \wedge A_1 = \text{PushStack}(\mathcal{V}[e_1][@scope])(H, A, l_{new})$

$\wedge arguments = \text{getArgumentsName}_P(fid_{callee})$

$\wedge l_{arg} = \mathcal{V}[e_3](H, A)$

$\wedge l_{this} = \text{getThis}(\mathcal{V}[e_2](H, A))$

$\wedge l_{new} = \text{newLocation}() \wedge fid_{callee} = \mathcal{V}[e_1][@function](H, A)$

$\wedge cp_{after-call} = \text{getAftercallFromCall}_P(cp)$

$\wedge \xrightarrow{\text{blue}} := \xrightarrow{\text{blue}} \cup \{ (cp, (fid_{callee}, \text{ENTRY})), ((fid_{callee}, \text{EXIT}), cp_{after-call}) \}$

$\wedge \xrightarrow{\text{exc}} := \xrightarrow{\text{exc}} \cup \{ ((fid_{callee}, \text{EXIT-EXC}), cp_{after-call}) \}$

$\wedge \text{BelongsTo} := \text{BelongsTo} \cup \{ (l_{new}, cp) \}$

$\mathcal{I}_{cp} \llbracket \text{call } (e_1, e_2, e_3) \rrbracket (H, A) = (H_1, A) \quad \text{if } \neg \text{IsCallable}(H, v) \vee v \notin \text{Loc}$

where  $v = \mathcal{V}[e_1](H, A)$

$H_1 = \text{RaiseException}(H, \text{TypeError})$

$\mathcal{I}_{cp} \llbracket \text{call } (e_1, e_2, e_3) \rrbracket (H, A) = (H_1, A) \quad \text{if } exc = \mathcal{V}[e_1](H, A)$

where  $H_1 = \text{RaiseException}(H, exc)$

$$\begin{aligned}
\mathcal{I}_{cp}[\text{after-call}(x)](H, A) &= \text{stuck} \quad \text{if } \neg \text{BelongsTo}(l, cp_{call}) \\
&\quad \text{where } l = \text{TopStack}(A) \\
&\quad \quad cp_{call} = \text{getCallFromAfterCall}_P(cp) \\
\mathcal{I}_{cp}[\text{after-call}(x)](H, A) &= (H_2, A_1) \quad \text{if } \text{BelongsTo}(l, cp_{call}) \\
&\quad \text{where } l = \text{TopStack}(A) \\
&\quad \quad cp_{call} = \text{getCallFromAfterCall}_P(cp) \\
&\quad \quad A_1 = H(l)(@up) \\
&\quad \quad H_1 = \text{VarStoreE}(H, A_1, x, H(\#temp)(@return), \text{true}) \\
&\quad \quad H_2 = H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto H(l)(@return)]] \\
\\
\mathcal{I}_{cp}[\text{assert}(e_1 \otimes e_2)](H, A) &= \mathcal{B}[e_1 \otimes e_2](H, A) \\
\\
\mathcal{I}_{cp}[\text{catch}(x)](H, A) &= (H_2, A) \\
&\quad \text{where } H_1 = \text{VarStore}(H, A, x, H(\#temp)(@exception), \text{true}), \\
&\quad \quad H_2 = \text{Delete}(H_1, \#temp, @exception) \\
\\
\mathcal{I}_{cp}[\text{return}(e)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \quad \text{if } v = \mathcal{V}[e](H, A) \\
\mathcal{I}_{cp}[\text{return}(e)](H, A) &= (H_1, A) \quad \text{if } exc = \mathcal{V}[e](H, A) \\
&\quad \text{where } H_1 = \text{RaiseException}(H, exc) \\
\\
\mathcal{I}_{cp}[\text{return}()](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto \text{undefined}]], A) \\
\\
\mathcal{I}_{cp}[\text{throw}(e)](H, A) &= (H_2, A) \\
&\quad \text{where } H_1 = \text{RaiseException}(H, \mathcal{V}[e](H, A)), \\
&\quad \quad \wedge H_2 = H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto \text{undefined}]] \\
\\
\mathcal{I}_{cp}[x := \text{toObject}(e)](H, A) &= (H_2, A) \quad \text{if } v = \mathcal{V}[e](H, A) \wedge (H_1, l_{new}) = \text{toObject}(H, v) \\
&\quad \text{where } H_2 = \text{VarStoreE}(H_1, A, x, l_{new}, \text{true}) \\
\mathcal{I}_{cp}[x := \text{toObject}(e)](H, A) &= (H_1, A) \quad \text{if } v = \mathcal{V}[e](H, A) \wedge (\_, exc) = \text{toObject}(H, v) \\
&\quad \text{where } H_1 = \text{RaiseException}(H, exc) \\
\mathcal{I}_{cp}[x := \text{toObject}(e)](H, A) &= (H_1, A) \quad \text{if } exc = \mathcal{V}[e](H, A) \\
&\quad \text{where } H_1 = \text{RaiseException}(H, exc) \\
\\
\mathcal{I}_{cp}[x := \text{isObject}(e)](H, A) &= (H_1, A) \quad \text{if } l = \mathcal{V}[e](H, A) \\
&\quad \text{where } H_1 = \text{VarStoreE}(H, A, x, \text{true}, \text{true}) \\
\mathcal{I}_{cp}[x := \text{isObject}(e)](H, A) &= (H_1, A) \quad \text{if } pv = \mathcal{V}[e](H, A) \\
&\quad \text{where } H_1 = \text{VarStoreE}(H, A, x, \text{false}, \text{true}) \\
\mathcal{I}_{cp}[x := \text{isObject}(e)](H, A) &= (H_1, A) \quad \text{if } exc = \mathcal{V}[e](H, A) \\
&\quad \text{where } H_1 = \text{RaiseException}(H, exc) \\
\\
\mathcal{I}_{cp}[x := \text{toString}(e)](H, A) &= (H_1, A) \quad \text{if } v = \mathcal{V}[e](H, A) \\
&\quad \text{where } pv = \text{toPrimitive}(v) \\
&\quad \quad H_1 = \text{VarStoreE}(H, A, x, \text{toString}(pv), \text{true}) \\
\mathcal{I}_{cp}[x := \text{toString}(e)](H, A) &= (H_1, A) \quad \text{if } exc = \mathcal{V}[e](H, A) \\
&\quad \text{where } H_1 = \text{RaiseException}(H, exc)
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp} \llbracket x := \diamond \text{toNumber}(e) \rrbracket (H, A) &= (H_1, A) \quad \text{if } l = \mathcal{V} \llbracket e \rrbracket (H, A) \\
&\text{where } pv = \text{toPrimitive}(l) \\
&\quad H_1 = \text{VarStoreE}(H, A, x, \text{toNumber}(pv), \text{true}) \\
\mathcal{I}_{cp} \llbracket x := \diamond \text{toNumber}(e) \rrbracket (H, A) &= (H_1, A) \quad \text{if } pv = \mathcal{V} \llbracket e \rrbracket (H, A) \\
&\text{where } H_1 = \text{VarStoreE}(H, A, x, \text{toNumber}(pv), \text{true}) \\
\mathcal{I}_{cp} \llbracket x := \diamond \text{toNumber}(e) \rrbracket (H, A) &= (H_1, A) \quad \text{if } exc = \mathcal{V} \llbracket e \rrbracket (H, A) \\
&\text{where } H_1 = \text{RaiseException}(H, exc)
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp} \llbracket x := \diamond \text{toBoolean}(e) \rrbracket (H, A) &= (H_1, A) \quad \text{if } v = \mathcal{V} \llbracket e \rrbracket (H, A) \\
&\text{where } H_1 = \text{VarStoreE}(H, A, x, \text{toBoolean}(v), \text{true}) \\
\mathcal{I}_{cp} \llbracket x := \diamond \text{toBoolean}(e) \rrbracket (H, A) &= (H_1, A) \quad \text{if } exc = \mathcal{V} \llbracket e \rrbracket (H, A) \\
&\text{where } H_1 = \text{RaiseException}(H, exc)
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp} \llbracket x_1 := \diamond \text{getBase}(x_2) \rrbracket (H, A) &= (H_1, A) \\
&\text{where } l_{base} = \text{LookupBase}(H, A, x_2) \\
&\quad H_1 = \text{VarStoreE}(H, A, x_1, l_{base}, \text{true})
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp} \llbracket x := \diamond \text{iteratorInit}(e) \rrbracket (H, A) &= (H_2, A) \\
&\text{where } l = \mathcal{V} \llbracket e \rrbracket (H, A) \\
&\quad P = \text{collectProps}(H, l) \\
&\quad o_{new} = \text{iteratorInit}(H(l), P, 0) \\
&\quad l_{new} = \text{newLocation}() \\
&\quad H_1 = H[l_{new} \mapsto o_{new}] \\
&\quad H_2 = \text{VarStoreE}(H_1, A, x, l_{new}, \text{true})
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp} \llbracket x_1 := \diamond \text{iteratorHasNext}(e, x_2) \rrbracket (H, A) &= (H_1, A) \\
&\text{where } l_1 = \mathcal{V} \llbracket x_2 \rrbracket (H, A) \\
&\quad l_2 = \mathcal{V} \llbracket e \rrbracket (H, A) \\
&\quad i = \text{next}(H, H(l_1), H(l_1)(\text{@}i), l_2) \\
&\quad b = \begin{cases} \text{true} & \text{if } i \in \text{Dom}(H(l_1)) \\ \text{false} & \text{otherwise} \end{cases} \\
&\quad H_1 = \text{VarStoreE}(H, A, x_1, b, \text{true})
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp} \llbracket x_1 := \diamond \text{iteratorNext}(e, x_2) \rrbracket (H, A) &= (H_2, A) \\
&\text{where } l_1 = \mathcal{V} \llbracket x_2 \rrbracket (H, A) \\
&\quad l_2 = \mathcal{V} \llbracket e \rrbracket (H, A) \\
&\quad i = \text{next}(H, H(l_1), H(l_1)(\text{@}i), l_2) \\
&\quad v = H(l_1)(\text{toString}(i)) \\
&\quad H_1 = H[l_1 \mapsto H(l_1)[\text{@}i \mapsto i + 1]] \\
&\quad H_2 = \text{VarStoreE}(H_1, A, x_1, v, \text{true})
\end{aligned}$$

$$\mathcal{V} \llbracket x \rrbracket (H, A) = \text{Lookup}(H, A, x)$$

$$\begin{aligned}
\mathcal{V} \llbracket e_1 \otimes e_2 \rrbracket (H, A) &= v_1 \otimes v_2 \quad \text{if } v_1 = \mathcal{V} \llbracket e_1 \rrbracket (H, A) \wedge v_2 = \mathcal{V} \llbracket e_2 \rrbracket (H, A) \\
\mathcal{V} \llbracket e_1 \otimes e_2 \rrbracket (H, A) &= exc \quad \text{if } exc = \mathcal{V} \llbracket e_1 \rrbracket (H, A) \\
\mathcal{V} \llbracket e_1 \otimes e_2 \rrbracket (H, A) &= exc \quad \text{if } v = \mathcal{V} \llbracket e_1 \rrbracket (H, A) \wedge exc = \mathcal{V} \llbracket e_2 \rrbracket (H, A)
\end{aligned}$$

$$\begin{aligned}
\mathcal{V} \llbracket \ominus e \rrbracket (H, A) &= \ominus v \quad \text{if } v = \mathcal{V} \llbracket e \rrbracket (H, A) \\
\mathcal{V} \llbracket \ominus e \rrbracket (H, A) &= exc \quad \text{if } exc = \mathcal{V} \llbracket e \rrbracket (H, A)
\end{aligned}$$

$$\mathcal{V} \llbracket e_1 [e_2] \rrbracket (H, A) = v \quad \text{where } l = \mathcal{V} \llbracket e_1 \rrbracket (H, A) \wedge s = \mathcal{V} \llbracket e_2 \rrbracket (H, A) \wedge v = \text{Proto}(H, l, s)$$

$$\mathcal{V} \llbracket n \rrbracket (H, A) = n$$

$$\mathcal{V} \llbracket \text{"s"} \rrbracket (H, A) = s$$

$$\begin{aligned}
\mathcal{V}[\text{true}](H, A) &= \text{true} \\
\mathcal{V}[\text{false}](H, A) &= \text{false} \\
\mathcal{V}[\text{null}](H, A) &= \text{null} \\
\mathcal{V}[\text{this}](H, A) &= l_{\text{this}} \quad \text{where } l_{\text{this}} = H(l)(\text{@this}) \wedge l = \text{TopStack}(A) \\
\mathcal{V}[e_1 \text{ instanceof } e_2](H, A) &= \text{inherit}(H, H(l_1)(\text{@proto}), l_3) \\
&\quad \text{where } \text{HasConstruct}(H, l_2) \\
&\quad \quad \wedge l_1 = \mathcal{V}[e_1](H, A) \wedge l_2 = \mathcal{V}[e_2](H, A) \\
&\quad \quad \wedge l_3 = \text{Proto}(H, l_2, \text{"prototype"}) \\
\mathcal{V}[e_1 \text{ instanceof } e_2](H, A) &= \text{false} \\
&\quad \text{where } \text{HasConstruct}(H, l_2) \\
&\quad \quad \wedge \mathcal{V}[e_1](H, A) \in \text{PValue} \wedge l_2 = \mathcal{V}[e_2](H, A) \\
\mathcal{V}[e_1 \text{ instanceof } e_2](H, A) &= \text{TypeError} \\
&\quad \text{where } \mathcal{V}[e_2](H, A) \in \text{PValue} \vee (\neg \text{HasConstruct}(H, l_2) \wedge l_2 = \mathcal{V}[e_2](H, A)) \\
\mathcal{V}[e_1 \text{ instanceof } e_2](H, A) &= \text{TypeError} \\
&\quad \text{where } \text{HasConstruct}(H, l_2) \wedge l_2 = \mathcal{V}[e_2](H, A) \wedge \text{Proto}(H, l_2, \text{"prototype"}) \in \text{PValue} \\
\mathcal{V}[e_1 \text{ instanceof } e_2](H, A) &= \text{exc} \\
&\quad \text{where } \text{exc} = \mathcal{V}[e_1](H, A) \in \text{Exception} \\
\mathcal{V}[e_1 \text{ instanceof } e_2](H, A) &= \text{exc} \\
&\quad \text{where } v = \mathcal{V}[e_1](H, A) \wedge \text{exc} = \mathcal{V}[e_2](H, A) \in \text{Exception} \\
\\
\mathcal{V}[e_1 \text{ in } e_2](H, A) &= \text{HasProperty}(H, l, x) \\
&\quad \text{where } v = \mathcal{V}[e_1](H, A) \wedge l = \mathcal{V}[e_2](H, A) \\
&\quad \quad \wedge x = \text{toString}(\text{toPrimitive}(v)) \\
\mathcal{V}[e_1 \text{ in } e_2](H, A) &= \text{TypeError} \\
&\quad \text{where } \mathcal{V}[e_1](H, A) \in \text{Value} \wedge \mathcal{V}[e_2](H, A) \in \text{PValue} \\
\mathcal{V}[e_1 \text{ in } e_2](H, A) &= \mathcal{V}[e_1](H, A) \\
&\quad \text{where } \mathcal{V}[e_1](H, A) \in \text{Exception} \\
\mathcal{V}[e_1 \text{ in } e_2](H, A) &= \text{exc} \\
&\quad \text{where } v = \mathcal{V}[e_1](H, A) \wedge \text{exc} = \mathcal{V}[e_2](H, A) \\
\\
\mathcal{V}[\text{typeof } e](H, A) &= \text{TypeTag}(H, v) \quad \text{if } v = \mathcal{V}[e](H, A) \\
\mathcal{V}[\text{typeof } e](H, A) &= \text{exc} \quad \text{if } \text{exc} = \mathcal{V}[e](H, A) \\
\\
\mathcal{B}[e](H, A) &= S \\
&\quad \text{where } \mathcal{V}[e](H, A) = v \\
&\quad \quad S = \begin{cases} (H, A) & \text{toBoolean}(v) = \text{true} \\ \text{stuck} & \text{toBoolean}(v) = \text{false} \end{cases} \\
\mathcal{B}[e](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[\text{@exception} \mapsto l_e]], A) \\
&\quad \text{where } \mathcal{V}[e](H, A) = \text{exc} \\
&\quad \quad l_e = \text{newLocation}() \\
&\quad \quad H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{exc})] \\
\\
\ominus ::= \text{void} \mid + \mid - \mid \sim \mid ! \\
\otimes ::= \mid \& \mid ^ \mid << \mid >> \mid >>> \\
&\quad \mid + \mid - \mid * \mid / \mid \% \mid == \mid != \mid === \mid !== \mid < \mid > \mid <= \mid >=
\end{aligned}$$

We consider the collecting semantics of program  $P$  that is characterized by an invariant  $\llbracket P \rrbracket \in \mathbb{C} \rightarrow \wp(\text{State})$ , collecting a set of reachable states at each control point. The collecting semantics is defined by the least fixpoint of composition of semantic functions  $F_{\text{control-flow}}, F_{\text{exception-flow}} \in (\mathbb{C} \rightarrow \wp(\text{State})) \rightarrow (\mathbb{C} \rightarrow \wp(\text{State}))$  such that,

$$\begin{aligned}
\text{ExcFlow}(S) &= \{ (H, A) \mid \text{stuck} \neq (H, A) \in S \wedge \text{HasProperty}(H, \#temp, \text{@exception}) \} \\
\text{NormalFlow}(S) &= \{ (H, A) \mid \text{stuck} \neq (H, A) \in S \wedge \neg \text{HasProperty}(H, \#temp, \text{@exception}) \} \\
f_{cp} &= \mathcal{C}_{cp}(\text{getCmd}_P(cp)) \\
F_{\text{control-flow}}(X) &= \lambda cp \in \mathbb{C}. \bigcup_{cp' \mapsto cp} f_{cp'}(\text{NormalFlow}(X(cp'))) \\
F_{\text{exception-flow}}(X) &= \lambda cp \in \mathbb{C}. \bigcup_{cp' \xrightarrow{\text{exc}} cp} f_{cp'}(\text{ExcFlow}(X(cp'))) \\
F &= F_{\text{control-flow}} \circ F_{\text{exception-flow}}
\end{aligned}$$

## Chapter 9

# CFG Abstract Semantics

`.../jsaf/analysis/typing/{package, Config}.scala`

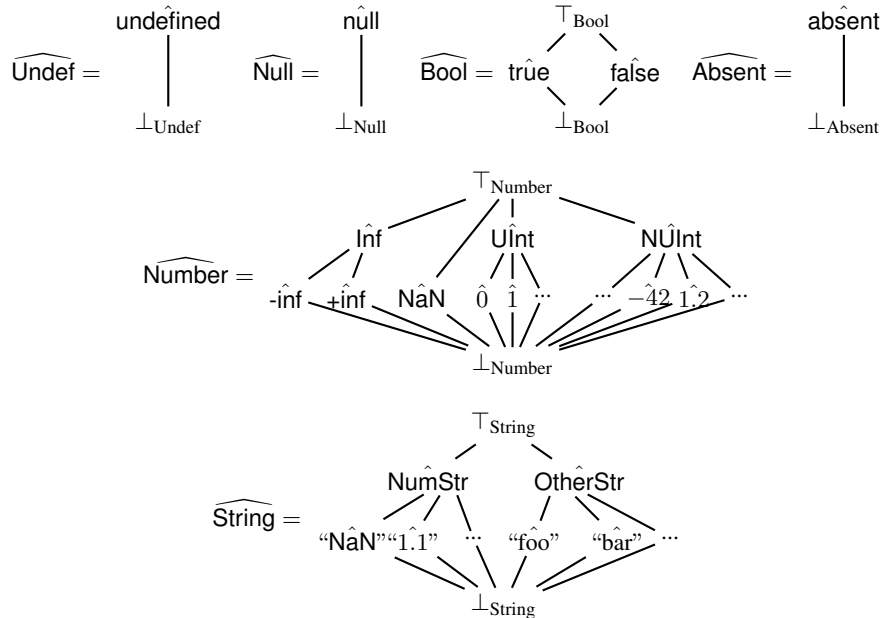
Assumptions and limitations are as follows:

- When a value is updated, a part of  $\widehat{\text{PropValue}}$  type value is directly used instead of  $\widehat{\text{PropValue}} \times \widehat{\text{Absent}}$ . In this case, the  $\widehat{\text{Absent}}$  value and the rest parts of  $\widehat{\text{PropValue}}$  is considered as  $\perp$ .  
e.g.)  $x \mapsto \langle \hat{v}, \hat{\text{false}}, \hat{\text{false}} \hat{\text{false}} \rangle$  means  $x \mapsto \langle \langle \hat{v}, \hat{\text{false}}, \hat{\text{false}} \hat{\text{false}} \rangle, \perp_{\text{Value}}, \perp_{\text{FunctionId}} \rangle, \perp_{\text{Absent}} \rangle$ .
- Semantics for helper functions is not written using denotational semantics(they are not compositional).
- For appropriate type conversion, a subscript is used. In this case, all the implicit values can be considered as  $\perp$ .
- We maintain mutable inter-procedural edge set ( $\xrightarrow{\text{ip}}$ ) throughout semantics.

## 9.1 Settings

`.../jsaf/analysis/typing/domain/{package, AbsDomain, DomainPrinter}.scala1`

$\hat{c}p \in$	$\widehat{\text{ControlPoint}}$	$=$	$\text{Node} \times \widehat{\text{CallContext}}$
$\hat{c}c \in$	$\widehat{\text{CallContext}}$	$=$	<i>Parameterized context-sensitivity. See Section 9.4</i>
$\hat{S}, (\hat{H}, \hat{C}) \in$	$\widehat{\text{State}}$	$=$	$\widehat{\text{Heap}} \times \widehat{\text{Context}}$
$\hat{H} \in$	$\widehat{\text{Heap}}$	$=$	$\widehat{\text{Loc}} \xrightarrow{\text{fin}} \widehat{\text{Obj}}$
$\hat{C} \in$	$\widehat{\text{Context}}$	$=$	$\wp(\widehat{\text{Loc}}) \times \wp(\widehat{\text{Loc}}) \times \wp(\widehat{\text{Address}}) \times \wp(\widehat{\text{Address}})$ <i>variable environment, this (moved to #PureLocal), may old, must old</i>
$\hat{l}_R, \hat{l}_O, \hat{l} \in$	$\widehat{\text{Loc}}$	$=$	$\widehat{\text{Address}} \times \widehat{\text{RecencyTag}}$
$\hat{a} \in$	$\widehat{\text{Address}}$	$::=$	$\#Global \mid \#StringProto \mid \#BooleanProto \mid \#FunctionProto$ $\mid \#RefErr \mid \#RangeErr \mid \#TypeErr \mid \#RefErrProto$ $\mid \#RangeErrProto \mid \#ArrayProto \mid \#TypeErrProto$ $\mid \#ObjProto \mid \#PureLocal \mid \#GlobalCallsite \mid \#Collapsed$ $\mid \hat{a}_1 \mid \dots$
	$\widehat{\text{RecencyTag}}$	$::=$	$Recent \mid Old$
$\hat{o} \in$	$\widehat{\text{Obj}}$	$=$	$\text{Prop} \xrightarrow{\text{fin}} \text{PropValue} \times \widehat{\text{Absent}}$
$propv \in$	$\widehat{\text{PropValue}}$	$=$	$\text{ObjectValue} \times \text{Value} \times \wp(\text{FunctionId})$
$\hat{ov} \in$	$\widehat{\text{ObjectValue}}$	$=$	$\text{Value} \times \text{Bool} \times \text{Bool} \times \text{Bool}$ <i>value, writable, enumerable, configurable</i>
$\hat{v} \in$	$\widehat{\text{Value}}$	$=$	$\text{PValue} \times \wp(\widehat{\text{Loc}})$
$\hat{pv} \in$	$\widehat{\text{PValue}}$	$=$	$\widehat{\text{Undef}} \times \widehat{\text{Null}} \times \widehat{\text{Bool}} \times \widehat{\text{Number}} \times \widehat{\text{String}}$
$\hat{exc} \in$	$\widehat{\text{Exception}}$	$::=$	$\text{Error} \mid \text{EvalError} \mid \text{RangeError} \mid \text{ReferenceError} \mid \text{SyntaxError} \mid \text{TypeError} \mid \text{URIError}$
	$\widehat{\text{IPEdge}}$	$=$	$\widehat{\text{ControlPoint}} \times \widehat{\text{ControlPoint}} \times \widehat{\text{Context}} \times \widehat{\text{Obj}}$
$\xrightarrow{\text{ip}} \in$	$\wp(\widehat{\text{IPEdge}})$		
$pe \in$	$\widehat{\text{PrunExpression}}$	$=$	$\{x, e_1[e_2]\}$
$re \in$	$\widehat{\text{RelExpr}}$	$=$	$\text{Expression} \S \text{Expression}$
$\S \in$	$\widehat{\text{IROP}}$	$=$	$\text{IRRelOP} \cup \text{IRObjOP}$
	$\widehat{\text{IRRelOP}}$	$=$	$== \mid != \mid === \mid !== \mid > \mid >= \mid < \mid <= \mid$
	$\widehat{\text{IRObjOP}}$	$=$	$\text{in} \mid \text{notIn} \mid \text{instanceof} \mid \text{notInstanceOf}$



<sup>1</sup> Among the  $\widehat{\text{IROP}}$  operators, we handle only  $==$ ,  $!=$ ,  $===$ , and  $!==$  for now as the  $\widehat{\text{K}}$  function describes in Section 6.2.



## 9.2 Domain Operators

$$\begin{aligned} \text{Heap Order} & : \widehat{\text{Heap}} \times \widehat{\text{Heap}} \rightarrow \text{Boolean} \\ \hat{H}_1 \sqsubseteq \hat{H}_2 & \stackrel{\text{def}}{=} \text{dom}(\hat{H}_1) \subseteq \text{dom}(\hat{H}_2) \wedge \forall \hat{l} \in \text{dom}(\hat{H}_1) : \hat{H}_1(\hat{l}) \sqsubseteq \hat{H}_2(\hat{l}) \end{aligned}$$

$$\begin{aligned} \text{Heap Join} & : \widehat{\text{Heap}} \times \widehat{\text{Heap}} \rightarrow \widehat{\text{Heap}} \\ \hat{H}_1 \sqcup \hat{H}_2 & \stackrel{\text{def}}{=} \forall \hat{l} \in \text{dom}(\hat{H}_1) \cup \text{dom}(\hat{H}_2) : \begin{cases} \left[ \hat{l} \mapsto \hat{H}_1(\hat{l}) \sqcup \hat{H}_2(\hat{l}) \right] & \text{if } \hat{l} \in \text{dom}(\hat{H}_1) \wedge \hat{l} \in \text{dom}(\hat{H}_2) \\ \left[ \hat{l} \mapsto \hat{H}_2(\hat{l}) \right] & \text{if } \hat{l} \notin \text{dom}(\hat{H}_1) \wedge \hat{l} \in \text{dom}(\hat{H}_2) \\ \left[ \hat{l} \mapsto \hat{H}_1(\hat{l}) \right] & \text{if } \hat{l} \in \text{dom}(\hat{H}_1) \wedge \hat{l} \notin \text{dom}(\hat{H}_2) \end{cases} \end{aligned}$$

$$\begin{aligned} \text{Heap Domain In} & : \widehat{\text{Heap}} \times \widehat{\text{Loc}} \rightarrow \text{Boolean} \\ \hat{l} \in \text{dom}(\hat{H}) & \stackrel{\text{def}}{=} \begin{cases} \text{true} & \text{if } \hat{l} \in \{\hat{l}' \mid (\hat{l}', \hat{o}) \in \hat{H}\} \\ \text{false} & \text{otherwise} \end{cases} \end{aligned}$$

*Although  $\perp_{Obj}$  is returned for non-existent locations, heap is still partial function.*

$$\begin{aligned} \text{Heap Lookup} & : \widehat{\text{Heap}} \times \widehat{\text{Loc}} \rightarrow \widehat{\text{Obj}} \\ \hat{H}(\hat{l}) & \stackrel{\text{def}}{=} \begin{cases} \hat{o} & \text{if } (\hat{l}, \hat{o}) \in \hat{H} \\ \perp_{Obj} & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \text{Heap Update} & : \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{Obj}} \rightarrow \widehat{\text{Heap}} \\ \hat{H}[\hat{l} \mapsto \hat{o}] & \stackrel{\text{def}}{=} \begin{cases} \{(\hat{l}, \hat{o})\} \cup (\hat{H} - \hat{l}) & \text{if } \hat{l} = \hat{l}_R \wedge \hat{o} \neq \perp_{Obj} \\ \perp_{Heap} & \text{if } \hat{l} = \hat{l}_R \wedge \hat{o} = \perp_{Obj} \\ \{(\hat{l}, \hat{H}(\hat{l}) \sqcup \hat{o})\} \cup (\hat{H} - \hat{l}) & \text{if } \hat{l} = \hat{l}_O \wedge \hat{H}(\hat{l}) \sqcup \hat{o} \neq \perp_{Obj} \\ \perp_{Heap} & \text{if } \hat{l} = \hat{l}_O \wedge \hat{H}(\hat{l}) \sqcup \hat{o} = \perp_{Obj} \end{cases} \end{aligned}$$

$$\begin{aligned} \text{Context Order} & : \widehat{\text{Context}} \times \widehat{\text{Context}} \rightarrow \text{Boolean} \\ \hat{C}_1 \sqsubseteq \hat{C}_2 & \stackrel{\text{def}}{=} \hat{C}_1.3 \subseteq \hat{C}_2.3 \wedge \\ & \hat{C}_1.4 \supseteq \hat{C}_2.4 \quad \text{order is opposite for must old set} \end{aligned}$$

$$\begin{aligned} \text{Context Join} & : \widehat{\text{Context}} \times \widehat{\text{Context}} \rightarrow \widehat{\text{Context}} \\ \hat{C}_1 \sqcup \hat{C}_2 & \stackrel{\text{def}}{=} \langle \{\}, \{\}, \hat{C}_1.3 \cup \hat{C}_2.3, \hat{C}_1.4 \cap \hat{C}_2.4 \rangle \end{aligned}$$

$$\begin{aligned} \text{Obj Order} & : \widehat{\text{Obj}} \times \widehat{\text{Obj}} \rightarrow \text{Boolean} \\ \hat{o}_1 \sqsubseteq \hat{o}_2 & \stackrel{\text{def}}{=} \forall x \in \text{dom}(\hat{o}_1) \cup \text{dom}(\hat{o}_2) : \hat{o}_1(x) \sqsubseteq \hat{o}_2(x) \end{aligned}$$

$$\begin{aligned} \text{Obj Join} & : \widehat{\text{Obj}} \times \widehat{\text{Obj}} \rightarrow \widehat{\text{Obj}} \\ \hat{o}_1 \sqcup \hat{o}_2 & \stackrel{\text{def}}{=} \forall x \in \text{dom}(\hat{o}_1) \cup \text{dom}(\hat{o}_2) : [x \mapsto \hat{o}_1(x) \sqcup \hat{o}_2(x)] \end{aligned}$$

$$\begin{aligned} \text{Obj Domain In} & : \widehat{\text{Obj}} \times \widehat{\text{String}} \rightarrow \widehat{\text{Bool}} \\ \hat{s} \in \text{dom}(\hat{o}) & \stackrel{\text{def}}{=} \begin{cases} x \in \text{dom}(\hat{o}) & \text{if } \hat{o} \neq \perp_{Obj} \wedge \hat{s} = \text{NumStrSingle}(x) \\ x \in \text{dom}(\hat{o}) & \text{if } \hat{o} \neq \perp_{Obj} \wedge \hat{s} = \text{OtherStrSingle}(x) \\ \hat{b}_1 & \text{if } \hat{o} \neq \perp_{Obj} \wedge \hat{s} = \text{NumStr} \\ \hat{b}_2 & \text{if } \hat{o} \neq \perp_{Obj} \wedge \hat{s} = \text{OtherStr} \\ \hat{b}_3 & \text{if } \hat{o} \neq \perp_{Obj} \wedge \hat{s} = \top_{String} \\ \perp_{Bool} & \text{if } \hat{o} = \perp_{Obj} \vee \hat{s} = \perp_{String} \end{cases} \\ \text{where } \hat{b}_1 & = \begin{cases} \top_{Bool} & \text{if } \hat{o}(@\text{default\_number}).1.1.1 \not\sqsubseteq \perp_{Value} \\ \top_{Bool} & \text{if } \hat{o}(@\text{default\_number}).1.1.1 \sqsubseteq \perp_{Value} \\ & \wedge \exists x \in \text{dom}(\hat{o}) : x \in \text{String} \wedge \text{“}x\text{”} \sqsubseteq \text{NumStr} \\ \text{false} & \text{otherwise} \end{cases} \\ \hat{b}_2 & = \begin{cases} \top_{Bool} & \text{if } \hat{o}(@\text{default\_other}).1.1.1 \not\sqsubseteq \perp_{Value} \\ \top_{Bool} & \text{if } \hat{o}(@\text{default\_other}).1.1.1 \sqsubseteq \perp_{Value} \\ & \wedge \exists x \in \text{dom}(\hat{o}) : x \in \text{String} \wedge \text{“}x\text{”} \sqsubseteq \text{OtherStr} \\ \text{false} & \text{otherwise} \end{cases} \\ \hat{b}_3 & = \begin{cases} \top_{Bool} & \text{if } \hat{o}(@\text{default\_number}).1.1.1 \not\sqsubseteq \perp_{Value} \vee \hat{o}(@\text{default\_other}).1.1.1 \not\sqsubseteq \perp_{Value} \\ \top_{Bool} & \text{if } \hat{o}(@\text{default\_number}).1.1.1 \sqsubseteq \perp_{Value} \wedge \hat{o}(@\text{default\_other}).1.1.1 \sqsubseteq \perp_{Value} \\ & \wedge \exists x \in \text{dom}(\hat{o}) : x \in \text{String} \\ \text{false} & \text{otherwise} \end{cases} \end{aligned}$$



$$\begin{aligned}
\text{Obj Domain In} & : \widehat{\text{Obj}} \times \text{Prop} \rightarrow \widehat{\text{Bool}} \\
x \in \text{dom}(\hat{o}) & \stackrel{\text{def}}{=} \begin{cases} \hat{b} & \text{if } \hat{o} \neq \perp_{\text{Obj}} \\ \perp_{\text{Bool}} & \text{if } \hat{o} = \perp_{\text{Obj}} \\ \text{true} & \text{if } \hat{o}(x) \not\sqsubseteq \perp \wedge \text{absent} \not\sqsubseteq \hat{o}(x).2 \\ \top_{\text{Bool}} & \text{if } \hat{o}(x) \not\sqsubseteq \perp \wedge \text{absent} \sqsubseteq \hat{o}(x).2 \\ \top_{\text{Bool}} & \text{if } \hat{o}(x) \sqsubseteq \perp \wedge x \in \text{String} \wedge \alpha(x) \sqsubseteq \text{NumStr} \\ & \quad \wedge \hat{o}(@\text{default\_number}).1.1.1 \not\sqsubseteq \perp_{\text{Value}} \\ \top_{\text{Bool}} & \text{if } \hat{o}(x) \sqsubseteq \perp \wedge x \in \text{String} \wedge \alpha(x) \sqsubseteq \text{OtherStr} \\ & \quad \wedge \hat{o}(@\text{default\_other}).1.1.1 \not\sqsubseteq \perp_{\text{Value}} \\ \text{false} & \text{if } \hat{o}(x) \sqsubseteq \perp \wedge x \in \text{String} \wedge \alpha(x) \sqsubseteq \text{NumStr} \\ & \quad \wedge \hat{o}(@\text{default\_number}).1.1.1 \sqsubseteq \perp_{\text{Value}} \\ \text{false} & \text{if } \hat{o}(x) \sqsubseteq \perp \wedge x \in \text{String} \wedge \alpha(x) \sqsubseteq \text{OtherStr} \\ & \quad \wedge \hat{o}(@\text{default\_other}).1.1.1 \sqsubseteq \perp_{\text{Value}} \\ \text{false} & \text{if } \hat{o}(x) \sqsubseteq \perp \wedge x \notin \text{String} \\ \text{false} & \text{otherwise} \end{cases} \\
\text{where } \hat{b} & =
\end{aligned}$$

$$\begin{aligned}
\text{Obj Lookup} & : \widehat{\text{Obj}} \times \widehat{\text{String}} \rightarrow \widehat{\text{PropValue}} \times \widehat{\text{Absent}} \\
\hat{o}(\hat{s}) & \stackrel{\text{def}}{=} \begin{cases} \hat{o}(x) & \text{if } \hat{s} = \text{NumStrSingle}(x) \\ \hat{o}(x) & \text{if } \hat{s} = \text{OtherStrSingle}(x) \\ \langle (\bigsqcup_{x \in P_1} \hat{o}(x)).1 \sqcup \hat{o}(@\text{default\_number}).1, \top_{\text{Absent}} \rangle & \text{if } \hat{s} = \text{NumStr} \\ \langle (\bigsqcup_{x \in P_2} \hat{o}(x)).1 \sqcup \hat{o}(@\text{default\_other}).1, \top_{\text{Absent}} \rangle & \text{if } \hat{s} = \text{OtherStr} \\ \left\langle \left( \bigsqcup_{x \in P_3} \hat{o}(x) \right).1 \sqcup \hat{o}(@\text{default\_number}).1, \top_{\text{Absent}} \right\rangle & \text{if } \hat{s} = \top_{\text{String}} \\ \perp_{\text{PropValue} \times \text{Absent}} & \text{if } \hat{s} = \perp_{\text{String}} \end{cases} \\
\text{where } P_1 & = \{x \mid x \in \text{dom}(\hat{o}) \wedge x \in \text{String} \wedge \hat{x} \sqsubseteq \text{NumStr}\} \\
P_2 & = \{x \mid x \in \text{dom}(\hat{o}) \wedge x \in \text{String} \wedge \hat{x} \sqsubseteq \text{OtherStr}\} \\
P_3 & = \{x \mid x \in \text{dom}(\hat{o}) \wedge x \in \text{String}\}
\end{aligned}$$

$$\begin{aligned}
\text{Obj Lookup} & : \widehat{\text{Obj}} \times \text{Prop} \rightarrow \widehat{\text{PropValue}} \times \widehat{\text{Absent}} \\
\hat{o}(x) & \stackrel{\text{def}}{=} \begin{cases} \langle \text{propv}, \text{abs} \rangle & \text{if } x \rightarrow \langle \text{propv}, \text{abs} \rangle \in \hat{o} \\ \langle \perp_{\text{PropValue}}, \perp_{\text{Absent}} \rangle & \text{if } x \rightarrow \langle \text{propv}, \text{abs} \rangle \notin \hat{o} \wedge x \notin \text{String} \\ \langle \text{propv}_2, \text{abs}_2 \rangle & \text{if } x \rightarrow \langle \text{propv}_1, \text{abs}_1 \rangle \notin \hat{o} \wedge x \in \text{String} \\ & \quad \wedge \alpha(x) \sqsubseteq \text{NumStr} \wedge @\text{default\_number} \rightarrow \langle \text{propv}_2, \text{abs}_2 \rangle \in \hat{o} \\ \langle \text{propv}_3, \text{abs}_3 \rangle & \text{if } x \rightarrow \langle \text{propv}_1, \text{abs}_1 \rangle \notin \hat{o} \wedge x \in \text{String} \\ & \quad \wedge \alpha(x) \sqsubseteq \text{OtherStr} \wedge @\text{default\_other} \rightarrow \langle \text{propv}_3, \text{abs}_3 \rangle \in \hat{o} \end{cases}
\end{aligned}$$

*Obj Update* :  $\widehat{\text{Obj}} \times \widehat{\text{String}} \times \widehat{\text{PropValue}} \rightarrow \widehat{\text{Obj}}$

$$\hat{o}[\hat{s} \mapsto \text{pr}\hat{o}pv] \stackrel{\text{def}}{=} \begin{cases} \hat{o}[x \mapsto \text{pr}\hat{o}pv] & \text{if } \hat{o} \neq \perp_{Obj} \wedge \hat{s} = \text{NumStrSingle}(x) \\ \hat{o}[x \mapsto \text{pr}\hat{o}pv] & \text{if } \hat{o} \neq \perp_{Obj} \wedge \hat{s} = \text{OtherStrSingle}(x) \\ \hat{o} \left[ \begin{array}{l} \forall x \in P_1 : x \mapsto \hat{o}(x) \sqcup \text{pr}\hat{o}pv, \\ @default\_number \mapsto \hat{o}(@default\_number) \sqcup \text{pr}\hat{o}pv \end{array} \right] & \text{if } \hat{o} \neq \perp_{Obj} \wedge \hat{s} = \text{NumStr} \\ \hat{o} \left[ \begin{array}{l} \forall x \in P_2 : x \mapsto \hat{o}(x) \sqcup \text{pr}\hat{o}pv, \\ @default\_other \mapsto \hat{o}(@default\_other) \sqcup \text{pr}\hat{o}pv \end{array} \right] & \text{if } \hat{o} \neq \perp_{Obj} \wedge \hat{s} = \text{OtherStr} \\ \hat{o} \left[ \begin{array}{l} \forall x \in P_3 : x \mapsto \hat{o}(x) \sqcup \text{pr}\hat{o}pv, \\ @default\_number \mapsto \hat{o}(@default\_number) \sqcup \text{pr}\hat{o}pv, \\ @default\_other \mapsto \hat{o}(@default\_other) \sqcup \text{pr}\hat{o}pv \end{array} \right] & \text{if } \hat{o} \neq \perp_{Obj} \wedge \hat{s} = \top_{String} \\ \perp_{Obj} & \text{if } \hat{o} = \perp_{Obj} \vee \hat{s} = \perp_{String} \end{cases}$$

where  $P_1 = \{x \mid x \in \text{dom}(\hat{o}) \wedge x \in \text{String} \wedge \hat{x} \sqsubseteq \text{NumStr}\}$   
 $P_2 = \{x \mid x \in \text{dom}(\hat{o}) \wedge x \in \text{String} \wedge \hat{x} \sqsubseteq \text{OtherStr}\}$   
 $P_3 = \{x \mid x \in \text{dom}(\hat{o}) \wedge x \in \text{String}\}$

*Obj Update* :  $\widehat{\text{Obj}} \times \text{Prop} \times \widehat{\text{PropValue}} \rightarrow \widehat{\text{Obj}}$

$$\hat{o}[x \mapsto \text{pr}\hat{o}pv] \stackrel{\text{def}}{=} \begin{cases} \{(x, \langle \text{pr}\hat{o}pv, \perp_{Absent} \rangle)\} \cup (\hat{o} \setminus \{(x, \langle \text{pr}\hat{o}pv', \hat{a}bs' \rangle)\}) & \text{if } \hat{o} \neq \perp_{Obj} \\ \perp_{Obj} & \text{if } \hat{o} = \perp_{Obj} \end{cases}$$

*Obj Update* :  $\widehat{\text{Obj}} \times \text{Prop} \times \widehat{\text{PropValue}} \times \widehat{\text{Absent}} \rightarrow \widehat{\text{Obj}}$

$$\hat{o}[x \mapsto \langle \text{pr}\hat{o}pv, \hat{a}bs \rangle] \stackrel{\text{def}}{=} \begin{cases} \{(x, \langle \text{pr}\hat{o}pv, \hat{a}bs \rangle)\} \cup (\hat{o} \setminus \{(x, \langle \text{pr}\hat{o}pv', \hat{a}bs' \rangle)\}) & \text{if } \hat{o} \neq \perp_{Obj} \\ \perp_{Obj} & \text{if } \hat{o} = \perp_{Obj} \end{cases}$$

*Obj Remove* :  $\widehat{\text{Obj}} \times \widehat{\text{String}} \rightarrow \widehat{\text{Obj}}$

$$\hat{o} - \hat{s} \stackrel{\text{def}}{=} \begin{cases} \hat{o} - x & \text{if } \hat{o} \neq \perp_{Obj} \wedge \hat{s} = \text{NumStrSingle}(x) \\ \hat{o} - x & \text{if } \hat{o} \neq \perp_{Obj} \wedge \hat{s} = \text{OtherStrSingle}(x) \\ \hat{o} \sqcup \bigsqcup_{x \in P_1} \{(y, \langle \text{pr}\hat{o}pv, \hat{a}bs \rangle) \mid (y, \langle \text{pr}\hat{o}pv, \hat{a}bs \rangle) \in \hat{o} \wedge y \neq x\} & \text{if } \hat{o} \neq \perp_{Obj} \wedge \hat{s} = \text{NumStr} \\ \hat{o} \sqcup \bigsqcup_{x \in P_2} \{(y, \langle \text{pr}\hat{o}pv, \hat{a}bs \rangle) \mid (y, \langle \text{pr}\hat{o}pv, \hat{a}bs \rangle) \in \hat{o} \wedge y \neq x\} & \text{if } \hat{o} \neq \perp_{Obj} \wedge \hat{s} = \text{OtherStr} \\ \hat{o} \sqcup \bigsqcup_{x \in P_3} \{(y, \langle \text{pr}\hat{o}pv, \hat{a}bs \rangle) \mid (y, \langle \text{pr}\hat{o}pv, \hat{a}bs \rangle) \in \hat{o} \wedge y \neq x\} & \text{if } \hat{o} \neq \perp_{Obj} \wedge \hat{s} = \top_{String} \\ \perp_{Obj} & \text{if } \hat{o} = \perp_{Obj} \vee \hat{s} = \perp_{String} \end{cases}$$

where  $P_1 = \{x \mid x \in \text{dom}(\hat{o}) \wedge x \in \text{String} \wedge \text{true} \sqsubseteq \hat{o}(x).1.1.4 \wedge \hat{x} \sqsubseteq \text{NumStr}\}$   
 $P_2 = \{x \mid x \in \text{dom}(\hat{o}) \wedge x \in \text{String} \wedge \text{true} \sqsubseteq \hat{o}(x).1.1.4 \wedge \hat{x} \sqsubseteq \text{OtherStr}\}$   
 $P_3 = \{x \mid x \in \text{dom}(\hat{o}) \wedge x \in \text{String} \wedge \text{true} \sqsubseteq \hat{o}(x).1.1.4\}$

*Obj Remove* :  $\widehat{\text{Obj}} \times \text{Prop} \rightarrow \widehat{\text{Obj}}$

$$\hat{o} - x \stackrel{\text{def}}{=} \begin{cases} \{(y, \langle \text{pr}\hat{o}pv, \hat{a}bs \rangle) \mid (y, \langle \text{pr}\hat{o}pv, \hat{a}bs \rangle) \in \hat{o} \wedge y \neq x\} & \text{if } \hat{o} \neq \perp_{Obj} \\ \perp_{Obj} & \text{if } \hat{o} = \perp_{Obj} \end{cases}$$

$\S^t$

:  $\text{IRRelOP} \rightarrow \text{IRRelOP}$

$$\S^t = \begin{cases} < & \text{if } \S = > \\ <= & \text{if } \S = >= \\ > & \text{if } \S = < \\ >= & \text{if } \S = <= \\ \S & \text{otherwise} \end{cases}$$

### 9.3 Helper Functions

.../jsaf/analysis/typing/Helper.scala

CanPut :  $\widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \rightarrow \widehat{\text{Bool}}$   
 $\widehat{\text{CanPut}}(\hat{H}, \hat{l}, \hat{s}) = \widehat{\text{CanPutHelp}}(\hat{H}, \hat{l}, \hat{s}, \hat{l})$

*Cycle in prototype chain is detected at implementation level.*

CanPutHelp :  $\widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \times \widehat{\text{Loc}} \rightarrow \widehat{\text{Bool}}$   
 $\widehat{\text{CanPutHelp}}(\hat{H}, \hat{l}_1, \hat{s}, \hat{l}_2) = \hat{b}_1 \sqcup \hat{b}_2$   
 where  $\hat{b}_1 = \begin{cases} \hat{H}(\hat{l}_1)(\hat{s}).1.1.2 \text{ // writable attribute} & \text{if } \text{true} \sqsubseteq (\hat{s} \in \text{dom}(\hat{H}(\hat{l}_1))) \\ \perp_{\text{Bool}} & \text{otherwise} \end{cases}$   
 $\hat{L}_{\text{proto}} = \hat{H}(\hat{l}_1)(\text{@proto}).1.1.1.2 \text{ // } \wp(\widehat{\text{Loc}}) \text{ type}$   
 $\hat{b}_2 = \begin{cases} \hat{b}_3 \sqcup \bigsqcup_{\hat{l}_{\text{proto}} \in \hat{L}_{\text{proto}}} \widehat{\text{CanPutHelp}}(\hat{H}, \hat{l}_{\text{proto}}, \hat{s}, \hat{l}_2) & \text{if } \text{false} \sqsubseteq (\hat{s} \in \text{dom}(\hat{H}(\hat{l}_1))) \\ \perp_{\text{Bool}} & \text{otherwise} \end{cases}$   
 $\hat{b}_3 = \begin{cases} \hat{H}(\hat{l}_2)(\text{@extensible}).1.2.1.3 & \text{if } \hat{H}(\hat{l}_1)(\text{@proto}).1.1.1.1.2 \not\sqsubseteq \perp_{\text{Null}} \\ \perp_{\text{Bool}} & \text{otherwise} \end{cases}$

CanPutVar :  $\widehat{\text{Heap}} \times \text{Prop} \rightarrow \widehat{\text{Bool}}$   
 $\widehat{\text{CanPutVar}}(\hat{H}, x) = \hat{b}_1 \sqcup \hat{b}_2$   
 where  $\hat{b}_1 = \begin{cases} \hat{H}(\#G\hat{\text{lobal}}_R)(x).1.1.2 & \text{if } \text{true} \sqsubseteq (x \in \text{dom}(\hat{H}(\#G\hat{\text{lobal}}))) \\ \perp_{\text{Bool}} & \text{otherwise} \end{cases}$   
 $\hat{b}_2 = \begin{cases} \widehat{\text{CanPut}}(\hat{H}, \#G\hat{\text{lobal}}_R, \hat{x}) & \text{if } \text{false} \sqsubseteq (x \in \text{dom}(\hat{H}(\#G\hat{\text{lobal}}))) \\ \perp_{\text{Bool}} & \text{otherwise} \end{cases}$

*Temporaries and pure local variables are always mutable in non-strict mode.*

*In strict-mode, “arguments” is immutable AND pure local, which invalidates current approach.*

CreateMutableBinding :  $\widehat{\text{Heap}} \times \text{Prop} \times \text{Value} \rightarrow \widehat{\text{Heap}}$   
 $\widehat{\text{CreateMutableBinding}}(\hat{H}, x, \hat{v}) = \hat{H}_1$  if  $\text{getVarKind}_P(x) = \text{PureLocalVar}$   
 where  $\hat{H}_1 = \hat{H}[\#P\hat{u}\hat{r}\hat{e}\hat{L}\hat{o}\hat{c}\hat{a}\hat{l}_R \mapsto \hat{H}(\#P\hat{u}\hat{r}\hat{e}\hat{L}\hat{o}\hat{c}\hat{a}\hat{l}_R)[x \mapsto \langle \hat{v}, \perp_{\text{Bool}}, \perp_{\text{Bool}}, \text{false} \rangle]]$   
 $\widehat{\text{CreateMutableBinding}}(\hat{H}, x, \hat{v}) = \hat{H}_1$  if  $\text{getVarKind}_P(x) = \text{CapturedVar}$   
 where  $\hat{H}_1 = \bigsqcup_{\hat{l} \in \hat{H}(\#P\hat{u}\hat{r}\hat{e}\hat{L}\hat{o}\hat{c}\hat{a}\hat{l}_R)(\text{@env}).1.2.2} \hat{H}[\hat{l} \mapsto \hat{H}(\hat{l})[x \mapsto \langle \hat{v}, \text{true}, \perp_{\text{Bool}}, \text{false} \rangle]]$   
 $\widehat{\text{CreateMutableBinding}}(\hat{H}, x, \hat{v}) = \hat{H}_1$  if  $\text{getVarKind}_P(x) = \text{CapturedCatchVar}$   
 where  $\hat{H}_1 = \hat{H}[\#C\hat{o}\hat{l}\hat{l}\hat{a}\hat{p}\hat{s}\hat{e}\hat{d}_O \mapsto \hat{H}(\#C\hat{o}\hat{l}\hat{l}\hat{a}\hat{p}\hat{s}\hat{e}\hat{d}_O)[x \mapsto \langle \hat{v}, \perp_{\text{Bool}}, \perp_{\text{Bool}}, \text{false} \rangle]]$   
 $\widehat{\text{CreateMutableBinding}}(\hat{H}, x, \hat{v}) = \hat{H}_1$  if  $\text{getVarKind}_P(x) = \text{GlobalVar}$   
 where  $\hat{H}_1 = \hat{H}[\#G\hat{\text{lobal}}_R \mapsto \hat{H}(\#G\hat{\text{lobal}}_R)[x \mapsto \langle \hat{v}, \text{true}, \text{true}, \text{false} \rangle]]$

$\hat{H}(\hat{l})(\hat{s}).1.1.4$  means the configurable attribute of the property.

Delete

$: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \rightarrow \widehat{\text{Heap}} \times \widehat{\text{Bool}}$

$\widehat{\text{Delete}}(\hat{H}, \hat{l}, \hat{s}) = (\hat{H}_1 \sqcup \hat{H}_2, \hat{b}_1 \sqcup \hat{b}_2)$

$$\text{where } (\hat{H}_1, \hat{b}_1) = \begin{cases} (\hat{H}, \text{false}) & \text{if } \text{true} \sqsubseteq \widehat{\text{HasOwnProperty}}(\hat{H}, \hat{l}, \hat{s}) \wedge \text{false} \sqsubseteq \hat{H}(\hat{l})(\hat{s}).1.1.4 \\ \perp_{\widehat{\text{Heap}} \times \widehat{\text{Bool}}} & \text{otherwise} \end{cases}$$

$$(\hat{H}_2, \hat{b}_2) = \begin{cases} (\hat{H}[\hat{l} \mapsto \hat{H}(\hat{l}) - \hat{s}], \text{true}) & \text{if } \begin{pmatrix} \text{true} \sqsubseteq \widehat{\text{HasOwnProperty}}(\hat{H}, \hat{l}, \hat{s}) \\ \wedge \text{true} \sqsubseteq \hat{H}(\hat{l})(\hat{s}).1.1.4 \end{pmatrix} \\ \perp_{\widehat{\text{Heap}} \times \widehat{\text{Bool}}} & \text{otherwise} \end{cases}$$

$$\text{if } \begin{pmatrix} \text{true} \sqsubseteq \widehat{\text{HasOwnProperty}}(\hat{H}, \hat{l}, \hat{s}) \\ \wedge \text{true} \sqsubseteq \hat{H}(\hat{l})(\hat{s}).1.1.4 \end{pmatrix} \vee (\text{false} \sqsubseteq \widehat{\text{HasOwnProperty}}(\hat{H}, \hat{l}, \hat{s}))$$

DeleteAll

$: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \rightarrow \widehat{\text{Heap}}$

$\widehat{\text{DeleteAll}}(\hat{H}, \hat{l}, \hat{s}) = \hat{H}_1$

where  $\hat{H}_2 = \widehat{\text{Delete}}(\hat{H}, \hat{l}, \hat{s}).1$

$$\hat{H}_1 = \begin{cases} \widehat{\text{DeleteAll}}(\hat{H}_2, \hat{l}_1, \hat{s}) & \text{if } \hat{H}(\hat{l})(\text{@proto}).1.1.1.1.2 \sqsubseteq \perp_{\text{Null}} \\ & \wedge \hat{H}(\hat{l})(\text{@proto}).1.1.1.2 = \{\hat{l}_1\} \\ \hat{H}_2 & \text{otherwise} \end{cases}$$

RaiseException

$: \widehat{\text{Heap}} \times \widehat{\text{Context}} \times \wp(\widehat{\text{Exception}}) \rightarrow \widehat{\text{Heap}} \times \widehat{\text{Context}}$

$\widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s) = (\hat{H}_1, \hat{C}_1)$

where  $\hat{v}_{old} = \hat{H}(\# \text{PureLocal}_R)(\text{@exception\_all}).1.2$

$\hat{v}_e = \langle \perp_{P\text{Value}}, \bigsqcup_{e\hat{x}c \in \hat{e}s} \widehat{\text{NewExceptionLoc}}(e\hat{x}c) \rangle$

$$\hat{H}_e = \hat{H} \left[ \# \text{PureLocal}_R \mapsto \hat{H}(\# \text{PureLocal}_R) \left[ \begin{array}{l} \text{@exception} \mapsto \hat{v}_e, \\ \text{@exception\_all} \mapsto \hat{v}_e \sqcup \hat{v}_{old} \end{array} \right] \right]$$

$$(\hat{H}_1, \hat{C}_1) = \begin{cases} (\hat{H}_e, \hat{C}) & \text{if } \hat{e}s \neq \{\} \\ (\perp_{\widehat{\text{Heap}}}, \perp_{\widehat{\text{Context}}}) & \text{otherwise} \end{cases}$$

NewExceptionLoc

$: \widehat{\text{Exception}} \rightarrow \widehat{\text{Loc}}$

$$\widehat{\text{NewExceptionLoc}}(\hat{H}, e\hat{x}c) = \begin{cases} \# \hat{E}rr_O & \text{if } e\hat{x}c = \hat{E}rror \\ \# \hat{E}valErr_O & \text{if } e\hat{x}c = \hat{E}val\hat{E}rror \\ \# \hat{R}angeErr_O & \text{if } e\hat{x}c = \hat{R}ange\hat{E}rror \\ \# \hat{R}efErr_O & \text{if } e\hat{x}c = \hat{R}eference\hat{E}rror \\ \# \hat{S}yntaxErr_O & \text{if } e\hat{x}c = \hat{S}yntax\hat{E}rror \\ \# \hat{T}ypeErr_O & \text{if } e\hat{x}c = \hat{T}ype\hat{E}rror \\ \# \hat{U}RIErr_O & \text{if } e\hat{x}c = \hat{U}RI\hat{E}rror \end{cases}$$

$$\begin{aligned}
\widehat{\text{getRel}} &: \widehat{\text{RelExpr}} \rightarrow \widehat{\text{State}} \rightarrow \wp(\widehat{\text{RelExpr}}) \\
\widehat{\text{getRel}}(pe \S e, \hat{S}) &= \{pe \S e\} \\
\widehat{\text{getRel}}((e_1 + e_2) \S e_3, \hat{S}) &= \widehat{\text{getRel}}(e_1 \S (e_3 - e_2), \hat{S}) \cup \widehat{\text{getRel}}(e_2 \S (e_3 - e_1), \hat{S}) \quad \text{if } \widehat{\text{validity}}_3(e_1, e_2, e_3, \hat{S}) \\
\widehat{\text{getRel}}((e_1 - e_2) \S e_3, \hat{S}) &= \widehat{\text{getRel}}(e_1 \S (e_3 + e_2), \hat{S}) \cup \widehat{\text{getRel}}(e_2 \S^t (e_1 - e_3), \hat{S}) \quad \text{if } \widehat{\text{validity}}_3(e_1, e_2, e_3, \hat{S}) \\
\widehat{\text{getRel}}((n * e_1) \S e_2, \hat{S}) &= \widehat{\text{getRel}}((e_1 * n) \S e_2, \hat{S}) \quad \text{if } \widehat{\text{validity}}_2(e_1, e_2, \hat{S}) \\
\widehat{\text{getRel}}((e_1 * n) \S e_2, \hat{S}) &= \widehat{\text{getRel}}(e_1 \S (e_2 / n), \hat{S}) \quad \text{if } n > 0 \wedge \widehat{\text{validity}}_2(e_1, e_2, \hat{S}) \\
\widehat{\text{getRel}}((e_1 * n) \S e_2, \hat{S}) &= \widehat{\text{getRel}}(e_1 \S^t (e_2 / n), \hat{S}) \quad \text{if } n < 0 \wedge \widehat{\text{validity}}_2(e_1, e_2, \hat{S}) \\
\widehat{\text{getRel}}((e_1 / n) \S e_2, \hat{S}) &= \widehat{\text{getRel}}(e_1 \S (e_2 * n), \hat{S}) \quad \text{if } n > 0 \wedge \widehat{\text{validity}}_2(e_1, e_2, \hat{S}) \\
\widehat{\text{getRel}}((e_1 / n) \S e_2, \hat{S}) &= \widehat{\text{getRel}}(e_1 \S^t (e_2 * n), \hat{S}) \quad \text{if } n < 0 \wedge \widehat{\text{validity}}_2(e_1, e_2, \hat{S}) \\
\widehat{\text{getRel}}(re) &= \emptyset \quad \text{otherwise}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{getThis}} &: \widehat{\text{Heap}} \times \widehat{\text{Value}} \rightarrow \wp(\widehat{\text{Loc}}) \\
\widehat{\text{getThis}}(\hat{H}, \hat{v}) &= \hat{L}_1 \cup \hat{L}_2 \cup \hat{L}_3 \\
\text{where } \hat{L}_1 &= \begin{cases} \{\#Global_R\} & \text{if } \text{undefined} \sqsubseteq \hat{v}.1.1 \vee \text{null} \sqsubseteq \hat{v}.1.2 \\ \{\} & \text{otherwise} \end{cases} \\
\hat{L}_2 &= \begin{cases} \{\#Global_R\} & \text{if } \exists \hat{l} \in \hat{v}.2 : \text{false} \sqsubseteq \widehat{\text{IsObject}}(\hat{h}, \hat{l}) \\ \{\} & \text{otherwise} \end{cases} \\
\hat{L}_3 &= \{\hat{l} \in \hat{v}.2 \mid \text{true} \sqsubseteq \widehat{\text{IsObject}}(\hat{h}, \hat{l})\}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{HasConstruct}} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \rightarrow \widehat{\text{Bool}} \\
\widehat{\text{HasConstruct}}(\hat{H}, \hat{l}) &= \hat{b}_1 \sqcup \hat{b}_2 \\
\text{where } \hat{b}_1 &= \begin{cases} \text{true} & \text{if } \text{true} \sqsubseteq (@\text{construct} \in \text{dom}(\hat{H}(\hat{l}))) \\ \perp_{\text{Bool}} & \text{otherwise} \end{cases} \\
\hat{b}_2 &= \begin{cases} \text{false} & \text{if } \text{false} \sqsubseteq (@\text{construct} \in \text{dom}(\hat{H}(\hat{l}))) \\ \perp_{\text{Bool}} & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{HasInstance}} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \rightarrow \widehat{\text{Bool}} \\
\widehat{\text{HasConstruct}}(\hat{H}, \hat{l}) &= \hat{b}_1 \sqcup \hat{b}_2 \\
\text{where } \hat{b}_1 &= \begin{cases} \text{true} & \text{if } \text{true} \sqsubseteq (@\text{hasinstance} \in \text{dom}(\hat{H}(\hat{l}))) \\ \perp_{\text{Bool}} & \text{otherwise} \end{cases} \\
\hat{b}_2 &= \begin{cases} \text{false} & \text{if } \text{false} \sqsubseteq (@\text{hasinstance} \in \text{dom}(\hat{H}(\hat{l}))) \\ \perp_{\text{Bool}} & \text{otherwise} \end{cases}
\end{aligned}$$

*Cycle in prototype chain is detected at implementation level.*

$$\begin{aligned}
\widehat{\text{HasProperty}} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \rightarrow \widehat{\text{Bool}} \\
\widehat{\text{HasProperty}}(\hat{H}, \hat{l}, \hat{s}) &= \hat{b}_1 \sqcup \hat{b}_2 \\
\text{where } \hat{b}_1 &= \begin{cases} \text{true} & \text{if } \text{true} \sqsubseteq \widehat{\text{HasOwnProperty}}(\hat{H}, \hat{l}, \hat{s}) \\ \perp_{\text{Bool}} & \text{otherwise} \end{cases} \\
\hat{L}_{\text{proto}} &= \hat{H}(\hat{l})(@\text{proto}).1.1.1.2 \\
\hat{b}_2 &= \begin{cases} \hat{b}_3 \sqcup \bigsqcup_{\hat{l}_{\text{proto}} \in \hat{L}_{\text{proto}}} \widehat{\text{HasProperty}}(\hat{H}, \hat{l}_{\text{proto}}, \hat{s}) & \text{if } \text{false} \sqsubseteq \widehat{\text{HasOwnProperty}}(\hat{H}, \hat{l}, \hat{s}) \\ \perp_{\text{Bool}} & \text{otherwise} \end{cases} \\
\hat{b}_3 &= \begin{cases} \text{false} & \text{if } \hat{H}(\hat{l}_1)(@\text{proto}).1.1.1.1.2 \not\sqsubseteq \perp_{\text{Null}} \\ \perp_{\text{Bool}} & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{HasOwnProperty}} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \rightarrow \widehat{\text{Bool}} \\
\widehat{\text{HasOwnProperty}}(\hat{H}, \hat{l}, \hat{s}) &= (\hat{s} \in \text{dom}(\hat{h}(\hat{l})))
\end{aligned}$$

*Cycle in prototype chain is detected at implementation level.*

$$\begin{aligned}
\underline{\widehat{\text{inherit}}} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{Loc}} \rightarrow \widehat{\text{Value}} \\
\underline{\widehat{\text{inherit}}}(\hat{H}, \hat{l}_1, \hat{l}_2) &= \begin{cases} \text{true} & \text{if } \hat{l}_1 \doteq \hat{l}_2 \\ \hat{v}_1 \sqcup \bigsqcup_{\hat{l} \in \hat{H}(\hat{l}_1)(@proto).1.1.1.2} \underline{\widehat{\text{inherit}}}(\hat{H}, \hat{l}, \hat{l}_2) & \text{if } \hat{l}_1 \not\doteq \hat{l}_2 \end{cases} \\
\text{where } \hat{v}_1 &= \begin{cases} \text{false} & \text{if } \hat{H}(\hat{l}_1)(@proto).1.1.1.1.2 \not\sqsubseteq \perp_{Null} \\ \perp_{Value} & \text{otherwise} \end{cases} \\
\\
\underline{\widehat{\text{inheritProto}}_1} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{Loc}} \times \widehat{\text{Bool}} \rightarrow \wp(\widehat{\text{Loc}}) \\
\underline{\widehat{\text{inheritProto}}_1}(\hat{H}, \hat{l}_1, \hat{l}_2, \hat{b}) &= \hat{L} \\
\text{where } \hat{L} &= \begin{cases} \{\hat{l}_1\} & \text{if } \hat{b} \sqsubseteq \underline{\widehat{\text{inherit}}}(\hat{H}, \hat{l}_1, \hat{l}_2) \\ \{\} & \text{otherwise} \end{cases} \\
\\
\underline{\widehat{\text{inheritProto}}_2} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{Loc}} \times \widehat{\text{Bool}} \rightarrow \wp(\widehat{\text{Loc}}) \\
\underline{\widehat{\text{inheritProto}}_2}(\hat{H}, \hat{l}_1, \hat{l}_2, \hat{b}) &= \hat{L} \\
\text{where } \hat{L} &= \begin{cases} \{\hat{l}_2\} & \text{if } \hat{b} \sqsubseteq \underline{\widehat{\text{inherit}}}(\hat{H}, \hat{l}_1, \hat{l}_2) \\ \{\} & \text{otherwise} \end{cases} \\
\\
\underline{\widehat{\text{isArray}}} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \rightarrow \widehat{\text{Bool}} \\
\underline{\widehat{\text{isArray}}}(\hat{H}, \hat{l}) &= \hat{b}_1 \sqcup \hat{b}_2 \\
\text{where } \hat{b}_1 &= \begin{cases} \text{true} & \text{if } \text{"Array"} \sqsubseteq \hat{H}(\hat{l})(@class).1.2 \\ \perp_{Bool} & \text{otherwise} \end{cases} \\
\hat{b}_2 &= \begin{cases} \text{false} & \text{if } \text{"Array"} \neq \hat{H}(\hat{l})(@class).1.2 \\ \perp_{Bool} & \text{otherwise} \end{cases} \\
\\
\underline{\widehat{\text{isArrayIndex}}} &: \widehat{\text{String}} \rightarrow \widehat{\text{Bool}} \\
\underline{\widehat{\text{isArrayIndex}}}(\hat{s}) &= \begin{cases} \top_{Bool} & \text{if } \hat{s} = \top_{String} \\ \top_{Bool} & \text{if } \hat{s} = \text{NumStr} \\ \text{false} & \text{if } \hat{s} = \text{OtherStr} \\ \text{true} & \text{if } \hat{s} = \text{NumStrSingle}(s) \wedge 0 \leq \text{ToNumber}(s) < 2^{32} - 1 \\ \top_{Bool} & \text{if } \hat{s} = \text{NumStrSingle}(s) \wedge (\text{ToNumber}(s) < 0 \vee 2^{32} - 1 \leq \text{ToNumber}(s)) \\ \text{false} & \text{if } \hat{s} = \text{OtherStrSingle} \\ \perp_{Bool} & \text{if } \hat{s} = \perp_{String} \end{cases} \\
\\
\underline{\widehat{\text{isCallable}}} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \rightarrow \widehat{\text{Bool}} \\
\underline{\widehat{\text{isCallable}}}(\hat{H}, \hat{l}) &= \hat{b}_1 \sqcup \hat{b}_2 \\
\text{where } \hat{b}_1 &= \begin{cases} \text{true} & \text{if } \text{true} \sqsubseteq (@function \in \text{dom}(\hat{H}(\hat{l}))) \\ \perp_{Bool} & \text{otherwise} \end{cases} \\
\hat{b}_2 &= \begin{cases} \text{false} & \text{if } \text{false} \sqsubseteq (@function \in \text{dom}(\hat{H}(\hat{l}))) \\ \perp_{Bool} & \text{otherwise} \end{cases} \\
\\
\underline{\widehat{\text{isObject}}} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \rightarrow \widehat{\text{Bool}} \\
\underline{\widehat{\text{isObject}}}(\hat{H}, \hat{l}) &= @class \in \text{dom}(\hat{h}(\hat{l}))
\end{aligned}$$

$$\begin{aligned}
\widehat{K} &: \text{IRRelOP} \rightarrow \widehat{\text{Value}} \rightarrow \widehat{\text{Value}} \times \widehat{\text{Absent}} \\
\widehat{K}_{!=} \hat{v}_1 &= (\top_{\text{Value}}, \widehat{\text{absent}}) \\
\widehat{K}_{==} \hat{v}_1 &= (\hat{v}_1, \hat{abs}) \\
\text{where } \hat{abs} &= \begin{cases} \widehat{\text{absent}} & \text{if } \widehat{\text{undefined}} \sqsubseteq \hat{v}_1.1.1 \\ \perp_{\text{Absent}} & \text{otherwise} \end{cases} \\
\widehat{K}_{!=} \hat{v}_1 &= (\top_{\text{Value}}, \widehat{\text{absent}}) \\
\widehat{K}_{==} \hat{v}_1 &= (\langle \langle \hat{v}_1.1.1 \sqcup \hat{pv}_1, \hat{v}_1.1.2 \sqcup \hat{pv}_2, \hat{v}_1.1.3 \sqcup \hat{pv}_3, \hat{v}_1.1.4 \sqcup \hat{pv}_4, \top_{\text{String}} \rangle, \top_{\widehat{\text{Loc}}} \rangle, \hat{abs}) \\
\text{where } \hat{abs} &= \begin{cases} \widehat{\text{absent}} & \text{if } \widehat{\text{undefined}} \sqsubseteq \hat{v}_1.1.1 \vee \widehat{\text{null}} \sqsubseteq \hat{v}_1.1.2 \\ \perp_{\text{Absent}} & \text{otherwise} \end{cases} \\
n_1 &= \begin{cases} \hat{1} & \text{if } \widehat{\text{true}} \sqsubseteq \hat{v}_1.1.3 \\ \perp_{\text{Number}} & \text{otherwise} \end{cases} \\
n_2 &= \begin{cases} \hat{0} & \text{if } \widehat{\text{false}} \sqsubseteq \hat{v}_1.1.3 \\ \perp_{\text{Number}} & \text{otherwise} \end{cases} \\
n_3 &= \widehat{\text{Str2Num}}((\hat{v}_1.1.5)_{P\widehat{\text{Value}}}) \\
n_4 &= \begin{cases} \perp_{\text{Number}} & \text{if } \hat{v}_1.1.4 \sqsubseteq \widehat{\text{NaN}} \\ \hat{v}_1.1.4 & \text{otherwise} \end{cases} \\
\hat{pv}_1 &= \begin{cases} \widehat{\text{undefined}} & \text{if } \widehat{\text{null}} \sqsubseteq \hat{v}_1.1.2 \\ \perp_{\text{Undef}} & \text{otherwise} \end{cases} \\
\hat{pv}_2 &= \begin{cases} \widehat{\text{null}} & \text{if } \widehat{\text{undefined}} \sqsubseteq \hat{v}_1.1.1 \\ \perp_{\text{Null}} & \text{otherwise} \end{cases} \\
\hat{pv}_3 &= \begin{cases} \top_{\text{Bool}} & \text{if } \widehat{\text{UINT}} \sqsubseteq \hat{v}_1.1.4 \vee \hat{v}_1.2 \neq \emptyset \\ \widehat{\text{true}} & \text{if } \hat{v}_1.2 = \emptyset \wedge (\hat{1} \sqsubseteq \hat{v}_1.1.4 \vee \hat{1} \sqsubseteq \widehat{\text{Str2Num}}((\hat{v}_1.1.5)_{P\widehat{\text{Value}}})) \\ \widehat{\text{false}} & \text{if } \hat{v}_1.2 = \emptyset \wedge (\hat{0} \sqsubseteq \hat{v}_1.1.4 \vee \hat{0} \sqsubseteq \widehat{\text{Str2Num}}((\hat{v}_1.1.5)_{P\widehat{\text{Value}}})) \\ \perp_{\text{Bool}} & \text{otherwise} \end{cases} \\
\hat{pv}_4 &= \begin{cases} n_1 \sqcup n_2 \sqcup n_3 \sqcup n_4 & \text{if } \hat{v}_1.2 = \emptyset \\ \top_{\text{Number}} & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{Lookup}} &: \widehat{\text{Heap}} \times \text{Prop} \rightarrow \widehat{\text{Value}} \times \wp(\widehat{\text{Exception}}) \\
\widehat{\text{Lookup}}(\hat{H}, x) &= (\hat{H}(\# \text{PureLocal}_R)(x).1.1.1, \{\}) \quad \text{if } \text{getVarKind}_P(x) = \text{PureLocalVar} \\
\widehat{\text{Lookup}}(\hat{H}, x) &= (\bigsqcup_{i \in \hat{H}(\# \text{PureLocal}_R)(@env).1.2.2} \widehat{\text{LookupL}}(\hat{H}, \hat{l}, x), \{\}) \quad \text{if } \text{getVarKind}_P(x) = \text{CapturedVar} \\
\widehat{\text{Lookup}}(\hat{H}, x) &= (\hat{H}(\# \text{Collapsed}_O)(x).1.1.1, \{\}) \quad \text{if } \text{getVarKind}_P(x) = \text{CapturedCatchVar} \\
\widehat{\text{Lookup}}(\hat{H}, x) &= \widehat{\text{LookupG}}(\hat{H}, x) \quad \text{if } \text{getVarKind}_P(x) = \text{GlobalVar}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{LookupG}} &: \widehat{\text{Heap}} \times \text{Prop} \rightarrow \widehat{\text{Value}} \times \wp(\widehat{\text{Exception}}) \\
\widehat{\text{LookupG}}(\hat{H}, x) &= (\hat{v}_1 \sqcup \hat{v}_2, \hat{e}s) \\
\text{where } \hat{v}_1 &= \begin{cases} \hat{H}(\# \text{Global}_R)(x).1.1.1 & \text{if } \text{true} \sqsubseteq (x \in \text{dom}(\hat{H}(\# \text{Global}))) \\ \perp_{\text{Value}} & \text{otherwise} \end{cases} \\
(\hat{v}_2, \hat{e}s) &= \begin{cases} (\hat{v}_3, \hat{e}\hat{x}c) & \text{if } \text{false} \sqsubseteq (x \in \text{dom}(\hat{H}(\# \text{Global}))) \\ (\perp_{\text{Value}}, \{\}) & \text{otherwise} \end{cases} \\
\hat{L}_{\text{proto}} &= \hat{H}(\# \text{Global}_R)(@proto).1.1.1.2 \\
\hat{v}_3 &= \bigsqcup_{i_{\text{proto}} \in \hat{L}_{\text{proto}}} \begin{cases} \widehat{\text{Proto}}(\hat{H}, \hat{l}_{\text{proto}}, \hat{x}) & \text{if } \text{true} \sqsubseteq \widehat{\text{HasProperty}}(\hat{H}, \hat{l}_{\text{proto}}, x) \\ \perp_{\text{Value}} & \text{otherwise} \end{cases} \\
\hat{e}\hat{x}c &= \bigsqcup_{i_{\text{proto}} \in \hat{L}_{\text{proto}}} \begin{cases} \{\text{ReferenceError}\} & \text{if } \text{false} \sqsubseteq \widehat{\text{HasProperty}}(\hat{H}, \hat{l}_{\text{proto}}, x) \\ \perp_{\text{Exception}} & \text{otherwise} \end{cases}
\end{aligned}$$

*Cycle in scope chain is detected at implementation level.*

$$\begin{aligned}
\widehat{\text{LookupL}} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \text{Prop} \rightarrow \widehat{\text{Value}} \\
\widehat{\text{LookupL}}(\hat{H}, \hat{l}, x) &= \hat{v}_1 \sqcup \hat{v}_2 \\
\text{where } \hat{v}_1 &= \begin{cases} \hat{H}(\hat{l})(x).1.1.1 & \text{if } \text{true} \sqsubseteq (x \in \text{dom}(\hat{H}(\hat{l}))) \\ \perp_{\text{Value}} & \text{otherwise} \end{cases} \\
\hat{L}_{\text{outer}} &= \hat{H}(\hat{l})(@outer).1.2.2 \\
\hat{v}_2 &= \begin{cases} \bigsqcup_{i_{\text{outer}} \in \hat{L}_{\text{outer}}} \widehat{\text{LookupL}}(\hat{H}, \hat{l}_{\text{outer}}, x) & \text{if } \text{false} \sqsubseteq (x \in \text{dom}(\hat{H}(\hat{l}))) \\ \perp_{\text{Value}} & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{LookupBase}} &: \widehat{\text{Heap}} \times \text{Prop} \rightarrow \wp(\widehat{\text{Loc}}) \\
\widehat{\text{LookupBase}}(\hat{H}, x) &= \{\# \text{PureLocal}_R\} \quad \text{if } \text{getVarKind}_P(x) = \text{PureLocalVar} \\
\widehat{\text{LookupBase}}(\hat{H}, x) &= \bigcup_{i \in \hat{H}(\# \text{PureLocal}_R)(@env).1.2.2} \widehat{\text{LookupBaseL}}(\hat{H}, \hat{l}, x) \quad \text{if } \text{getVarKind}_P(x) = \text{CapturedVar} \\
\widehat{\text{LookupBase}}(\hat{H}, x) &= \{\# \text{Collapsed}_O\} \quad \text{if } \text{getVarKind}_P(x) = \text{CapturedCatchVar} \\
\widehat{\text{LookupBase}}(\hat{H}, x) &= \widehat{\text{LookupBaseG}}(\hat{H}, x) \quad \text{if } \text{getVarKind}_P(x) = \text{GlobalVar}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{LookupBaseG}} &: \widehat{\text{Heap}} \times \text{Prop} \rightarrow \wp(\widehat{\text{Loc}}) \\
\widehat{\text{LookupBaseG}}(\hat{H}, x) &= \hat{L}_1 \cup \hat{L}_2 \\
\text{where } \hat{L}_1 &= \begin{cases} \{\# \text{Global}_R\} & \text{if } \text{true} \sqsubseteq (x \in \text{dom}(\hat{H}(\# \text{Global}_R))) \\ \{\} & \text{otherwise} \end{cases} \\
\hat{L}_2 &= \begin{cases} \hat{L}_3 & \text{if } \text{false} \sqsubseteq (x \in \text{dom}(\hat{H}(\# \text{Global}_R))) \\ \{\} & \text{otherwise} \end{cases} \\
\hat{L}_{\text{proto}} &= \hat{H}(\# \text{Global}_R)(@proto).1.1.1.2 \\
\hat{L}_3 &= \bigsqcup_{i_{\text{proto}} \in \hat{L}_{\text{proto}}} \widehat{\text{ProtoBase}}(\hat{H}, \hat{l}_{\text{proto}}, \hat{x})
\end{aligned}$$

*Cycle in scope chain is detected at implementation level.*

$$\begin{aligned}
\widehat{\text{LookupBaseL}} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \text{Prop} \rightarrow \wp(\widehat{\text{Loc}}) \\
\widehat{\text{LookupBaseL}}(\hat{H}, \hat{l}, x) &= \hat{L}_1 \cup \hat{L}_2 \\
\text{where } \hat{L}_1 &= \begin{cases} \{\hat{l}\} & \text{if } \text{true} \sqsubseteq (x \in \text{dom}(\hat{H}(\hat{l}))) \\ \{\} & \text{otherwise} \end{cases} \\
\hat{L}_{\text{outer}} &= \hat{H}(\hat{l})(@outer).1.2.2 \\
\hat{L}_2 &= \begin{cases} \bigcup_{i_{\text{outer}} \in \hat{L}_{\text{outer}}} \widehat{\text{LookupBaseL}}(\hat{H}, \hat{l}_{\text{outer}}, x) & \text{if } \text{false} \sqsubseteq (x \in \text{dom}(\hat{H}(\hat{l}))) \\ \{\} & \text{otherwise} \end{cases}
\end{aligned}$$



$$\begin{aligned} \widehat{\text{NewBoolean}} &: \widehat{\text{Value}} \rightarrow \widehat{\text{Obj}} \\ \widehat{\text{NewBoolean}}(\hat{v}) &= \left\{ \begin{array}{l} @class \mapsto \text{"Boolean"}_{\text{Value}}, \\ @proto \mapsto \langle \langle \perp_{P\text{Value}}, \{\# \text{BoolProto}_R\} \rangle, \text{false}, \text{false}, \text{false} \rangle, \\ @extensible \mapsto \text{true}_{\text{Value}}, \\ @primitive \mapsto \hat{v} \end{array} \right\} \end{aligned}$$

$$\begin{aligned} \widehat{\text{NewNumber}} &: \widehat{\text{Value}} \rightarrow \widehat{\text{Obj}} \\ \widehat{\text{NewNumber}}(\hat{v}) &= \left\{ \begin{array}{l} @class \mapsto \text{"Number"}_{\text{Value}}, \\ @proto \mapsto \langle \langle \perp_{P\text{Value}}, \{\# \text{NumProto}_R\} \rangle, \text{false}, \text{false}, \text{false} \rangle, \\ @extensible \mapsto \text{true}_{\text{Value}}, \\ @primitive \mapsto \hat{v} \end{array} \right\} \end{aligned}$$

$$\begin{aligned} \widehat{\text{NewString}} &: \widehat{\text{Value}} \rightarrow \widehat{\text{Obj}} \\ \widehat{\text{NewString}}(\hat{v}) &= \hat{o}_1 \sqcup \hat{o}_2 \\ &\text{where } \hat{s} = \hat{v}.1.5 \wedge \hat{v}_{len} = \text{length}(\hat{s}) \\ \hat{o}_1 &= \left\{ \begin{array}{l} @class \mapsto \text{"String"}_{\text{Value}}, \\ @proto \mapsto \langle \langle \perp_{P\text{Value}}, \{\# \text{StrProto}_R\} \rangle, \text{false}, \text{false}, \text{false} \rangle, \\ @extensible \mapsto \text{true}_{\text{Value}}, \\ @primitive \mapsto \hat{v}, \\ \text{"length"} \mapsto \langle (\hat{v}_{len})_{\text{Value}}, \text{false}, \text{false}, \text{false} \rangle \end{array} \right\} \\ \hat{o}_2 &= \left\{ \begin{array}{l} \text{"i"} \mapsto \langle (\hat{v}_{char})_{\text{Value}}, \text{false}, \text{true}, \text{false} \rangle \end{array} \middle| \begin{array}{l} 0 \leq i \\ \wedge \exists l \in \gamma(\hat{v}_{len}). i < l \\ \wedge \hat{v}_{char} = \text{charAt}(\hat{s}, i) \end{array} \right\} \end{aligned}$$

$$\begin{aligned} \widehat{\text{NewDeclEnvRecord}} &: \widehat{\text{Value}} \rightarrow \widehat{\text{Obj}} \\ &\text{outer is either location set or null value} \\ \widehat{\text{NewDeclEnvRecord}}(\hat{v}) &= \{ @outer \mapsto \hat{v} \} \end{aligned}$$

$$\begin{aligned} \widehat{\text{NewObject}} &: \widehat{\text{Loc}} \rightarrow \widehat{\text{Obj}} \\ \widehat{\text{NewObject}}(\hat{l}) &= \left\{ \begin{array}{l} @class \mapsto \text{"Object"}_{\text{Value}}, \\ @proto \mapsto \langle \langle \perp_{P\text{Value}}, \{\hat{l}\} \rangle, \text{false}, \text{false}, \text{false} \rangle, \\ @extensible \mapsto \text{true}_{\text{Value}} \end{array} \right\} \end{aligned}$$

$$\begin{aligned} \widehat{\text{NewArgObject}} &: \widehat{\text{Number}} \rightarrow \widehat{\text{Obj}} \\ \widehat{\text{NewArgObject}}(\hat{n}) &= \left\{ \begin{array}{l} @class \mapsto \text{"Arguments"}_{\text{Value}}, \\ @proto \mapsto \langle \langle \perp_{P\text{Value}}, \{\# \text{ObjProto}_R\} \rangle, \text{false}, \text{false}, \text{false} \rangle, \\ \text{"length"} \mapsto \langle \hat{n}_{\text{Value}}, \text{true}, \text{false}, \text{true} \rangle, \\ @extensible \mapsto \text{true}_{\text{Value}} \end{array} \right\} \end{aligned}$$

$$\begin{aligned} \widehat{\text{NewArrayObject}} &: \widehat{\text{Number}} \rightarrow \widehat{\text{Obj}} \\ \widehat{\text{NewArrayObject}}(\hat{n}) &= \left\{ \begin{array}{l} @class \mapsto \text{"Array"}_{\text{Value}}, \\ @proto \mapsto \langle \langle \perp_{P\text{Value}}, \{\# \text{ArrayProto}_R\} \rangle, \text{false}, \text{false}, \text{false} \rangle, \\ \text{"length"} \mapsto \langle \hat{n}_{\text{Value}}, \text{true}, \text{false}, \text{false} \rangle, \\ @extensible \mapsto \text{true}_{\text{Value}} \end{array} \right\} \end{aligned}$$

$$\begin{aligned} \widehat{\text{NewFunctionObject}} &: \widehat{\text{FunctionId}} \times \widehat{\text{Value}} \times \widehat{\text{Loc}} \times \widehat{\text{Number}} \rightarrow \widehat{\text{Obj}} \\ &\text{scope is either location set or null value} \\ \widehat{\text{NewFunctionObject}}(\hat{fid}, \hat{v}, \hat{l}, \hat{n}) &= \left\{ \begin{array}{l} @class \mapsto \text{"Function"}_{\text{Value}}, \\ @proto \mapsto \langle \langle \perp_{P\text{Value}}, \{\# \text{FunctionProto}_R\} \rangle, \text{false}, \text{false}, \text{false} \rangle, \\ @extensible \mapsto \text{true}_{\text{Value}}, \\ @function \mapsto \{\hat{fid}\}, \\ @construct \mapsto \{\hat{fid}\}, \\ @hasinstance \mapsto \top_{\text{Null}}, \\ @scope \mapsto \hat{v}, \\ \text{"prototype"} \mapsto \langle \langle \perp_{P\text{Value}}, \{\hat{l}\} \rangle, \text{true}, \text{false}, \text{false} \rangle, \\ \text{"length"} \mapsto \langle \hat{n}_{\text{Value}}, \text{false}, \text{false}, \text{false} \rangle \end{array} \right\} \end{aligned}$$

$$\begin{aligned} \widehat{\text{NewPureLocal}} &: \widehat{\text{Value}} \times \wp(\widehat{\text{Loc}}) \rightarrow \widehat{\text{Obj}} \\ &\text{env is either location set or null value} \\ \widehat{\text{NewPureLocal}}(\hat{v}_{env}, \hat{L}_{this}) &= \left\{ \begin{array}{l} @env \mapsto \hat{v}_{env}, \\ @this \mapsto \hat{L}_{this}, \\ @exception \mapsto \perp_{\text{PropValue}}, \\ @exception\_all \mapsto \perp_{\text{PropValue}}, \\ @return \mapsto \text{undefined}_{\text{Value}} \end{array} \right\} \end{aligned}$$

$$\begin{aligned}
\widehat{\text{Oldify}} &: \widehat{\text{Heap}} \times \widehat{\text{Context}} \times \widehat{\text{Address}} \rightarrow \widehat{\text{Heap}} \times \widehat{\text{Context}} \\
\widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}) &= \begin{cases} (\hat{H}_1, \hat{C}_1) & \text{if } \hat{C} \neq \perp_{\text{Context}} \\ (\perp_{\text{Heap}}, \perp_{\text{Context}}) & \text{if } \hat{C} = \perp_{\text{Context}} \end{cases} \\
\text{where } \hat{l}_R &= (\hat{a}, \text{Recent}) \wedge \hat{l}_O = (\hat{a}, \text{Old}) \\
\wedge \hat{H}_1 &= \begin{cases} (\hat{H}[l_O \mapsto \hat{H}(\hat{l}_R)] - \hat{l}_R)\{\hat{l}_O/\hat{l}_R\} & \text{if } \hat{l}_R \in \text{dom}(\hat{H}) \\ \hat{H}\{\hat{l}_O/\hat{l}_R\} & \text{if } \hat{l}_R \notin \text{dom}(\hat{H}) \end{cases} \\
\wedge \hat{C}_1 &= \{\{\}, \{\}, \hat{C}.3 \cup \{\hat{a}\}, \hat{C}.4 \cup \{\hat{a}\}\}
\end{aligned}$$

*At function return, this method oldifies bypassed pure local object.*

$$\begin{aligned}
\widehat{\text{FixOldify}} &: \widehat{\text{Context}} \times \widehat{\text{Obj}} \times \wp(\widehat{\text{Address}}) \times \wp(\widehat{\text{Address}}) \rightarrow \widehat{\text{Context}} \times \widehat{\text{Obj}} \\
\widehat{\text{FixOldify}}(\hat{C}_0, \hat{o}_0, \hat{A}_{\text{may}}, \hat{A}_{\text{must}}) &= \begin{cases} (\hat{C}_n, \hat{o}_n) & \text{if } \hat{C} \neq \perp_{\text{Context}} \\ (\perp_{\text{Context}}, \perp_{\text{Obj}}) & \text{if } \hat{C} = \perp_{\text{Context}} \end{cases} \\
\text{where } \hat{a}_1 \cdots \hat{a}_n &= \hat{A}_{\text{may}} \wedge \\
\forall 1 \leq i \leq n. & \\
\hat{l}_{R_i} &= (\hat{a}_i, \text{Recent}) \wedge \hat{l}_{O_i} = (\hat{a}_i, \text{Old}) \wedge \\
\hat{C}_i &= \begin{cases} \langle \{\}, \{\}, \hat{C}_{i-1}.3 \cup \{\hat{a}_i\}, \hat{C}_{i-1}.4 \cup \{\hat{a}_i\} \rangle & \text{if } a_i \in \hat{A}_{\text{must}} \\ \langle \{\}, \{\}, \hat{C}_{i-1}.3 \cup \{\hat{a}_i\}, \hat{C}_{i-1}.4 \rangle & \text{if } a_i \notin \hat{A}_{\text{must}} \end{cases} \\
\hat{o}_i &= \begin{cases} \hat{o}_i = \hat{o}_{i-1}\{\hat{l}_{O_i}/\hat{l}_{R_i}\} & \text{if } a_i \in \hat{A}_{\text{must}} \\ \hat{o}_i = \hat{o}_{i-1}\{\{\hat{l}_{O_i}, \hat{l}_{R_i}\}/\hat{l}_{R_i}\} & \text{if } a_i \notin \hat{A}_{\text{must}} \end{cases}
\end{aligned}$$

*Cycle in prototype chain is detected at implementation level.*

$$\begin{aligned}
\widehat{\text{Proto}} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \rightarrow \widehat{\text{Value}} \\
\widehat{\text{Proto}}(\hat{H}, \hat{l}, \hat{s}) &= \hat{v}_1 \sqcup \hat{v}_2 \\
\text{where } \hat{v}_1 &= \begin{cases} \hat{H}(\hat{l})(\hat{s}).1.1.1 & \text{true} \sqsubseteq (\hat{s} \in \text{dom}(\hat{H}(\hat{l}))) \\ \perp_{\text{Value}} & \text{otherwise} \end{cases} \\
\hat{L}_{\text{proto}} &= \hat{H}(\hat{l})(\text{@proto}).1.1.1.2 \\
\hat{v}_2 &= \begin{cases} \hat{v}_3 \sqcup \bigsqcup_{\hat{l}_{\text{proto}} \in \hat{L}_{\text{proto}}} \widehat{\text{Proto}}(\hat{H}, \hat{l}_{\text{proto}}, \hat{s}) & \text{false} \sqsubseteq (\hat{s} \in \text{dom}(\hat{H}(\hat{l}))) \\ \perp_{\text{Value}} & \text{otherwise} \end{cases} \\
\hat{v}_3 &= \begin{cases} \text{undefined}_{\text{Value}} & \text{if } \hat{H}(\hat{l})(\text{@proto}).1.1.1.1.2 \not\sqsubseteq \perp_{\text{Null}} \\ \perp_{\text{Value}} & \text{otherwise} \end{cases}
\end{aligned}$$

*Cycle in prototype chain is detected at implementation level.*

$$\begin{aligned}
\widehat{\text{ProtoBase}} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \rightarrow \wp(\widehat{\text{Loc}}) \\
\widehat{\text{ProtoBase}}(\hat{H}, \hat{l}, \hat{s}) &= \hat{L}_1 \cup \hat{L}_2 \\
\text{where } \hat{l} &\in \text{dom}(\hat{H}) \\
\wedge \hat{L}_1 &= \begin{cases} \{\hat{l}\} & \text{true} \sqsubseteq (\hat{s} \in \text{dom}(\hat{H}(\hat{l}))) \\ \{\} & \text{otherwise} \end{cases} \\
\wedge \hat{L}_{\text{proto}} &= \hat{H}(\hat{l})(\text{@proto}).1.1.1.2 \\
\wedge \hat{L}_2 &= \begin{cases} \bigsqcup_{\hat{l}_{\text{proto}} \in \hat{L}_{\text{proto}}} \widehat{\text{ProtoBase}}(\hat{H}, \hat{l}_{\text{proto}}, \hat{s}) & \text{false} \sqsubseteq (\hat{s} \in \text{dom}(\hat{H}(\hat{l}))) \\ \{\} & \text{otherwise} \end{cases}
\end{aligned}$$

Pruning<sub>1</sub>

$: \widehat{\text{PrunExpr}} \times \widehat{\text{Value}} \times \widehat{\text{IRRelOP}} \times \widehat{\text{Value}} \times \widehat{\text{State}} \rightarrow \widehat{\text{State}}$

$\widehat{\text{Pruning}}_1(pe, \hat{v}_1, \hat{s}, \hat{v}_2, (\hat{H}, \hat{C})) = (\hat{H}_1, \hat{C}_1)$

where  $(\hat{v}, \hat{abs}) = \widehat{K}_{\hat{s}}(\hat{v}_2)$

$$\hat{s} = \begin{cases} \text{"x"} & \text{if } pe = x \\ \widehat{\text{toString}}(\hat{pv}) & \text{if } pe = e_1[e_2] \\ \text{where } \hat{pv} = \widehat{\text{toPrimitive}}((\hat{V}[\![e_2]\!])(\hat{H}, \hat{C})).1 & \end{cases}$$

$$\hat{L}_{base} = \begin{cases} \widehat{\text{LookupBase}}(\hat{H}, \hat{C}.1, \text{"x"}) & \text{if } pe = x \\ \bigsqcup_{\hat{l} \in (\hat{V}[\![e_1]\!])(\hat{H}, \hat{C})).1.2} \widehat{\text{ProtoBase}}(\hat{H}, \hat{l}, \hat{s}) & \text{if } pe = e_1[e_2] \end{cases}$$

$$\hat{propv} = \begin{cases} \langle \langle \hat{v} \sqcap \hat{v}_1, \hat{ov}.2, \hat{ov}.3, \hat{ov}.4 \rangle, \perp_{Value}, \perp_{FunctionId} \rangle & \text{if } \widehat{\text{size}}(\hat{L}_{base}) = 1 \\ \text{where } \hat{l} \in \hat{L}_{base} & \\ \hat{ov} = \hat{H}(\hat{l})(\hat{s}).1.1 & \\ \perp_{PropValue} & \text{otherwise} \end{cases}$$

$$(\hat{H}_1, \hat{C}_1) = \begin{cases} (\hat{H}[\hat{l} \mapsto \hat{H}(\hat{l})[\hat{s} \mapsto \langle \hat{propv}, \hat{abs} \sqcap \hat{H}(\hat{l})(\hat{s}).2 \rangle]], \hat{C}) & \text{if } \widehat{\text{size}}(\hat{L}_{base}) = 1 \wedge \{x\} = \gamma(\hat{s}) \\ \text{where } \hat{l} \in \hat{L}_{base} & \\ (\perp_{Heap}, \perp_{Context}) & \text{if } \widehat{\text{size}}(\hat{L}_{base}) = 0 \\ (\hat{H}, \hat{C}) & \text{otherwise} \end{cases}$$

Pruning<sub>2</sub>

$: \widehat{\text{RelExpr}} \times \widehat{\text{State}} \rightarrow \widehat{\text{State}}$

$\widehat{\text{Pruning}}_2(re, (\hat{H}, \hat{C})) = (\hat{H}_1, \hat{C}_1)$

where  $e_1 \hat{s} e_2 = re$

$\hat{v}_1 = (\hat{V}[\![e_1]\!])(\hat{H}, \hat{C}).1$

$\hat{v}_2 = (\hat{V}[\![e_2]\!])(\hat{H}, \hat{C}).1$

$\hat{s} = \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\hat{v}_1))$

$$\hat{L}_{base} = \begin{cases} \bigsqcup_{\hat{l} \in \hat{v}_2.2} \widehat{\text{ProtoBase}}(\hat{H}, \hat{l}, \hat{s}) & \text{if } \hat{s} = \text{in} \\ \hat{v}_2.2 & \text{otherwise} \end{cases}$$

$$(\hat{H}_1, \hat{C}_1) = \begin{cases} (\hat{H}[\hat{l} \mapsto \hat{H}(\hat{l})[\hat{s} \mapsto (\hat{H}(\hat{l})(\hat{s})).1]], \hat{C}) & \text{if } \{\hat{l}\} = \hat{L}_{base} \wedge \{x\} = \gamma(\hat{s}) \wedge \hat{s} = \text{in} \\ (\widehat{\text{DeleteAll}}(\hat{H}, \hat{l}, \hat{s}), \hat{C}) & \text{if } \{\hat{l}\} = \hat{L}_{base} \wedge \{x\} = \gamma(\hat{s}) \wedge \hat{s} = \text{notIn} \\ (\widehat{\text{PrunInstanceof}}(\hat{l}_1, \hat{l}, \text{true}, \hat{H}), \hat{C}) & \text{if } \{\hat{l}\} = \hat{L}_{base} \wedge \{\hat{l}_1\} = \hat{v}_1.2 \\ & \wedge \hat{s} = \text{instanceof} \\ (\widehat{\text{PrunInstanceof}}(\hat{l}_1, \hat{l}, \text{false}, \hat{H}), \hat{C}) & \text{if } \{\hat{l}\} = \hat{L}_{base} \wedge \{\hat{l}_1\} = \hat{v}_1.2 \\ & \wedge \hat{s} = \text{notInstanceOf} \\ (\perp_{Heap}, \perp_{Context}) & \text{if } \widehat{\text{size}}(\hat{L}_{base}) = 0 \\ (\hat{H}, \hat{C}) & \text{otherwise} \end{cases}$$

PrunInstanceof

$: \widehat{\text{Loc}} \times \widehat{\text{Loc}} \times \widehat{\text{Bool}} \times \widehat{\text{Heap}} \rightarrow \widehat{\text{Heap}}$

$\widehat{\text{PrunInstanceof}}(\hat{l}_{obj}, \hat{l}_{fun}, \hat{b}, \hat{H}) = \hat{H}_1 \sqcap \hat{H}_2$

where  $\hat{L}_{prototype} = \hat{H}(\hat{l}_{fun})(\text{"prototype"}).1.1.1.2$

$\hat{L}_{proto} = \hat{H}(\hat{l}_{obj})(\text{@proto}).1.1.1.2$

$\hat{L}_1 = \bigsqcup_{\hat{l}_1 \in \hat{L}_{proto}} \bigsqcup_{\hat{l}_2 \in \hat{L}_{prototype}} \widehat{\text{inheritProto}}_2(\hat{H}, \hat{l}_1, \hat{l}_2, \hat{b})$

$\hat{L}_2 = \bigsqcup_{\hat{l}_1 \in \hat{L}_{proto}} \bigsqcup_{\hat{l}_2 \in \hat{L}_{prototype}} \widehat{\text{inheritProto}}_1(\hat{H}, \hat{l}_1, \hat{l}_2, \hat{b})$

$$\hat{H}_1 = \hat{H} \left[ \hat{l}_{obj} \mapsto \hat{H}(\hat{l}_{obj}) \right] \left[ \text{@proto} \mapsto \left\langle \begin{array}{l} \langle \perp_{PValue}, \hat{L}_1 \rangle, \\ \text{false}, \\ \text{false}, \\ \text{false} \end{array} \right\rangle \right]$$

$$\hat{H}_2 = \hat{H} \left[ \hat{l}_{fun} \mapsto \hat{H}(\hat{l}_{fun}) \right] \left[ \text{"prototype"} \mapsto \left\langle \begin{array}{l} \langle \perp_{PValue}, \hat{L}_2 \rangle, \\ \text{false}, \\ \text{false}, \\ \text{false} \end{array} \right\rangle \right]$$

size

$: \wp(\widehat{\text{Loc}}) \rightarrow \text{Number}$

$\widehat{\text{size}}(\{\}) = 0$

$\widehat{\text{size}}(\hat{L}) = 1 + \widehat{\text{size}}(\hat{L}_1) \quad \text{where } \hat{l} \in \hat{L}$

$$\begin{aligned}
\widehat{\text{VarStore}} &: \widehat{\text{Heap}} \times \text{Prop} \times \widehat{\text{Value}} \rightarrow \widehat{\text{Heap}} \\
\widehat{\text{VarStore}}(\hat{H}, x, \hat{v}) &= \hat{H}_1 \quad \text{if } \text{getVarKind}_P(x) = \text{PureLocalVar} \\
&\quad \text{where } \hat{H}_1 = \hat{H}[\# \text{PureLocal}_R \mapsto \hat{H}(\# \text{PureLocal}_R)[x \mapsto \langle \hat{v}, \perp_{\text{Bool}}, \perp_{\text{Bool}}, \text{false} \rangle]] \\
\widehat{\text{VarStore}}(\hat{H}, x, \hat{v}) &= \hat{H}_1 \quad \text{if } \text{getVarKind}_P(x) = \text{CapturedVar} \\
&\quad \text{where } \hat{H}_1 = \bigsqcup_{i \in \hat{H}(\# \text{PureLocal}_R)(\text{@env}).1.2.2} \widehat{\text{VarStoreL}}(\hat{H}, \hat{i}, x, \hat{v}) \\
\widehat{\text{VarStore}}(\hat{H}, x, \hat{v}) &= \hat{H}_1 \quad \text{if } \text{getVarKind}_P(x) = \text{CapturedCatchVar} \\
&\quad \text{where } \hat{H}_1 = \hat{H}[\# \text{Collapsed}_O \mapsto \hat{H}(\# \text{Collapsed}_O)[x \mapsto \langle \hat{v}, \perp_{\text{Bool}}, \perp_{\text{Bool}}, \text{false} \rangle]] \\
\widehat{\text{VarStore}}(\hat{H}, x, \hat{v}) &= \hat{H}_1 \sqcup \hat{H}_2 \quad \text{if } \text{getVarKind}_P(x) = \text{GlobalVar} \\
&\quad \text{where } \hat{H}_1 = \begin{cases} \widehat{\text{VarStoreG}}(\hat{H}, x, \hat{v}) & \text{if } \text{true} \sqsubseteq \text{CanPutVar}(\hat{H}, x) \\ \perp_{\text{Heap}} & \text{otherwise} \end{cases} \\
&\quad \wedge \hat{H}_2 = \begin{cases} \hat{H} & \text{if } \text{false} \sqsubseteq \text{CanPutVar}(\hat{H}, x) \\ \perp_{\text{Heap}} & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{VarStoreG}} &: \widehat{\text{Heap}} \times \text{Prop} \times \widehat{\text{Value}} \rightarrow \widehat{\text{Heap}} \\
\widehat{\text{VarStoreG}}(\hat{H}, x, \hat{v}) &= \hat{H}_1 \sqcup \hat{H}_2 \\
&\quad \text{where } \hat{l}_g = \# \text{Global}_R \wedge \hat{v}_{\text{old}} = \hat{H}(\hat{l}_g)(x).1.1 \\
&\quad \hat{H}_1 = \begin{cases} \widehat{\text{PropStore}}(\hat{H}, \hat{l}_g, \hat{x}, \hat{v}) & \text{if } \text{false} \sqsubseteq (x \in \text{dom}(\hat{H}(\hat{l}_g))) \\ \perp_{\text{Heap}} & \text{otherwise} \end{cases} \\
&\quad \hat{H}_2 = \begin{cases} \hat{H}[\hat{l}_g \mapsto \hat{H}(\hat{l}_g)[x \mapsto \langle \hat{v}, \hat{v}_{\text{old}}.2, \hat{v}_{\text{old}}.3, \hat{v}_{\text{old}}.4 \rangle]] & \text{if } \text{true} \sqsubseteq (x \in \text{dom}(\hat{H}(\hat{l}_g))) \\ \perp_{\text{Heap}} & \text{otherwise} \end{cases}
\end{aligned}$$

*Writable is false only for function name variables, which is always determined exactly.  
Cycle in scope chain is detected at implementation level.*

$$\begin{aligned}
\widehat{\text{VarStoreL}} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \text{Prop} \times \widehat{\text{Value}} \rightarrow \widehat{\text{Heap}} \\
\widehat{\text{VarStoreL}}(\hat{H}, \hat{l}, x, \hat{v}) &= \hat{H}_1 \sqcup \hat{H}_2 \\
&\quad \text{where } \hat{H}_1 = \begin{cases} \hat{H}[\hat{l} \mapsto \hat{H}(\hat{l})[x \mapsto \langle \hat{v}, \text{true}, \perp_{\text{Bool}}, \text{false} \rangle]] & \text{if } \text{true} \sqsubseteq (x \in \text{dom}(\hat{H}(\hat{l}))) \wedge \hat{H}(\hat{l})(x).1.1.2 = \text{true} \\ \hat{H} & \text{if } \text{true} \sqsubseteq (x \in \text{dom}(\hat{H}(\hat{l}))) \wedge \hat{H}(\hat{l})(x).1.1.2 = \text{false} \\ \perp_{\text{Heap}} & \text{otherwise} \end{cases} \\
&\quad \hat{L}_{\text{outer}} = \hat{H}(\hat{l})(\text{@outer}).1.2.2 \\
&\quad \hat{H}_2 = \begin{cases} \bigsqcup_{i_{\text{outer}} \in \hat{L}_{\text{outer}}} \widehat{\text{VarStoreL}}(\hat{H}, \hat{i}_{\text{outer}}, x, \hat{v}) & \text{false} \sqsubseteq (x \in \text{dom}(\hat{H}(\hat{l}))) \\ \perp_{\text{Heap}} & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{PropStore}} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \times \widehat{\text{Value}} \rightarrow \widehat{\text{Heap}} \\
\widehat{\text{PropStore}}(\hat{H}, \hat{l}, \hat{s}, \hat{v}) &= \hat{H}_1 \sqcup \hat{H}_2 \\
&\quad \text{where } \hat{H}_1 = \begin{cases} \hat{H}[\hat{l} \mapsto \hat{H}(\hat{l})[\hat{s} \mapsto \langle \hat{v}, \text{true}, \text{true}, \text{true} \rangle]] & \text{if } \text{false} \sqsubseteq (\hat{s} \in \text{dom}(\hat{H}(\hat{l}))) \\ \perp_{\text{Heap}} & \text{otherwise} \end{cases} \\
&\quad \hat{v}_{\text{old}} = \hat{H}(\hat{l})(\hat{s}).1.1 \\
&\quad \hat{H}_2 = \begin{cases} \hat{H}[\hat{l} \mapsto \hat{H}(\hat{l})[\hat{s} \mapsto \langle \hat{v}, \hat{v}_{\text{old}}.2, \hat{v}_{\text{old}}.3, \hat{v}_{\text{old}}.4 \rangle]] & \text{if } \text{true} \sqsubseteq (\hat{s} \in \text{dom}(\hat{H}(\hat{l}))) \\ \perp_{\text{Heap}} & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{ReturnStore}} &: \widehat{\text{Heap}} \times \widehat{\text{Value}} \rightarrow \widehat{\text{Heap}} \\
\widehat{\text{ReturnStore}}(\hat{H}, \hat{v}) &= \hat{H}[\# \text{PureLocal}_R \mapsto \hat{H}(\# \text{PureLocal}_R)(\text{@return} \mapsto \hat{v})]
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{toBoolean}} &: \widehat{\text{Value}} \rightarrow \widehat{\text{Bool}} \\
\widehat{\text{toBoolean}}(\hat{v}) &= \langle \langle \perp, \perp, \bigcup_{n=1 \dots 8} \hat{b}_n, \perp, \perp \rangle, \{\} \rangle \\
\text{where } \hat{b}_1 &= \text{false} \quad \text{if } \text{undefined} \sqsubseteq \hat{v}.1.1 \\
\hat{b}_2 &= \text{false} \quad \text{if } \text{null} \sqsubseteq \hat{v}.1.2 \\
\hat{b}_3 &= \hat{v}.1.3 \\
\hat{b}_4 &= \text{false} \quad \text{if } \hat{0} \sqsubseteq \hat{v}.1.4 \vee \text{NaN} \sqsubseteq \hat{v}.1.4 \\
\hat{b}_5 &= \text{true} \quad \text{if } \hat{v}.1.4 \not\sqsubseteq \perp_{\text{number}} \wedge \hat{v}.1.4 \neq \hat{0} \wedge \hat{v}.1.4 \neq \text{NaN} \\
\hat{b}_6 &= \text{false} \quad \text{if } \hat{v}.1.5 \not\sqsubseteq \hat{v}.1.5 \\
\hat{b}_7 &= \text{true} \quad \text{if } \hat{v}.1.5 \not\sqsubseteq \perp_{\text{string}} \wedge \hat{v}.1.5 \neq \hat{v}.1.5 \\
\hat{b}_8 &= \text{true} \quad \text{if } \hat{v}.2 \not\sqsubseteq \perp_{\text{Loc}}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{toNumber}} &: \widehat{\text{PValue}} \rightarrow \widehat{\text{Number}} \\
\widehat{\text{toNumber}}(\hat{pv}) &= \hat{n}_1 \sqcup \hat{n}_2 \sqcup \hat{n}_3 \sqcup \hat{n}_4 \sqcup \hat{n}_5 \\
\text{where } \hat{n}_1 &= \text{NaN} \quad \text{if } \text{undefined}_{\text{Value}} \sqsubseteq \hat{pv} \\
\hat{n}_2 &= \hat{0} \quad \text{if } \text{null} \sqsubseteq \hat{pv} \vee \text{false} \sqsubseteq \hat{pv} \\
\hat{n}_3 &= \hat{1} \quad \text{if } \text{true} \sqsubseteq \hat{pv} \\
\hat{n}_4 &= \hat{pv}.4 \\
\hat{n}_5 &= \text{Str2Num}(\hat{pv}) \quad \text{if } \hat{pv}.5 \not\sqsubseteq \perp_{\text{string}}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{toString}} &: \widehat{\text{PValue}} \rightarrow \widehat{\text{String}} \\
\widehat{\text{toString}}(\hat{pv}) &= \hat{s}_1 \sqcup \hat{s}_2 \sqcup \hat{s}_3 \sqcup \hat{s}_4 \sqcup \hat{s}_5 \\
\text{where } \hat{s}_1 &= \text{"undefined"} \quad \text{if } \hat{pv}.1 \not\sqsubseteq \perp_{\text{Undefined}} \\
\hat{s}_2 &= \text{"null"} \quad \text{if } \hat{pv}.2 \not\sqsubseteq \perp_{\text{Null}} \\
\hat{s}_3 &= \text{"pv.3"} \quad \text{if } \hat{pv}.3 \not\sqsubseteq \perp_{\text{Bool}} \\
\hat{s}_4 &= \text{"pv.4"} \quad \text{if } \hat{pv}.4 \not\sqsubseteq \perp_{\text{Number}} \\
\hat{s}_5 &= \hat{pv}.5
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{toStringSet}} &: \widehat{\text{PValue}} \rightarrow \wp(\widehat{\text{String}}) \\
\widehat{\text{toStringSet}}(\hat{pv}) &= \hat{ss} \text{ with redundancies removed} \\
\text{where } \hat{ss}_1 &= \begin{cases} \{\text{"undefined"}\} & \text{if } \hat{pv}.1 \not\sqsubseteq \perp_{\text{Undefined}} \\ \{\} & \text{otherwise} \end{cases} \\
\hat{ss}_2 &= \begin{cases} \{\text{"null"}\} & \text{if } \hat{pv}.2 \not\sqsubseteq \perp_{\text{Null}} \\ \{\} & \text{otherwise} \end{cases} \\
\hat{ss}_3 &= \begin{cases} \{\text{"pv.3"}\} & \text{if } \hat{pv}.3 \not\sqsubseteq \perp_{\text{Bool}} \\ \{\} & \text{otherwise} \end{cases} \\
\hat{ss}_4 &= \begin{cases} \{\text{"pv.4"}\} & \text{if } \hat{pv}.4 \not\sqsubseteq \perp_{\text{Number}} \\ \{\} & \text{otherwise} \end{cases} \\
\hat{ss}_5 &= \begin{cases} \{\hat{pv}.5\} & \text{if } \hat{pv}.5 \not\sqsubseteq \perp_{\text{String}} \\ \{\} & \text{otherwise} \end{cases} \\
\hat{ss} &= \hat{ss}_1 \cup \hat{ss}_2 \cup \hat{ss}_3 \cup \hat{ss}_4 \cup \hat{ss}_5
\end{aligned}$$

$\widehat{\text{toObject}} : \widehat{\text{Heap}} \times \widehat{\text{Context}} \times \widehat{\text{Value}} \times \widehat{\text{Address}} \rightarrow \widehat{\text{Heap}} \times \widehat{\text{Context}} \times \widehat{\text{Value}} \times \wp(\widehat{\text{Exception}})$

$$\widehat{\text{toObject}}(\hat{H}, \hat{C}, \hat{v}, \hat{a}) = ((\perp_{PValue}, \hat{L}_3), \hat{H}_4, \hat{C}_4, \hat{e}s)$$

where  $\hat{L} = \hat{v}.2$

$$\begin{aligned} \hat{o}_1 &= \begin{cases} \widehat{\text{NewString}}(\hat{v}.1.5) & \text{if } \hat{v}.1.5 \not\sqsubseteq \perp_{string} \\ \perp_{Obj} & \text{otherwise} \end{cases} \\ \hat{o}_2 &= \begin{cases} \widehat{\text{NewBoolean}}(\hat{v}.1.3) & \text{if } \hat{v}.1.3 \not\sqsubseteq \perp_{boolean} \\ \perp_{Obj} & \text{otherwise} \end{cases} \\ \hat{o}_3 &= \begin{cases} \widehat{\text{NewNumber}}(\hat{v}.1.4) & \text{if } \hat{v}.1.4 \not\sqsubseteq \perp_{number} \\ \perp_{Obj} & \text{otherwise} \end{cases} \\ \hat{e}s &= \begin{cases} \{\widehat{\text{TypeException}}\} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{undef} \vee \hat{v}.1.2 \not\sqsubseteq \perp_{null} \\ \{\} & \text{otherwise} \end{cases} \\ \hat{o} &= \hat{o}_1 \sqcup \hat{o}_2 \sqcup \hat{o}_3 \\ (\hat{H}_1, \hat{C}_1) &= \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new}) \quad // \text{Recency Abstraction} \\ \hat{l}_R &= (\hat{a}, \widehat{\text{Recent}}) \quad // \text{Recency Abstraction} \\ (\hat{L}_1, \hat{H}_2, \hat{C}_2) &= \begin{cases} (\{\hat{l}_R\}, \hat{H}_1[\hat{l}_R \mapsto \hat{o}], \hat{C}_1) & \text{if } \hat{o} \not\sqsubseteq \perp_{Obj} \\ (\{\}, \perp_{Heap}, \perp_{Context}) & \text{otherwise} \end{cases} \\ (\hat{L}_2, \hat{H}_3, \hat{C}_3) &= \begin{cases} (\hat{L}, \hat{H}, \hat{C}) & \text{if } \hat{L} \not\sqsubseteq \{\} \\ (\{\}, \perp_{Heap}, \perp_{Context}) & \text{otherwise} \end{cases} \\ \hat{L}_3 &= \hat{L}_1 \sqcup \hat{L}_2 \wedge \hat{H}_4 = \hat{H}_2 \sqcup \hat{H}_3 \wedge \hat{C}_4 = \hat{C}_2 \sqcup \hat{C}_3 \end{aligned}$$

$\widehat{\text{toPrimitive}} : \widehat{\text{Value}} \rightarrow \widehat{\text{PValue}}$

$$\widehat{\text{toPrimitive}}(\hat{v}) = \hat{v}.1 \sqcup \widehat{\text{Obj2Str}}(\hat{v}.2)$$

*For all case of  $\hat{s}_n$  if the condition is false, the value of  $\hat{s}_n$  is  $\perp_{String}$ .*

$\widehat{\text{TypeTag}} : \widehat{\text{Heap}} \times \widehat{\text{Value}} \rightarrow \widehat{\text{String}}$

$$\begin{aligned} \widehat{\text{TypeTag}}(\hat{H}, \hat{v}) &= \hat{s}_1 \sqcup \hat{s}_2 \sqcup \hat{s}_3 \sqcup \hat{s}_4 \sqcup \hat{s}_5 \sqcup \hat{s}_6 \sqcup \hat{s}_7 \\ \hat{s}_1 &= \text{"number"} & \text{if } \hat{v}.1.4 \not\sqsubseteq \perp_{number} \\ \hat{s}_2 &= \text{"boolean"} & \text{if } \hat{v}.1.3 \not\sqsubseteq \perp_{boolean} \\ \hat{s}_3 &= \text{"string"} & \text{if } \hat{v}.1.5 \not\sqsubseteq \perp_{string} \\ \text{where } \hat{s}_4 &= \text{"object"} & \text{if } \hat{v}.2 \not\sqsubseteq \perp_{Loc} \wedge \text{false} \sqsubseteq \bigsqcup_{i \in \hat{v}.2} \widehat{\text{IsCallable}}(\hat{H}, \hat{i}) \\ \hat{s}_5 &= \text{"function"} & \text{if } \hat{v}.2 \not\sqsubseteq \perp_{Loc} \wedge \text{true} \sqsubseteq \bigsqcup_{i \in \hat{v}.2} \widehat{\text{IsCallable}}(\hat{H}, \hat{i}) \\ \hat{s}_6 &= \text{"object"} & \text{if } \hat{v}.1.2 \not\sqsubseteq \perp_{null} \\ \hat{s}_7 &= \text{"undefined"} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{undef} \end{aligned}$$

$\widehat{\text{validity}}_1 : \widehat{\text{Expression}} \times \widehat{\text{State}} \rightarrow \text{Boolean}$

$$\begin{aligned} \widehat{\text{validity}}_1(e, (\hat{H}, \hat{C})) &= b \\ \text{where } \hat{v} &= (\hat{\mathcal{V}}[e])(\hat{H}, \hat{C}).1 \\ b &= \begin{cases} \text{true} & \text{if } \hat{v}.1.1 \sqsubseteq \perp_{Undef} \wedge \hat{v}.1.2 \sqsubseteq \perp_{Null} \wedge (\hat{v}.1.4 \sqsubseteq \widehat{\text{U}}\widehat{\text{Int}} \vee \hat{v}.1.4 \sqsubseteq \widehat{\text{N}}\widehat{\text{U}}\widehat{\text{Int}}) \\ & \wedge \hat{v}.1.5 \sqsubseteq \perp_{String} \wedge \hat{v}.2 = \{\} \\ \text{false} & \text{otherwise} \end{cases} \end{aligned}$$

$\widehat{\text{validity}}_2 : \widehat{\text{Expression}} \times \widehat{\text{Expression}} \times \widehat{\text{State}} \rightarrow \text{Boolean}$

$$\widehat{\text{validity}}_2(e_1, e_2, (\hat{H}, \hat{S})) = \widehat{\text{validity}}_1(e_1, \hat{S}) \wedge \widehat{\text{validity}}_1(e_2, \hat{S})$$

$\widehat{\text{validity}}_3 : \widehat{\text{Expression}} \times \widehat{\text{Expression}} \times \widehat{\text{Expression}} \times \widehat{\text{State}} \rightarrow \text{Boolean}$

$$\widehat{\text{validity}}_3(e_1, e_2, e_3, (\hat{H}, \hat{S})) = \widehat{\text{validity}}_1(e_1, \hat{S}) \wedge \widehat{\text{validity}}_1(e_2, \hat{S}) \wedge \widehat{\text{validity}}_1(e_3, \hat{S})$$

$\widehat{\text{X}} : \widehat{\text{RelExpr}} \rightarrow \widehat{\text{State}} \rightarrow \widehat{\text{State}}$

$$\begin{aligned} \widehat{\text{X}}[re](\hat{H}, \hat{C}) &= (\hat{H}_1, \hat{C}_1) \\ \text{where } e_1 \S e_2 &= re \\ \hat{v}_1 &= (\hat{\mathcal{V}}[e_1])(\hat{H}, \hat{C}).1 \\ \hat{v}_2 &= (\hat{\mathcal{V}}[e_2])(\hat{H}, \hat{C}).1 \\ (\hat{H}_1, \hat{C}_1) &= \begin{cases} \widehat{\text{Pruning}}_1(e_1, \hat{v}_1, \S, \hat{v}_2, (\hat{H}, \hat{C})) & \text{if } \S \in \text{IRRelOP} \wedge e_1 \in \text{PrunExpression} \\ \widehat{\text{Pruning}}_2(re, (\hat{H}, \hat{C})) & \text{if } \S \in \text{IRObjOP} \\ (\hat{H}, \hat{C}) & \text{otherwise} \end{cases} \end{aligned}$$



## 9.4 Context-sensitivity

.../jsaf/analysis/typing/CallContext.scala

### 9.4.1 Context-insensitive

$$\begin{aligned}
 \widehat{\text{CallContext}} &= \widehat{\text{Address}} \\
 \text{global}\widehat{\text{CallContext}} &= \#Global\hat{Call}site \\
 \text{New}\widehat{\text{CallContext}} &: \widehat{\text{CallContext}} \times \text{FunctionId} \times \widehat{\text{Loc}} \times \wp(\widehat{\text{Loc}}) \rightarrow \wp(\widehat{\text{CallContext}} \times \widehat{\text{Obj}}) \\
 &\quad \text{caller context, callee function, callsite, this} \\
 \text{New}\widehat{\text{CallContext}}(\hat{c}c, fid, \hat{l}, \hat{L}) &= \\
 &\quad \begin{cases} \{(\#Global\hat{Call}site, \text{New}\widehat{\text{PureLocal}}(\{\hat{l}\}, \hat{L}))\} & \text{if } \text{isUserFunction}_P(fid) \\ \{(\hat{l}.1, \text{New}\widehat{\text{PureLocal}}(\{\hat{l}\}, \hat{L}))\} & \text{otherwise} \end{cases}
 \end{aligned}$$

### 9.4.2 1-callsite sensitivity

$$\begin{aligned}
 \widehat{\text{CallContext}} &= \widehat{\text{Address}} \times \widehat{\text{Address}} \\
 \text{global}\widehat{\text{CallContext}} &= (\#Global\hat{Call}site, \#Global\hat{Call}site) \\
 \text{New}\widehat{\text{CallContext}} &: \widehat{\text{CallContext}} \times \text{FunctionId} \times \widehat{\text{Loc}} \times \wp(\widehat{\text{Loc}}) \rightarrow \wp(\widehat{\text{CallContext}} \times \widehat{\text{Obj}}) \\
 &\quad \text{caller context, callee function, callsite, this} \\
 \text{New}\widehat{\text{CallContext}}(\hat{c}c, fid, \hat{l}, \hat{L}) &= \\
 &\quad \begin{cases} \{(\langle \hat{l}.1, \#Global\hat{Call}site \rangle, \text{New}\widehat{\text{PureLocal}}(\{\hat{l}\}, \hat{L}))\} & \text{if } \text{isUserFunction}_P(fid) \\ \{(\langle \hat{c}c.1, \hat{l}.1 \rangle, \text{New}\widehat{\text{PureLocal}}(\{\hat{l}\}, \hat{L}))\} & \text{otherwise} \end{cases}
 \end{aligned}$$

### 9.4.3 k-callsite sensitivity

$$\begin{aligned}
 \widehat{\text{CallContext}} &= \widehat{\text{Address list}} \\
 \text{global}\widehat{\text{CallContext}} &= \text{nil} \\
 \text{New}\widehat{\text{CallContext}} &: \widehat{\text{CallContext}} \times \text{FunctionId} \times \widehat{\text{Loc}} \times \wp(\widehat{\text{Loc}}) \rightarrow \wp(\widehat{\text{CallContext}} \times \widehat{\text{Obj}}) \\
 &\quad \text{caller context, callee function, callsite, this} \\
 \text{New}\widehat{\text{CallContext}}(\hat{c}c, fid, \hat{l}, \hat{L}) &= \\
 &\quad \begin{cases} \{(\langle \hat{l}.1 :: \hat{c}c \rangle_k, \text{New}\widehat{\text{PureLocal}}(\{\hat{l}\}, \hat{L}))\} & \text{if } \text{isUserFunction}_P(fid) \\ \{(\langle \hat{l}.1 :: \hat{c}c \rangle_{k+1}, \text{New}\widehat{\text{PureLocal}}(\{\hat{l}\}, \hat{L}))\} & \text{otherwise} \end{cases}
 \end{aligned}$$

### 9.4.4 callsite-set sensitivity

$$\begin{aligned}
 \widehat{\text{CallContext}} &= \wp(\widehat{\text{Address}}) \\
 \text{global}\widehat{\text{CallContext}} &= \{\} \\
 \text{New}\widehat{\text{CallContext}} &: \widehat{\text{CallContext}} \times \text{FunctionId} \times \widehat{\text{Loc}} \times \wp(\widehat{\text{Loc}}) \rightarrow \wp(\widehat{\text{CallContext}} \times \widehat{\text{Obj}}) \\
 &\quad \text{caller context, callee function, callsite, this} \\
 \text{New}\widehat{\text{CallContext}}(\hat{c}c, fid, \hat{l}, \hat{L}) &= \{\langle \hat{c}c \cup \{\hat{l}.1\}, \text{New}\widehat{\text{PureLocal}}(\{\hat{l}\}, \hat{L}) \rangle\}
 \end{aligned}$$



### 9.4.5 1-object sensitivity

$$\begin{aligned}
\widehat{\text{CallContext}} &= \widehat{\text{Loc}} \times \widehat{\text{Address}} \\
\text{global}\widehat{\text{CallContext}} &= (\# \widehat{\text{Global}}_R, \# \widehat{\text{GlobalCallsite}}) \\
\text{New}\widehat{\text{CallContext}} &: \widehat{\text{CallContext}} \times \text{FunctionId} \times \widehat{\text{Loc}} \times \wp(\widehat{\text{Loc}}) \rightarrow \wp(\widehat{\text{CallContext}} \times \widehat{\text{Obj}}) \\
&\quad \text{caller context, callee function, callsite, this} \\
\text{New}\widehat{\text{CallContext}}(\hat{c}c, fid, \hat{l}, \hat{L}) &= \\
&\quad \begin{cases} \bigcup_{\hat{l}_{this} \in \hat{L}} \{ \langle \hat{l}_{this}, \# \widehat{\text{GlobalCallsite}} \rangle, \text{New}\widehat{\text{PureLocal}}(\{\hat{l}\}, \{\hat{l}_{this}\}) \} & \text{if } \text{isUserFunction}_P(fid) \\ \{ \langle (\hat{c}c.1, \hat{l}.1), \text{New}\widehat{\text{PureLocal}}(\{\hat{l}\}, \hat{L}) \rangle \} & \text{otherwise} \end{cases}
\end{aligned}$$

### 9.4.6 1-object sensitivity (TAJS style)

$$\begin{aligned}
\widehat{\text{CallContext}} &= \wp(\widehat{\text{Loc}}) \times \widehat{\text{Address}} \\
\text{global}\widehat{\text{CallContext}} &= (\{\# \widehat{\text{Global}}_R\}, \# \widehat{\text{GlobalCallsite}}) \\
\text{New}\widehat{\text{CallContext}} &: \widehat{\text{CallContext}} \times \text{FunctionId} \times \widehat{\text{Loc}} \times \wp(\widehat{\text{Loc}}) \rightarrow \wp(\widehat{\text{CallContext}} \times \widehat{\text{Obj}}) \\
&\quad \text{caller context, callee function, callsite, this} \\
\text{New}\widehat{\text{CallContext}}(\hat{c}c, fid, \hat{l}, \hat{L}) &= \\
&\quad \begin{cases} \{ \langle (\hat{L}, \# \widehat{\text{GlobalCallsite}}), \text{New}\widehat{\text{PureLocal}}(\{\hat{l}\}, \hat{L}) \rangle \} & \text{if } \text{isUserFunction}_P(fid) \\ \{ \langle (\hat{c}c.1, \hat{l}.1), \text{New}\widehat{\text{PureLocal}}(\{\hat{l}\}, \hat{L}) \rangle \} & \text{otherwise} \end{cases}
\end{aligned}$$

## 9.5 Semantics

.../jsaf/analysis/typing/{Typing, Semantics, Operator, Worklist, Fixpoint}.scala

$$\begin{aligned}
\hat{\mathcal{E}} &\in \widehat{\text{IPEdge}} \rightarrow \widehat{\text{State}} \rightarrow \widehat{\text{State}} \\
\hat{\mathcal{C}} &\in \widehat{\text{ControlPoint}} \rightarrow \widehat{\text{Command}} \rightarrow \widehat{\text{State}} \rightarrow \widehat{\text{State}} \times \widehat{\text{State}} \\
\hat{\mathcal{I}} &\in \widehat{\text{ControlPoint}} \rightarrow \widehat{\text{Instruction}} \rightarrow \widehat{\text{State}} \times \widehat{\text{State}} \rightarrow \widehat{\text{State}} \times \widehat{\text{State}} \\
\hat{\mathcal{V}} &\in \widehat{\text{Expression}} \rightarrow \widehat{\text{State}} \rightarrow \widehat{\text{Value}} \times \wp(\widehat{\text{Exception}}) \\
\hat{\mathcal{B}} &\in \widehat{\text{Expression}} \rightarrow \widehat{\text{State}} \times \widehat{\text{State}} \rightarrow \widehat{\text{State}} \times \widehat{\text{State}}
\end{aligned}$$

$$\begin{aligned}
&\hat{\mathcal{E}}[\hat{c}p \hookrightarrow_{\hat{\mathcal{C}}, \hat{\sigma}} ((fid, \text{ENTRY}), \hat{c}c)](\perp_{Heap}, \hat{C}_1) = \perp_{State} \\
&\hat{\mathcal{E}}[\hat{c}p \hookrightarrow_{\hat{\mathcal{C}}, \hat{\sigma}} ((fid, \text{ENTRY}), \hat{c}c)](\hat{H}_1, \hat{C}_1) = (\hat{H}_3, \hat{C}) \\
&\text{where } \hat{\sigma}_{env} = \text{NewDeclEnvRecord}(\hat{\sigma}(@scope).1.2) \\
&\quad \wedge \hat{\sigma}_2 = \hat{\sigma} - @scope \\
&\quad \wedge \hat{H}_2 = \hat{H}_1[\#PureLocal_R \mapsto \hat{\sigma}_2] \\
&\quad \wedge \hat{H}_3 = \bigsqcup_{\hat{l}_{env} \in \hat{\sigma}_2(@env).1.2.2} \hat{H}_2[\hat{l}_{env} \mapsto \hat{\sigma}_{env}]
\end{aligned}$$

$$\begin{aligned}
&\hat{\mathcal{E}}[\hat{c}p \hookrightarrow_{\hat{\mathcal{C}}, \hat{\sigma}} ((fid, \text{EXIT}), \hat{c}c)](\perp_{Heap}, \hat{C}_1) = \perp_{State} \\
&\hat{\mathcal{E}}[\hat{c}p \hookrightarrow_{\hat{\mathcal{C}}, \hat{\sigma}} ((fid, \text{EXIT}), \hat{c}c)](\hat{H}_1, \hat{C}_1) = \begin{cases} (\hat{H}_3, \hat{C}_2) & \text{if } \hat{C}_2 \neq \perp_{Context} \\ \perp_{State} & \text{if } \hat{C}_2 = \perp_{Context} \end{cases} \\
&\text{where } (\hat{C}_2, \hat{\sigma}_1) = \widehat{\text{FixOldify}}(\hat{\mathcal{C}}, \hat{\sigma}, \hat{C}_1.3, \hat{C}_1.4) \\
&\quad \wedge \hat{v} = \hat{H}_1(\#PureLocal)(@return).1.2 \\
&\quad \wedge \hat{H}_2 = \hat{H}_1[\#PureLocal_R \mapsto \hat{\sigma}_1] \\
&\quad \wedge \hat{H}_3 = \widehat{\text{VarStore}}(\hat{H}_2, \text{getReturnVar}_P(\hat{c}p.1), \hat{v})
\end{aligned}$$

$$\begin{aligned}
&\hat{\mathcal{E}}[\hat{c}p \hookrightarrow_{\hat{\mathcal{C}}, \hat{\sigma}} ((fid, \text{EXIT-EXC}), \hat{c}c)](\perp_{Heap}, \hat{C}_1) = \perp_{State} \\
&\hat{\mathcal{E}}[\hat{c}p \hookrightarrow_{\hat{\mathcal{C}}, \hat{\sigma}} ((fid, \text{EXIT-EXC}), \hat{c}c)](\hat{H}_1, \hat{C}_1) = \begin{cases} (\hat{H}_2, \hat{C}_2) & \text{if } \hat{C}_2 \neq \perp_{Context} \\ \perp_{State} & \text{if } \hat{C}_2 = \perp_{Context} \end{cases} \\
&\text{where } (\hat{C}_2, \hat{\sigma}_1) = \widehat{\text{FixOldify}}(\hat{\mathcal{C}}, \hat{\sigma}, \hat{C}_1.3, \hat{C}_1.4) \\
&\quad \wedge \hat{v} = \hat{H}_1(\#PureLocal)(@exception).1.2 \\
&\quad \wedge \hat{v}_{old} = \hat{\sigma}_1(@exception.all).1.2 \\
&\quad \wedge \hat{H}_2 = \hat{H}_1 \left[ \#PureLocal_R \mapsto \hat{\sigma}_1 \left[ \begin{array}{l} @exception \mapsto \hat{v}, \\ @exception.all \mapsto \hat{v} \sqcup \hat{v}_{old} \end{array} \right] \right]
\end{aligned}$$

$$\hat{\mathcal{C}}_{cp}[\![c]\!](\perp_{Heap}, \perp_{Context}) = (\perp_{State}, \perp_{State})$$

$$\hat{\mathcal{C}}_{cp}[\![\text{entry}]\!](\hat{H}_0, \hat{C}) = ((\hat{H}_m, \hat{C}), \perp_{State})$$

where  $((fid_{this}, \text{ENTRY}), \hat{c}) = \hat{c}_p$

$$\wedge x_1 \cdots x_n = \widehat{\text{getArgVars}}_P(fid_{this}) \wedge x_{n+1} \cdots x_m = \widehat{\text{getLocalVars}}_P(fid_{this})$$

$$\wedge \hat{L}_{arg} = \hat{H}_0(\#PureLocal_R)(\widehat{\text{getArgumentsName}}(fid_{this})).1.1.1.2$$

$$\wedge \forall 1 \leq i \leq n. \hat{H}_i = \widehat{\text{CreateMutableBinding}}(\hat{H}_{i-1}, x_i, \bigsqcup_{\hat{l}_{arg} \in \hat{L}_{arg}} \widehat{\text{Proto}}(\hat{H}_{i-1}, \hat{l}_{arg}, "i - 1"))$$

$$\wedge \forall n+1 \leq j \leq m. \hat{H}_j = \widehat{\text{CreateMutableBinding}}(\hat{H}_{j-1}, x_j, \text{undefined}_{Value})$$

$$\hat{\mathcal{C}}_{cp}[\![\text{exit}]\!](\hat{H}, \hat{C}) = ((\hat{H}, \hat{C}), \perp_{State})$$

$$\hat{\mathcal{C}}_{cp}[\![\text{exit-exc}]\!](\hat{H}, \hat{C}) = ((\hat{H}, \hat{C}), \perp_{State})$$

$$\hat{\mathcal{C}}_{cp}[\![i^+]\!](\hat{H}, \hat{C}) = (\hat{\mathcal{I}}_{cp}[\![i]\!](\hat{H}, \hat{C}), \perp_{State})^+$$

$$\hat{\mathcal{I}}_{cp}[\![i]\!](\perp_{Heap}, \hat{C}, \hat{S}) = (\perp_{State}, \hat{S})$$

$$\hat{\mathcal{I}}_{cp}[\![x := \text{alloc}(e^?) \hat{a}_{new}]\!](\hat{H}, \hat{C}, \hat{S}) = ((\hat{H}_3, \hat{C}_1), \hat{S}_1)$$

where  $\hat{l}_R = (\hat{a}_{new}, \widehat{Recent}) \wedge (\hat{H}_1, \hat{C}_1) = \widehat{Oldify}(\hat{H}, \hat{C}, \hat{a}_{new})$  // Recency Abstraction

$\wedge (\hat{v}, \hat{e}s) = \hat{\mathcal{V}}[\![e]\!](\hat{H}_1, \hat{C}_1)$  // if  $e$  is None,  $\hat{v}$  is considered as an element of PValue.

$$\wedge \hat{L}_p = \hat{v}.2 \wedge \hat{L}_v = \begin{cases} \{ \#ObjProto_R \} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{ \} & \text{otherwise} \end{cases}$$

$$\wedge \hat{H}_2 = \hat{H}_1[\hat{l}_R \mapsto \bigsqcup_{\hat{l}_p \in \hat{L}_p \cup \hat{L}_v} \widehat{\text{NewObject}}(\hat{l}_p)]$$

$$\wedge \hat{H}_3 = \widehat{\text{VarStore}}(\hat{H}_2, x, \langle \perp_{PValue}, \{\hat{l}_R\} \rangle)$$

$$\wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s)$$

$$\hat{\mathcal{I}}_{cp}[\![x := \text{allocArray}(n) \hat{a}_{new}]\!](\hat{H}, \hat{C}, \hat{S}) = ((\hat{H}_3, \hat{C}_1), \hat{S}_1)$$

where  $\hat{l}_R = (\hat{a}_{new}, \widehat{Recent}) \wedge (\hat{H}_1, \hat{C}_1) = \widehat{Oldify}(\hat{H}, \hat{C}, \hat{a}_{new})$  // Recency Abstraction

$$\wedge \hat{n} = (\hat{\mathcal{V}}[\![n]\!](\hat{H}_1, \hat{C}_1)).1.1.4$$

$$\wedge \hat{H}_2 = \hat{H}_1[\hat{l}_R \mapsto \widehat{\text{NewArrayObject}}(\hat{n})]$$

$$\wedge \hat{H}_3 = \widehat{\text{VarStore}}(\hat{H}_2, x, \langle \perp_{PValue}, \{\hat{l}_R\} \rangle)$$

$$\hat{\mathcal{I}}_{cp}[\![x := \text{allocArg}(n) \hat{a}_{new}]\!](\hat{H}, \hat{C}, \hat{S}) = ((\hat{H}_3, \hat{C}_1), \hat{S}_1)$$

where  $\hat{l}_R = (\hat{a}_{new}, \widehat{Recent}) \wedge (\hat{H}_1, \hat{C}_1) = \widehat{Oldify}(\hat{H}, \hat{C}, \hat{a}_{new})$  // Recency Abstraction

$$\wedge \hat{n} = (\hat{\mathcal{V}}[\![n]\!](\hat{H}_1, \hat{C}_1)).1.1.4$$

$$\wedge \hat{H}_2 = \hat{H}_1[\hat{l}_R \mapsto \widehat{\text{NewArgObject}}(\hat{n})]$$

$$\wedge \hat{H}_3 = \widehat{\text{VarStore}}(\hat{H}_2, x, \langle \perp_{PValue}, \{\hat{l}_R\} \rangle)$$

$$\begin{aligned}
\hat{\mathcal{I}}_{cp} \llbracket x := e \rrbracket \left( (\hat{H}, \hat{C}), \hat{S} \right) &= \left( (\hat{H}_1, \hat{C}_1), \hat{S}_1 \right) \\
\text{where } (\hat{v}, \hat{es}) &= \hat{\mathcal{V}} \llbracket e \rrbracket (\hat{H}, \hat{C}) \\
\wedge (\hat{H}_1, \hat{C}_1) &= \begin{cases} \widehat{\text{VarStore}}(\hat{H}, x, \hat{v}), \hat{C} & \text{if } \hat{v} \not\sqsubseteq \perp_{Value} \\ (\perp_{Heap}, \perp_{Context}) & \text{otherwise} \end{cases} \\
\wedge \hat{S}_1 &= \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{es})
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{cp} \llbracket x_1 := \text{delete}(x_2) \rrbracket \left( (\hat{H}, \hat{C}), \hat{S} \right) &= \left( \widehat{\text{VarStore}}(\hat{H}_1, x_1, \hat{b}_{Value}), \hat{C} \right), \hat{S} \\
\text{where } \hat{L}_{base} &= \widehat{\text{LookupBase}}(\hat{H}, x_2) \\
\wedge (\hat{H}_1, \hat{b}) &= \bigsqcup_{\hat{l}_{base} \in \hat{L}_{base}} \widehat{\text{Delete}}(\hat{H}, \hat{l}_{base}, \hat{x}_2)
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{cp} \llbracket x := \text{delete}(e) \rrbracket \left( (\hat{H}, \hat{C}), \hat{S} \right) &= \left( (\hat{H}_1, \hat{C}_1), \hat{S}_1 \right) \\
\text{where } (\hat{v}, \hat{es}) &= \hat{\mathcal{V}} \llbracket e \rrbracket (\hat{H}, \hat{C}) \\
\wedge (\hat{H}_1, \hat{C}_1) &= \begin{cases} \widehat{\text{VarStore}}(\hat{H}, x, \text{true}_{Value}), \hat{C} & \text{if } \hat{v} \not\sqsubseteq \perp_{Value} \\ (\perp_{Heap}, \perp_{Context}) & \text{otherwise} \end{cases} \\
\wedge \hat{S}_1 &= \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{es})
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{cp} \llbracket x := \text{delete}(e_1, e_2) \rrbracket \left( (\hat{H}, \hat{C}), \hat{S} \right) &= \left( (\hat{H}_2, \hat{C}_2), \hat{S}_1 \right) \\
\text{where } \hat{L} &= (\hat{\mathcal{V}} \llbracket e_1 \rrbracket (\hat{H}, \hat{C})).1.2 \wedge (\hat{v}, \hat{es}) = \hat{\mathcal{V}} \llbracket e_2 \rrbracket (\hat{H}, \hat{C}) \\
\wedge \hat{ss} &= \begin{cases} \widehat{\text{toStringSet}}(\widehat{\text{toPrimitive}}(\hat{v})) & \text{if } \hat{v} \not\sqsubseteq \perp_{Value} \\ \{\} & \text{otherwise} \end{cases} \\
\wedge (\hat{H}_1, \hat{b}) &= \bigsqcup_{\hat{l} \in \hat{L}} \bigsqcup_{\hat{s} \in \hat{ss}} \widehat{\text{Delete}}(\hat{H}, \hat{l}, \hat{s}) \\
\wedge (\hat{H}_2, \hat{C}_2) &= \begin{cases} \widehat{\text{VarStore}}(\hat{H}_1, x, \hat{b}_{Value}), \hat{C} & \text{if } \hat{H}_1 \not\sqsubseteq \perp_{Heap} \\ (\perp_{Heap}, \perp_{Context}) & \text{otherwise} \end{cases} \\
\wedge \hat{S}_1 &= \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{es})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{\text{cp}} \llbracket e_1 \mid e_2 \rrbracket = e_3 \rrbracket \left( (\hat{H}, \hat{C}), \hat{S} \right) = \left( (\hat{H}_1, \hat{C}_1), \hat{S}_1 \right) \\
& \text{where } \hat{L} = (\hat{\mathcal{V}} \llbracket e_1 \rrbracket (\hat{H}, \hat{C})).1.2 \wedge (\hat{s}, \hat{e}s_s) = (\hat{\mathcal{V}} \llbracket e_2 \rrbracket (\hat{H}, \hat{C})) \wedge (\hat{v}, \hat{e}s) = \hat{\mathcal{V}} \llbracket e_3 \rrbracket (\hat{H}, \hat{C}) \\
& \wedge \hat{v}_{\text{newLen}} = \widehat{\text{ToUInt32}}(\hat{v}) \wedge \hat{v}_{\text{oldLen}} = \hat{H}(\hat{l})(\text{"length"}).1.1.1.1.4 \\
& \wedge \hat{L}_{\text{NArr}} = \left\{ \hat{l} \mid \hat{l} \in \hat{L} \wedge \text{false} \sqsubseteq \widehat{\text{IsArray}}(\hat{H}, \hat{l}) \wedge \text{true} \sqsubseteq \widehat{\text{CanPut}}(\hat{H}, \hat{l}, \hat{s}) \right\} \\
& \wedge \hat{L}_{\text{Arr}} = \left\{ \hat{l} \mid \hat{l} \in \hat{L} \wedge \text{true} \sqsubseteq \widehat{\text{IsArray}}(\hat{H}, \hat{l}) \wedge \text{true} \sqsubseteq \widehat{\text{CanPut}}(\hat{H}, \hat{l}, \hat{s}) \right\} \\
& \wedge \hat{H}_{\text{CanPut}} = \begin{cases} \hat{H} & \text{if } \exists \hat{l} \in \hat{L} : \text{false} \sqsubseteq \widehat{\text{CanPut}}(\hat{H}, \hat{l}, \hat{s}) \\ \perp_{\text{Heap}} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_{\text{NArr}} = \bigsqcup_{\hat{l} \in \hat{L}_{\text{NArr}}} \widehat{\text{PropStore}}(\hat{H}, \hat{l}, \hat{s}, \hat{v}) \\
& \wedge (\hat{H}_{\text{Arr}}, \hat{e}s_{\text{Arr}}) = \bigsqcup_{\hat{l} \in \hat{L}_{\text{Arr}}} (\hat{H}_{\text{Arr}_{\text{length}}} \sqcup \hat{H}_{\text{Arr}_{\text{index}}} \sqcup \hat{H}_{\text{Arr}_{\text{other}}}, \hat{e}s_1) \\
& \wedge (\hat{H}_{\text{Arr}_{\text{length}}}, \hat{e}s_1) = \begin{cases} (\hat{H}_{\text{Arr}_{\text{length}1}}, \hat{e}s_{\text{len}}) & \text{if "length"} \sqsubseteq \hat{s} \\ (\perp_{\text{Heap}}, \perp_{\text{Exception}}) & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_{\text{Arr}_{\text{length}1}} = \begin{cases} \hat{H}_{\text{Arr}_{\text{length}2}} \sqcup \hat{H}_{\text{Arr}_{\text{length}3}} \sqcup \hat{H}_{\text{Arr}_{\text{length}4}} & \text{if true} \sqsubseteq (\widehat{\text{ToNumber}}(\hat{v}) \hat{=} \hat{v}_{\text{newLen}}) \\ \perp_{\text{Heap}} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_{\text{Arr}_{\text{length}2}} = \begin{cases} \widehat{\text{PropStore}}(\hat{H}, \hat{l}, \text{"length"}, \hat{v}) & \text{if true} \sqsubseteq (\hat{v}_{\text{oldLen}} \hat{\leq} \hat{v}_{\text{newLen}}) \wedge \text{true} \sqsubseteq \widehat{\text{CanPut}}(\hat{H}, \hat{l}, \text{"length"}) \\ \perp_{\text{Heap}} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_{\text{Arr}_{\text{length}3}} = \begin{cases} \hat{H} & \text{if false} \sqsubseteq \widehat{\text{CanPut}}(\hat{H}, \hat{l}, \text{"length"}) \\ \perp_{\text{Heap}} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_{\text{Arr}_{\text{length}4}} = \begin{cases} \bigsqcup_{x=\hat{v}_{\text{oldLen}}-1 \text{ to } \hat{v}_{\text{newLen}}} \widehat{\text{Delete}}(\widehat{\text{PropStore}}(\hat{H}, \hat{l}, \text{"length"}, \hat{v}), \hat{l}, x) & \text{if } \hat{v}_{\text{newLen}} \hat{<} \hat{v}_{\text{oldLen}} \\ \widehat{\text{PropStore}}(\hat{H}, \hat{l}, \text{"length"}, \hat{v}) & \text{otherwise} \end{cases} \quad \wedge \text{true} \sqsubseteq \widehat{\text{CanPut}}(\hat{H}, \hat{l}, \text{"length"}) \\
& \wedge \hat{e}s_{\text{len}} = \begin{cases} \{\widehat{\text{RangeError}}\} & \text{if false} \sqsubseteq (\widehat{\text{ToNumber}}(\hat{v}) \hat{=} \widehat{\text{ToUInt32}}(\hat{v})) \\ \perp_{\text{Exception}} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_{\text{Arr}_{\text{index}}} = \begin{cases} \hat{H}_{\text{Arr}_{\text{index}1}} \sqcup \hat{H}_{\text{Arr}_{\text{index}2}} \sqcup \hat{H}_{\text{Arr}_{\text{index}3}} & \text{if true} \sqsubseteq \widehat{\text{IsArrayIndex}}(\hat{s}) \\ \perp_{\text{Heap}} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_{\text{Arr}_{\text{index}1}} = \begin{cases} \hat{H} & \text{if true} \sqsubseteq (\hat{v}_{\text{oldLen}} \hat{\leq} \widehat{\text{ToUInt32}}(\hat{s})) \wedge \text{false} \sqsubseteq \widehat{\text{CanPut}}(\hat{H}, \hat{l}, \text{"length"}) \\ \perp_{\text{Heap}} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_{\text{Arr}_{\text{index}2}} = \begin{cases} \widehat{\text{PropStore}}(\hat{H}, \hat{l}, \hat{s}, \hat{v}) & \text{if true} \sqsubseteq (\widehat{\text{ToUInt32}}(\hat{s}) \hat{<} \hat{v}_{\text{oldLen}}) \\ \perp_{\text{Heap}} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_{\text{Arr}_{\text{index}3}} = \begin{cases} \widehat{\text{PropStore}}(\widehat{\text{PropStore}}(\hat{H}, \hat{l}, \hat{s}, \hat{v}), \hat{l}, \text{"length"}, \widehat{\text{ToUInt32}}(\hat{s} \hat{+} 1)) & \text{if true} \sqsubseteq (\hat{v}_{\text{oldLen}} \hat{\leq} \widehat{\text{ToUInt32}}(\hat{s})) \\ \perp_{\text{Heap}} & \text{otherwise} \end{cases} \quad \wedge \text{true} \sqsubseteq \widehat{\text{CanPut}}(\hat{H}, \hat{l}, \text{"length"}) \\
& \wedge \hat{H}_{\text{Arr}_{\text{other}}} = \begin{cases} \widehat{\text{PropStore}}(\hat{H}, \hat{l}, \hat{s}, \hat{v}) & \text{if } \hat{s} \neq \text{"length"} \wedge \text{false} \sqsubseteq \widehat{\text{IsArrayIndex}}(\hat{s}) \\ \perp_{\text{Heap}} & \text{otherwise} \end{cases} \\
& \wedge (\hat{H}_1, \hat{C}_1) = (\hat{H}_{\text{CanPut}} \sqcup \hat{H}_{\text{NArr}} \sqcup \hat{H}_{\text{Arr}}, \hat{C}) \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s_s \sqcup \hat{e}s \sqcup \hat{e}s_{\text{Arr}})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket x_1 := \text{function } (fid) \hat{a}_{new1}, \hat{a}_{new2} \rrbracket ((\hat{H}, \hat{C}), \hat{S}) \\
&= \left( \left( \hat{H}_3 \left[ \begin{array}{l} \hat{l}_{R1} \mapsto \widehat{\text{NewFunctionObject}}(fid, \hat{H}_3(\# \text{PureLocal}_R)(\text{@env}).1.2, \hat{l}_{R2}, \hat{n}), \\ \hat{l}_{R2} \mapsto \hat{o}_{new} \llbracket \text{"constructor"} \mapsto \langle \langle \perp_{PValue}, \{\hat{l}_{R1}\} \rangle, \text{true}, \text{false}, \text{true} \rangle \end{array} \right], \hat{C}_2 \right), \hat{S} \right) \\
&\quad \text{where } \hat{n} = \alpha(| \widehat{\text{getArgVars}}_P(fid) |) \\
&\quad \wedge \hat{o}_{new} = \widehat{\text{NewObject}}(\# \text{ObjProto}_R) \\
&\quad \wedge \hat{l}_{R1} = (\hat{a}_{new1}, \widehat{\text{Recent}}) \wedge (\hat{H}_1, \hat{C}_1) = \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new1}) \quad // \text{Recency Abstraction} \\
&\quad \wedge \hat{l}_{R2} = (\hat{a}_{new2}, \widehat{\text{Recent}}) \wedge (\hat{H}_2, \hat{C}_2) = \widehat{\text{Oldify}}(\hat{H}_1, \hat{C}_1, \hat{a}_{new2}) \quad // \text{Recency Abstraction} \\
&\quad \wedge \hat{H}_3 = \widehat{\text{VarStore}}(\hat{H}_2, x_1, \langle \perp_{PValue}, \{\hat{l}_{R1}\} \rangle) \\
\\
& \hat{\mathcal{I}}_{cp} \llbracket x_1 := \text{function } x_2 (fid) \hat{a}_{new1}, \hat{a}_{new2}, \hat{a}_{new3} \rrbracket ((\hat{H}, \hat{C}), \hat{S}) \\
&= \left( \left( \hat{H}_5 \left[ \begin{array}{l} \hat{l}_{R1} \mapsto \widehat{\text{NewFunctionObject}}(fid, \{\hat{l}_{R3}\}_{Value}, \hat{l}_{R2}, \hat{n}), \\ \hat{l}_{R2} \mapsto \hat{o}_{new} \llbracket \text{"constructor"} \mapsto \langle \langle \perp_{PValue}, \{\hat{l}_{R1}\} \rangle, \text{true}, \text{false}, \text{true} \rangle \end{array} \right], \hat{C}_3 \right), \hat{S} \right) \\
&\quad \text{where } \hat{n} = \alpha(| \widehat{\text{getArgVars}}_P(fid) |) \\
&\quad \wedge \hat{o}_{new} = \widehat{\text{NewObject}}(\# \text{ObjProto}_R) \\
&\quad \wedge \hat{l}_{R1} = (\hat{a}_{new1}, \widehat{\text{Recent}}) \wedge (\hat{H}_1, \hat{C}_1) = \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new1}) \quad // \text{Recency Abstraction} \\
&\quad \wedge \hat{l}_{R2} = (\hat{a}_{new2}, \widehat{\text{Recent}}) \wedge (\hat{H}_2, \hat{C}_2) = \widehat{\text{Oldify}}(\hat{H}_1, \hat{C}_1, \hat{a}_{new2}) \quad // \text{Recency Abstraction} \\
&\quad \wedge \hat{l}_{R3} = (\hat{a}_{new3}, \widehat{\text{Recent}}) \wedge (\hat{H}_3, \hat{C}_3) = \widehat{\text{Oldify}}(\hat{H}_2, \hat{C}_2, \hat{a}_{new3}) \quad // \text{Recency Abstraction} \\
&\quad \wedge \hat{o}_{env} = \widehat{\text{NewDeclEnvRecord}}(\hat{H}_3(\# \text{PureLocal}_R)(\text{@env}).1.2) \\
&\quad \wedge \hat{H}_4 = \hat{H}_3[\hat{l}_{R3} \mapsto \hat{o}_{env}[x_2 \mapsto \langle \langle \perp_{PValue}, \{\hat{l}_{R1}\} \rangle, \text{false}, \perp_{Bool}, \text{false} \rangle]] \\
&\quad \wedge \hat{H}_5 = \widehat{\text{VarStore}}(\hat{H}_4, x_1, \langle \perp_{PValue}, \{\hat{l}_{R1}\} \rangle)
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{\hat{c}p} \llbracket \text{construct}(e_1, e_2, e_3) \hat{a}_{new} \rrbracket \left( (\hat{H}, \hat{C}), \hat{S} \right) = \left( (\hat{H}_3, \hat{C}_1), \hat{S}_1 \right) \\
& \text{where } \hat{L}_R = (\hat{a}_{new}, \text{Recent}) \wedge (\hat{H}_1, \hat{C}_1) = \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new}) \quad // \text{Recency Abstraction} \\
& \wedge (\hat{v}_1, \hat{e}s_1) = \hat{\mathcal{V}} \llbracket e_1 \rrbracket (\hat{H}_1, \hat{C}_1) \wedge \hat{L}_f = \left\{ \hat{l} \mid \hat{l} \in \hat{v}_1.2 \wedge \text{true} \sqsubseteq \widehat{\text{HasConstruct}}(\hat{H}_1, \hat{l}) \right\} \\
& \wedge \hat{L}_{this} = \widehat{\text{getThis}}(\hat{H}_1, \hat{\mathcal{V}} \llbracket e_2 \rrbracket (\hat{H}_1, \hat{C}_1).1) \\
& \wedge \hat{v}_{arg} = \hat{\mathcal{V}} \llbracket e_3 \rrbracket (\hat{H}_1, \hat{C}_1).1 \\
& \wedge \hat{o}_{old} = \hat{H}_1(\# \text{PureLocal}_R) \\
& \wedge \hat{c}_{caller} = \hat{c}p.2 \\
& \wedge n_{after-call} = \widehat{\text{getAftercallFromCall}}_P(\hat{c}p.1) \\
& \wedge \hat{c}p_{after-call} = (n_{after-call}, \hat{c}_{caller}) \\
& \wedge \hat{c}p_{exc} = (\widehat{\text{getExcSucc}}_P(n_{after-call}), \hat{c}_{caller}) \\
& \wedge \hat{\hookrightarrow} := \hat{\hookrightarrow}^{\text{ip}} \cup \bigcup_{\hat{l}_f \in \hat{L}_f} \bigcup_{fid \in \hat{H}_1(\hat{l}_f)(\text{@construct}).1.3} \bigcup_{(\hat{c}_{new}, \hat{o}_{new}) \in \widehat{\text{NewCallContext}}(\hat{c}_{caller}, fid, \hat{l}_R, \hat{L}_{this})} \left\{ \begin{array}{l} \hat{c}p \xrightarrow{\text{ip}}_{\hat{c}_{new}, \hat{o}_{new_2}} ((fid, \text{ENTRY}), \hat{c}_{new}) \\ \text{where } \hat{C}_{new} = \langle \{\}, \{\}, \{\}, \{\} \rangle \\ \hat{o}_{new_2} = \hat{o}_{new} \left[ \begin{array}{l} \widehat{\text{getArgumentsName}}(fid) \mapsto \langle \hat{v}_{arg}, \text{true}, \text{false}, \text{false} \rangle, \\ \text{@scope} \mapsto \hat{H}_1(\hat{l}_f)(\text{@scope}).1 \end{array} \right] \\ ((fid, \text{EXIT}), \hat{c}_{new}) \xrightarrow{\text{ip}}_{\hat{C}_1, \hat{o}_{old}} \hat{c}p_{after-call}, \\ ((fid, \text{EXIT-EXC}), \hat{c}_{new}) \xrightarrow{\text{ip}}_{\hat{C}_1, \hat{o}_{old}} \hat{c}p_{exc} \end{array} \right\} \\
& \wedge \hat{H}_2 = \bigsqcup_{\hat{l} \in \hat{v}_{arg}.2} \hat{H}_1 \left[ \hat{l} \mapsto \hat{H}_1(\hat{l}) \left[ \text{"callee"} \mapsto \langle \langle \perp_{PValue}, \hat{L}_f \rangle, \text{true}, \text{false}, \text{true} \rangle \right] \right] \\
& \wedge \hat{e}s_2 = \{\text{TypeError}\} \quad \text{if } \exists \hat{l} \in \hat{v}_1.2 : \text{false} \sqsubseteq \widehat{\text{HasConstruct}}(\hat{H}_1, \hat{l}) \\
& \wedge \hat{e}s_3 = \{\text{TypeError}\} \quad \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\
& \wedge \hat{e}s = \hat{e}s_1 \sqcup \hat{e}s_2 \sqcup \hat{e}s_3 \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}_1, \hat{C}_1, \hat{e}s) \\
& \wedge \hat{H}_3 = \begin{cases} \hat{H}_2 & \text{if } \hat{L}_f \neq \{\} \\ \perp_{Heap} & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{\hat{c}p} \llbracket \text{call}(e_1, e_2, e_3) \hat{a}_{new} \rrbracket \left( (\hat{H}, \hat{C}), \hat{S} \right) = \left( (\hat{H}_3, \hat{C}_1), \hat{S}_1 \right) \\
& \text{where } \hat{L}_R = (\hat{a}_{new}, \text{Recent}) \wedge (\hat{H}_1, \hat{C}_1) = \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new}) \quad // \text{Recency Abstraction} \\
& \wedge (\hat{v}_1, \hat{e}s_1) = \hat{\mathcal{V}} \llbracket e_1 \rrbracket (\hat{H}_1, \hat{C}_1) \wedge \hat{L}_f = \left\{ \hat{l} \mid \hat{l} \in \hat{v}_1.2 \wedge \text{true} \sqsubseteq \widehat{\text{IsCallable}}(\hat{H}_1, \hat{l}) \right\} \\
& \wedge \hat{L}_{this} = \widehat{\text{getThis}}(\hat{H}_1, \hat{\mathcal{V}} \llbracket e_2 \rrbracket (\hat{H}_1, \hat{C}_1).1) \\
& \wedge \hat{v}_{arg} = \hat{\mathcal{V}} \llbracket e_3 \rrbracket (\hat{H}_1, \hat{C}_1).1 \\
& \wedge \hat{o}_{old} = \hat{H}_1(\# \text{PureLocal}_R) \\
& \wedge \hat{c}_{caller} = \hat{c}p.2 \\
& \wedge n_{after-call} = \widehat{\text{getAftercallFromCall}}_P(\hat{c}p.1) \\
& \wedge \hat{c}p_{after-call} = (n_{after-call}, \hat{c}_{caller}) \\
& \wedge \hat{c}p_{exc} = (\widehat{\text{getExcSucc}}_P(n_{after-call}), \hat{c}_{caller}) \\
& \wedge \hat{\hookrightarrow} := \hat{\hookrightarrow}^{\text{ip}} \cup \bigcup_{\hat{l}_f \in \hat{L}_f} \bigcup_{fid \in \hat{H}_1(\hat{l}_f)(\text{@function}).1.3} \bigcup_{(\hat{c}_{new}, \hat{o}_{new}) \in \widehat{\text{NewCallContext}}(\hat{c}_{caller}, fid, \hat{l}_R, \hat{L}_{this})} \left\{ \begin{array}{l} \hat{c}p \xrightarrow{\text{ip}}_{\hat{c}_{new}, \hat{o}_{new_2}} ((fid, \text{ENTRY}), \hat{c}_{new}) \\ \text{where } \hat{C}_{new} = \langle \{\}, \{\}, \{\}, \{\} \rangle \\ \hat{o}_{new_2} = \hat{o}_{new} \left[ \begin{array}{l} \widehat{\text{getArgumentsName}}(fid) \mapsto \langle \hat{v}_{arg}, \text{true}, \text{false}, \text{false} \rangle, \\ \text{@scope} \mapsto \hat{H}_1(\hat{l}_f)(\text{@scope}).1 \end{array} \right] \\ ((fid, \text{EXIT}), \hat{c}_{new}) \xrightarrow{\text{ip}}_{\hat{C}_1, \hat{o}_{old}} \hat{c}p_{after-call}, \\ ((fid, \text{EXIT-EXC}), \hat{c}_{new}) \xrightarrow{\text{ip}}_{\hat{C}_1, \hat{o}_{old}} \hat{c}p_{exc} \end{array} \right\} \\
& \wedge \hat{H}_2 = \bigsqcup_{\hat{l} \in \hat{v}_{arg}.2} \hat{H}_1 \left[ \hat{l} \mapsto \hat{H}_1(\hat{l}) \left[ \text{"callee"} \mapsto \langle \langle \perp_{PValue}, \hat{L}_f \rangle, \text{true}, \text{false}, \text{true} \rangle \right] \right] \\
& \wedge \hat{e}s_2 = \{\text{TypeError}\} \quad \text{if } \exists \hat{l} \in \hat{v}_1.2 : \text{false} \sqsubseteq \widehat{\text{IsCallable}}(\hat{H}_1, \hat{l}) \\
& \wedge \hat{e}s_3 = \{\text{TypeError}\} \quad \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\
& \wedge \hat{e}s = \hat{e}s_1 \sqcup \hat{e}s_2 \sqcup \hat{e}s_3 \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}_1, \hat{C}_1, \hat{e}s) \\
& \wedge \hat{H}_3 = \begin{cases} \hat{H}_2 & \text{if } \hat{L}_f \neq \{\} \\ \perp_{Heap} & \text{otherwise} \end{cases}
\end{aligned}$$

$$\hat{\mathcal{I}}_{cp}[\![\text{assert } (e_1 \otimes e_2)]\!] \left( (\hat{H}, \hat{C}), \hat{S} \right) = \left( \hat{\mathcal{B}}[\![e_1 \otimes e_2]\!] (\hat{H}, \hat{C}), \hat{S} \right)$$

$$\hat{\mathcal{I}}_{cp}[\![\text{catch } (x)]\!] \left( (\hat{H}, \hat{C}), \hat{S} \right) = \left( (\hat{H}_2, \hat{C}), \perp_{State} \right)$$

$$\begin{aligned} \text{where } \hat{v}_{old} &= \hat{H}(\# \text{PureLocal}_R)(\text{@exception\_all}).1.2 \\ \wedge \hat{H}_1 &= \widehat{\text{CreateMutableBinding}}(\hat{H}, x, \hat{H}(\# \text{PureLocal}_R)(\text{@exception}).1.2) \\ \wedge \hat{H}_2 &= \hat{H}_1[\# \text{PureLocal}_R \mapsto \hat{H}_1(\# \text{PureLocal}_R)[\text{@exception} \mapsto \hat{v}_{old}]] \end{aligned}$$

$$\hat{\mathcal{I}}_{cp}[\![\text{return } (e)]\!] \left( (\hat{H}, \hat{C}), \hat{S} \right) = \left( (\hat{H}_1, \hat{C}_1), \hat{S}_1 \right)$$

$$\begin{aligned} \text{where } (\hat{v}, \hat{e}s) &= \hat{\mathcal{V}}[\![e]\!](\hat{H}, \hat{C}) \\ \wedge (\hat{H}_1, \hat{C}_1) &= \begin{cases} (\hat{H}[\# \text{PureLocal}_R \mapsto \hat{H}(\# \text{PureLocal}_R)[\text{@return} \mapsto \hat{v}]], \hat{C}) & \text{if } \hat{v} \not\sqsubseteq \perp_{Value} \\ (\perp_{Heap}, \perp_{Context}) & \text{otherwise} \end{cases} \\ \wedge \hat{S}_1 &= \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s) \end{aligned}$$

$$\hat{\mathcal{I}}_{cp}[\![\text{return } ()]\!] \left( (\hat{H}, \hat{C}), \hat{S} \right) = \left( (\hat{H}_1, \hat{C}), \hat{S} \right)$$

$$\text{where } \hat{H}_1 = \hat{H}[\# \text{PureLocal}_R \mapsto \hat{H}(\# \text{PureLocal}_R)[\text{@return} \mapsto \text{undefined}_{Value}]]$$

$$\hat{\mathcal{I}}_{cp}[\![\text{throw } (e)]\!] \left( (\hat{H}, \hat{C}), \hat{S} \right) = \left( \perp_{State}, \hat{S}_1 \right)$$

$$\begin{aligned} \text{where } (\hat{v}, \hat{e}s) &= \hat{\mathcal{V}}[\![e]\!](\hat{H}, \hat{C}) \\ \wedge \hat{v}_{old} &= \hat{H}(\# \text{PureLocal}_R)(\text{@exception\_all}).1.2 \\ \wedge \hat{H}_1 &= \hat{H} \left[ \# \text{PureLocal}_R \mapsto \hat{H}(\# \text{PureLocal}_R) \left[ \begin{array}{l} \text{@return} \mapsto \text{undefined}_{Value}, \\ \text{@exception} \mapsto \hat{v}, \\ \text{@exception\_all} \mapsto \hat{v} \sqcup \hat{v}_{old} \end{array} \right] \right] \\ \wedge (\hat{H}_e, \hat{C}_e) &= \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s) \wedge \hat{S}_1 = \hat{S} \sqcup (\hat{H}_1 \sqcup \hat{H}_e, \hat{C} \sqcup \hat{C}_e) \end{aligned}$$

$$\hat{\mathcal{I}}_{cp}[\![x := \widehat{\text{toObject}}(e)_{anew}]\!] \left( (\hat{H}, \hat{C}), \hat{S} \right) = \left( (\hat{H}_3, \hat{C}_3), \hat{S}_1 \right)$$

$$\begin{aligned} \text{where } (\hat{v}, \hat{e}s_1) &= \hat{\mathcal{V}}[\![e]\!](\hat{H}, \hat{C}) \\ \wedge (\hat{H}_1, \hat{C}_1, \hat{v}_1, \hat{e}s_2) &= \widehat{\text{toObject}}(\hat{H}, \hat{C}, \hat{v}, \hat{a}_{new}) \\ \wedge (\hat{H}_2, \hat{C}_2) &= \begin{cases} (\widehat{\text{VarStore}}(\hat{H}_1, x, \hat{v}_1), \hat{C}_1) & \text{if } \hat{v}_1 \not\sqsubseteq \perp_{Value} \\ (\perp_{Heap}, \perp_{Context}) & \text{otherwise} \end{cases} \\ \wedge (\hat{H}_3, \hat{C}_3, \hat{e}s_3) &= \begin{cases} (\hat{H}_2, \hat{C}_2, \hat{e}s_1 \sqcup \hat{e}s_2) & \text{if } \hat{v} \not\sqsubseteq \perp_{Value} \\ (\perp_{Heap}, \perp_{Context}, \hat{e}s_1) & \text{otherwise} \end{cases} \\ \wedge \hat{S}_1 &= \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s_3) \end{aligned}$$

$$\hat{\mathcal{I}}_{cp}[\![x := \widehat{\text{isObject}}(e)]\!] \left( (\hat{H}, \hat{C}), \hat{S} \right) = \left( (\hat{H}_1, \hat{C}_1), \hat{S}_1 \right)$$

$$\begin{aligned} \text{where } (\hat{v}, \hat{e}s) &= \hat{\mathcal{V}}[\![e]\!](\hat{H}, \hat{C}) \\ \wedge (\hat{H}_1, \hat{C}_1) &= \begin{cases} (\widehat{\text{VarStore}}(\hat{H}, x, \hat{b}_{Value}), \hat{C}) & \text{if } \hat{v} \not\sqsubseteq \perp_{Value} \\ (\perp_{Heap}, \perp_{Context}) & \text{otherwise} \end{cases} \\ \wedge \hat{b}_1 &= \begin{cases} \text{true} & \text{if } \hat{v}.2 \not\sqsubseteq \perp_{Loc} \\ \perp_{Bool} & \text{otherwise} \end{cases} \wedge \hat{b}_2 = \begin{cases} \text{false} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \perp_{Bool} & \text{otherwise} \end{cases} \\ \wedge \hat{b} &= \hat{b}_1 \sqcup \hat{b}_2 \\ \wedge \hat{S}_1 &= \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s) \end{aligned}$$



$$\begin{aligned}
\hat{\mathcal{I}}_{\hat{c}p} \llbracket x := \widehat{\text{toNumber}}(e) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_1, \hat{C}_1), \hat{S}_1) \\
\text{where } (\hat{v}, \hat{es}) &= \hat{\mathcal{V}}[e](\hat{H}, \hat{C}) \\
\wedge (\hat{H}_1, \hat{C}_1) &= \begin{cases} (\widehat{\text{VarStore}}(\hat{H}, x, (\widehat{\text{toNumber}}(\hat{p}v))_{\text{Value}}), \hat{C}) & \text{if } \hat{v} \not\sqsubseteq \perp_{\text{Value}} \\ (\perp_{\text{Heap}}, \perp_{\text{Context}}) & \text{otherwise} \end{cases} \\
\wedge \hat{p}v &= \widehat{\text{toPrimitive}}(\hat{v}) \\
\wedge \hat{S}_1 &= \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{es}) \\
\hat{\mathcal{I}}_{\hat{c}p} \llbracket x_1 := \widehat{\text{getBase}}(x_2) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\widehat{\text{VarStore}}(\hat{H}, x_1, (\perp_{P\text{Value}}, \hat{L}_{\text{base}})), \hat{C}), \hat{S}) \\
\text{where } \hat{L}_{\text{base}} &= \widehat{\text{LookupBase}}(\hat{H}, x_2) \\
\hat{\mathcal{I}}_{\hat{c}p} \llbracket x := \widehat{\text{iteratorInit}}(e) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}, \hat{C}), \hat{S}) \\
\hat{\mathcal{I}}_{\hat{c}p} \llbracket x := \widehat{\text{iteratorHasNext}}(e_1, e_2) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\widehat{\text{VarStore}}(\hat{H}, x, (\top_{\text{Bool}})_{\text{Value}}), \hat{C}), \hat{S}) \\
\hat{\mathcal{I}}_{\hat{c}p} \llbracket x := \widehat{\text{iteratorNext}}(e_1, e_2) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\widehat{\text{VarStore}}(\hat{H}, x, (\top_{\text{String}})_{\text{Value}}), \hat{C}), \hat{S}) \\
\hat{\mathcal{I}}_{\hat{c}p} \llbracket \text{noop} \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}, \hat{C}), \hat{S}) \\
\hat{\mathcal{V}}[x](\hat{H}, \hat{C}) &= \widehat{\text{Lookup}}(\hat{H}, x) \\
\hat{\mathcal{V}}[e_1 \otimes e_2](\hat{H}, \hat{C}) &= (\hat{v}, \hat{es}) \\
\text{where } (\hat{v}_1, \hat{es}_1) &= \hat{\mathcal{V}}[e_1](\hat{H}, \hat{C}) \wedge (\hat{v}_2, \hat{es}_2) = \hat{\mathcal{V}}[e_2](\hat{H}, \hat{C}) \\
\wedge (\hat{v}, \hat{es}) &= \begin{cases} (\perp_{\text{Value}}, \hat{es}_1) & \text{if } \hat{v}_1 \sqsubseteq \perp_{\text{Value}} \\ (\perp_{\text{Value}}, \hat{es}_1 \sqcup \hat{es}_2) & \text{if } \hat{v}_1 \not\sqsubseteq \perp_{\text{Value}} \wedge \hat{v}_2 \sqsubseteq \perp_{\text{Value}} \\ (\hat{v}_1 \hat{\otimes} \hat{v}_2, \hat{es}_1 \sqcup \hat{es}_2) & \text{otherwise} \end{cases} \\
\hat{\mathcal{V}}[\ominus e](\hat{H}, \hat{C}) &= (\hat{\ominus} \hat{v}, \hat{es}) \quad \text{where } (\hat{v}, \hat{es}) = \hat{\mathcal{V}}[e](\hat{H}, \hat{C}) \\
\hat{\mathcal{V}}[e_1 [e_2]](\hat{H}, \hat{C}) &= (\hat{v}_1, \hat{es}) \\
\text{where } \hat{L} &= (\hat{\mathcal{V}}[e_1](\hat{H}, \hat{C})).1.2 \wedge (\hat{v}, \hat{es}) = \hat{\mathcal{V}}[e_2](\hat{H}, \hat{C}) \\
\wedge \hat{s}s &= \begin{cases} \widehat{\text{toStringSet}}(\widehat{\text{toPrimitive}}(\hat{v})) & \text{if } \hat{v} \not\sqsubseteq \perp_{\text{Value}} \\ \{\} & \text{otherwise} \end{cases} \\
\wedge \hat{v}_1 &= \bigsqcup_{\hat{l} \in \hat{L}} \bigsqcup_{\hat{s} \in \hat{s}s} \widehat{\text{Proto}}(\hat{H}, \hat{l}, \hat{s}) \\
\hat{\mathcal{V}}[\text{n}](\hat{H}, \hat{C}) &= (\hat{n}_{\text{Value}}, \perp_{\text{Exception}}) \\
\hat{\mathcal{V}}[\text{"s"}](\hat{H}, \hat{C}) &= (\hat{s}_{\text{Value}}, \perp_{\text{Exception}}) \\
\hat{\mathcal{V}}[\text{true}](\hat{H}, \hat{C}) &= (\hat{\text{true}}_{\text{Value}}, \perp_{\text{Exception}}) \\
\hat{\mathcal{V}}[\text{false}](\hat{H}, \hat{C}) &= (\hat{\text{false}}_{\text{Value}}, \perp_{\text{Exception}}) \\
\hat{\mathcal{V}}[\text{null}](\hat{H}, \hat{C}) &= (\hat{\text{null}}_{\text{Value}}, \perp_{\text{Exception}}) \\
\hat{\mathcal{V}}[\text{this}](\hat{H}, \hat{C}) &= (\langle \perp_{P\text{Value}}, \hat{H}(\# \text{PureLocal})(@this).1.2.2 \rangle, \perp_{\text{Exception}})
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{V}}[e_1 \text{ instanceof } e_2](\hat{H}, \hat{C}) &= (\hat{b}_{Value}, \hat{es}) \\
\text{where } (\hat{v}_1, \hat{es}_1) &= \hat{\mathcal{V}}[e_1](\hat{H}, \hat{C}) \wedge (\hat{v}_2, \hat{es}_2) = \hat{\mathcal{V}}[e_2](\hat{H}, \hat{C}) \\
\wedge \hat{L}_1 &= \hat{v}_1.2 \wedge \hat{L}_2 = \hat{v}_2.2 \\
\wedge \hat{L}_3 &= \left\{ \hat{l} \mid \hat{l} \in \hat{L}_2 \wedge \text{true} \sqsubseteq \widehat{\text{HasInstance}}(\hat{H}, \hat{l}) \right\} \\
\wedge \hat{v}_{proto} &= \bigsqcup_{\hat{l} \in \hat{L}_3} \widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"prototype"}) \\
\wedge \hat{L}_4 &= \hat{v}_{proto}.2 \\
\wedge \hat{L}_5 &= \left\{ \hat{l} \mid \hat{l} \in \hat{L}_2 \wedge \text{false} \sqsubseteq \widehat{\text{HasInstance}}(\hat{H}, \hat{l}) \right\} \\
\wedge \hat{b}_1 &= \bigsqcup_{\hat{l}_1 \in \hat{L}_1} \bigsqcup_{\hat{l}_2 \in \hat{L}_4} \widehat{\text{inherit}}(\hat{H}, \hat{l}_1, \hat{l}_2) \\
\wedge \hat{b}_2 &= \begin{cases} \text{false} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \wedge \hat{L}_4 \not\sqsubseteq \{\} \\ \perp_{Bool} & \text{otherwise} \end{cases} \\
\wedge \hat{es}_3 &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_2.1 \not\sqsubseteq \perp_{PValue} \vee \hat{L}_5 \not\sqsubseteq \{\} \vee \hat{v}_{proto}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
\wedge \hat{b} &= \hat{b}_1 \sqcup \hat{b}_2 \wedge \hat{es} = \hat{es}_1 \sqcup \hat{es}_2 \sqcup \hat{es}_3
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{V}}[e_1 \text{ in } e_2](\hat{H}, \hat{C}) &= (\hat{b}_{Value}, \hat{es}) \\
\text{where } (\hat{v}_1, \hat{es}_1) &= \hat{\mathcal{V}}[e_1](\hat{H}, \hat{C}) \wedge (\hat{v}_2, \hat{es}_2) = \hat{\mathcal{V}}[e_2](\hat{H}, \hat{C}) \\
\wedge \hat{s} &= \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\hat{v}_1)) \\
\wedge \hat{b} &= \bigsqcup_{\hat{l} \in \hat{v}_2.2} \widehat{\text{HasProperty}}(\hat{H}, \hat{l}, \hat{s}) \\
\wedge \hat{es}_3 &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_2.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
\wedge \hat{es} &= \hat{es}_1 \sqcup \hat{es}_2 \sqcup \hat{es}_3
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{V}}[\text{typeof } x](\hat{H}, \hat{C}) &= ((\hat{s}_1 \sqcup \hat{s}_2)_{Value}, \{\}) \\
\text{where } (\hat{v}, \hat{es}) &= \hat{\mathcal{V}}[x](\hat{H}, \hat{C}) \\
\wedge \hat{s}_1 &= \widehat{\text{TypeTag}}(\hat{H}, \hat{v}) \\
\wedge \hat{s}_2 &= \begin{cases} \text{"undefined"} & \text{if } \text{ReferenceError} \in \hat{es} \\ \perp_{String} & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{V}}[\text{typeof } e](\hat{H}, \hat{C}) &= ((\widehat{\text{TypeTag}}(\hat{H}, \hat{v}))_{Value}, \hat{es}) \\
\text{where } (\hat{v}, \hat{es}) &= \hat{\mathcal{V}}[e](\hat{H}, \hat{C})
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{B}}[e]((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_1, \hat{C}_1), \hat{S}_1) \\
\text{where } relSet &= \begin{cases} \widehat{\text{getRel}}(e_1 \S e_2, (\hat{H}, \hat{C})) \cup \widehat{\text{getRel}}(e_2 \S^t e_1, (\hat{H}, \hat{C})) & \text{if } e_1 \S e_2 = e \wedge \S \in \text{IRRelOP} \\ \{e\} & \text{if } e_1 \S e_2 = e \wedge \S \in \text{IRObjOP} \\ \emptyset & \text{otherwise} \end{cases} \\
(\hat{v}, \hat{es}) &= \hat{\mathcal{V}}[e](\hat{H}, \hat{C}) \\
\hat{S}_1 &= \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{es}) \\
(\hat{H}_1, \hat{C}_1) &= \begin{cases} \bigsqcup_{re \in relSet} \widehat{\text{X}}[re](\hat{H}, \hat{C}) & \text{if } relSet \neq \emptyset \wedge \text{true} \sqsubseteq \widehat{\text{toBoolean}}(\hat{v}).1.3 \\ (\hat{H}, \hat{C}) & \text{if } relSet = \emptyset \wedge \text{true} \sqsubseteq \widehat{\text{toBoolean}}(\hat{v}).1.3 \\ (\perp_{Heap}, \perp_{Context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\ominus &::= \text{void} \mid + \mid - \mid \sim \mid ! \\
\otimes &::= \mid \mid \& \mid ^ \mid << \mid >> \mid >>> \\
&\mid + \mid - \mid * \mid / \mid \% \mid == \mid != \mid === \mid !== \mid < \mid > \mid <= \mid >=
\end{aligned}$$

## Chapter 10

# Sparse Analysis(Incomplete)

### 10.1 Access Analysis

- New location and property name pairs  $\langle \#Context, 1 \rangle, \langle \#Context, 2 \rangle$  are introduced to stand for each of  $\widehat{Context}$  values.

### 10.1.1 Helper functions for definition set

$$\begin{aligned}
\widehat{\text{CreateMutableBinding}}_{def} &: \widehat{\text{Heap}} \times \wp(\widehat{\text{Loc}}) \times \text{Prop} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop}) \\
\widehat{\text{CreateMutableBinding}}_{def}(\hat{H}, \hat{L}, x) &= \{ \langle \# \text{PureLocal}_R, x \rangle \} \quad \text{if } \widehat{\text{getVarKind}}_P(x) = \text{PureLocalVar} \\
\widehat{\text{CreateMutableBinding}}_{def}(\hat{H}, \hat{L}, x) &= \{ \langle \hat{l}, x \rangle \mid \hat{l} \in \hat{L} \} \quad \text{if } \widehat{\text{getVarKind}}_P(x) = \text{CapturedVar} \\
\widehat{\text{CreateMutableBinding}}_{def}(\hat{H}, \hat{L}, x) &= \{ \langle \# \text{Collapsed}_O, x \rangle \} \quad \text{if } \widehat{\text{getVarKind}}_P(x) = \text{CapturedCatchV} \\
\widehat{\text{CreateMutableBinding}}_{def}(\hat{H}, \hat{L}, x) &= \{ \langle \# \text{Global}_R, x \rangle \} \quad \text{if } \widehat{\text{getVarKind}}_P(x) = \text{GlobalVar}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{Oldify}}_{def} &: \widehat{\text{Heap}} \times \widehat{\text{Context}} \times \widehat{\text{Address}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop}) \\
\widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}) &= LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5 \\
\text{where } \hat{l}_R &= (\hat{a}, \text{Recent}) \wedge \hat{l}_O = (\hat{a}, \text{Old}) \\
LP_1 &= \begin{cases} \{ \langle \hat{l}_O, s \rangle, \langle \hat{l}_R, s \rangle \mid s \in \text{dom}(\hat{H}(\hat{l}_R)) \} & \text{if } \hat{l}_R \in \text{dom}(\hat{H}) \\ \{ \} & \text{otherwise} \end{cases} \\
LP_2 &= \begin{cases} \{ \langle \hat{l}_O, s \rangle, \langle \hat{l}_R, s \rangle \mid s \in \text{dom}(\hat{H}(\hat{l}_O)) \} & \text{if } \hat{l}_O \in \text{dom}(\hat{H}) \\ \{ \} & \text{otherwise} \end{cases} \\
LP_3 &= \{ \langle \# \text{Context}, 1 \rangle \} \quad \text{if } \hat{l}_R \in \hat{C}.1 \\
LP_4 &= \{ \langle \# \text{Context}, 2 \rangle \} \quad \text{if } \hat{l}_R \in \hat{C}.2 \\
LP_5 &= \{ \langle \hat{l}, s \rangle \mid \hat{l} \in \text{dom}(\hat{H}), s \in \text{dom}(\hat{H})(\hat{l}), \hat{l}_R \in \hat{H}(\hat{l})(s).1.1.1.2 \vee \hat{l}_R \in \hat{H}(s).1.2.2 \}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{NewObject}}_{def} &: \text{Unit} \rightarrow \wp(\text{Prop}) \\
\widehat{\text{NewObject}}_{def}() &= \{ @class, @proto, @extensible, @default_UInt, @default_NUInt \}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{NewArrayObject}}_{def} &: \text{Unit} \rightarrow \wp(\text{Prop}) \\
\widehat{\text{NewArrayObject}}_{def}() &= \{ @class, @proto, "length", @extensible, @default_UInt, @default_NUInt \}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{NewArgObject}}_{def} &: \text{Unit} \rightarrow \wp(\text{Prop}) \\
\widehat{\text{NewArgObject}}_{def}() &= \{ @class, @proto, "length", @extensible, @default_UInt, @default_NUInt \}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{NewFunctionObject}}_{def} &: \text{Unit} \rightarrow \wp(\text{Prop}) \\
\widehat{\text{NewFunctionObject}}_{def}() &= \left\{ @class, @proto, @extensible, @function, @construct, @scope, @default_UInt, @default_NUInt, "prototype", "length" \right\}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{NewDeclEnvRecord}}_{def} &: \text{Unit} \rightarrow \wp(\text{Prop}) \\
\widehat{\text{NewDeclEnvRecord}}_{def}() &= \{ @outer, @default_UInt, @default_NUInt \}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{NewBoolean}}_{def} &: \text{Unit} \rightarrow \wp(\text{Prop}) \\
\widehat{\text{NewBoolean}}_{def}() &= \{ @class, @proto, @extensible, @primitive, @default_UInt, @default_NUInt \}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{NewNumber}}_{def} &: \text{Unit} \rightarrow \wp(\text{Prop}) \\
\widehat{\text{NewNumber}}_{def}() &= \{ @class, @proto, @extensible, @primitive, @default_UInt, @default_NUInt \}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{NewDate}}_{def} &: \text{Unit} \rightarrow \wp(\text{Prop}) \\
\widehat{\text{NewDate}}_{def}() &= \{ @class, @proto, @extensible, @primitive, @default_UInt, @default_NUInt \}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{NewString}}_{def} &: \text{Value} \rightarrow \wp(\text{Prop}) \\
\widehat{\text{NewString}}_{def}(\hat{v}) &= LP_1 \cup LP_2 \\
\text{where } \hat{v}_{len} &= \text{length}(\hat{v}.1.5) \\
LP_1 &= \{ @class, @proto, @extensible, @primitive, @default_UInt, @default_NUInt \} \\
LP_2 &= \{ "i" \mid 0 \leq i \wedge \exists l \in \gamma(\hat{v}_{len}).i < l \}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{NewPureLocal}}_{def} &: \text{Unit} \rightarrow \wp(\text{Prop}) \\
\widehat{\text{NewPureLocal}}_{def}() &= \{ @exception, @exception_all, @return, @default_UInt, @default_NUInt \}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{VarStore}}_{def} &: \widehat{\text{Heap}} \times \wp(\widehat{\text{Loc}}) \times \text{Prop} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop}) \\
\widehat{\text{VarStore}}_{def}(\hat{H}, \hat{L}, x) &= \{ \langle \# \text{PureLocal}_R, x \rangle \} \quad \text{if } \text{getVarKind}_P(x) = \text{PureLocalVar} \\
\widehat{\text{VarStore}}_{def}(\hat{H}, \hat{L}, x) &= \bigcup_{\hat{l} \in \hat{L}} \widehat{\text{VarStoreL}}_{def}(\hat{H}, \hat{l}, x) \quad \text{if } \text{getVarKind}_P(x) = \text{CapturedVar} \\
\widehat{\text{VarStore}}_{def}(\hat{H}, \hat{L}, x) &= \{ \langle \# \text{Collapsed}_O, x \rangle \} \quad \text{if } \text{getVarKind}_P(x) = \text{CapturedCatchVar} \\
\widehat{\text{VarStore}}_{def}(\hat{H}, \hat{L}, x) &= \widehat{\text{VarStoreG}}_{def}(\hat{H}, x)
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{VarStoreL}}_{def} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \text{Prop} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop}) \\
\widehat{\text{VarStoreL}}_{def}(\hat{H}, \hat{l}, x) &= LP_1 \cup LP_2 \\
\text{where } LP_1 &= \begin{cases} \{ \langle \hat{l}, x \rangle \} & \text{if } \text{true} \sqsubseteq (x \in \text{dom}(\hat{H}(\hat{l}))) \wedge \hat{H}(\hat{l})(x).1.1.2 = \text{true} \\ \{\} & \text{otherwise} \end{cases} \\
\hat{L}_{outer} &= \hat{H}(\hat{l})(\text{@outer}).1.2.2 \\
LP_2 &= \begin{cases} \bigcup_{\hat{l}_{outer} \in \hat{L}_{outer}} \widehat{\text{VarStoreL}}_{def}(\hat{H}, \hat{l}_{outer}, x) & \text{if } \text{false} \sqsubseteq (x \in \text{dom}(\hat{H}(\hat{l}))) \\ \{\} & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{VarStoreG}}_{def} &: \widehat{\text{Heap}} \times \text{Prop} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop}) \\
\widehat{\text{VarStoreG}}_{def}(\hat{H}, x) &= LP_1 \cup LP_2 \\
\text{where } \hat{l}_g &= \# \text{Global}_R \\
LP_1 &= \begin{cases} \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}_g, \alpha(x)) & \text{if } \text{false} \sqsubseteq (x \in \text{dom}(\hat{H}(\hat{l}_g))) \\ \{\} & \text{otherwise} \end{cases} \\
LP_2 &= \begin{cases} \{ \langle \hat{l}_g, x \rangle \} & \text{if } \text{true} \sqsubseteq (x \in \text{dom}(\hat{H}(\hat{l}_g))) \\ \{\} & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{PropStore}}_{def} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop}) \\
\widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \hat{s}) &= \{ \langle \hat{l}, \hat{s} \rangle \}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{ReturnStore}}_{def} &: \text{Unit} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop}) \\
\widehat{\text{ReturnStore}}_{def}() &= \{ \langle \# \text{PureLocal}_R, \text{@return} \rangle \}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{Delete}}_{def} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop}) \\
\widehat{\text{Delete}}_{def}(\hat{H}, \hat{l}, \hat{s}) &= LP \\
\text{where } LP &= \{ \langle \hat{l}, \hat{s} \rangle \} \quad \text{if } (\text{true} \sqsubseteq \widehat{\text{HasOwnProperty}}(\hat{H}, \hat{l}, \hat{s}) \wedge \text{true} \sqsubseteq \hat{H}(\hat{l})(\hat{s}).1.1.4) \\
&\quad \vee (\text{false} \sqsubseteq \widehat{\text{hasOwnProperty}}(\hat{H}, \hat{l}, \hat{s}))
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{toObject}}_{def} &: \widehat{\text{Heap}} \times \text{Context} \times \widehat{\text{Value}} \times \widehat{\text{Address}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop}) \\
\widehat{\text{toObject}}_{def}(\hat{H}, \hat{C}, \hat{v}, \hat{a}) &= LP \\
\text{where } O_1 &= \begin{cases} \widehat{\text{NewString}}_{def}(\hat{v}.1.5) & \text{if } \hat{v}.1.5 \not\sqsubseteq \perp_{string} \\ \{\} & \text{otherwise} \end{cases} \\
O_2 &= \begin{cases} \widehat{\text{NewBoolean}}_{def}() & \text{if } \hat{v}.1.3 \not\sqsubseteq \perp_{boolean} \\ \{\} & \text{otherwise} \end{cases} \\
O_3 &= \begin{cases} \widehat{\text{NewNumber}}_{def}() & \text{if } \hat{v}.1.4 \not\sqsubseteq \perp_{number} \\ \{\} & \text{otherwise} \end{cases} \\
O &= O_1 \cup O_2 \cup O_3 \\
LP &= \begin{cases} \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}) \cup \{ \langle \hat{l}_R, s \rangle \mid s \in O \} & \text{if } O \neq \emptyset \\ \{\} & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{RaiseException}}_{def} &: \wp(\widehat{\text{Exception}}) \wp(\widehat{\text{Loc}} \times \text{Prop}) \\
\widehat{\text{RaiseException}}_{def}(\hat{e}s) &= LP \\
\text{where } LP &= \begin{cases} \{ \langle \# \text{PureLocal}_R, \text{@exception\_all} \rangle, \} & \text{if } \hat{e}s \neq \{\} \\ \{ \langle \# \text{PureLocal}_R, \text{@exception} \rangle \} & \text{otherwise} \end{cases}
\end{aligned}$$

### 10.1.2 Helper functions for use set

$\widehat{\text{Oldify}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Context}} \times \widehat{\text{Address}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{Oldify}}_{use}(\hat{H}, \hat{C}, \hat{a}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4$ where $\hat{l}_R = (\hat{a}, \text{Recent}) \wedge \hat{l}_O = (\hat{a}, \text{Old})$ $LP_1 = \left\{ \begin{array}{l} \{ \langle \hat{l}_O, s \rangle, \langle \hat{l}_R, s \rangle \mid s \in \text{dom}(\hat{H}(\hat{l}_R)) \} \quad \text{if } \hat{l}_R \in \text{dom}(\hat{H}) \\ \{ \} \quad \text{otherwise} \end{array} \right.$ $LP_2 = \left\{ \begin{array}{l} \{ \langle \hat{l}_O, s \rangle, \langle \hat{l}_R, s \rangle \mid s \in \text{dom}(\hat{H}(\hat{l}_O)) \} \quad \text{if } \hat{l}_O \in \text{dom}(\hat{H}) \\ \{ \} \quad \text{otherwise} \end{array} \right.$ $LP_3 = \{ \langle \#Context, 1 \rangle, \langle \#Context, 2 \rangle \}$ $LP_4 = \{ \langle \hat{l}, s \rangle \mid \hat{l} \in \text{dom}(\hat{H}), s \in \text{dom}(\hat{H})(\hat{l}), \hat{l}_R \in \hat{H}(\hat{l})(s).1.1.1.2 \vee \hat{l}_R \in \hat{H}(s).1.2.2 \}$
$\widehat{\text{VarStore}}_{use}$	$: \widehat{\text{Heap}} \times \wp(\widehat{\text{Loc}}) \times \text{Prop} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{VarStore}}_{use}(\hat{H}, \hat{L}, x) = \{ \} \quad \text{if } \text{getVarKind}_P(x) = \text{PureLocalVar}$ $\widehat{\text{VarStore}}_{use}(\hat{H}, \hat{L}, x) = \bigcup_{\hat{l} \in \hat{L}} \widehat{\text{VarStoreL}}_{use}(\hat{H}, \hat{l}, x) \quad \text{if } \text{getVarKind}_P(x) = \text{CapturedVar}$ $\widehat{\text{VarStore}}_{use}(\hat{H}, \hat{L}, x) = \{ \langle \#Collapsed_O, x \rangle \} \quad \text{if } \text{getVarKind}_P(x) = \text{CapturedCatchVar}$ $\widehat{\text{VarStore}}_{use}(\hat{H}, \hat{L}, x) = \widehat{\text{VarStoreG}}_{use}(\hat{H}, x) \cup \widehat{\text{CanPutVar}}_{use}(\hat{H}, x)$
$\widehat{\text{VarStoreL}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{VarStoreL}}_{use}(\hat{H}, \hat{l}, x) = \{ \langle \hat{l}, x \rangle \} \cup LP$ where $\hat{L}_{outer} = \hat{H}(\hat{l})(@outer).1.2.2$ $LP = \left\{ \begin{array}{l} \{ \langle \hat{l}, @outer \rangle \} \cup \bigcup_{\hat{l}_{outer} \in \hat{L}_{outer}} \widehat{\text{VarStoreL}}_{use}(\hat{H}, \hat{l}_{outer}, x) \quad \text{if } \text{false} \sqsubseteq (x \in \text{dom}(\hat{H}(\hat{l}))) \\ \{ \} \quad \text{otherwise} \end{array} \right.$
$\widehat{\text{VarStoreG}}_{use}$	$: \widehat{\text{Heap}} \times \text{Prop} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{VarStoreG}}_{use}(\hat{H}, x) = \{ \langle \hat{l}_g, x \rangle \} \cup LP$ where $\hat{l}_g = \#Global_R$ $LP = \left\{ \begin{array}{l} \widehat{\text{PropStore}}_{use}(\hat{H}, \hat{l}_g, \alpha(x)) \quad \text{if } \text{false} \sqsubseteq (x \in \text{dom}(\hat{H}(\hat{l}_g))) \\ \{ \} \quad \text{otherwise} \end{array} \right.$
$\widehat{\text{PropStore}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{PropStore}}_{use}(\hat{H}, \hat{l}, \hat{s}) = \{ \langle \hat{l}, \hat{s} \rangle \}$
$\widehat{\text{CanPutVar}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{String}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{CanPutVar}}_{use}(\hat{H}, \hat{s}) = \{ \langle \#Global_R, x \rangle \} \cup LP$ where $LP = \left\{ \begin{array}{l} \widehat{\text{CanPut}}_{use}(\hat{H}, \#Global_R, \alpha(x)) \quad \text{if } \text{false} \sqsubseteq (x \in \text{dom}(\hat{H}(\#Global_R))) \\ \{ \} \quad \text{otherwise} \end{array} \right.$
$\widehat{\text{CanPut}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{CanPut}}_{use}(\hat{H}, \hat{l}, \hat{s}) = \widehat{\text{CanPutHelp}}_{use}(\hat{H}, \hat{l}, \hat{s}, \hat{l})$
$\widehat{\text{CanPutHelp}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \times \widehat{\text{Loc}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{CanPutHelp}}_{use}(\hat{H}, \hat{l}_1, \hat{s}, \hat{l}_2) = \{ \langle \hat{l}_1, \hat{s} \rangle, \langle \hat{l}_1, @proto \rangle \} \cup LP_1 \cup LP_2$ where $\hat{L}_{proto} = \hat{H}(\hat{l}_1)(@proto).1.1.1.2$ $LP_1 = \left\{ \begin{array}{l} \bigcup_{\hat{l}_{proto} \in \hat{L}_{proto}} \widehat{\text{CanPutHelp}}_{use}(\hat{H}, \hat{l}_{proto}, \hat{s}, \hat{l}_2) \quad \text{if } \text{false} \sqsubseteq (\hat{s} \in \text{dom}(\hat{H}(\hat{l}_1))) \\ \{ \} \quad \text{otherwise} \end{array} \right.$ $LP_2 = \left\{ \begin{array}{l} \{ \langle \hat{l}_2, "@extensible" \rangle \} \quad \text{if } \hat{H}(\hat{l}_1)(@proto).1.1.1.2 \not\sqsubseteq \perp_{Null} \\ \{ \} \quad \text{otherwise} \end{array} \right.$
$\widehat{\text{Delete}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{Delete}}_{use}(\hat{H}, \hat{l}, \hat{s}) = \{ \langle \hat{l}, \hat{s} \rangle \}$
$\widehat{\text{IsArray}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{IsArray}}_{use}(\hat{H}, \hat{l}) = \{ \langle \hat{l}, @class \rangle \}$

$\widehat{\text{LookupBase}}_{use}$	$: \widehat{\text{Heap}} \times \wp(\widehat{\text{Loc}}) \times \text{Prop} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{LookupBase}}_{use}(\hat{H}, \hat{L}, x) = \{ \}$ $\widehat{\text{LookupBase}}_{use}(\hat{H}, \hat{L}, x) = \bigcup_{\hat{l} \in \hat{L}} \widehat{\text{LookupBaseL}}_{use}(\hat{H}, \hat{l}, x)$ $\widehat{\text{LookupBase}}_{use}(\hat{H}, \hat{L}, x) = \{ \}$ $\widehat{\text{LookupBase}}_{use}(\hat{H}, \hat{L}, x) = \widehat{\text{LookupBaseG}}_{use}(\hat{H}, x)$	$\text{if } \widehat{\text{getVarKind}}_P(x) = \text{PureLocalVar}$ $\text{if } \widehat{\text{getVarKind}}_P(x) = \text{CapturedVar}$ $\text{if } \widehat{\text{getVarKind}}_P(x) = \text{CapturedCatchV}$ $\text{if } \widehat{\text{getVarKind}}_P(x) = \text{GlobalVar}$
$\widehat{\text{LookupBaseL}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \text{Prop} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{LookupBaseL}}_{use}(\hat{H}, \hat{l}, x) = \{ \langle \hat{l}, x \rangle \} \cup LP$ $\text{where } \hat{L}_{outer} = \hat{H}(\hat{l})(@outer).1.2.2$ $LP = \begin{cases} \{ \langle \hat{l}, @outer \rangle \} \cup \bigcup_{\hat{l}_{outer} \in \hat{L}_{outer}} \widehat{\text{LookupBaseL}}_{use}(\hat{H}, \hat{l}_{outer}, x) & \text{if } \text{false} \sqsubseteq (x \dot{\in} \dots) \\ \{ \} & \text{otherwise} \end{cases}$	
$\widehat{\text{LookupBaseG}}_{use}$	$: \widehat{\text{Heap}} \times \text{Prop} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{LookupBaseG}}_{use}(\hat{H}, x) = \{ \langle \#G\hat{l}ocal_R, x \rangle, \langle \hat{l}, @outer \rangle \} \cup LP_1 \cup LP_2$ $\text{where } \hat{L}_{proto} = \hat{H}(\#G\hat{l}ocal_R)(@proto).1.1.1.2$ $LP_1 = \{ \langle \hat{l}_{proto}, x \rangle \mid \hat{l}_{proto} \in \hat{L}_{proto} \}$ $LP_2 = \bigcup_{\hat{l}_{proto} \in \hat{L}_{proto}} \begin{cases} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}_{proto}, \alpha(x)) & \text{if } \text{true} \sqsubseteq \widehat{\text{HasProperty}}(\hat{H}, \hat{l}_{proto}, \alpha(x)) \\ \{ \} & \text{otherwise} \end{cases}$	
$\widehat{\text{Proto}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \hat{s}) = \{ \langle \hat{l}, \hat{s} \rangle, \langle \hat{l}, @proto \rangle \} \cup LP$ $\text{where } \hat{L}_{proto} = \hat{H}(\hat{l})(@proto).1.1.1.2$ $LP = \begin{cases} \bigcup_{\hat{l}_{proto} \in \hat{L}_{proto}} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}_{proto}, \hat{s}) & \text{if } \text{false} \sqsubseteq (\hat{s} \dot{\in} dom(\hat{H}(\hat{l}))) \\ \{ \} & \text{otherwise} \end{cases}$	
$\widehat{\text{HasConstruct}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{HasConstruct}}_{use}(\hat{H}, \hat{l}) = \{ \langle \hat{l}, @construct \rangle \}$	
$\widehat{\text{IsCallable}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{IsCallable}}_{use}(\hat{H}, \hat{l}) = \{ \langle \hat{l}, @function \rangle \}$	
$\widehat{\text{getThis}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Value}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{getThis}}_{use}(\hat{H}, \hat{v}) = LP$ $\text{where } LP = \{ \langle \hat{l}, @class \rangle \mid \hat{l} \in \hat{v}.2 \}$	
$\widehat{\text{CreateMutableBinding}}_{use}$	$: \widehat{\text{Heap}} \times \wp(\widehat{\text{Loc}}) \times \text{Prop} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{CreateMutableBinding}}_{use}(\hat{H}, \hat{L}, x) = \{ \}$ $\widehat{\text{CreateMutableBinding}}_{use}(\hat{H}, \hat{L}, x) = \{ \langle \hat{l}, x \rangle \mid \hat{l} \in \hat{L} \}$ $\widehat{\text{CreateMutableBinding}}_{use}(\hat{H}, \hat{L}, x) = \{ \langle \#C\hat{o}llapsed_O, x \rangle \}$ $\widehat{\text{CreateMutableBinding}}_{use}(\hat{H}, \hat{L}, x) = \{ \}$	$\text{if } \widehat{\text{getVarKind}}_P(x) = \text{PureLocalVar}$ $\text{if } \widehat{\text{getVarKind}}_P(x) = \text{CapturedVar}$ $\text{if } \widehat{\text{getVarKind}}_P(x) = \text{CapturedCatchV}$ $\text{if } \widehat{\text{getVarKind}}_P(x) = \text{GlobalVar}$
$\widehat{\text{inherit}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{Loc}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{inherit}}_{use}(\hat{H}, \hat{l}_1, \hat{l}_2) = \{ \langle \hat{l}_1, @proto \rangle \} \cup LP$ $\text{where } LP = \begin{cases} \bigcup_{\hat{l} \in \hat{H}(\hat{l}_1)(@proto).1.1.1.2} \widehat{\text{inherit}}_{use}(\hat{H}, \hat{l}, \hat{l}_2) & \text{if } \hat{l}_1 \neq \hat{l}_2 \\ \{ \} & \text{otherwise} \end{cases}$	
$\widehat{\text{TypeTag}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Value}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{TypeTag}}_{use}(\hat{H}, \hat{v}) = \bigcup_{\hat{l} \in \hat{v}.2} \widehat{\text{IsCallable}}_{use}(\hat{H}, \hat{l})$	

$\widehat{\text{Lookup}}_{use}$	$: \widehat{\text{Heap}} \times \wp(\widehat{\text{Loc}}) \times \text{Prop} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{Lookup}}_{use}(\hat{H}, \hat{L}, x) = \{ \langle \# \text{PureLocal}_R, x \rangle \}$ if $\widehat{\text{getVarKind}}_P(x) = \text{PureLocalVar}$ $\widehat{\text{Lookup}}_{use}(\hat{H}, \hat{L}, x) = \bigcup_{\hat{l} \in \hat{L}} \widehat{\text{LookupL}}_{use}(\hat{H}, \hat{l}, x)$ if $\widehat{\text{getVarKind}}_P(x) = \text{CapturedVar}$ $\widehat{\text{Lookup}}_{use}(\hat{H}, \hat{L}, x) = \{ \langle \# \text{Collapsed}_O, x \rangle \}$ if $\widehat{\text{getVarKind}}_P(x) = \text{CapturedCatchVar}$ $\widehat{\text{Lookup}}_{use}(\hat{H}, \hat{L}, x) = \widehat{\text{LookupG}}_{use}(\hat{H}, x)$ if $\widehat{\text{getVarKind}}_P(x) = \text{GlobalVar}$
$\widehat{\text{LookupL}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{LookupL}}_{use}(\hat{H}, \hat{l}, x) = \{ \langle \hat{l}, x \rangle \} \cup LP$ where $\hat{L}_{outer} = \hat{H}(\hat{l})(@outer).1.2.2$ $LP = \begin{cases} \{ \langle \hat{l}, @outer \rangle \} \cup \bigcup_{\hat{l}_{outer} \in \hat{L}_{outer}} \widehat{\text{LookupL}}_{use}(\hat{H}, \hat{l}_{outer}, x) & \text{if } \text{false} \sqsubseteq (x \in \text{dom}(\hat{H}(\hat{l}))) \\ \{\} & \text{otherwise} \end{cases}$
$\widehat{\text{LookupG}}_{use}$	$: \widehat{\text{Heap}} \times \text{Prop} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{LookupG}}_{use}(\hat{H}, x) = LP_1 \cup LP_2 \cup LP_3$ where $\hat{L}_{proto} = \hat{H}(\# \text{Global}_R)(@proto).1.1.1.2$ $LP_1 = \{ \langle \# \text{Global}, x \rangle, \langle \# \text{Global}, @proto \rangle \}$ $LP_2 = \{ \langle \hat{l}_{proto}, x \rangle \mid \hat{l}_{proto} \in \hat{L}_{proto} \}$ $LP_3 = \bigcup_{\hat{l}_{proto} \in \hat{L}_{proto}} \begin{cases} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}_{proto}, \alpha(x)) & \text{if } \text{true} \sqsubseteq \widehat{\text{HasProperty}}(\hat{H}, \hat{l}_{proto}, \alpha(x)) \\ \{\} & \text{otherwise} \end{cases}$
$\widehat{\text{toObject}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Context}} \times \widehat{\text{Value}} \times \widehat{\text{Address}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{toObject}}_{use}(\hat{H}, \hat{C}, \hat{v}, \hat{a}) = LP$ where $LP = \begin{cases} \widehat{\text{Oldify}}_{use}(\hat{H}, \hat{C}, \hat{a}) & \text{if } \hat{v}.1.5 \not\sqsubseteq \perp_{string} \vee \hat{v}.1.3 \not\sqsubseteq \perp_{boolean} \vee \hat{v}.1.4 \not\sqsubseteq \perp_{number} \\ \{\} & \text{otherwise} \end{cases}$
$\widehat{\text{HasOwnProperty}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{HasOwnProperty}}_{use}(\hat{H}, \hat{l}, \hat{s}) = \{ \langle \hat{l}, \hat{s} \rangle \}$
$\widehat{\text{RaiseException}}_{use}$	$: \wp(\widehat{\text{Exception}}) \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{RaiseException}}_{use}(\hat{e}s) = LP$ where $LP = \begin{cases} \{ \langle \# \text{PureLocal}_R, @exception\_all \rangle \} & \text{if } \hat{e}s \neq \{\} \\ \{\} & \text{otherwise} \end{cases}$
$\widehat{\text{HasProperty}}_{use}$	$: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})$ $\widehat{\text{HasProperty}}_{use}(\hat{H}, \hat{l}, \hat{s}) = LP_1 \cup LP_2 \cup LP_3$ where $\hat{L}_{proto} = \hat{H}(\hat{l})(@proto).1.1.1.2$ $LP_1 = \widehat{\text{HasOwnProperty}}_{use}(\hat{H}, \hat{l}, \hat{s})$ $LP_2 = \{ \langle \hat{l}, @proto \rangle \}$ $LP_3 = \begin{cases} \bigcup_{\hat{l}_{proto} \in \hat{L}_{proto}} \widehat{\text{HasProperty}}_{use}(\hat{H}, \hat{l}_{proto}, \hat{s}) & \text{if } \text{false} \sqsubseteq \widehat{\text{HasOwnProperty}}(\hat{H}, \hat{l}, \hat{s}) \\ \{\} & \text{otherwise} \end{cases}$



### 10.1.3 Semantic functions

$$\begin{aligned}\hat{\mathcal{C}}_{def} &\in \text{Command} \rightarrow \widehat{\text{State}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop}) \\ \hat{\mathcal{C}}_{use} &\in \text{Command} \rightarrow \widehat{\text{State}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop}) \\ \hat{\mathcal{I}}_{def} &\in \text{Instruction} \rightarrow \widehat{\text{State}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop}) \\ \hat{\mathcal{I}}_{use} &\in \text{Instruction} \rightarrow \widehat{\text{State}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop}) \\ \hat{\mathcal{V}}_{use} &\in \text{Expression} \rightarrow \widehat{\text{State}} \rightarrow \wp(\widehat{\text{Loc}} \times \text{Prop})\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{E}}_{def} \llbracket \hat{c}p \hookrightarrow_{\hat{C}, \hat{o}} ((fid, \text{ENTRY}), \hat{c}c) \rrbracket (\hat{H}, \hat{C}_1) &= LP_1 \cup LP_2 \\
\text{where } \hat{o}_2 &= \hat{o} - \text{@scope} \\
LP_1 &= \left\{ \langle \# \widehat{PureLocal}_R, x \rangle \mid x \in \text{dom}(\hat{o}_2) \right\} \\
LP_2 &= \left\{ \langle \hat{l}_{env}, x \rangle \mid \hat{l}_{env} \in \hat{C}.1, x \in \widehat{\text{NewDeclEnvRecord}}_{def}() \right\}
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{E}}_{use} \llbracket \hat{c}p \hookrightarrow_{\hat{C}, \hat{o}} ((fid, \text{ENTRY}), \hat{c}c) \rrbracket (\hat{H}, \hat{C}_1) &= LP \\
\text{where } \hat{o}_2 &= \hat{o} - \text{@scope} \\
LP &= \left\{ \langle \hat{l}_{env}, x \rangle \mid \hat{l}_{env} \in \hat{C}.1, x \in \widehat{\text{NewDeclEnvRecord}}_{def}() \right\}
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{C}}_{def} \llbracket \text{entry} \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\text{where } ((fid_{this}, \text{ENTRY}), \hat{c}c) &= \hat{c}p \\
\wedge x_1 \cdots x_n &= \widehat{\text{getArgVars}}_P(fid_{this}) \wedge x_{n+1} \cdots x_m = \widehat{\text{getLocalVars}}_P(fid_{this}) \\
LP_1 &= \bigcup_{1 \leq i \leq n} \widehat{\text{CreateMutableBinding}}_{def}(\hat{H}, \hat{C}.1, x_i) \\
LP_2 &= \bigcup_{n+1 \leq j \neq m} \widehat{\text{CreateMutableBinding}}_{def}(\hat{H}, \hat{C}.1, x_j)
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{C}}_{use} \llbracket \text{entry} \rrbracket (\hat{H}, \hat{C}) &= \left\{ \langle \# \text{Context}, 1 \rangle \right\} \cup LP_1 \cup LP_2 \\
\text{where } ((fid_{this}, \text{ENTRY}), \hat{c}c) &= \hat{c}p \\
\hat{L}_{arg} &= \hat{H}(\# \widehat{PureLocal}_R)(\widehat{\text{getArgumentsName}}(fid_{this})).1.1.1.2 \\
\wedge x_1 \cdots x_n &= \widehat{\text{getArgVars}}_P(fid_{this}) \wedge x_{n+1} \cdots x_m = \widehat{\text{getLocalVars}}_P(fid_{this}) \\
LP_1 &= \left\{ \langle \# \widehat{PureLocal}_R, \widehat{\text{getArgumentsName}}(fid_{this}) \rangle \right\} \\
LP_2 &= \bigcup_{i \in \hat{L}_{arg}} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, "i - 1") \\
LP_3 &= \bigcup_{1 \leq i \leq n} \widehat{\text{CreateMutableBinding}}_{use}(\hat{H}, \hat{C}.1, x_i) \\
LP_4 &= \bigcup_{n+1 \leq j \neq m} \widehat{\text{CreateMutableBinding}}_{use}(\hat{H}, \hat{C}.1, x_j)
\end{aligned}$$

$$\hat{\mathcal{C}}_{def} \llbracket \text{exit} \rrbracket (\hat{H}, \hat{C}) = \{\}$$

$$\hat{\mathcal{C}}_{use} \llbracket \text{exit} \rrbracket (\hat{H}, \hat{C}) = \{\}$$

$$\hat{\mathcal{C}}_{def} \llbracket \text{exit-exc} \rrbracket (\hat{H}, \hat{C}) = \{\}$$

$$\hat{\mathcal{C}}_{use} \llbracket \text{exit-exc} \rrbracket (\hat{H}, \hat{C}) = \{\}$$

$$\hat{\mathcal{C}}_{def} \llbracket i^+ \rrbracket (\hat{H}, \hat{C}) = \bigcup_{i \in i^+} \hat{\mathcal{I}}_{def} \llbracket i \rrbracket (\hat{H}, \hat{C})$$

$$\hat{\mathcal{C}}_{use} \llbracket i^+ \rrbracket (\hat{H}, \hat{C}) = \bigcup_{i \in i^+} \hat{\mathcal{I}}_{use} \llbracket i \rrbracket (\hat{H}, \hat{C})$$

$$\hat{\mathcal{I}}_{def} \llbracket x := \text{alloc}(e^?) \hat{a}_{new} \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4$$

$$\begin{aligned}
\text{where } \hat{l}_R &= (\hat{a}_{new}, \text{Recent}) \\
(\hat{v}, \hat{e}s) &= \hat{\mathcal{V}} \llbracket e \rrbracket (\hat{H}, \hat{C}) \\
LP_1 &= \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_{new}) \\
LP_2 &= \left\{ \langle \hat{l}_R, s \rangle \mid s \in \widehat{\text{NewObject}}_{def}() \right\} \\
LP_3 &= \widehat{\text{VarStore}}_{def}(\hat{H}, \hat{C}.1, x) \\
LP_4 &= \widehat{\text{RaiseException}}_{def}(\hat{e}s)
\end{aligned}$$

$$\hat{\mathcal{I}}_{use} \llbracket x := \text{alloc}(e^?) \hat{a}_{new} \rrbracket (\hat{H}, \hat{C}) = \left\{ \langle \# \text{Context}, 1 \rangle \right\} \cup LP_1 \cup LP_2 \cup LP_3 \cup LP_4$$

$$\begin{aligned}
\text{where } (\hat{v}, \hat{e}s) &= \hat{\mathcal{V}} \llbracket e \rrbracket (\hat{H}, \hat{C}) \\
LP_1 &= \widehat{\text{Oldify}}_{use}(\hat{H}, \hat{C}, \hat{a}_{new}) \\
LP_2 &= \widehat{\mathcal{V}}_{use} \llbracket e \rrbracket (\hat{H}, \hat{C}) \quad // \text{if } e \text{ is None, } LP_2 \text{ is an empty set.} \\
LP_3 &= \widehat{\text{VarStore}}_{use}(\hat{H}, \hat{C}.1, x) \\
LP_4 &= \widehat{\text{RaiseException}}_{use}(\hat{e}s)
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{def} \llbracket x := \text{allocArray}(n) \hat{a}_{new} \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \\
\text{where } \hat{l}_R &= (\hat{a}_{new}, \text{Recent}) \\
LP_1 &= \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_{new}) \\
LP_2 &= \left\{ \langle \hat{l}_R, s \rangle \mid s \in \widehat{\text{NewArrayObject}}_{def}() \right\} \\
LP_3 &= \widehat{\text{VarStore}}_{def}(\hat{H}, \hat{C}.1, x) \\
\\
\hat{\mathcal{I}}_{use} \llbracket x := \text{allocArray}(n) \hat{a}_{new} \rrbracket (\hat{H}, \hat{C}) &= \left\{ \langle \#Context, 1 \rangle \right\} \cup LP_1 \cup LP_2 \\
\text{where } LP_1 &= \widehat{\text{Oldify}}_{use}(\hat{H}, \hat{C}, \hat{a}_{new}) \\
LP_2 &= \widehat{\text{VarStore}}_{use}(\hat{H}, \hat{C}.1, x) \\
\\
\hat{\mathcal{I}}_{def} \llbracket x := \text{allocArg}(n) \hat{a}_{new} \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \\
\text{where } \hat{l}_R &= (\hat{a}_{new}, \text{Recent}) \\
LP_1 &= \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_{new}) \\
LP_2 &= \left\{ \langle \hat{l}_R, s \rangle \mid s \in \widehat{\text{NewArgObject}}_{def}() \right\} \\
LP_3 &= \widehat{\text{VarStore}}_{def}(\hat{H}, \hat{C}.1, x) \\
\\
\hat{\mathcal{I}}_{use} \llbracket x := \text{allocArg}(n) \hat{a}_{new} \rrbracket (\hat{H}, \hat{C}) &= \left\{ \langle \#Context, 1 \rangle \right\} \cup LP_1 \cup LP_2 \\
\text{where } LP_1 &= \widehat{\text{Oldify}}_{use}(\hat{H}, \hat{C}, \hat{a}_{new}) \\
LP_2 &= \widehat{\text{VarStore}}_{use}(\hat{H}, \hat{C}.1, x) \\
\\
\hat{\mathcal{I}}_{def} \llbracket x := e \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\text{where } (\hat{v}, \hat{e}s) &= \hat{\mathcal{V}} \llbracket e \rrbracket (\hat{H}, \hat{C}) \\
LP_1 &= \widehat{\text{VarStore}}_{def}(\hat{H}, \hat{H}(\#PureLocal_R)(@env).1.2.2, x) \\
LP_2 &= \widehat{\text{RaiseException}}_{def}(\hat{e}s) \\
\\
\hat{\mathcal{I}}_{use} \llbracket x := e \rrbracket (\hat{H}, \hat{C}) &= \left\{ \langle \#PureLocal_R, @env \rangle \right\} \cup LP_1 \cup LP_2 \cup LP_3 \\
\text{where } (\hat{v}, \hat{e}s) &= \hat{\mathcal{V}} \llbracket e \rrbracket (\hat{H}, \hat{C}) \\
LP_1 &= \widehat{\text{VarStore}}_{use}(\hat{H}, \hat{H}(\#PureLocal_R)(@env).1.2.2, x) \\
LP_2 &= \hat{\mathcal{V}}_{use} \llbracket e \rrbracket (\hat{H}, \hat{C}) \\
LP_3 &= \widehat{\text{RaiseException}}_{use}(\hat{e}s)
\end{aligned}$$

$$\hat{\mathcal{I}}_{def} \llbracket x_1 := \text{delete } (x_2) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2$$

$$\text{where } \hat{L}_{base} = \widehat{\text{LookupBase}}(\hat{H}, \hat{C}.1, x_2)$$

$$LP_1 = \widehat{\text{VarStore}}_{def}(\hat{H}, \hat{C}.1, x_1)$$

$$LP_2 = \bigcup_{\hat{l}_{base} \in \hat{L}_{base}} \widehat{\text{Delete}}_{def}(\hat{H}, \hat{l}_{base}, \hat{x}_2)$$

$$\hat{\mathcal{I}}_{use} \llbracket x_1 := \text{delete } (x_2) \rrbracket (\hat{H}, \hat{C}) = \{ \langle \#Context, 1 \rangle \} \cup LP_1 \cup LP_2 \cup LP_3$$

$$\text{where } \hat{L}_{base} = \widehat{\text{LookupBase}}(\hat{H}, \hat{C}.1, x_2)$$

$$LP_1 = \widehat{\text{VarStore}}_{use}(\hat{H}, \hat{C}.1, x_1)$$

$$LP_2 = \widehat{\text{LookupBase}}_{use}(\hat{H}, \hat{C}.1, x_2)$$

$$LP_3 = \bigcup_{\hat{l}_{base} \in \hat{L}_{base}} \widehat{\text{Delete}}_{use}(\hat{H}, \hat{l}_{base}, \hat{x}_2)$$

$$\hat{\mathcal{I}}_{def} \llbracket x := \text{delete } (e) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2$$

$$\text{where } (\hat{v}, \hat{es}) = \hat{\mathcal{V}} \llbracket e \rrbracket (\hat{H}, \hat{C})$$

$$LP_1 = \widehat{\text{VarStore}}_{def}(\hat{H}, \hat{C}.1, x)$$

$$LP_2 = \widehat{\text{RaiseException}}_{def}(\hat{es})$$

$$\hat{\mathcal{I}}_{use} \llbracket x := \text{delete } (e) \rrbracket (\hat{H}, \hat{C}) = \{ \langle \#Context, 1 \rangle \} \cup LP_1 \cup LP_2 \cup LP_3$$

$$\text{where } (\hat{v}, \hat{es}) = \hat{\mathcal{V}} \llbracket e \rrbracket (\hat{H}, \hat{C})$$

$$LP_1 = \widehat{\text{VarStore}}_{use}(\hat{H}, \hat{C}.1, x)$$

$$LP_2 = \hat{\mathcal{V}}_{use} \llbracket e \rrbracket (\hat{H}, \hat{C})$$

$$LP_3 = \widehat{\text{RaiseException}}_{use}(\hat{es})$$

$$\hat{\mathcal{I}}_{def} \llbracket x := \text{delete } (e_1, e_2) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

$$\text{where } \hat{L} = (\hat{\mathcal{V}} \llbracket e_1 \rrbracket (\hat{H}, \hat{C})).1.2 \wedge (\hat{v}, \hat{es}) = \hat{\mathcal{V}} \llbracket e_2 \rrbracket (\hat{H}, \hat{C})$$

$$\hat{s}s = \widehat{\text{toStringSet}}(\widehat{\text{toPrimitive}}(\hat{v}))$$

$$LP_1 = \widehat{\text{VarStore}}_{def}(\hat{H}, \hat{C}.1, x)$$

$$LP_2 = \bigcup_{\hat{l} \in \hat{L}} \bigcup_{\hat{s} \in \hat{s}s} \widehat{\text{Delete}}_{def}(\hat{H}, \hat{l}, \hat{s})$$

$$LP_3 = \widehat{\text{RaiseException}}_{def}(\hat{es})$$

$$\hat{\mathcal{I}}_{use} \llbracket x := \text{delete } (e_1, e_2) \rrbracket (\hat{H}, \hat{C}) = \{ \langle \#Context, 1 \rangle \} \cup LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5$$

$$\text{where } \hat{L} = (\hat{\mathcal{V}} \llbracket e_1 \rrbracket (\hat{H}, \hat{C})).1.2 \wedge (\hat{v}, \hat{es}) = \hat{\mathcal{V}} \llbracket e_2 \rrbracket (\hat{H}, \hat{C})$$

$$\hat{s}s = \widehat{\text{toStringSet}}(\widehat{\text{toPrimitive}}(\hat{v}))$$

$$LP_1 = \widehat{\text{VarStore}}_{use}(\hat{H}, \hat{C}.1, x)$$

$$LP_2 = \hat{\mathcal{V}}_{use} \llbracket e_1 \rrbracket (\hat{H}, \hat{C})$$

$$LP_3 = \hat{\mathcal{V}}_{use} \llbracket e_2 \rrbracket (\hat{H}, \hat{C})$$

$$LP_4 = \bigcup_{\hat{l} \in \hat{L}} \bigcup_{\hat{s} \in \hat{s}s} \widehat{\text{Delete}}_{use}(\hat{H}, \hat{l}, \hat{s})$$

$$LP_5 = \widehat{\text{RaiseException}}_{use}(\hat{es})$$

$$\hat{\mathcal{I}}_{use} \llbracket x := \text{delete } (e_1, e_2) \rrbracket (\hat{H}, \hat{C}) = \{ \langle \#Context, 1 \rangle \} \cup LP_1 \cup LP_2 \cup LP_3 \cup LP_4$$

$$\text{where } \hat{L} = (\hat{\mathcal{V}} \llbracket e_1 \rrbracket (\hat{H}, \hat{C})).1.2 \wedge \hat{s} = (\hat{\mathcal{V}} \llbracket e_2 \rrbracket (\hat{H}, \hat{C})).1.1.5$$

$$LP_1 = \widehat{\text{VarStore}}_{use}(\hat{H}, \hat{C}.1, x)$$

$$LP_2 = \hat{\mathcal{V}}_{use} \llbracket e_1 \rrbracket (\hat{H}, \hat{C})$$

$$LP_3 = \hat{\mathcal{V}}_{use} \llbracket e_2 \rrbracket (\hat{H}, \hat{C})$$

$$LP_4 = \bigcup_{\hat{l} \in \hat{L}} \widehat{\text{Delete}}_{use}(\hat{H}, \hat{l}, \hat{s})$$

$$\begin{aligned}
& \hat{\mathcal{L}}_{def} \llbracket e_1 [e_2] = e_3 \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_{ex} \\
& \text{where } \hat{L} = (\hat{\mathcal{V}} \llbracket e_1 \rrbracket (\hat{H}, \hat{C})).1.2 \\
& (\hat{v}_{index}, \hat{es}_{index}) = (\hat{\mathcal{V}} \llbracket e_2 \rrbracket (\hat{H}, \hat{C})) \\
& (\hat{v}_{rhs}, \hat{es}_{rhs}) = \hat{\mathcal{V}} \llbracket e_3 \rrbracket (\hat{H}, \hat{C}) \\
& LP_{ex} = \widehat{\text{RaiseException}}_{def}(\hat{es}_1) \\
& (LP_1, \hat{es}_1) = \begin{cases} (\{\}, \hat{es}_{index}) & \text{if } \hat{v}_{index} \sqsubseteq \perp_{Value} \\ (LP_2, \hat{es}_2) & \text{otherwise} \end{cases} \\
& (LP_2, \hat{es}_2) = \begin{cases} (\{\}, \hat{es}_{index} \cup \hat{es}_{rhs}) & \text{if } \hat{v}_{rhs} \sqsubseteq \perp_{Value} \\ (LP_3, \hat{es}_3 \cup \hat{es}_{index} \cup \hat{es}_{rhs}) & \text{otherwise} \end{cases} \\
& \hat{S} = \widehat{\text{toStringSet}}(\widehat{\text{toPrimitive}}(\hat{v}_{index})) \\
& (LP_3, \hat{es}_3) = \bigcup_{\hat{s} \in \hat{S}} (LP_{N\text{Arr}} \cup LP_{Arr}, \hat{es}_{Arr}) \\
& \hat{L}_{N\text{Arr}} = \left\{ \hat{l} \mid \hat{l} \in \hat{L} \wedge \text{false} \sqsubseteq \widehat{\text{IsArray}}(\hat{H}, \hat{l}) \wedge \text{true} \sqsubseteq \widehat{\text{CanPut}}(\hat{H}, \hat{l}, \hat{s}) \right\} \\
& \hat{L}_{Arr} = \left\{ \hat{l} \mid \hat{l} \in \hat{L} \wedge \text{true} \sqsubseteq \widehat{\text{IsArray}}(\hat{H}, \hat{l}) \wedge \text{true} \sqsubseteq \widehat{\text{CanPut}}(\hat{H}, \hat{l}, \hat{s}) \right\} \\
& LP_{N\text{Arr}} = \bigcup_{\hat{l} \in \hat{L}_{N\text{Arr}}} \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \hat{s}) \\
& (LP_{Arr}, \hat{es}_{Arr}) = \bigcup_{\hat{l} \in \hat{L}} (LP_{length} \cup LP_{index} \cup LP_{normal}, \hat{es}_{len}) \\
& (LP_{length}, \hat{es}_{len}) = \begin{cases} (LP_{length_2}, \hat{es}_{len_2}) & \text{if } \text{"length"} \sqsubseteq \hat{s} \\ (\{\}, \{\}) & \text{otherwise} \end{cases} \\
& LP_{len_2} = \begin{cases} LP_{len_3} \cup LP_{len_4} & \text{if } \text{true} \sqsubseteq \hat{v}_{value} \hat{=} \hat{v}_{newLen}.1.4 \\ \{\} & \text{otherwise} \end{cases} \\
& \hat{es}_{len_2} = \begin{cases} \{\widehat{\text{RangeError}}\} & \text{if } \text{false} \sqsubseteq \hat{v}_{value} \hat{=} \hat{v}_{newLen}.1.4 \\ \{\} & \text{otherwise} \end{cases} \\
& LP_{len_3} = \begin{cases} \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \text{"length"}) & \text{if } \text{true} \sqsubseteq \hat{v}_{value} \hat{\leq} \hat{v}_{newLen}.1.4 \wedge \text{true} \sqsubseteq \widehat{\text{CanPut}}(\hat{H}, \hat{l}, \text{"length"}) \\ \{\} & \text{otherwise} \end{cases} \\
& LP_{len_4} = \begin{cases} \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \text{"length"}) \cup \bigcup_{x=\hat{v}_{oldLen}-1 \text{ to } \hat{v}_{newLen}} \widehat{\text{Delete}}(\hat{H}, \hat{l}, x) & \text{if } \text{false} \sqsubseteq \hat{v}_{value} \hat{=} \hat{v}_{newLen}.1.4 \wedge \text{true} \sqsubseteq \widehat{\text{CanPut}}(\hat{H}, \hat{l}, \text{"length"}) \\ \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \text{"length"}, \hat{v}) & \text{otherwise} \end{cases} \\
& LP_{index} = \begin{cases} LP_{index_1} \cup LP_{index_2} & \text{if } \text{true} \sqsubseteq \widehat{\text{IsArrayIndex}}(\hat{s}) \\ \{\} & \text{otherwise} \end{cases} \\
& LP_{index_1} = \begin{cases} \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \hat{s}) & \text{if } \text{true} \sqsubseteq (\hat{n}_{index} \hat{<} \hat{n}_{oldLen}) \\ \{\} & \text{otherwise} \end{cases} \\
& LP_{index_2} = \begin{cases} \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \hat{s}) \cup \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \text{"length"}) & \text{if } \text{true} \sqsubseteq (\hat{n}_{oldLen} \hat{\leq} \hat{n}_{index}) \wedge \text{true} \sqsubseteq \widehat{\text{CanPut}}(\hat{H}, \hat{l}, \text{"length"}) \\ \{\} & \text{otherwise} \end{cases} \\
& LP_{normal} = \begin{cases} \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \hat{s}) & \text{if } \hat{s} \neq \text{"length"} \wedge \text{false} \sqsubseteq \widehat{\text{IsArrayIndex}}(\hat{s}) \\ \{\} & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{L}}_{use} \llbracket e_1 [e_2] = e_3 \rrbracket (\hat{H}, \hat{C}) = \{ \langle \#Context, 1 \rangle, \langle \#Context, 2 \rangle \} \cup LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5 \cup LP_6 \cup LP_7 \\
& \text{where } \hat{L} = (\hat{\mathcal{V}} \llbracket e_1 \rrbracket (\hat{H}, \hat{C})).1.2 \wedge (\hat{v}_{index}, \hat{es}_{index}) = \hat{\mathcal{V}} \llbracket e_2 \rrbracket (\hat{H}, \hat{C}) \wedge (\hat{v}_{rhs}, \hat{es}_{rhs}) = \hat{\mathcal{V}} \llbracket e_3 \rrbracket (\hat{H}, \hat{C}) \\
& \wedge \hat{S} = \widehat{\text{toStringSet}}(\widehat{\text{toPrimitive}}(\hat{v}_{index})) \wedge \hat{T} = \left\{ \hat{l} \mid \hat{l} \in \hat{L} \wedge \exists \hat{s} \in \hat{S} : \text{true} \sqsubseteq \widehat{\text{CanPut}}(\hat{H}, \hat{l}, \hat{s}) \right\} \\
& LP_1 = \bigcup_{\hat{l} \in \hat{T}} \bigcup_{\hat{s} \in \hat{S}} \widehat{\text{PropStore}}_{use}(\hat{H}, \hat{l}, \hat{s}) \\
& LP_2 = \hat{\mathcal{V}}_{use} \llbracket e_1 \rrbracket (\hat{H}, \hat{C}) \\
& LP_3 = \hat{\mathcal{V}}_{use} \llbracket e_2 \rrbracket (\hat{H}, \hat{C}) \\
& LP_4 = \hat{\mathcal{V}}_{use} \llbracket e_3 \rrbracket (\hat{H}, \hat{C}) \\
& LP_5 = \bigcup_{\hat{l} \in \hat{L}} \bigcup_{\hat{s} \in \hat{S}} \widehat{\text{CanPut}}_{use}(\hat{H}, \hat{l}, \hat{s}) \\
& \hat{n}_{value} = \widehat{\text{ToNumber}}(\widehat{\text{ToPrimitive}}(\hat{v}_{rhs})) \\
& \hat{v}_{newLen} = \widehat{\text{ToUInt32}}(\hat{v}_{rhs}) \\
& \hat{es}_{len} = \begin{cases} \{\widehat{\text{RangeError}}\} & \text{if } \text{false} \sqsubseteq \hat{v}_{value} \hat{=} \hat{v}_{newLen}.1.4 \\ \{\} & \text{otherwise} \end{cases} \\
& LP_6 = \widehat{\text{RaiseException}}_{use}(\hat{es}_{index} \sqcup \hat{es}_{rhs} \sqcup \hat{es}_{len}) \\
& \hat{L}_{N\text{Arr}} = \left\{ \hat{l} \mid \hat{l} \in \hat{L} \wedge \text{false} \sqsubseteq \widehat{\text{IsArray}}(\hat{H}, \hat{l}) \wedge \exists \hat{s} \in \hat{S} : \text{true} \sqsubseteq \widehat{\text{CanPut}}(\hat{H}, \hat{l}, \hat{s}) \right\} \\
& LP_{N\text{Arr}} = \bigcup_{\hat{l} \in \hat{L}_{N\text{Arr}}} \bigcup_{\hat{s} \in \hat{S}} \widehat{\text{PropStore}}_{use}(\hat{H}, \hat{l}, \hat{s}) \\
& \hat{L}_{Arr} = \left\{ \hat{l} \mid \hat{l} \in \hat{L} \wedge \text{true} \sqsubseteq \widehat{\text{IsArray}}(\hat{H}, \hat{l}) \wedge \exists \hat{s} \in \hat{S} : \text{true} \sqsubseteq \widehat{\text{CanPut}}(\hat{H}, \hat{l}, \hat{s}) \right\} \\
& LP_{Arr} = \bigcup_{\hat{l} \in \hat{L}_{N\text{Arr}}} \left( \begin{aligned} & \widehat{\text{PropStore}}_{use}(\hat{H}, \hat{l}, \text{"length"}) \cup \widehat{\text{CanPut}}_{use}(\hat{H}, \hat{l}, \text{"length"}) \\ & \cup \widehat{\text{Delete}}_{use}(\hat{H}, \hat{l}, \text{SFN}\hat{umStr}) \cup \{ \langle \hat{l}, \text{"length"} \rangle \} \\ & \cup \bigcup_{\hat{s} \in \hat{S}} \widehat{\text{PropStore}}_{use}(\hat{H}, \hat{l}, \hat{s}) \end{aligned} \right) \\
& LP_7 = LP_{N\text{Arr}} \cup LP_{Arr}
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{def} \llbracket x_1 := \text{function } (fid) \hat{a}_{new1}, \hat{a}_{new2} \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5 \cup LP_6 \\
\text{where } \hat{l}_{R1} &= (\hat{a}_{new1}, \text{Recent}) \wedge \hat{l}_{R2} = (\hat{a}_{new2}, \text{Recent}) \\
LP_1 &= \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_{new1}) \\
LP_2 &= \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_{new2}) \\
LP_3 &= \left\{ \langle \hat{l}_{R1}, s \rangle \mid s \in \widehat{\text{NewFunctionObject}}_{def}() \right\} \\
LP_4 &= \left\{ \langle \hat{l}_{R2}, s \rangle \mid s \in \widehat{\text{NewObject}}_{def}() \right\} \\
LP_5 &= \left\{ \langle \hat{l}_{R2}, \text{"constructor"} \rangle \right\} \\
LP_6 &= \widehat{\text{VarStore}}_{def}(\hat{H}, \hat{C}.1, x_1)
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use} \llbracket x_1 := \text{function } (fid) \hat{a}_{new1}, \hat{a}_{new2} \rrbracket (\hat{H}, \hat{C}) &= \left\{ \langle \#Context, 1 \rangle \right\} \cup LP_1 \cup LP_2 \cup LP_3 \\
\text{where } LP_1 &= \widehat{\text{Oldify}}_{use}(\hat{H}, \hat{C}, \hat{a}_{new1}) \\
LP_2 &= \widehat{\text{Oldify}}_{use}(\hat{H}, \hat{C}, \hat{a}_{new2}) \\
LP_3 &= \widehat{\text{VarStore}}_{use}(\hat{H}, \hat{C}.1, x_1)
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{def} \llbracket x_1 := \text{function } x_2 (fid) \hat{a}_{new1}, \hat{a}_{new2}, \hat{a}_{new3} \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5 \cup LP_6 \cup LP_7 \cup LP_8 \cup LP_9 \\
\text{where } \hat{l}_{R1} &= (\hat{a}_{new1}, \text{Recent}) \wedge \hat{l}_{R2} = (\hat{a}_{new2}, \text{Recent}) \\
LP_1 &= \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_{new1}) \\
LP_2 &= \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_{new2}) \\
LP_3 &= \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_{new3}) \\
LP_4 &= \left\{ \langle \hat{l}_{R1}, s \rangle \mid s \in \widehat{\text{NewFunctionObject}}_{def}() \right\} \\
LP_5 &= \left\{ \langle \hat{l}_{R2}, s \rangle \mid s \in \widehat{\text{NewObject}}_{def}() \right\} \\
LP_6 &= \left\{ \langle \hat{l}_{R2}, \text{"constructor"} \rangle \right\} \\
LP_7 &= \left\{ \langle \hat{l}_{R3}, s \rangle \mid s \in \widehat{\text{NewDeclEnvRecord}}_{def}() \right\} \\
LP_8 &= \left\{ \langle \hat{l}_{R3}, x_2 \rangle \right\} \\
LP_9 &= \widehat{\text{VarStore}}_{def}(\hat{H}, \hat{C}.1, x_1)
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use} \llbracket x_1 := \text{function } x_2 (fid) \hat{a}_{new1}, \hat{a}_{new2}, \hat{a}_{new3} \rrbracket (\hat{H}, \hat{C}) &= \left\{ \langle \#Context, 1 \rangle \right\} \cup LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\
\text{where } LP_1 &= \widehat{\text{Oldify}}_{use}(\hat{H}, \hat{C}, \hat{a}_{new1}) \\
LP_2 &= \widehat{\text{Oldify}}_{use}(\hat{H}, \hat{C}, \hat{a}_{new2}) \\
LP_3 &= \widehat{\text{Oldify}}_{use}(\hat{H}, \hat{C}, \hat{a}_{new3}) \\
LP_4 &= \widehat{\text{VarStore}}_{use}(\hat{H}, \hat{C}.1, x_1)
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{def} \llbracket \text{construct } (e_1, e_2, e_3) \hat{a}_{new} \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \\
\text{where } (\hat{v}_1, \hat{e}s_1) &= \hat{\mathcal{V}} \llbracket e_1 \rrbracket (\hat{H}, \hat{C}) \\
\hat{v}_{arg} &= \hat{\mathcal{V}} \llbracket e_3 \rrbracket (\hat{H}, \hat{C}).1 \\
\hat{e}s_2 &= \{\text{TypeError}\} \quad \text{if } \exists \hat{l} \in \hat{v}_1.2 : \text{false} \sqsubseteq \widehat{\text{HasConstruct}}(\hat{H}, \hat{l}) \\
\hat{e}s_3 &= \{\text{TypeError}\} \quad \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\
\hat{e}s &= \hat{e}s_1 \sqcup \hat{e}s_2 \sqcup \hat{e}s_3 \\
LP_1 &= \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_{new}) \\
LP_2 &= \left\{ \langle \hat{l}, \text{"callee"} \rangle \mid \hat{l} \in \hat{v}_{arg}.2 \right\} \\
LP_3 &= \widehat{\text{RaiseException}}_{def}(\hat{e}s)
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use} \llbracket \text{construct } (e_1, e_2, e_3) \hat{a}_{new} \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5 \cup LP_6 \cup LP_7 \cup LP_8 \cup LP_9 \cup LP_{10} \\
\text{where } (\hat{v}_1, \hat{e}s_1) &= \hat{\mathcal{V}} \llbracket e_1 \rrbracket (\hat{H}, \hat{C}) \\
\hat{v}_{arg} &= \hat{\mathcal{V}} \llbracket e_3 \rrbracket (\hat{H}, \hat{C}).1 \\
\hat{L}_f &= \left\{ \hat{l} \mid \hat{l} \in \hat{v}_1.2 \wedge \text{true} \sqsubseteq \widehat{\text{HasConstruct}}(\hat{H}_1, \hat{l}) \right\} \\
\hat{e}s_2 &= \{\text{TypeError}\} \quad \text{if } \exists \hat{l} \in \hat{v}_1.2 : \text{false} \sqsubseteq \widehat{\text{HasConstruct}}(\hat{H}, \hat{l}) \\
\hat{e}s_3 &= \{\text{TypeError}\} \quad \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\
\hat{e}s &= \hat{e}s_1 \sqcup \hat{e}s_2 \sqcup \hat{e}s_3 \\
LP_1 &= \widehat{\text{Oldify}}_{use}(\hat{H}, \hat{C}, \hat{a}_{new}) \\
LP_2 &= \hat{\mathcal{V}}_{use} \llbracket e_1 \rrbracket (\hat{H}, \hat{C}) \\
LP_3 &= \hat{\mathcal{V}}_{use} \llbracket e_2 \rrbracket (\hat{H}, \hat{C}) \\
LP_4 &= \hat{\mathcal{V}}_{use} \llbracket e_3 \rrbracket (\hat{H}, \hat{C}) \\
LP_5 &= \bigcup_{\hat{l} \in \hat{v}_1.2} \widehat{\text{HasConstruct}}_{use}(\hat{H}, \hat{l}) \\
LP_6 &= \widehat{\text{getThis}}_{use}(\hat{H}, \hat{\mathcal{V}} \llbracket e_2 \rrbracket (\hat{H}, \hat{C}).1) \\
LP_7 &= \left\{ \langle \hat{l}_f, @construct \rangle \mid \hat{l}_f \in \hat{L}_f \right\} \\
LP_8 &= \left\{ \langle \hat{l}, \text{"callee"} \rangle \mid \hat{l} \in \hat{v}_{arg}.2 \right\} \\
LP_9 &= \widehat{\text{RaiseException}}_{use}(\hat{e}s) \\
LP_{10} &= \left\{ \langle \#PureLocal_R, x \rangle \mid \text{true} \sqsubseteq x \in \text{dom}(\hat{H}(\#PureLocal_R)) \right\}
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{def}[\text{call}(e_1, e_2, e_3) \hat{a}_{new}](\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\text{where } (\hat{v}_1, \hat{e}s_1) &= \hat{\mathcal{V}}[e_1](\hat{H}_1, \hat{C}_1) \\
\hat{v}_{arg} &= \hat{\mathcal{V}}[e_3](\hat{H}, \hat{C}).1 \\
\hat{e}s_2 &= \{\text{TypeError}\} \quad \text{if } \exists \hat{l} \in \hat{v}_1.2 : \text{false} \sqsubseteq \widehat{\text{IsCallable}}(\hat{H}, \hat{l}) \\
\hat{e}s_3 &= \{\text{TypeError}\} \quad \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\
\hat{e}s &= \hat{e}s_1 \sqcup \hat{e}s_2 \sqcup \hat{e}s_3 \\
LP_1 &= \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_{new}) \\
LP_2 &= \{ \langle \hat{l}, \text{"callee"} \rangle \mid \hat{l} \in \hat{v}_{arg}.2 \} \\
LP_3 &= \widehat{\text{RaiseException}}_{def}(\hat{e}s)
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use}[\text{call}(e_1, e_2, e_3) \hat{a}_{new}](\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5 \cup LP_6 \cup LP_7 \cup LP_8 \cup LP_9 \cup LP_{10} \\
\text{where } (\hat{v}_1, \hat{e}s_1) &= \hat{\mathcal{V}}[e_1](\hat{H}_1, \hat{C}_1) \\
\hat{v}_{arg} &= \hat{\mathcal{V}}[e_3](\hat{H}, \hat{C}).1 \\
\hat{L}_f &= \left\{ \hat{l} \mid \hat{l} \in \hat{v}_1.2 \wedge \text{true} \sqsubseteq \widehat{\text{IsCallable}}(\hat{H}_1, \hat{l}) \right\} \\
\hat{e}s_2 &= \{\text{TypeError}\} \quad \text{if } \exists \hat{l} \in \hat{v}_1.2 : \text{false} \sqsubseteq \widehat{\text{IsCallable}}(\hat{H}, \hat{l}) \\
\hat{e}s_3 &= \{\text{TypeError}\} \quad \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\
\hat{e}s &= \hat{e}s_1 \sqcup \hat{e}s_2 \sqcup \hat{e}s_3 \\
LP_1 &= \widehat{\text{Oldify}}_{use}(\hat{H}, \hat{C}, \hat{a}_{new}) \\
LP_2 &= \hat{\mathcal{V}}_{use}[e_1](\hat{H}, \hat{C}) \\
LP_3 &= \hat{\mathcal{V}}_{use}[e_2](\hat{H}, \hat{C}) \\
LP_4 &= \hat{\mathcal{V}}_{use}[e_3](\hat{H}, \hat{C}) \\
LP_5 &= \bigcup_{\hat{l} \in \hat{v}_1.2} \widehat{\text{IsCallable}}_{use}(\hat{H}, \hat{l}) \\
LP_6 &= \widehat{\text{getThis}}_{use}(\hat{H}, \hat{\mathcal{V}}[e_2](\hat{H}, \hat{C}).1) \\
LP_7 &= \{ \langle \hat{l}_f, @function \rangle \mid \hat{l}_f \in \hat{L}_f \} \\
LP_8 &= \{ \langle \hat{l}, \text{"callee"} \rangle \mid \hat{l} \in \hat{v}_{arg}.2 \} \\
LP_9 &= \widehat{\text{RaiseException}}_{use}(\hat{e}s) \\
LP_{10} &= \{ \langle \#PureLocal_R, x \rangle \mid \text{true} \sqsubseteq x \in \text{dom}(\hat{H}(\#PureLocal_R)) \}
\end{aligned}$$

$$\hat{\mathcal{I}}_{def}[\text{assert}(e_1 \otimes e_2)](\hat{H}, \hat{C}) = \hat{\mathcal{V}}_{use}[e_1](\hat{H}, \hat{C}) \cup \hat{\mathcal{V}}_{use}[e_2](\hat{H}, \hat{C})$$

$$\hat{\mathcal{I}}_{use}[\text{assert}(e_1 \otimes e_2)](\hat{H}, \hat{C}) = \hat{\mathcal{V}}_{use}[e_1](\hat{H}, \hat{C}) \cup \hat{\mathcal{V}}_{use}[e_2](\hat{H}, \hat{C})$$

$$\begin{aligned}
\hat{\mathcal{I}}_{def}[\text{catch}(x)](\hat{H}, \hat{C}) &= \{ \langle \#PureLocal_R, @exception \rangle \} \cup LP \\
\text{where } LP &= \widehat{\text{CreateMutableBinding}}_{def}(\hat{H}, \hat{C}.1, x)
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use}[\text{catch}(x)](\hat{H}, \hat{C}) &= \{ \langle \#Context, 1 \rangle \} \cup LP_1 \cup LP_2 \\
\text{where } LP_1 &= \widehat{\text{CreateMutableBinding}}_{use}(\hat{H}, \hat{C}.1, x) \\
LP_2 &= \{ \langle \#PureLocal_R, @exception\_all \rangle, \langle \#PureLocal_R, @exception \rangle \}
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{def}[\text{return}(e)](\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\text{where } (\hat{v}, \hat{e}s) &= \hat{\mathcal{V}}[e](\hat{H}, \hat{C}) \\
LP_1 &= \{ \langle \#PureLocal_R, @return \rangle \} \\
LP_2 &= \widehat{\text{RaiseException}}_{def}(\hat{e}s)
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use}[\text{return}(e)](\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\text{where } (\hat{v}, \hat{e}s) &= \hat{\mathcal{V}}[e](\hat{H}, \hat{C}) \\
LP_1 &= \hat{\mathcal{V}}_{use}[e](\hat{H}, \hat{C}) \\
LP_2 &= \widehat{\text{RaiseException}}_{use}(\hat{e}s)
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{def}[\text{return}()](\hat{H}, \hat{C}) &= LP \\
\text{where } LP &= \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\hat{\mathcal{I}}_{use}[\text{return}()](\hat{H}, \hat{C}) = \{\}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{def}[\text{throw}(e)](\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\text{where } (\hat{v}, \hat{e}s) &= \hat{\mathcal{V}}[e](\hat{H}, \hat{C}) \\
LP_1 &= \{ \langle \#PureLocal_R, @exception \rangle, \langle \#PureLocal_R, @exception\_all \rangle \} \\
LP_2 &= \widehat{\text{RaiseException}}_{def}(\hat{e}s)
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use}[\text{throw}(e)](\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \quad 110 \\
\text{where } (\hat{v}, \hat{e}s) &= \hat{\mathcal{V}}[e](\hat{H}, \hat{C}) \\
LP_1 &= \hat{\mathcal{V}}_{use}[e](\hat{H}, \hat{C}) \\
LP_2 &= \{ \langle \#PureLocal_R, @exception\_all \rangle \} \\
LP_3 &= \widehat{\text{RaiseException}}_{use}(\hat{e}s)
\end{aligned}$$

$$\begin{aligned}\hat{I}_{def} \llbracket x := \widehat{\text{toObject}}(e)_{a_{new}} \rrbracket(\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \\ \text{where } (\hat{v}, \hat{es}) &= \hat{V} \llbracket e \rrbracket(\hat{H}, \hat{C}) \\ LP_1 &= \widehat{\text{VarStore}}_{def}(\hat{H}, \hat{C}.1, x) \\ LP_2 &= \widehat{\text{toObject}}_{def}(\hat{H}, \hat{C}, \hat{v}, \hat{a}_{new}) \\ LP_3 &= \widehat{\text{RaiseException}}_{def}(\hat{es})\end{aligned}$$

$$\begin{aligned}\hat{I}_{use} \llbracket x := \widehat{\text{toObject}}(e)_{a_{new}} \rrbracket(\hat{H}, \hat{C}) &= \{ \langle \#Context, 1 \rangle \} \cup LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\ \text{where } (\hat{v}, \hat{es}) &= \hat{V} \llbracket e \rrbracket(\hat{H}, \hat{C}) \\ LP_1 &= \hat{V}_{use} \llbracket e \rrbracket(\hat{H}, \hat{C}) \\ LP_2 &= \widehat{\text{VarStore}}_{use}(\hat{H}, \hat{C}.1, x) \\ LP_3 &= \widehat{\text{toObject}}_{use}(\hat{H}, \hat{C}, \hat{v}, \hat{a}_{new}) \\ LP_4 &= \widehat{\text{RaiseException}}_{use}(\hat{es})\end{aligned}$$

$$\begin{aligned}\hat{I}_{def} \llbracket x := \widehat{\text{isObject}}(e) \rrbracket(\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\ \text{where } (\hat{v}, \hat{es}) &= \hat{V} \llbracket e \rrbracket(\hat{H}, \hat{C}) \\ LP_1 &= \widehat{\text{VarStore}}_{def}(\hat{H}, \hat{C}.1, x) \\ LP_2 &= \widehat{\text{RaiseException}}_{def}(\hat{es})\end{aligned}$$

$$\begin{aligned}\hat{I}_{use} \llbracket x := \widehat{\text{isObject}}(e) \rrbracket(\hat{H}, \hat{C}) &= \{ \langle \#Context, 1 \rangle \} \cup LP_1 \cup LP_2 \cup LP_3 \\ \text{where } (\hat{v}, \hat{es}) &= \hat{V} \llbracket e \rrbracket(\hat{H}, \hat{C}) \\ LP_1 &= \hat{V}_{use} \llbracket e \rrbracket(\hat{H}, \hat{C}) \\ LP_2 &= \widehat{\text{VarStore}}_{use}(\hat{H}, \hat{C}.1, x) \\ LP_3 &= \widehat{\text{RaiseException}}_{use}(\hat{es})\end{aligned}$$

$$\begin{aligned}\hat{I}_{def} \llbracket x := \widehat{\text{toString}}(e) \rrbracket(\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\ \text{where } (\hat{v}, \hat{es}) &= \hat{V} \llbracket e \rrbracket(\hat{H}, \hat{C}) \\ LP_1 &= \widehat{\text{VarStore}}_{def}(\hat{H}, \hat{C}.1, x) \\ LP_2 &= \widehat{\text{RaiseException}}_{def}(\hat{es})\end{aligned}$$

$$\begin{aligned}\hat{I}_{use} \llbracket x := \widehat{\text{toString}}(e) \rrbracket(\hat{H}, \hat{C}) &= \{ \langle \#Context, 1 \rangle \} \cup LP_1 \cup LP_2 \cup LP_3 \\ \text{where } (\hat{v}, \hat{es}) &= \hat{V} \llbracket e \rrbracket(\hat{H}, \hat{C}) \\ LP_1 &= \hat{V}_{use} \llbracket e \rrbracket(\hat{H}, \hat{C}) \\ LP_2 &= \widehat{\text{VarStore}}_{use}(\hat{H}, \hat{C}.1, x) \\ LP_3 &= \widehat{\text{RaiseException}}_{use}(\hat{es})\end{aligned}$$

$$\begin{aligned}\hat{I}_{def} \llbracket x := \widehat{\text{toNumber}}(e) \rrbracket(\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\ \text{where } LP_1 &= \widehat{\text{VarStore}}_{def}(\hat{H}, \hat{C}.1, x) \\ LP_2 &= \widehat{\text{RaiseException}}_{def}(\hat{es})\end{aligned}$$

$$\begin{aligned}\hat{I}_{use} \llbracket x := \widehat{\text{toNumber}}(e) \rrbracket(\hat{H}, \hat{C}) &= \{ \langle \#Context, 1 \rangle \} \cup LP_1 \cup LP_2 \cup LP_3 \\ \text{where } (\hat{v}, \hat{es}) &= \hat{V} \llbracket e \rrbracket(\hat{H}, \hat{C}) \\ LP_1 &= \hat{V}_{use} \llbracket e \rrbracket(\hat{H}, \hat{C}) \\ LP_2 &= \widehat{\text{VarStore}}_{use}(\hat{H}, \hat{C}.1, x) \\ LP_3 &= \widehat{\text{RaiseException}}_{use}(\hat{es})\end{aligned}$$

$$\begin{aligned}\hat{I}_{def} \llbracket x_1 := \widehat{\text{getBase}}(x_2) \rrbracket(\hat{H}, \hat{C}) &= LP \\ \text{where } LP &= \widehat{\text{VarStore}}_{def}(\hat{H}, \hat{C}.1, x_1)\end{aligned}$$

$$\begin{aligned}\hat{I}_{use} \llbracket x_1 := \widehat{\text{getBase}}(x_2) \rrbracket(\hat{H}, \hat{C}) &= \{ \langle \#Context, 1 \rangle \} \cup LP_1 \cup LP_2 \\ \text{where } LP_1 &= \widehat{\text{VarStore}}_{use}(\hat{H}, \hat{C}.1, x_1) \\ LP_2 &= \widehat{\text{LookupBase}}_{use}(\hat{H}, \hat{C}.1, x_2)\end{aligned}$$

$$\hat{I}_{def} \llbracket x := \widehat{\text{iteratorInit}}(e) \rrbracket(\hat{H}, \hat{C}) = \{ \}$$

$$\hat{I}_{use} \llbracket x := \widehat{\text{iteratorInit}}(e) \rrbracket(\hat{H}, \hat{C}) = \{ \}$$



$$\hat{\mathcal{I}}_{def} \llbracket x := \widehat{\text{iteratorHasNext}}(e_1, e_2) \rrbracket(\hat{H}, \hat{C}) = LP$$

where  $LP = \widehat{\text{VarStore}}_{def}(\hat{H}, \hat{C}.1, x)$

$$\hat{\mathcal{I}}_{use} \llbracket x := \widehat{\text{iteratorHasNext}}(e_1, e_2) \rrbracket(\hat{H}, \hat{C}) = \{ \langle \#Context, 1 \rangle \} \cup LP$$

where  $LP = \widehat{\text{VarStore}}_{use}(\hat{H}, \hat{C}.1, x)$

$$\hat{\mathcal{I}}_{def} \llbracket x := \widehat{\text{iteratorNext}}(e_1, e_2) \rrbracket(\hat{H}, \hat{C}) = LP$$

where  $LP = \widehat{\text{VarStore}}_{def}(\hat{H}, \hat{C}.1, x)$

$$\hat{\mathcal{I}}_{use} \llbracket x := \widehat{\text{iteratorNext}}(e_1, e_2) \rrbracket(\hat{H}, \hat{C}) = \{ \langle \#Context, 1 \rangle \} \cup LP$$

where  $LP = \widehat{\text{VarStore}}_{use}(\hat{H}, \hat{C}.1, x)$

$$\hat{\mathcal{V}}_{use} \llbracket x \rrbracket(\hat{H}, \hat{C}) = \{ \langle \#Context, 1 \rangle \} \cup \widehat{\text{Lookup}}_{use}(\hat{H}, \hat{C}.1, x)$$

$$\hat{\mathcal{V}}_{use} \llbracket e_1 \otimes e_2 \rrbracket(\hat{H}, \hat{C}) = \hat{\mathcal{V}}_{use} \llbracket e_1 \rrbracket(\hat{H}, \hat{C}) \cup \hat{\mathcal{V}}_{use} \llbracket e_2 \rrbracket(\hat{H}, \hat{C})$$

$$\hat{\mathcal{V}}_{use} \llbracket \ominus e \rrbracket(\hat{H}, \hat{C}) = \hat{\mathcal{V}}_{use} \llbracket e \rrbracket(\hat{H}, \hat{C})$$

$$\hat{\mathcal{V}}_{use} \llbracket e_1 [e_2] \rrbracket(\hat{H}, \hat{C}) = \hat{\mathcal{V}}_{use} \llbracket e_1 \rrbracket(\hat{H}, \hat{C}) \cup \hat{\mathcal{V}}_{use} \llbracket e_2 \rrbracket(\hat{H}, \hat{C}) \cup LP$$

where  $\hat{L} = (\hat{\mathcal{V}} \llbracket e_1 \rrbracket(\hat{H}, \hat{C})).1.2 \wedge (\hat{v}, \hat{e}s) = \hat{\mathcal{V}} \llbracket e_2 \rrbracket(\hat{H}, \hat{C})$   
 $\hat{s}s = \widehat{\text{toStringSet}}(\widehat{\text{toPrimitive}}(\hat{v}))$   
 $LP = \bigcup_{\hat{l} \in \hat{L}} \bigcup_{\hat{s} \in \hat{s}s} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \hat{s})$

$$\hat{\mathcal{V}}_{use} \llbracket e_1 \text{ instanceof } e_2 \rrbracket(\hat{H}, \hat{C}) = \hat{\mathcal{V}}_{use} \llbracket e_1 \rrbracket(\hat{H}, \hat{C}) \cup \hat{\mathcal{V}}_{use} \llbracket e_2 \rrbracket(\hat{H}, \hat{C}) \cup LP_1 \cup LP_2 \cup LP_3$$

where  $(\hat{v}_1, \hat{e}s_1) = \hat{\mathcal{V}} \llbracket e_1 \rrbracket(\hat{H}, \hat{C}) \wedge (\hat{v}_2, \hat{e}s_2) = \hat{\mathcal{V}} \llbracket e_2 \rrbracket(\hat{H}, \hat{C})$   
 $\hat{L}_1 = \hat{v}_1.2 \wedge \hat{L}_2 = \hat{v}_2.2$   
 $\hat{L}_3 = \{ \hat{l} \mid \hat{l} \in \hat{L}_2 \wedge \text{true} \sqsubseteq \widehat{\text{HasConstruct}}(\hat{H}, \hat{l}) \}$   
 $\hat{L}_4 = \hat{v}_{proto}.2$   
 $\hat{v}_{proto} = \bigsqcup_{\hat{l} \in \hat{L}_3} \widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"prototype"})$   
 $LP_1 = \bigcup_{\hat{l} \in \hat{L}_2} \{ \hat{l}, @construct \}$   
 $LP_2 = \bigcup_{\hat{l} \in \hat{L}_3} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{"prototype"})$   
 $LP_3 = \bigcup_{\hat{l}_1 \in \hat{L}_1} \bigcup_{\hat{l}_2 \in \hat{L}_4} \widehat{\text{inherit}}_{use}(\hat{H}, \hat{l}_1, \hat{l}_2)$

$$\hat{\mathcal{V}}_{use} \llbracket e_1 \text{ in } e_2 \rrbracket(\hat{H}, \hat{C}) = \hat{\mathcal{V}}_{use} \llbracket e_1 \rrbracket(\hat{H}, \hat{C}) \cup \hat{\mathcal{V}}_{use} \llbracket e_2 \rrbracket(\hat{H}, \hat{C}) \cup LP$$

where  $(\hat{v}_1, \hat{e}s_1) = \hat{\mathcal{V}} \llbracket e_1 \rrbracket(\hat{H}, \hat{C})$   
 $(\hat{v}_2, \hat{e}s_2) = \hat{\mathcal{V}} \llbracket e_2 \rrbracket(\hat{H}, \hat{C})$   
 $\hat{s} = \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\hat{v}_1))$   
 $LP = \bigcup_{\hat{l} \in \hat{v}_2.2} \widehat{\text{HasProperty}}_{use}(\hat{H}, \hat{l}, \hat{s})$

$$\hat{\mathcal{V}}_{use} \llbracket \text{typeof } e \rrbracket(\hat{H}, \hat{C}) = \hat{\mathcal{V}}_{use} \llbracket e \rrbracket(\hat{H}, \hat{C}) \cup LP$$

where  $(\hat{v}, \hat{e}s) = \hat{\mathcal{V}} \llbracket e \rrbracket(\hat{H}, \hat{C})$   
 $LP = \widehat{\text{TypeTag}}_{use}(\hat{H}, \hat{v})$

# Chapter 11

## Built-in Objects

### 11.1 Concrete Semantics

#### 11.1.1 Helper Functions

getMatcher :  $\text{MatcherId} \rightarrow (\text{String} \times \text{Int} \rightarrow \text{MatchResult})$

NewRegExp :  $\text{Value} \times \text{Bool} \times \text{Bool} \times \text{Bool} \times \text{MatcherId} \rightarrow \text{Obj}$

$$\text{NewRegExp}(v_{\text{source}}, b_g, b_i, b_m, \text{mid}) = \left\{ \begin{array}{l} \text{@class} \mapsto \text{"RegExp"}, \\ \text{@proto} \mapsto \left\{ \begin{array}{l} \text{value} = \# \text{RegExpProto}; \\ \text{writable} = \text{false}; \\ \text{enumerable} = \text{false}; \\ \text{configurable} = \text{false} \end{array} \right\}, \\ \text{@matcher} \mapsto \text{mid}, \\ \text{"source"} \mapsto \left\{ \begin{array}{l} \text{value} = v_{\text{source}}; \\ \text{writable} = \text{false}; \\ \text{enumerable} = \text{false}; \\ \text{configurable} = \text{false} \end{array} \right\}, \\ \text{"global"} \mapsto \left\{ \begin{array}{l} \text{value} = b_g; \\ \text{writable} = \text{false}; \\ \text{enumerable} = \text{false}; \\ \text{configurable} = \text{false} \end{array} \right\}, \\ \text{"ignoreCase"} \mapsto \left\{ \begin{array}{l} \text{value} = b_i; \\ \text{writable} = \text{false}; \\ \text{enumerable} = \text{false}; \\ \text{configurable} = \text{false} \end{array} \right\}, \\ \text{"multiline"} \mapsto \left\{ \begin{array}{l} \text{value} = b_m; \\ \text{writable} = \text{false}; \\ \text{enumerable} = \text{false}; \\ \text{configurable} = \text{false} \end{array} \right\}, \\ \text{"lastIndex"} \mapsto \left\{ \begin{array}{l} \text{value} = 0; \\ \text{writable} = \text{true}; \\ \text{enumerable} = \text{false}; \\ \text{configurable} = \text{false} \end{array} \right\} \end{array} \right\}$$

#### 11.1.2 Global

$\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"isNaN"}, \text{args})]\!](H, A) = (H[\#temp \mapsto H(\#temp)[\text{@return} \mapsto v]], A)$   
 where  $v = \begin{cases} \text{true} & \text{if } \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(\text{args}, \text{"0"}))) = \text{NaN} \\ \text{false} & \text{otherwise} \end{cases}$

$\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"isFinite"}, \text{args})]\!](H, A) = (H[\#temp \mapsto H(\#temp)[\text{@return} \mapsto v]], A)$   
 where  $v = \begin{cases} \text{false} & \text{if } \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(\text{args}, \text{"0"}))) \in \{ \text{NaN}, \text{Inf}, -\text{Inf} \} \\ \text{true} & \text{otherwise} \end{cases}$

### 11.1.3 Object

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Object.constructor"}, args)\!]\!](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\
&\text{where } v = \text{getArgValue}(args, "0") \wedge v \in \mathbf{Loc} \\
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Object.constructor"}, args)\!]\!](H, A) &= (H_1[\#temp \mapsto H(\#temp)[@return \mapsto l]], A) \\
&\text{where } v = \text{getArgValue}(args, "0") \wedge v \in \mathbf{String} \cup \mathbf{Number} \cup \mathbf{Bool} \\
&\quad \wedge l = \text{newLocation}() \wedge o = \text{toObject}(v) \wedge H_1 = H[l \mapsto o] \\
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Object.constructor"}, args)\!]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } v = \text{getArgValue}(args, "0") \wedge v \in \{\mathbf{undefined}, \mathbf{null}\} \\
&\quad \wedge l = \text{newLocation}() \wedge o = \text{NewObject}(\#ObjProto) \wedge H_1 = H[l \mapsto o] \\
\\
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Object.getPrototypeOf"}, args)\!]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \text{getArgValue}(args, "0") \wedge v \notin \mathbf{Loc} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\mathbf{TypeError})] \\
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Object.getPrototypeOf"}, args)\!]\!](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v_2]], A) \\
&\text{where } v_1 = \text{getArgValue}(args, "0") \wedge v_1 \in \mathbf{Loc} \wedge v_2 = H(v)(@proto).value
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.getOwnPropertyDescriptor"}, args)\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \notin \text{Loc} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.getOwnPropertyDescriptor"}, args)\!](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto \text{undefined}]], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \in \text{Loc} \wedge s = \text{toString}(\text{toPrimitive}(\text{getArgValue}(args, \text{"1"}))) \wedge s \notin \text{dom}(H(v)) \\
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.getOwnPropertyDescriptor"}, args)\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \in \text{Loc} \wedge s = \text{toString}(\text{toPrimitive}(\text{getArgValue}(args, \text{"1"}))) \wedge s \in \text{dom}(H(v)) \\
&\quad \wedge l = \text{newLocation}() \wedge o = \text{NewObject}(\#ObjProto) \\
&\quad \wedge o_1 = \begin{cases} o & \left[ \begin{array}{l} \text{value} \mapsto \begin{cases} \text{value} : H(v)(s).\text{value} \\ \text{writable} : \text{true} \\ \text{enumerable} : \text{true} \\ \text{configurable} : \text{true} \end{cases} \\ \text{writable} \mapsto \begin{cases} \text{value} : H(v)(s).\text{writable} \\ \text{writable} : \text{true} \\ \text{enumerable} : \text{true} \\ \text{configurable} : \text{true} \end{cases} \end{array} \right] & \text{if } \text{IsDataDescriptor}(H(v), s) \\ o & \text{otherwise} \end{cases} \\
&\quad \wedge o_2 = o_1 \begin{cases} \text{enumerable} \mapsto \begin{cases} \text{value} : H(v)(s).\text{enumerable}, & \text{writable} : \text{true} \\ \text{enumerable} : \text{true}, & \text{configurable} : \text{true} \end{cases} \\ \text{configurable} \mapsto \begin{cases} \text{value} : H(v)(s).\text{configurable}, & \text{writable} : \text{true} \\ \text{enumerable} : \text{true}, & \text{configurable} : \text{true} \end{cases} \end{cases} \\
&\quad \wedge H_1 = H[l \mapsto o_2] \\
\\
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.getOwnPropertyNames"}, args)\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \notin \text{Loc} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.getOwnPropertyNames"}, args)\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \in \text{Loc} \\
&\quad \wedge l = \text{newLocation}() \wedge o = \text{NewArrayObject}(0) \wedge n = 0 \\
&\quad \wedge o_1 = o \left[ \forall s \in \text{dom}(H(v)) : \text{toString}(n^{++}) \mapsto \begin{cases} \text{value} : s \\ \text{writable} : \text{true} \\ \text{enumerable} : \text{true} \\ \text{configurable} : \text{true} \end{cases} \right] \\
&\quad \wedge H_1 = H[l \mapsto o_1] \\
\\
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.create"}, args)\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge (v \notin \text{Loc} \vee v \in \{\text{null}\}) \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.create"}, args)\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \in \text{Loc} \wedge |args| = 1 \\
&\quad \wedge l = \text{newLocation}() \wedge o = \text{NewObject}(v) \wedge H_1 = H[l \mapsto o_1] \\
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.create"}, args)\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } v_1 = \text{getArgValue}(args, \text{"0"}) \wedge v \in \text{Loc} \wedge |args| > 1 \wedge v_2 = \text{getArgValue}(args, \text{"1"}) \\
&\quad \wedge l = \text{newLocation}() \wedge o = \text{NewObject}(v_1) \\
&\quad \wedge o_1 = \begin{cases} o & \left[ \forall x \in \text{dom}(H(v_2)) : x \mapsto \begin{cases} \text{value} : H(v_2)(x)(\text{"value"}) \\ \text{writable} : H(v_2)(x)(\text{"writable"}) \\ \text{enumerable} : H(v_2)(x)(\text{"enumerable"}) \\ \text{configurable} : H(v_2)(x)(\text{"configurable"}) \end{cases} \right] & v_2 = \text{undefined} \\ o & \text{otherwise} \end{cases} \\
&\quad \wedge H_1 = H[l \mapsto o_1]
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.defineProperty"}, args)\!]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \text{getArgValue}(args, "0") \wedge v \notin \text{Loc} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.defineProperty"}, args)\!]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v_1 = \text{getArgValue}(args, "0") \wedge v_1 \in \text{Loc} \wedge v_2 = \text{getArgValue}(args, "2") \wedge v_2 \notin \text{Loc} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.defineProperty"}, args)\!]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v_1]], A) \\
&\text{where } v_1 = \text{getArgValue}(args, "0") \wedge v_1 \in \text{Loc} \wedge v_2 = \text{getArgValue}(args, "2") \wedge v_2 \in \text{Loc} \\
&\quad \wedge s = \text{toString}(\text{getArgValue}(args, "1")) \\
&\quad \wedge o = H(v_1) \left[ s \mapsto \left\{ \begin{array}{l} \text{value} : \text{Proto}(H, v_2, \text{"value"}) \\ \text{writable} : \text{Proto}(H, v_2, \text{"writable"}) \\ \text{enumerable} : \text{Proto}(H, v_2, \text{"enumerable"}) \\ \text{configurable} : \text{Proto}(H, v_2, \text{"configurable"}) \end{array} \right\} \right] \\
&\quad \wedge H_1 = H[l \mapsto o]
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.defineProperties"}, args)\!]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \text{getArgValue}(args, "0") \wedge v \notin \text{Loc} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.defineProperties"}, args)\!]\!](H, A) &= (H_2[\#temp \mapsto H_2(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v_1 = \text{getArgValue}(args, "0") \wedge v_1 \in \text{Loc} \wedge v_2 = \text{getArgValue}(args, "1") \wedge (H_1, exc) = \text{ToObject}(H, v_2) \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)] \\
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.defineProperties"}, args)\!]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v_1]], A) \\
&\text{where } v_1 = \text{getArgValue}(args, "0") \wedge v_1 \in \text{Loc} \wedge v_2 = \text{getArgValue}(args, "1") \wedge (H_1, l_1) = \text{ToObject}(H, v_2) \\
&\quad \wedge o = H(v_1) \left[ \forall x \in \text{dom}(H(v_2)) : x \mapsto \left\{ \begin{array}{l} \text{value} : H(v_2)(x)(\text{"value"}) \\ \text{writable} : H(v_2)(x)(\text{"writable"}) \\ \text{enumerable} : H(v_2)(x)(\text{"enumerable"}) \\ \text{configurable} : H(v_2)(x)(\text{"configurable"}) \end{array} \right\} \right] \\
&\quad \wedge H_1 = H[l \mapsto o]
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.seal"}, args)\!]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \text{getArgValue}(args, "0") \wedge v \notin \text{Loc} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.seal"}, args)\!]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v]], A) \\
&\text{where } v = \text{getArgValue}(args, "0") \wedge v \in \text{Loc} \\
&\quad \wedge H_1 = H \left[ H(v) \mapsto \left[ \begin{array}{l} \forall x \in \text{Dom}(H(v)) : x \mapsto H(v)(x) \text{ with } \text{configurable} = \text{false};, \\ @\text{extensible} \mapsto \text{false}; \end{array} \right] \right]
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.freeze"}, args)\!]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \text{getArgValue}(args, "0") \wedge v \notin \text{Loc} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Object.seal"}, args)\!]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v]], A) \\
&\text{where } v = \text{getArgValue}(args, "0") \wedge v \in \text{Loc} \\
&\quad \wedge H_1 = H \left[ H(v) \left[ \begin{array}{l} \forall x \in P_1 : x \mapsto H(v)(x) \text{ with } \text{writable} = \text{false}; \text{configurable} = \text{false};, \\ \forall y \in P_2 : y \mapsto H(v)(y) \text{ with } \text{configurable} = \text{false};, \\ @\text{extensible} \mapsto \text{false}; \end{array} \right] \right] \\
&\quad \wedge P_1 = \{x \mid x \in \text{dom}(H(v)(x)) \wedge \text{IsDataDescriptor}(x)\} \\
&\quad \wedge P_2 = \{x \mid x \in \text{dom}(H(v)(x)) \wedge \neg \text{IsDataDescriptor}(x)\}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.preventExtensions"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)][@exception \mapsto l_e], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \notin \text{Loc} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.preventExtensions"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)][@return \mapsto v], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \in \text{Loc} \\
&\quad \wedge H_1 = H[H(v) \mapsto [@extensible \mapsto \text{false}]]
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.isSealed"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)][@exception \mapsto l_e], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \notin \text{Loc} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.isSealed"}, args) \rrbracket (H, A) &= (H[\#temp \mapsto H(\#temp)][@return \mapsto \text{false}], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \in \text{Loc} \wedge \exists x \in \text{dom}(H(v)) : H(v)(x).configurable = \text{true} \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.isSealed"}, args) \rrbracket (H, A) &= (H[\#temp \mapsto H(\#temp)][@return \mapsto b], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \in \text{Loc} \wedge \forall x \in \text{dom}(H(v)) : H(v)(x).configurable = \text{false} \\
&\quad \wedge b = \begin{cases} \text{true} & \text{if } H(v)(@extensible) = \text{false} \\ \text{false} & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.isFrozen"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)][@exception \mapsto l_e], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \notin \text{Loc} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.isFrozen"}, args) \rrbracket (H, A) &= (H[\#temp \mapsto H(\#temp)][@return \mapsto \text{false}], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \in \text{Loc} \\
&\quad \wedge \exists x \in \text{dom}(H(v)) : \left( \begin{aligned} &(\text{IsDataDescription}(x) \wedge (H(v)(x).writable = \text{true} \vee H(v)(x).configurable = \text{true})) \\ &\vee (\neg \text{IsDataDescription} \wedge H(v)(x).configurable = \text{true}) \end{aligned} \right) \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.isFrozen"}, args) \rrbracket (H, A) &= (H[\#temp \mapsto H(\#temp)][@return \mapsto b], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \in \text{Loc} \\
&\quad \wedge \forall x \in \text{dom}(H(v)) : \left( \begin{aligned} &(\text{IsDataDescription}(x) \wedge H(v)(x).writable = \text{false} \wedge H(v)(x).configurable = \text{false}) \\ &\vee (\neg \text{IsDataDescription} \wedge H(v)(x).configurable = \text{false}) \end{aligned} \right) \\
&\quad \wedge b = \begin{cases} \text{true} & \text{if } H(v)(@extensible) = \text{false} \\ \text{false} & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.isExtensible"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)][@exception \mapsto l_e], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \notin \text{Loc} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.isExtensible"}, args) \rrbracket (H, A) &= (H[\#temp \mapsto H(\#temp)][@return \mapsto H(v)(@extensible)], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \in \text{Loc}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.keys"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)][@exception \mapsto l_e], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \notin \text{Loc} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.keys"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)][@return \mapsto l], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge v \in \text{Loc} \wedge P = |\{x \mid x \in \text{dom}(H(v)) \wedge H(v)(x).enumerable = \text{true}\}| \\
&\quad \wedge n_1 = |P| \wedge l = \text{newLocation}() \wedge o = \text{NewArrayObject}(n_1) \wedge n_2 = 0 \\
&\quad \wedge o_1 = o \left[ \begin{array}{c} \forall x \in P : \text{toString}(n_2^{++}) \mapsto \left\{ \begin{array}{l} \text{value} : x \\ \text{writable} : \text{true} \\ \text{enumerable} : \text{true} \\ \text{configurable} : \text{true} \end{array} \right\} \end{array} \right] \\
&\quad \wedge H_1 = H[l \mapsto o_1]
\end{aligned}$$

### 11.1.4 Object.prototype

$\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Object.prototype.toString"}, args)](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A)$   
 where  $\mathcal{V}_{cp}[\text{this}](H, A) = \text{undefined} \wedge s = \text{"[object Undefined]"}$   
 $\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Object.prototype.toString"}, args)](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A)$   
 where  $\mathcal{V}_{cp}[\text{this}](H, A) = \text{null} \wedge s = \text{"[object Null]"}$   
 $\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Object.prototype.toString"}, args)](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto s]], A)$   
 where  $v_1 = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v_1 \notin \{\text{undefined}, \text{null}\}$   
 $\wedge (H_1, v_2) = \text{toObject}(H, v_1) \wedge s = \text{"[object" + } H(v_2)(\text{@class}) + \text{"}]"$

$\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Object.prototype.toLocaleString"}, args)](H, A) = (H_2[\#temp \mapsto H_2(\#temp)[@exception \mapsto l_e]], A)$   
 where  $v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, exc) = \text{toObject}(H, v)$   
 $\wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)]$   
 $\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Object.prototype.toLocaleString"}, args)](H, A) = (H_2[\#temp \mapsto H_2(\#temp)[@exception \mapsto l_e]], A)$   
 where  $v_1 = \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, v_2) = \text{toObject}(H, v_1) \wedge H_1(v_2)(\text{"toString"}) \notin \text{Loc}$   
 $\wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})]$   
 $\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Object.prototype.toLocaleString"}, args)](H, A) = (H_2[\#temp \mapsto H_2(\#temp)[@exception \mapsto l_e]], A)$   
 where  $v_1 = \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, v_2) = \text{toObject}(H, v_1) \wedge v_3 = H_1(v_2)(\text{"toString"}) \wedge v_3 \in \text{Loc}$   
 $\neg \text{IsCallable}(H_1, v_3) \wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})]$   
 $\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Object.prototype.toLocaleString"}, args)](H, A) = (H_2[\#temp \mapsto H_2(\#temp)[@return \mapsto l_e]], A)$   
 where  $v_1 = \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, v_2) = \text{toObject}(H, v_1) \wedge v_3 = H_1(v_2)(\text{"toString"}) \wedge v_3 \in \text{Loc}$   
 $\text{IsCallable}(H_1, v_3) \text{????}$

$\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Object.prototype.valueOf"}, args)](H, A) = (H_2[\#temp \mapsto H_2(\#temp)[@exception \mapsto l_e]], A)$   
 where  $v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, exc) = \text{toObject}(H, v)$   
 $\wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)]$   
 $\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Object.prototype.valueOf"}, args)](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v_1]], A)$   
 where  $v_1 = \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, v_2) = \text{toObject}(H, v_1) \wedge H(v)(\text{@class}) = \text{"Object"}$

$\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Object.prototype.hasOwnProperty"}, args)](H, A) = (H_2[\#temp \mapsto H_2(\#temp)[@exception \mapsto l_e]], A)$   
 where  $v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, exc) = \text{toObject}(H, v)$   
 $\wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)]$   
 $\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Object.prototype.hasOwnProperty"}, args)](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto b]], A)$   
 where  $v_1 = \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, v_2) = \text{toObject}(H, v_1) \wedge v_3 = \text{getArgValue}(args, \text{"0"})$   
 $\wedge s = \text{toString}(\text{toPrimitive}(v_3)) \wedge b = \text{HasOwnProperty}(H_1, v_2, s)$

$\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Object.prototype.isPrototypeOf"}, args)](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto \text{false}]], A)$   
 where  $v = \text{getArgValue}(args, \text{"0"}) \wedge v \notin \text{Loc}$   
 $\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Object.prototype.isPrototypeOf"}, args)](H, A) = (H_2[\#temp \mapsto H_2(\#temp)[@exception \mapsto l_e]], A)$   
 where  $v_1 = \text{getArgValue}(args, \text{"0"}) \wedge v_1 \in \text{Loc} \wedge v_2 = \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, exc) = \text{toObject}(H, v_2)$   
 $\wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)]$   
 $\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Object.prototype.isPrototypeOf"}, args)](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v_4]], A)$   
 where  $v_1 = \text{getArgValue}(args, \text{"0"}) \wedge v_1 \in \text{Loc} \wedge v_2 = \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, v_3) = \text{toObject}(H, v_2)$   
 $v_4 = \text{inherit}(H_1, v_1, v_3)$

$\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Object.prototype.propertyIsEnumerable"}, args)](H, A) = (H_2[\#temp \mapsto H_2(\#temp)[@exception \mapsto l_e]], A)$   
 where  $v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, exc) = \text{toObject}(H, v)$   
 $\wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)]$   
 $\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Object.prototype.propertyIsEnumerable"}, args)](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto \text{false}]], A)$   
 where  $v_1 = \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, v_2) = \text{toObject}(H, v_1) \wedge v_3 = \text{getArgValue}(args, \text{"0"})$   
 $\wedge s = \text{toString}(\text{toPrimitive}(v_3)) \wedge \neg \text{HasOwnProperty}(H_1, v_2, s)$   
 $\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Object.prototype.propertyIsEnumerable"}, args)](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto b]], A)$   
 where  $v_1 = \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, v_2) = \text{toObject}(H, v_1) \wedge v_3 = \text{getArgValue}(args, \text{"0"})$   
 $\wedge s = \text{toString}(\text{toPrimitive}(v_3)) \wedge \text{HasOwnProperty}(H_1, v_2, s) \wedge b = H_1(v_2)(s).enumerable$

## 11.1.5 Function

### 11.1.6 Function.prototype

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Function.prototype.toString"}, \text{args})]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[\text{@exception} \mapsto l_e]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v \notin \text{Loc} \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Function.prototype.toString"}, \text{args})]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[\text{@exception} \mapsto l_e]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v \in \text{Loc} \wedge H(v)(\text{@class}) \neq \text{"Function"} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Function.prototype.toString"}, \text{args})]\!](H, A) &= (H[\#temp \mapsto H(\#temp)[\text{@return} \mapsto s]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v \in \text{Loc} \wedge H(v)(\text{@class}) = \text{"Function"} \wedge s = \text{fid2String}(H(v)(\text{@function}))
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Function.prototype.apply"}, \text{args})]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[\text{@exception} \mapsto l_e]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v \notin \text{Loc} \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Function.prototype.apply"}, \text{args})]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[\text{@exception} \mapsto l_e]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v \in \text{Loc} \wedge \neg \text{IsCallable}(H, v) \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Function.prototype.apply"}, \text{args})]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[\text{@exception} \mapsto l_e]], A) \\
&\text{where } v_{fun} = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v_{fun} \in \text{Loc} \wedge \text{IsCallable}(H, v_{fun}) \\
&\quad \wedge v_{arg} = \text{getArgValue}(\text{args}, "1") \wedge v_{arg} \notin \{ \text{null}, \text{undefined} \} \wedge v_{arg} \notin \text{Loc} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Function.prototype.apply"}, \text{args})]\!](H, A) &= (H_2, A_1) \\
&\text{where } v_{fun} = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v_{fun} \in \text{Loc} \wedge \text{IsCallable}(H, v_{fun}) \\
&\quad \wedge v_{arg} = \text{getArgValue}(\text{args}, "1") \wedge v_{arg} \in \{ \text{null}, \text{undefined} \} \wedge o_{arg} = \text{NewArgObject}(0) \\
&\quad \wedge l_{arg} = \text{newLocation}() \wedge H_1 = H[l_{arg} \mapsto o_{arg}] \wedge l_{scope} = \text{newLocation}() \\
&\quad \wedge A_1 = \text{PushStack}(H(v_{fun})(\text{@scope}), l_{scope}) \\
&\quad \wedge O_{scope} = \left\{ \begin{array}{l} \text{arguments} \mapsto \left\{ \begin{array}{l} \text{value} : l_{arg}, \\ \text{writable} : \text{true}, \\ \text{unumerable} : \text{false}, \\ \text{configurable} : \text{false} \end{array} \right\}, \\ \text{@this} \mapsto \text{getArgValue}(\text{args}, "0"), \\ \text{@up} \mapsto A, \\ \text{@return} \mapsto H(\#temp)(\text{@return}) \end{array} \right\} \wedge H_2 = H_1[l_{new} \mapsto O_{scope}] \\
&\quad \wedge \text{fid}_{callee} = H(v_{fun})(\text{@function}) \wedge \text{cp}_{after-call} = \text{getAftercallFromCall}_P(\text{cp}) \\
&\quad \wedge \hookrightarrow := \hookrightarrow \cup \{ (cp, (\text{fid}_{callee}, \text{ENTRY})), ((\text{fid}_{callee}, \text{EXIT}), \text{cp}_{after-call}) \} \\
&\quad \wedge \xrightarrow{\text{exc}} := \xrightarrow{\text{exc}} \cup \{ ((\text{fid}_{callee}, \text{EXIT-EXC}), \text{cp}_{after-call}) \} \\
&\quad \wedge \text{BelongsTo} := \text{BelongsTo} \cup \{ (l_{new}, \text{cp}) \} \\
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Function.prototype.apply"}, \text{args})]\!](H, A) &= (H_2, A_1) \\
&\text{where } v_{fun} = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v_{fun} \in \text{Loc} \wedge \text{IsCallable}(H, v_{fun}) \\
&\quad \wedge v_{arg} = \text{getArgValue}(\text{args}, "1") \wedge v_{arg} \notin \{ \text{null}, \text{undefined} \} \wedge v_{arg} \in \text{Loc} \wedge n_{len} = \text{Proto}(H, v_{arg}, \text{"length"}) \\
&\quad \wedge o_{arg} = \text{NewArgObject}(n_{len}) [\forall i \in \{ 0, \dots, n_{len} - 1 \} : "i" \mapsto \text{Proto}(H, v_{arg}, "i")] \wedge l_{arg} = \text{newLocation}() \\
&\quad \wedge H_1 = H[l_{arg} \mapsto o_{arg}] \wedge o_{arg} = \text{NewArgObject}(0) \wedge l_{arg} = \text{newLocation}() \wedge H_1 = H[l_{arg} \mapsto o_{arg}] \\
&\quad \wedge l_{scope} = \text{newLocation}() \wedge A_1 = \text{PushStack}(H(v_{fun})(\text{@scope}), l_{scope}) \\
&\quad \wedge O_{scope} = \left\{ \begin{array}{l} \text{arguments} \mapsto \left\{ \begin{array}{l} \text{value} : l_{arg}, \\ \text{writable} : \text{true}, \\ \text{unumerable} : \text{false}, \\ \text{configurable} : \text{false} \end{array} \right\}, \\ \text{@this} \mapsto \text{getArgValue}(\text{args}, "0"), \\ \text{@up} \mapsto A, \\ \text{@return} \mapsto H(\#temp)(\text{@return}) \end{array} \right\} \wedge H_2 = H_1[l_{new} \mapsto O_{scope}] \\
&\quad \wedge \text{fid}_{callee} = H(v_{fun})(\text{@function}) \wedge \text{cp}_{after-call} = \text{getAftercallFromCall}_P(\text{cp}) \\
&\quad \wedge \hookrightarrow := \hookrightarrow \cup \{ (cp, (\text{fid}_{callee}, \text{ENTRY})), ((\text{fid}_{callee}, \text{EXIT}), \text{cp}_{after-call}) \} \\
&\quad \wedge \xrightarrow{\text{exc}} := \xrightarrow{\text{exc}} \cup \{ ((\text{fid}_{callee}, \text{EXIT-EXC}), \text{cp}_{after-call}) \} \\
&\quad \wedge \text{BelongsTo} := \text{BelongsTo} \cup \{ (l_{new}, \text{cp}) \}
\end{aligned}$$



$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Function.prototype.call"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \text{Loc} \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Function.prototype.call"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \text{Loc} \wedge \neg \text{IsCallable}(H, v) \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Function.prototype.call"}, args)](H, A) &= (H_2, A_1) \\
&\text{where } v_{fun} = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v_{fun} \in \text{Loc} \wedge \text{IsCallable}(H, v_{fun}) \wedge n_{len} = \text{ToUInt32}(\text{getArgValue}(args, \text{"length"})) \\
&\quad \wedge o_{arg} = \text{NewArgObject}(n_{len} - 1) [\forall i \in \{1, \dots, n_{len}\} : \text{"i"} \mapsto \text{getArgValue}(args, \text{"i"})] \\
&\quad \wedge l_{arg} = \text{newLocation}() \wedge H_1 = H[l_{arg} \mapsto o_{arg}] \\
&\quad \wedge l_{scope} = \text{newLocation}() \wedge A_1 = \text{PushStack}(H(v_{fun})(@scope), l_{scope}) \\
&\quad \wedge O_{scope} = \left\{ \begin{array}{l} \text{arguments} \mapsto \left\{ \begin{array}{l} \text{value} : l_{arg}, \\ \text{writable} : \text{true}, \\ \text{unumarable} : \text{false}, \\ \text{configurable} : \text{false} \end{array} \right\}, \\ @this \mapsto \text{getArgValue}(args, \text{"0"}), \\ @up \mapsto A, \\ @return \mapsto H(\#temp)(@return) \end{array} \right\} \wedge H_2 = H_1[l_{new} \mapsto o_{scope}] \\
&\quad \wedge fid_{callee} = H(v_{fun})(@function) \wedge cp_{after-call} = \text{getAftercallFromCall}_P(cp) \\
&\quad \wedge \xrightarrow{\text{exc}} := \xrightarrow{\text{exc}} \cup \left\{ (cp, (fid_{callee}, \text{ENTRY})), ((fid_{callee}, \text{EXIT}), cp_{after-call}) \right\} \\
&\quad \wedge \xrightarrow{\text{exc}} := \xrightarrow{\text{exc}} \cup \left\{ ((fid_{callee}, \text{EXIT-EXC}), cp_{after-call}) \right\} \\
&\quad \wedge \text{BelongsTo} := \text{BelongsTo} \cup \left\{ (l_{new}, cp) \right\}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Function.prototype.bind"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \text{Loc} \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Function.prototype.bind"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \text{Loc} \wedge \neg \text{IsCallable}(H, v) \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})]
\end{aligned}$$

### 11.1.7 Array

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.constructor"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } \text{getArgValue}(args, \text{"length"}) = 0 \wedge l = \text{newLocation}() \wedge H_1 = H[l \mapsto \text{NewArrayObject}(0)] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.constructor"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v_{len} = \text{getArgValue}(args, \text{"length"}) \wedge v_{len} = 1 \wedge v_{len} \in \text{Number} \wedge v_{len} \neq \text{ToUInt32}(v_{len}) \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{RangeError})] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.constructor"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } v_{len} = \text{getArgValue}(args, \text{"length"}) \wedge v_{len} = 1 \wedge v_{len} \in \text{Number} \wedge n_{len32} = \text{ToUInt32}(v_{len}) \wedge v_{len} = n_{len32} \\
&\quad \wedge l = \text{newLocation}() \wedge H_1 = H[l \mapsto \text{NewArrayObject}(n_{len32})] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.constructor"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } v_{len} = \text{getArgValue}(args, \text{"length"}) \wedge v_{len} = 1 \wedge v_{len} \notin \text{Number} \\
&\quad \wedge l = \text{newLocation}() \wedge H_1 = H[l \mapsto \text{NewArrayObject}(1)[\text{"0"} \mapsto v_{len}]] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.constructor"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } v_{len} = \text{getArgValue}(args, \text{"length"}) \wedge v_{len} > 1 \wedge l = \text{newLocation}() \\
&\quad \wedge H_1 = H[l \mapsto \text{NewArrayObject}(v_{len})[\forall i \in \{0, \dots, v_{len} - 1\} : \text{"i"} \mapsto \text{getArgValue}(args, \text{"i"})]] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.isArray"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto \text{false}]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \text{Loc} \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.isArray"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto b]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \text{Loc} \wedge b = \begin{cases} \text{true} & \text{if } H(v)(@class) = \text{"Array"} \\ \text{false} & \text{otherwise} \end{cases}
\end{aligned}$$

### 11.1.8 Array.prototype

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Array.prototype.toString"}, args)]\!](H, A) &= (H_2[\#temp \mapsto H_2(\#temp)[@exception \mapsto l_e]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge (H_1, exc) = \text{ToObject}(H, v) \\
&\wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)] \\
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Array.prototype.toString"}, args)]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto s_{join}]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge (H_1, l) = \text{ToObject}(H, v) \\
&\wedge s = \begin{cases} \text{"[object" + } H(v_2)(@class) + \text{"} & \text{if } \text{Proto}(H, l, \text{"join"}) \notin \text{Loc} \vee \text{IsCallable}(H_1, \text{Proto}(H, l, \text{"join"})) \\ s_{join} & \text{otherwise} \end{cases} \\
&\wedge n_{len} = \text{Proto}(H_1, l, \text{"length"}) \\
&\wedge s_i = \begin{cases} \text{"} & \text{if } \text{Proto}(H_1, l, \text{"i"}) \in \{\text{null}, \text{undefined}\} \\ \text{ToString}(\text{ToPrimitive}(\text{Proto}(H_1, l, \text{"i"}))) & \text{otherwise} \end{cases} \\
&\wedge s_{join} = \begin{cases} \text{"} & \text{if } n_{len} = 0 \\ s_0 + \text{" , " + } s_1 + \text{" , " + } \dots + \text{" , " + } s_{n_{len}-1} & \text{otherwise} \end{cases}
\end{aligned}$$
  

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Array.prototype.concat"}, args)]\!](H, A) &= (H_2[\#temp \mapsto H_2(\#temp)[@exception \mapsto l_e]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge (H_1, exc) = \text{ToObject}(H, v) \\
&\wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)] \\
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Array.prototype.concat"}, args)]\!](H, A) &= (H_2[\#temp \mapsto H_2(\#temp)[@return \mapsto l_{new}]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge (H_1, l) = \text{ToObject}() \wedge n = 0 \\
&\wedge o = \text{NewArrayObject}(0) [\forall i \in \{0, \dots, H(l)(\text{"length"}) - 1\} : \text{toString}(n^{++}) \mapsto H(l)(\text{"i"})] \\
&\wedge v_{len} = \text{getArgValue}(args, \text{"length"}) \wedge v_i = \text{getArgValue}(args, \text{"i"}) \\
&\wedge o_1 = o [\forall i \in \{0, v_{len} - 1\} : \begin{cases} \forall j \in \{0, \dots, H(v_i)(\text{"length"}) - 1\} : & \text{if } v_i \in \text{Loc} \\ \text{toString}(n^{++}) \mapsto \text{Proto}(H, v_i, \text{"j"}) & \wedge H(v_i)(@class) = \text{"Array"} \\ \text{toString}(n^{++}) \mapsto v_i & \text{otherwise} \end{cases} ] \\
&\wedge l_{new} = \text{newLocation}() \wedge H_2 = H_1[l_{new} \mapsto o_1]
\end{aligned}$$
  

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Array.prototype.join"}, args)]\!](H, A) &= (H_2[\#temp \mapsto H_2(\#temp)[@exception \mapsto l_e]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge (H_1, exc) = \text{ToObject}(H, v) \\
&\wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)] \\
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Array.prototype.join"}, args)]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto s]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge (H_1, l) = \text{ToObject}(H, v) \wedge v_0 = \text{getArgValue}(args, \text{"0"}) \\
&\wedge s_{sep} = \begin{cases} \text{" , "} & \text{if } v_0 = \text{undefined} \\ \text{ToString}(\text{ToPrimitive}(v_0)) & \text{otherwise} \end{cases} \\
&\wedge n_{len} = \text{Proto}(H_1, l, \text{"length"}) \\
&\wedge s_i = \begin{cases} \text{"} & \text{if } \text{Proto}(H_1, l, \text{"i"}) \in \{\text{null}, \text{undefined}\} \\ \text{ToString}(\text{ToPrimitive}(\text{Proto}(H_1, l, \text{"i"}))) & \text{otherwise} \end{cases} \\
&\wedge s = \begin{cases} \text{"} & \text{if } n_{len} = 0 \\ s_0 + s_{sep} + s_1 + s_{sep} + \dots + s_{sep} + s_{n_{len}-1} & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Array.prototype.pop"}, args) \rrbracket (H, A) &= (H_2[\#temp \mapsto H_2(\#temp)][@exception \mapsto l_e], A) \\
&\text{where } v_{this} = \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge (H_1, exc) = \text{ToObject}(H, v_{this}) \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)] \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Array.prototype.pop"}, args) \rrbracket (H, A) &= (H_2[\#temp \mapsto H_2(\#temp)][@return \mapsto v], A) \\
&\text{where } v_{this} = \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge (H_1, l) = \text{ToObject}(H, v_{this}) \wedge n_{len} = \text{ToUInt32}(\text{ToPrimitive}(\text{Proto}(H_1, l, \text{"length"}))) \\
&\quad \wedge (H_2, v) = \begin{cases} (\text{PropStore}(H_1, l, \text{"length"}, 0), \text{undefined}) & \text{if } n_{len} = 0 \\ \left( \begin{array}{l} \text{Delete}(\text{PropStore}(H_1, l, \text{"length"}, n_{len} - 1), l, \text{ToString}(n_{len} - 1)).1, \\ \text{Proto}(H_1, l, \text{ToString}(n_{len} - 1)) \end{array} \right) & \text{otherwise} \end{cases} \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Array.prototype.push"}, args) \rrbracket (H, A) &= (H_2[\#temp \mapsto H_2(\#temp)][@exception \mapsto l_e], A) \\
&\text{where } v_{this} = \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge (H_1, exc) = \text{ToObject}(H, v_{this}) \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)] \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Array.prototype.push"}, args) \rrbracket (H, A) &= (H_3[\#temp \mapsto H_3(\#temp)][@return \mapsto n], A) \\
&\text{where } v_{this} = \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge (H_1, l) = \text{ToObject}(H, v_{this}) \\
&\quad \wedge n_{len} = \text{ToUInt32}(\text{ToPrimitive}(\text{Proto}(H_1, l, \text{"length"}))) \wedge n_{arglen} = \text{getArgValue}(args, \text{"length"}) \\
&\quad \wedge H_2 = H_1[l \mapsto H_1(l) \mid \forall i \in \{0, \dots, n_{arglen} - 1\} : \text{ToString}(n_{len} + i) \mapsto \text{getArgValue}(args, \text{"i"})] \\
&\quad \wedge n = n_{len} + n_{arglen} \wedge H_3 = \text{PropStore}(H_2, l, \text{"length"}, n) \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Array.prototype.reverse"}, args) \rrbracket (H, A) &= (H_2[\#temp \mapsto H_2(\#temp)][@exception \mapsto l_e], A) \\
&\text{where } v_{this} = \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge (H_1, exc) = \text{ToObject}(H, v_{this}) \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)] \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Array.prototype.reverse"}, args) \rrbracket (H, A) &= (H_2[\#temp \mapsto H_2(\#temp)][@return \mapsto l], A) \\
&\text{where } v_{this} = \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge (H_1, l) = \text{ToObject}(H, v_{this}) \\
&\quad \wedge n_{len} = \text{ToUInt32}(\text{ToPrimitive}(\text{Proto}(H_1, l, \text{"length"}))) \wedge n_{last} = n_{len} - 1 \wedge n_{mid} = \text{native.floor}(n_{len}/2) \\
&\quad \wedge b_i = \text{HasProperty}(H_1, l, i) \wedge o = H(l) \\
&\quad \wedge o_1 = o \left[ \forall i \in \{0, \dots, n_{mid} - 1\} : \begin{cases} \text{ToString}(i) \mapsto \text{Proto}(H_1, l, \text{ToString}(n_{last} - i)), & \text{if } b_i \wedge b_{n_{last} - i} \\ \text{ToString}(n_{last} - i) \mapsto \text{Proto}(H_1, l, \text{ToString}(i)) & \text{if } \neg b_i \wedge b_{n_{last} - i} \\ \text{ToString}(i) \mapsto \text{Proto}(H_1, l, \text{ToString}(n_{last} - i)) & \text{if } b_i \wedge \neg b_{n_{last} - i} \\ \text{ToString}(n_{last} - i) \mapsto \text{Proto}(H_1, l, \text{ToString}(i)) & \text{if } b_i \wedge \neg b_{n_{last} - i} \end{cases} \right] \\
&\quad \wedge H_2 = H_1[l \mapsto o_1] \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Array.prototype.shift"}, args) \rrbracket (H, A) &= (H_2[\#temp \mapsto H_2(\#temp)][@exception \mapsto l_e], A) \\
&\text{where } v_{this} = \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge (H_1, exc) = \text{ToObject}(H, v_{this}) \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)] \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Array.prototype.shift"}, args) \rrbracket (H, A) &= (H_2[\#temp \mapsto H_2(\#temp)][@return \mapsto v], A) \\
&\text{where } v_{this} = \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge (H_1, l) = \text{ToObject}(H, v_{this}) \\
&\quad \wedge n_{len} = \text{ToUInt32}(\text{ToPrimitive}(\text{Proto}(H_1, l, \text{"length"}))) \\
&\quad \wedge (H_2, v) = \begin{cases} (H_1, \text{undefined}) & \text{if } n_{len} = 0 \\ (H_1[l \mapsto o_1], \text{Proto}(H_1, l, \text{"0"})) & \text{otherwise} \end{cases} \\
&\quad \wedge o_1 = H_1(l) \mid \forall i \in \{1, \dots, n_{len} - 1\} : \text{ToString}(i) \mapsto \text{Proto}(H_1, l, \text{ToString}(i - 1)) \quad \text{if } \text{HasProperty}(H_1, l, i) \quad ]
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.prototype.slice"}, args)](H, A) &= (H_2[\#temp \mapsto H_2(\#temp)[@exception \mapsto l_e]], A) \\
\text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, exc) = \text{ToObject}(H, v_{this}) \\
&\wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.prototype.slice"}, args)](H, A) &= (H_2[\#temp \mapsto H_2(\#temp)[@return \mapsto l_{new}]], A) \\
\text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, l) = \text{ToObject}(H, v_{this}) \\
&\wedge n_{len} = \text{ToUInt32}(\text{ToPrimitive}(\text{Proto}(H_1, l, \text{"length"}))) \\
&\wedge n_{argstart} = \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, \text{"0"}))) \\
&\wedge n_{start} = \begin{cases} 0 & \text{if } n_{argstart} < 0 \wedge n_{len} + n_{argstart} \leq 0 \\ n_{len} + n_{argstart} & \text{if } n_{argstart} < 0 \wedge n_{len} + n_{argstart} > 0 \\ n_{argstart} & \text{if } n_{argstart} \geq 0 \wedge n_{argstart} < n_{len} \\ n_{len} & \text{if } n_{argstart} \geq 0 \wedge n_{argstart} \geq n_{len} \end{cases} \\
&\wedge n_{argend} = \begin{cases} n_{len} & \text{if } \text{getArgValue}(args, \text{"1"}) = \text{undefined} \\ \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, \text{"1"}))) & \text{otherwise} \end{cases} \\
&\wedge n_{end} = \begin{cases} 0 & \text{if } n_{argend} < 0 \wedge n_{len} + n_{argend} \leq 0 \\ n_{len} + n_{argend} & \text{if } n_{argend} < 0 \wedge n_{len} + n_{argend} > 0 \\ n_{argend} & \text{if } n_{argend} \geq 0 \wedge n_{argend} < n_{len} \\ n_{len} & \text{if } n_{argend} \geq 0 \wedge n_{argend} \geq n_{len} \end{cases} \\
&\wedge o = \text{NewArrayObject}(0) \\
&\wedge o_1 = o [\forall i \in \{n_{start}, \dots, n_{end} - 1\} : \text{ToString}(i) \mapsto \text{Proto}(H_1, l, \text{ToString}(i - 1)) \text{ if } \text{HasProperty}(H_1, l, i)] \\
&\wedge l_{new} = \text{newLocation}() \wedge H_2 = H_1[l_{new} \mapsto o_1]
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.prototype.splice"}, args)](H, A) &= (H_2[\#temp \mapsto H_2(\#temp)[@exception \mapsto l_e]], A) \\
\text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, exc) = \text{ToObject}(H, v_{this}) \\
&\wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.prototype.splice"}, args)](H, A) &= (H_3[\#temp \mapsto H_3(\#temp)[@return \mapsto l_{new}]], A) \\
\text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, l) = \text{ToObject}(H, v_{this}) \\
&\wedge n_{arglen} = \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, \text{"length"}))) \wedge n_{arglen} = 2 \\
&\wedge n_{len} = \text{ToUInt32}(\text{ToPrimitive}(\text{Proto}(H_1, l, \text{"length"}))) \\
&\wedge n_{argstart} = \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, \text{"0"}))) \\
&\wedge n_{start} = \begin{cases} 0 & \text{if } n_{argstart} < 0 \wedge n_{len} + n_{argstart} \leq 0 \\ n_{len} + n_{argstart} & \text{if } n_{argstart} < 0 \wedge n_{len} + n_{argstart} > 0 \\ n_{argstart} & \text{if } n_{argstart} \geq 0 \wedge n_{argstart} < n_{len} \\ n_{len} & \text{if } n_{argstart} \geq 0 \wedge n_{argstart} \geq n_{len} \end{cases} \\
&\wedge n_{argdel} = \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, \text{"1"}))) \\
&\wedge n_{del} = \min(\max(n_{argdel}, 0), n_{len} - n_{start}) \\
&\wedge o = \text{NewArrayObject}(0) \\
&\wedge o_1 = o [\forall i \in \{0, \dots, n_{del} - 1\} : \text{ToString}(i) \mapsto \text{Proto}(H_1, l, n_{start} + i) \text{ if } \text{HasProperty}(H_1, l, i + n_{del})] \\
&\wedge H_2 = H_1[l \mapsto H_1(l) [\forall i \in \{n_{start}, \dots, n_{start} + n_{del} - 1\} : \text{ToString}(i) \not\mapsto \text{// delete prop}]] \\
&\wedge l_{new} = \text{newLocation}() \wedge H_3 = H_2[l_{new} \mapsto o_1]
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.prototype.splice"}, args)](H, A) &= (H_2[\#temp \mapsto H_2(\#temp)[@return \mapsto l_{new}]], A) \\
\text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, l) = \text{ToObject}(H, v_{this}) \\
&\wedge n_{arglen} = \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, \text{"length"}))) \wedge n_{arglen} > 2 \wedge n_{replace} = n_{arglen} - 2 \\
&\wedge n_{len} = \text{ToUInt32}(\text{ToPrimitive}(\text{Proto}(H_1, l, \text{"length"}))) \\
&\wedge n_{argstart} = \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, \text{"0"}))) \\
&\wedge n_{start} = \begin{cases} 0 & \text{if } n_{argstart} < 0 \wedge n_{len} + n_{argstart} \leq 0 \\ n_{len} + n_{argstart} & \text{if } n_{argstart} < 0 \wedge n_{len} + n_{argstart} > 0 \\ n_{argstart} & \text{if } n_{argstart} \geq 0 \wedge n_{argstart} < n_{len} \\ n_{len} & \text{if } n_{argstart} \geq 0 \wedge n_{argstart} \geq n_{len} \end{cases} \\
&\wedge n_{argdel} = \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, \text{"1"}))) \\
&\wedge n_{del} = \min(\max(n_{argdel}, 0), n_{len} - n_{start}) \\
&\wedge o = \text{NewArrayObject}(0) \\
&\wedge o_1 = o [\forall i \in \{0, \dots, n_{del} - 1\} : \text{ToString}(i) \mapsto \text{Proto}(H_1, l, n_{start} + i) \text{ if } \text{HasProperty}(H_1, l, i + n_{del})] \\
&\wedge H_2 = H_1 \left[ l \mapsto H_1(l) \left[ \begin{array}{l} \forall i \in \{n_{start}, \dots, n_{start} + n_{del} - 1\} : \text{ToString}(i) \not\mapsto \text{// delete prop} \\ \forall j \in \{0, \dots, n_{del} - 1\} : \text{ToString}(j) \mapsto \text{getArgValue}(args, n_{start} + j), \\ \forall k \in \{0, \dots, n_{len} - n_{start} - n_{del} - 1\} : \\ \quad \text{ToString}(n_{start} + n_{replace} + k) \mapsto \text{Proto}(H_1, l, n_{start} + n_{del} + k) \end{array} \right] \right] \\
&\wedge l_{new} = \text{newLocation}() \wedge H_3 = H_2[l_{new} \mapsto o_1]
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.prototype.unshift"}, args)](H, A) &= (H_2[\#temp \mapsto H_2(\#temp)[@exception \mapsto l_e]], A) \\
\text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, exc) = \text{ToObject}(H, v_{this}) \\
&\wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.prototype.unshift"}, args)](H, A) &= (H_2[\#temp \mapsto H_2(\#temp)[@exception \mapsto n]], A) \\
\text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, l) = \text{ToObject}(H, v_{this}) \\
&\wedge n_{arglen} = \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, \text{"length"}))) \\
&\wedge n_{len} = \text{ToUInt32}(\text{ToPrimitive}(\text{Proto}(H_1, l, \text{"length"}))) \\
&\wedge n_{argstart} = \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, \text{"0"}))) \\
&\wedge H_2 = H_1 \left[ l \mapsto H_1(l) \left[ \begin{array}{l} \forall i \in \{0, \dots, n_{len} - 1\} : \\ \quad \text{ToString}(n_{arglen} + i) \mapsto \text{Proto}(H_1, l, i) \quad \text{if } \text{HasProperty}(H_1, l, i) \\ \forall j \in \{0, \dots, n_{arglen} - 1\} : \text{ToString}(j) \mapsto \text{getArgValue}(args, j) \end{array} \right] \right] \\
&\wedge l_{new} = \text{newLocation}() \wedge H_3 = H_2[l_{new} \mapsto o_1] \wedge n = n_{len} + n_{arglen}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.prototype.indexOf"}, args)](H, A) &= (H_2[\#temp \mapsto H_2(\#temp)[@exception \mapsto l_e]], A) \\
\text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, exc) = \text{ToObject}(H, v_{this}) \\
&\wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.prototype.indexOf"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto n_{pos}]], A) \\
\text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, l) = \text{ToObject}(H, v_{this}) \wedge v_{find} = \text{getArgValue}(args, \text{"0"}) \\
&\wedge n_{len} = \text{ToUInt32}(\text{ToPrimitive}(\text{Proto}(H_1, l, \text{"length"}))) \\
&\wedge n_{start} = \begin{cases} \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, \text{"1"}))) & \text{if } \text{getArgValue}(args, \text{"length"}) > 1 \\ 0 & \text{otherwise} \end{cases} \\
&\wedge n_{pos} = \begin{cases} -1 & \text{if } n_{start} > n_{len} - 1 \\ -1 & \text{if } \neg \exists i \in \{n_{start}, \dots, n_{len} - 1\} : \\ & \quad (\text{HasProperty}(H_1, l, i) \wedge \text{Proto}(H, l, i) = v_{find}) \\ \min \left( \begin{array}{l} \forall i \in \{n_{start}, \dots, n_{len} - 1\} : \\ \quad \left( \begin{array}{l} \text{HasProperty}(H_1, l, i) \\ \wedge \text{Proto}(H, l, i) = v_{find} \end{array} \right) \end{array} \right) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.prototype.lastIndexOf"}, args)](H, A) &= (H_2[\#temp \mapsto H_2(\#temp)[@exception \mapsto l_e]], A) \\
\text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, exc) = \text{ToObject}(H, v_{this}) \\
&\wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(exc)] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Array.prototype.lastIndexOf"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto n_{pos}]], A) \\
\text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge (H_1, l) = \text{ToObject}(H, v_{this}) \wedge v_{find} = \text{getArgValue}(args, \text{"0"}) \\
&\wedge n_{len} = \text{ToUInt32}(\text{ToPrimitive}(\text{Proto}(H_1, l, \text{"length"}))) \\
&\wedge n_{end} = \begin{cases} \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, \text{"1"}))) & \text{if } \text{getArgValue}(args, \text{"length"}) > 1 \\ n_{len} - 1 & \text{otherwise} \end{cases} \\
&\wedge n_{pos} = \begin{cases} -1 & \text{if } \neg \exists i \in \{0, \dots, n_{end}\} : \\ & \quad (\text{HasProperty}(H_1, l, i) \wedge \text{Proto}(H, l, i) = v_{find}) \\ \max \left( \begin{array}{l} \forall i \in \{0, \dots, n_{len}\} : \\ \quad \left( \begin{array}{l} \text{HasProperty}(H_1, l, i) \\ \wedge \text{Proto}(H, l, i) = v_{find} \end{array} \right) \end{array} \right) & \text{otherwise} \end{cases}
\end{aligned}$$

### 11.1.9 String

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.constructor"}, args)](H, A) &= H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l_{new}]], A) \\
\text{where } s &= \begin{cases} \text{""} & \text{if } \text{getArgValue}(args, \text{"length"}) < 1 \\ \text{toString}(\text{toPrimitive}(\text{getArgValue}(args, \text{"0"}))) & \text{otherwise} \end{cases} \\
&\wedge l_{new} = \text{newLocation}() \wedge H_1 = H[l_{new} \mapsto \text{Newstring}(s)]
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.fromCharCode"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\
\text{where } s_{init} &= \text{""} \wedge s_i = \text{toString}(\text{native.toChar}(\text{toPrimitive}(\text{getArgValue}(args, \text{"i"})))) \quad // \text{java, scala} \\
&\wedge n = \text{getArgValue}(args, \text{"length"}) \wedge s = s_{init} + s_0 + s_1 + \dots + s_n
\end{aligned}$$

### 11.1.10 String.prototype

$$\begin{aligned}
&\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.toString"}, args)](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\quad \text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \text{Loc} \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
&\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.toString"}, args)](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\quad \text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \text{Loc} \wedge H(v)(@class) \neq \text{"String"} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
&\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.toString"}, args)](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\
&\quad \text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \text{Loc} \wedge H(v)(@class) = \text{"String"} \wedge s = H(v)(@primitive) \\
\\
&\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.valueOf"}, args)](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\quad \text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \text{Loc} \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
&\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.valueOf"}, args)](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\quad \text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \text{Loc} \wedge H(v)(@class) \neq \text{"String"} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
&\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.valueOf"}, args)](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\
&\quad \text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \text{Loc} \wedge H(v)(@class) = \text{"String"} \wedge s = H(v)(@primitive) \\
\\
&\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.charAt"}, args)](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\quad \text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \{ \text{undefined}, \text{null} \} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
&\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.charAt"}, args)](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto s_2]], A) \\
&\quad \text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \{ \text{undefined}, \text{null} \} \wedge s_1 = \text{ToString}(\text{ToPrimitive}(v)) \\
&\quad \wedge n_{pos} = \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, "0"))) \wedge n_{size} = s.length \\
&\quad \wedge s_2 = \begin{cases} "" & \text{if } n_{pos} < 0 \vee n_{pos} \geq n_{size} \\ s(n_{pos}) & \text{otherwise} \end{cases} \\
&\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.charCodeAt"}, args)](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\quad \text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \{ \text{undefined}, \text{null} \} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
&\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.charCodeAt"}, args)](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto n]], A) \\
&\quad \text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \{ \text{undefined}, \text{null} \} \wedge s_1 = \text{ToString}(\text{ToPrimitive}(v)) \\
&\quad \wedge n_{pos} = \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, "0"))) \wedge n_{size} = s.length \\
&\quad \wedge n = \begin{cases} \text{NaN} & \text{if } n_{pos} < 0 \vee n_{pos} \geq n_{size} \\ \text{native.toInt}(s(n_{pos})) & \text{otherwise} \quad // \text{java, scala} \end{cases} \\
\\
&\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.concat"}, args)](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\quad \text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \{ \text{undefined}, \text{null} \} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
&\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.concat"}, args)](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\
&\quad \text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \{ \text{undefined}, \text{null} \} \wedge s_{this} = \text{ToString}(\text{ToPrimitive}(v)) \\
&\quad \wedge s_i = \text{ToString}(\text{ToPrimitive}(\text{getArgValue}(args, "0"))) \wedge n_{len} = \text{getArgValue}(args, "length") \\
&\quad \wedge s = s_{this} + s_0 + s_1 + \dots + s_{n_{len}-1}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.indexOf"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \{ \text{undefined}, \text{null} \} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.indexOf"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto n_{pos}]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \{ \text{undefined}, \text{null} \} \wedge s_{this} = \text{ToString}(\text{ToPrimitive}(v)) \\
&\quad \wedge s_{find} = \text{ToString}(\text{ToPrimitive}(\text{getArgValue}(args, "0"))) \\
&\quad \wedge n_{argstart} = \begin{cases} 0 & \text{if } \text{getArgValue}(args, "1") = \text{undefined} \\ \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, "1"))) & \text{otherwise} \end{cases} \\
&\quad \wedge n_{start} = \min(\max(n_{argstart}, 0), s_{this}.length) \\
&\quad \wedge n_{pos} = \text{native.string.indexOf}(s_{this}, s_{find}, n_{start}) \quad // \text{java, scala} \\
\\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.lastIndexOf"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \{ \text{undefined}, \text{null} \} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.lastIndexOf"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto n_{pos}]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \{ \text{undefined}, \text{null} \} \wedge s_{this} = \text{ToString}(\text{ToPrimitive}(v)) \\
&\quad \wedge s_{find} = \text{ToString}(\text{ToPrimitive}(\text{getArgValue}(args, "0"))) \\
&\quad \wedge n_{argend} = \begin{cases} \text{Inf} & \text{if } \text{getArgValue}(args, "1") = \text{undefined} \\ \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, "1"))) & \text{otherwise} \end{cases} \\
&\quad \wedge n_{start} = \min(\max(n_{argstart}, 0), s_{this}.length) \\
&\quad \wedge n_{pos} = \text{native.string.lastIndexOf}(s_{this}, s_{find}, n_{start}) \quad // \text{java, scala} \\
\\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.localeCompare"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \{ \text{undefined}, \text{null} \} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.localeCompare"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto n]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \{ \text{undefined}, \text{null} \} \wedge s_{this} = \text{ToString}(\text{ToPrimitive}(v)) \\
&\quad \wedge s_{that} = \text{ToString}(\text{ToPrimitive}(\text{getArgValue}(args, "0"))) \\
&\quad \wedge n = \text{native.string.compare}(s_{this}, s_{that}) \quad // \text{java, scala} \\
\\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.slice"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \{ \text{undefined}, \text{null} \} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.slice"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \{ \text{undefined}, \text{null} \} \wedge s_{this} = \text{ToString}(\text{ToPrimitive}(v)) \\
&\quad \wedge n_{argstart} = \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, "0"))) \\
&\quad \wedge n_{argend} = \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, "1"))) \\
&\quad \wedge n_{strlen} = s_{this}.length \\
&\quad \wedge n_{start} = \begin{cases} \max(n_{strlen} + n_{argstart}, 0) & \text{if } n_{argstart} < 0 \\ \min(n_{argstart}, n_{strlen}) & \text{otherwise} \end{cases} \\
&\quad \wedge n_{end} = \begin{cases} \max(n_{strlen} + n_{argend}, 0) & \text{if } n_{argend} < 0 \\ \min(n_{argend}, n_{strlen}) & \text{otherwise} \end{cases} \\
&\quad \wedge s = \text{native.string.slice}(s_{this}, n_{start}, n_{end}) \quad // \text{java, scala}
\end{aligned}$$



$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.substring"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \{ \text{undefined}, \text{null} \} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.substring"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \{ \text{undefined}, \text{null} \} \wedge s_{this} = \text{ToString}(\text{ToPrimitive}(v)) \\
&\quad \wedge n_{strlen} = s_{this}.length \\
&\quad \wedge n_{argstart} = \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, "0"))) \\
&\quad \wedge n_{argend} = \begin{cases} n_{strlen} & \text{if } \text{getArgValue}(args, "1") = \text{undefined} \\ \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(args, "1"))) & \text{otherwise} \end{cases} \\
&\quad \wedge n_{start} = \min(\max(n_{argstart}, 0), n_{strlen}) \\
&\quad \wedge n_{end} = \min(\max(n_{argend}, 0), n_{strlen}) \\
&\quad \wedge s = \text{native.string.slice}(s_{this}, \min(n_{start}, n_{end}), \max(n_{start}, n_{end})) \quad // \text{java, scala}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.toLowerCase"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \{ \text{undefined}, \text{null} \} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.toLowerCase"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \{ \text{undefined}, \text{null} \} \wedge s_{this} = \text{ToString}(\text{ToPrimitive}(v)) \\
&\quad \wedge s = \text{native.string.toLowerCase}(s_{this}) \quad // \text{java, scala}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.toLocaleLowerCase"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \{ \text{undefined}, \text{null} \} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.toLocaleLowerCase"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \{ \text{undefined}, \text{null} \} \wedge s_{this} = \text{ToString}(\text{ToPrimitive}(v)) \\
&\quad \wedge s = \text{native.string.toLocaleLowerCase}(s_{this}) \quad // \text{java, scala}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.toUpperCase"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \{ \text{undefined}, \text{null} \} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.toUpperCase"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \{ \text{undefined}, \text{null} \} \wedge s_{this} = \text{ToString}(\text{ToPrimitive}(v)) \\
&\quad \wedge s = \text{native.string.toUpperCase}(s_{this}) \quad // \text{java, scala}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.toLocaleUpperCase"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \{ \text{undefined}, \text{null} \} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.toLocaleUpperCase"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \{ \text{undefined}, \text{null} \} \wedge s_{this} = \text{ToString}(\text{ToPrimitive}(v)) \\
&\quad \wedge s = \text{native.string.toLocaleUpperCase}(s_{this}) \quad // \text{java, scala}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.trim"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \{ \text{undefined}, \text{null} \} \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_1 = H[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"String.prototype.trim"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\
\text{where } v &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \{ \text{undefined}, \text{null} \} \wedge s_{this} = \text{ToString}(\text{ToPrimitive}(v)) \\
&\quad \wedge s = \text{native.string.trim}(s_{this}) \quad // \text{java, scala}
\end{aligned}$$

### 11.1.11 Boolean

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Boolean.constructor"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
\text{where } v &= \text{getArgValue}(args, "0") \wedge l = \text{NewLocation}() \\
&\quad \wedge o = \text{NewBoolean}(\text{toBoolean}(\text{toPrimitive}(v))) \wedge H_1 = H[l \mapsto o]
\end{aligned}$$



### 11.1.12 Boolean.prototype

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltintCall}(\text{"Boolean.prototype.toString"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \text{Boolean} \wedge (v \notin \text{Loc} \vee (v \in \text{Loc} \wedge H(v)(@class) \neq \text{"Boolean"})) \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\text{BuiltintCall}(\text{"Boolean.prototype.toString"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge b = \begin{cases} v & \text{if } v \in \text{Boolean} \\ H(v)(@primitive) & \text{if } v \in \text{Loc} \wedge H(v)(@class) = \text{"Boolean"} \end{cases} \\
&\quad \wedge s = \begin{cases} \text{"true"} & \text{if } b = \text{true} \\ \text{"false"} & \text{if } b = \text{false} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltintCall}(\text{"Boolean.prototype.valueOf"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \text{Boolean} \wedge (v \notin \text{Loc} \vee (v \in \text{Loc} \wedge H(v)(@class) \neq \text{"Boolean"})) \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\text{BuiltintCall}(\text{"Boolean.prototype.valueOf"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto b]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge b = \begin{cases} v & \text{if } v \in \text{Boolean} \\ H(v)(@primitive) & \text{if } v \in \text{Loc} \wedge H(v)(@class) = \text{"Boolean"} \end{cases}
\end{aligned}$$

### 11.1.13 Number

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltintCall}(\text{"Number.constructor"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } \text{getArgValue}(args, \text{"length"}) < 1 \wedge l = \text{NewLocation}() \wedge o = \text{NewNumber}(0) \wedge H_1 = H[l \mapsto o] \\
\mathcal{I}_{cp}[\text{BuiltintCall}(\text{"Number.constructor"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge \text{getArgValue}(args, \text{"length"}) \geq 1 \wedge l = \text{NewLocation}() \\
&\quad \wedge o = \text{NewNumber}(\text{toNumber}(\text{toPrimitive}(v))) \wedge H_1 = H[l \mapsto o]
\end{aligned}$$

### 11.1.14 Number.prototype

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltintCall}(\text{"Number.prototype.valueOf"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \text{Number} \wedge (v \notin \text{Loc} \vee (v \in \text{Loc} \wedge H(v)(@class) \neq \text{"Number"})) \\
&\quad \wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\text{BuiltintCall}(\text{"Number.prototype.valueOf"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto n]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge n = \begin{cases} v & \text{if } v \in \text{Number} \\ H(v)(@primitive) & \text{if } v \in \text{Loc} \wedge H(v)(@class) = \text{"Number"} \end{cases}
\end{aligned}$$

### 11.1.15 Math

$$\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Number.abs"}, args)]\!](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n_2]], A)$$

where  $n_1 = \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, "0")))$

$$n_2 = \begin{cases} \text{NaN} & \text{if } n_1 = \text{NaN} \\ \text{Inf} & \text{if } n_1 \in \{ -\text{Inf}, \text{Inf} \} \\ -n_1 & \text{if } v < 0 \\ n_1 & \text{if } 0 \leq v \end{cases}$$

$$\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Number.acos"}, args)]\!](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n_2]], A)$$

where  $n_1 = \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, "0")))$

$$n_2 = \begin{cases} \text{NaN} & \text{if } n_1 \in \{ \text{NaN}, \text{Inf}, -\text{Inf}, n \mid n < -1 \vee 1 < n \} \\ \text{native.acos}(n_1) & \text{otherwise} \end{cases}$$

$$\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Number.asin"}, args)]\!](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n_2]], A)$$

where  $n_1 = \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, "0")))$

$$n_2 = \begin{cases} \text{NaN} & \text{if } n_1 \in \{ \text{NaN}, \text{Inf}, -\text{Inf}, n \mid n < -1 \vee 1 < n \} \\ \text{native.asin}(n_1) & \text{otherwise} \end{cases}$$

$$\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Number.atan"}, args)]\!](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n_2]], A)$$

where  $n_1 = \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, "0")))$

$$n_2 = \begin{cases} \text{NaN} & \text{if } n_1 = \text{NaN} \\ \frac{\pi}{2} & \text{if } n_1 = \text{Inf} \\ -\frac{\pi}{2} & \text{if } n_1 = -\text{Inf} \\ \text{native.atan}(n_1) & \text{otherwise} \end{cases}$$

$$\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Number.atan2"}, args)]\!](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n_3]], A)$$

where  $n_1 = \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, "0")))$   $\wedge$   $n_2 = \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, "1")))$

$$n_3 = \begin{cases} \text{NaN} & \text{if } n_1 = \text{NaN} \vee n_2 = \text{NaN} \\ 0 & \text{if } n_1 = n \wedge n_2 = \text{Inf} \\ +0 & \text{if } n_1 > 0 \wedge n_1 \notin \{ -\text{Inf}, \text{Inf} \} \wedge n_2 = \text{Inf} \\ \pi & \text{if } n_1 > 0 \wedge n_1 \notin \{ -\text{Inf}, \text{Inf} \} \wedge n_2 = -\text{Inf} \\ -0 & \text{if } n_1 < 0 \wedge n_1 \notin \{ -\text{Inf}, \text{Inf} \} \wedge n_2 = \text{Inf} \\ -\pi & \text{if } n_1 < 0 \wedge n_1 \notin \{ -\text{Inf}, \text{Inf} \} \wedge n_2 = -\text{Inf} \\ \frac{\pi}{2} & \text{if } n_1 = \text{Inf} \wedge n_2 \notin \{ -\text{Inf}, \text{Inf} \} \\ -\frac{\pi}{2} & \text{if } n_1 = -\text{Inf} \wedge n_2 \notin \{ -\text{Inf}, \text{Inf} \} \\ \frac{\pi}{4} & \text{if } n_1 = \text{Inf} \wedge n_2 = \text{Inf} \\ \frac{3\pi}{4} & \text{if } n_1 = \text{Inf} \wedge n_2 = -\text{Inf} \\ -\frac{\pi}{4} & \text{if } n_1 = -\text{Inf} \wedge n_2 = \text{Inf} \\ -\frac{3\pi}{4} & \text{if } n_1 = -\text{Inf} \wedge n_2 = -\text{Inf} \\ \text{native.atan2}(n_1) & \text{otherwise} \end{cases}$$

$$\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Number.ceil"}, args)]\!](H, A) = (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n_2]], A)$$

where  $n_1 = \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, "0")))$

$$n_2 = \begin{cases} n_1 & \text{if } n_1 \in \{ \text{NaN}, \text{Inf}, -\text{Inf} \} \\ \text{native.ceil}(n_1) & \text{otherwise} \end{cases}$$

$$\begin{aligned} \mathcal{I}_{cp}[\llbracket \text{BuiltinCall}(\text{"Number.cos"}, args) \rrbracket](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n_2]], A) \\ \text{where } n_1 &= \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, \text{"0"}))) \\ n_2 &= \begin{cases} \text{NaN} & \text{if } n_1 \in \{ \text{NaN}, \text{Inf}, -\text{Inf} \} \\ \text{native.cos}(n_1) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp}[\llbracket \text{BuiltinCall}(\text{"Number.exp"}, args) \rrbracket](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n_2]], A) \\ \text{where } n_1 &= \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, \text{"0"}))) \\ n_2 &= \begin{cases} n_1 & \text{if } n_1 \in \{ \text{NaN}, \text{Inf} \} \\ 0 & \text{if } n_1 = -\text{Inf} \\ \text{native.exp}(n_1) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp}[\llbracket \text{BuiltinCall}(\text{"Number.floor"}, args) \rrbracket](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n_2]], A) \\ \text{where } n_1 &= \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, \text{"0"}))) \\ n_2 &= \begin{cases} n_1 & \text{if } n_1 \in \{ \text{NaN}, \text{Inf}, -\text{Inf} \} \\ \text{native.floor}(n_1) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp}[\llbracket \text{BuiltinCall}(\text{"Number.log"}, args) \rrbracket](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n_2]], A) \\ \text{where } n_1 &= \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, \text{"0"}))) \\ n_2 &= \begin{cases} \text{NaN} & \text{if } n_1 \in \{ \text{NaN}, -\text{Inf}, n \mid n < 0 \} \\ \text{Inf} & \text{if } n_1 = \text{Inf} \\ -\text{Inf} & \text{if } n_1 = 0 \\ \text{native.log}(n_1) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp}[\llbracket \text{BuiltinCall}(\text{"Number.max"}, args) \rrbracket](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n]], A) \\ \text{where } v_{len} &= \text{getArgValue}(args, \text{"length"}) \wedge n_i = \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, \text{"i"}))) \\ n &= \begin{cases} -\text{Inf} & \text{if } v_{len} = 0 \\ \text{NaN} & \text{if } \exists i \in \{0, \dots, v_{len}\} : n_i = \text{NaN} \\ n_{i_1} & \text{if } \exists i_1 \in \{0, \dots, v_{len}\} : \forall i_2 \in \{0, \dots, v_{len}\} : n_{i_1} \geq n_{i_2} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp}[\llbracket \text{BuiltinCall}(\text{"Number.min"}, args) \rrbracket](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n]], A) \\ \text{where } v_{len} &= \text{getArgValue}(args, \text{"length"}) \wedge n_i = \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, \text{"i"}))) \\ n &= \begin{cases} -\text{Inf} & \text{if } v_{len} = 0 \\ \text{NaN} & \text{if } \exists i \in \{0, \dots, v_{len}\} : n_i = \text{NaN} \\ n_{i_1} & \text{if } \exists i_1 \in \{0, \dots, v_{len}\} : \forall i_2 \in \{0, \dots, v_{len}\} : n_{i_1} \leq n_{i_2} \end{cases} \end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Number.pow"}, args)]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n_3]], A) \\
\text{where } n_1 &= \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, "0"))) \wedge n_2 = \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, "1"))) \\
n_3 &= \begin{cases} \text{NaN} & \text{if } n_2 = \text{NaN} \\ 1 & \text{if } n_2 = 0 \\ \text{NaN} & \text{if } n_1 = \text{NaN} \wedge n_2 \neq 0 \\ \text{Inf} & \text{if } (n_1 > 1 \vee -n_1 > 1) \wedge n_2 = \text{Inf} \\ 0 & \text{if } (n_1 > 1 \vee -n_1 > 1) \wedge n_2 = -\text{Inf} \\ \text{NaN} & \text{if } (n_1 == 1 \vee -n_1 == 1) \wedge v_{y1} \in \{ \text{Inf}, -\text{Inf} \} \\ 0 & \text{if } (n_1 < 1 \vee -n_1 < 1) \wedge v_{y1} = \text{Inf} \\ \text{Inf} & \text{if } (n_1 < 1 \vee -n_1 < 1) \wedge v_{y1} = -\text{Inf} \\ \text{Inf} & \text{if } n_1 = \text{Inf} \wedge n_2 > 0 \\ 0 & \text{if } n_1 = \text{Inf} \wedge n_2 < 0 \\ -\text{Inf} & \text{if } n_1 = -\text{Inf} \wedge n_2 > 0 \wedge n_2 \neq \text{Inf} \wedge n_2 \% 2 = 1 \\ \text{Inf} & \text{if } n_1 = -\text{Inf} \wedge n_2 > 0 \wedge n_2 \neq \text{Inf} \wedge n_2 \% 2 = 0 \\ 0 & \text{if } n_1 = -\text{Inf} \wedge v_{y1} < 0 \\ 0 & \text{if } n_1 = 0 \wedge n_2 > 0 \\ \text{Inf} & \text{if } n_1 = 0 \wedge n_2 < 0 \\ \text{NaN} & \text{if } v_{x1} < 0 \wedge v_{x1} \neq -\text{Inf} \wedge v_{y1} \neq \{ \text{Inf}, -\text{Inf} \} \wedge \neg \text{isInt}(v_{y1}) \\ \text{native.pow}(n_1) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Number.random"}, args)]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n]], A) \\
\text{where } n &= \text{native.random}()
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Number.round"}, args)]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n_2]], A) \\
\text{where } n_1 &= \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, "0"))) \\
n_2 &= \begin{cases} n_1 & \text{if } n_1 \in \{ \text{NaN}, \text{Inf}, -\text{Inf} \} \\ \text{native.round}(n_1) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Number.sin"}, args)]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n_2]], A) \\
\text{where } n_1 &= \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, "0"))) \\
n_2 &= \begin{cases} \text{NaN} & \text{if } n_1 \in \{ \text{NaN}, \text{Inf}, -\text{Inf} \} \\ \text{native.sin}(n_1) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Number.sqrt"}, args)]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n_2]], A) \\
\text{where } n_1 &= \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, "0"))) \\
n_2 &= \begin{cases} n_1 & \text{if } n_1 \in \{ \text{NaN}, \text{Inf} \} \\ \text{NaN} & \text{if } n_1 < 0 \vee n_1 = -\text{Inf} \\ \text{native.sqrt}(n_1) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Number.tan"}, args)]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto n_2]], A) \\
\text{where } n_1 &= \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, "0"))) \\
n_2 &= \begin{cases} \text{NaN} & \text{if } n_1 \in \{ \text{NaN}, \text{Inf}, -\text{Inf} \} \\ \text{native.tan}(n_1) & \text{otherwise} \end{cases}
\end{aligned}$$

### 11.1.16 Date

$$\begin{aligned}
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.constructor"}, \text{args}) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)][@return \mapsto l], A) \\
&\text{where } \text{getArgValue}(\text{args}, \text{"length"}) = 0 \\
&\quad \wedge n = \text{native.Calendar.getInstance().getTimeInMillis()} \quad // \text{java, scala} \\
&\quad \wedge o = \text{NewDateObject}(n) \wedge l = \text{newLocation}() \wedge H_1 = H[l \mapsto o] \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.constructor"}, \text{args}) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)][@return \mapsto l], A) \\
&\text{where } \text{getArgValue}(\text{args}, \text{"length"}) = 1 \wedge v = \text{getArgValue}(\text{args}, \text{"0"}) \wedge v \in \text{String} \\
&\quad \wedge o = \text{NewDateObject}(v) \wedge l = \text{newLocation}() \wedge H_1 = H[l \mapsto o] \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.constructor"}, \text{args}) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)][@return \mapsto l], A) \\
&\text{where } \text{getArgValue}(\text{args}, \text{"length"}) = 1 \wedge v = \text{getArgValue}(\text{args}, \text{"0"}) \wedge v \notin \text{String} \\
&\quad \wedge n = \text{ToNumber}(\text{ToPrimitive}(v)) \wedge o = \text{NewDateObject}(\text{TimeClip}(n)) \wedge l = \text{newLocation}() \wedge H_1 = H[l \mapsto o] \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.constructor"}, \text{args}) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)][@return \mapsto l], A) \\
&\text{where } n_{arglen} = \text{getArgValue}(\text{args}, \text{"length"}) \wedge n_{arglen} > 1 \\
&\quad \wedge n_1 = \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(\text{args}, \text{"0"}))) \\
&\quad \wedge n_{year} = \begin{cases} n_1 + 1900 & \text{if } n_1 \neq \text{NaN} \wedge 0 \leq n_1 \wedge n_1 \leq 99 \\ n_1 & \text{otherwise} \end{cases} \\
&\quad \wedge n_{month} = \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(\text{args}, \text{"1"}))) \\
&\quad \wedge n_{date} = \begin{cases} \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(\text{args}, \text{"2"}))) & \text{if } n_{arglen} > 2 \\ 1 & \text{otherwise} \end{cases} \\
&\quad \wedge n_{hour} = \begin{cases} \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(\text{args}, \text{"3"}))) & \text{if } n_{arglen} > 3 \\ 0 & \text{otherwise} \end{cases} \\
&\quad \wedge n_{min} = \begin{cases} \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(\text{args}, \text{"4"}))) & \text{if } n_{arglen} > 4 \\ 0 & \text{otherwise} \end{cases} \\
&\quad \wedge n_{sec} = \begin{cases} \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(\text{args}, \text{"5"}))) & \text{if } n_{arglen} > 5 \\ 0 & \text{otherwise} \end{cases} \\
&\quad \wedge n_{ms} = \begin{cases} \text{ToNumber}(\text{ToPrimitive}(\text{getArgValue}(\text{args}, \text{"6"}))) & \text{if } n_{arglen} > 6 \\ 0 & \text{otherwise} \end{cases} \\
&\quad \wedge n = \text{MakeDate}(\text{MakeDay}(n_{year}, n_{month}, n_{date}), \text{MakeTime}(n_{hour}, n_{min}, n_{sec}, n_{ms})) \\
&\quad \wedge o = \text{NewDateObject}(v) \wedge l = \text{newLocation}() \wedge H_1 = H[l \mapsto o] \\
\mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.now"}, \text{args}) \rrbracket (H, A) &= (H[\#temp \mapsto H(\#temp)][@return \mapsto n], A) \\
&\text{where } n = \text{native.Calendar.getInstance().getTimeInMillis()} \quad // \text{java, scala}
\end{aligned}$$

### 11.1.17 Date.prototype

$$\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Date.prototype.toString"}, args)]\!](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\ \text{where } v_1 = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v_2 = H(v_1)(@primitive) \wedge s = (\text{native.util.Date}(v_2)).toString()$$

$$\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Date.prototype.toString"}, args)]\!](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\ \text{where } v_1 = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v_2 = H(v_1)(@primitive) \wedge s = (\text{native.util.Date}(v_2)).toString()$$

$$\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Date.prototype.toString"}, args)]\!](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\ \text{where } v_1 = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v_2 = H(v_1)(@primitive) \wedge s = (\text{native.util.Date}(v_2)).toString()$$

$$\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Date.prototype.toString"}, args)]\!](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\ \text{where } v_1 = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v_2 = H(v_1)(@primitive) \wedge s = (\text{native.util.Date}(v_2)).toString()$$

$$\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Date.prototype.toString"}, args)]\!](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\ \text{where } v_1 = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v_2 = H(v_1)(@primitive) \wedge s = (\text{native.util.Date}(v_2)).toString()$$

$$\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Date.prototype.toString"}, args)]\!](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto s]], A) \\ \text{where } v_1 = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v_2 = H(v_1)(@primitive) \wedge s = (\text{native.util.Date}(v_2)).toString()$$

$$\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Date.prototype.toString"}, args)]\!](H, A) = (H[\#temp \mapsto 1(\#temp)[@return \mapsto v_2]], A) \\ \text{where } v_1 = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v_2 = H(v_1)(@primitive)$$

$$\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Date.prototype.toString"}, args)]\!](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto v_2]], A) \\ \text{where } v_1 = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v_2 = H(v_1)(@primitive)$$

$$\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Date.prototype.toString"}, args)]\!](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v = \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).get(YEAR) & \text{otherwise} \end{cases}$$

$$\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Date.prototype.toString"}, args)]\!](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v = \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).get(YEAR) & \text{otherwise} \end{cases}$$

$$\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Date.prototype.toString"}, args)]\!](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v = \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).get(MONTH) & \text{otherwise} \end{cases}$$

$$\mathcal{I}_{cp}[\![\text{BuiltintCall}(\text{"Date.prototype.toString"}, args)]\!](H, A) = (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} = \mathcal{V}_{cp}[\![\text{this}]\!](H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v = \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).get(MONTH) & \text{otherwise} \end{cases}$$

$$\begin{aligned} \mathcal{I}_{cp}[\text{BuiltintCall}(\text{"Date.prototype.getDate"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v &= \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).\text{get}(\text{DAY\_OF\_MONTH}) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp}[\text{BuiltintCall}(\text{"Date.prototype.getUTCDate"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v &= \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).\text{get}(\text{DAY\_OF\_MONTH}) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp}[\text{BuiltintCall}(\text{"Date.prototype.getDay"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v &= \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).\text{get}(\text{DAY\_OF\_WEEK}) - 1 & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp}[\text{BuiltintCall}(\text{"Date.prototype.getUTCDay"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v &= \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).\text{get}(\text{DAY\_OF\_WEEK}) - 1 & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp}[\text{BuiltintCall}(\text{"Date.prototype.getHours"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v &= \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).\text{get}(\text{HOURS}) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp}[\text{BuiltintCall}(\text{"Date.prototype.getUTCHours"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v &= \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).\text{get}(\text{HOURS}) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp}[\text{BuiltintCall}(\text{"Date.prototype.getMinutes"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v &= \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).\text{get}(\text{MINUTE}) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp}[\text{BuiltintCall}(\text{"Date.prototype.getUTCMinutes"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp}[\text{this}](H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v &= \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).\text{get}(\text{MINUTE}) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.getMinutes"}, args) \rrbracket (H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v &= \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).get(MINUTE) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.getUTCMinutes"}, args) \rrbracket (H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v &= \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).get(MINUTE) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.getSeconds"}, args) \rrbracket (H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v &= \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).get(SECOND) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.getUTCSeconds"}, args) \rrbracket (H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v &= \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).get(SECOND) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.getMilliseconds"}, args) \rrbracket (H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v &= \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).get(MILLISECOND) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.getUTCMilliseconds"}, args) \rrbracket (H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v &= \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).get(MILLISECOND) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.getTimeZoneOffset"}, args) \rrbracket (H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \\ v &= \begin{cases} \text{NaN} & \text{if } v_{time} = \text{NaN} \\ \text{native.Calendar}(v_{time}).get(ZONE_OFFSET) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.setTime"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v = \text{ToNumber}(\text{getArgValue}(args, \text{"0"})) \\ &\wedge H_1 = H[v_{this} \mapsto H(v_{this})[@ \mapsto v]] \end{aligned}$$



$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.setMilliseconds"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \wedge v_{arg} = \text{ToNumber}(\text{getArgValue}(args, \text{"0"})) \\ &\wedge v = \text{native.Calendar}(v_{time}).\text{set}(\text{MILLISECOND}, v_{arg}).\text{getTimeInMillis}() \\ &\wedge H_1 = H[v_{this} \mapsto H(v_{this})[@ \mapsto v]] \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.setUTCMilliseconds"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \wedge v_{arg} = \text{ToNumber}(\text{getArgValue}(args, \text{"0"})) \\ &\wedge v = \text{native.Calendar}(v_{time}).\text{set}(\text{MILLISECOND}, v_{arg}).\text{getTimeInMillis}() \\ &\wedge H_1 = H[v_{this} \mapsto H(v_{this})[@ \mapsto v]] \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.setSeconds"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \wedge v_{arg} = \text{ToNumber}(\text{getArgValue}(args, \text{"0"})) \\ &\wedge v = \text{native.Calendar}(v_{time}).\text{set}(\text{SECOND}, v_{arg}).\text{getTimeInMillis}() \\ &\wedge H_1 = H[v_{this} \mapsto H(v_{this})[@ \mapsto v]] \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.setUTCSeconds"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \wedge v_{arg} = \text{ToNumber}(\text{getArgValue}(args, \text{"0"})) \\ &\wedge v = \text{native.Calendar}(v_{time}).\text{set}(\text{SECOND}, v_{arg}).\text{getTimeInMillis}() \\ &\wedge H_1 = H[v_{this} \mapsto H(v_{this})[@ \mapsto v]] \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.setMinutes"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \wedge v_{arg} = \text{ToNumber}(\text{getArgValue}(args, \text{"0"})) \\ &\wedge v = \text{native.Calendar}(v_{time}).\text{set}(\text{MINUTE}, v_{arg}).\text{getTimeInMillis}() \\ &\wedge H_1 = H[v_{this} \mapsto H(v_{this})[@ \mapsto v]] \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.setUTCMinutes"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \wedge v_{arg} = \text{ToNumber}(\text{getArgValue}(args, \text{"0"})) \\ &\wedge v = \text{native.Calendar}(v_{time}).\text{set}(\text{MINUTE}, v_{arg}).\text{getTimeInMillis}() \\ &\wedge H_1 = H[v_{this} \mapsto H(v_{this})[@ \mapsto v]] \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.setHours"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \wedge v_{arg} = \text{ToNumber}(\text{getArgValue}(args, \text{"0"})) \\ &\wedge v = \text{native.Calendar}(v_{time}).\text{set}(\text{HOURS}, v_{arg}).\text{getTimeInMillis}() \\ &\wedge H_1 = H[v_{this} \mapsto H(v_{this})[@ \mapsto v]] \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.setUTCHours"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \wedge v_{arg} = \text{ToNumber}(\text{getArgValue}(args, \text{"0"})) \\ &\wedge v = \text{native.Calendar}(v_{time}).\text{set}(\text{HOURS}, v_{arg}).\text{getTimeInMillis}() \\ &\wedge H_1 = H[v_{this} \mapsto H(v_{this})[@ \mapsto v]] \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setDate"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \wedge v_{arg} = \text{ToNumber}(\text{getArgValue}(args, \text{"0"})) \\ &\wedge v = \text{native.Calendar}(v_{time}).\text{set}(\text{DAY\_OF\_MONTH}, v_{arg}).\text{getTimeInMillis}() \\ &\wedge H_1 = H[v_{this} \mapsto H(v_{this})[@ \mapsto v]] \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setUTCDate"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \wedge v_{arg} = \text{ToNumber}(\text{getArgValue}(args, \text{"0"})) \\ &\wedge v = \text{native.Calendar}(v_{time}).\text{set}(\text{DAY\_OF\_MONTH}, v_{arg}).\text{getTimeInMillis}() \\ &\wedge H_1 = H[v_{this} \mapsto H(v_{this})[@ \mapsto v]] \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setMonth"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \wedge v_{arg} = \text{ToNumber}(\text{getArgValue}(args, \text{"0"})) \\ &\wedge v = \text{native.Calendar}(v_{time}).\text{set}(\text{MONTH}, v_{arg}).\text{getTimeInMillis}() \\ &\wedge H_1 = H[v_{this} \mapsto H(v_{this})[@ \mapsto v]] \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setUTCMonth"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \wedge v_{arg} = \text{ToNumber}(\text{getArgValue}(args, \text{"0"})) \\ &\wedge v = \text{native.Calendar}(v_{time}).\text{set}(\text{MONTH}, v_{arg}).\text{getTimeInMillis}() \\ &\wedge H_1 = H[v_{this} \mapsto H(v_{this})[@ \mapsto v]] \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setFullYear"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \wedge v_{arg} = \text{ToNumber}(\text{getArgValue}(args, \text{"0"})) \\ &\wedge v = \text{native.Calendar}(v_{time}).\text{set}(\text{YEAR}, v_{arg}).\text{getTimeInMillis}() \\ &\wedge H_1 = H[v_{this} \mapsto H(v_{this})[@ \mapsto v]] \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setUTCFullYear"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto v]], A) \\ \text{where } v_{this} &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_{time} = H(v_{this})(@primitive) \wedge v_{arg} = \text{ToNumber}(\text{getArgValue}(args, \text{"0"})) \\ &\wedge v = \text{native.Calendar}(v_{time}).\text{set}(\text{YEAR}, v_{arg}).\text{getTimeInMillis}() \\ &\wedge H_1 = H[v_{this} \mapsto H(v_{this})[@ \mapsto v]] \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toUTCString"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto s]], A) \\ \text{where } v_1 &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_2 = H(v_1)(@primitive) \wedge s = (\text{native.util.Date}(v_2)).\text{toString}() \end{aligned}$$

$$\begin{aligned} \mathcal{I}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toISOString"}, args) \rrbracket (H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto s]], A) \\ \text{where } v_1 &= \mathcal{V}_{cp} \llbracket \text{this} \rrbracket (H, A) \wedge v_2 = H(v_1)(@primitive) \wedge s = (\text{native.util.Date}(v_2)).\text{toString}() \end{aligned}$$

### 11.1.18 RegExp

$$\begin{aligned}
& \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"RegExp"}, args) \rrbracket (H, A) = (H_1, A) \\
& \quad \text{if } v_1 \in \text{Loc} \wedge H(v_1)(\text{@class}) = \text{"RegExp"} \wedge v_2 = \text{undefined} \\
& \quad \quad \text{where } v_1 = \text{getArgValue}(args, \text{"0"}) \wedge v_2 = \text{getArgValue}(args, \text{"1"}) \\
& \quad \quad \quad \wedge H_1 = H[\#temp \mapsto H(\#temp)[\text{@return} \mapsto v_1]] \\
& \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"RegExp"}, args) \rrbracket (H, A) = \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"RegExp.constructor"}, args) \rrbracket (H, A) \\
\\
& \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"RegExp.constructor"}, args) \rrbracket (H, A) = (H_2, A) \\
& \quad \text{if } v_1 \in \text{Loc} \wedge H(v_1)(\text{@class}) = \text{"RegExp"} \wedge v_2 = \text{undefined} \\
& \quad \quad \text{where } v_1 = \text{getArgValue}(args, \text{"0"}) \wedge v_2 = \text{getArgValue}(args, \text{"1"}) \\
& \quad \quad \quad \wedge v_{source} = H(v_1)(\text{"source"}) \\
& \quad \quad \quad \wedge b_g = H(v_1)(\text{"global"}) \\
& \quad \quad \quad \wedge b_i = H(v_1)(\text{"ignoreCase"}) \\
& \quad \quad \quad \wedge b_m = H(v_1)(\text{"multiline"}) \\
& \quad \quad \quad \wedge mid = H(v_1)(\text{@matcher}) \\
& \quad \quad \quad \wedge o = \text{NewRegExp}(v_{source}, b_g, b_i, b_m, mid) \\
& \quad \quad \quad \wedge l = \text{NewLocation}() \\
& \quad \quad \quad \wedge H_1 = H[l \mapsto o] \\
& \quad \quad \quad \wedge H_2 = H_1[\#temp \mapsto H_1(\#temp)[\text{@return} \mapsto l]] \\
& \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"RegExp.constructor"}, args) \rrbracket (H, A) = (H_1, A) \\
& \quad \text{if } v_1 \in \text{Loc} \wedge H(v_1)(\text{@class}) = \text{"RegExp"} \wedge v_2 \neq \text{undefined} \\
& \quad \quad \text{where } v_1 = \text{getArgValue}(args, \text{"0"}) \wedge v_2 = \text{getArgValue}(args, \text{"1"}) \\
& \quad \quad \quad \wedge H_1 = \text{RaiseException}(H, \text{TypeError}) \\
& \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"RegExp.constructor"}, args) \rrbracket (H, A) = (H_1, A) \\
& \quad \text{if } v_1 \notin \text{Loc} \wedge v_{match} \in \text{MatcherId} \\
& \quad \quad \text{where } v_1 = \text{getArgValue}(args, \text{"0"}) \wedge v_2 = \text{getArgValue}(args, \text{"1"}) \\
& \quad \quad \quad \wedge v_P = \begin{cases} \text{""} & \text{if } v_1 = \text{undefined} \\ \text{toString}(v_1) & \text{otherwise} \end{cases} \\
& \quad \quad \quad \wedge v_F = \begin{cases} \text{""} & \text{if } v_2 = \text{undefined} \\ \text{toString}(v_2) & \text{otherwise} \end{cases} \\
& \quad \quad \quad \wedge v_{match} = \text{RegExpParser}(v_P, v_F) \\
& \quad \quad \quad \wedge o = \text{NewRegExp}(v_{source}, b_g, b_i, b_m, v_{match}) \\
& \quad \quad \quad \wedge l = \text{NewLocation}() \\
& \quad \quad \quad \wedge H_1 = H[l \mapsto o] \\
& \mathcal{I}_{cp} \llbracket \text{BuiltinCall}(\text{"RegExp.constructor"}, args) \rrbracket (H, A) = (H_1, A) \\
& \quad \text{if } v_1 \notin \text{Loc} \wedge exc \in \text{Exception} \\
& \quad \quad \text{where } v_1 = \text{getArgValue}(args, \text{"0"}) \wedge v_2 = \text{getArgValue}(args, \text{"1"}) \\
& \quad \quad \quad \wedge v_P = \begin{cases} \text{""} & \text{if } v_1 = \text{undefined} \\ \text{toString}(v_1) & \text{otherwise} \end{cases} \\
& \quad \quad \quad \wedge v_F = \begin{cases} \text{""} & \text{if } v_2 = \text{undefined} \\ \text{toString}(v_2) & \text{otherwise} \end{cases} \\
& \quad \quad \quad \wedge exc = \text{RegExpParser}(v_P, v_F) \\
& \quad \quad \quad \wedge H_1 = \text{RaiseException}(H, exc)
\end{aligned}$$

### 11.1.19 RegExp.prototype

$$\begin{aligned}
& \mathcal{I}_{cp}[\text{BuiltinCall}(\text{"RegExp.prototype.exec"}, args)](H, A) = (H_3, A) \\
& \text{if } v_{exec} \in \text{Object} \times \text{Int} \\
& \text{where } v_1 = \text{getArgValue}(args, \text{"0"}) \\
& \quad \wedge v_R = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v_S = \text{toString}(v_1) \\
& \quad \wedge v_{lastIndex} = H(v_R)(\text{"lastIndex"}) \wedge i = \text{ToInteger}(v_{lastIndex}) \\
& \quad \wedge v_g = H(v_R)(\text{"global"}) \\
& \quad \wedge v_i = H(v_R)(\text{"ignoreCase"}) \\
& \quad \wedge v_m = H(v_R)(\text{"multiline"}) \\
& \quad \wedge mid = H(v_R)(\text{"@matcher"}) \\
& \quad \wedge v_{exec} = \text{exec}(mid, v_S, i, v_g, v_i, v_m) \\
& \quad \wedge l = \text{NewLocation}() \\
& \quad \wedge H_1 = H[l \mapsto v_{exec}.1] \\
& \quad \wedge H_2 = \begin{cases} H_1[v_R \mapsto H_1(v_R)[\text{"lastIndex"} \mapsto v_{exec}.2]] & \text{if } v_g = \text{true} \\ H_1 & \text{otherwise} \end{cases} \\
& \quad \wedge H_3 = H_2[\#temp \mapsto H_1(\#temp)[\text{@return} \mapsto l]] \\
& \mathcal{I}_{cp}[\text{BuiltinCall}(\text{"RegExp.prototype.exec"}, args)](H, A) = (H_1, A) \\
& \text{if } v_{exec} = \text{null} \\
& \text{where } v_1 = \text{getArgValue}(args, \text{"0"}) \\
& \quad \wedge v_R = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v_S = \text{toString}(v_1) \\
& \quad \wedge v_{lastIndex} = H(v_R)(\text{"lastIndex"}) \wedge i = \text{ToInteger}(v_{lastIndex}) \\
& \quad \wedge v_g = H(v_R)(\text{"global"}) \\
& \quad \wedge v_i = H(v_R)(\text{"ignoreCase"}) \\
& \quad \wedge v_m = H(v_R)(\text{"multiline"}) \\
& \quad \wedge mid = H(v_R)(\text{"@matcher"}) \\
& \quad \wedge v_{exec} = \text{exec}(mid, v_S, i, v_g, v_i, v_m) \\
& \quad \wedge H_1 = H[\#temp \mapsto H_1(\#temp)[\text{@return} \mapsto \text{null}]] \\
& \mathcal{I}_{cp}[\text{BuiltinCall}(\text{"RegExp.prototype.exec"}, args)](H, A) = (H_1, A) \\
& \text{where } v_1 = \text{getArgValue}(args, \text{"0"}) \\
& \quad \wedge v_R = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v_S = \text{toString}(v_1) \\
& \quad \wedge v_{lastIndex} = H(v_R)(\text{"lastIndex"}) \wedge i = \text{ToInteger}(v_{lastIndex}) \\
& \quad \wedge v_g = H(v_R)(\text{"global"}) \\
& \quad \wedge v_i = H(v_R)(\text{"ignoreCase"}) \\
& \quad \wedge v_m = H(v_R)(\text{"multiline"}) \\
& \quad \wedge mid = H(v_R)(\text{"@matcher"}) \\
& \quad \wedge v_{exec} = \text{exec}(mid, v_S, i, v_g, v_i, v_m) \\
& \quad \wedge v_{return} = \begin{cases} \text{true} & \text{if } v_{exec} \neq \text{null} \\ \text{false} & \text{otherwise} \end{cases} \\
& \quad \wedge H_1 = H[\#temp \mapsto H_1(\#temp)[\text{@return} \mapsto v_{return}]] \\
& \mathcal{I}_{cp}[\text{BuiltinCall}(\text{"RegExp.prototype.toString"}, args)](H, A) = (H_1, A) \\
& \text{where } v_R = \mathcal{V}_{cp}[\text{this}](H, A) \\
& \quad \wedge v_{src} = H(v_R)(\text{"source"}) \\
& \quad \wedge v_g = H(v_R)(\text{"global"}) \\
& \quad \wedge v_i = H(v_R)(\text{"ignoreCase"}) \\
& \quad \wedge v_m = H(v_R)(\text{"multiline"}) \\
& \quad \wedge s_1 = \begin{cases} "g" & \text{if } v_g = \text{true} \\ "" & \text{otherwise} \end{cases} \\
& \quad \wedge s_2 = \begin{cases} "i" & \text{if } v_i = \text{true} \\ "" & \text{otherwise} \end{cases} \\
& \quad \wedge s_3 = \begin{cases} "m" & \text{if } v_m = \text{true} \\ "" & \text{otherwise} \end{cases} \\
& \quad \wedge v_{return} = "/" + v_{src} + "/" + s_1 + s_2 + s_3 \\
& \quad \wedge H_1 = H[\#temp \mapsto H_1(\#temp)[\text{@return} \mapsto v_{return}]]
\end{aligned}$$

### 11.1.20 Error

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Error.constructor"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } \text{getArgValue}(args, \text{"length"}) < 1 \wedge l = \text{NewLocation}() \\
&\quad \wedge o = \left\{ \begin{array}{l} @class \mapsto \text{"Error"}, \quad @proto \mapsto \#ErrorProto, \\ @extensible \mapsto \text{true} \end{array} \right\} \wedge H_1 = H[l \mapsto o] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Error.constructor"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge \text{getArgValue}(args, \text{"length"}) \geq 1 \wedge l = \text{NewLocation}() \\
&\quad \wedge o = \left\{ \begin{array}{l} @class \mapsto \text{"Error"}, \quad @proto \mapsto \#ErrorProto, \\ @extensible \mapsto \text{true}, \quad message \mapsto \text{toString}(\text{toPrimitive}(v)) \end{array} \right\} \\
&\quad \wedge H_1 = H[l \mapsto o]
\end{aligned}$$

### 11.1.21 Error.prototype

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Error.prototype.toString"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@exception \mapsto l_e]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \notin \text{Loc} \wedge l_e = \text{newLocation}() \wedge H_2 = H_1[l_e \mapsto \text{NewExceptionObject}(\text{TypeError})] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Error.prototype.toString"}, args)](H, A) &= (H[\#temp \mapsto H(\#temp)[@return \mapsto s_3]], A) \\
&\text{where } v = \mathcal{V}_{cp}[\text{this}](H, A) \wedge v \in \text{Loc} \\
s_1 &= \begin{cases} H(v)(\text{"name"}) & \text{if } H(v)(\text{"name"}) \neq \text{undefined} \\ \text{"Error"} & \text{otherwise} \end{cases} \\
s_2 &= \begin{cases} \text{toString}(\text{toPrimitive}(H(v)(\text{"message"}))) & \text{if } H(v)(\text{"message"}) \neq \text{undefined} \\ "" & \text{otherwise} \end{cases} \\
s_3 &= \begin{cases} s_2 & \text{if } s_1 = "" \\ s_1 & \text{if } s_2 = "" \\ s_1 + " : " + s_2 & \text{otherwise} \end{cases}
\end{aligned}$$

### 11.1.22 EvalError

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Error.constructor"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } \text{getArgValue}(args, \text{"length"}) < 1 \wedge l = \text{NewLocation}() \\
&\quad \wedge o = \left\{ \begin{array}{l} @class \mapsto \text{"Error"}, \quad @proto \mapsto \#EvalErrorProto, \\ @extensible \mapsto \text{true} \end{array} \right\} \wedge H_1 = H[l \mapsto o] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Error.constructor"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge \text{getArgValue}(args, \text{"length"}) \geq 1 \wedge l = \text{NewLocation}() \\
&\quad \wedge o = \left\{ \begin{array}{l} @class \mapsto \text{"Error"}, \quad @proto \mapsto \#EvalErrorProto, \\ @extensible \mapsto \text{true}, \quad message \mapsto \text{toString}(\text{toPrimitive}(v)) \end{array} \right\} \\
&\quad \wedge H_1 = H[l \mapsto o]
\end{aligned}$$

### 11.1.23 RangeError

$$\begin{aligned}
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Error.constructor"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } \text{getArgValue}(args, \text{"length"}) < 1 \wedge l = \text{NewLocation}() \\
&\quad \wedge o = \left\{ \begin{array}{l} @class \mapsto \text{"Error"}, \quad @proto \mapsto \#RangeErrorProto, \\ @extensible \mapsto \text{true} \end{array} \right\} \wedge H_1 = H[l \mapsto o] \\
\mathcal{I}_{cp}[\text{BuiltinCall}(\text{"Error.constructor"}, args)](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge \text{getArgValue}(args, \text{"length"}) \geq 1 \wedge l = \text{NewLocation}() \\
&\quad \wedge o = \left\{ \begin{array}{l} @class \mapsto \text{"Error"}, \quad @proto \mapsto \#RangeErrorProto, \\ @extensible \mapsto \text{true}, \quad message \mapsto \text{toString}(\text{toPrimitive}(v)) \end{array} \right\} \\
&\quad \wedge H_1 = H[l \mapsto o]
\end{aligned}$$

### 11.1.24 ReferenceError

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Error.constructor"}, args)]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } \text{getArgValue}(args, \text{"length"}) < 1 \wedge l = \text{NewLocation}() \\
&\wedge o = \left\{ \begin{array}{l} @class \mapsto \text{"Error"}, \quad @proto \mapsto \#ReferenceErrorProto, \\ @extensible \mapsto \text{true} \end{array} \right\} \wedge H_1 = H[l \mapsto o] \\
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Error.constructor"}, args)]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge \text{getArgValue}(args, \text{"length"}) \geq 1 \wedge l = \text{NewLocation}() \\
&\wedge o = \left\{ \begin{array}{l} @class \mapsto \text{"Error"}, \quad @proto \mapsto \#ReferenceErrorProto, \\ @extensible \mapsto \text{true}, \quad message \mapsto \text{toString}(\text{toPrimitive}(v)) \end{array} \right\} \\
&\wedge H_1 = H[l \mapsto o]
\end{aligned}$$

### 11.1.25 SyntaxError

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Error.constructor"}, args)]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } \text{getArgValue}(args, \text{"length"}) < 1 \wedge l = \text{NewLocation}() \\
&\wedge o = \left\{ \begin{array}{l} @class \mapsto \text{"Error"}, \quad @proto \mapsto \#SyntaxErrorProto, \\ @extensible \mapsto \text{true} \end{array} \right\} \wedge H_1 = H[l \mapsto o] \\
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Error.constructor"}, args)]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge \text{getArgValue}(args, \text{"length"}) \geq 1 \wedge l = \text{NewLocation}() \\
&\wedge o = \left\{ \begin{array}{l} @class \mapsto \text{"Error"}, \quad @proto \mapsto \#SyntaxErrorProto, \\ @extensible \mapsto \text{true}, \quad message \mapsto \text{toString}(\text{toPrimitive}(v)) \end{array} \right\} \\
&\wedge H_1 = H[l \mapsto o]
\end{aligned}$$

### 11.1.26 TypeError

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Error.constructor"}, args)]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } \text{getArgValue}(args, \text{"length"}) < 1 \wedge l = \text{NewLocation}() \\
&\wedge o = \left\{ \begin{array}{l} @class \mapsto \text{"Error"}, \quad @proto \mapsto \#TypeErrorProto, \\ @extensible \mapsto \text{true} \end{array} \right\} \wedge H_1 = H[l \mapsto o] \\
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Error.constructor"}, args)]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge \text{getArgValue}(args, \text{"length"}) \geq 1 \wedge l = \text{NewLocation}() \\
&\wedge o = \left\{ \begin{array}{l} @class \mapsto \text{"Error"}, \quad @proto \mapsto \#TypeErrorProto, \\ @extensible \mapsto \text{true}, \quad message \mapsto \text{toString}(\text{toPrimitive}(v)) \end{array} \right\} \\
&\wedge H_1 = H[l \mapsto o]
\end{aligned}$$

### 11.1.27 URIError

$$\begin{aligned}
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Error.constructor"}, args)]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } \text{getArgValue}(args, \text{"length"}) < 1 \wedge l = \text{NewLocation}() \\
&\wedge o = \left\{ \begin{array}{l} @class \mapsto \text{"Error"}, \quad @proto \mapsto \#URIErrorProto, \\ @extensible \mapsto \text{true} \end{array} \right\} \wedge H_1 = H[l \mapsto o] \\
\mathcal{I}_{cp}[\![\text{BuiltinCall}(\text{"Error.constructor"}, args)]\!](H, A) &= (H_1[\#temp \mapsto H_1(\#temp)[@return \mapsto l]], A) \\
&\text{where } v = \text{getArgValue}(args, \text{"0"}) \wedge \text{getArgValue}(args, \text{"length"}) \geq 1 \wedge l = \text{NewLocation}() \\
&\wedge o = \left\{ \begin{array}{l} @class \mapsto \text{"Error"}, \quad @proto \mapsto \#URIErrorProto, \\ @extensible \mapsto \text{true}, \quad message \mapsto \text{toString}(\text{toPrimitive}(v)) \end{array} \right\} \\
&\wedge H_1 = H[l \mapsto o]
\end{aligned}$$

## 11.2 Abstract Semantics

### 11.2.1 Helper

$$\begin{aligned}
\widehat{\text{DefineProperty}} &: \widehat{\text{Heap}} \times \widehat{\text{Loc}} \times \widehat{\text{String}} \times \widehat{\text{Loc}} \rightarrow \widehat{\text{Heap}} \\
\widehat{\text{ToPropertyDescriptor}}(\hat{H}, \hat{l}_1, \hat{s}, \hat{l}_2) &= \hat{H}_1 \\
\text{where } \hat{H}_1 &= \hat{H}[\hat{l}_1 \mapsto \hat{H}(\hat{l}_1)[\hat{s} \mapsto \langle \hat{v}_{val}, \hat{b}_w, \hat{b}_e, \hat{b}_c \rangle]] \\
&\quad // \text{skip when AccessorDescriptor} \\
&\quad \wedge \hat{v}_{val} = \widehat{\text{Proto}}(\hat{H}, \hat{l}_2, \text{"value"}) \\
&\quad \wedge \hat{b}_w = \widehat{\text{toBoolean}}(\widehat{\text{Proto}}(\hat{H}, \hat{l}_2, \text{"writable"})) \\
&\quad \wedge \hat{b}_e = \widehat{\text{toBoolean}}(\widehat{\text{Proto}}(\hat{H}, \hat{l}_2, \text{"enumerable"})) \\
&\quad \wedge \hat{b}_c = \widehat{\text{toBoolean}}(\widehat{\text{Proto}}(\hat{H}, \hat{l}_2, \text{"configurable"}))
\end{aligned}$$

$$\begin{aligned}
\widehat{\text{TimeClip}} &: \widehat{\text{Number}} \rightarrow \widehat{\text{Number}} \\
\widehat{\text{TimeClip}}(\hat{n}) &= \begin{cases} \top_{\text{Number}} & \text{if } \text{UInt} \sqsubseteq \hat{n} \vee \text{NUInt} \sqsubseteq \hat{n} \\ \text{NaN} & \text{if } \neg \text{inf} = \hat{n} \vee \text{inf} = \hat{n} \vee \text{NaN} = \hat{n} \\ \text{NaN} & \text{if } \text{NUIntSingle}(n) = \hat{n} \wedge \text{abs}(n) > 8.64 \times 10^{15} \\ \widehat{\text{toInteger}}(\hat{n}) & \text{if } \text{NUIntSingle}(n) = \hat{n} \wedge \text{abs}(n) \leq 8.64 \times 10^{15} \\ \perp_{\text{Number}} & \text{if } \hat{n} \sqsubseteq \perp_{\text{Number}} \end{cases}
\end{aligned}$$

### 11.2.2 Global

$$\begin{aligned}
\hat{\mathcal{I}}_{cp}[\![\text{BuiltinCall}(\text{"isNaN"}, \text{args})]\!](\langle \hat{H}_1, \hat{C} \rangle, \hat{S}) &= (\langle \hat{H}_1, \hat{C} \rangle, \hat{S}) \\
\text{where } \hat{n} &= \widehat{\text{toNumber}}(\widehat{\text{toPrimitive}}(\widehat{\text{getArgValue}}(\text{"0"}))) \\
\wedge \hat{b} &= \begin{cases} \text{true} & \text{if } \text{NaN} = \hat{n} \\ \text{false} & \text{if } \text{NaN} \neq \hat{n} \wedge \text{NaN} \not\sqsubseteq \hat{n} \\ \top_{\text{bool}} & \text{if } \text{NaN} \neq \hat{n} \wedge \text{NaN} \sqsubseteq \hat{n} \\ \perp_{\text{bool}} & \text{otherwise} \end{cases} \\
\wedge \hat{H}_1 &= \widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{b}))
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{cp}[\![\text{BuiltinCall}(\text{"isFinite"}, \text{args})]\!](\langle \hat{H}, \hat{C} \rangle, \hat{S}) &= (\langle \hat{H}_1, \hat{C} \rangle, \hat{S}) \\
\text{where } \hat{n} &= \widehat{\text{toNumber}}(\widehat{\text{toPrimitive}}(\widehat{\text{getArgValue}}(\text{"0"}))) \\
\wedge \hat{b} &= \begin{cases} \text{false} & \text{if } \text{NaN} = \hat{n} \vee \text{inf} = \hat{n} \vee \neg \text{inf} = \hat{n} \\ \top_{\text{bool}} & \text{if } \text{NaN} \sqsubseteq \hat{n} \vee \text{inf} \sqsubseteq \hat{n} \vee \neg \text{inf} \sqsubseteq \hat{n} \\ \text{true} & \text{if } \text{NaN} \not\sqsubseteq \hat{n} \wedge \text{inf} \not\sqsubseteq \hat{n} \wedge \neg \text{inf} \not\sqsubseteq \hat{n} \\ \perp_{\text{bool}} & \text{otherwise} \end{cases} \\
\wedge \hat{H}_1 &= \widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{b}))
\end{aligned}$$

### 11.2.3 Object

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Object.constructor"}, args)_{\hat{a}_{new}} \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_8, \hat{C}_8), \hat{S}_1) \\
& \text{where } \hat{v} = \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"0"}) \\
& \wedge (\hat{v}_1, \hat{H}_1, \hat{C}_1) = \begin{cases} (Value(\hat{v}.2), \hat{H}, \hat{C}) & \text{if } \hat{v}.2 \neq \{\} \\ (\perp_{value}, \perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\
& \wedge (\hat{v}_2, \hat{H}_2, \hat{C}_2, \hat{e}s_2) = \begin{cases} (\hat{v}_4, \hat{H}_4, \hat{C}_4, \hat{e}s) & \text{if } \hat{v}.1.3 \not\sqsubseteq \perp_{bool} \vee \hat{v}.1.4 \not\sqsubseteq \perp_{num} \vee \hat{v}.1.5 \not\sqsubseteq \perp_{string} \\ (\perp_{value}, \perp_{heap}, \perp_{context}, \{\}) & \text{otherwise} \end{cases} \\
& \wedge \hat{v}_{prim} = Value(PValue(\perp_{undef}, \perp_{null}, \hat{v}.1.3, \hat{v}.1.4, \hat{v}.1.5)) \\
& \wedge (\hat{v}_4, \hat{H}_4, \hat{C}_4, \hat{e}s) = \widehat{\text{toObject}}(\hat{H}, \hat{C}, \hat{v}_{prim}, \hat{a}_{new}) \\
& \wedge (\hat{v}_3, \hat{H}_3, \hat{C}_3) = \begin{cases} (Value(\{\hat{l}_R\}), \hat{H}_6, \hat{C}_5) & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{undef} \vee \hat{v}.1.2 \not\sqsubseteq \perp_{null} \\ (\perp_{value}, \perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\
& \wedge \hat{l}_R = (\hat{a}_{new}, \text{Recent}) \wedge (\hat{H}_5, \hat{C}_5) = \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new}) \quad // \text{Recency Abstraction} \\
& \wedge \hat{H}_6 = \widehat{\text{allocObject}}(\hat{H}_5, \{ \#ObjProto_R \}, \hat{l}_R) \\
& \wedge (\hat{v}_7, \hat{H}_7, \hat{C}_7) = (\hat{v}_1 \sqcup \hat{v}_2 \sqcup \hat{v}_3, \hat{H}_1 \sqcup \hat{H}_2 \sqcup \hat{H}_3, \hat{C}_1 \sqcup \hat{C}_2 \sqcup \hat{C}_3) \\
& \wedge (\hat{H}_8, \hat{C}_8) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}_7, \hat{v}_7), \hat{C}_7) & \text{if } \hat{v}_7 \not\sqsubseteq \perp_{value} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}_2, \hat{C}_2, \hat{e}s_2)
\end{aligned}$$



$$\hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.getPrototypeOf"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}_1)$$

$$\begin{aligned} \text{where } \hat{v}_1 &= \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"0"}) \\ \wedge \hat{v}_2 &= \bigsqcup_{\hat{l} \in \hat{v}_1.2} \hat{H}(\hat{l})(\text{@proto}).1.1.1 \\ \wedge \hat{e}s &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ \wedge (\hat{H}_1, \hat{C}_1) &= \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \hat{v}_2), \hat{C}) & \text{if } \hat{v}_2 \not\sqsubseteq \perp_{value} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\ \wedge \hat{S}_1 &= \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s) \end{aligned}$$

$$\hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.getOwnPropertyDescriptor"}, args)_{\hat{a}_{new}} \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_7, \hat{C}_7), \hat{S}_1)$$

$$\begin{aligned} \text{where } \hat{v}_1 &= \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"0"}) \wedge \hat{s}_{prop} = \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"1"}))) \\ \wedge \hat{e}s &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ \wedge \hat{o}v &= \bigsqcup_{\hat{l} \in \hat{v}_1.2} \hat{H}(\hat{l})(\hat{s}_{prop}).1.1 \\ \wedge (\hat{v}_2, \hat{H}_2, \hat{C}_2) &= \begin{cases} (Value(PValue(\top_{undef})), \hat{H}, \hat{C}) & \text{if } \top_{undef} \sqsubseteq \hat{o}v.1.1.1 \\ (\perp_{value}, \perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\ \wedge (\hat{v}_3, \hat{H}_3, \hat{C}_3) &= \begin{cases} (Value(\{\hat{l}_R\}), \hat{H}_5, \hat{C}_4) & \text{if } Value(Pvalue(\perp_{undef}, \hat{o}v.1.1.2, \hat{o}v.1.1.3, \hat{o}v.1.1.4, \hat{o}v.1.1.5), \hat{v}.1.2) \\ & \not\sqsubseteq \perp_{value} \\ (\perp_{value}, \perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\ \wedge \hat{l}_R &= (\hat{a}_{new}, \text{Recent}) \wedge (\hat{H}_4, \hat{C}_4) = \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new}) \quad // \text{Recency Abstraction} \\ \wedge \hat{o}_{new} &= \widehat{\text{NewObject}}(\#ObjProto_R) \\ \wedge \hat{o}_1 &= \begin{cases} \hat{o}_{new} \left[ \begin{array}{l} \text{"value"} \mapsto \langle \hat{v}_2.1.1.1, \text{true}, \text{true}, \text{true} \rangle \\ \text{"writable"} \mapsto \langle \hat{v}_2.1.1.2, \text{true}, \text{true}, \text{true} \rangle \end{array} \right] & \text{if } \text{IsDataDescriptor}(H(v), s) \\ \hat{o}_{new} & \text{otherwise} // \text{skip when AccessorDescriptor} \end{cases} \\ \wedge \hat{o}_2 &= \hat{o}_1 \left[ \begin{array}{l} \text{"enumerable"} \mapsto \langle \hat{v}_2.1.1.3, \text{true}, \text{true}, \text{true} \rangle \\ \text{"configurable"} \mapsto \langle \hat{v}_2.1.1.4, \text{true}, \text{true}, \text{true} \rangle \end{array} \right] \\ \wedge \hat{H}_5 &= \hat{H}_4[\hat{l}_R \mapsto \hat{o}_2] \\ \wedge \hat{H}_6 &= \hat{H}_2 \sqcup \hat{H}_3 \\ \wedge (\hat{H}_7, \hat{C}_7) &= \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}_6, \hat{v}_2 \sqcup \hat{v}_3), \hat{C}_2 \sqcup \hat{C}_3) & \text{if } \hat{v}_2 \not\sqsubseteq \perp_{value} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\ \wedge \hat{S}_1 &= \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s) \end{aligned}$$

$$\hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.getOwnPropertyNames"}, args)_{\hat{a}_{new}} \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_3, \hat{C}_3), \hat{S}_1)$$

$$\begin{aligned} \text{where } \hat{v}_1 &= \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"0"}) \\ \wedge \hat{e}s &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ \wedge \hat{o} &= \bigsqcup_{\hat{l} \in \hat{v}_1.2} \hat{H}(\hat{l}) \wedge n = 0 \\ \wedge \hat{l}_R &= (\hat{a}_{new}, \text{Recent}) \wedge (\hat{H}_1, \hat{C}_1) = \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new}) \quad // \text{Recency Abstraction} \\ \wedge \hat{o}_1 &= \widehat{\text{NewArray}}(0) \left[ \forall s \in \text{dom}(o) : n^{++} \mapsto \langle s, \text{true}, \text{true}, \text{true} \rangle \right] // \text{ignore @default, unsound??} \\ \wedge \hat{H}_2 &= \hat{H}_1[\hat{l}_R \mapsto \hat{o}_1] \\ \wedge (\hat{H}_3, \hat{C}_3) &= (\widehat{\text{ReturnStore}}(\hat{H}_2, Value(\{\hat{l}_R\})), \hat{C}_1) \\ \wedge \hat{S}_1 &= \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s) \end{aligned}$$

$$\text{where } \hat{l}_R = (\hat{a}_{new}, \text{Recent}) \wedge (\hat{H}_1, \hat{C}_1) = \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new}) \quad // \text{Recency Abstraction}$$

$$\begin{aligned} \wedge \hat{v} &= \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"0"}) \wedge \hat{e}s = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ \wedge \hat{o}_1 &= \bigsqcup_{\hat{l} \in \hat{v}.2} \widehat{\text{NewArrayObject}}(\text{UInt})[\forall s \in \text{dom}(\hat{H}_1(\hat{l})) : \text{NumStr} \mapsto \langle s, \text{true}, \text{true}, \text{true} \rangle] \\ \wedge \hat{o}_2 &= \begin{cases} \widehat{\text{NewArrayObject}}(\text{UInt})[\text{NumStr} \mapsto \langle \text{NumStr}, \text{true}, \text{true}, \text{true} \rangle] & \text{if } \hat{H}_1(\hat{l})(\text{"@default\_number"}) \not\sqsubseteq \perp_{PropValue} \\ \perp_{Obj} & \text{otherwise} \end{cases} \\ \wedge \hat{o}_3 &= \begin{cases} \widehat{\text{NewArrayObject}}(\text{UInt})[\text{NumStr} \mapsto \langle \text{OtherStr}, \text{true}, \text{true}, \text{true} \rangle] & \text{if } \hat{H}_1(\hat{l})(\text{"@default\_other"}) \not\sqsubseteq \perp_{PropValue} \\ \perp_{Obj} & \text{otherwise} \end{cases} \\ \wedge \hat{H}_2 &= \hat{H}_1[\hat{l}_R \mapsto \hat{o}_1 \sqcup \hat{o}_2 \sqcup \hat{o}_3] \wedge (\hat{H}_3, \hat{C}_3) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}_2, Value(\hat{l}_R)), \hat{C}) & \text{if } \hat{o} \not\sqsubseteq \perp_{Obj} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\ \wedge \hat{S}_1 &= \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s) \end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Object.create"}, args)_{\hat{a}_{new}} \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_4, \hat{C}_4), \hat{S}_1) \\
& \text{where } \hat{l}_R = (\hat{a}_{new}, \text{Recent}) \wedge (\hat{H}_1, \hat{C}_1) = \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new}) \quad // \text{Recency Abstraction} \\
& \wedge \hat{v}_1 = \widehat{\text{getArgValue}}(\hat{H}_1, \hat{C}_1, \text{"0"}) \wedge \hat{e}s_1 = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{n}_{arglen} = \widehat{\text{toUInt32}}(\widehat{\text{getArgValue}}(\hat{H}_1, \hat{C}_1, \text{"length"})) \\
& \wedge \hat{v}_2 = \widehat{\text{getArgValue}}(\hat{H}_1, \hat{C}_1, \text{"1"}) \wedge \hat{e}s_2 = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_2.1 \not\sqsubseteq \perp_{PValue} \wedge \hat{n}_{arglen} = \hat{2} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_2 = \hat{H}_1[\hat{l}_R \mapsto \widehat{\text{NewObject}}(\hat{v}_1.2)] \\
& \wedge \hat{H}_3 = \begin{cases} \bigsqcup_{\hat{l}_2 \in \hat{v}_2.2} \bigsqcup_{s \in \widehat{\text{GetProps}}(\hat{H}_2, \hat{l}_2)} \widehat{\text{DefineProperty}}(\hat{H}_2, \hat{l}_R, \hat{s}, \hat{l}_2) & \text{if } \hat{n}_{arglen} = \hat{2} \\ \hat{H}_2 & \text{otherwise} \end{cases} \\
& \wedge (\hat{H}_4, \hat{C}_4) = (\widehat{\text{ReturnStore}}(\hat{H}_2, \text{Value}(\{\hat{l}_R\}), \hat{C}_1)) \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s_1 \sqcup \hat{e}s_2)
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Object.defineProperty"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S}_1) \\
& \text{where } \hat{v}_1 = \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"0"}) \wedge \hat{e}s_1 = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{s}_{name} = \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"1"}))) \\
& \wedge \hat{v}_2 = \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"2"}) \wedge \hat{e}s_2 = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_2.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_1 = \bigsqcup_{\hat{l}_1 \in \hat{v}_1.2} \bigsqcup_{\hat{l}_2 \in \hat{v}_2.2} \widehat{\text{DefineProperty}}(\hat{H}, \hat{l}_1, \hat{s}_{name}, \hat{l}_2) \\
& \wedge (\hat{H}_2, \hat{C}_2) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}_1, \text{Value}(\hat{v}_1.2)), \hat{C}) & \text{if } \text{Value}(\hat{v}_1.2) \not\sqsubseteq \perp_{value} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s_1 \sqcup \hat{e}s_2)
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Object.defineProperties"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S}_1) \\
& \text{where } \hat{v}_1 = \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"0"}) \wedge \hat{e}s_1 = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{v}_2 = \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"1"}) \wedge \hat{e}s_2 = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_1 = \bigsqcup_{\hat{l}_1 \in \hat{v}_1.2} \bigsqcup_{\hat{l}_2 \in \hat{v}_2.2} \bigsqcup_{s \in \widehat{\text{GetProps}}(\hat{H}, \hat{l}_2)} \widehat{\text{DefineProperty}}(\hat{H}, \hat{l}_1, \hat{s}, \hat{l}_2) \\
& \wedge (\hat{H}_2, \hat{C}_2) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}_1, \text{Value}(\hat{v}_1.2)), \hat{C}) & \text{if } \text{Value}(\hat{v}_1.2) \not\sqsubseteq \perp_{value} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s_1 \sqcup \hat{e}s_2)
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Object.seal"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S}_1) \\
& \text{where } \hat{v} = \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, "0") \wedge \hat{es} = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_1 = \bigsqcup_{\hat{i} \in \hat{v}.2} \bigsqcup_{s \in \widehat{\text{GetProps}}(\hat{H}, \hat{i})} \hat{H} \left[ \hat{i} \mapsto \hat{H}(\hat{i}) \left[ s \mapsto \left\langle \begin{array}{l} \hat{H}(\hat{i})(x).1.1.1, \hat{H}(\hat{i})(x).1.1.2, \\ \hat{H}(\hat{i})(x).1.1.3, \text{false} \end{array} \right\rangle \right] \right] \\
& \wedge (\hat{H}_2, \hat{C}_2) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}_1, \text{Value}(\hat{v}.2)), \hat{C}) & \text{if } \text{Value}(\hat{v}.2) \not\sqsubseteq \perp_{value} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{es})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Object.freeze"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_4, \hat{C}_4), \hat{S}_1) \\
& \text{where } \hat{v} = \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, "0") \wedge \hat{es} = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_1 = \bigsqcup_{\hat{i} \in \hat{v}.2} \bigsqcup_{s \in \hat{P}_{data}} \hat{H} \left[ \hat{i} \mapsto \hat{H}(\hat{i}) \left[ s \mapsto \left\langle \begin{array}{l} \hat{H}(\hat{i})(x).1.1.1, \text{false}, \\ \hat{H}(\hat{i})(x).1.1.3, \text{false} \end{array} \right\rangle \right] \right] \\
& \wedge \hat{H}_2 = \bigsqcup_{\hat{i} \in \hat{v}.2} \bigsqcup_{s \in \hat{P}_{access}} \hat{H} \left[ \hat{i} \mapsto \hat{H}(\hat{i}) \left[ s \mapsto \left\langle \begin{array}{l} \hat{H}(\hat{i})(x).1.1.1, \text{false}, \\ \hat{H}(\hat{i})(x).1.1.3, \text{false} \end{array} \right\rangle \right] \right] \\
& \wedge \hat{P}_{data} = \{x \mid x \in \widehat{\text{GetProps}}(\hat{H}(\hat{i})) \wedge \text{true} \sqsubseteq \text{IsDataDescriptor}(x)\} \\
& \wedge \hat{P}_{access} = \{x \mid x \in \widehat{\text{GetProps}}(\hat{H}(\hat{i})) \wedge \text{false} \sqsubseteq \text{IsDataDescriptor}(x)\} \\
& \wedge \hat{H}_3 = \hat{H}_1 \sqcup \hat{H}_2 \\
& \wedge (\hat{H}_4, \hat{C}_4) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}_3, \text{Value}(\hat{v}.2)), \hat{C}) & \text{if } \text{Value}(\hat{v}.2) \not\sqsubseteq \perp_{value} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{es})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Object.preventExtensions"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S}_1) \\
& \text{where } \hat{v} = \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, "0") \wedge \hat{es} = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_1 = \bigsqcup_{\hat{i} \in \hat{v}.2} \hat{H} \left[ \hat{i} \mapsto \hat{H}(\hat{i}) \left[ @extensible \mapsto \text{false} \right] \right] \\
& \wedge (\hat{H}_2, \hat{C}_2) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}_1, \text{Value}(\hat{v}.2)), \hat{C}) & \text{if } \text{Value}(\hat{v}.2) \not\sqsubseteq \perp_{value} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{es})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.isSealed"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}_1) \\
& \text{where } \hat{v} = \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, "0") \wedge \hat{es} = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{b}_{f_i} = \begin{cases} \text{false} & \text{if } \exists x \in \widehat{\text{GetProps}}(\hat{H}(\hat{l})) : \text{true} \sqsubseteq \hat{H}(\hat{l})(x).1.1.3 \\ \perp_{bool} & \text{otherwise} \end{cases} \\
& \wedge \hat{b}_{t_i} = \begin{cases} \top_{bool} & \text{if } \forall x \in \widehat{\text{GetProps}}(\hat{H}(\hat{l})) : \text{false} \sqsubseteq \hat{H}(\hat{l})(x).1.1.3 \wedge \top_{bool} \sqsubseteq \hat{H}(\hat{l})(@extensible) \\ \text{true} & \text{if } \forall x \in \widehat{\text{GetProps}}(\hat{H}(\hat{l})) : \text{false} \sqsubseteq \hat{H}(\hat{l})(x).1.1.3 \wedge \text{false} \sqsubseteq \hat{H}(\hat{l})(@extensible) \\ \text{false} & \text{if } \forall x \in \widehat{\text{GetProps}}(\hat{H}(\hat{l})) : \text{false} \sqsubseteq \hat{H}(\hat{l})(x).1.1.3 \wedge \text{true} \sqsubseteq \hat{H}(\hat{l})(@extensible) \\ \perp_{bool} & \text{otherwise} \end{cases} \\
& \wedge \hat{b} = \bigsqcup_{i \in \hat{v}.2} (\hat{b}_{f_i} \sqcup \hat{b}_{t_i}) \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\text{ReturnStore}(\hat{H}, \text{Value}(\hat{b})), \hat{C}) & \text{if } \hat{b} \not\sqsubseteq \perp_{Bool} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{es})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.isFrozen"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}_1) \\
& \text{where } \hat{v} = \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, "0") \wedge \hat{es} = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{b}_{f_i} = \begin{cases} \text{false} & \text{if } \exists x \in \hat{P}_{data} : \text{true} \sqsubseteq \hat{H}(\hat{l})(x).1.1.2 \\ \text{false} & \text{if } \exists x \in \hat{P}_{access} : \text{true} \sqsubseteq \hat{H}(\hat{l})(x).1.1.4 \\ \perp_{bool} & \text{otherwise} \end{cases} \\
& \wedge \hat{b}_{t_i} = \begin{cases} \top_{bool} & \text{if } \forall x \in \hat{P}_{data} : \text{false} \sqsubseteq \hat{H}(\hat{l})(x).1.1.2 \wedge \forall x \in \hat{P}_{access} : \text{false} \sqsubseteq \hat{H}(\hat{l})(x).1.1.4 \wedge \top_{bool} \sqsubseteq \hat{H}(\hat{l})(@extensible) \\ \text{true} & \text{if } \forall x \in \hat{P}_{data} : \text{false} \sqsubseteq \hat{H}(\hat{l})(x).1.1.2 \wedge \forall x \in \hat{P}_{access} : \text{false} \sqsubseteq \hat{H}(\hat{l})(x).1.1.4 \wedge \text{false} \sqsubseteq \hat{H}(\hat{l})(@extensible) \\ \text{false} & \text{if } \forall x \in \hat{P}_{data} : \text{false} \sqsubseteq \hat{H}(\hat{l})(x).1.1.2 \wedge \forall x \in \hat{P}_{access} : \text{false} \sqsubseteq \hat{H}(\hat{l})(x).1.1.4 \wedge \text{true} \sqsubseteq \hat{H}(\hat{l})(@extensible) \\ \perp_{bool} & \text{otherwise} \end{cases} \\
& \wedge \hat{P}_{data} = \{x \mid x \in \widehat{\text{GetProps}}(\hat{H}(\hat{l})) \wedge \text{true} \sqsubseteq \text{IsDataDescriptor}(x)\} \\
& \wedge \hat{P}_{access} = \{x \mid x \in \widehat{\text{GetProps}}(\hat{H}(\hat{l})) \wedge \text{false} \sqsubseteq \text{IsDataDescriptor}(x)\} \\
& \wedge \hat{b} = \bigsqcup_{i \in \hat{v}.2} (\hat{b}_{f_i} \sqcup \hat{b}_{t_i}) \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\text{ReturnStore}(\hat{H}, \text{Value}(\hat{b})), \hat{C}) & \text{if } \hat{b} \not\sqsubseteq \perp_{Bool} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{es})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.isExtensible"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}_1) \\
& \text{where } \hat{v} = \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, "0") \wedge \hat{es} = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{b} = \bigsqcup_{i \in \hat{v}.2} \hat{H}(\hat{l})(@extensible).1.2 \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\text{ReturnStore}(\hat{H}, \text{Value}(\hat{b})), \hat{C}) & \text{if } \hat{b} \not\sqsubseteq \perp_{Bool} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{es})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Object.keys"}, args)_{\hat{a}_{new}} \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}_1) \\
& \text{where } \hat{l}_R = (\hat{a}_{new}, \text{Recent}) \wedge (\hat{H}_1, \hat{C}_1) = \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new}) \quad // \text{Recency Abstraction} \\
& \wedge \hat{v} = \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, "0") \wedge \hat{es} = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{o}_1 = \bigsqcup_{i \in \hat{v}.2} \widehat{\text{NewArrayObject}}(\text{UInt})[\forall \hat{s} \in \hat{P}_{enum} : \text{NumStr} \mapsto \langle \hat{s}, \text{true}, \text{true}, \text{true} \rangle] \\
& \wedge \hat{P}_{enum} = \{s \mid s \in \text{dom}(\hat{H}_1(\hat{l})) \wedge \text{true} \sqsubseteq \hat{H}_1(\hat{l})(s).1.1.3\} \\
& \wedge \hat{o}_2 = \begin{cases} \widehat{\text{NewArrayObject}}(\text{UInt})[\text{NumStr} \mapsto \langle \text{NumStr}, \text{true}, \text{true}, \text{true} \rangle] & \text{if } \hat{H}_1(\hat{l})(@default\_number) \not\sqsubseteq \perp_{PropValue} \\ \perp_{Obj} & \text{otherwise} \end{cases} \\
& \wedge \hat{o}_3 = \begin{cases} \widehat{\text{NewArrayObject}}(\text{UInt})[\text{NumStr} \mapsto \langle \text{OtherStr}, \text{true}, \text{true}, \text{true} \rangle] & \text{if } \hat{H}_1(\hat{l})(@default\_other) \not\sqsubseteq \perp_{PropValue} \\ \perp_{Obj} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_2 = \hat{H}_1[\hat{l}_R \mapsto \hat{o}_1 \sqcup \hat{o}_2 \sqcup \hat{o}_3] \wedge (\hat{H}_3, \hat{C}_3) = \begin{cases} (\text{ReturnStore}(\hat{H}_2, \text{Value}(\hat{l}_R)), \hat{C}) & \text{if } \hat{o} \not\sqsubseteq \perp_{Obj} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{es})
\end{aligned}$$

## 11.2.4 Object.prototype

$$\begin{aligned} \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Object.prototype.toString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_1, \hat{C}_1), \hat{S}) \\ \text{where } \hat{s} = \bigsqcup_{i \in \hat{C}.2} &\begin{cases} \alpha(\text{"[object]" + s + "[ ]"}) & \text{if } \hat{H}(\hat{l})(@class) = \text{NumStrSingle}(s) \\ \alpha(\text{"[object]" + s + "[ ]"}) & \text{if } \hat{H}(\hat{l})(@class) = \text{OtherStrSingle}(s) \\ \perp_{string} & \text{if } \hat{H}(\hat{l})(@class) = \perp_{string} \\ \text{OtherStr} & \text{otherwise} \end{cases} \\ \wedge (\hat{H}_1, \hat{C}_1) &= \begin{cases} (\text{ReturnStore}(\hat{H}, \text{Value}(\hat{s})), \hat{C}) & \text{if } \hat{s} \not\sqsubseteq \perp_{String} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Object.prototype.toLocaleString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) \\ = \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Object.prototype.toString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) \end{aligned}$$

$$\begin{aligned} \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Object.prototype.ValueOf"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_1, \hat{C}_1), \hat{S}) \\ \text{where } (\hat{H}_1, \hat{C}_1) &= \begin{cases} (\text{ReturnStore}(\hat{H}, \text{Value}(\hat{C}.2)), \hat{C}) & \text{if } \text{Value}(\hat{C}.2) \not\sqsubseteq \perp_{Value} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Object.prototype.hasOwnProperty"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_1, \hat{C}_1), \hat{S}) \\ \text{where } \hat{s} = \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"0"}))) \\ \wedge \hat{b} = \bigsqcup_{i \in \hat{C}.2} &\widehat{\text{HasOwnProperty}}(\hat{H}, \hat{l}, \hat{s}) \\ \wedge (\hat{H}_1, \hat{C}_1) &= \begin{cases} (\text{ReturnStore}(\hat{H}, \text{Value}(\hat{b})), \hat{C}) & \text{if } \hat{b} \not\sqsubseteq \perp_{Bool} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Object.prototype.isPrototypeOf"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_1, \hat{C}_1), \hat{S}) \\ \text{where } \hat{v} = \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"0"}) \\ \wedge \hat{b}_1 = \begin{cases} \text{false} & \text{if } \hat{v}.1 \sqsubseteq \perp_{PValue} \\ \perp_{bool} & \text{otherwise} \end{cases} \quad \wedge \hat{b}_2 = \bigsqcup_{i \in \hat{v}.2} \hat{b}_{3_i} \sqcup \hat{b}_{4_i} \\ \wedge \hat{v}_{proto_i} = \hat{H}(\hat{l})(@proto).1.2 \\ \wedge \hat{b}_{3_i} = \begin{cases} \text{false} & \text{if } \top_{null} \sqsubseteq \hat{v}_{proto_i}.1.2 \\ \perp_{bool} & \text{otherwise} \end{cases} \\ \wedge \hat{b}_{4_i} = (\text{Value}(\hat{v}.2) \hat{=} \text{Value}(\hat{v}_{proto_i}.2)).1.3 \\ \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\text{ReturnStore}(\hat{H}, \text{Value}(\hat{b}_1 \sqcup \hat{b}_2)), \hat{C}) & \text{if } \hat{b}_1 \sqcup \hat{b}_2 \not\sqsubseteq \perp_{Bool} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Object.prototype.propertyIsEnumerable"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_1, \hat{C}_1), \hat{S}) \\ \text{where } \hat{s} = \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"0"}))) \\ \wedge \hat{b} = \bigsqcup_{i \in \hat{C}.2} \hat{b}_{1_i} \sqcup \hat{b}_{2_i} \\ \wedge \hat{b}_{1_i} = \begin{cases} \text{false} & \text{if } \top_{undef} \sqsubseteq \hat{H}(\hat{l})(\hat{s}).1.1.1.1.1 \\ \perp_{bool} & \text{otherwise} \end{cases} \\ \wedge \hat{b}_{2_i} = \begin{cases} \hat{H}(\hat{l}).1.1.3 & \text{if } \hat{H}(\hat{l})(\hat{s}).1.1.1.1.1 \sqsubseteq \perp_{undef} \\ \perp_{bool} & \text{otherwise} \end{cases} \\ \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\text{ReturnStore}(\hat{H}, \text{Value}(\hat{b})), \hat{C}) & \text{if } \hat{b} \not\sqsubseteq \perp_{Bool} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \end{aligned}$$

## 11.2.5 Function.prototype

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\![\text{BuiltintCall}(\text{"Function.prototype.toString"}, args)\!]_{\hat{a}_{new}}]\!((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S}) \\
& \text{where } \hat{e}s_1 = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{C}.2.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{e}s_2 = \begin{cases} \{\text{TypeError}\} & \text{if } \exists \hat{l} \in \hat{C}.2.2 : \hat{H}(\hat{l})(\text{@class}) \neq \text{"Function"} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{L}_{fun} = \{\hat{l} \mid \hat{l} \in \hat{C}.2.2 \wedge \hat{H}(\hat{l})(\text{@class}) = \text{"Function"}\} \\
& \wedge \hat{s} = \bigsqcup_{\hat{l} \in \hat{L}_{fun}} \widehat{\text{fid2String}}(\hat{H}(\hat{l})(\text{@function})) \\
& \wedge (\hat{H}_1, \hat{C}_1) = (\hat{H}[\#PureLocal_R \mapsto \hat{H}(\#PureLocal_R)[\text{@return} \mapsto \hat{s}]], \hat{C}) \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s_1 \sqcup \hat{e}s_2)
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\![\text{BuiltintCall}(\text{"Function.prototype.apply"}, args)\!]_{\hat{a}_{new}}]\!((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S}) \\
& \text{where } \hat{v}_1 = \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"0"}) \\
& \wedge \hat{e}s_1 = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{e}s_2 = \begin{cases} \{\text{TypeError}\} & \text{if } \text{false} \sqsubseteq \bigsqcup_{\hat{l} \in \hat{v}_1.2} : \widehat{\text{IsCallable}}(\hat{H}, \hat{l}) \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{L}_f = \{\hat{l} \mid \hat{l} \in \hat{v}_1.2 \wedge \text{true} \sqsubseteq \widehat{\text{IsCallable}}(\hat{H}, \hat{l})\} \\
& \wedge \hat{v}_2 = \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"1"}) \\
& \wedge \hat{e}s_3 = \begin{cases} \{\text{TypeError}\} & \text{if } \langle \perp_{undef}, \perp_{null}, \hat{v}_2.1.3, \hat{v}_2.1.4, \hat{v}_2.1.5 \rangle \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge
\end{aligned}$$

## 11.2.6 Array

$$\begin{aligned} & \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Array"}, args)]_{\hat{a}_{new}}((\hat{H}, \hat{C}), \hat{S}) \\ &= \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Array.constructor"}, args)]_{\hat{a}_{new}}((\hat{H}, \hat{C}), \hat{S}) \end{aligned}$$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Array.constructor"}, args)]_{\hat{a}_{new}}((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_3, \hat{C}_3), \hat{S}_1)$$

where  $(\hat{H}_1, \hat{C}_1) = \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new}) \wedge \hat{l}_R = (\hat{a}_{new}, \text{Recent})$  // *Recency Abstraction*

$$\begin{aligned} \hat{n}_{arglen} &= \text{toUInt32}(\text{getArgValue}(\hat{H}_1, \hat{C}_1, \text{"length"})) \\ \wedge \hat{o}_1 &= \begin{cases} \hat{o}_{arg1_1} \sqcup \hat{o}_{arg1_2} & \text{if } \text{UIntSingle}(1) = \hat{n}_{arglen} \\ \hat{o}_{argn} & \text{if } \text{UIntSingle}(n_{arglen}) = \hat{n}_{arglen} \wedge n > 1 \\ \hat{o}_{arg1_1} \sqcup \hat{o}_{arg1_2} \sqcup \hat{o}_{uint} & \text{if } \text{UInt} \sqsubseteq \hat{n}_{arglen} \\ \perp_{Obj} & \text{if } \hat{n}_{arglen} \sqsubseteq \perp_{number} \end{cases} \\ \wedge \hat{v}_i &= \text{getArgValue}(\hat{H}_1, \hat{C}_1, "i") \\ \wedge \hat{v}_{0notNum} &= \text{Value}(\langle \hat{v}_0.1.1, \hat{v}_0.1.2, \hat{v}_0.1.3, \perp_{Number}, \hat{v}_0.1.5 \rangle, \hat{v}_0.2) \\ \wedge \hat{o}_{arg1_1} &= \begin{cases} \widehat{\text{NewArrayObject}}(1)[0 \mapsto \hat{v}_{0notNum}] & \text{if } \hat{v}_{0notNum} \not\sqsubseteq \perp_{Value} \\ \perp_{Obj} & \text{otherwise} \end{cases} \\ \wedge \hat{o}_{arg1_2} &= \begin{cases} \widehat{\text{NewArrayObject}}(\hat{v}_0.1.4) & \text{if } \hat{v}_0.1.4 \not\sqsubseteq \perp_{Number} \\ \perp_{Obj} & \text{otherwise} \end{cases} \\ \wedge \hat{e}s &= \begin{cases} \{\text{RangeError}\} & \text{if } \text{UIntSingle}(1) = \hat{n}_{arglen} \wedge \hat{v}_0.1.4 \not\sqsubseteq \text{UInt} \\ \{\} & \text{otherwise} \end{cases} \\ \wedge \hat{o}_{argn} &= \widehat{\text{NewArrayObject}}(n_{arglen})[\forall i \in \{0, \dots, n_{arglen} - 1\} : i \mapsto v_i] \\ \wedge \hat{o}_{uint} &= \widehat{\text{NewArrayObject}}(n_{arglen})[@default\_number \mapsto \hat{v}_{allarg}] \\ \wedge \hat{v}_{allarg} &= \text{getArgValue}(\hat{H}_1, \hat{C}_1, \text{UInt}) \\ \wedge \hat{H}_2 &= \hat{H}_1[\hat{l}_R \mapsto \hat{o}_1] \\ \wedge (\hat{H}_3, \hat{C}_3) &= \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}_2, \text{Value}(\hat{l}_R)), \hat{C}) & \text{if } \hat{o}_1 \not\sqsubseteq \perp_{Obj} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\ \wedge \hat{S}_1 &= \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s) \end{aligned}$$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Array.isArray"}, args)]_{\hat{a}_{new}}((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $\hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, "0")$

$$\begin{aligned} \wedge \hat{b}_1 &= \begin{cases} \text{false} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \perp_{bool} & \text{otherwise} \end{cases} \\ \wedge \hat{b}_2 &= \begin{cases} \text{true} & \text{if } \exists \hat{l} \in \hat{v}.2 : \text{"Array"} \sqsubseteq \hat{H}(\hat{l})(@class).1.2.1.5 \\ \perp_{bool} & \text{otherwise} \end{cases} \\ \wedge \hat{b}_3 &= \begin{cases} \text{false} & \text{if } \exists \hat{l} \in \hat{v}.2 : \hat{H}(\hat{l})(@class).1.2.1.5 \not\sqsubseteq \text{"Array"} \\ \perp_{bool} & \text{otherwise} \end{cases} \\ \wedge \hat{b} &= \hat{b}_1 \sqcup \hat{b}_2 \sqcup \hat{b}_3 \\ \wedge (\hat{H}_1, \hat{C}_1) &= \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{b})), \hat{C}) & \text{if } \hat{b} \not\sqsubseteq \perp_{Bool} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \end{aligned}$$

## 11.2.7 Array.prototype

$$\hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Array.prototype.toString"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_3, \hat{C}_3), \hat{S})$$

where *// [[get]] join, [[call]]*

$$\begin{aligned} \hat{v}_{length} &= \bigsqcup_{i \in \hat{C}_{1.2}} \widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"}) \\ \wedge \hat{s} &= \begin{cases} \hat{s}_0 + \hat{s}_{sep} + \dots + \hat{s}_{sep} + \hat{s}_{n_{len}-1} & \text{if } \hat{v}_{length}.1.4 = \text{UIntSingle}(n_{len}) \\ \perp_{string} & \text{if } \hat{v}_{length}.1.4 = \perp_{number} \\ \top_{string} & \text{otherwise} \end{cases} \\ \wedge \hat{s}_i &= \begin{cases} \hat{\omega} & \text{if } \hat{v}_i \not\sqsubseteq \perp_{Undef} \vee \hat{v}_i \not\sqsubseteq \perp_{Null} \\ \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\text{Value}(\langle \perp_{Undef}, \perp_{Null}, \hat{v}_{arg}.1.3, \hat{v}_{arg}.1.4, \hat{v}_{arg}.1.5 \rangle, v_{arg}.2))) & \text{otherwise} \end{cases} \\ \wedge \hat{v}_i &= \bigsqcup_{i \in \hat{C}_{1.2}} \widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"i"}) \wedge \hat{v}_{arg} = \text{getArgValue}(args, \text{"0"}) \\ \wedge \hat{s}_{sep} &= \text{" , " } \\ \wedge (\hat{H}_1, \hat{C}_1) &= (\hat{H}[\#PureLocal_R \mapsto \hat{H}(\#PureLocal_R)[@return \mapsto \hat{s}]], \hat{C}) \end{aligned}$$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Array.prototype.toLocaleString"}, args)]((\hat{H}, \hat{C}), \hat{S})$$

$$= \hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Array.prototype.toString"}, args)]((\hat{H}, \hat{C}), \hat{S})$$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Array.prototype.concat"}, args)]_{\hat{a}_{new}}((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_3, \hat{C}_3), \hat{S})$$

where  $(\hat{H}_1, \hat{C}_1) = \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new}) \wedge \hat{l}_R = (\hat{a}_{new}, \text{Recent})$  *// Recency Abstraction*

$$\begin{aligned} \wedge \hat{n}_{len} &= \text{getArgValue}(\hat{H}_1, \hat{C}_1, \text{"length"}).1.4 \\ \wedge \hat{H}_2 &= \begin{cases} \perp_{Heap} & \text{if } \hat{n}_{len} = \perp_{Number} \\ \hat{H}_1[\hat{l}_R \mapsto \hat{o}_1] & \text{if } \hat{n}_{len} = \text{UIntSingle}(n_{arglen}) \\ \hat{H}_1[\hat{l}_R \mapsto \hat{o}_2] & \text{if } \hat{n}_{len} \neq \text{UIntSingle} \end{cases} \\ \wedge \hat{o}_{this} &= \bigsqcup_{i \in \hat{C}_{1.2}} \hat{H}_1(\hat{l}) \\ \wedge \hat{o}_1 &= \begin{cases} \hat{o}_3 & \text{if } \hat{o}_{this}(\text{"length"}) = \text{UIntSingle}(n_{len}) \\ \hat{o}_4 & \text{otherwise} \end{cases} \\ \wedge \hat{o}_2 &= \hat{o}_{this}[\text{@default\_number} \mapsto \hat{o}_{this}(\text{@default\_number}) \sqcup \text{Value}(\top_{PValue}, \{\})] \\ \wedge \hat{o}_3 &= \hat{o}_{this}[\forall i \in \{0, \dots, n_{arglen} - 1\} : i + n_{len} \mapsto \hat{v}_{arg_i}, \text{length} \mapsto \alpha(n_{len} + n_{arglen})] \\ \wedge \hat{v}_{arg_i} &= \text{getArgValue}(\hat{H}_1, \hat{C}_1, \text{"i"}) \\ \wedge \hat{o}_4 &= \hat{o}_{this}[\text{@default\_number} \mapsto \hat{o}_{this}(\text{@default\_number}) \sqcup \bigsqcup_{i \in \{0, \dots, n_{len}\}} \hat{v}_{arg_i}] \\ \wedge (\hat{H}_3, \hat{C}_3) &= (\hat{H}_2[\#PureLocal_R \mapsto \hat{H}_2(\#PureLocal_R)[@return \mapsto \text{Value}(\hat{l}_R)]], \hat{C}) \end{aligned}$$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Array.prototype.join"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_3, \hat{C}_3), \hat{S})$$

$$\begin{aligned} \text{where } \hat{v}_{length} &= \bigsqcup_{i \in \hat{C}_{1.2}} \widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"}) \\ \wedge \hat{s} &= \begin{cases} \hat{s}_0 + \hat{s}_{sep} + \dots + \hat{s}_{sep} + \hat{s}_{n_{len}-1} & \text{if } \hat{v}_{length}.1.4 = \text{UIntSingle}(n_{len}) \\ \perp_{string} & \text{if } \hat{v}_{length}.1.4 = \perp_{number} \\ \top_{string} & \text{otherwise} \end{cases} \\ \wedge \hat{s}_i &= \begin{cases} \hat{\omega} & \text{if } \hat{v}_i \not\sqsubseteq \perp_{Undef} \vee \hat{v}_i \not\sqsubseteq \perp_{Null} \\ \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\text{Value}(\langle \perp_{Undef}, \perp_{Null}, \hat{v}_{arg}.1.3, \hat{v}_{arg}.1.4, \hat{v}_{arg}.1.5 \rangle, v_{arg}.2))) & \text{otherwise} \end{cases} \\ \wedge \hat{v}_i &= \bigsqcup_{i \in \hat{C}_{1.2}} \widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"i"}) \wedge \hat{v}_{arg} = \text{getArgValue}(args, \text{"0"}) \\ \wedge \hat{s}_{sep} &= \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\text{Value}(\langle \perp_{undef}, \hat{v}_{arg}.1.2, \hat{v}_{arg}.1.3, \hat{v}_{arg}.1.4, \hat{v}_{arg}.1.5 \rangle, v_{arg}.2))) \sqcup \hat{s}_{udf} \\ \wedge \hat{s}_{udf} &= \begin{cases} \text{" , " } & \text{if } v_{1.1.1} \sqsubseteq \perp_{Undef} \\ \perp_{string} & \text{otherwise} \end{cases} \\ \wedge (\hat{H}_1, \hat{C}_1) &= (\hat{H}[\#PureLocal_R \mapsto \hat{H}(\#PureLocal_R)[@return \mapsto \hat{s}]], \hat{C}) \end{aligned}$$



$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Array.prototype.pop"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_5, \hat{C}_5), \hat{S}) \\
& \text{where } (\hat{v}_i, \hat{H}_{1_i}) = \begin{cases} (Value(\top_{undef}), \hat{H}_{2_i}) & \text{if } \hat{n}_{len_i} = \text{UIntSingle}(0) \\ (\widehat{\text{Proto}}(\hat{H}, \hat{l}, n_{len} - 1), \hat{H}_{3_i}) & \text{if } \hat{n}_{len_i} = \text{UIntSingle}(n_{len}) \\ (\perp_{value}, \perp_{Heap}) & \text{if } \hat{n}_{len_i} = \perp_{number} \\ (\hat{H}(\hat{l})(\text{@default\_number}), \hat{H}) & \text{otherwise} \end{cases} \\
& \wedge \hat{n}_{len_i} = \text{toUInt32}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"})) \\
& \wedge \hat{H}_{2_i} = \hat{H}[\hat{l} \mapsto \hat{H}(\hat{l})[\text{"length"} \mapsto 0]] \\
& \wedge \hat{H}_{3_i} = (\widehat{\text{Delete}}(\hat{H}, \hat{l}, n_{len} - 1).1)[\hat{l} \mapsto \hat{H}(\hat{l})[\text{"length"} \mapsto n_{len} - 1]] \\
& \wedge (\hat{v}, \hat{H}_4) = \bigsqcup_{i \in \hat{C}.2} (\hat{v}_i, \hat{H}_{1_i}) \\
& \wedge (\hat{H}_5, \hat{C}_5) = (\hat{H}_4[\#PureLocal_R \mapsto \hat{H}_4(\#PureLocal_R)[\text{@return} \mapsto \hat{v}]], \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Array.prototype.push"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_3, \hat{C}_3), \hat{S}) \\
& \text{where } \hat{n}_{len_i} = \text{toUInt32}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"})) \\
& \wedge \hat{n}_{arglen} = \text{toUInt32}(\text{getArgValue}(args, \text{"length"})) \\
& \wedge (\hat{H}_1, \hat{v}_1) = \bigsqcup_{i \in \hat{C}.2} \begin{cases} \perp_{Heap}, \perp_{value} & \text{if } \hat{n}_{arglen} = \perp_{Number} \\ \hat{H}_1[\hat{l} \mapsto \hat{o}_1], \hat{n}_{len_i} + \hat{n}_{arglen} & \text{if } \hat{n}_{len_i} = \text{UIntSingle}(n_{arglen}) \\ \hat{H}_1[\hat{l} \mapsto \hat{o}_2], \hat{n}_{len_i} & \text{otherwise} \end{cases} \\
& \wedge \hat{o}_1 = \hat{H}(\hat{l})[\forall i \in \{0, \dots, n_{arglen} - 1\} : i + \hat{n}_{len} \mapsto \text{getArgValue}(args, i), \text{"length"} \mapsto \hat{n}_{len} + \hat{n}_{arglen}] \\
& \wedge \hat{o}_2 = \hat{H}(\hat{l})[\hat{n}_{arglen} \mapsto \text{getArgValue}(args, \hat{n}_{arglen})] \\
& \wedge (\hat{H}_2, \hat{C}_2) = (\hat{H}_1[\#PureLocal_R \mapsto \hat{H}_1(\#PureLocal_R)[\text{@return} \mapsto \hat{v}_1]], \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Array.prototype.reverse"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S}) \\
& \text{where } \hat{H}_1 = \bigsqcup_{i \in \hat{C}.2} \begin{cases} \hat{H}[\hat{l} \mapsto \hat{o}_1] & \text{if } \hat{n}_{len_i} = \text{UIntSingle}(n_{len_i}) \\ \hat{H}[\hat{l} \mapsto \hat{o}_2] & \text{if } \hat{n}_{len_i} = \text{UInt} \end{cases} \\
& \wedge \hat{n}_{len_i} = \text{toUInt32}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"})) \\
& \wedge \hat{o}_1 = \forall i \in \{0, \dots, n_{mid_i} - 1\} : \hat{o}_{low1} \sqcup \hat{o}_{low2} \sqcup \hat{o}_{up1} \sqcup \hat{o}_{up2} \\
& \wedge n_{up} = n_{len_i} - i - 1 \\
& \wedge \hat{o}_{low1} = \begin{cases} \hat{H}(\hat{l})[n_{up} \mapsto \widehat{\text{Proto}}(\hat{H}, \hat{l}, i)] & \text{if } \text{true} \sqsubseteq \widehat{\text{HasProperty}}(\hat{H}, \hat{l}, i) \\ \hat{H}(\hat{l}) & \text{otherwise} \end{cases} \\
& \wedge \hat{o}_{low2} = \begin{cases} \hat{H}(\hat{l}) - n_{up} & \text{if } \text{false} \sqsubseteq \widehat{\text{HasProperty}}(\hat{H}, \hat{l}, i) \\ \hat{H}(\hat{l}) & \text{otherwise} \end{cases} \\
& \wedge \hat{o}_{up1} = \begin{cases} \hat{H}(\hat{l})[i \mapsto \widehat{\text{Proto}}(\hat{H}, \hat{l}, n_{up})] & \text{if } \text{true} \sqsubseteq \widehat{\text{HasProperty}}(\hat{H}, \hat{l}, n_{up}) \\ \hat{H}(\hat{l}) & \text{otherwise} \end{cases} \\
& \wedge \hat{o}_{up2} = \begin{cases} \hat{H}(\hat{l}) - i & \text{if } \text{false} \sqsubseteq \widehat{\text{HasProperty}}(\hat{H}, \hat{l}, n_{up}) \\ \hat{H}(\hat{l}) & \text{otherwise} \end{cases} \\
& \wedge \hat{o}_2 = \forall s \in \widehat{\text{GetUIntProps}}(\hat{H}, \hat{l}) : \hat{o}_3 - s \\
& \wedge \hat{o}_3 = \hat{H}(\hat{l})[\text{@default\_number} \mapsto \hat{H}(\hat{l})(\text{@default\_number})] \sqcup \bigsqcup_{s \in \widehat{\text{GetUIntProps}}(\hat{H}, \hat{l})} \hat{H}(\hat{l})(s) \\
& \wedge (\hat{H}_2, \hat{C}_2) = (\hat{H}_1[\#PureLocal_R \mapsto \hat{H}_1(\#PureLocal_R)[\text{@return} \mapsto \hat{C}.2]], \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Array.prototype.shift"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S}) \\
& \text{where } (\hat{H}_1, \hat{v}_1) = \bigsqcup_{\hat{l} \in \hat{C}.2} \begin{cases} (\hat{H}[\hat{l} \mapsto \hat{o}_1], \hat{v}_{head}) & \text{if } \hat{n}_{len_{\hat{l}}} = \text{UIntSingle}(n_{len_{\hat{l}}}) \\ (\hat{H}[\hat{l} \mapsto \hat{o}_2], \hat{v}_{uint}) & \text{if } \hat{n}_{len_{\hat{l}}} = \text{UInt} \end{cases} \\
& \wedge \hat{n}_{len_{\hat{l}}} = \widehat{\text{toUInt32}}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"})) \\
& \wedge \hat{o}_2 = (\forall i \in \{1, \dots, n_{len_{\hat{l}}} - 1\} : \hat{H}(\hat{l})[i - 1 \mapsto \hat{H}(\hat{l})(i)] - n_{len_{\hat{l}}}) \\
& \wedge \hat{v}_{head} = \begin{cases} \widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"0"}) & \text{if } n_{len_{\hat{l}}} \neq 0 \\ \text{Value}(\top_{undef}) & \text{if } n_{len_{\hat{l}}} = 0 \end{cases} \\
& \wedge \hat{o}_2 = \bigsqcup_{i \in \widehat{\text{GetUIntProps}}(\hat{H}, \hat{l})} (\hat{H}(\hat{l})[i - 1 \mapsto \hat{H}(\hat{l})(i)] - i) \\
& \wedge \hat{v}_{uint} = \text{Value}(\top_{undef}) \sqcup \widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"0"}) \\
& \wedge (\hat{H}_2, \hat{C}_2) = (\hat{H}_1[\# \text{PureLocal}_R \mapsto \hat{H}_1(\# \text{PureLocal}_R)[@return \mapsto \hat{v}_1]], \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Array.prototype.slice"}, args) \rrbracket_{\hat{a}_{new}} ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S}) \\
& \text{where } (\hat{H}_1, \hat{C}_1) = \text{Oldify}(\hat{H}, \hat{C}, \hat{a}_{new}) \wedge \hat{l}_R = (\hat{a}_{new}, \text{Recent}) \quad // \text{Recency Abstraction} \\
& \wedge \hat{o}_{new} = \text{NewArrayObject}(0) \\
& \wedge \hat{v}_{len} = \widehat{\text{toUInt32}}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"})) \\
& \wedge \hat{v}_{start} = \widehat{\text{toInteger}}(\text{getArgValue}(args, \text{"0"})) \\
& \wedge \hat{n}_k = \begin{cases} \max((\hat{v}_{start} + v_{len}), 0) \sqcup \min(\hat{v}_{start}, v_{len}) & \text{if } \top_{bool} = \hat{v}_{start} < 0 \\ \max((\hat{v}_{start} + v_{len}), 0) & \text{if } \text{true} = \hat{v}_{start} < 0 \\ \min(\hat{v}_{start}, v_{len}) & \text{if } \text{false} = \hat{v}_{start} < 0 \end{cases} \\
& \wedge \hat{v}_{end} = \begin{cases} \widehat{\text{toInteger}}(\text{getArgValue}(args, \text{"0"})) \sqcup \hat{v}_{len} & \text{if } \top_{undef} \sqsubseteq \text{getArgValue}(args, \text{"1"}).1.1 \\ \widehat{\text{toInteger}}(\text{getArgValue}(args, \text{"0"})) & \text{otherwise} \end{cases} \\
& \wedge \hat{n}_{final} = \begin{cases} \max((\hat{v}_{end} + v_{len}), 0) \sqcup \min(\hat{v}_{end}, v_{len}) & \text{if } \top_{bool} = \hat{v}_{end} < 0 \\ \max((\hat{v}_{end} + v_{len}), 0) & \text{if } \text{true} = \hat{v}_{end} < 0 \\ \min(\hat{v}_{end}, v_{len}) & \text{if } \text{false} = \hat{v}_{end} < 0 \end{cases} \\
& \wedge \hat{o} = \begin{cases} \hat{o}_{slice} & \text{if } \hat{n}_k = \text{UIntSingle}(n_k) \wedge \hat{n}_{final} = \text{UIntSingle}(n_{final}) \\ \hat{o}_{uint} & \text{otherwise} \end{cases} \\
& \wedge \hat{o}_{slice} = \bigsqcup_{i \in \{n_k, \dots, n_{final} - 1\}} \hat{o}_{slice1} \sqcup \hat{o}_{slice2} \\
& \wedge \hat{o}_{slice1} = \begin{cases} \hat{o}_{new}[i - n_k \mapsto \hat{H}(\hat{l})(i)] & \text{if } \text{true} \sqsubseteq \widehat{\text{HasProperty}}(\hat{H}, \hat{l}, i) \\ \perp_{obj} & \text{otherwise} \end{cases} \\
& \wedge \hat{o}_{slice2} = \begin{cases} \hat{o}_{new} & \text{if } \text{false} \sqsubseteq \widehat{\text{HasProperty}}(\hat{H}, \hat{l}, i) \\ \perp_{obj} & \text{otherwise} \end{cases} \\
& \wedge \hat{o}_{uint} = \hat{o}_{new}[@default\_number \mapsto \hat{H}(\hat{l})(@default\_number)] \sqcup \text{Value}(\top_{undef}) \sqcup \bigsqcup_{i \in \widehat{\text{GetUIntProps}}(\hat{H}, \hat{l})} \hat{H}(\hat{l})(i) \\
& \wedge \hat{H}_1 = \hat{H}[\hat{l}_R \mapsto \bigsqcup_{\hat{l} \in \hat{C}.2} \hat{o}] \\
& \wedge (\hat{H}_2, \hat{C}_2) = (\hat{H}_1[\# \text{PureLocal}_R \mapsto \hat{H}_1(\# \text{PureLocal}_R)[@return \mapsto \hat{l}_R]], \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Array.prototype.splice"}, args) \rrbracket_{\hat{a}_{new}}((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S}) \\
& \text{where } (\hat{H}_1, \hat{C}_1) = \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new}) \wedge \hat{l}_R = (\hat{a}_{new}, \text{Recent}) \quad // \text{Recency Abstraction} \\
& \wedge \hat{o}_{new} = \text{NewArrayObject}(0) \\
& \wedge \hat{v}_{len} = \text{toUInt32}(\text{Proto}(\hat{H}, \hat{l}, \text{"length"})) \\
& \wedge \hat{n}_{argstat} = \text{getArgValue}(args, \text{"0"}), 0) \\
& \wedge \hat{n}_{start} = \begin{cases} \max((\hat{v}_{argstat} + \hat{v}_{len}), 0) \sqcup \min(\hat{v}_{argstat}, \hat{v}_{len}) & \text{if } \top_{bool} = \hat{v}_{argstat} < 0 \\ \max((\hat{v}_{argstat} + \hat{v}_{len}), 0) & \text{if } \text{true} = \hat{v}_{argstat} < 0 \\ \min(\hat{v}_{argstat}, \hat{v}_{len}) & \text{if } \text{false} = \hat{v}_{argstat} < 0 \end{cases} \\
& \wedge \hat{v}_{count} = \min(\text{toInteger}(\text{getArgValue}(args, \text{"1"})), 0), \hat{v}_{len} - \hat{n}_{start}) \\
& \wedge \hat{o} = \begin{cases} \hat{o}_{splice}[length \mapsto n_{final} - n_k] & \text{if } \hat{n}_{start} = \text{UIntSingle}(n_{start}) \wedge \hat{n}_{count} = \text{UIntSingle}(n_{count}) \\ \hat{o}_{uint}[length \mapsto \text{UInt}] & \text{otherwise} \end{cases} \\
& \wedge \hat{o}_{this_l} = \begin{cases} \hat{o}_{this_{del}}[length \mapsto n_{final} - n_k] & \text{if } \hat{n}_{start} = \text{UIntSingle}(n_{start}) \wedge \hat{n}_{count} = \text{UIntSingle}(n_{count}) \\ \hat{o}_{this_{uint}}[length \mapsto \text{UInt}] & \text{otherwise} \end{cases} \\
& \wedge \hat{o}_{slice} = \bigsqcup_{i \in \{n_k, \dots, n_{final} - 1\}} \hat{o}_{slice1} \sqcup \hat{o}_{slice2} \\
& \wedge \hat{o}_{slice1} = \begin{cases} \hat{o}_{new}[i - n_k \mapsto \hat{H}(\hat{l})(i)] & \text{if } \text{true} \sqsubseteq \widehat{\text{HasProperty}}(\hat{H}, \hat{l}, i) \\ \perp_{obj} & \text{otherwise} \end{cases} \\
& \wedge \hat{o}_{slice2} = \begin{cases} \hat{o}_{new} & \text{if } \text{false} \sqsubseteq \widehat{\text{HasProperty}}(\hat{H}, \hat{l}, i) \\ \perp_{obj} & \text{otherwise} \end{cases} \\
& \wedge \hat{o}_{uint} = \hat{o}_{new}[\text{@default\_number} \mapsto \hat{H}(\hat{l})(\text{@default\_number}) \sqcup \text{Value}(\top_{undef}) \sqcup \bigsqcup_{i \in \widehat{\text{GetUIntProps}}(\hat{H}, \hat{l})} \hat{H}(\hat{l})(i)] \\
& \wedge \hat{o}_{this_{uint}} = \hat{H}(\hat{l})[\text{@default\_number} \mapsto \hat{H}(\hat{l})(\text{@default\_number}) \sqcup \text{Value}(\top_{undef}) \sqcup \bigsqcup_{i \in \widehat{\text{GetUIntProps}}(\hat{H}, \hat{l})} \hat{H}(\hat{l})(i)] \\
& \wedge \hat{H}_1 = \hat{H}[\hat{l}_R \mapsto \hat{o}] \\
& \wedge (\hat{H}_2, \hat{C}_2) = (\hat{H}_1[\#PureLocal_R \mapsto \hat{H}_1(\#PureLocal_R)[\text{@return} \mapsto \hat{l}_R]], \hat{C})
\end{aligned}$$

## 11.2.8 String

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"String"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{n}_{arglen} = \widehat{\text{toUInt32}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"length"})) \\
& \quad \wedge \hat{s}_1 = \begin{cases} \hat{\omega} & \text{if } \text{UIntSingle}(0) \sqsubseteq \hat{n}_{arglen} \\ \perp_{string} & \text{otherwise} \end{cases} \\
& \quad \wedge \hat{s}_2 = \begin{cases} \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"0"}))) & \text{if } \text{UIntSingle}(n) \sqsubseteq \hat{n}_{arglen} \wedge n > 0 \\ \perp_{string} & \text{otherwise} \end{cases} \\
& \quad \wedge \hat{s} = \hat{s}_1 \sqcup \hat{s}_2 \\
& \quad \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{s})), \hat{C}) & \text{if } \hat{s} \not\sqsubseteq \perp_{String} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"String.constructor"}, args)]_{\hat{a}_{new}}((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_3, \hat{C}_3), \hat{S}) \\
& \text{where } (\hat{H}_1, \hat{C}_1) = \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new}) \wedge \hat{l}_R = (\hat{a}_{new}, \text{Recent}) \quad // \text{Recency Abstraction} \\
& \quad \wedge \hat{n}_{arglen} = \widehat{\text{toUInt32}}(\widehat{\text{getArgValue}}(\hat{H}_1, \hat{C}_1, \text{"length"})) \\
& \quad \wedge \hat{s}_1 = \begin{cases} \hat{\omega} & \text{if } \text{UIntSingle}(0) \sqsubseteq \hat{n}_{arglen} \\ \perp_{string} & \text{otherwise} \end{cases} \\
& \quad \wedge \hat{s}_2 = \begin{cases} \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\widehat{\text{getArgValue}}(\hat{H}_1, \hat{C}_1, \text{"0"}))) & \text{if } \text{UIntSingle}(n) \sqsubseteq \hat{n}_{arglen} \wedge n > 0 \\ \perp_{string} & \text{otherwise} \end{cases} \\
& \quad \wedge \hat{s} = \hat{s}_1 \sqcup \hat{s}_2 \\
& \quad \wedge \hat{H}_2 = \hat{H}_1[\hat{l}_R \mapsto \widehat{\text{NewString}}(\hat{s})] \\
& \quad \wedge (\hat{H}_3, \hat{C}_3) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}_2, \text{Value}(\hat{l}_R)), \hat{C}_1) & \text{if } \hat{s} \not\sqsubseteq \perp_{String} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"String.fromCharCode"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{n}_{arglen} = \widehat{\text{toUInt32}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"length"})) \\
& \quad \wedge \hat{s}_1 = \begin{cases} \hat{\omega} & \text{if } \text{UIntSingle}(0) \sqsubseteq \hat{n}_{arglen} \\ \perp_{string} & \text{otherwise} \end{cases} \\
& \quad \wedge \hat{s}_2 = \begin{cases} \top_{String} & \text{if } \top_{UIntSingle}(n) \neq \hat{n}_{arglen} \wedge \hat{n}_{arglen} \not\sqsubseteq \perp_{Number} \\ \hat{\omega} \hat{\vdash} \hat{s}_0 \hat{\vdash} \dots \hat{\vdash} \hat{s}_{n-1} & \text{if } \text{UIntSingle}(n) \sqsubseteq \hat{n}_{arglen} \wedge n > 0 \\ \perp_{string} & \text{otherwise} \end{cases} \\
& \quad \wedge \hat{s}_i = \widehat{\text{toChar}}(\widehat{\text{toUInt16}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"i"}))) \wedge \hat{s} = \hat{s}_1 \sqcup \hat{s}_2 \\
& \quad \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{s})), \hat{C}) & \text{if } \hat{s} \not\sqsubseteq \perp_{String} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

## 11.2.9 String.prototype

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"String.prototype.toString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}_1) \\
& \text{where } \hat{e}s = \begin{cases} \{\text{TypeError}\} & \text{if } \exists \hat{l} \in \hat{C}.2 : \hat{H}(\hat{l})(\text{@class}).1.2.1.5 \neq \text{"string"} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{L}_{string} = \{\hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \hat{H}(\hat{l})(\text{@class}).1.2.1.5 = \text{"string"}\} \\
& \wedge \hat{v} = \bigsqcup_{\hat{l} \in \hat{L}_{string}} \hat{H}(\hat{l})(\text{@primitive}).1.2 \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \hat{v}), \hat{C}) & \text{if } \hat{v} \not\sqsubseteq \perp_{value} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s)
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"String.prototype.valueOf"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}_1) \\
& \text{where } \hat{e}s = \begin{cases} \{\text{TypeError}\} & \text{if } \exists \hat{l} \in \hat{C}.2 : \hat{H}(\hat{l})(\text{@class}).1.2.1.5 \neq \text{"string"} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{L}_{string} = \{\hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \hat{H}(\hat{l})(\text{@class}).1.2.1.5 = \text{"string"}\} \\
& \wedge \hat{v} = \bigsqcup_{\hat{l} \in \hat{L}_{string}} \hat{H}(\hat{l})(\text{@primitive}).1.2 \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \hat{v}), \hat{C}) & \text{if } \hat{v} \not\sqsubseteq \perp_{value} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s)
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"String.prototype.charAt"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{L}_{prim} = \{\hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \text{"@primitive"} \in \hat{H}(\hat{l})\} \\
& \wedge \hat{v}_{this} = \bigsqcup_{\hat{l} \in \hat{L}_{prim}} \hat{H}(\hat{l})(\text{@primitive}).1.2 \quad // [[DefaultValue]]? \\
& \wedge \hat{s}_{this} = \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\hat{v}_{this})) \\
& \wedge \hat{n}_{size} = |\hat{s}_{this}| \\
& \wedge \hat{n}_{pos} = \widehat{\text{toInteger}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"0"})) \\
& \wedge \hat{v}_1 = \begin{cases} \hat{v}_{this} & \text{if } \text{true} \sqsubseteq (\hat{n}_{pos} < 0) \\ \perp_{value} & \text{otherwise} \end{cases} \\
& \wedge \hat{v}_2 = \begin{cases} \hat{v}_{this} & \text{if } \text{true} \sqsubseteq (\hat{n}_{size} < \hat{n}_{pos}) \vee \text{true} \sqsubseteq (\hat{n}_{size} = \hat{n}_{pos}) \\ \perp_{value} & \text{otherwise} \end{cases} \\
& \wedge \hat{v}_3 = \hat{v} = \hat{v}_1 \sqcup \hat{v}_2 \sqcup \alpha(\text{native.charAt}(\gamma(\hat{s}_{this}), \gamma(\hat{n}_{pos}))) \quad // java, scala \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \hat{v}), \hat{C}) & \text{if } \hat{v} \not\sqsubseteq \perp_{value} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"String.prototype.charCodeAt"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{L}_{prim} = \{\hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \text{"@primitive"} \in \hat{H}(\hat{l})\} \\
& \wedge \hat{v}_{this} = \bigsqcup_{\hat{l} \in \hat{L}_{prim}} \hat{H}(\hat{l})(\text{@primitive}).1.2 \quad // [[DefaultValue]]? \\
& \wedge \hat{s}_{this} = \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\hat{v}_{this})) \\
& \wedge \hat{n}_{size} = |\hat{s}_{this}| \\
& \wedge \hat{n}_{pos} = \widehat{\text{toInteger}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"0"})) \\
& \wedge \hat{v}_1 = \begin{cases} \text{NaN} & \text{if } \text{true} \sqsubseteq (\hat{n}_{pos} < 0) \\ \perp_{value} & \text{otherwise} \end{cases} \\
& \wedge \hat{v}_2 = \begin{cases} \text{NaN} & \text{if } \text{true} \sqsubseteq (\hat{n}_{size} < \hat{n}_{pos}) \vee \text{true} \sqsubseteq (\hat{n}_{size} = \hat{n}_{pos}) \\ \perp_{value} & \text{otherwise} \end{cases} \\
& \wedge \hat{v} = \hat{v}_1 \sqcup \hat{v}_2 \sqcup \alpha(\text{native.charCodeAt}(\gamma(\hat{s}_{this}), \gamma(\hat{n}_{pos})).\text{toInt}) \quad // java, scala \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \hat{v}), \hat{C}) & \text{if } \hat{v} \not\sqsubseteq \perp_{value} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\hat{\mathcal{I}}_{cp}[\llbracket \text{BuiltinCall}(\text{"String.prototype.concat"}, args) \rrbracket]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

$$\begin{aligned} \text{where } \hat{L}_{prim} &= \{\hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \text{"@primitive"} \in \hat{H}(\hat{l})\} \\ \wedge \hat{v}_{this} &= \bigsqcup_{\hat{l} \in \hat{L}_{prim}} \hat{H}(\hat{l})(\text{"@primitive"}).1.2 \quad // [[DefaultValue]]?? \\ \wedge \hat{s}_{this} &= \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\hat{v}_{this})) \\ \wedge \hat{n}_{arglen} &= \widehat{\text{getArgValue}}(args, \text{"length"}).1.4 \\ \wedge \hat{s} &= \begin{cases} \perp_{string} & \text{if } \hat{n}_{arglen} = \perp_{number} \\ \top_{string} & \text{if } \hat{n}_{arglen} \neq \text{UIntSingle} \\ \hat{s}_{this} + \hat{s}_0 + \dots + \hat{s}_{n-1} & \text{if } \hat{n}_{arglen} = \text{UIntSingle}(n) \end{cases} \\ \wedge \hat{s}_i &= \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\widehat{\text{getArgValue}}(args, \text{"i"}))) \\ \wedge (\hat{H}_1, \hat{C}_1) &= \begin{cases} (\text{ReturnStore}(\hat{H}, \text{Value}(\hat{s})), \hat{C}) & \text{if } \hat{s} \not\sqsubseteq \perp_{String} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \end{aligned}$$

$$\hat{\mathcal{I}}_{cp}[\llbracket \text{BuiltinCall}(\text{"String.prototype.indexOf"}, args) \rrbracket]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

$$\begin{aligned} \text{where } \hat{L}_{prim} &= \{\hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \text{"@primitive"} \in \hat{H}(\hat{l})\} \\ \wedge \hat{v}_{this} &= \bigsqcup_{\hat{l} \in \hat{L}_{prim}} \hat{H}(\hat{l})(\text{"@primitive"}).1.2 \quad // [[DefaultValue]]?? \\ \wedge \hat{s}_{this} &= \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\hat{v}_{this})) \\ \wedge \hat{n} &= \begin{cases} \perp_{number} & \text{if } \hat{s}_{this} = \perp_{string} \\ \hat{n}' & \text{if } \hat{s}_{this} = \text{NumStrSingle}(s_{this}) \vee \hat{s}_{this} = \text{OtherStrSingle}(s_{this}) \\ \top_{number} & \text{otherwise} \end{cases} \\ \wedge \hat{s}_{search} &= \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\widehat{\text{getArgValue}}(args, \text{"0"}))) \\ \wedge \hat{n}' &= \begin{cases} \perp_{number} & \text{if } \hat{s}_{search} = \perp_{string} \\ \hat{n}'' & \text{if } \hat{s}_{search} = \text{NumStrSingle}(s_{search}) \vee \hat{s}_{search} = \text{OtherStrSingle}(s_{search}) \\ \top_{number} & \text{otherwise} \end{cases} \\ \wedge \hat{n}_{pos} &= \widehat{\text{toInteger}}(\widehat{\text{getArgValue}}(args, \text{"1"})) \\ \wedge \hat{n}'' &= \begin{cases} \perp_{number} & \text{if } \hat{n}_{pos} = \perp_{number} \\ \hat{n}''' & \text{if } \hat{n}_{pos} = \text{UIntSingle}(n_{pos}) \\ \top_{number} & \text{otherwise} \end{cases} \\ \wedge n_{start} &= \min(\max(n_{pos}, 0), s_{this}.length) \\ \wedge \hat{n}''' &= \alpha(\text{native.string.indexOf}(s_{this}, s_{search}, n_{start})) \quad // java, scala \\ \wedge (\hat{H}_1, \hat{C}_1) &= \begin{cases} (\text{ReturnStore}(\hat{H}, \text{Value}(\hat{n})), \hat{C}) & \text{if } \hat{n} \not\sqsubseteq \perp_{Number} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \end{aligned}$$

$$\hat{\mathcal{I}}_{cp}[\llbracket \text{BuiltinCall}(\text{"String.prototype.lastIndexOf"}, args) \rrbracket]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

$$\begin{aligned} \text{where } \hat{L}_{prim} &= \{\hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \text{"@primitive"} \in \hat{H}(\hat{l})\} \\ \wedge \hat{v}_{this} &= \bigsqcup_{\hat{l} \in \hat{L}_{prim}} \hat{H}(\hat{l})(\text{"@primitive"}).1.2 \quad // [[DefaultValue]]?? \\ \wedge \hat{s}_{this} &= \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\hat{v}_{this})) \\ \wedge \hat{n} &= \begin{cases} \perp_{number} & \text{if } \hat{s}_{this} = \perp_{string} \\ \hat{n}' & \text{if } \hat{s}_{this} = \text{NumStrSingle}(s_{this}) \vee \hat{s}_{this} = \text{OtherStrSingle}(s_{this}) \\ \top_{number} & \text{otherwise} \end{cases} \\ \wedge \hat{s}_{search} &= \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\widehat{\text{getArgValue}}(args, \text{"0"}))) \\ \wedge \hat{n}' &= \begin{cases} \perp_{number} & \text{if } \hat{s}_{search} = \perp_{string} \\ \hat{n}'' & \text{if } \hat{s}_{search} = \text{NumStrSingle}(s_{search}) \vee \hat{s}_{search} = \text{OtherStrSingle}(s_{search}) \\ \top_{number} & \text{otherwise} \end{cases} \\ \wedge \hat{n}_{pos} &= \widehat{\text{toInteger}}(\widehat{\text{getArgValue}}(args, \text{"1"})) \\ \wedge \hat{n}'' &= \begin{cases} \perp_{number} & \text{if } \hat{n}_{pos} = \perp_{number} \\ \hat{n}''' & \text{if } \hat{n}_{pos} = \text{UIntSingle}(n_{pos}) \\ \top_{number} & \text{otherwise} \end{cases} \\ \wedge n_{start} &= \min(\max(n_{pos}, 0), s_{this}.length) \\ \wedge \hat{n}''' &= \alpha(\text{native.string.lastIndexOf}(s_{this}, s_{search}, n_{start})) \quad // java, scala \\ \wedge (\hat{H}_1, \hat{C}_1) &= \begin{cases} (\text{ReturnStore}(\hat{H}, \text{Value}(\hat{n})), \hat{C}) & \text{if } \hat{n} \not\sqsubseteq \perp_{Number} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"String.prototype.localeCompare"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{L}_{prim} = \{\hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \text{"@primitive"} \in \hat{H}(\hat{l})\} \\
& \wedge \hat{v}_{this} = \bigsqcup_{i \in \hat{L}_{prim}} \hat{H}(\hat{l})(\text{@primitive}).1.2 \quad // [[DefaultValue]]?? \\
& \wedge \hat{s}_{this} = \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\hat{v}_{this})) \\
& \wedge \hat{n} = \begin{cases} \perp_{number} & \text{if } \hat{s}_{this} = \perp_{string} \\ \hat{n}' & \text{if } \hat{s}_{this} = \text{NumStrSingle}(s_{this}) \vee \hat{s}_{this} = \text{OtherStrSingle}(s_{this}) \\ \top_{number} & \text{otherwise} \end{cases} \\
& \wedge \hat{s}_{that} = \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\text{getArgValue}(args, "0"))) \\
& \wedge \hat{n}' = \begin{cases} \perp_{number} & \text{if } \hat{s}_{that} = \perp_{string} \\ \hat{n}'' & \text{if } \hat{s}_{that} = \text{NumStrSingle}(s_{that}) \vee \hat{s}_{that} = \text{OtherStrSingle}(s_{that}) \\ \top_{number} & \text{otherwise} \end{cases} \\
& \wedge \hat{n}'' = \alpha(\text{native.string.compare}(s_{this}, s_{that})) \quad // \text{java, scala} \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{n})), \hat{C}) & \text{if } \hat{n} \not\sqsubseteq \perp_{Number} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"String.prototype.slice"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{L}_{prim} = \{\hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \text{"@primitive"} \in \hat{H}(\hat{l})\} \\
& \wedge \hat{v}_{this} = \bigsqcup_{i \in \hat{L}_{prim}} \hat{H}(\hat{l})(\text{@primitive}).1.2 \quad // [[DefaultValue]]?? \\
& \wedge \hat{s}_{this} = \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\hat{v}_{this})) \\
& \wedge \hat{s} = \begin{cases} \perp_{string} & \text{if } \hat{s}_{this} = \perp_{string} \\ \hat{s}' & \text{if } \hat{s}_{this} = \text{NumStrSingle}(s_{this}) \vee \hat{s}_{this} = \text{OtherStrSingle}(s_{this}) \\ \top_{string} & \text{otherwise} \end{cases} \\
& \wedge \hat{n}_{start} = \widehat{\text{toInteger}}(\text{getArgValue}(args, "0")) \\
& \wedge \hat{s}' = \begin{cases} \perp_{string} & \text{if } \hat{n}_{start} = \perp_{number} \\ \hat{s}'' & \text{if } \hat{n}_{start} = \text{UIntSingle}(n_{start}) \vee \hat{n}_{start} = \text{NUIntSingle}(n_{start}) \\ \top_{string} & \text{otherwise} \end{cases} \\
& \wedge \hat{n}_{end} = \widehat{\text{toInteger}}(\text{getArgValue}(args, "1")) \\
& \wedge \hat{s}'' = \begin{cases} \perp_{string} & \text{if } \hat{n}_{end} = \perp_{number} \\ \hat{s}''' & \text{if } \hat{n}_{end} = \text{UIntSingle}(n_{end}) \vee \hat{n}_{end} = \text{NUIntSingle}(n_{end}) \\ \top_{string} & \text{otherwise} \end{cases} \\
& \wedge \hat{n}'_{start} = \begin{cases} \max(n_{start} + s_{this}.length, 0) & \text{if } n_{start} < 0 \\ \min(n_{start}, s_{this}.length) & \text{otherwise} \end{cases} \\
& \wedge \hat{n}'_{end} = \begin{cases} \max(n_{end} + s_{this}.length, 0) & \text{if } n_{end} < 0 \\ \min(n_{end}, s_{this}.length) & \text{otherwise} \end{cases} \\
& \wedge \hat{s}''' = \alpha(\text{native.string.slice}(s_{this}, \hat{s}'_{start}, \hat{s}'_{end})) \quad // \text{java, scala} \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{s})), \hat{C}) & \text{if } \hat{s} \not\sqsubseteq \perp_{String} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"String.prototype.substring"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{L}_{prim} = \{\hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \text{"@primitive"} \in \hat{H}(\hat{l})\} \\
& \wedge \hat{v}_{this} = \bigsqcup_{\hat{l} \in \hat{L}_{prim}} \hat{H}(\hat{l})(\text{"@primitive"}).1.2 \quad // [[DefaultValue]]?? \\
& \wedge \hat{s}_{this} = \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\hat{v}_{this})) \\
& \wedge \hat{s} = \begin{cases} \perp_{string} & \text{if } \hat{s}_{this} = \perp_{string} \\ \hat{s}' & \text{if } \hat{s}_{this} = \text{NumStrSingle}(s_{this}) \vee \hat{s}_{this} = \text{OtherStrSingle}(s_{this}) \\ \top_{string} & \text{otherwise} \end{cases} \\
& \wedge \hat{n}_{start} = \widehat{\text{toInteger}}(\widehat{\text{getArgValue}}(args, "0")) \\
& \wedge \hat{s}' = \begin{cases} \perp_{string} & \text{if } \hat{n}_{start} = \perp_{number} \\ \hat{s}'' & \text{if } \hat{n}_{start} = \text{UIntSingle}(n_{start}) \vee \hat{n}_{start} = \text{NUIntSingle}(n_{start}) \\ \top_{string} & \text{otherwise} \end{cases} \\
& \wedge \hat{n}_{end} = \widehat{\text{toInteger}}(\widehat{\text{getArgValue}}(args, "1")) \\
& \wedge \hat{s}'' = \begin{cases} \perp_{string} & \text{if } \hat{n}_{end} = \perp_{number} \\ \hat{s}''' & \text{if } \hat{n}_{end} = \text{UIntSingle}(n_{end}) \vee \hat{n}_{end} = \text{NUIntSingle}(n_{end}) \\ \top_{string} & \text{otherwise} \end{cases} \\
& \wedge n'_{start} = \min(\max(n_{start}, 0), s_{this}.length) \wedge n'_{end} = \min(\max(n_{end}, 0), s_{this}.length) \\
& \wedge \hat{s}''' = \alpha(\text{native.string.slice}(s_{this}, \min(n'_{start}, n'_{end}), \max(n'_{start}, n'_{end}))) \quad // java, scala \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{s})), \hat{C}) & \text{if } \hat{s} \not\sqsubseteq \perp_{String} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"String.prototype.toLowerCase"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{L}_{prim} = \{\hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \text{"@primitive"} \in \hat{H}(\hat{l})\} \\
& \wedge \hat{v}_{this} = \bigsqcup_{\hat{l} \in \hat{L}_{prim}} \hat{H}(\hat{l})(\text{"@primitive"}).1.2 \quad // [[DefaultValue]]?? \\
& \wedge \hat{s}_{this} = \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\hat{v}_{this})) \\
& \wedge \hat{s} = \begin{cases} \perp_{string} & \text{if } \hat{s}_{this} = \perp_{string} \\ \hat{s}' & \text{if } \hat{s}_{this} = \text{NumStrSingle}(s_{this}) \vee \hat{s}_{this} = \text{OtherStrSingle}(s_{this}) \\ \top_{string} & \text{otherwise} \end{cases} \\
& \wedge \hat{s}' = \alpha(\text{native.string.toLowerCase}(s_{this})) \quad // java, scala \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{s})), \hat{C}) & \text{if } \hat{s} \not\sqsubseteq \perp_{String} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"String.prototype.toLocaleLowerCase"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{L}_{prim} = \{\hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \text{"@primitive"} \in \hat{H}(\hat{l})\} \\
& \wedge \hat{v}_{this} = \bigsqcup_{\hat{l} \in \hat{L}_{prim}} \hat{H}(\hat{l})(\text{"@primitive"}).1.2 \quad // [[DefaultValue]]?? \\
& \wedge \hat{s}_{this} = \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\hat{v}_{this})) \\
& \wedge \hat{s} = \begin{cases} \perp_{string} & \text{if } \hat{s}_{this} = \perp_{string} \\ \hat{s}' & \text{if } \hat{s}_{this} = \text{NumStrSingle}(s_{this}) \vee \hat{s}_{this} = \text{OtherStrSingle}(s_{this}) \\ \top_{string} & \text{otherwise} \end{cases} \\
& \wedge \hat{s}' = \alpha(\text{native.string.toLocaleLowerCase}(s_{this})) \quad // java, scala \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{s})), \hat{C}) & \text{if } \hat{s} \not\sqsubseteq \perp_{String} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$



$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"String.prototype.toUpperCase"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{L}_{prim} = \{\hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \text{"@primitive"} \in \hat{H}(\hat{l})\} \\
& \wedge \hat{v}_{this} = \bigsqcup_{\hat{l} \in \hat{L}_{prim}} \hat{H}(\hat{l})(\text{"@primitive"}).1.2 \quad // [[DefaultValue]]?? \\
& \wedge \hat{s}_{this} = \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\hat{v}_{this})) \\
& \wedge \hat{s} = \begin{cases} \perp_{string} & \text{if } \hat{s}_{this} = \perp_{string} \\ \hat{s}' & \text{if } \hat{s}_{this} = \text{NumStrSingle}(s_{this}) \vee \hat{s}_{this} = \text{OtherStrSingle}(s_{this}) \\ \top_{string} & \text{otherwise} \end{cases} \\
& \wedge \hat{s}' = \alpha(\text{native.string.toUpperCase}(s_{this})) \quad // \text{java, scala} \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{s})), \hat{C}) & \text{if } \hat{s} \not\sqsubseteq \perp_{String} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"String.prototype.toLocaleUpperCase"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{L}_{prim} = \{\hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \text{"@primitive"} \in \hat{H}(\hat{l})\} \\
& \wedge \hat{v}_{this} = \bigsqcup_{\hat{l} \in \hat{L}_{prim}} \hat{H}(\hat{l})(\text{"@primitive"}).1.2 \quad // [[DefaultValue]]?? \\
& \wedge \hat{s}_{this} = \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\hat{v}_{this})) \\
& \wedge \hat{s} = \begin{cases} \perp_{string} & \text{if } \hat{s}_{this} = \perp_{string} \\ \hat{s}' & \text{if } \hat{s}_{this} = \text{NumStrSingle}(s_{this}) \vee \hat{s}_{this} = \text{OtherStrSingle}(s_{this}) \\ \top_{string} & \text{otherwise} \end{cases} \\
& \wedge \hat{s}' = \alpha(\text{native.string.toUpperCase}(s_{this})) \quad // \text{java, scala} \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{s})), \hat{C}) & \text{if } \hat{s} \not\sqsubseteq \perp_{String} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"String.prototype.trim"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{L}_{prim} = \{\hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \text{"@primitive"} \in \hat{H}(\hat{l})\} \\
& \wedge \hat{v}_{this} = \bigsqcup_{\hat{l} \in \hat{L}_{prim}} \hat{H}(\hat{l})(\text{"@primitive"}).1.2 \quad // [[DefaultValue]]?? \\
& \wedge \hat{s}_{this} = \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\hat{v}_{this})) \\
& \wedge \hat{s} = \begin{cases} \perp_{string} & \text{if } \hat{s}_{this} = \perp_{string} \\ \hat{s}' & \text{if } \hat{s}_{this} = \text{NumStrSingle}(s_{this}) \vee \hat{s}_{this} = \text{OtherStrSingle}(s_{this}) \\ \top_{string} & \text{otherwise} \end{cases} \\
& \wedge \hat{s}' = \alpha(\text{native.string.trim}(s_{this})) \quad // \text{java, scala} \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{s})), \hat{C}) & \text{if } \hat{s} \not\sqsubseteq \perp_{String} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

### 11.2.10 Boolean

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Boolean.constructor"}, args) \rrbracket_{\hat{a}_{new}} ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_3, \hat{C}_3), \hat{S}) \\
& \text{where } \hat{b} = \widehat{\text{toBoolean}}(\text{getArgValue}(args, \text{"0"})) \\
& \wedge (\hat{H}_1, \hat{C}_1) = \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new}) \quad // \text{Recency Abstraction} \\
& \wedge \hat{l}_R = (\hat{a}_{new}, \text{Recent}) \quad // \text{Recency Abstraction} \\
& \wedge \hat{o}_{new} = \widehat{\text{NewBoolean}}(\hat{b}) \\
& \wedge \hat{H}_2 = \hat{H}_1[\hat{l}_R \mapsto \hat{o}_{new}] \\
& \wedge (\hat{H}_3, \hat{C}_3) = (\widehat{\text{ReturnStore}}(\hat{H}_2, \text{Value}(\hat{l}_R)), \hat{C}_1)
\end{aligned}$$

### 11.2.11 Boolean.prototype

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Boolean.prototype.toString"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}_1) \\
& \text{where } \hat{L}_{this} = \hat{C}.2 \\
& \wedge \hat{e}s = \begin{cases} \{\text{TypeError}\} & \text{if } \exists l \in \hat{L}_{this} : \hat{H}(l)(@class).1.2.1.5 \neq \text{"Boolean"} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{L}_{bool} = \{ l \mid l \in \hat{L}_{this} \wedge \hat{H}(l)(@class).1.2.1.5 = \text{"Boolean"} \} \\
& \wedge \hat{b} = \bigsqcup_{l \in \hat{L}_{bool}} \hat{H}(l)(@primitive).1.2.1.3 \\
& \wedge \hat{s} = \begin{cases} \text{"true"} & \text{if } \hat{b} = \text{true} \\ \text{"false"} & \text{if } \hat{b} = \text{false} \\ \text{OtherStr} & \text{if } \hat{b} \sqsubseteq \text{true} \wedge \hat{b} \sqsubseteq \text{false} \\ \perp_{string} & \text{otherwise} \end{cases} \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s) \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{s})), \hat{C}) & \text{if } \hat{s} \not\sqsubseteq \perp_{string} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Boolean.prototype.valueOf"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}_1) \\
& \text{where } \hat{L}_{this} = \hat{C}.2 \\
& \wedge \hat{e}s = \begin{cases} \{\text{TypeError}\} & \text{if } \exists l \in \hat{L}_{this} : \hat{H}(l)(@class).1.2.1.5 \neq \text{"Boolean"} \\ \{\} & \text{otherwise} \end{cases} \\
& \wedge \hat{L}_{bool} = \{ l \mid l \in \hat{L}_{this} \wedge \hat{H}(l)(@class).1.2.1.5 = \text{"Boolean"} \} \\
& \wedge \hat{b} = \bigsqcup_{l \in \hat{L}_{bool}} \hat{H}(l)(@primitive).1.2.1.3 \\
& \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{e}s) \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{b})), \hat{C}) & \text{if } \hat{b} \not\sqsubseteq \perp_{string} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

### 11.2.12 Number

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Number"}, args)_{\hat{a}_{new}}]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_3, \hat{C}_3), \hat{S}) \\
& \text{where } \wedge \hat{n}_{len} = \widehat{\text{toUInt32}}(\widehat{\text{getArgValue}}(args, \text{"length"})) \\
& \wedge \hat{v}_{arg1} = \widehat{\text{getArgValue}}(args, \text{"0"}) \\
& \wedge \hat{v}_1 = \begin{cases} \text{Value}(\alpha(0)) & \text{if } \text{UIntSgle}(0) \sqsubseteq \hat{n}_{len} \\ \perp_{value} & \text{otherwise} \end{cases} \\
& \wedge \hat{v}_2 = \begin{cases} \text{Value}(\widehat{\text{toNumber}}(\widehat{\text{toPrimitive}}(\hat{v}_{arg1}))) & \text{if } \text{UIntSgle}(1) \neq \hat{n}_{len} \wedge \hat{n}_{len} \not\sqsubseteq \perp_{Number} \\ \perp_{value} & \text{otherwise} \end{cases} \\
& \wedge \hat{v} = \hat{v}_1 \sqcup \hat{v}_2 \\
& \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}, \hat{v}), \hat{C}) & \text{if } \hat{v} \not\sqsubseteq \perp_{value} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Number.constructor"}, args)_{\hat{a}_{new}}]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_3, \hat{C}_3), \hat{S}) \\
& \text{where } (\hat{H}_1, \hat{C}_1) = \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new}) \wedge \hat{l}_R = (\hat{a}_{new}, \text{Recent}) \quad // \text{Recency Abstraction} \\
& \wedge \hat{n}_{len} = (\widehat{\text{getArgValue}}(args, \text{"length"})).1.4 \\
& \wedge \hat{v}_1 = \begin{cases} \text{Value}(\alpha(0)) & \text{if } \text{UIntSgle}(0) \sqsubseteq \hat{n}_{len} \\ \perp_{value} & \text{otherwise} \end{cases} \\
& \wedge \hat{v}_2 = \begin{cases} \widehat{\text{toNumber}}(\widehat{\text{toPrimitive}}(\widehat{\text{getArgValue}}(args, \text{"0"}))) & \text{if } \text{UIntSgle}(1) \sqsubseteq \hat{n}_{len} \\ \perp_{value} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_2 = \begin{cases} \hat{H}_1[\hat{l}_R \mapsto \widehat{\text{NewNumber}}(\hat{v}_1 \sqcup \hat{v}_2)] & \text{if } \hat{v}_1 \sqcup \hat{v}_2 \sqsubseteq \perp_{value} \\ \perp_{Heap} & \text{otherwise} \end{cases} \\
& \wedge (\hat{H}_3, \hat{C}_3) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}_2, \text{Value}(\hat{l}_R)), \hat{C}_1) & \text{if } \hat{v}_1 \sqcup \hat{v}_2 \not\sqsubseteq \perp_{value} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

### 11.2.13 Number.prototype

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Number.prototype.toString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}_1) \\
& \text{where } \hat{n}_{arglen} = \text{toUInt32}(\text{getArgValue}(args, \text{"length"})) \\
& \quad \wedge \hat{v}_{prim} = \bigsqcup_{\hat{l} \in \hat{C}.2} \hat{H}(\hat{l})(\text{@primitive}).1.2 \\
& \quad \wedge \hat{L}_{num} = \{ l \mid l \in \hat{L}_{this} \wedge \hat{H}(\hat{l})(\text{@class}).1.2.1.5 = \text{"Number"} \} \\
& \quad \wedge \hat{es}_1 = \begin{cases} \{\text{TypeError}\} & \text{if } \exists \hat{l} \in \hat{L}_{this} : \hat{H}(\hat{l})(\text{@class}).1.2.1.5 \neq \text{"Number"} \\ \{\} & \text{otherwise} \end{cases} \\
& \quad \wedge (\hat{v}, \hat{es}_2) = \begin{cases} (Value(\text{toString}(\hat{v}_{prim}.1)), \perp_{Exception}) & \text{if } \hat{n}_{arglen} = \text{UIntSingle}(0) \\ (Value(\top_{String}), \hat{es}_{arg}) & \text{if } \hat{n}_{arglen} = \text{UIntSingle}(n_{arglen}) \wedge n_{arglen} > 0 \\ (\perp_{Value}, \perp_{Exception}) & \text{if } \hat{n}_{arglen} = \perp_{Number} \\ (Value(\top_{String}), \perp_{Exception}) & \text{otherwise} \end{cases} \\
& \quad \wedge \hat{es}_{arg} = \begin{cases} \{\text{RangeError}\} & \text{if } n_{arglen} < 1 \vee n_{arglen} > 36 \\ \{\} & \text{otherwise} \end{cases} \\
& \quad \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{es}_1 \sqcup \hat{es}_2) \\
& \quad \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\text{ReturnStore}(\hat{H}, Value(\hat{s})), \hat{C}) & \text{if } \hat{s} \not\sqsubseteq \perp_{String} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Number.prototype.toLocaleString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{n}_{arglen} = \text{toUInt32}(\text{getArgValue}(args, \text{"length"})) \\
& \quad \wedge \hat{v}_{prim} = \bigsqcup_{\hat{l} \in \hat{C}.2} \hat{H}(\hat{l})(\text{@primitive}).1.2 \wedge \hat{v} = Value(\text{toString}(\hat{v}_{prim}.1)) \\
& \quad \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\text{ReturnStore}(\hat{H}, \hat{v}), \hat{C}) & \text{if } \hat{v} \not\sqsubseteq \perp_{Value} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Number.prototype.valueOf"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}_1) \\
& \text{where } \hat{es} = \begin{cases} \{\text{TypeError}\} & \text{if } \exists \hat{l} \in \hat{C}.2 : \hat{H}(\hat{l})(\text{@class}).1.2.1.5 \neq \text{"Number"} \\ \{\} & \text{otherwise} \end{cases} \\
& \quad \wedge \hat{L}_{num} = \{ l \mid l \in \hat{C}.2 \wedge \hat{H}(\hat{l})(\text{@class}).1.2.1.5 = \text{"Number"} \} \\
& \quad \wedge \hat{n} = \bigsqcup_{\hat{l} \in \hat{L}_{num}} \hat{H}(\hat{l})(\text{@primitive}).1.2.1.4 \\
& \quad \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{es}) \\
& \quad \wedge (\hat{H}_1, \hat{C}_1) = \begin{cases} (\text{ReturnStore}(\hat{H}, Value(\hat{n})), \hat{C}) & \text{if } \hat{s} \not\sqsubseteq \perp_{Number} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Number.prototype.toFixed"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}_1) \\
& \text{where } \hat{v}_1 = \text{getArgValue}(args, \text{"0"}) \\
& \quad \wedge \hat{es} = \begin{cases} \{\text{RangeError}\} & \text{if } \hat{v}_1 < \hat{0} \vee \hat{v}_1 > \hat{20} \\ \{\} & \text{otherwise} \end{cases} \\
& \quad \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{es}) \\
& \quad \wedge (\hat{H}_1, \hat{C}_1) = (\text{ReturnStore}(\hat{H}, Value(\top_{String})), \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Number.prototype.toExponential"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}_1) \\
& \text{where } \hat{v}_1 = \text{getArgValue}(args, \text{"0"}) \\
& \quad \wedge \hat{es} = \begin{cases} \{\text{RangeError}\} & \text{if } \hat{v}_1 < \hat{0} \vee \hat{v}_1 > \hat{20} \\ \{\} & \text{otherwise} \end{cases} \\
& \quad \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{es}) \\
& \quad \wedge (\hat{H}_1, \hat{C}_1) = (\text{ReturnStore}(\hat{H}, Value(\top_{String})), \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Number.prototype.toPrecision"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}_1) \\
& \text{where } \hat{v}_1 = \text{getArgValue}(args, \text{"0"}) \\
& \quad \wedge \hat{es} = \begin{cases} \{\text{RangeError}\} & \text{if } \hat{v}_1 < \hat{1} \vee \hat{v}_1 > \hat{21} \\ \{\} & \text{otherwise} \end{cases} \\
& \quad \wedge \hat{S}_1 = \hat{S} \sqcup \widehat{\text{RaiseException}}(\hat{H}, \hat{C}, \hat{es}) \\
& \quad \wedge (\hat{H}_1, \hat{C}_1) = (\text{ReturnStore}(\hat{H}, Value(\top_{String})), \hat{C})
\end{aligned}$$

### 11.2.14 Math

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Math.abs"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{v} = \text{getArgValue}(args, \text{"0"}) \wedge \hat{n} = \widehat{\text{toNumber}(\text{toPrimitive}(\hat{v}))} \\
& \wedge \hat{p}\hat{v} = \begin{cases} \hat{n} & \text{if } \hat{n} \in \{ \text{NaN}, \text{UInt}, \text{NUInt}, \perp_{\text{Number}} \} \\ +\text{Inf} & \text{if } \hat{n} \in \{ +\text{Inf}, -\text{Inf}, \text{Inf} \} \\ \alpha(\text{abs}(\hat{n})) & \text{if } \hat{n} \in \{ \text{UIntSingle}(\hat{n}_1), \text{NUIntSingle}(\hat{n}_1) \} \\ \top_{\text{Number}} & \text{otherwise} \end{cases} \\
& \wedge (\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{p}\hat{v})), \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Math.acos"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{v} = \text{getArgValue}(args, \text{"0"}) \wedge \hat{n} = \widehat{\text{toNumber}(\text{toPrimitive}(\hat{v}))} \\
& \wedge \hat{p}\hat{v} = \begin{cases} \perp_{\text{Number}} & \text{if } \hat{n} = \perp_{\text{Number}} \\ \text{NaN} & \text{if } \hat{n} \in \left\{ \text{NaN}, \text{Inf}, +\text{Inf}, -\text{Inf}, \right. \\ & \left. \text{UIntSingle}(\hat{n}_1), \text{NUIntSingle}(\hat{n}_1) \mid n_1 < -1 \vee 1 < n_1 \right\} \\ \alpha(\text{acos}(\hat{n})) & \text{if } \hat{n} \in \left\{ \text{UIntSingle}(\hat{n}), \text{NUIntSingle}(\hat{n}_1) \mid -1 \geq \hat{n} \geq 1 \right\} \\ \top_{\text{Number}} & \text{otherwise} \end{cases} \\
& \wedge (\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{p}\hat{v})), \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Math.asin"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{v} = \text{getArgValue}(args, \text{"0"}) \wedge \hat{n} = \widehat{\text{toNumber}(\text{toPrimitive}(\hat{v}))} \\
& \wedge \hat{p}\hat{v} = \begin{cases} \perp_{\text{Number}} & \text{if } \hat{n} = \perp_{\text{Number}} \\ \text{NaN} & \text{if } \hat{n} \in \left\{ \text{NaN}, \text{Inf}, +\text{Inf}, -\text{Inf}, \right. \\ & \left. \text{UIntSingle}(\hat{n}), \text{NUIntSingle}(\hat{n}) \mid n_1 < -1 \vee 1 < n_1 \right\} \\ \alpha(\text{asin}(\hat{n})) & \text{if } \hat{n} \in \left\{ \text{UIntSingle}(\hat{n}), \text{NUIntSingle}(\hat{n}) \mid -1 \geq \hat{n} \geq 1 \right\} \\ \top_{\text{Number}} & \text{otherwise} \end{cases} \\
& \wedge (\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{p}\hat{v})), \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Math.atan"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{v} = \text{getArgValue}(args, \text{"0"}) \wedge \hat{n} = \widehat{\text{toNumber}(\text{toPrimitive}(\hat{v}))} \\
& \wedge \hat{p}\hat{v} = \begin{cases} \perp_{\text{Number}} & \text{if } \hat{n} = \perp_{\text{Number}} \\ \text{NaN} & \text{if } \hat{n} = \text{NaN} \\ \text{NUInt} & \text{if } \hat{n} = \text{Inf} \\ \text{NUIntSingle}(\frac{\hat{\pi}}{2}) & \text{if } \hat{n} = +\text{Inf} \\ \text{NUIntSingle}(-\frac{\hat{\pi}}{2}) & \text{if } \hat{n} = -\text{Inf} \\ \alpha(\text{atan}(\hat{n})) & \text{if } \hat{n} \in \{ \text{UIntSingle}(\hat{n}_1), \text{NUIntSingle}(\hat{n}) \} \\ \top_{\text{Number}} & \text{otherwise} \end{cases} \\
& \wedge (\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{p}\hat{v})), \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Math.atan2"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{v}_x = \widehat{\text{getArgValue}}(args, \text{"0"}) \wedge \hat{n}_x = \widehat{\text{toNumber}}(\widehat{\text{toPrimitive}}(\hat{v}_x)) \\
& \quad \wedge \hat{v}_y = \widehat{\text{getArgValue}}(args, \text{"1"}) \wedge \hat{n}_y = \widehat{\text{toNumber}}(\widehat{\text{toPrimitive}}(\hat{v}_y)) \\
& \quad \wedge \hat{p}v_1 = \begin{cases} \perp_{Number} & \text{if } \hat{n}_y = \perp_{Number} \vee \hat{n}_x = \perp_{Number} \\ \text{NaN} & \text{if } \hat{n}_y = \text{NaN} \vee \hat{n}_x = \text{NaN} \\ \top_{Number} & \text{if } \hat{n}_y = \top_{Number} \vee \hat{n}_x = \top_{Number} \end{cases} \\
& \quad \wedge \hat{p}v_2 = \begin{cases} \text{UInt}\hat{S}\text{ngle}(\hat{0}) & \text{if } \hat{n}_y \in \left\{ \text{UInt}, \text{NUInt}, \text{UInt}\hat{S}\text{ngle}(\hat{n}_1), \text{NUInt}\hat{S}\text{ngle}(\hat{n}_1) \right\} \\ & \quad \wedge \hat{n}_x = +\text{Inf} \\ \text{UInt} & \text{if } \hat{n}_y \in \left\{ \text{UInt}, \text{NUInt} \right\} \wedge \hat{n}_x = -\text{Inf} \\ \text{NUInt}\hat{S}\text{ngle}(\hat{\pi}) & \text{if } \hat{n}_y \in \left\{ \text{UInt}\hat{S}\text{ngle}(\hat{n}_1), \text{NUInt}\hat{S}\text{ngle}(\hat{n}_1) \mid \hat{0} \leq \hat{n}_1 \right\} \\ & \quad \wedge \hat{n}_x = -\text{Inf} \\ \text{NUInt}\hat{S}\text{ngle}(-\hat{\pi}) & \text{if } \hat{n}_y \in \left\{ \text{NUInt}\hat{S}\text{ngle}(\hat{n}_1) \mid \hat{n}_1 < \hat{0} \right\} \\ & \quad \wedge \hat{n}_x = -\text{Inf} \\ \text{UInt} & \text{if } \hat{n}_y \in \left\{ \text{UInt}, \text{NUInt} \right\} \wedge \hat{n}_x = \text{Inf} \\ \text{NUInt}\hat{S}\text{ngle}(\frac{\hat{\pi}}{2}) & \text{if } \hat{n}_y = +\text{Inf} \\ & \quad \wedge \hat{n}_x \in \left\{ \text{UInt}, \text{NUInt}, \text{UInt}\hat{S}\text{ngle}(\hat{n}_1), \text{NUInt}\hat{S}\text{ngle}(\hat{n}_1) \right\} \\ \text{NUInt}\hat{S}\text{ngle}(-\frac{\hat{\pi}}{2}) & \text{if } \hat{n}_y = -\text{Inf} \\ & \quad \wedge \hat{n}_x \in \left\{ \text{UInt}, \text{NUInt}, \text{UInt}\hat{S}\text{ngle}(\hat{n}_1), \text{NUInt}\hat{S}\text{ngle}(\hat{n}_1) \right\} \\ \text{NUInt}\hat{S}\text{ngle}(\frac{\hat{\pi}}{4}) & \text{if } \hat{n}_y = +\text{Inf} \wedge \hat{n}_x = +\text{Inf} \\ \text{NUInt}\hat{S}\text{ngle}(\frac{3\hat{\pi}}{4}) & \text{if } \hat{n}_y = +\text{Inf} \wedge \hat{n}_x = -\text{Inf} \\ \text{NUInt}\hat{S}\text{ngle}(\frac{-\hat{\pi}}{4}) & \text{if } \hat{n}_y = -\text{Inf} \wedge \hat{n}_x = +\text{Inf} \\ \text{NUInt}\hat{S}\text{ngle}(\frac{-3\hat{\pi}}{4}) & \text{if } \hat{n}_y = -\text{Inf} \wedge \hat{n}_x = -\text{Inf} \\ \text{NUInt} & \text{if } \hat{n}_y = \text{Inf} \wedge \hat{n}_x \in \left\{ +\text{Inf}, -\text{Inf} \right\} \\ \text{NUInt} & \text{if } \hat{n}_y \in \left\{ +\text{Inf}, -\text{Inf} \right\} \wedge \hat{n}_x = \text{Inf} \\ \text{NUInt} & \text{if } \hat{n}_y = \text{Inf} \wedge \hat{n}_x = \text{Inf} \\ \alpha(\text{atan2}(\hat{n}_1, \hat{n}_2)) & \text{if } \hat{n}_y \in \left\{ \text{UInt}\hat{S}\text{ngle}(\hat{n}_1), \text{NUInt}\hat{S}\text{ngle}(\hat{n}_1) \right\} \\ & \quad \wedge \hat{n}_x \in \left\{ \text{UInt}\hat{S}\text{ngle}(\hat{n}_2), \text{NUInt}\hat{S}\text{ngle}(\hat{n}_2) \right\} \\ \top_{Number} & \text{otherwise} \end{cases} \\
& \quad \wedge \hat{p}v = \hat{p}v_1 \sqcup \hat{p}v_2 \sqcup \hat{p}v_3 \sqcup \hat{p}v_4 \\
& \quad \wedge (\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{p}v)), \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Math.ceil"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{v} = \widehat{\text{getArgValue}}(args, \text{"0"}) \wedge \hat{n} = \widehat{\text{toNumber}}(\widehat{\text{toPrimitive}}(\hat{v})) \\
& \quad \wedge \hat{p}v = \begin{cases} \hat{n} & \text{if } \hat{n} \in \left\{ \perp_{Number}, \text{NaN}, \text{Inf}, +\text{Inf}, -\text{Inf}, \text{UInt}, \text{UInt}\hat{S}\text{ngle}(\hat{n}) \right\} \\ \alpha(\text{ceil}(\hat{n})) & \text{if } \hat{n} = \text{NUInt}\hat{S}\text{ngle}(\hat{n}) \\ \top_{Number} & \text{otherwise} \end{cases} \\
& \quad \wedge (\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{p}v)), \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Math.cos"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{v} = \widehat{\text{getArgValue}}(args, \text{"0"}) \wedge \hat{n} = \widehat{\text{toNumber}}(\widehat{\text{toPrimitive}}(\hat{v})) \\
& \quad \wedge \hat{p}v = \begin{cases} \perp_{Number} & \text{if } \hat{n} = \perp_{Number} \\ \text{NaN} & \text{if } \hat{n} \in \left\{ \text{NaN}, +\text{Inf}, -\text{Inf}, \text{Inf} \right\} \\ \alpha(\cos(\hat{n})) & \text{if } \hat{n} \in \left\{ \text{UInt}\hat{S}\text{ngle}(\hat{n}), \text{NUInt}\hat{S}\text{ngle}(\hat{n}) \right\} \\ \top_{Number} & \text{otherwise} \end{cases} \\
& \quad \wedge (\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{p}v)), \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Math.exp"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{v} = \text{getArgValue}(args, \text{"0"}) \wedge \hat{n} = \widehat{\text{toNumber}(\text{toPrimitive}(\hat{v}))} \\
& \wedge \hat{p}v = \begin{cases} \hat{n} & \text{if } \hat{n} \in \{ \perp_{Number}, \text{NaN}, +\text{Inf}, \text{NUInt} \} \\ \text{UIntSingle}(\hat{0}) & \text{if } \hat{n} = -\text{Inf} \\ \alpha(\exp(\hat{n})) & \text{if } \hat{n} \in \{ \text{UIntSingle}(\hat{n}), \text{NUIntSingle}(\hat{n}) \} \\ \top_{Number} & \text{otherwise} \end{cases} \\
& \wedge (\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{p}v)), \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Math.floor"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{v} = \text{getArgValue}(args, \text{"0"}) \wedge \hat{n} = \widehat{\text{toNumber}(\text{toPrimitive}(\hat{v}))} \\
& \wedge \hat{p}v = \begin{cases} \hat{n} & \text{if } \hat{n} \in \{ \perp_{Number}, \text{Inf}, +\text{Inf}, -\text{Inf}, \text{NaN}, \text{UInt}, \text{UIntSingle}(\hat{n}) \} \\ \alpha(\text{floor}(\hat{n})) & \text{if } \hat{n} = \text{NUIntSingle}(\hat{n}) \\ \top_{Number} & \text{otherwise} \end{cases} \\
& \wedge (\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{p}v)), \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Math.log"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{v} = \text{getArgValue}(args, \text{"0"}) \wedge \hat{n} = \widehat{\text{toNumber}(\text{toPrimitive}(\hat{v}))} \\
& \wedge \hat{p}v = \begin{cases} \perp_{Number} & \text{if } \hat{n} = \perp_{Number} \\ \text{NaN} & \text{if } \hat{n} \in \{ \text{NaN}, -\text{Inf}, \text{NUIntSingle}(\hat{n}) \mid \hat{n} < \hat{0} \} \\ +\text{Inf} & \text{if } \hat{n} = +\text{Inf} \\ -\text{Inf} & \text{if } \hat{n} = \text{UIntSingle}(\hat{0}) \\ \alpha(\log(\hat{n})) & \text{if } \hat{n} \in \{ \text{UIntSingle}(\hat{n}), \text{NUIntSingle}(\hat{n}_1) \mid \hat{0} < \hat{n} \} \\ \top_{Number} & \text{otherwise} \end{cases} \\
& \wedge (\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{p}v)), \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Math.max"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{n}_{arglen} = \widehat{getArgValue}(args, \text{"length"}).1.4 \\
& \wedge \hat{n}_{arg_i} = \widehat{toNumber}(\widehat{toPrimitive}(\widehat{getArgValue}(args, \text{"i"}))) \\
& \wedge \hat{n}_1 = \begin{cases} \top_{number} & \text{if } \text{NUIntSingle} \sqsubseteq n_{arglen} \vee \hat{\text{inf}} \sqsubseteq n_{arglen} \vee \hat{\text{-inf}} \sqsubseteq n_{arglen} \\ & \vee \text{NaN} \sqsubseteq n_{arglen} \vee \text{UInt} \sqsubseteq n_{arglen} \\ \hat{n}_2 & \text{if } \hat{n}_{arglen} = \text{UIntSingle} \\ \perp_{number} & \text{if } \hat{n}_{arglen} = \perp_{number} \end{cases} \\
& \wedge \hat{n}_2 = \begin{cases} \hat{\text{-Inf}} & \text{if } n_{arglen} = \text{UIntSingle}(0) \\ \hat{n}_3 \sqcup \hat{N} & \text{if } n_{arglen} = \text{UIntSingle}(n) \wedge n > 0 \end{cases} \\
& \wedge \hat{n}_3 = \begin{cases} \text{NaN} & \text{if } n_{arglen} = \text{UIntSingle}(n) \wedge n > 0 \wedge \exists i \in \{1, \dots, n-1\} : \text{NaN} \sqsubseteq n_{arg_i} \\ \perp_{number} & \text{otherwise} \end{cases} \\
& \wedge \hat{N} = \left\{ n_{arg_i} \mid n_{arglen} = \text{UIntSingle}(n) \wedge i \in \{0, \dots, n-1\} \wedge \forall j \in \{0, \dots, n-1\} : n_{arg_i} \hat{\geq} n_{arg_j} \right\} \\
& \wedge (\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{n}_1)), \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Math.min"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{n}_{arglen} = \widehat{getArgValue}(args, \text{"length"}).1.4 \\
& \wedge \hat{n}_{arg_i} = \widehat{toNumber}(\widehat{toPrimitive}(\widehat{getArgValue}(args, \text{"i"}))) \\
& \wedge \hat{n}_1 = \begin{cases} \top_{number} & \text{if } \text{NUIntSingle} \sqsubseteq n_{arglen} \vee \hat{\text{inf}} \sqsubseteq n_{arglen} \vee \hat{\text{-inf}} \sqsubseteq n_{arglen} \\ & \vee \text{NaN} \sqsubseteq n_{arglen} \vee \text{UInt} \sqsubseteq n_{arglen} \\ \hat{n}_2 & \text{if } \hat{n}_{arglen} = \text{UIntSingle} \\ \perp_{number} & \text{if } \hat{n}_{arglen} = \perp_{number} \end{cases} \\
& \wedge \hat{n}_2 = \begin{cases} \hat{\text{Inf}} & \text{if } n_{arglen} = \text{UIntSingle}(0) \\ \hat{n}_3 \sqcup \hat{N} & \text{if } n_{arglen} = \text{UIntSingle}(n) \wedge n > 0 \end{cases} \\
& \wedge \hat{n}_3 = \begin{cases} \text{NaN} & \text{if } n_{arglen} = \text{UIntSingle}(n) \wedge n > 0 \wedge \exists i \in \{1, \dots, n-1\} : \text{NaN} \sqsubseteq n_{arg_i} \\ \perp_{number} & \text{otherwise} \end{cases} \\
& \wedge \hat{N} = \left\{ n_{arg_i} \mid n_{arglen} = \text{UIntSingle}(n) \wedge i \in \{0, \dots, n-1\} \wedge \forall j \in \{0, \dots, n-1\} : n_{arg_i} \hat{\leq} n_{arg_j} \right\} \\
& \wedge (\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \text{Value}(\hat{n}_1)), \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Math.pow"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } \hat{v}_x = \text{getArgValue}(args, \text{"0"}) \wedge \hat{n}_x = \widehat{\text{toNumber}(\text{toPrimitive}(\hat{v}_x))} \\
& \quad \wedge \hat{v}_y = \text{getArgValue}(args, \text{"1"}) \wedge \hat{n}_y = \widehat{\text{toNumber}(\text{toPrimitive}(\hat{v}_y))} \\
& \quad \wedge \hat{p}v_1 = \begin{cases} \perp_{Number} & \text{if } \hat{n}_y = \perp_{Number} \vee \hat{n}_x = \perp_{Number} \\ \text{UIntSingle}(\hat{1}) & \text{if } \hat{n}_y = \text{UIntSingle}(\hat{0}) \\ \text{NaN} & \text{if } \hat{n}_y = \text{NaN} \\ \text{NaN} & \text{if } \hat{n}_x = \text{NaN} \wedge \hat{n}_y \neq \text{UIntSingle}(\hat{0}) \\ \top_{Number} & \text{if } \hat{n}_x = \top_{Number} \vee \hat{n}_y = \top_{Number} \\ \text{NaN} & \text{if } \hat{n}_x \in \left\{ \text{NUIntSingle}(\hat{n}_1) \mid \hat{n}_1 < 0 \right\} \\ & \quad \wedge \hat{n}_y \in \left\{ \text{NUIntSingle}(\hat{n}_1) \mid \neg isInt(\hat{n}_1) \right\} \end{cases} \\
& \quad \wedge \hat{p}v_2 = \begin{cases} \text{UIntSingle}(\hat{0}) & \text{if } \hat{n}_x = \text{UIntSingle}(\hat{0}) \\ & \quad \wedge \hat{n}_y \in \left\{ +\hat{Inf}, \text{UIntSingle}(\hat{n}_1), \text{NUIntSingle}(\hat{n}_1) \mid \hat{0} < \hat{n}_1 \right\} \\ +\hat{Inf} & \text{if } \hat{n}_x = \text{UIntSingle}(\hat{0}) \\ & \quad \wedge \hat{n}_y \in \left\{ -\hat{Inf}, \text{NUIntSingle}(\hat{n}_1) \mid \hat{n}_1 < \hat{0} \right\} \\ +\hat{Inf} & \text{if } \hat{n}_x = +\hat{Inf} \\ & \quad \wedge \hat{n}_y \in \left\{ +\hat{Inf}, \text{UIntSingle}(\hat{n}_1), \text{NUIntSingle}(\hat{n}_1) \mid \hat{0} < \hat{n}_1 \right\} \\ \text{UIntSingle}(\hat{0}) & \text{if } \hat{n}_x = +\hat{Inf} \wedge \hat{n}_y \in \left\{ -\hat{Inf}, \text{NUIntSingle}(\hat{n}_1) \mid \hat{n}_1 < \hat{0} \right\} \\ -\hat{Inf} & \text{if } \hat{n}_x = -\hat{Inf} \\ & \quad \wedge \hat{n}_y \in \left\{ \text{UIntSingle}(\hat{n}_1), \text{NUIntSingle}(\hat{n}_1) \mid \hat{0} < \hat{n}_1 \wedge isOdd(\hat{n}_1) \right\} \\ +\hat{Inf} & \text{if } \hat{n}_x = -\hat{Inf} \\ & \quad \wedge \hat{n}_y \in \left\{ +\hat{Inf}, \text{UIntSingle}(\hat{n}_1), \text{NUIntSingle}(\hat{n}_1) \mid \hat{0} < \hat{n}_1 \wedge \neg isOdd(\hat{n}_1) \right\} \\ \text{UIntSingle}(\hat{0}) & \text{if } \hat{n}_x = -\hat{Inf} \wedge \hat{n}_y \in \left\{ -\hat{Inf}, \text{NUIntSingle}(\hat{n}_1) \mid \hat{n}_1 < \hat{0} \right\} \\ \text{UIntSingle}(\hat{0}) & \text{if } \hat{n}_x = \hat{Inf} \wedge \hat{n}_y \in \left\{ -\hat{Inf}, \text{NUIntSingle}(\hat{n}_1) \mid \hat{n}_1 < \hat{0} \right\} \\ +\hat{Inf} & \text{if } \hat{n}_x = \hat{Inf} \\ & \quad \wedge \hat{n}_y \in \left\{ +\hat{Inf}, \text{UIntSingle}(\hat{n}_1), \text{NUIntSingle}(\hat{n}_1) \mid \hat{0} < \hat{n}_1 \wedge \neg isOdd(\hat{n}_1) \right\} \\ +\hat{Inf} & \text{if } \hat{v}_{xa}.1.4 \in \left\{ \text{UIntSingle}(\hat{n}_1), \text{NUIntSingle}(\hat{n}_1) \mid \hat{n}_1 < -1 \vee 1 < \hat{n}_1 \right\} \\ & \quad \wedge \hat{n}_y = +\hat{Inf} \\ \text{UIntSingle}(\hat{0}) & \text{if } \hat{n}_x \in \left\{ \text{UIntSingle}(\hat{n}_1), \text{NUIntSingle}(\hat{n}_1) \mid -1 < \hat{n}_1 < 1 \right\} \\ & \quad \wedge \hat{n}_y = +\hat{Inf} \\ \text{UIntSingle}(\hat{0}) & \text{if } \hat{n}_x \in \left\{ \text{UIntSingle}(\hat{n}_1), \text{NUIntSingle}(\hat{n}_1) \mid \hat{n}_1 < -1 \vee 1 < \hat{n}_1 \right\} \\ & \quad \wedge \hat{n}_y = -\hat{Inf} \\ +\hat{Inf} & \text{if } \hat{n}_x \in \left\{ \text{UIntSingle}(\hat{n}_1), \text{NUIntSingle}(\hat{n}_1) \mid -1 < \hat{n}_1 < 1 \right\} \\ & \quad \wedge \hat{n}_y = -\hat{Inf} \\ \text{NaN} & \text{if } \hat{n}_x = \text{UIntSingle}(\hat{1}) \wedge \hat{n}_y \in \left\{ \hat{Inf}, +\hat{Inf}, -\hat{Inf} \right\} \\ \alpha(pow(\hat{n}_1, \hat{n}_2)) & \text{if } \hat{n}_x \in \left\{ \text{UIntSingle}(\hat{n}_1), \text{NUIntSingle}(\hat{n}_1) \right\} \\ & \quad \wedge \hat{n}_y \in \left\{ \text{UIntSingle}(\hat{n}_2), \text{NUIntSingle}(\hat{n}_2) \right\} \\ \top_{Number} & \text{otherwise} \end{cases} \\
& \quad \wedge \hat{p}v = \hat{p}v_1 \sqcup \hat{p}v_2 \sqcup \hat{p}v_3 \sqcup \hat{p}v_4 \sqcup \hat{p}v_5 \\
& \quad \wedge (\hat{H}_1, \hat{C}_1) = (\text{ReturnStore}(\hat{H}, \text{Value}(\hat{p}v)), \hat{C})
\end{aligned}$$



$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Math.random"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $\wedge (\hat{H}_1, \hat{C}_1) = (\text{ReturnStore}(\hat{H}, \text{Value}(\top_{Number})), \hat{C})$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Math.round"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $\hat{v} = \text{getArgValue}(args, \text{"0"}) \wedge \hat{n} = \text{toNumber}(\text{toPrimitive}(\hat{v}))$

$$\wedge \hat{p}v = \begin{cases} \hat{n} & \text{if } \hat{n} \in \{ \text{NaN}, \text{Inf}, +\text{Inf}, -\text{Inf}, \text{UInt}, \text{NUInt}, \perp_{Number} \} \\ \alpha(\text{round}(\hat{n})) & \text{if } \hat{n} \in \{ \text{UIntSingle}(\hat{n}_1), \text{NUIntSingle}(\hat{n}) \} \\ \top_{Number} & \text{otherwise} \end{cases}$$

$\wedge (\hat{H}_1, \hat{C}_1) = (\text{ReturnStore}(\hat{H}, \text{Value}(\hat{p}v)), \hat{C})$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Math.sin"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $\hat{v} = \text{getArgValue}(args, \text{"0"}) \wedge \hat{n} = \text{toNumber}(\text{toPrimitive}(\hat{v}))$

$$\wedge \hat{p}v = \begin{cases} \perp_{Number} & \text{if } \hat{n} = \perp_{Number} \\ \text{NaN} & \text{if } \hat{n} \in \{ \text{NaN}, +\text{Inf}, -\text{Inf}, \text{Inf} \} \\ \alpha(\sin(\hat{n})) & \text{if } \hat{n} \in \{ \text{UIntSingle}(\hat{n}), \text{NUIntSingle}(\hat{n}) \} \\ \top_{Number} & \text{otherwise} \end{cases}$$

$\wedge (\hat{H}_1, \hat{C}_1) = (\text{ReturnStore}(\hat{H}, \text{Value}(\hat{p}v)), \hat{C})$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Math.sqrt"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $\hat{v} = \text{getArgValue}(args, \text{"0"}) \wedge \hat{n} = \text{toNumber}(\text{toPrimitive}(\hat{v}))$

$$\wedge \hat{p}v = \begin{cases} \hat{n} & \text{if } \hat{n} \in \{ \perp_{Number}, \text{NaN}, +\text{Inf} \} \\ \text{NaN} & \text{if } \hat{n} \in \{ -\text{Inf}, \text{NUIntSingle}(\hat{n}) \mid \hat{n} < 0 \} \\ \alpha(\text{sqrt}(\hat{n})) & \text{if } \hat{n} \in \{ \text{UIntSingle}(\hat{n}), \text{NUIntSingle}(\hat{n}) \mid 0 \leq \hat{n} \} \\ \top_{Number} & \text{otherwise} \end{cases}$$

$\wedge (\hat{H}_1, \hat{C}_1) = (\text{ReturnStore}(\hat{H}, \text{Value}(\hat{p}v)), \hat{C})$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Math.tan"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $\hat{v} = \text{getArgValue}(args, \text{"0"}) \wedge \hat{n} = \text{toNumber}(\text{toPrimitive}(\hat{v}))$

$$\wedge \hat{p}v = \begin{cases} \hat{n} & \text{if } \hat{n} \in \{ \perp_{Number}, \text{NaN} \} \\ \text{NaN} & \text{if } \hat{n} \in \{ \text{Inf}, +\text{Inf}, -\text{Inf} \} \\ \alpha(\text{tan}(\hat{n})) & \text{if } \hat{n} \in \{ \text{UIntSingle}(\hat{n}), \text{NUIntSingle}(\hat{n}) \} \\ \top_{Number} & \text{otherwise} \end{cases}$$

$\wedge (\hat{H}_1, \hat{C}_1) = (\text{ReturnStore}(\hat{H}, \text{Value}(\hat{p}v)), \hat{C})$

### 11.2.15 Date

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $(\hat{H}_1, \hat{C}_1) = (\text{ReturnStore}(\hat{H}, \top_{String}), \hat{C})$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.constructor"}, args)_{\hat{a}_{new}} \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_3, \hat{C}_3), \hat{S}) \\
& \text{where } \hat{l}_R = (\hat{a}_{new}, \text{Recent}) \wedge (\hat{H}_1, \hat{C}_1) = \widehat{\text{Oldify}}(\hat{H}, \hat{C}, \hat{a}_{new}) \quad // \text{Recency Abstraction} \\
& \wedge \hat{n}_{arglen} = \widehat{\text{toUInt32}}(\widehat{\text{getArgValue}}(\hat{H}_1, \hat{C}_1, \text{"length"})) \\
& \wedge \hat{pv}_1 = \widehat{\text{toPrimitive}}(\widehat{\text{getArgValue}}(\hat{H}_1, \hat{C}_1, \text{"0"})) \\
& \wedge \hat{n}_{prim_1} = \begin{cases} \hat{n}_{prim_3} \sqcup \hat{n}_{prim_4} & \text{if } \text{UIntSingle}(1) \sqsubseteq \hat{n}_{arglen} \\ \perp_{Number} & \text{otherwise} \end{cases} \\
& \wedge \hat{n}_{prim_2} = \begin{cases} \top_{Number} & \text{if } \text{UIntSingle}(n) \sqsubseteq \hat{n}_{arglen} \wedge n \neq 1 \\ \perp_{Number} & \text{otherwise} \end{cases} \\
& \wedge \hat{n}_{prim_3} = \begin{cases} \top_{Number} & \text{if } \hat{pv}_1.5 \not\sqsubseteq \perp_{String} \quad // \text{parse} \\ \perp_{Number} & \text{otherwise} \end{cases} \\
& \wedge \hat{pv}_{nonstr} = PValue(\hat{v}_1.1, \hat{v}_1.2, \hat{v}_1.3, \hat{v}_1.4, \perp_{String}) \\
& \wedge \hat{n}_{prim_4} = \begin{cases} \widehat{\text{toNumber}}(\hat{v}_{nonstr}) & \text{if } \hat{pv}_{nonstr} \not\sqsubseteq \perp_{PValue} \\ \perp_{Number} & \text{otherwise} \end{cases} \\
& \wedge \hat{n}_{prim} = \hat{n}_{prim_1} \sqcup \hat{n}_{prim_2} \\
& \wedge \hat{H}_2 = \hat{H}_1[\hat{l}_R \mapsto \widehat{\text{NewDate}}(\hat{n}_{prim})] \\
& \wedge (\hat{H}_3, \hat{C}_3) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}_2, \text{Value}(\hat{l}_R)), \hat{C}_1) & \text{if } \hat{n}_{prim} \not\sqsubseteq \perp_{Number} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.parse"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } (\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \top_{Number}), \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.now"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S}) \\
& \text{where } (\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \top_{Number}), \hat{C})
\end{aligned}$$

### 11.2.16 Date.prototype

$$\hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $(\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \top_{String}), \hat{C})$

$$\hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $(\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \top_{String}), \hat{C})$

$$\hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $(\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \top_{String}), \hat{C})$

$$\hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $(\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \top_{String}), \hat{C})$

$$\hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $(\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \top_{String}), \hat{C})$

$$\hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $(\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}, \top_{String}), \hat{C})$

$$\hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $\hat{v} = \bigsqcup_{i \in \hat{C}.2} \hat{H}(\hat{i})(\text{@primitive})$   
 $(\hat{H}_1, \hat{C}_1) = (\hat{H}[\#Pur\hat{e}Local_R \mapsto \hat{H}(\#Pur\hat{e}Local_R)[\text{@return} \mapsto \hat{v}]], \hat{C})$

$$\hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $\hat{v} = \bigsqcup_{i \in \hat{C}.2} \hat{H}(\hat{i})(\text{@primitive})$   
 $(\hat{H}_1, \hat{C}_1) = (\hat{H}[\#Pur\hat{e}Local_R \mapsto \hat{H}(\#Pur\hat{e}Local_R)[\text{@return} \mapsto \hat{v}]], \hat{C})$

$$\hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $(\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}_1, Value(\top_{Number})), \hat{C})$

$$\hat{\mathcal{I}}_{cp} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $\hat{n}_{time} = \hat{H}(\hat{i})(\text{@primitive}).1.4$   
 $\hat{v} = \bigsqcup_{i \in \hat{C}.2} \begin{cases} \perp_{Value} & \text{if } \hat{n}_{time} \sqsubseteq \perp_{number} \\ \hat{v}_{get} & \text{if } \hat{n}_{time} = \text{UIntSingle}(n_{time}) \vee \hat{n}_{time} = \text{NUIntSingle}(n_{time}) \\ Value(\top_{Number}) & \text{otherwise} \end{cases}$   
 $\hat{v}_{get} = \alpha(\text{native.Calendar}(n_{time}).get(YEAR)) \quad // \text{java, scala}$   
 $(\hat{H}_1, \hat{C}_1) = (\hat{H}[\#Pur\hat{e}Local_R \mapsto \hat{H}(\#Pur\hat{e}Local_R)[\text{@return} \mapsto \hat{v}]], \hat{C})$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date.prototype.getMonth"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $(\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}_1, \text{Value}(\top_{\text{Number}})), \hat{C})$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date.prototype.getUTCMonth"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $\hat{n}_{time} = \hat{H}(\hat{l})(\text{@primitive}).1.4$

$$\hat{v} = \bigsqcup_{i \in \hat{C}.2} \begin{cases} \perp_{\text{Value}} & \text{if } \hat{n}_{time} \sqsubseteq \perp_{\text{number}} \\ \hat{v}_{get} & \text{if } \hat{n}_{time} = \text{UIntSingle}(n_{time}) \vee \hat{n}_{time} = \text{NUIntSingle}(n_{time}) \\ \text{Value}(\top_{\text{Number}}) & \text{otherwise} \end{cases}$$

$$\hat{v}_{get} = \alpha(\text{native.Calendar}(\hat{n}_{time}).\text{get}(\text{MONTH})) \quad // \text{java, scala}$$

$$(\hat{H}_1, \hat{C}_1) = (\hat{H}[\#Pur\hat{e}Local_R \mapsto \hat{H}(\#Pur\hat{e}Local_R)[\text{@return} \mapsto \hat{v}]], \hat{C})$$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date.prototype.getDate"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $(\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}_1, \text{Value}(\top_{\text{Number}})), \hat{C})$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date.prototype.getUTCDate"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $\hat{n}_{time} = \hat{H}(\hat{l})(\text{@primitive}).1.4$

$$\hat{v} = \bigsqcup_{i \in \hat{C}.2} \begin{cases} \perp_{\text{Value}} & \text{if } \hat{n}_{time} \sqsubseteq \perp_{\text{number}} \\ \hat{v}_{get} & \text{if } \hat{n}_{time} = \text{UIntSingle}(n_{time}) \vee \hat{n}_{time} = \text{NUIntSingle}(n_{time}) \\ \text{Value}(\top_{\text{Number}}) & \text{otherwise} \end{cases}$$

$$\hat{v}_{get} = \alpha(\text{native.Calendar}(\hat{n}_{time}).\text{get}(\text{DAY_OF_MONTH})) \quad // \text{java, scala}$$

$$(\hat{H}_1, \hat{C}_1) = (\hat{H}[\#Pur\hat{e}Local_R \mapsto \hat{H}(\#Pur\hat{e}Local_R)[\text{@return} \mapsto \hat{v}]], \hat{C})$$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date.prototype.getDay"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $(\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}_1, \text{Value}(\top_{\text{Number}})), \hat{C})$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date.prototype.getUTCDay"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $\hat{n}_{time} = \hat{H}(\hat{l})(\text{@primitive}).1.4$

$$\hat{v} = \bigsqcup_{i \in \hat{C}.2} \begin{cases} \perp_{\text{Value}} & \text{if } \hat{n}_{time} \sqsubseteq \perp_{\text{number}} \\ \hat{v}_{get} & \text{if } \hat{n}_{time} = \text{UIntSingle}(n_{time}) \vee \hat{n}_{time} = \text{NUIntSingle}(n_{time}) \\ \text{Value}(\top_{\text{Number}}) & \text{otherwise} \end{cases}$$

$$\hat{v}_{get} = \alpha(\text{native.Calendar}(\hat{n}_{time}).\text{get}(\text{DAY_OF_WEEK})) \quad // \text{java, scala}$$

$$(\hat{H}_1, \hat{C}_1) = (\hat{H}[\#Pur\hat{e}Local_R \mapsto \hat{H}(\#Pur\hat{e}Local_R)[\text{@return} \mapsto \hat{v}]], \hat{C})$$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Date.prototype.getHours"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $(\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}_1, \text{Value}(\top_{\text{Number}})), \hat{C})$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Date.prototype.getUTCHours"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $\hat{n}_{time} = \hat{H}(\hat{l})(@primitive).1.4$

$$\hat{v} = \bigsqcup_{\hat{l} \in \hat{C}.2} \begin{cases} \perp_{\text{Value}} & \text{if } \hat{n}_{time} \sqsubseteq \perp_{\text{number}} \\ \hat{v}_{get} & \text{if } \hat{n}_{time} = \text{UIntSingle}(n_{time}) \vee \hat{n}_{time} = \text{NUIntSingle}(n_{time}) \\ \text{Value}(\top_{\text{Number}}) & \text{otherwise} \end{cases}$$

$$\hat{v}_{get} = \alpha(\text{native.Calendar}(n_{time}).get(\text{HOURS})) \quad // \text{java, scala}$$

$$(\hat{H}_1, \hat{C}_1) = (\hat{H}[\#PureLocal_R \mapsto \hat{H}(\#PureLocal_R)[@return \mapsto \hat{v}]], \hat{C})$$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Date.prototype.getMinutes"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $(\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}_1, \text{Value}(\top_{\text{Number}})), \hat{C})$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Date.prototype.getUTCMinutes"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $\hat{n}_{time} = \hat{H}(\hat{l})(@primitive).1.4$

$$\hat{v} = \bigsqcup_{\hat{l} \in \hat{C}.2} \begin{cases} \perp_{\text{Value}} & \text{if } \hat{n}_{time} \sqsubseteq \perp_{\text{number}} \\ \hat{v}_{get} & \text{if } \hat{n}_{time} = \text{UIntSingle}(n_{time}) \vee \hat{n}_{time} = \text{NUIntSingle}(n_{time}) \\ \text{Value}(\top_{\text{Number}}) & \text{otherwise} \end{cases}$$

$$\hat{v}_{get} = \alpha(\text{native.Calendar}(n_{time}).get(\text{MINUTE})) \quad // \text{java, scala}$$

$$(\hat{H}_1, \hat{C}_1) = (\hat{H}[\#PureLocal_R \mapsto \hat{H}(\#PureLocal_R)[@return \mapsto \hat{v}]], \hat{C})$$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Date.prototype.getSeconds"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $(\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}_1, \text{Value}(\top_{\text{Number}})), \hat{C})$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltintCall}(\text{"Date.prototype.getUTCSeconds"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $\hat{n}_{time} = \hat{H}(\hat{l})(@primitive).1.4$

$$\hat{v} = \bigsqcup_{\hat{l} \in \hat{C}.2} \begin{cases} \perp_{\text{Value}} & \text{if } \hat{n}_{time} \sqsubseteq \perp_{\text{number}} \\ \hat{v}_{get} & \text{if } \hat{n}_{time} = \text{UIntSingle}(n_{time}) \vee \hat{n}_{time} = \text{NUIntSingle}(n_{time}) \\ \text{Value}(\top_{\text{Number}}) & \text{otherwise} \end{cases}$$

$$\hat{v}_{get} = \alpha(\text{native.Calendar}(n_{time}).get(\text{SECOND})) \quad // \text{java, scala}$$

$$(\hat{H}_1, \hat{C}_1) = (\hat{H}[\#PureLocal_R \mapsto \hat{H}(\#PureLocal_R)[@return \mapsto \hat{v}]], \hat{C})$$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date.prototype.getMilliseconds"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $(\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}_1, \text{Value}(\top_{\text{Number}})), \hat{C})$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date.prototype.getUTCMilliseconds"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $\hat{n}_{time} = \hat{H}(\hat{l})(\text{@primitive}).1.4$

$$\hat{v} = \bigsqcup_{\hat{l} \in \hat{C}.2} \begin{cases} \perp_{\text{Value}} & \text{if } \hat{n}_{time} \sqsubseteq \perp_{\text{number}} \\ \hat{v}_{get} & \text{if } \hat{n}_{time} = \text{UIntSingle}(n_{time}) \vee \hat{n}_{time} = \text{NUIntSingle}(n_{time}) \\ \text{Value}(\top_{\text{Number}}) & \text{otherwise} \end{cases}$$

$$\hat{v}_{get} = \alpha(\text{native.Calendar}(n_{time}).\text{get}(\text{MILLISECOND})) \quad // \text{java, scala}$$

$$(\hat{H}_1, \hat{C}_1) = (\hat{H}[\#PureLocal_R \mapsto \hat{H}(\#PureLocal_R)[\text{@return} \mapsto \hat{v}]], \hat{C})$$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date.prototype.getTimezoneOffset"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_1, \hat{C}_1), \hat{S})$$

where  $(\hat{H}_1, \hat{C}_1) = (\widehat{\text{ReturnStore}}(\hat{H}_1, \text{Value}(\top_{\text{Number}})), \hat{C})$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date.prototype.setTime"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S})$$

where  $\hat{n}_{time} = \widehat{\text{TimeClip}}(\widehat{\text{toNumber}}(\widehat{\text{toPrimitive}}(\text{getArgValue}(args, "0"))))$

$$\hat{H}_1 = \bigsqcup_{\hat{l} \in \hat{C}.2} \hat{H}[\hat{l} \mapsto \hat{H}(\hat{l})[\text{@primitive} \mapsto \hat{n}_{time}]]$$

$$(\hat{H}_2, \hat{C}_2) = (\hat{H}_1[\#PureLocal_R \mapsto \hat{H}_1(\#PureLocal_R)[\text{@return} \mapsto \hat{n}_{time}]], \hat{C})$$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date.prototype.setMilliseconds"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S})$$

where  $\hat{H}_1 = \bigsqcup_{\hat{l} \in \hat{C}.2} \hat{H}[\hat{l} \mapsto \hat{H}(\hat{l})[\text{@primitive} \mapsto \top_{\text{Number}}]]$

$$\wedge (\hat{H}_2, \hat{C}_2) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}_1, \top_{\text{Number}}), \hat{C}) & \text{if } \hat{H}_1 \not\sqsubseteq \perp_{\text{Heap}} \\ (\perp_{\text{heap}}, \perp_{\text{context}}) & \text{otherwise} \end{cases}$$

$$\hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date.prototype.setUTCMilliseconds"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S})$$

where  $\hat{n}_1 = \widehat{\text{toNumber}}(\widehat{\text{toPrimitive}}(\text{getArgValue}(args, "0")))$

$$\hat{n}_{time} = \begin{cases} \perp_{\text{Value}} & \text{if } \hat{n}_1 \sqsubseteq \perp_{\text{number}} \\ \widehat{\text{TimeClip}}(\hat{n}_{native}) & \text{if } \hat{n}_1 = \text{UIntSingle}(n_1) \vee \hat{n}_1 = \text{NUIntSingle}(n_1) \\ \top_{\text{Number}} & \text{otherwise} \end{cases}$$

$$\hat{n}_{native} = \alpha(\text{native.Calendar}(n_{time}).\text{set}(\text{MILLISECOND}, n_1).\text{getTimeInMills}()) \quad // \text{java, scala}$$

$$\hat{H}_1 = \bigsqcup_{\hat{l} \in \hat{C}.2} \hat{H}[\hat{l} \mapsto \hat{H}(\hat{l})[\text{@primitive} \mapsto \hat{n}_{time}]]$$

$$(\hat{H}_2, \hat{C}_2) = (\hat{H}_1[\#PureLocal_R \mapsto \hat{H}_1(\#PureLocal_R)[\text{@return} \mapsto \hat{n}_{time}]], \hat{C})$$

$$\begin{aligned} \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.setSeconds"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_2, \hat{C}_2), \hat{S}) \\ \text{where } \hat{H}_1 &= \bigsqcup_{i \in \hat{C}.2} \hat{H}[\hat{l} \mapsto \hat{H}(\hat{l})[\text{@primitive} \mapsto \top_{Number}]] \\ \wedge (\hat{H}_2, \hat{C}_2) &= \begin{cases} (\text{ReturnStore}(\hat{H}_1, \top_{Number}), \hat{C}) & \text{if } \hat{H}_1 \not\sqsubseteq \perp_{Heap} \\ (\perp_{Heap}, \perp_{Context}) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.setUTCSeconds"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_2, \hat{C}_2), \hat{S}) \\ \text{where } \hat{n}_1 &= \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, \text{"0"}))) \\ \hat{n}_{time} &= \begin{cases} \perp_{Value} & \text{if } \hat{n}_1 \sqsubseteq \perp_{number} \\ \text{TimeClip}(\hat{n}_{native}) & \text{if } \hat{n}_1 = \text{UIntSingle}(n_1) \vee \hat{n}_1 = \text{NUIntSingle}(n_1) \\ \top_{Number} & \text{otherwise} \end{cases} \\ \hat{n}_{native} &= \alpha(\text{native.Calendar}(\hat{n}_{time}).\text{set}(\text{SECOND}, n_1).\text{getTimeInMills()}) \quad // \text{java, scala} \\ \hat{H}_1 &= \bigsqcup_{i \in \hat{C}.2} \hat{H}[\hat{l} \mapsto \hat{H}(\hat{l})[\text{@primitive} \mapsto \hat{n}_{time}]] \\ (\hat{H}_2, \hat{C}_2) &= (\hat{H}_1[\#PureLocal_R \mapsto \hat{H}_1(\#PureLocal_R)[\text{@return} \mapsto \hat{n}_{time}]], \hat{C}) \end{aligned}$$

$$\begin{aligned} \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.setMinutes"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_2, \hat{C}_2), \hat{S}) \\ \text{where } \hat{H}_1 &= \bigsqcup_{i \in \hat{C}.2} \hat{H}[\hat{l} \mapsto \hat{H}(\hat{l})[\text{@primitive} \mapsto \top_{Number}]] \\ \wedge (\hat{H}_2, \hat{C}_2) &= \begin{cases} (\text{ReturnStore}(\hat{H}_1, \top_{Number}), \hat{C}) & \text{if } \hat{H}_1 \not\sqsubseteq \perp_{Heap} \\ (\perp_{Heap}, \perp_{Context}) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.setUTCMinutes"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_2, \hat{C}_2), \hat{S}) \\ \text{where } \hat{n}_1 &= \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, \text{"0"}))) \\ \hat{n}_{time} &= \begin{cases} \perp_{Value} & \text{if } \hat{n}_1 \sqsubseteq \perp_{number} \\ \text{TimeClip}(\hat{n}_{native}) & \text{if } \hat{n}_1 = \text{UIntSingle}(n_1) \vee \hat{n}_1 = \text{NUIntSingle}(n_1) \\ \top_{Number} & \text{otherwise} \end{cases} \\ \hat{n}_{native} &= \alpha(\text{native.Calendar}(\hat{n}_{time}).\text{set}(\text{MINUTE}, n_1).\text{getTimeInMills()}) \quad // \text{java, scala} \\ \hat{H}_1 &= \bigsqcup_{i \in \hat{C}.2} \hat{H}[\hat{l} \mapsto \hat{H}(\hat{l})[\text{@primitive} \mapsto \hat{n}_{time}]] \\ (\hat{H}_2, \hat{C}_2) &= (\hat{H}_1[\#PureLocal_R \mapsto \hat{H}_1(\#PureLocal_R)[\text{@return} \mapsto \hat{n}_{time}]], \hat{C}) \end{aligned}$$

$$\begin{aligned} \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.setHours"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_2, \hat{C}_2), \hat{S}) \\ \text{where } \hat{H}_1 &= \bigsqcup_{i \in \hat{C}.2} \hat{H}[\hat{l} \mapsto \hat{H}(\hat{l})[\text{@primitive} \mapsto \top_{Number}]] \\ \wedge (\hat{H}_2, \hat{C}_2) &= \begin{cases} (\text{ReturnStore}(\hat{H}_1, \top_{Number}), \hat{C}) & \text{if } \hat{H}_1 \not\sqsubseteq \perp_{Heap} \\ (\perp_{Heap}, \perp_{Context}) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date.prototype.setUTCHours"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S}) \\
& \text{where } \hat{n}_1 = \widehat{\text{toNumber}}(\widehat{\text{toPrimitive}}(\text{getArgValue}(args, \text{"0"}))) \\
& \hat{n}_{time} = \begin{cases} \perp_{Value} & \text{if } \hat{n}_1 \sqsubseteq \perp_{number} \\ \widehat{\text{TimeClip}}(\hat{n}_{native}) & \text{if } \hat{n}_1 = \text{UIntSingle}(n_1) \vee \hat{n}_1 = \text{NUIntSingle}(n_1) \\ \top_{Number} & \text{otherwise} \end{cases} \\
& \hat{n}_{native} = \alpha(\text{native.Calendar}(\hat{n}_{time}).\text{set}(\text{HOURS}, n_1).\text{getTimeInMills}()) \quad // \text{java, scala} \\
& \hat{H}_1 = \bigsqcup_{i \in \hat{C}.2} \hat{H}[i \mapsto \hat{H}(i)[@primitive \mapsto \top_{Number}]] \\
& (\hat{H}_2, \hat{C}_2) = (\hat{H}_1[\#PureLocal_R \mapsto \hat{H}_1(\#PureLocal_R)[@return \mapsto \hat{n}_{time}]], \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date.prototype.setDate"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S}) \\
& \text{where } \hat{H}_1 = \bigsqcup_{i \in \hat{C}.2} \hat{H}[i \mapsto \hat{H}(i)[@primitive \mapsto \top_{Number}]] \\
& \wedge (\hat{H}_2, \hat{C}_2) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}_1, \top_{Number}), \hat{C}) & \text{if } \hat{H}_1 \not\sqsubseteq \perp_{Heap} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date.prototype.setUTCDate"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S}) \\
& \text{where } \hat{n}_1 = \widehat{\text{toNumber}}(\widehat{\text{toPrimitive}}(\text{getArgValue}(args, \text{"0"}))) \\
& \hat{n}_{time} = \begin{cases} \perp_{Value} & \text{if } \hat{n}_1 \sqsubseteq \perp_{number} \\ \widehat{\text{TimeClip}}(\hat{n}_{native}) & \text{if } \hat{n}_1 = \text{UIntSingle}(n_1) \vee \hat{n}_1 = \text{NUIntSingle}(n_1) \\ \top_{Number} & \text{otherwise} \end{cases} \\
& \hat{n}_{native} = \alpha(\text{native.Calendar}(\hat{n}_{time}).\text{set}(\text{DAY_OF_MONTH}, n_1).\text{getTimeInMills}()) \quad // \text{java, scala} \\
& \hat{H}_1 = \bigsqcup_{i \in \hat{C}.2} \hat{H}[i \mapsto \hat{H}(i)[@primitive \mapsto \hat{n}_{time}]] \\
& (\hat{H}_2, \hat{C}_2) = (\hat{H}_1[\#PureLocal_R \mapsto \hat{H}_1(\#PureLocal_R)[@return \mapsto \hat{n}_{time}]], \hat{C})
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date.prototype.setMonth"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S}) \\
& \text{where } \hat{H}_1 = \bigsqcup_{i \in \hat{C}.2} \hat{H}[i \mapsto \hat{H}(i)[@primitive \mapsto \top_{Number}]] \\
& \wedge (\hat{H}_2, \hat{C}_2) = \begin{cases} (\widehat{\text{ReturnStore}}(\hat{H}_1, \top_{Number}), \hat{C}) & \text{if } \hat{H}_1 \not\sqsubseteq \perp_{Heap} \\ (\perp_{heap}, \perp_{context}) & \text{otherwise} \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp}[\text{BuiltinCall}(\text{"Date.prototype.setUTCMonth"}, args)]((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_2, \hat{C}_2), \hat{S}) \\
& \text{where } \hat{n}_1 = \widehat{\text{toNumber}}(\widehat{\text{toPrimitive}}(\text{getArgValue}(args, \text{"0"}))) \\
& \hat{n}_{time} = \begin{cases} \perp_{Value} & \text{if } \hat{n}_1 \sqsubseteq \perp_{number} \\ \widehat{\text{TimeClip}}(\hat{n}_{native}) & \text{if } \hat{n}_1 = \text{UIntSingle}(n_1) \vee \hat{n}_1 = \text{NUIntSingle}(n_1) \\ \top_{Number} & \text{otherwise} \end{cases} \\
& \hat{n}_{native} = \alpha(\text{native.Calendar}(\hat{n}_{time}).\text{set}(\text{MONTH}, n_1).\text{getTimeInMills}()) \quad // \text{java, scala} \\
& \hat{H}_1 = \bigsqcup_{i \in \hat{C}.2} \hat{H}[i \mapsto \hat{H}(i)[@primitive \mapsto \hat{n}_{time}]] \\
& (\hat{H}_2, \hat{C}_2) = (\hat{H}_1[\#PureLocal_R \mapsto \hat{H}_1(\#PureLocal_R)[@return \mapsto \hat{n}_{time}]], \hat{C})
\end{aligned}$$



$$\begin{aligned} \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.setFullYear"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_2, \hat{C}_2), \hat{S}) \\ \text{where } \hat{H}_1 &= \bigsqcup_{i \in \hat{C}.2} \hat{H}[\hat{l} \mapsto \hat{H}(\hat{l})[\text{@primitive} \mapsto \top_{Number}]] \\ \wedge (\hat{H}_2, \hat{C}_2) &= \begin{cases} (\text{ReturnStore}(\hat{H}_1, \top_{Number}), \hat{C}) & \text{if } \hat{H}_1 \not\sqsubseteq \perp_{Heap} \\ (\perp_{Heap}, \perp_{context}) & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.setUTCFullYear"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_2, \hat{C}_2), \hat{S}) \\ \text{where } \hat{n}_1 &= \text{toNumber}(\text{toPrimitive}(\text{getArgValue}(args, \text{"0"}))) \\ \hat{n}_{time} &= \begin{cases} \perp_{Value} & \text{if } \hat{n}_1 \sqsubseteq \perp_{number} \\ \text{TimeClip}(\hat{n}_{native}) & \text{if } \hat{n}_1 = \text{UIntSingle}(n_1) \vee \hat{n}_1 = \text{NUIntSingle}(n_1) \\ \top_{Number} & \text{otherwise} \end{cases} \\ \hat{n}_{native} &= \alpha(\text{native.Calendar}(\hat{n}_{time}).\text{set}(\text{YEAR}, n_1).\text{getTimeInMills}()) \quad // \text{java, scala} \\ \hat{H}_1 &= \bigsqcup_{i \in \hat{C}.2} \hat{H}[\hat{l} \mapsto \hat{H}(\hat{l})[\text{@primitive} \mapsto \hat{n}_{time}]] \\ (\hat{H}_2, \hat{C}_2) &= (\hat{H}_1[\#PureLocal_R \mapsto \hat{H}_1(\#PureLocal_R)[\text{@return} \mapsto \hat{n}_{time}]], \hat{C}) \end{aligned}$$

$$\begin{aligned} \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.toUTCString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_1, \hat{C}_1), \hat{S}) \\ \text{where } (\hat{H}_1, \hat{C}_1) &= (\text{ReturnStore}(\hat{H}, \top_{String}), \hat{C}) \end{aligned}$$

$$\begin{aligned} \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Date.prototype.toISOString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_1, \hat{C}_1), \hat{S}) \\ \text{where } (\hat{H}_1, \hat{C}_1) &= (\text{ReturnStore}(\hat{H}, \top_{String}), \hat{C}) \end{aligned}$$

### 11.2.17 Error

$$\begin{aligned} \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Error.constructor"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_4, \hat{C}_4), \hat{S}) \\ \text{where } \hat{v}_{arg} &= \text{getArgValue}(args, \text{"0"}) \wedge \hat{s} = \text{toString}(\text{toPrimitive}(\hat{v}_{arg})) \wedge \hat{l}_e = \#Err_O \\ \wedge \hat{H}_1 &= \begin{cases} \hat{H}[\hat{l}_e \mapsto \hat{H}(\hat{l}_e)[\text{message} \mapsto \hat{s}]] & \text{if } \hat{v}_{arg}.1.1 \sqsubseteq \perp_{undef} \\ \perp_{Heap} & \text{otherwise} \end{cases} \quad \wedge \hat{H}_2 = \begin{cases} \hat{H} & \text{if } \hat{v}_{arg}.1.1 \not\sqsubseteq \perp_{undef} \\ \perp_{Heap} & \text{otherwise} \end{cases} \\ \wedge \hat{H}_3 &= \hat{H}_1 \sqcup \hat{H}_2 \wedge (\hat{H}_4, \hat{C}_4) = (\text{ReturnStore}(\hat{H}_3, \text{Value}(\hat{l}_e)), \hat{C}) \end{aligned}$$

### 11.2.18 Error.prototype

$$\begin{aligned} \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"Error.prototype.toString"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) &= ((\hat{H}_1, \hat{C}_1), \hat{S}) \\ \text{where } \hat{L}_{this} &= \hat{C}.2 \wedge \hat{v}_{name} = \bigsqcup_{l \in L_{this}} \widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"name"}) \wedge \hat{v}_{msg} = \bigsqcup_{l \in L_{this}} \widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"message"}) \\ \wedge \hat{s}_1 &= \begin{cases} \text{"Error"} & \text{if } \hat{v}_{name}.1.1 \not\sqsubseteq \perp_{undef} \\ \perp_{string} & \text{otherwise} \end{cases} \\ \wedge \hat{s}_2 &= \text{toString}(\text{PValue}(\perp_{undef}, \hat{v}_{name}.1.2, \hat{v}_{name}.1.3, \hat{v}_{name}.1.4, \hat{v}_{name}.1.5)) \\ \wedge \hat{s}_{name} &= \hat{s}_1 \sqcup \hat{s}_2 \\ \wedge \hat{s}_3 &= \begin{cases} \hat{s}_1 & \text{if } \hat{v}_{msg}.1.1 \not\sqsubseteq \perp_{undef} \\ \perp_{string} & \text{otherwise} \end{cases} \\ \wedge \hat{s}_4 &= \text{toString}(\text{PValue}(\perp_{undef}, \hat{v}_{msg}.1.2, \hat{v}_{msg}.1.3, \hat{v}_{msg}.1.4, \hat{v}_{msg}.1.5)) \\ \wedge \hat{s}_{msg} &= \hat{s}_3 \sqcup \hat{s}_4 \\ \wedge \hat{s}_5 &= \begin{cases} \hat{s}_{msg} & \text{if } \hat{s}_1 \sqsubseteq \hat{s}_{name} \\ \perp_{string} & \text{otherwise} \end{cases} \quad \wedge \hat{s}_6 = \begin{cases} \hat{s}_{name} & \text{if } \hat{s}_1 \sqsubseteq \hat{s}_{msg} \\ \perp_{string} & \text{otherwise} \end{cases} \quad \wedge \hat{s}_7 = \hat{s}_{name} + \text{" : " } + \hat{s}_{msg} \\ \wedge \hat{s}_{ret} &= \hat{s}_5 \sqcup \hat{s}_6 \sqcup \hat{s}_7 \\ \wedge (\hat{H}_1, \hat{C}_1) &= \begin{cases} (\text{ReturnStore}(\hat{H}, \text{Value}(\hat{s}_{ret})), \hat{C}) & \text{if } \hat{s}_{ret} \not\sqsubseteq \perp_{String} \\ (\perp_{Heap}, \perp_{context}) & \text{otherwise} \end{cases} \end{aligned}$$

### 11.2.19 EvalError

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"EvalError.constructor"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_4, \hat{C}_4), \hat{S}) \\
& \text{where } \hat{v}_{arg} = \text{getArgValue}(args, \text{"0"}) \wedge \hat{s} = \widehat{\text{toString}(\text{toPrimitive}(\hat{v}_{arg}))} \wedge \hat{l}_e = \#EvalErr_O \\
& \wedge \hat{H}_1 = \begin{cases} \hat{H}[\hat{l}_e \mapsto \hat{H}(\hat{l}_e)[\text{message} \mapsto \hat{s}]] & \text{if } \hat{v}_{arg}.1.1 \sqsubseteq \perp_{undef} \\ \perp_{Heap} & \text{otherwise} \end{cases} \quad \wedge \hat{H}_2 = \begin{cases} \hat{H} & \text{if } \hat{v}_{arg}.1.1 \not\sqsubseteq \perp_{undef} \\ \perp_{Heap} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_3 = \hat{H}_1 \sqcup \hat{H}_2 \wedge (\hat{H}_4, \hat{C}_4) = (\widehat{\text{ReturnStore}}(\hat{H}_3, \text{Value}(\hat{l}_e)), \hat{C})
\end{aligned}$$

### 11.2.20 RangeError

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"RangeError.constructor"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_4, \hat{C}_4), \hat{S}) \\
& \text{where } \hat{v}_{arg} = \text{getArgValue}(args, \text{"0"}) \wedge \hat{s} = \widehat{\text{toString}(\text{toPrimitive}(\hat{v}_{arg}))} \wedge \hat{l}_e = \#RangeErr_O \\
& \wedge \hat{H}_1 = \begin{cases} \hat{H}[\hat{l}_e \mapsto \hat{H}(\hat{l}_e)[\text{message} \mapsto \hat{s}]] & \text{if } \hat{v}_{arg}.1.1 \sqsubseteq \perp_{undef} \\ \perp_{Heap} & \text{otherwise} \end{cases} \quad \wedge \hat{H}_2 = \begin{cases} \hat{H} & \text{if } \hat{v}_{arg}.1.1 \not\sqsubseteq \perp_{undef} \\ \perp_{Heap} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_3 = \hat{H}_1 \sqcup \hat{H}_2 \wedge (\hat{H}_4, \hat{C}_4) = (\widehat{\text{ReturnStore}}(\hat{H}_3, \text{Value}(\hat{l}_e)), \hat{C})
\end{aligned}$$

### 11.2.21 ReferenceError

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"ReferenceError.constructor"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_4, \hat{C}_4), \hat{S}) \\
& \text{where } \hat{v}_{arg} = \text{getArgValue}(args, \text{"0"}) \wedge \hat{s} = \widehat{\text{toString}(\text{toPrimitive}(\hat{v}_{arg}))} \wedge \hat{l}_e = \#RefErr_O \\
& \wedge \hat{H}_1 = \begin{cases} \hat{H}[\hat{l}_e \mapsto \hat{H}(\hat{l}_e)[\text{message} \mapsto \hat{s}]] & \text{if } \hat{v}_{arg}.1.1 \sqsubseteq \perp_{undef} \\ \perp_{Heap} & \text{otherwise} \end{cases} \quad \wedge \hat{H}_2 = \begin{cases} \hat{H} & \text{if } \hat{v}_{arg}.1.1 \not\sqsubseteq \perp_{undef} \\ \perp_{Heap} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_3 = \hat{H}_1 \sqcup \hat{H}_2 \wedge (\hat{H}_4, \hat{C}_4) = (\widehat{\text{ReturnStore}}(\hat{H}_3, \text{Value}(\hat{l}_e)), \hat{C})
\end{aligned}$$

### 11.2.22 SyntaxError

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"SyntaxError.constructor"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_4, \hat{C}_4), \hat{S}) \\
& \text{where } \hat{v}_{arg} = \text{getArgValue}(args, \text{"0"}) \wedge \hat{s} = \widehat{\text{toString}(\text{toPrimitive}(\hat{v}_{arg}))} \wedge \hat{l}_e = \#SyntaxErr_O \\
& \wedge \hat{H}_1 = \begin{cases} \hat{H}[\hat{l}_e \mapsto \hat{H}(\hat{l}_e)[\text{message} \mapsto \hat{s}]] & \text{if } \hat{v}_{arg}.1.1 \sqsubseteq \perp_{undef} \\ \perp_{Heap} & \text{otherwise} \end{cases} \quad \wedge \hat{H}_2 = \begin{cases} \hat{H} & \text{if } \hat{v}_{arg}.1.1 \not\sqsubseteq \perp_{undef} \\ \perp_{Heap} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_3 = \hat{H}_1 \sqcup \hat{H}_2 \wedge (\hat{H}_4, \hat{C}_4) = (\widehat{\text{ReturnStore}}(\hat{H}_3, \text{Value}(\hat{l}_e)), \hat{C})
\end{aligned}$$

### 11.2.23 TypeError

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"TypeError.constructor"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_4, \hat{C}_4), \hat{S}) \\
& \text{where } \hat{v}_{arg} = \text{getArgValue}(args, \text{"0"}) \wedge \hat{s} = \widehat{\text{toString}(\text{toPrimitive}(\hat{v}_{arg}))} \wedge \hat{l}_e = \#TypeErr_O \\
& \wedge \hat{H}_1 = \begin{cases} \hat{H}[\hat{l}_e \mapsto \hat{H}(\hat{l}_e)[\text{message} \mapsto \hat{s}]] & \text{if } \hat{v}_{arg}.1.1 \sqsubseteq \perp_{undef} \\ \perp_{Heap} & \text{otherwise} \end{cases} \quad \wedge \hat{H}_2 = \begin{cases} \hat{H} & \text{if } \hat{v}_{arg}.1.1 \not\sqsubseteq \perp_{undef} \\ \perp_{Heap} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_3 = \hat{H}_1 \sqcup \hat{H}_2 \wedge (\hat{H}_4, \hat{C}_4) = (\widehat{\text{ReturnStore}}(\hat{H}_3, \text{Value}(\hat{l}_e)), \hat{C})
\end{aligned}$$

### 11.2.24 URIError

$$\begin{aligned}
& \hat{\mathcal{I}}_{cp} \llbracket \text{BuiltinCall}(\text{"URIError.constructor"}, args) \rrbracket ((\hat{H}, \hat{C}), \hat{S}) = ((\hat{H}_4, \hat{C}_4), \hat{S}) \\
& \text{where } \hat{v}_{arg} = \text{getArgValue}(args, \text{"0"}) \wedge \hat{s} = \widehat{\text{toString}(\text{toPrimitive}(\hat{v}_{arg}))} \wedge \hat{l}_e = \#URIErr_O \\
& \wedge \hat{H}_1 = \begin{cases} \hat{H}[\hat{l}_e \mapsto \hat{H}(\hat{l}_e)[\text{message} \mapsto \hat{s}]] & \text{if } \hat{v}_{arg}.1.1 \sqsubseteq \perp_{undef} \\ \perp_{Heap} & \text{otherwise} \end{cases} \quad \wedge \hat{H}_2 = \begin{cases} \hat{H} & \text{if } \hat{v}_{arg}.1.1 \not\sqsubseteq \perp_{undef} \\ \perp_{Heap} & \text{otherwise} \end{cases} \\
& \wedge \hat{H}_3 = \hat{H}_1 \sqcup \hat{H}_2 \wedge (\hat{H}_4, \hat{C}_4) = (\widehat{\text{ReturnStore}}(\hat{H}_3, \text{Value}(\hat{l}_e)), \hat{C})
\end{aligned}$$

## 11.3 Access Analysis

### 11.3.1 Global

$$\begin{aligned}
& \hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Global.parseInt"}, args)](\hat{H}, \hat{C}) = LP_1 \\
& \text{where } LP_1 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Global.encodeURIComponent"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } \hat{es} = \{\text{URIError}\} \\
& \quad LP_1 = \widehat{\text{RaiseException}}_{def}(\hat{es}) \\
& \quad LP_2 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"URIError.isNaN"}, args)](\hat{H}, \hat{C}) = LP_1 \\
& \text{where } LP_1 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"URIError.isFinite"}, args)](\hat{H}, \hat{C}) = LP_1 \\
& \text{where } LP_1 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Global.parseInt"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \\
& \text{where } LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, "0") \\
& \quad LP_2 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, "1") \\
& \quad LP_3 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, "length") \\
\\
& \hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Global.encodeURIComponent"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } \hat{es} = \{\text{URIError}\} \\
& \quad LP_1 = \widehat{\text{RaiseException}}_{def}(\hat{es}) \\
& \quad LP_2 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"URIError.isNaN"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, "0") \\
& \quad LP_2 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"URIError.isFinite"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, "0") \\
& \quad LP_2 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

### 11.3.2 Object

$$\begin{aligned}
& \hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Object"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\
& \text{where } \hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, "0") \\
& \quad (LP_1, \hat{es}) = \begin{cases} (\widehat{\text{toObject}}_{def}(\hat{H}, \hat{C}, \hat{v}_{new}, \hat{a}_1), \hat{es}'_1) & \text{if } \hat{v}.1.3 \not\sqsubseteq \perp_{Bool} \vee \hat{v}.1.3 \not\sqsubseteq \perp_{Number} \vee \hat{v}.1.3 \not\sqsubseteq \perp_{String} \\ (\{\}, \{\}) & \text{otherwise} \end{cases} \\
& \quad \hat{v}_{new} = \text{Value}(PValue(\perp_{Undef}, \perp_{Null}, \hat{v}.1.3, \hat{v}.1.4, \hat{v}.1.5), \hat{v}.2) \\
& \quad \hat{es}' = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \vee \hat{v}.1.2 \not\sqsubseteq \perp_{Null} \\ \{\} & \text{otherwise} \end{cases} \\
& \quad LP_2 = \begin{cases} LP'_2 \cup \bigcup_{s \in \widehat{\text{NewObject}}_{def}} \{ \langle \hat{l}_R, s \rangle \} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \vee \hat{v}.1.2 \not\sqsubseteq \perp_{Null} \\ \{\} & \text{otherwise} \end{cases} \\
& \quad LP'_2 = \widehat{\text{Oldify}}_{def}((\hat{H}, \hat{C}, \hat{v}_{new}, \hat{a}_1) \\
& \quad \hat{l}_R = (\hat{a}_1, \text{Recent}) \\
& \quad LP_3 = \widehat{\text{RaiseException}}_{def}(\hat{es}) \\
& \quad LP_4 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{def}[\text{BuiltintCall}(\text{"Object.constructor"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\
& \text{where } \hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& (LP_1, \hat{e}s) = \begin{cases} (\bigcup_{\hat{l} \in \hat{C}.2} \bigcup_{s \in \hat{P}_1 \cup \hat{P}_2 \cup \hat{P}_3} \{ \langle \hat{l}, s \rangle \}, \hat{e}s') & \text{if } \hat{v}.1.3 \not\sqsubseteq \perp_{Bool} \vee \hat{v}.1.3 \not\sqsubseteq \perp_{Number} \vee \hat{v}.1.3 \not\sqsubseteq \perp_{String} \\ (\{\}, \{\}) & \text{otherwise} \end{cases} \\
& \hat{v}_{new} = \text{Value}(\text{PValue}(\perp_{Undef}, \perp_{Null}, \hat{v}.1.3, \hat{v}.1.4, \hat{v}.1.5), \hat{v}.2) \\
& \hat{P}_1 = \begin{cases} \widehat{\text{NewBool}}_{def} & \text{if } \hat{v}_{new}.1.3 \not\sqsubseteq \perp_{Bool} \\ \{\} & \text{otherwise} \end{cases} \\
& \hat{P}_2 = \begin{cases} \widehat{\text{NewNumber}}_{def} & \text{if } \hat{v}_{new}.1.4 \not\sqsubseteq \perp_{Number} \\ \{\} & \text{otherwise} \end{cases} \\
& \hat{P}_3 = \begin{cases} \widehat{\text{NewString}}_{def}(\hat{v}_{new}.1.5) & \text{if } \hat{v}_{new}.1.5 \not\sqsubseteq \perp_{String} \\ \{\} & \text{otherwise} \end{cases} \\
& \hat{e}s' = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \vee \hat{v}.1.2 \not\sqsubseteq \perp_{Null} \\ \{\} & \text{otherwise} \end{cases} \\
& LP_2 = \begin{cases} \bigcup_{\hat{l} \in \hat{C}.2} \bigcup_{s \in \widehat{\text{NewObject}}_{def}} \{ \langle \hat{l}, s \rangle \} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \vee \hat{v}.1.2 \not\sqsubseteq \perp_{Null} \\ \{\} & \text{otherwise} \end{cases} \\
& \hat{l}_R = (\hat{a}_1, \text{Recent}) \\
& LP_3 = \widehat{\text{RaiseException}}_{def}(\hat{e}s) \\
& LP_4 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{def}[\text{BuiltintCall}(\text{"Object.getPrototypeOf"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } \hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& \hat{e}s = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& LP_1 = \widehat{\text{RaiseException}}_{def}(\hat{e}s) \\
& LP_2 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{def}[\text{BuiltintCall}(\text{"Object.getOwnPropertyDescriptor"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\
& \text{where } \hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& \hat{e}s = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& \hat{l}_R = (\hat{a}_1, \text{Recent}) \\
& LP_1 = \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_1) \\
& LP_2 = \{ \langle \hat{l}_R, \text{"value"} \rangle, \langle \hat{l}_R, \text{"writable"} \rangle, \langle \hat{l}_R, \text{"enumerable"} \rangle, \langle \hat{l}_R, \text{"configurable"} \rangle \} \\
& LP_3 = \widehat{\text{RaiseException}}_{def}(\hat{e}s) \\
& LP_4 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{def}[\text{BuiltintCall}(\text{"Object.getOwnPropertyNames"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\
& \text{where } \hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& \hat{e}s = \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
& \hat{l}_R = (\hat{a}_1, \text{Recent}) \\
& LP_1 = \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_1) \\
& LP_2 = \bigcup_{\hat{l} \in \hat{v}.2} \bigcup_{i \in \{0, \dots, |\widehat{\text{GetProps}}(\hat{H}, \hat{l})| - 1\}} \{ \langle \hat{l}, i \rangle \} \\
& LP_3 = \widehat{\text{RaiseException}}_{def}(\hat{e}s) \\
& LP_4 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Object.create"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5$$

where  $\hat{l}_R = (\hat{a}_1, \text{Recent})$

$$\begin{aligned} LP_1 &= \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_1) \\ \hat{v}_1 &= \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\ \hat{e}s_1 &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ \hat{n}_{len} &= \text{toUInt32}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"length"})) \\ \hat{v}_2 &= \text{getArgValue}(\hat{H}, \hat{C}, \text{"1"}) \\ \hat{e}s_2 &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{n}_{len} = \hat{2} \wedge \hat{v}_2.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ LP_2 &= \bigcup_{s \in \widehat{\text{NewObject}}_{def}} \{ \langle \hat{l}_R, s \rangle \} \\ LP_3 &= \begin{cases} \bigcup_{i \in \hat{v}_2.2} \widehat{\text{DefineProperties}}_{def}(\hat{H}, \hat{l}_R, \hat{l}_i) & \text{if } \hat{n}_{len} = \hat{2} \\ \{\} & \text{otherwise} \end{cases} \\ LP_4 &= \widehat{\text{RaiseException}}_{def}(\hat{e}s_1 \sqcup \hat{e}s_2) \\ LP_5 &= \{ \langle \#PureLocal_R, @return \rangle \} \end{aligned}$$

$$\hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Object.defineProperty"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

where  $\hat{v}_1 = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"})$

$$\begin{aligned} \hat{e}s_1 &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ \hat{s}_{name} &= \text{toString}(\text{toPrimitive}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"1"}))) \\ \hat{v}_2 &= \text{getArgValue}(\hat{H}, \hat{C}, \text{"2"}) \\ \hat{e}s_2 &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{n}_{len} = \hat{2} \wedge \hat{v}_2.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ LP_1 &= \bigcup_{i_1 \in \hat{v}_1.2} \bigcup_{i_2 \in \hat{v}_2.2} \widehat{\text{DefineProperty}}_{def}(\hat{H}, \hat{l}_1, \hat{s}_{name}, \hat{l}_2) \\ LP_2 &= \widehat{\text{RaiseException}}_{def}(\hat{e}s_1 \sqcup \hat{e}s_2) \\ LP_3 &= \{ \langle \#PureLocal_R, @return \rangle \} \end{aligned}$$

$$\hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Object.defineProperties"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

where  $\hat{v}_1 = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"})$

$$\begin{aligned} \hat{e}s_1 &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ \hat{v}_2 &= \text{getArgValue}(\hat{H}, \hat{C}, \text{"1"}) \\ \hat{e}s_2 &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{n}_{len} = \hat{2} \wedge \hat{v}_2.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ LP_1 &= \bigcup_{i_1 \in \hat{v}_1.2} \bigcup_{i_2 \in \hat{v}_2.2} \widehat{\text{DefineProperties}}_{def}(\hat{H}, \hat{l}_1, \hat{l}_2) \\ LP_2 &= \widehat{\text{RaiseException}}_{def}(\hat{e}s_1 \sqcup \hat{e}s_2) \\ LP_3 &= \{ \langle \#PureLocal_R, @return \rangle \} \end{aligned}$$

$$\hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Object.seal"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

$$\hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Object.freeze"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

where  $\hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"})$

$$\begin{aligned} \hat{e}s &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ LP_1 &= \bigcup_{i_1 \in \hat{v}.2} \{ \langle \hat{l}_i, @extensible \rangle \} \cup \bigcup_{s \in \widehat{\text{GetProps}}(\hat{H}, \hat{l}_i)} \{ \langle \hat{l}_i, s \rangle \} \\ LP_2 &= \widehat{\text{RaiseException}}_{def}(\hat{e}s) \\ LP_3 &= \{ \langle \#PureLocal_R, @return \rangle \} \end{aligned}$$

$$\hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Object.preventExtensions"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

where  $\hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"})$

$$\begin{aligned} \hat{e}s &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ LP_1 &= \bigcup_{i_1 \in \hat{v}.2} \{ \langle \hat{l}_i, @extensible \rangle \} \\ LP_2 &= \widehat{\text{RaiseException}}_{def}(\hat{e}s) \\ LP_3 &= \{ \langle \#PureLocal_R, @return \rangle \} \end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{def}[\text{BuiltintCall}(\text{"Object.isSealed"}, args)](\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{def}[\text{BuiltintCall}(\text{"Object.isFrozen"}, args)](\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{def}[\text{BuiltintCall}(\text{"Object.isExtensible"}, args)](\hat{H}, \hat{C}) &= LP_1 \cup LP_2
\end{aligned}$$

where  $\hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"})$

$$\begin{aligned}
\hat{e}s &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
LP_1 &= \widehat{\text{RaiseException}}_{def}(\hat{e}s) \\
LP_2 &= \{ \langle \# \text{PureLocal}_R, @return \rangle \}
\end{aligned}$$

$$\hat{\mathcal{I}}_{def}[\text{BuiltintCall}(\text{"Object.keys"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4$$

where  $\hat{l}_R = (\hat{a}_1, \text{Recent})$

$$\begin{aligned}
LP_1 &= \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_1) \\
\hat{v} &= \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
\hat{e}s &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
LP_2 &= \bigcup_{i \in \hat{v}.2} \bigcup_{s \in \widehat{\text{NewArrayObject}}_{def}} \{ \langle \hat{l}_R, s \rangle \} \\
LP_3 &= \widehat{\text{RaiseException}}_{def}(\hat{e}s) \\
LP_4 &= \{ \langle \# \text{PureLocal}_R, @return \rangle \}
\end{aligned}$$

$$\hat{\mathcal{I}}_{use}[\text{BuiltintCall}(\text{"Object"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5$$

where  $\hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"})$

$$\begin{aligned}
LP_1 &= \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
(LP_2, \hat{e}s) &= \begin{cases} (\widehat{\text{toObject}}_{use}(\hat{H}, \hat{C}, \hat{v}_{new}, \hat{a}_1), \hat{e}s'_1) & \text{if } \hat{v}.1.3 \not\sqsubseteq \perp_{Bool} \vee \hat{v}.1.3 \not\sqsubseteq \perp_{Number} \vee \hat{v}.1.3 \not\sqsubseteq \perp_{String} \\ (\{\}, \{\}) & \text{otherwise} \end{cases} \\
\hat{v}_{new} &= \text{Value}(PValue(\perp_{Undef}, \perp_{Null}, \hat{v}.1.3, \hat{v}.1.4, \hat{v}.1.5), \hat{v}.2) \\
\hat{e}s'_1 &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \vee \hat{v}.1.2 \not\sqsubseteq \perp_{Null} \\ \{\} & \text{otherwise} \end{cases} \\
LP_3 &= \begin{cases} \widehat{\text{Oldify}}_{use}(\hat{H}, \hat{C}, \hat{v}_{new}, \hat{a}_1) & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \vee \hat{v}.1.2 \not\sqsubseteq \perp_{Null} \\ \{\} & \text{otherwise} \end{cases} \\
LP_4 &= \widehat{\text{RaiseException}}_{def}(\hat{e}s) \\
LP_5 &= \{ \langle \# \text{PureLocal}_R, @return \rangle \}
\end{aligned}$$

$$\hat{\mathcal{I}}_{use}[\text{BuiltintCall}(\text{"Object.constructor"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5$$

where  $LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"})$

$\hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"})$

$$\begin{aligned}
(LP_2, \hat{e}s) &= \begin{cases} (\bigcup_{i \in \hat{C}.2} \bigcup_{s \in \hat{P}_1 \cup \hat{P}_2 \cup \hat{P}_3} \{ \langle \hat{l}, s \rangle \}, \hat{e}s'_1) & \text{if } \hat{v}.1.3 \not\sqsubseteq \perp_{Bool} \vee \hat{v}.1.3 \not\sqsubseteq \perp_{Number} \vee \hat{v}.1.3 \not\sqsubseteq \perp_{String} \\ (\{\}, \{\}) & \text{otherwise} \end{cases} \\
\hat{v}_{new} &= \text{Value}(PValue(\perp_{Undef}, \perp_{Null}, \hat{v}.1.3, \hat{v}.1.4, \hat{v}.1.5), \hat{v}.2) \\
\hat{P}_1 &= \begin{cases} \widehat{\text{NewBool}}_{def} & \text{if } \hat{v}_{new}.1.3 \not\sqsubseteq \perp_{Bool} \\ \{\} & \text{otherwise} \end{cases} \\
\hat{P}_2 &= \begin{cases} \widehat{\text{NewNumber}}_{def} & \text{if } \hat{v}_{new}.1.4 \not\sqsubseteq \perp_{Number} \\ \{\} & \text{otherwise} \end{cases} \\
\hat{P}_3 &= \begin{cases} \widehat{\text{NewString}}_{def}(\hat{v}_{new}.1.5) & \text{if } \hat{v}_{new}.1.5 \not\sqsubseteq \perp_{String} \\ \{\} & \text{otherwise} \end{cases} \\
\hat{e}s'_1 &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \vee \hat{v}.1.2 \not\sqsubseteq \perp_{Null} \\ \{\} & \text{otherwise} \end{cases} \\
LP_3 &= \begin{cases} \bigcup_{i \in \hat{C}.2} \bigcup_{s \in \widehat{\text{NewObject}}_{def}} \{ \langle \hat{l}, s \rangle \} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \vee \hat{v}.1.2 \not\sqsubseteq \perp_{Null} \\ \{\} & \text{otherwise} \end{cases} \\
\hat{l}_R &= (\hat{a}_1, \text{Recent}) \\
LP_4 &= \widehat{\text{RaiseException}}_{use}(\hat{e}s) \\
LP_5 &= \{ \langle \# \text{PureLocal}_R, @return \rangle \}
\end{aligned}$$

$$\hat{\mathcal{I}}_{use}[\![\text{BuiltintCall}(\text{"Object.getPrototypeOf"}, args)]\!](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4$$

$$\begin{aligned} \text{where } \hat{v} &= \widehat{getArgValue}(\hat{H}, \hat{C}, "0") \\ LP_1 &= \widehat{getArgValue}_{use}(\hat{H}, \hat{C}, "0") \\ \hat{e}s &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ LP_2 &= \bigcup_{\hat{l} \in \hat{C}.2} \{ \langle \hat{l}, @proto \rangle \} \\ LP_3 &= \widehat{RaiseException}_{def}(\hat{e}s) \\ LP_4 &= \{ \langle \#PureLocal_R, @return \rangle \} \end{aligned}$$

$$\hat{\mathcal{I}}_{use}[\![\text{BuiltintCall}(\text{"Object.getOwnPropertyDescriptor"}, args)]\!](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5$$

$$\begin{aligned} \text{where } \hat{v} &= \widehat{getArgValue}(\hat{H}, \hat{C}, "0") \\ \hat{s} &= \widehat{toString}(\widehat{toPrimitive}(\widehat{getArgValue}(\hat{H}, \hat{C}, "1"))) \\ LP_1 &= \widehat{getArgValue}_{use}(\hat{H}, \hat{C}, "0") \cup \widehat{getArgValue}_{use}(\hat{H}, \hat{C}, "1") \\ \hat{e}s &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ \hat{l}_R &= (\hat{a}_1, \text{Recent}) \\ LP_2 &= \bigcup_{\hat{l} \in \hat{C}.2} \widehat{absPair}(\hat{H}, \hat{l}, \hat{s}) \\ LP_3 &= \widehat{Oldify}_{use}(\hat{H}, \hat{C}, \hat{a}_1) \\ LP_4 &= \widehat{RaiseException}_{use}(\hat{e}s) \\ LP_5 &= \{ \langle \#PureLocal_R, @return \rangle \} \end{aligned}$$

$$\hat{\mathcal{I}}_{use}[\![\text{BuiltintCall}(\text{"Object.getOwnPropertyNames"}, args)]\!](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5$$

$$\begin{aligned} \text{where } \hat{l}_R &= (\hat{a}_1, \text{Recent}) \\ LP_1 &= \widehat{Oldify}_{use}(\hat{H}, \hat{C}, \hat{a}_1) \\ \hat{v} &= \widehat{getArgValue}(\hat{H}, \hat{C}, "0") \\ LP_2 &= \widehat{getArgValue}_{use}(\hat{H}, \hat{C}, "0") \\ \hat{e}s &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ LP_3 &= \bigcup_{\hat{l} \in \hat{v}.2} \bigcup_{s \in \widehat{GetProps}(\hat{H}, \hat{l})} \{ \langle \hat{l}, s \rangle, \langle \hat{l}, "@default\_number" \rangle, \langle \hat{l}, "@default\_other" \rangle \} \\ LP_4 &= \widehat{RaiseException}_{use}(\hat{e}s) \\ LP_5 &= \{ \langle \#PureLocal_R, @return \rangle \} \end{aligned}$$

$$\hat{\mathcal{I}}_{use}[\![\text{BuiltintCall}(\text{"Object.create"}, args)]\!](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5$$

$$\begin{aligned} \text{where } \hat{l}_R &= (\hat{a}_1, \text{Recent}) \\ LP_1 &= \widehat{Oldify}_{use}(\hat{H}, \hat{C}, \hat{a}_1) \\ \hat{v}_1 &= \widehat{getArgValue}(\hat{H}, \hat{C}, "0") \\ \hat{v}_2 &= \widehat{getArgValue}(\hat{H}, \hat{C}, "1") \\ \hat{n}_{len} &= \widehat{toUint32}(\widehat{getArgValue}(\hat{H}, \hat{C}, "1")) \\ LP_2 &= \widehat{getArgValue}_{use}(\hat{H}, \hat{C}, "0") \cup \widehat{getArgValue}_{use}(\hat{H}, \hat{C}, "1") \cup \widehat{getArgValue}_{use}(\hat{H}, \hat{C}, "length") \\ \hat{e}s_1 &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ \hat{n}_{len} &= \widehat{toUint32}(\widehat{getArgValue}(\hat{H}, \hat{C}, "length")) \\ \hat{e}s_2 &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{n}_{len} = \hat{2} \wedge \hat{v}_2.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ LP_3 &= \begin{cases} \bigcup_{\hat{l} \in \hat{v}_2.2} \widehat{DefineProperties}_{use}(\hat{H}, \hat{l}_R, \hat{l}) & \text{if } \hat{n}_{len} = \hat{2} \\ \{\} & \text{otherwise} \end{cases} \\ LP_4 &= \widehat{RaiseException}_{use}(\hat{e}s_1 \sqcup \hat{e}s_2) \\ LP_5 &= \{ \langle \#PureLocal_R, @return \rangle \} \end{aligned}$$

$$\hat{\mathcal{I}}_{use}[\![\text{BuiltintCall}(\text{"Object.defineProperty"}, args)]\!](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

$$\begin{aligned} \text{where } \hat{v}_1 &= \widehat{getArgValue}(\hat{H}, \hat{C}, "0") \\ \hat{s}_{name} &= \widehat{toString}(\widehat{toPrimitive}(\widehat{getArgValue}(\hat{H}, \hat{C}, "1"))) \\ \hat{v}_2 &= \widehat{getArgValue}(\hat{H}, \hat{C}, "2") \\ LP_2 &= \widehat{getArgValue}_{use}(\hat{H}, \hat{C}, "0") \cup \widehat{getArgValue}_{use}(\hat{H}, \hat{C}, "1") \cup \widehat{getArgValue}_{use}(\hat{H}, \hat{C}, "2") \\ \hat{e}s_1 &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ \hat{e}s_2 &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{n}_{len} = \hat{2} \wedge \hat{v}_2.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\ LP_1 &= \bigcup_{\hat{l}_1 \in \hat{v}_1.2} \bigcup_{\hat{l}_2 \in \hat{v}_2.2} \widehat{DefineProperty}_{use}(\hat{H}, \hat{l}_1, \hat{s}_{name}, \hat{l}_2) \\ LP_3 &= \{ \langle \#PureLocal_R, @return \rangle \} \end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use}[\![\text{BuiltinCall}(\text{"Object.defineProperties"}, args)\!]\!](\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \\
\text{where } \hat{v}_1 &= \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
\hat{v}_2 &= \text{getArgValue}(\hat{H}, \hat{C}, \text{"1"}) \\
LP_2 &= \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \cup \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"1"}) \\
\hat{e}s_1 &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
\hat{e}s_2 &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{n}_{len} = \hat{2} \wedge \hat{v}_2.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
LP_1 &= \bigcup_{\hat{i}_1 \in \hat{v}_1.2} \bigcup_{\hat{i}_2 \in \hat{v}_2.2} \widehat{\text{DefineProperties}}_{use}(\hat{H}, \hat{i}_1, \hat{i}_2) LP_2 = \widehat{\text{RaiseException}}_{use}(\hat{e}s_1 \sqcup \hat{e}s_2) \\
LP_3 &= \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use}[\![\text{BuiltinCall}(\text{"Object.seal"}, args)\!]\!](\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\
\hat{\mathcal{I}}_{use}[\![\text{BuiltinCall}(\text{"Object.freeze"}, args)\!]\!](\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\
\text{where } \hat{v} &= \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
LP_1 &= \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
\hat{e}s &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
LP_2 &= \bigcup_{\hat{i}_1 \in \hat{v}.2} \bigcup_{s \in \widehat{\text{GetProps}}(\hat{H}, \hat{i})} \{ \langle \hat{l}, s \rangle \} \\
LP_3 &= \widehat{\text{RaiseException}}_{use}(\hat{e}s) \\
LP_4 &= \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use}[\![\text{BuiltinCall}(\text{"Object.preventExtensions"}, args)\!]\!](\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \\
\text{where } \hat{v} &= \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
LP_1 &= \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
\hat{e}s &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
LP_2 &= \widehat{\text{RaiseException}}_{use}(\hat{e}s) \\
LP_3 &= \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use}[\![\text{BuiltinCall}(\text{"Object.isSealed"}, args)\!]\!](\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\
\hat{\mathcal{I}}_{use}[\![\text{BuiltinCall}(\text{"Object.isFrozen"}, args)\!]\!](\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\
\text{where } \hat{v} &= \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
LP_1 &= \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
\hat{e}s &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
LP_2 &= \bigcup_{\hat{i}_1 \in \hat{v}.2} \{ \langle \hat{l}, @extensible \rangle \} \cup \bigcup_{s \in \widehat{\text{GetProps}}(\hat{H}, \hat{i})} \{ \langle \hat{l}, s \rangle \} \\
LP_3 &= \widehat{\text{RaiseException}}_{use}(\hat{e}s) \\
LP_4 &= \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use}[\![\text{BuiltinCall}(\text{"Object.isExtensible"}, args)\!]\!](\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\text{where } \hat{v} &= \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
LP_1 &= \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
\hat{e}s &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
LP_2 &= \bigcup_{\hat{i}_1 \in \hat{v}.2} \{ \langle \hat{l}, @extensible \rangle \} \\
LP_3 &= \widehat{\text{RaiseException}}_{use}(\hat{e}s) \\
LP_4 &= \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use}[\![\text{BuiltinCall}(\text{"Object.keys"}, args)\!]\!](\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5 \\
\text{where } \hat{l}_R &= (\hat{a}_1, \text{Recent}) \\
LP_1 &= \widehat{\text{Oldify}}_{use}(\hat{H}, \hat{C}, \hat{a}_1) \\
\hat{v} &= \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
LP_2 &= \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
\hat{e}s &= \begin{cases} \{\text{TypeError}\} & \text{if } \hat{v}_1.1 \not\sqsubseteq \perp_{PValue} \\ \{\} & \text{otherwise} \end{cases} \\
LP_3 &= \bigcup_{\hat{i} \in \hat{v}.2} \bigcup_{s \in \widehat{\text{GetProps}}(\hat{H}, \hat{i})} \{ \langle \hat{l}, s \rangle, \langle \hat{l}, @default\_number \rangle, \langle \hat{l}, @default\_other \rangle \} \\
LP_4 &= \widehat{\text{RaiseException}}_{use}(\hat{e}s) \\
LP_5 &= \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$



### 11.3.3 Object.prototype

$$\begin{aligned}
\hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Object.prototype.toString"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \\
\hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Object.prototype.toLocaleString"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \\
\hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Object.prototype.valueOf"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \\
\hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Object.prototype.hasOwnProperty"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \\
\hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Object.prototype.isPrototypeOf"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \\
\hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Object.prototype.propertyIsEnumerable"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \\
\text{where } LP_1 &= \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltinCall}(\text{"Object.prototype.toString"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltinCall}(\text{"Object.prototype.toLocaleString"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\text{where } LP_1 &= \bigcup_{i \in \hat{C}.2} \{ \langle \hat{i}, @class \rangle \} \\
LP_2 &= \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltinCall}(\text{"Object.prototype.valueOf"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \\
\text{where } LP_1 &= \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltinCall}(\text{"Object.prototype.hasOwnProperty"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \\
\text{where } \hat{v} &= \widehat{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
\hat{s} &= \widehat{toString}(\widehat{toPrimitive}(\hat{v})) \\
LP_1 &= \widehat{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
LP_2 &= \bigcup_{i \in \hat{C}.2} \widehat{HasOwnProperty}_{use}(\hat{H}, \hat{i}, \hat{s}) \\
LP_3 &= \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltinCall}(\text{"Object.prototype.isPrototypeOf"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \\
\text{where } \hat{v} &= \widehat{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
LP_1 &= \widehat{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
LP_2 &= \bigcup_{i \in \hat{C}.2} \{ \langle \hat{i}, @proto \rangle \} \\
LP_3 &= \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltinCall}(\text{"Object.prototype.propertyIsEnumerable"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \\
\text{where } \hat{s} &= \widehat{toString}(\widehat{toPrimitive}(\widehat{getArgValue}(\hat{H}, \hat{C}, \text{"0"}))) \\
LP_1 &= \widehat{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
LP_2 &= \bigcup_{i \in \hat{C}.2} \widehat{absPair}(\hat{H}, \hat{i}, \hat{s}) \\
LP_3 &= \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

### 11.3.4 Function

### 11.3.5 Function.prototype

$$\hat{\mathcal{I}}_{def}[\![\text{BuiltintCall}(\text{"Function.prototype"}, args)]\!](\hat{H}, \hat{C}) = LP_1$$

where  $LP_1 = \{ \langle \#PureLocal_R, @return \rangle \}$

$$\hat{\mathcal{I}}_{def}[\![\text{BuiltintCall}(\text{"Function.prototype.toString"}, args)]\!](\hat{H}, \hat{C}) = LP_1 \cup LP_2$$

where  $\hat{e}s = \begin{cases} \{\text{TypeError}\} & \text{if } \exists \hat{l} \in \hat{C}.2 : \hat{H}(\hat{l})(@class).1.2.1.5 \neq \text{"Function"} \\ \{\} & \text{otherwise} \end{cases}$

$$LP_1 = \widehat{\text{RaiseException}}_{def}(\hat{e}s)$$

$$LP_2 = \{ \langle \#PureLocal_R, @return \rangle \}$$

$$\hat{\mathcal{I}}_{def}[\![\text{BuiltintCall}(\text{"Function.prototype.apply"}, args)]\!](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5 \cup LP_6$$

where  $LP_1 = \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_1) \cup \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_2) \cup \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_3)$

$$\hat{e}s_1 = \begin{cases} \{\text{TypeError}\} & \text{if } \exists \hat{l} \in \hat{C}.2 : \text{false} \sqsubseteq \widehat{\text{IsCallable}}(\hat{H}, \hat{l}) \\ \{\} & \text{otherwise} \end{cases}$$

$$\hat{v}_{arg} = \text{getArgValue}(\hat{H}, \hat{C}, "1")$$

$$\hat{v}_{arg1} = \text{Value}(\text{PValue}(\perp_{Undef}, \perp_{Null}, \hat{v}_{arg}.1.3, \hat{v}_{arg}.1.4, \hat{v}_{arg}.1.5), \hat{v}_{arg}.2)$$

$$(\hat{v}_{arg2}, \hat{e}s_2) = \begin{cases} (\text{Value}(\perp_{PValue}, \hat{v}_{arg1}.2), \{\text{TypeError}\}) & \text{if } \hat{v}_{arg1}.1 \not\sqsubseteq \perp_{PValue} \\ (\hat{v}_{arg1}, \{\}) & \text{otherwise} \end{cases}$$

$$LP_2 = \begin{cases} LP'_2 & \text{if } \hat{v}_{arg2} \not\sqsubseteq \perp_{Value} \\ \{\} & \text{otherwise} \end{cases}$$

$$LP'_2 = \bigcup_{i \in \hat{v}_{arg2}.2} \begin{cases} \bigcup_{i \in \{0, \dots, n-1\}} \{ \langle \hat{l}_{R_3}, i \rangle \} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \\ \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ \widehat{\text{absPair}}(\hat{H}, \hat{l}_{R_3}, \text{NumStr}) & \text{otherwise} \end{cases}$$

$$\hat{n}_{len} = \widehat{\text{toUInt32}}(\text{Proto}(\hat{H}, \hat{l}, \text{"length"}))$$

$$\hat{v}_{this} = \text{getArgValue}(\hat{H}, \hat{l}, "0")$$

$$\hat{L}_{arg} = \widehat{\text{getThis}}(\hat{H}, \hat{v}_{this})$$

$$\hat{v}_{this2} = \text{Value}(\text{PValue}(\perp_{Undef}, \perp_{Null}, \hat{v}_{this}.1.3, \hat{v}_{this}.1.4, \hat{v}_{this}.1.5), \hat{L}_{arg})$$

$$LP_3 = \widehat{\text{toObject}}_{def}(\hat{H}, \hat{C}, \hat{v}_{this2}, \hat{a}_4)$$

$$LP_4 = \{ \langle \hat{l}_{R_3}, \text{"callee"} \rangle \}$$

$$LP_5 = \widehat{\text{RaiseException}}_{def}(\hat{e}s_1 \sqcup \hat{e}s_2)$$

$$LP_6 = \{ \langle \#PureLocal_R, @return \rangle \}$$

$$\hat{\mathcal{I}}_{def}[\![\text{BuiltintCall}(\text{"Function.prototype.call"}, args)]\!](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5 \cup LP_6$$

where  $LP_1 = \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_1) \cup \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_2)$

$$\hat{e}s = \begin{cases} \{\text{TypeError}\} & \text{if } \exists \hat{l} \in \hat{C}.2 : \text{false} \sqsubseteq \widehat{\text{IsCallable}}(\hat{H}, \hat{l}) \\ \{\} & \text{otherwise} \end{cases}$$

$$\hat{n}_{len} = \text{getArgValue}(\hat{H}, \hat{l}, \text{"length"}) \hat{-} \hat{1}$$

$$LP_2 = \begin{cases} \bigcup_{i \in \{0, \dots, n-1\}} \{ \langle \hat{l}_{R_1}, i \rangle \} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \vee \hat{n}_{len} = \text{NUIntSingle}(n) \\ \{\} & \text{otherwise} \end{cases}$$

$$\hat{v}_{this} = \text{getArgValue}(\hat{H}, \hat{l}, "0")$$

$$\hat{L}_{arg} = \widehat{\text{getThis}}(\hat{H}, \hat{v}_{this})$$

$$\hat{v}_{this2} = \text{Value}(\text{PValue}(\perp_{Undef}, \perp_{Null}, \hat{v}_{this}.1.3, \hat{v}_{this}.1.4, \hat{v}_{this}.1.5), \hat{L}_{arg})$$

$$LP_3 = \widehat{\text{toObject}}_{def}(\hat{H}, \hat{C}, \hat{v}_{this2}, \hat{a}_4)$$

$$LP_4 = \{ \langle \hat{l}_{R_3}, \text{"callee"} \rangle \}$$

$$LP_5 = \widehat{\text{RaiseException}}_{def}(\hat{e}s_1 \sqcup \hat{e}s_2)$$

$$LP_6 = \{ \langle \#PureLocal_R, @return \rangle \}$$

$$\hat{\mathcal{I}}_{use}[\text{BuiltintCall}(\text{"Function.prototype"}, args)](\hat{H}, \hat{C}) = LP_1$$

where  $LP_1 = \{ \langle \#PureLocal_R, @return \rangle \}$

$$\hat{\mathcal{I}}_{use}[\text{BuiltintCall}(\text{"Function.prototype.toString"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

where  $\hat{e}s = \begin{cases} \{\text{TypeError}\} & \text{if } \exists \hat{l} \in \hat{C}.2 : \hat{H}(\hat{l})(@class).1.2.1.5 \neq \text{"Function"} \\ \{\} & \text{otherwise} \end{cases}$

$LP_1 = \bigcup_{\hat{l} \in \hat{C}.2} \{ \langle \hat{l}, @class \rangle \}$

$LP_2 = \text{RaiseException}_{use}(\hat{e}s)$

$LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}$

$$\hat{\mathcal{I}}_{use}[\text{BuiltintCall}(\text{"Function.prototype.apply"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5 \cup LP_6 \cup LP_7$$

where  $LP_1 = \text{Oldify}_{use}(\hat{H}, \hat{C}, \hat{a}_1) \cup \text{Oldify}_{use}(\hat{H}, \hat{C}, \hat{a}_2) \cup \text{Oldify}_{use}(\hat{H}, \hat{C}, \hat{a}_3)$

$\hat{e}s_1 = \begin{cases} \{\text{TypeError}\} & \text{if } \exists \hat{l} \in \hat{C}.2 : \text{false} \sqsubseteq \widehat{\text{IsCallable}}(\hat{H}, \hat{l}) \\ \{\} & \text{otherwise} \end{cases}$

$\hat{L}_{fun} = \{ \hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \text{true} \sqsubseteq \widehat{\text{IsCallable}}(\hat{H}, \hat{l}) \}$

$\hat{v}_{arg} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"1"})$

$LP_2 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \cup \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"1"})$

$\hat{v}_{arg1} = \text{Value}(PValue(\perp_{Undef}, \perp_{Null}, \hat{v}_{arg}.1.3, \hat{v}_{arg}.1.4, \hat{v}_{arg}.1.5), \hat{v}_{arg}.2)$

$(\hat{v}_{arg2}, \hat{e}s_2) = \begin{cases} (\text{Value}(\perp_{PValue}, \hat{v}_{arg1}.2), \{\text{TypeError}\}) & \text{if } \hat{v}_{arg1}.1 \not\sqsubseteq \perp_{PValue} \\ (\hat{v}_{arg1}, \{\}) & \text{otherwise} \end{cases}$

$LP_3 = \begin{cases} LP'_3 & \text{if } \hat{v}_{arg2} \not\sqsubseteq \perp_{Value} \\ \{\} & \text{otherwise} \end{cases}$

$LP'_3 = \bigcup_{\hat{l} \in \hat{v}_{arg2}.2} \hat{L}_{P_{len}} \cup \begin{cases} \bigcup_{i \in \{0, \dots, n-1\}} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \hat{i}) & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \\ \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{NumStr}) & \text{otherwise} \end{cases}$

$\hat{n}_{len} = \text{toUInt32}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"}))$

$\hat{L}_{P_{len}} = \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{"length"})$

$\hat{v}_{this} = \text{getArgValue}(\hat{H}, \hat{l}, \text{"0"})$

$\hat{L}_{arg} = \widehat{\text{getThis}}(\hat{H}, \hat{v}_{this})$

$\hat{v}_{this2} = \text{Value}(PValue(\perp_{Undef}, \perp_{Null}, \hat{v}_{this}.1.3, \hat{v}_{this}.1.4, \hat{v}_{this}.1.5), \hat{L}_{arg})$

$LP_4 = \text{toObject}_{use}(\hat{H}, \hat{C}, \hat{v}_{this2}, \hat{a}_4)$

$LP_5 = \bigcup_{\hat{l} \in \hat{L}_{fun}} \{ \langle \hat{l} @ function \rangle, \langle \hat{l} @ scope \rangle \}$

$LP_6 = \text{RaiseException}_{def}(\hat{e}s_1 \sqcup \hat{e}s_2)$

$LP_7 = \{ \langle \#PureLocal_R, @return \rangle \}$

$$\hat{\mathcal{I}}_{use}[\text{BuiltintCall}(\text{"Function.prototype.call"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5 \cup LP_6 \cup LP_7$$

where  $LP_1 = \text{Oldify}_{def}(\hat{H}, \hat{C}, \hat{a}_1) \cup \text{Oldify}_{def}(\hat{H}, \hat{C}, \hat{a}_2)$

$\hat{e}s = \begin{cases} \{\text{TypeError}\} & \text{if } \exists \hat{l} \in \hat{C}.2 : \text{false} \sqsubseteq \widehat{\text{IsCallable}}(\hat{H}, \hat{l}) \\ \{\} & \text{otherwise} \end{cases}$

$LP_2 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"length"}) \cup \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"})$

$\hat{n}_{len} = \text{getArgValue}(\hat{H}, \hat{l}, \text{"length"}) \hat{-} 1$

$LP_3 = \begin{cases} \bigcup_{i \in \{0, \dots, n-1\}} \text{getArgValue}_{use}(\hat{H}, \hat{C}, i+1) & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \vee \hat{n}_{len} = \text{NUIntSingle}(n) \\ \{\} & \text{otherwise} \end{cases}$

$\hat{v}_{this} = \text{getArgValue}(\hat{H}, \hat{l}, \text{"0"})$

$\hat{L}_{arg} = \widehat{\text{getThis}}(\hat{H}, \hat{v}_{this})$

$\hat{v}_{this2} = \text{Value}(PValue(\perp_{Undef}, \perp_{Null}, \hat{v}_{this}.1.3, \hat{v}_{this}.1.4, \hat{v}_{this}.1.5), \hat{L}_{arg})$

$LP_4 = \text{toObject}_{use}(\hat{H}, \hat{C}, \hat{v}_{this2}, \hat{a}_4)$

$LP_5 = \bigcup_{\hat{l} \in \hat{L}_{fun}} \{ \langle \hat{l} @ function \rangle, \langle \hat{l} @ scope \rangle \}$

$LP_6 = \text{RaiseException}_{def}(\hat{e}s_1 \sqcup \hat{e}s_2)$

$LP_7 = \{ \langle \#PureLocal_R, @return \rangle \}$

### 11.3.6 Array

$$\hat{\mathcal{I}}_{def}[\llbracket \text{BuiltinCall}(\text{"Array"}, args) \rrbracket](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4$$

where  $\hat{l}_R = (\hat{a}_1, \text{Recent})$

$$LP_1 = \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_1)$$

$$\hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"})$$

$$\hat{n}_{len} = \text{toUInt32}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"length"}))$$

$$\hat{e}s = \begin{cases} \hat{e}s' & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \wedge n = 1 \\ \{\} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \wedge n! = 1 \\ \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ \hat{e}s' & \text{otherwise} \end{cases}$$

$$\hat{e}s' = \begin{cases} \{\} & \text{if } \hat{v}.1.4 = \text{UInt} \vee \hat{v}.1.4 = \text{UIntSingle} \vee \hat{v}.1.4 = \text{NumBot} \\ \{\text{RangeError}\} & \text{otherwise} \end{cases}$$

$$LP_2 = \bigcup_{s \in \widehat{\text{NewArrayObject}}_{def}} \{ \langle \hat{l}_R, s \rangle \}$$

$$LP_3 = \widehat{\text{RaiseException}}_{def}(\hat{e}s_1 \sqcup \hat{e}s_2)$$

$$LP_4 = \{ \langle \# \text{PureLocal}_R, @return \rangle \}$$

$$\hat{\mathcal{I}}_{def}[\llbracket \text{BuiltinCall}(\text{"Array.constructor"}, args) \rrbracket](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

where  $\hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"})$

$$\hat{n}_{len} = \text{toUInt32}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"length"}))$$

$$\hat{e}s = \begin{cases} \hat{e}s' & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \wedge n = 1 \\ \{\} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \wedge n! = 1 \\ \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ \hat{e}s' & \text{otherwise} \end{cases}$$

$$\hat{e}s' = \begin{cases} \{\} & \text{if } \hat{v}.1.4 = \text{UInt} \vee \hat{v}.1.4 = \text{UIntSingle} \vee \hat{v}.1.4 = \text{NumBot} \\ \{\text{RangeError}\} & \text{otherwise} \end{cases}$$

$$LP_1 = \bigcup_{\hat{l} \in \hat{C}.2} \bigcup_{s \in \widehat{\text{NewArrayObject}}_{def}} \{ \langle \hat{l}, s \rangle \}$$

$$LP_2 = \widehat{\text{RaiseException}}_{def}(\hat{e}s_1 \sqcup \hat{e}s_2)$$

$$LP_3 = \{ \langle \# \text{PureLocal}_R, @return \rangle \}$$

$$\hat{\mathcal{I}}_{def}[\llbracket \text{BuiltinCall}(\text{"Array.isArray"}, args) \rrbracket](\hat{H}, \hat{C}) = LP_1$$

where  $LP_1 = \{ \langle \# \text{PureLocal}_R, @return \rangle \}$

$$\hat{\mathcal{I}}_{use}[\llbracket \text{BuiltinCall}(\text{"Array"}, args) \rrbracket](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4$$

where  $\hat{l}_R = (\hat{a}_1, \text{Recent})$

$$LP_1 = \widehat{\text{Oldify}}_{use}(\hat{H}, \hat{C}, \hat{a}_1)$$

$$\hat{n}_{arglen} = \text{toUInt32}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"length"}))$$

$$LP_2 = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \cup \text{getArgValue}(\hat{H}, \hat{C}, \text{"length"})$$

$$\hat{e}s = \begin{cases} \hat{e}s' & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \wedge n = 1 \\ \{\} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \wedge n! = 1 \\ \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ \hat{e}s' & \text{otherwise} \end{cases}$$

$$\hat{e}s' = \begin{cases} \{\} & \text{if } \hat{v}.1.4 = \text{UInt} \vee \hat{v}.1.4 = \text{UIntSingle} \vee \hat{v}.1.4 = \text{NumBot} \\ \{\text{RangeError}\} & \text{otherwise} \end{cases}$$

$$LP_3 = \begin{cases} \bigcup_{i \in \{0, \dots, n-1\}} \{ \langle \hat{l}_R, i \rangle \} & \text{if } \hat{n}_{arglen} = \text{UIntSingle}(n) \\ \{\} & \text{if } \hat{n}_{arglen} = \perp_{Number} \\ \text{ahfabsPair}(\hat{H}, \hat{l}_R, \text{NumStr}) & \text{otherwise} \end{cases}$$

$$LP_4 = \widehat{\text{RaiseException}}_{use}(\hat{e}s_1 \sqcup \hat{e}s_2)$$

$$LP_5 = \{ \langle \# \text{PureLocal}_R, @return \rangle \}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{use} \llbracket \text{BuiltinCall}(\text{"Array.constructor"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5 \\
& \text{where } \hat{v} = \widehat{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& \hat{n}_{arg} = \widehat{toUInt32}(\widehat{getArgValue}(\hat{H}, \hat{C}, \text{"length"})) \\
& LP_1 = \widehat{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \cup \widehat{getArgValue}(\hat{H}, \hat{C}, \text{"length"}) \\
& \hat{e}s = \begin{cases} \hat{e}s' & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \wedge n = 1 \\ \{\} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \wedge n \neq 1 \\ \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ \hat{e}s' & \text{otherwise} \end{cases} \\
& \hat{e}s' = \begin{cases} \{\} & \text{if } \hat{v}.1.4 = \text{UInt} \vee \hat{v}.1.4 = \text{UIntSingle} \vee \hat{v}.1.4 = \text{NumBot} \\ \{\text{RangeError}\} & \text{otherwise} \end{cases} \\
& LP_2 = \begin{cases} \bigcup_{i \in \hat{C}.2} \bigcup_{i \in \{0, \dots, n-1\}} \{ \langle \hat{l}, i \rangle \} & \text{if } \hat{n}_{arglen} = \text{UIntSingle}(n) \\ \{\} & \text{if } \hat{n}_{arglen} = \perp_{Number} \\ \bigcup_{i \in \hat{C}.2} \widehat{absPair}(\hat{H}, \hat{l}, \text{NumStr}) & \text{otherwise} \end{cases} \\
& LP_3 = \bigcup_{i \in \hat{C}.2} \bigcup_{s \in \widehat{NewArrayObject}_{def}} LP_4 = \widehat{RaiseException}_{use}(\hat{e}s_1 \sqcup \hat{e}s_2) \\
& LP_5 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{use} \llbracket \text{BuiltinCall}(\text{"Array.isArray"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \\
& \text{where } \hat{v} = \widehat{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& LP_1 = \widehat{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
& LP_2 = \bigcup_{i \in \hat{v}.2} \{ \langle \hat{l}, @class \rangle \} \\
& LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

### 11.3.7 Array.prototype

$$\begin{aligned}
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Array.prototype.toString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Array.prototype.toLocaleString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Array.prototype.join"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \text{where } LP_1 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Array.prototype.concat"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \\
& \text{where } \hat{l}_R = (\hat{a}_1, \text{Recent}) \\
& LP_1 = \widehat{Oldify}_{def}(\hat{H}, \hat{C}, \hat{a}_1) \\
& \hat{n}_{arglen} = \widehat{toUInt32}(\widehat{getArgValue}(\hat{H}, \hat{C}, \text{"length"})) \\
& LP_2 = \begin{cases} \{\} & \text{if } \hat{n}_{arglen} = \perp_{Number} \\ LP'_2 & \text{if } \hat{n}_{arglen} = \text{UIntSingle}(n_{arglen}) \\ LP_{array} & \text{otherwise} \end{cases} \\
& LP'_2 = \bigcup_{i \in \hat{C}.2} \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{array} \cup \bigcup_{i \in \{0, \dots, n-1\}} \{ \langle \hat{l}_R, i \rangle \} & \text{if } \hat{n}_{arglen} = \text{UIntSingle}(n) \\ LP_{array} & \text{otherwise} \end{cases} \\
& \hat{n}_{len} = \widehat{toUInt32}(\widehat{Proto}(\hat{H}, \hat{l}, \text{"length"})) \\
& LP_{array} = \bigcup_{s \in \widehat{NewArrayObject}_{def}} \{ \langle \hat{l}_R, s \rangle \} \\
& LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\hat{\mathcal{I}}_{def}[\text{BuiltintCall}(\text{"Array.prototype.pop"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5$$

where  $LP_1 = \bigcup_{i \in \hat{C}.2} \begin{cases} LP_{length} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n_{len}) \wedge n_{len} = 0 \\ LP_{length} \cup \widehat{\text{Delete}}_{def}(\hat{H}, \hat{l}, n_{len} - 1) & \text{if } \hat{n}_{len} = \text{UIntSingle}(n_{len}) \wedge n_{len} > 0 \\ \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{length} \cup \widehat{\text{Delete}}_{def}(\hat{H}, \hat{l}, \text{NumStr}) & \text{otherwise} \end{cases}$ 

$$\hat{n}_{len} = \text{toUInt32}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"}))$$

$$LP_{length} = \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \text{"length"})$$

$$LP_2 = \{ \langle \#PureLocal_R, @return \rangle \}$$

$$\hat{\mathcal{I}}_{def}[\text{BuiltintCall}(\text{"Array.prototype.push"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2$$

where  $\hat{n}_{arg} = \text{toUInt32}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"length"}))$

$$LP_1 = \begin{cases} \{\} & \text{if } \hat{n}_{arg} = \perp_{Number} \\ LP'_1 & \text{if } \hat{n}_{arg} = \text{UIntSingle}(n_{arg}) \\ \bigcup_{i \in \hat{C}.2} \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \text{NumStr}) & \text{otherwise} \end{cases}$$

$$LP'_1 = \bigcup_{i \in \hat{C}.2} \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \text{"length"}) \cup \bigcup_{i \in \{0, \dots, n_{arg}-1\}} \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, i + n) & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \\ \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \text{NumStr}) & \text{otherwise} \end{cases}$$

$$\hat{n}_{len} = \text{toUInt32}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"}))$$

$$LP_2 = \{ \langle \#PureLocal_R, @return \rangle \}$$

$$\hat{\mathcal{I}}_{def}[\text{BuiltintCall}(\text{"Array.prototype.reverse"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2$$

where  $LP_1 = \bigcup_{i \in \hat{C}.2} \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP'_1 & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \\ \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \text{NumStr}) \cup \widehat{\text{Delete}}_{def}(\hat{H}, \hat{l}, \text{NumStr}) & \text{otherwise} \end{cases}$ 

$$\hat{n}_{len} = \text{toUInt32}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"}))$$

$$LP'_1 = \bigcup_{i \in \{0, \dots, \text{floor}(n/2)\}} LP_{swap} \cup LP_{up} \cup LP_{low}$$

$$LP_{swap} = \begin{cases} \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \hat{s}_{low}) \cup \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \hat{s}_{up}) & \text{if } \text{true} \sqsubseteq \hat{b}_{low} \wedge \text{true} \sqsubseteq \hat{b}_{up} \\ \{\} & \text{otherwise} \end{cases}$$

$$LP_{up} = \begin{cases} \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \hat{s}_{low}) \cup \widehat{\text{Delete}}_{def}(\hat{H}, \hat{l}, \hat{s}_{up}) & \text{if } \text{false} \sqsubseteq \hat{b}_{low} \wedge \text{true} \sqsubseteq \hat{b}_{up} \\ \{\} & \text{otherwise} \end{cases}$$

$$LP_{low} = \begin{cases} \widehat{\text{Delete}}_{def}(\hat{H}, \hat{l}, \hat{s}_{low}) \cup \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \hat{s}_{up}) & \text{if } \text{true} \sqsubseteq \hat{b}_{low} \wedge \text{false} \sqsubseteq \hat{b}_{up} \\ \{\} & \text{otherwise} \end{cases}$$

$$\hat{s}_{low} = \hat{i}$$

$$\hat{s}_{up} = n - \hat{i} - 1$$

$$\hat{b}_{low} \text{ HasProperty}(\hat{H}, \hat{C}, \hat{s}_{low})$$

$$\hat{b}_{up} \text{ HasProperty}(\hat{H}, \hat{C}, \hat{s}_{up})$$

$$LP_2 = \{ \langle \#PureLocal_R, @return \rangle \}$$

$$\hat{\mathcal{I}}_{def}[\text{BuiltintCall}(\text{"Array.prototype.shift"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2$$

where  $LP_1 = \bigcup_{i \in \hat{C}.2} \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP'_1 & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \\ LP_{storelen} \cup \widehat{\text{Delete}}_{def}(\hat{H}, \hat{l}, \text{NumStr}) & \text{otherwise} \end{cases}$ 

$$\hat{n}_{len} = \text{toUInt32}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"}))$$

$$LP'_1 = \begin{cases} LP_{storelen} & \text{if } n = 0 \\ LP_{array} \cup LP_{delete} \cup LP_{storelen} & \text{otherwise} \end{cases}$$

$$LP_{array} = \bigcup_{i \in \{1, \dots, n-1\}} LP_{shift1} \cup LP_{shift2}$$

$$LP_{shift1} = \begin{cases} \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \hat{s}_{to}) & \text{if } \text{true} \sqsubseteq \hat{b} \\ \{\} & \text{otherwise} \end{cases}$$

$$LP_{shift2} = \begin{cases} \widehat{\text{Delete}}_{def}(\hat{H}, \hat{l}, \hat{s}_{to}) & \text{if } \text{false} \sqsubseteq \hat{b} \\ \{\} & \text{otherwise} \end{cases}$$

$$LP_{delete} = \widehat{\text{Delete}}_{def}(\hat{H}, \hat{l}, n - 1)$$

$$LP_{storelen} = \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \text{"length"})$$

$$\hat{s}_{from} = \hat{i}$$

$$\hat{s}_{to} = n - \hat{i} - 1$$

$$\hat{b} = \text{HasProperty}(\hat{H}, \hat{C}, \hat{s}_{from})$$

$$LP_2 = \{ \langle \#PureLocal_R, @return \rangle \}$$

$$\hat{\mathcal{I}}_{def}[\text{BuiltintCall}(\text{"Array.prototype.slice"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

where  $\hat{l}_R = (\hat{a}_1, \text{Recent})$

$$LP_1 = \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_1)$$

$$\hat{n}_{start} = \widehat{\text{toInteger}}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}))$$

$$\hat{n}_{end} = \widehat{\text{toInteger}}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"1"}))$$

$$LP_2 = \begin{cases} \{\} & \text{if } \hat{n}_{start} = \perp_{Number} \vee \hat{n}_{end} = \perp_{Number} \\ LP_{single} & \text{if } \gamma(\hat{n}_{start}) = n_{start} \wedge \gamma(\hat{n}_{end}) = n_{end} \\ LP_{top} & \text{otherwise} \end{cases}$$

$$LP_{single} = \bigcup_{i \in \hat{C}.2} \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{array} \cup \bigcup_{i \in \{0, \dots, n_{span}-1\}} \{ \langle \hat{l}_R, i \rangle \} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \\ LP_{array} & \text{otherwise} \end{cases}$$

$$LP_{top} = \bigcup_{i \in \hat{C}.2} \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{array} & \text{otherwise} \end{cases}$$

$$\hat{n}_{len} = \widehat{\text{toUInt32}}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"}))$$

$$LP_{array} = \bigcup_{s \in \widehat{\text{NewArrayObject}}_{def}} \{ \langle \hat{l}_R, s \rangle \}$$

$$n_{from} = \begin{cases} \max(n + n_{start}, 0) & \text{if } \hat{n}_{len} = \perp_{Number} \\ \min(n_{start}, n) & \text{otherwise} \end{cases}$$

$$n_{to} = \begin{cases} \max(n + n_{end}, 0) & \text{if } \hat{n}_{len} = \perp_{Number} \\ \min(n_{end}, n) & \text{otherwise} \end{cases}$$

$$n_{span} = \max(n_{to} - n_{from}, 0)$$

$$LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}$$

$$\hat{\mathcal{I}}_{def}[\text{BuiltintCall}(\text{"Array.prototype.splice"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

where  $\hat{l}_R = (\hat{a}_1, \text{Recent})$

$$LP_1 = \widehat{\text{Oldify}}_{def}(\hat{H}, \hat{C}, \hat{a}_1)$$

$$\hat{n}_{arg} = \widehat{\text{toInteger}}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"length"}))$$

$$\hat{n}_{start} = \widehat{\text{toInteger}}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}))$$

$$\hat{n}_{count} = \widehat{\text{toInteger}}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"1"}))$$

$$LP_2 = \begin{cases} \{\} & \text{if } \hat{n}_{start} = \perp_{Number} \vee \hat{n}_{count} = \perp_{Number} \\ LP_{single} & \text{if } \gamma(\hat{n}_{start}) = n_{start} \wedge \gamma(\hat{n}_{count}) = n_{count} \\ LP_{top} & \text{otherwise} \end{cases}$$

$$LP_{single} = \bigcup_{i \in \hat{C}.2} \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{array} \cup LP_{single1} \cup LP_{single2} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n_{len}) \\ LP_{array} \cup LP_{topstore} \cup LP_{topdelete} & \text{otherwise} \end{cases}$$

$$LP_{single1} = \bigcup_{i \in \{0, \dots, n_{delCount}-1\}} \{ \langle \hat{l}_R, i \rangle \}$$

$$n_{delCount} = \min(\max(n_{count}, 0), n_{len} - n_{start})$$

$$LP_{single2} = \begin{cases} \{\} & \text{if } \hat{n}_{arg} = \perp_{Number} \\ LP_{single3} & \text{if } \hat{n}_{arg} = \text{UIntSingle}(n_{arg}) \\ \bigcup LP_{topstore} \cup LP_{topdelete} & \text{otherwise} \end{cases}$$

$$LP_{single3} = \begin{cases} LP_{singlemove1} \cup LP_{singleadd} \cup LP_{singledelete} \cup LP_{singlelength} & \text{if } n_{addCount} < n_{count} \\ LP_{singlemove2} \cup LP_{singleadd} \cup LP_{singlelength} & \text{otherwise} \end{cases}$$

$$n_{addCount} = n_{arg} - 2$$

$$LP_{singlemove1} = \bigcup_{i \in \{n_{moveStart}, \dots, n_{len}-1\}} \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \hat{s}_{to1}) \cup \widehat{\text{Delete}}_{def}(\hat{H}, \hat{l}, \hat{s}_{to1})$$

$$LP_{singlemove2} = \bigcup_{i \in \{0, \dots, n_{len}-n_{moveStart}-1\}} \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \hat{s}_{to2}) \cup \widehat{\text{Delete}}_{def}(\hat{H}, \hat{l}, \hat{s}_{to2})$$

$$\hat{s}_{to1} = i - n_{count} + n_{addCount}$$

$$\hat{s}_{to2} = n_{len} - 1 - i - n_{count} + n_{addCount}$$

$$LP_{singleadd} = \bigcup_{i \in \{0, \dots, n_{addCount}-1\}} \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, n_{start} + i)$$

$$LP_{singledelete} = \bigcup_{i \in \{n_{newLen}, \dots, n_{len}-1\}} \widehat{\text{Delete}}_{def}(\hat{H}, \hat{l}, i)$$

$$n_{newLen} = n_{len} + n_{addCount} - n_{count} LP_{singlelength} = \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \text{"length"})$$

$$LP_{top} = \bigcup_{i \in \hat{C}.2} \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{array} \cup LP_{topstore} \cup LP_{topdelete} & \text{otherwise} \end{cases}$$

$$\hat{n}_{len} = \widehat{\text{toUInt32}}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"}))$$

$$LP_{array} = \bigcup_{s \in \widehat{\text{NewArrayObject}}_{def}} \{ \langle \hat{l}_R, s \rangle \}$$

$$LP_{topstore} = \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \text{NumStr})$$

$$LP_{topdelete} = \widehat{\text{Delete}}_{def}(\hat{H}, \hat{l}, \text{NumStr})$$

$$LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Array.prototype.unshift"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } \hat{n}_{arg} = \widehat{\text{toUInt32}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"length"})) \\
& LP_1 = \begin{cases} \{\} & \text{if } \hat{n}_{arg} = \perp_{Number} \\ LP_{single} & \text{if } \hat{n}_{arg} = \text{UIntSingle}(n_{arg}) \\ LP_{top} & \text{otherwise} \end{cases} \\
& \hat{n}_{len} = \widehat{\text{toUInt32}}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"})) \\
& LP_{single} = \bigcup_{i \in \hat{C}.2} \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{unshift} \cup LP_{add} \cup LP_{singlelength} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n_{len}) \\ LP_{store} \cup LP_{delete} & \text{otherwise} \end{cases} \\
& LP_{unshift} = \bigcup_{i \in \{0, \dots, n_{len}-1\}} \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \hat{s}_{to}) \cup \widehat{\text{Delete}}_{def}(\hat{H}, \hat{l}, \hat{s}_{to}) \\
& \hat{s}_{to} = n_{len} - 1 - i + n_{arg} \\
& LP_{add} = \bigcup_{i \in \{0, \dots, n_{arg}-1\}} \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, i) \\
& LP_{delete} = \widehat{\text{Delete}}_{def}(\hat{H}, \hat{l}, \text{NumStr}) \\
& LP_{store} = \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \text{NumStr}) \\
& LP_{singlelength} = \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{l}, \text{"length"}) \\
& LP_{top} = \bigcup_{i \in \hat{C}.2} \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{store} \cup LP_{delete} & \text{otherwise} \end{cases} \\
& LP_2 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Array.prototype.indexOf"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Array.prototype.lastIndexOf"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \text{where } LP_1 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{use} \llbracket \text{BuiltinCall}(\text{"Array.prototype.toString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \\
& \hat{\mathcal{I}}_{use} \llbracket \text{BuiltinCall}(\text{"Array.prototype.toLocaleString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \\
& \text{where } \hat{n}_{len} = \widehat{\text{toUInt32}}(\bigcup_{i \in \hat{C}.2} \widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"})) \\
& LP_1 = \bigcup_{i \in \hat{C}.2} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{"length"}) \\
& LP_2 = \begin{cases} LP'_2 \cup LP''_2 & \text{if } \hat{n}_{len} = \text{UIntSingle}(n_{len}) \wedge n_{len} > 0 \\ \{\} & \text{otherwise} \end{cases} \\
& LP'_2 = \bigcup_{i \in \hat{C}.2} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{"0"}) \\
& LP''_2 = \bigcup_{i \in \hat{C}.2} \bigcup_{i \in \{1, \dots, n_{len}-1\}} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{"i"}) \\
& LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{use} \llbracket \text{BuiltinCall}(\text{"Array.prototype.concat"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\
& \text{where } \hat{l}_R = (\hat{a}_1, \text{Recent}) \\
& LP_1 = \widehat{\text{Oldify}}_{use}(\hat{H}, \hat{C}, \hat{a}_1) \\
& \hat{n}_{arglen} = \widehat{\text{toUInt32}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"length"})) \\
& LP_2 = \widehat{\text{getArgValue}}_{use}(\hat{H}, \hat{C}, \text{"length"}) \\
& LP_3 = \begin{cases} \{\} & \text{if } \hat{n}_{arglen} = \perp_{Number} \\ LP_{single} & \text{if } \hat{n}_{arglen} = \text{UIntSingle}(n_{arglen}) \\ LP_{top} & \text{otherwise} \end{cases} \\
& LP_{single} = \bigcup_{i \in \hat{C}.2} \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{len} \cup LP_{array} & \text{if } \hat{n}_{arglen} = \text{UIntSingle}(n) \\ \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{NumStr}) & \text{otherwise} \end{cases} \\
& \hat{n}_{len} = \widehat{\text{toUInt32}}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"})) \\
& LP_{len} = \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{"length"}) \\
& LP_{array} = \bigcup_{i \in \{0, \dots, n-1\}} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, i) \cup \bigcup_{i \in \{0, \dots, n-1\}} \widehat{\text{getArgValue}}_{use}(\hat{H}, \hat{l}, i) \\
& LP_{top} = \bigcup_{i \in \hat{C}.2} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{NumStr}) \cup \widehat{\text{getArgValue}}_{use}(\hat{H}, \hat{C}, \text{NumStr}) \\
& LP_4 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{use} \llbracket \text{BuiltinCall}(\text{"Array.prototype.join"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\
& \text{where } LP_1 = \widehat{\text{getArgValue}}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
& \hat{n}_{len} = \widehat{\text{toUInt32}}(\bigcup_{i \in \hat{C}.2} \widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"})) \\
& LP_2 = \bigcup_{i \in \hat{C}.2} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{"length"}) \\
& LP_3 = \begin{cases} LP_{first} \cup LP_{remain} & \text{if } \hat{n}_{arglen} = \text{UIntSingle}(n_{arglen}) \\ \{\} & \text{otherwise} \end{cases} \\
& LP_{first} = \bigcup_{i \in \hat{C}.2} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{"0"}) \\
& LP_{remain} = \bigcup_{i \in \hat{C}.2} \bigcup_{i \in \{1, \dots, n_{arglen}-1\}} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, i) \\
& LP_4 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$



$$\hat{\mathcal{I}}_{use}[\text{BuiltintCall}(\text{"Array.prototype.pop"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

$$\text{where } \hat{n}_{len} = \text{toUInt32}(\bigcup_{i \in \hat{C}.2} \widehat{\text{Proto}}(\hat{H}, \hat{i}, \text{"length"}))$$

$$LP_1 = \bigcup_{i \in \hat{C}.2} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{i}, \text{"length"})$$

$$LP_2 = \bigcup_{i \in \hat{C}.2} \begin{cases} LP_{length} \cup LP_{store} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n_{len}) \wedge n_{len} = 0 \\ LP_{length} \cup LP_{single} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n_{len}) \wedge n_{len} > 0 \\ \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{length} \cup LP_{top} & \text{otherwise} \end{cases}$$

$$\hat{n}_{len} = \text{toUInt32}(\widehat{\text{Proto}}(\hat{H}, \hat{i}, \text{"length"}))$$

$$LP_{single} = \widehat{\text{Proto}}_{use}(\hat{H}, \hat{i}, n_{len} - 1) \cup \widehat{\text{Delete}}_{use}(\hat{H}, \hat{i}, n_{len} - 1) \cup \widehat{\text{Delete}}_{def}(\hat{H}, \hat{i}, n_{len} - 1) \cup LP_{store}$$

$$LP_{top} = \widehat{\text{Proto}}_{use}(\hat{H}, \hat{i}, \text{NumStr}) \cup \widehat{\text{Delete}}_{use}(\hat{H}, \hat{i}, \text{NumStr}) \cup \widehat{\text{Delete}}_{def}(\hat{H}, \hat{i}, \text{NumStr}) \cup LP_{store}$$

$$LP_{store} = \widehat{\text{PropStore}}_{use}(\hat{H}, \hat{i}, \text{"length"}) \cup \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{i}, \text{"length"})$$

$$LP_{length} = \widehat{\text{Proto}}_{use}(\hat{H}, \hat{i}, \text{"length"})$$

$$LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}$$

$$\hat{\mathcal{I}}_{use}[\text{BuiltintCall}(\text{"Array.prototype.push"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

$$\text{where } \hat{n}_{arg} = \text{toUInt32}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"length"}))$$

$$LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"length"})$$

$$LP_2 = \begin{cases} \{\} & \text{if } \hat{n}_{arg} = \perp_{Number} \\ LP_{single} & \text{if } \hat{n}_{arg} = \text{UIntSingle}(n_{arg}) \\ LP_{top} & \text{otherwise} \end{cases}$$

$$LP_{single} = \bigcup_{i \in \hat{C}.2} LP_{length} \cup \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{single1} \cup LP_{single2} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \\ LP_{top} & \text{otherwise} \end{cases}$$

$$\hat{n}_{len} = \text{toUInt32}(\widehat{\text{Proto}}(\hat{H}, \hat{i}, \text{"length"}))$$

$$LP_{single1} = \bigcup_{i \in \{0, \dots, n-1\}} \widehat{\text{PropStore}}_{use}(\hat{H}, \hat{i}, \hat{i}) \cup \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{i}, \hat{i}) \cup \text{getArgValue}_{use}(\hat{H}, \hat{C}, i)$$

$$LP_{single2} = \widehat{\text{PropStore}}_{use}(\hat{H}, \hat{i}, \text{"length"}) \cup \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{i}, \text{"length"})$$

$$LP_{length} = \widehat{\text{Proto}}_{use}(\hat{H}, \hat{i}, \text{"length"})$$

$$LP_{top} = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{NumStr}) \cup \bigcup_{i \in \hat{C}.2} \widehat{\text{PropStore}}_{use}(\hat{H}, \hat{i}, \text{NumStr}) \cup \widehat{\text{PropStore}}_{def}(\hat{H}, \hat{i}, \text{NumStr})$$

$$LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}$$

$$\hat{\mathcal{I}}_{use}[\text{BuiltintCall}(\text{"Array.prototype.reverse"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2$$

$$\text{where } LP_1 = \bigcup_{i \in \hat{C}.2} LP_{len} LP'_1$$

$$\hat{n}_{len} = \text{toUInt32}(\widehat{\text{Proto}}(\hat{H}, \hat{i}, \text{"length"}))$$

$$LP_{len} = \widehat{\text{Proto}}_{use}(\hat{H}, \hat{i}, \text{"length"})$$

$$LP'_1 = \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{single} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \\ LP_{top} & \text{otherwise} \end{cases}$$

$$LP_{single} = \bigcup_{i \in \{0, \dots, \text{floor}(n/2)\}} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{i}, \hat{s}_{low}) \cup \widehat{\text{Proto}}_{use}(\hat{H}, \hat{i}, \hat{s}_{up}) \cup LP_{swap} \cup LP_{up} \cup LP_{low}$$

$$LP_{swap} = \begin{cases} \widehat{\text{PropStore}}_{use/def}(\hat{H}, \hat{i}, \hat{s}_{low}) \cup \widehat{\text{PropStore}}_{use/def}(\hat{H}, \hat{i}, \hat{s}_{up}) & \text{if } \text{true} \sqsubseteq \hat{b}_{low} \wedge \text{true} \sqsubseteq \hat{b}_{up} \\ \{\} & \text{otherwise} \end{cases}$$

$$LP_{up} = \begin{cases} \widehat{\text{PropStore}}_{use/def}(\hat{H}, \hat{i}, \hat{s}_{low}) \cup \widehat{\text{Delete}}_{use/def}(\hat{H}, \hat{i}, \hat{s}_{up}) & \text{if } \text{false} \sqsubseteq \hat{b}_{low} \wedge \text{true} \sqsubseteq \hat{b}_{up} \\ \{\} & \text{otherwise} \end{cases}$$

$$LP_{low} = \begin{cases} \widehat{\text{Delete}}_{use/def}(\hat{H}, \hat{i}, \hat{s}_{low}) \cup \widehat{\text{PropStore}}_{use/def}(\hat{H}, \hat{i}, \hat{s}_{up}) & \text{if } \text{true} \sqsubseteq \hat{b}_{low} \wedge \text{false} \sqsubseteq \hat{b}_{up} \\ \{\} & \text{otherwise} \end{cases}$$

$$LP_{top} = \widehat{\text{Proto}}_{use}(\hat{H}, \hat{i}, \text{NumStr}) \cup \widehat{\text{PropStore}}_{use/def}(\hat{H}, \hat{i}, \text{NumStr}) \cup \widehat{\text{Delete}}_{use/def}(\hat{H}, \hat{i}, \text{NumStr})$$

$$\hat{s}_{low} = \hat{i}$$

$$\hat{s}_{up} = n - \hat{i} - 1$$

$$\hat{b}_{low} \text{ HasProperty}(\hat{H}, \hat{C}, \hat{s}_{low})$$

$$\hat{b}_{up} \text{ HasProperty}(\hat{H}, \hat{C}, \hat{s}_{up})$$

$$LP_2 = \{ \langle \#PureLocal_R, @return \rangle \}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Array.prototype.shift"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } LP_1 = \bigcup_{i \in \hat{C}.2} LP_{len} \cup LP'_1 \hat{n}_{len} = \widehat{\text{toUInt32}}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"})) \\
& LP_{len} = \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{"length"}) \\
& LP'_1 = \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{single} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \\ LP_{top} & \text{otherwise} \end{cases} \\
& LP_{single} = \begin{cases} LP_{store_{len}} & \text{if } n = 0 \\ \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \hat{0}) \cup LP_{array} \cup LP_{delete} \cup LP_{store_{len}} & \text{otherwise} \end{cases} \\
& LP_{array} = \bigcup_{i \in \{1, \dots, n-1\}} LP_{shift1} \cup LP_{shift2} \\
& LP_{shift1} = \begin{cases} \widehat{\text{PropStore}}_{use/def}(\hat{H}, \hat{l}, \hat{s}_{to}) \cup \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \hat{s}_{from}) & \text{if } \text{true} \sqsubseteq \hat{b} \\ \{\} & \text{otherwise} \end{cases} \\
& LP_{shift2} = \begin{cases} \widehat{\text{Delete}}_{use/def}(\hat{H}, \hat{l}, \hat{s}_{to}) & \text{if } \text{false} \sqsubseteq \hat{b} \\ \{\} & \text{otherwise} \end{cases} \\
& LP_{delete} = \widehat{\text{Delete}}_{use/def}(\hat{H}, \hat{l}, n - 1) \\
& LP_{store_{len}} = \widehat{\text{PropStore}}_{use/def}(\hat{H}, \hat{l}, \text{"length"}) \\
& LP_{top} = \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{NumStr}) \cup \widehat{\text{PropStore}}_{use/def}(\hat{H}, \hat{l}, \text{"length"}) \cup \widehat{\text{Delete}}_{use/def}(\hat{H}, \hat{l}, \text{NumStr}) \\
& \hat{s}_{from} = \hat{i} \\
& \hat{s}_{to} = n - \hat{i} - 1 \\
& \hat{b} = \widehat{\text{HasProperty}}(\hat{H}, \hat{C}, \hat{s}_{from}) \\
& LP_2 = \{ \langle \# \text{PureLocal}_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Array.prototype.slice"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\
& \text{where } \hat{l}_R = (\hat{a}_1, \text{Recent}) \\
& LP_1 = \widehat{\text{Oldify}}_{use}(\hat{H}, \hat{C}, \hat{a}_1) \\
& \hat{n}_{start} = \widehat{\text{toInteger}}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"0"})) \\
& \hat{n}_{end} = \widehat{\text{toInteger}}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"1"})) \\
& LP_2 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \sqcup \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"1"}) \\
& LP_3 = \begin{cases} \{\} & \text{if } \hat{n}_{start} = \perp_{Number} \vee \hat{n}_{end} = \perp_{Number} \\ LP_{single} & \text{if } \gamma(\hat{n}_{start}) = n_{start} \wedge \gamma(\hat{n}_{end}) = n_{end} \\ LP_{top} & \text{otherwise} \end{cases} \\
& LP_{single} = \bigcup_{i \in \hat{C}.2} \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{array} \cup \bigcup_{i \in \{0, \dots, n_{span}-1\}} LP_{slice} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \\ \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{NumStr}) & \text{otherwise} \end{cases} \\
& LP_{slice} = \begin{cases} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{from} + i) & \text{if } \text{true} \sqsubseteq \widehat{\text{HasProperty}}(\hat{H}, \hat{l}, i) \\ \{\} \cup LP_{array} & \text{otherwise} \end{cases} \\
& LP_{top} = \bigcup_{i \in \hat{C}.2} \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{length} \cup LP_{array} & \text{otherwise} \end{cases} \\
& \hat{n}_{len} = \widehat{\text{toUInt32}}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"})) \\
& LP_{array} = \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{NumStr}) & \text{otherwise} \end{cases} \\
& LP_{length} = \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{"length"}) \\
& n_{from} = \begin{cases} \max(n + n_{start}, 0) & \text{if } \hat{n}_{len} = \perp_{Number} \\ \min(n_{start}, n) & \text{otherwise} \end{cases} \\
& n_{to} = \begin{cases} \max(n + n_{end}, 0) & \text{if } \hat{n}_{len} = \perp_{Number} \\ \min(n_{end}, n) & \text{otherwise} \end{cases} \\
& n_{span} = \max(n_{to} - n_{from}, 0) \\
& LP_4 = \{ \langle \# \text{PureLocal}_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
& \hat{\mathcal{L}}_{use} \llbracket \text{BuiltintCall}(\text{"Array.prototype.splice"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\
& \text{where } LP_1 = \widehat{\text{Oldify}}_{-use}(\hat{H}, \hat{C}, \hat{a}_1) \\
& \hat{n}_{arg} = \widehat{\text{toInteger}}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"length"})) \\
& \hat{n}_{start} = \widehat{\text{toInteger}}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"0"})) \\
& \hat{n}_{count} = \widehat{\text{toInteger}}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"1"})) \\
& LP_2 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \cup \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"1"}) \cup \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"length"}) \\
& LP_3 = \begin{cases} \{\} & \text{if } \hat{n}_{start} = \perp_{Number} \vee \hat{n}_{count} = \perp_{Number} \\ LP_{single} & \text{if } \gamma(\hat{n}_{start}) = n_{start} \wedge \gamma(\hat{n}_{count}) = n_{count} \\ LP_{top} & \text{otherwise} \end{cases} \\
& LP_{single} = \bigcup_{\hat{i} \in \hat{C}.2} LP_{len} \cup \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{single_1} \cup LP_{single_2} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n_{len}) \\ LP_{topproto} \cup LP_{topstore} \cup LP_{topdelete} \cup LP_{topget} & \text{otherwise} \end{cases} \\
& LP_{single_1} = \bigcup_{i \in \{0, \dots, n_{delCount} - 1\}} \begin{cases} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, i + \hat{f}_{from}) & \text{if } \text{true} \sqsubseteq \widehat{\text{HasProperty}}(\hat{H}, \hat{l}, i) \\ \{\} & \text{otherwise} \end{cases} \\
& n_{delCount} = \min(\max(n_{count}, 0), n_{len} - n_{start}) \\
& LP_{single_2} = \begin{cases} \{\} & \text{if } \hat{n}_{arg} = \perp_{Number} \\ LP_{single_3} & \text{if } \hat{n}_{arg} = \text{UIntSingle}(n_{arg}) \\ LP_{topstore} \cup LP_{topdelete} \cup LP_{topget} & \text{otherwise} \end{cases} \\
& LP_{single_3} = \begin{cases} LP_{single_{move1}} \cup LP_{single_{add}} \cup LP_{single_{delete}} \cup LP_{single_{length}} & \text{if } n_{addCount} < n_{count} \\ LP_{single_{move2}} \cup LP_{single_{add}} \cup LP_{single_{length}} & \text{otherwise} \end{cases} \\
& n_{addCount} = n_{arg} - 2 \\
& LP_{single_{move1}} = \bigcup_{i \in \{n_{moveStart}, \dots, n_{len} - 1\}} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \hat{s}_{from1}) \cup LP_{move1_1} \cup LP_{move1_2} \\
& LP_{move1_1} = \begin{cases} \widehat{\text{PropStore}}_{use/def}(\hat{H}, \hat{l}, \hat{s}_{to1}) & \text{if } \text{true} = \widehat{\text{HasProperty}}(\hat{H}, \hat{l}, \hat{s}_{from1}) \\ \{\} & \text{otherwise} \end{cases} \\
& LP_{move1_2} = \begin{cases} \widehat{\text{Delete}}_{use/def}(\hat{H}, \hat{l}, \hat{s}_{to1}) & \text{if } \text{false} = \widehat{\text{HasProperty}}(\hat{H}, \hat{l}, \hat{s}_{from1}) \\ \{\} & \text{otherwise} \end{cases} \\
& LP_{single_{move2}} = \bigcup_{i \in \{0, \dots, n_{len} - n_{moveStart} - 1\}} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \hat{s}_{from2}) \cup LP_{move2_1} \cup LP_{move2_2} \\
& LP_{move2_1} = \begin{cases} \widehat{\text{PropStore}}_{use/def}(\hat{H}, \hat{l}, \hat{s}_{to1}) & \text{if } \text{true} = \widehat{\text{HasProperty}}(\hat{H}, \hat{l}, \hat{s}_{from1}) \\ \{\} & \text{otherwise} \end{cases} \\
& LP_{move2_2} = \begin{cases} \widehat{\text{Delete}}_{use/def}(\hat{H}, \hat{l}, \hat{s}_{to1}) & \text{if } \text{false} = \widehat{\text{HasProperty}}(\hat{H}, \hat{l}, \hat{s}_{from1}) \\ \{\} & \text{otherwise} \end{cases} \\
& \hat{s}_{to1} = i - n_{count} + \hat{n}_{addCount} \\
& \hat{s}_{to2} = n_{len} - 1 - i - n_{count} + n_{addCount} \\
& \hat{s}_{from1} = \hat{i} \\
& \hat{s}_{from2} = n_{len} - \hat{i} - 1 \\
& LP_{single_{add}} = \bigcup_{i \in \{0, \dots, n_{addCount} - 1\}} \text{getArgValue}(\hat{H}, \hat{C}, i + \hat{s}_2) \cup \widehat{\text{PropStore}}_{use/def}(\hat{H}, \hat{l}, n_{start} + i) \\
& LP_{single_{delete}} = \bigcup_{i \in \{n_{newLen}, \dots, n_{len} - 1\}} \widehat{\text{Delete}}_{use}(\hat{H}, \hat{l}, i) \\
& LP_{single_{length}} = \widehat{\text{PropStore}}_{use}(\hat{H}, \hat{l}, \text{"length"}) \\
& n_{newLen} = n_{len} + n_{addCount} - n_{count} \\
& LP_{top} = \bigcup_{\hat{i} \in \hat{C}.2} LP_{len} \cup \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{topproto} \cup LP_{topstore} \cup LP_{topdelete} \cup LP_{topget} & \text{otherwise} \end{cases} \\
& \hat{n}_{len} = \widehat{\text{toUInt32}}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"})) \\
& LP_{len} = \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{"length"}) \\
& LP_{topproto} = \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{NumStr}) \\
& LP_{topstore} = \widehat{\text{PropStore}}_{use/def}(\hat{H}, \hat{l}, \text{NumStr}) \\
& LP_{topdelete} = \widehat{\text{Delete}}_{use/def}(\hat{H}, \hat{l}, \text{NumStr}) \\
& LP_{topget} = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{NumStr}) \\
& LP_4 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\hat{\mathcal{L}}_{use}[\text{BuiltintCall}(\text{"Array.prototype.unshift"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

$$\text{where } \hat{n}_{arg} = \widehat{\text{toUInt32}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"length"}))$$

$$LP_1 = \widehat{\text{getArgValue}}_{use}(\hat{H}, \hat{C}, \text{"length"}) \quad LP_2 = \begin{cases} \{\} & \text{if } \hat{n}_{arg} = \perp_{Number} \\ LP_{single} & \text{if } \hat{n}_{arg} = \text{UIntSingle}(n_{arg}) \\ LP_{top} & \text{otherwise} \end{cases}$$

$$\hat{n}_{len} = \widehat{\text{toUInt32}}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"}))$$

$$LP_{len} = \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{"length"})$$

$$LP_{single} = \bigcup_{i \in \hat{C}.2} LP_{len} \cup \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ LP_{unshift} \cup LP_{add} \cup LP_{singlelength} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n_{len}) \\ \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{NumStr}) \cup LP_{store} \cup LP_{delete} & \text{otherwise} \end{cases}$$

$$LP_{unshift} = \bigcup_{i \in \{0, \dots, n_{len}-1\}} LP_{unshift1} \cup LP_{unshift2}$$

$$LP_{unshift1} = \begin{cases} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \hat{s}_{from}) \cup \widehat{\text{PropStore}}_{use/def}(\hat{H}, \hat{l}, \hat{s}_{to}) & \text{if } \text{true} \sqsubseteq \widehat{\text{HasProperty}}(\hat{H}, \hat{l}, \hat{s}_{from}) \\ \{\} & \text{otherwise} \end{cases}$$

$$LP_{unshift2} = \begin{cases} \widehat{\text{Delete}}_{use/def}(\hat{H}, \hat{l}, \hat{s}_{to}) & \text{if } \text{true} \sqsubseteq \widehat{\text{HasProperty}}(\hat{H}, \hat{l}, \hat{s}_{from}) \\ \{\} & \text{otherwise} \end{cases}$$

$$\hat{s}_{to} = n_{len} - 1 - i + n_{arg}$$

$$LP_{add} = \bigcup_{i \in \{0, \dots, n_{arg}-1\}} \widehat{\text{getArgValue}}_{use}(\hat{H}, \hat{C}, i) \cup \widehat{\text{PropStore}}_{use/def}(\hat{H}, \hat{l}, i)$$

$$LP_{singlelength} = \widehat{\text{PropStore}}_{use/def}(\hat{H}, \hat{l}, \text{"length"})$$

$$LP_{delete} = \widehat{\text{Delete}}_{use/def}(\hat{H}, \hat{l}, \text{NumStr})$$

$$LP_{store} = \widehat{\text{PropStore}}_{use/def}(\hat{H}, \hat{l}, \text{NumStr})$$

$$LP_{top} = \bigcup_{i \in \hat{C}.2} LP_{len} \cup \begin{cases} \{\} & \text{if } \hat{n}_{len} = \perp_{Number} \\ \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{NumStr}) \cup LP_{store} \cup LP_{delete} & \text{otherwise} \end{cases}$$

$$LP_3 = \{ \langle \# \text{PureLocal}_R, @return \rangle \}$$

$$\hat{\mathcal{L}}_{use}[\text{BuiltintCall}(\text{"Array.prototype.indexOf"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

$$\text{where } \hat{n}_{arg} = \widehat{\text{toUInt32}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"length"}))$$

$$LP_1 = \widehat{\text{getArgValue}}_{use}(\hat{H}, \hat{C}, \text{"length"})$$

$$LP_2 = \begin{cases} LP_{search} \cup LP_{single} & \text{if } \hat{n}_{arg} = \text{UIntSingle}(n_{arg}) \\ \{\} & \text{otherwise} \end{cases}$$

$$\hat{v}_{search} = \widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"0"})$$

$$LP_{search} = \widehat{\text{getArgValue}}_{use}(\hat{H}, \hat{C}, \text{"0"})$$

$$LP_{single} = \bigcup_{i \in \hat{C}.2} LP_{len} \cup \begin{cases} LP_{start} \cup LP_{find} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n_{len}) \wedge n_{len} \neq 0 \\ \{\} & \text{otherwise} \end{cases}$$

$$\hat{n}_{len} = \widehat{\text{toUInt32}}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"}))$$

$$LP_{len} = \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{"length"})$$

$$\hat{n}_{start} = \begin{cases} \widehat{\text{toInteger}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"1"})) & \text{if } n_{arg} > 1 \\ \hat{0} & \text{otherwise} \end{cases}$$

$$LP_{start} = \begin{cases} \widehat{\text{getArgValue}}_{use}(\hat{H}, \hat{C}, \text{"1"}) & \text{if } n_{arg} > 1 \\ \hat{0} & \text{otherwise} \end{cases}$$

$$LP_{find} = \begin{cases} \bigcup_{i \in \{0, \dots, n_k-1\}} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, i) & \text{if } (\hat{n}_{start} = \text{UIntSingle}(n_{start}) \vee \hat{n}_{start} = \text{NUIntSingle}(n_{start})) \wedge n_{start} \\ \{\} & \text{otherwise} \end{cases}$$

$$n_k = \begin{cases} n_{len} - \text{abs}(n_{start}) & \text{if } n_{start} < 0 \\ n_{start} & \text{otherwise} \end{cases}$$

$$LP_3 = \{ \langle \# \text{PureLocal}_R, @return \rangle \}$$

$$\begin{aligned}
& \hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Array.prototype.lastIndexOf"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \text{where } \hat{n}_{arg} = \widehat{\text{toUInt32}}(\text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"length"})) \\
& LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"length"}) \\
& LP_2 = \begin{cases} LP_{search} \cup LP_{single} & \text{if } \hat{n}_{arg} = \text{UIntSingle}(n_{arg}) \\ \{\} & \text{otherwise} \end{cases} \\
& \hat{v}_{search} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& LP_{search} = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
& LP_{single} = \bigcup_{i \in \hat{C}.2} LP_{len} \cup \begin{cases} LP_{start} \cup LP_{find} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n_{len}) \wedge n_{len} \neq 0 \\ \{\} & \text{otherwise} \end{cases} \\
& \hat{n}_{len} = \widehat{\text{toUInt32}}(\widehat{\text{Proto}}(\hat{H}, \hat{l}, \text{"length"})) \\
& LP_{len} = \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, \text{"length"}) \\
& \hat{n}_{start} = \begin{cases} \widehat{\text{toInteger}}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"1"})) & \text{if } n_{arg} > 1 \\ \hat{0} & \text{otherwise} \end{cases} \\
& LP_{start} = \begin{cases} \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"1"}) & \text{if } n_{arg} > 1 \\ \hat{0} & \text{otherwise} \end{cases} \\
& LP_{find} = \begin{cases} \bigcup_{i \in \{0, \dots, n_k - 1\}} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, k - i) & \text{if } (\hat{n}_{start} = \text{UIntSingle}(n_{start}) \vee \hat{n}_{start} = \text{NUIntSingle}(n_{start})) \wedge n_s \\ \{\} & \text{otherwise} \end{cases} \\
& n_k = \begin{cases} \min(n_{start}, n_{len} - 1) & \text{if } n_{start} \geq 0 \\ n_{len} - \text{abs}(n_{start}) & \text{otherwise} \end{cases} \\
& LP_3 = \{ \langle \# \text{PureLocal}_R, @return \rangle \}
\end{aligned}$$

### 11.3.8 String

$$\hat{\mathcal{I}}_{def}[\![\text{BuiltinCall}(\text{"String"}, args)]\!](\hat{H}, \hat{C}) = LP_1$$

where  $LP_1 = \{ \langle \#PureLocal_R, @return \rangle \}$

$$\hat{\mathcal{I}}_{def}[\![\text{BuiltinCall}(\text{"String.constructor"}, args)]\!](\hat{H}, \hat{C}) = LP_1 \cup LP_2$$

where  $\hat{n}_{len} = \widehat{\text{toUInt32}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"length"}))$

$$\hat{s} = \begin{cases} \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"0"}))) & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \wedge n = 0 \\ \perp_{String} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \wedge n > 0 \\ \top_{String} & \text{if } \hat{n}_{len} = \perp_{Number} \\ & \text{otherwise} \end{cases}$$

$$LP_1 = \bigcup_{i \in \hat{C}.2} \bigcup_{s \in \widehat{\text{NewString}}_{def}(\hat{s})} \{ \langle \hat{l}, s \rangle \}$$

$$LP_2 = \{ \langle \#PureLocal_R, @return \rangle \}$$

$$\hat{\mathcal{I}}_{def}[\![\text{BuiltinCall}(\text{"String.fromCharCode"}, args)]\!](\hat{H}, \hat{C}) = LP_1$$

where  $LP_1 = \{ \langle \#PureLocal_R, @return \rangle \}$

$$\hat{\mathcal{I}}_{use}[\![\text{BuiltinCall}(\text{"String"}, args)]\!](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

where  $\hat{n}_{len} = \widehat{\text{toUInt32}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"length"}))$

$$LP_1 = \widehat{\text{getArgValue}}_{use}(\hat{H}, \hat{C}, \text{"length"})$$

$$LP_2 = \begin{cases} \{ \} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \wedge n == 0 \\ \widehat{\text{getArgValue}}_{use}(\hat{H}, \hat{C}, \text{"0"}) & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \wedge n > 0 \\ \widehat{\text{getArgValue}}_{use}(\hat{H}, \hat{C}, \text{"0"}) & \text{if } \text{UInt} \sqsubseteq \hat{n}_{len} \\ \{ \} & \text{otherwise} \end{cases}$$

$$LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}$$

$$\hat{\mathcal{I}}_{use}[\![\text{BuiltinCall}(\text{"String.constructor"}, args)]\!](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4$$

where  $\hat{n}_{len} = \widehat{\text{toUInt32}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"length"}))$

$$LP_1 = \widehat{\text{getArgValue}}_{use}(\hat{H}, \hat{C}, \text{"length"})$$

$$LP_2 = \begin{cases} \widehat{\text{getArgValue}}_{use}(\hat{H}, \hat{C}, \text{"0"}) & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \wedge n > 0 \\ \{ \} & \text{otherwise} \end{cases}$$

$$\hat{s} = \begin{cases} \widehat{\text{toString}}(\widehat{\text{toPrimitive}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"0"}))) & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \wedge n = 0 \\ \perp_{String} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \wedge n > 0 \\ \top_{String} & \text{if } \hat{n}_{len} = \perp_{Number} \\ & \text{otherwise} \end{cases}$$

$$LP_3 = \bigcup_{i \in \hat{C}.2} \bigcup_{s \in \widehat{\text{NewString}}_{def}(\hat{s})} \{ \langle \hat{l}, s \rangle \}$$

$$LP_4 = \{ \langle \#PureLocal_R, @return \rangle \}$$

$$\hat{\mathcal{I}}_{use}[\![\text{BuiltinCall}(\text{"String.fromCharCode"}, args)]\!](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

where  $\hat{n}_{len} = \widehat{\text{toUInt32}}(\widehat{\text{getArgValue}}(\hat{H}, \hat{C}, \text{"length"}))$

$$LP_1 = \widehat{\text{getArgValue}}_{use}(\hat{H}, \hat{C}, \text{"length"})$$

$$LP_2 = \begin{cases} \bigcup_{i \in \{0, \dots, n-1\}} \widehat{\text{getArgValue}}_{use}(\hat{H}, \hat{C}, i) & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \\ \widehat{\text{getArgValue}}_{use}(\hat{H}, \hat{C}, \text{NumStr}) & \text{if } \text{UInt} \sqsubseteq \hat{n}_{len} \\ \{ \} & \text{otherwise} \end{cases}$$

$$LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}$$

### 11.3.9 String.prototype

$$\begin{aligned}
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"String.prototype.toString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"String.prototype.valueOf"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } \hat{e}s = \begin{cases} \{\text{TypeError}\} & \text{if } \exists \hat{l} \in \hat{C}.2 : \hat{H}(\hat{l})(@class).1.2.1.5 \neq \text{"String"} \\ \{\} & \text{otherwise} \end{cases} \\
& LP_1 = \widehat{\text{RaiseException}}_{def}(\hat{e}s) \\
& LP_2 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"String.prototype.charAt"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"String.prototype.charCodeAt"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"String.prototype.concat"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"String.prototype.indexOf"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"String.prototype.lastIndexOf"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"String.prototype.localeCompare"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"String.prototype.slice"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"String.prototype.substring"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"String.prototype.toLowerCase"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"String.prototype.toLocaleLowerCase"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"String.prototype.toUpperCase"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"String.prototype.toLocaleUpperCase"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"String.prototype.trim"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \text{where } LP_1 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"String.prototype.toString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4$$

$$\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"String.prototype.valueOf"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4$$

$$\text{where } \hat{e}s = \begin{cases} \{\text{TypeError}\} & \text{if } \exists \hat{l} \in \hat{C}.2 : \hat{H}(\hat{l})(\text{@class}).1.2.1.5 \neq \text{"String"} \\ \{\} & \text{otherwise} \end{cases}$$

$$LP_1 = \bigcup_{\hat{l} \in \hat{C}.2} \{ \langle \hat{l}, \text{@class} \rangle \}$$

$$\hat{L}_{string} = \{ \hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \hat{H}(\hat{l})(\text{@class}).1.2.1.5 = \text{"String"} \}$$

$$LP_2 = \bigcup_{\hat{l} \in \hat{L}_{string}} \{ \langle \hat{l}, \text{@primitive} \rangle \}$$

$$LP_3 = \text{RaiseException}_{use}(\hat{e}s)$$

$$LP_4 = \{ \langle \# \text{PureLocal}_R, \text{@return} \rangle \}$$

$$\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"String.prototype.charAt"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

$$\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"String.prototype.charCodeAtAt"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

$$\text{where } LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"length"})$$

$$LP_2 = \bigcup_{\hat{l} \in \hat{C}.2} \{ \langle \hat{l}, \text{@primitive} \rangle \}$$

$$LP_3 = \{ \langle \# \text{PureLocal}_R, \text{@return} \rangle \}$$

$$\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"String.prototype.concat"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4$$

$$\text{where } \hat{n}_{len} = \text{toUInt32}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"length"}))$$

$$LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"length"})$$

$$LP_2 = \bigcup_{\hat{l} \in \hat{C}.2} \{ \langle \hat{l}, \text{@primitive} \rangle \}$$

$$LP_3 = \begin{cases} \{\} & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \wedge n = 0 \\ \bigcup_{i \in \{0, \dots, n-1\}} \text{getArgValue}_{use}(\hat{H}, \hat{C}, i) & \text{if } \hat{n}_{len} = \text{UIntSingle}(n) \wedge n > 0 \\ \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{NumStr}) & \text{if } \text{UInt} \sqsubseteq \hat{n}_{len} \\ \{\} & \text{otherwise} \end{cases}$$

$$LP_4 = \{ \langle \# \text{PureLocal}_R, \text{@return} \rangle \}$$

$$\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"String.prototype.localeCompare"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1$$

$$\text{where } LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"})$$

$$LP_2 = \bigcup_{\hat{l} \in \hat{C}.2} \{ \langle \hat{l}, \text{@primitive} \rangle \}$$

$$LP_3 = \{ \langle \# \text{PureLocal}_R, \text{@return} \rangle \}$$

$$\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"String.prototype.indexOf"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

$$\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"String.prototype.lastIndexOf"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

$$\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"String.prototype.slice"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

$$\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"String.prototype.substring"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

$$\text{where } LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \cup \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"1"})$$

$$LP_2 = \bigcup_{\hat{l} \in \hat{C}.2} \{ \langle \hat{l}, \text{@primitive} \rangle \}$$

$$LP_3 = \{ \langle \# \text{PureLocal}_R, \text{@return} \rangle \}$$

$$\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"String.prototype.toLowerCase"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2$$

$$\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"String.prototype.toLocaleLowerCase"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2$$

$$\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"String.prototype.toUpperCase"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2$$

$$\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"String.prototype.toLocaleUpperCase"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2$$

$$\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"String.prototype.trim"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2$$

$$\text{where } LP_1 = \bigcup_{\hat{l} \in \hat{C}.2} \{ \langle \hat{l}, \text{@primitive} \rangle \}$$

$$LP_2 = \{ \langle \# \text{PureLocal}_R, \text{@return} \rangle \}$$



### 11.3.10 Boolean

$$\begin{aligned}
& \hat{I}_{def} \llbracket \text{BuiltinCall}(\text{"Boolean"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \text{where } LP_1 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{I}_{def} \llbracket \text{BuiltinCall}(\text{"Boolean.constructor"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } LP_1 = \bigcup_{i \in \hat{C}.2} \bigcup_{s \in \widehat{NewBoolean}_{def}} \{ \langle \hat{l}, s \rangle \} \\
& \quad LP_2 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{I}_{use} \llbracket \text{BuiltinCall}(\text{"Boolean"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \\
& \text{where } LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
& \quad LP_2 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"length"}) \\
& \quad LP_3 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{I}_{use} \llbracket \text{BuiltinCall}(\text{"Boolean.constructor"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\
& \text{where } LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
& \quad LP_2 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"length"}) \\
& \quad LP_3 = \bigcup_{i \in \hat{C}.2} \bigcup_{s \in \widehat{NewBoolean}_{def}} \{ \langle \hat{l}, s \rangle \} \\
& \quad LP_4 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

### 11.3.11 Boolean.prototype

$$\begin{aligned}
& \hat{I}_{def} \llbracket \text{BuiltinCall}(\text{"Boolean.prototype.toString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \hat{I}_{def} \llbracket \text{BuiltinCall}(\text{"Boolean.prototype.valueOf"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } \hat{e}s = \begin{cases} \{ \text{TypeError} \} & \text{if } \exists \hat{l} \in \hat{C}.2 : \hat{H}(\hat{l})(@class).1.2.1.5 \neq \text{"Boolean"} \\ \{ \} & \text{otherwise} \end{cases} \\
& \quad LP_1 = \widehat{RaiseException}_{def}(\hat{e}s) \\
& \quad LP_2 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{I}_{use} \llbracket \text{BuiltinCall}(\text{"Boolean.prototype.toString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\
& \hat{I}_{use} \llbracket \text{BuiltinCall}(\text{"Boolean.prototype.valueOf"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\
& \text{where } LP_1 = \bigcup_{i \in \hat{C}.2} \{ \langle \hat{l}, @class \rangle \} \\
& \quad \hat{e}s = \begin{cases} \{ \text{TypeError} \} & \text{if } \exists \hat{l} \in \hat{C}.2 : \hat{H}(\hat{l})(@class).1.2.1.5 \neq \text{"Boolean"} \\ \{ \} & \text{otherwise} \end{cases} \\
& \quad LP_2 = \widehat{RaiseException}_{use}(\hat{e}s) \\
& \quad \hat{L}_{bool} = \{ \hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \hat{H}(\hat{l})(@class).1.2.1.5 = \text{"Boolean"} \} \\
& \quad LP_3 = \bigcup_{i \in \hat{L}_{bool}} \{ \langle \hat{l}, @primitive \rangle \} \\
& \quad LP_4 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

### 11.3.12 Number

$$\hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Number"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1$$

where  $LP_1 = \{ \langle \#PureLocal_R, @return \rangle \}$

$$\hat{\mathcal{I}}_{def} \llbracket \text{BuiltinCall}(\text{"Number.constructor"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2$$

where  $LP_1 = \bigcup_{i \in \hat{C}.2} \bigcup_{s \in \widehat{NewNumber}_{def}} \{ \langle \hat{l}, s \rangle \}$   
 $LP_2 = \{ \langle \#PureLocal_R, @return \rangle \}$

$$\hat{\mathcal{I}}_{use} \llbracket \text{BuiltinCall}(\text{"Number"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

where  $LP_1 = getArgValue_{use}(\hat{H}, \hat{C}, \text{"0"})$   
 $LP_2 = getArgValue_{use}(\hat{H}, \hat{C}, \text{"length"})$   
 $LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}$

$$\hat{\mathcal{I}}_{use} \llbracket \text{BuiltinCall}(\text{"Number.constructor"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4$$

where  $LP_1 = getArgValue_{use}(\hat{H}, \hat{C}, \text{"0"})$   
 $LP_2 = getArgValue_{use}(\hat{H}, \hat{C}, \text{"length"})$   
 $LP_3 = \bigcup_{i \in \hat{C}.2} \bigcup_{s \in \widehat{NewNumber}_{def}} \{ \langle \hat{l}, s \rangle \}$   
 $LP_4 = \{ \langle \#PureLocal_R, @return \rangle \}$

### 11.3.13 Number.prototype

$$\begin{aligned}
& \hat{I}_{def} \llbracket \text{BuiltintCall}(\text{"Number.prototype.toString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } \hat{n}_{arglen} = \widehat{\text{ToUint32}}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"length"})) \\
& \quad \hat{v}_1 = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& \quad \hat{e}s_1 = \begin{cases} \{\text{TypeError}\} & \text{if } \exists \hat{l} \in \hat{C}.2 : \hat{H}(\hat{l})(\text{@class}).1.2.1.5 \neq \text{"Number"} \\ \{\} & \text{otherwise} \end{cases} \\
& \quad \hat{e}s_2 = \begin{cases} \{\} & \text{if } \hat{n}_{arglen} = \text{UIntSingle}(n) \wedge n = 0 \\ \{\text{RangeError}\} & \text{if } \hat{n}_{arglen} = \text{UIntSingle}(n) \wedge n > 0 \wedge (\text{true} \sqsubseteq \hat{v}_1 \hat{<} 2 \vee \text{true} \sqsubseteq \hat{v}_1 \hat{>} 36) \\ \{\} & \text{if } \hat{n}_{arglen} = \text{UIntSingle}(n) \wedge n > 0 \wedge \text{false} \sqsubseteq \hat{v}_1 \hat{<} 2 \wedge \text{false} \sqsubseteq \hat{v}_1 \hat{>} 36 \\ \{\} & \text{if } \hat{n}_{arglen} = \perp_{\text{number}} \\ \{\text{RangeError}\} & \text{otherwise} \end{cases} \\
& \quad LP_1 = \widehat{\text{RaiseException}}_{def}(\hat{e}s_1 \sqcup \hat{e}s_2) \\
& \quad LP_2 = \{ \langle \# \text{PureLocal}_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
& \hat{I}_{def} \llbracket \text{BuiltintCall}(\text{"Number.prototype.toLocaleString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \text{where } LP_1 = \{ \langle \# \text{PureLocal}_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
& \hat{I}_{def} \llbracket \text{BuiltintCall}(\text{"Number.prototype.valueOf"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } \hat{e}s = \begin{cases} \{\text{TypeError}\} & \text{if } \exists \hat{l} \in \hat{C}.2 : \hat{H}(\hat{l})(\text{@class}).1.2.1.5 \neq \text{"Number"} \\ \{\} & \text{otherwise} \end{cases} \\
& \quad LP_1 = \widehat{\text{RaiseException}}_{def}(\hat{e}s) \\
& \quad LP_2 = \{ \langle \# \text{PureLocal}_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
& \hat{I}_{def} \llbracket \text{BuiltintCall}(\text{"Number.prototype.toFixed"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } \hat{v}_1 = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& \quad \hat{v}_2 = \begin{cases} \text{Value}(\text{PValue}(\hat{v}_1.1.1, \hat{v}_1.1.2, \hat{v}_1.1.3, \hat{0} \sqcup \hat{v}_1.1.4, \hat{v}_1.1.5), \hat{v}_1.2) & \text{if } \top_{U_{undef}} \sqsubseteq \hat{v}_1.1 \\ \hat{v}_1 & \text{otherwise} \end{cases} \\
& \quad \hat{e}s = \begin{cases} \{\text{RangeError}\} & \text{if } \text{true} \sqsubseteq \hat{v}_2 \hat{<} \hat{0} \vee \text{true} \sqsubseteq \hat{v}_2 \hat{>} \hat{0} \\ \{\} & \text{otherwise} \end{cases} \\
& \quad LP_1 = \widehat{\text{RaiseException}}_{def}(\hat{e}s) \\
& \quad LP_2 = \{ \langle \# \text{PureLocal}_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
& \hat{I}_{def} \llbracket \text{BuiltintCall}(\text{"Number.prototype.toExponential"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } \hat{v}_1 = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& \quad \hat{v}_2 = \begin{cases} \text{Value}(\text{PValue}(\hat{v}_1.1.1, \hat{v}_1.1.2, \hat{v}_1.1.3, \hat{v}_1.1.4, \hat{v}_1.1.5), \hat{v}_1.2) & \text{if } \top_{U_{undef}} \sqsubseteq \hat{v}_1.1 \\ \hat{v}_1 & \text{otherwise} \end{cases} \\
& \quad \hat{e}s = \begin{cases} \{\text{RangeError}\} & \text{if } \text{true} \sqsubseteq \hat{v}_2 \hat{<} \hat{0} \vee \text{true} \sqsubseteq \hat{v}_2 \hat{>} \hat{0} \\ \{\} & \text{otherwise} \end{cases} \\
& \quad LP_1 = \widehat{\text{RaiseException}}_{def}(\hat{e}s) \\
& \quad LP_2 = \{ \langle \# \text{PureLocal}_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
& \hat{I}_{def} \llbracket \text{BuiltintCall}(\text{"Number.prototype.toPrecision"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } \hat{v}_1 = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& \quad \hat{v}_2 = \begin{cases} \text{Value}(\text{PValue}(\hat{v}_1.1.1, \hat{v}_1.1.2, \hat{v}_1.1.3, \hat{v}_1.1.4, \hat{v}_1.1.5), \hat{v}_1.2) & \text{if } \top_{U_{undef}} \sqsubseteq \hat{v}_1.1 \\ \hat{v}_1 & \text{otherwise} \end{cases} \\
& \quad \hat{e}s = \begin{cases} \{\text{RangeError}\} & \text{if } \text{true} \sqsubseteq \hat{v}_2 \hat{<} \hat{1} \vee \text{true} \sqsubseteq \hat{v}_2 \hat{>} \hat{1} \\ \{\} & \text{otherwise} \end{cases} \\
& \quad LP_1 = \widehat{\text{RaiseException}}_{def}(\hat{e}s) \\
& \quad LP_2 = \{ \langle \# \text{PureLocal}_R, @return \rangle \}
\end{aligned}$$

$$\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Number.prototype.toString"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \cup LP_5 \cup LP_6$$

$$\text{where } \hat{n}_{arglen} = \widehat{\text{ToUint32}}(\text{getArgValue}(\hat{H}, \hat{C}, \text{"length"}))$$

$$LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"length"})$$

$$\hat{v}_1 = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"})$$

$$\hat{es}_1 = \begin{cases} \{\text{TypeError}\} & \text{if } \exists \hat{l} \in \hat{C}.2 : \hat{H}(\hat{l})(\text{@class}).1.2.1.5 \neq \text{"Number"} \\ \{\} & \text{otherwise} \end{cases}$$

$$LP_2 = \bigcup_{\hat{l} \in \hat{C}.2} \{ \langle \hat{l}, \text{@class} \rangle \}$$

$$\hat{L}_{num} = \{ \hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \hat{H}(\hat{l})(\text{@class}).1.2.1.5 = \text{"Number"} \}$$

$$LP_3 = \bigcup_{\hat{l} \in \hat{L}_{number}} \{ \langle \hat{l}, \text{@primitive} \rangle \}$$

$$\hat{(es_2, LP_4)} = \begin{cases} (\{\}, \{\}) & \text{if } \hat{n}_{arglen} = \text{Uintsingle}(n) \wedge n = 0 \\ (\{\text{RangeError}\}, \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"})) & \text{if } \hat{n}_{arglen} = \text{Uintsingle}(n) \wedge n > 0 \wedge (\text{true} \sqsubseteq \hat{v}_1 \hat{<} \hat{2} \vee \text{true} \sqsubseteq \hat{v}_1 \hat{>} \hat{2}) \\ (\{\}, \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"})) & \text{if } \hat{n}_{arglen} = \text{Uintsingle}(n) \wedge n > 0 \wedge \text{false} \sqsubseteq \hat{v}_1 \hat{<} \hat{2} \wedge \text{false} \sqsubseteq \hat{v}_1 \hat{>} \hat{2} \\ (\{\}, \{\}) & \text{if } \hat{n}_{arglen} = \perp_{number} \\ (\{\text{RangeError}\}, \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"})) & \text{otherwise} \end{cases}$$

$$LP_5 = \widehat{\text{RaiseException}}_{use}(\hat{es}_1 \sqcup \hat{es}_2)$$

$$LP_6 = \{ \langle \# \text{PureLocal}_R, \text{@return} \rangle \}$$

$$\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Number.prototype.toLocaleString"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

$$\text{where } LP_1 = \bigcup_{\hat{l} \in \hat{C}.2} \{ \langle \hat{l}, \text{@primitive} \rangle \}$$

$$LP_2 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"length"})$$

$$LP_3 = \{ \langle \# \text{PureLocal}_R, \text{@return} \rangle \}$$

$$\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Number.prototype.valueOf"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4$$

$$\text{where } \hat{es} = \begin{cases} \{\text{TypeError}\} & \text{if } \exists \hat{l} \in \hat{C}.2 : \hat{H}(\hat{l})(\text{@class}).1.2.1.5 \neq \text{"Number"} \\ \{\} & \text{otherwise} \end{cases}$$

$$\hat{L}_{num} = \{ \hat{l} \mid \hat{l} \in \hat{C}.2 \wedge \hat{H}(\hat{l})(\text{@class}).1.2.1.5 = \text{"Number"} \}$$

$$LP_1 = \bigcup_{\hat{l} \in \hat{C}.2} \{ \langle \hat{l}, \text{@class} \rangle \}$$

$$LP_2 = \bigcup_{\hat{l} \in \hat{L}_{number}} \{ \langle \hat{l}, \text{@primitive} \rangle \}$$

$$LP_3 = \widehat{\text{RaiseException}}_{use}(\hat{es})$$

$$LP_4 = \{ \langle \# \text{PureLocal}_R, \text{@return} \rangle \}$$

$$\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Number.prototype.toFixed"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

$$\text{where } \hat{v}_1 = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"})$$

$$LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"})$$

$$\hat{v}_2 = \begin{cases} \text{Value}(\text{PValue}(\hat{v}_1.1.1, \hat{v}_1.1.2, \hat{v}_1.1.3, \hat{0} \sqcup \hat{v}_1.1.4, \hat{v}_1.1.5), \hat{v}_1.2) & \text{if } \top_{Undef} \sqsubseteq \hat{v}_1.1 \\ \hat{v}_1 & \text{otherwise} \end{cases}$$

$$\hat{es} = \begin{cases} \{\text{RangeError}\} & \text{if } \text{true} \sqsubseteq \hat{v}_2 \hat{<} \hat{0} \vee \text{true} \sqsubseteq \hat{v}_2 \hat{>} \hat{20} \\ \{\} & \text{otherwise} \end{cases}$$

$$LP_2 = \widehat{\text{RaiseException}}_{use}(\hat{es})$$

$$LP_3 = \{ \langle \# \text{PureLocal}_R, \text{@return} \rangle \}$$

$$\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Number.prototype.toExponential"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

$$\text{where } \hat{v}_1 = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"})$$

$$LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"})$$

$$\hat{v}_2 = \begin{cases} \text{Value}(\text{PValue}(\hat{v}_1.1.1, \hat{v}_1.1.2, \hat{v}_1.1.3, \hat{v}_1.1.4, \hat{v}_1.1.5), \hat{v}_1.2) & \text{if } \top_{Undef} \sqsubseteq \hat{v}_1.1 \\ \hat{v}_1 & \text{otherwise} \end{cases}$$

$$\hat{es} = \begin{cases} \{\text{RangeError}\} & \text{if } \text{true} \sqsubseteq \hat{v}_2 \hat{<} \hat{1} \vee \text{true} \sqsubseteq \hat{v}_2 \hat{>} \hat{21} \\ \{\} & \text{otherwise} \end{cases}$$

$$LP_2 = \widehat{\text{RaiseException}}_{use}(\hat{es})$$

$$LP_3 = \{ \langle \# \text{PureLocal}_R, \text{@return} \rangle \}$$

$$\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Number.prototype.toPrecision"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3$$

$$\text{where } \hat{v}_1 = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"})$$

$$LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"})$$

$$\hat{v}_2 = \begin{cases} \text{Value}(\text{PValue}(\hat{v}_1.1.1, \hat{v}_1.1.2, \hat{v}_1.1.3, \hat{v}_1.1.4, \hat{v}_1.1.5), \hat{v}_1.2) & \text{if } \top_{Undef} \sqsubseteq \hat{v}_1.1 \\ \hat{v}_1 & \text{otherwise} \end{cases}$$

$$\hat{es} = \begin{cases} \{\text{RangeError}\} & \text{if } \text{true} \sqsubseteq \hat{v}_2 \hat{<} \hat{1} \vee \text{true} \sqsubseteq \hat{v}_2 \hat{>} \hat{21} \\ \{\} & \text{otherwise} \end{cases}$$

$$LP_2 = \widehat{\text{RaiseException}}_{use}(\hat{es})$$

$$LP_3 = \{ \langle \# \text{PureLocal}_R, \text{@return} \rangle \}$$

### 11.3.14 Math

$$\begin{aligned}
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.abs"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.acos"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.asin"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.atan"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.atan2"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.ceil"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.cos"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.exp"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.floor"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.max"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.min"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.pow"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.log"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.random"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.round"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.sin"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.sqrt"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"Math.tan"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\text{where } LP_1 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.random"}, args)](\hat{H}, \hat{C}) = LP_1 \\
&\text{where } LP_1 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.abs"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.acos"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.asin"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.atan"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.ceil"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.cos"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.exp"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.floor"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.log"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.round"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.sin"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.sqrt"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.tan"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
&\text{where } LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \wedge LP_2 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.atan2"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \\
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.pow"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \\
&\text{where } LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \wedge LP_2 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"1"}) \\
&\quad \wedge LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

$$\begin{aligned}
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.max"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \\
&\hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"Math.min"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \\
&\text{where } \hat{n} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"length"}) \\
&\quad LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"length"}) \\
&\quad LP_2 = \begin{cases} \bigsqcup_{i \in \{0, \dots, n-1\}} \text{getArgValue}_{use}(\hat{H}, \hat{C}, i) & \text{if } \hat{n} = \text{UIntSingle}(n) \\ \{\} & \text{otherwise} \end{cases} \\
&\quad LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

### 11.3.15 Date

$$\begin{aligned}
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \text{where } LP_1 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.constructor"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } LP_1 = \bigcup_{i \in \hat{C}.2} \bigcup_{s \in \widehat{NewDate}_{def}} \{ \langle \hat{l}, s \rangle \} \\
& \quad LP_2 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.now"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \text{where } LP_1 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \text{where } LP_1 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.constructor"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \cup LP_4 \\
& \text{where } LP_1 = getArgValue_{use}(\hat{H}, \hat{C}, \text{"length"}) \\
& \quad LP_2 = getArgValue_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
& \quad LP_3 = \bigcup_{i \in \hat{C}.2} \bigcup_{s \in \widehat{NewDate}_{def}} \{ \langle \hat{l}, s \rangle \} \\
& \quad LP_4 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.now"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \text{where } LP_1 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

### 11.3.16 Date.prototype

$$\begin{aligned}
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toDateString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toTimeString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toLocaleString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toLocaleDateString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toLocaleTimeString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toUTCString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.toISOString"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.valueOf"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getTime"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getFullYear"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getMonth"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getDate"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getDay"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getHours"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getMinutes"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getSeconds"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getMilliseconds"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getTimezoneOffset"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getUTCFullYear"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getUTCMonth"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getUTCDate"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getUTCDay"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getUTCHours"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getUTCMinutes"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getUTCSeconds"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getUTCMilliseconds"}, args) \rrbracket (\hat{H}, \hat{C}) = LP_1 \\
& \text{where } LP_1 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$



$$\begin{aligned}
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.prototype.valueOf"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.prototype.getTime"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setTime"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setMilliseconds"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setSeconds"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setMinutes"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setHours"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setDate"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setMonth"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setFullYear"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setUTCMilliseconds"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setUTCSeconds"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setUTCMinutes"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setUTCHours"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setUTCDate"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setUTCMonth"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Date.prototype.setUTCFullYear"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\text{where } LP_1 &= \bigcup_{i \in \hat{C}.2} \{ \langle \hat{l}, @primitive \rangle \} \\
LP_2 &= \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

### 11.3.17 RegExp

### 11.3.18 RegExp.prototype

### 11.3.19 Error

$$\begin{aligned}
\hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Error.constructor"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \\
\text{where } \hat{v} &= \text{getArgValue}(\hat{H}, \hat{C}, "0") \\
LP_1 &= \begin{cases} \{ \langle \#ErrorLoc_O, "message" \rangle \} & \text{if } \hat{v}.1.1 \not\models \perp_{Undef} \\ \{ \} & \text{otherwise} \end{cases} \\
LP_2 &= \{ \langle \#PureLocal_R, @return \rangle \} \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Error.constructor"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \\
\text{where } LP_1 &= \text{getArgValue}_{use}(\hat{H}, \hat{C}, "0") \\
LP_2 &= \begin{cases} \{ \langle \#ErrorLoc_O, "message" \rangle \} & \text{if } \hat{v}.1.1 \not\models \perp_{Undef} \\ \{ \} & \text{otherwise} \end{cases} \\
LP_3 &= \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

### 11.3.20 Error.prototype

$$\begin{aligned}
\hat{\mathcal{I}}_{def} \llbracket \text{BuiltintCall}(\text{"Error.prototype.toString"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \\
\text{where } LP_1 &= \{ \langle \#PureLocal_R, @return \rangle \} \\
\hat{\mathcal{I}}_{use} \llbracket \text{BuiltintCall}(\text{"Error.prototype.toString"}, args) \rrbracket (\hat{H}, \hat{C}) &= LP_1 \cup LP_2 \cup LP_3 \\
\text{where } LP_1 &= \bigsqcup_{i \in \hat{C}.2} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, "name") \\
LP_2 &= \bigsqcup_{i \in \hat{C}.2} \widehat{\text{Proto}}_{use}(\hat{H}, \hat{l}, "message") \\
LP_3 &= \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$



### 11.3.21 EvalError

$$\begin{aligned}
& \hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"EvalError.constructor"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } \hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& LP_1 = \begin{cases} \{ \langle \#EvalErrorLoc_O, \text{"message"} \rangle \} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \\ \{ \} & \text{otherwise} \end{cases} \\
& LP_2 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"EvalError.constructor"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \\
& \text{where } LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
& \hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& LP_2 = \begin{cases} \{ \langle \#EvalErrorLoc_O, \text{"message"} \rangle \} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \\ \{ \} & \text{otherwise} \end{cases} \\
& LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

### 11.3.22 RangeError

$$\begin{aligned}
& \hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"RangeError.constructor"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } \hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& LP_1 = \begin{cases} \{ \langle \#RangeErrorLoc_O, \text{"message"} \rangle \} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \\ \{ \} & \text{otherwise} \end{cases} \\
& LP_2 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"RangeError.constructor"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \\
& \text{where } LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
& \hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& LP_2 = \begin{cases} \{ \langle \#RangeErrorLoc_O, \text{"message"} \rangle \} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \\ \{ \} & \text{otherwise} \end{cases} \\
& LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

### 11.3.23 ReferenceError

$$\begin{aligned}
& \hat{\mathcal{I}}_{def}[\text{BuiltinCall}(\text{"ReferenceError.constructor"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } \hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& LP_1 = \begin{cases} \{ \langle \#RefErrorLoc_O, \text{"message"} \rangle \} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \\ \{ \} & \text{otherwise} \end{cases} \\
& LP_2 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{use}[\text{BuiltinCall}(\text{"ReferenceError.constructor"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \\
& \text{where } LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
& \hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& LP_2 = \begin{cases} \{ \langle \#RefErrorLoc_O, \text{"message"} \rangle \} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \\ \{ \} & \text{otherwise} \end{cases} \\
& LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

### 11.3.24 SyntaxError

$$\begin{aligned}
& \hat{\mathcal{I}}_{def}[\text{BuiltintCall}(\text{"SyntaxError.constructor"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } \hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& LP_1 = \begin{cases} \{ \langle \#SyntaxErrorLoc_O, \text{"message"} \rangle \} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \\ \{ \} & \text{otherwise} \end{cases} \\
& LP_2 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{use}[\text{BuiltintCall}(\text{"SyntaxError.constructor"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \\
& \text{where } LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
& \hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& LP_2 = \begin{cases} \{ \langle \#SyntaxErrorLoc_O, \text{"message"} \rangle \} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \\ \{ \} & \text{otherwise} \end{cases} \\
& LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

### 11.3.25 TypeError

$$\begin{aligned}
& \hat{\mathcal{I}}_{def}[\text{BuiltintCall}(\text{"TypeError.constructor"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } \hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& LP_1 = \begin{cases} \{ \langle \#TypeErrorLoc_O, \text{"message"} \rangle \} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \\ \{ \} & \text{otherwise} \end{cases} \\
& LP_2 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{use}[\text{BuiltintCall}(\text{"TypeError.constructor"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \\
& \text{where } LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
& \hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& LP_2 = \begin{cases} \{ \langle \#TypeErrorLoc_O, \text{"message"} \rangle \} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \\ \{ \} & \text{otherwise} \end{cases} \\
& LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

### 11.3.26 URIError

$$\begin{aligned}
& \hat{\mathcal{I}}_{def}[\text{BuiltintCall}(\text{"URIError.constructor"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \cup LP_3 \\
& \text{where } \hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& LP_1 = \begin{cases} \{ \langle \#URIErrorLoc_O, \text{"message"} \rangle \} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \\ \{ \} & \text{otherwise} \end{cases} \\
& LP_2 = \{ \langle \#PureLocal_R, @return \rangle \} \\
\\
& \hat{\mathcal{I}}_{use}[\text{BuiltintCall}(\text{"URIError.constructor"}, args)](\hat{H}, \hat{C}) = LP_1 \cup LP_2 \\
& \text{where } LP_1 = \text{getArgValue}_{use}(\hat{H}, \hat{C}, \text{"0"}) \\
& \hat{v} = \text{getArgValue}(\hat{H}, \hat{C}, \text{"0"}) \\
& LP_2 = \begin{cases} \{ \langle \#URIErrorLoc_O, \text{"message"} \rangle \} & \text{if } \hat{v}.1.1 \not\sqsubseteq \perp_{Undef} \\ \{ \} & \text{otherwise} \end{cases} \\
& LP_3 = \{ \langle \#PureLocal_R, @return \rangle \}
\end{aligned}$$

### 11.3.27 JSON

$$\hat{\mathcal{I}}_{def}[\![\text{BuiltintCall}(\text{"JSON.parse"}, args)]\!](\hat{H}, \hat{C}) = LP_1$$

where  $LP_1 = \{ \langle \#PureLocal_R, @return \rangle \}$

$$\hat{\mathcal{I}}_{def}[\![\text{BuiltintCall}(\text{"JSON.stringify"}, args)]\!](\hat{H}, \hat{C}) = LP_1$$

where  $LP_1 = \{ \langle \#PureLocal_R, @return \rangle \}$

$$\hat{\mathcal{I}}_{use}[\![\text{BuiltintCall}(\text{"JSON.parse"}, args)]\!](\hat{H}, \hat{C}) = LP_1$$

where  $LP_1 = \{ \langle \#PureLocal_R, @return \rangle \}$

$$\hat{\mathcal{I}}_{use}[\![\text{BuiltintCall}(\text{"JSON.stringify"}, args)]\!](\hat{H}, \hat{C}) = LP_1$$

where  $LP_1 = \{ \langle \#PureLocal_R, @return \rangle \}$