

# BasicIntroduction

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## 0.1 An Introduction to Basic Julia

This quick introduction assumes that you have basic knowledge of some scripting language and provides an example of the Julia syntax. So before we explain anything, let's just treat it like a scripting language, take a head-first dive into Julia, and see what happens.

You'll notice that, given the right syntax, almost everything will "just work". There will be some peculiarities, and these we will be the facts which we will study in much more depth. Usually, these oddities/differences from other scripting languages are "the source of Julia's power".

### 0.1.1 Array Syntax

The array syntax is similar to MATLAB's conventions.

```
In [11]: a = Vector{Float64}(5) # Create a length 5 Vector (dimension 1 array) of Float64's

a = [1;2;3;4;5] # Create the column vector [1 2 3 4 5]

a = [1 2 3 4] # Create the row vector [1 2 3 4]

a[3] = 2 # Change the third element of a (using linear indexing) to 2

b = Matrix{Float64}(4,2) # Define a Matrix of Float64's of size (4,2)

c = Array{Float64,4}((4,5,6,7)) # Define a (4,5,6,7) array of Float64's

mat = [1 2 3 4
        3 4 5 6
        4 4 4 6
        3 3 3 3] #Define the matrix inline

mat[1,2] = 4 # Set element (1,2) (row 1, column 2) to 4

mat

Out[11]: 4×4 Array{Int64,2}:
 1  4  3  4
 3  4  5  6
 4  4  4  6
 3  3  3  3
```

Note that, in the console (called the REPL), you can use `;` to surpress the output. In a script this is done automatically. Note that the “value” of an array is its pointer to the memory location. This means that arrays which are set equal affect the same values:

```
In [12]: a = [1;3;4]
         b = a
         b[1] = 10
         a

Out [12]: 3-element Array{Int64,1}:
          10
           3
           4
```

To set an array equal to the values to another array, use `copy`

```
In [13]: a = [1;4;5]
         b = copy(a)
         b[1] = 10
         a

Out [13]: 3-element Array{Int64,1}:
           1
           4
           5
```

We can also make an array of a similar size and shape via the function `similar`, or make an array of zeros/ones with `zeros` or `ones` respectively:

```
In [14]: c = similar(a)
         d = zeros(a)
         e = ones(a)
         println(c); println(d); println(e)

[786432,0,0]
[0,0,0]
[1,1,1]
```

Note that arrays can be index'd by arrays:

```
In [15]: a[1:2]

Out [15]: 2-element Array{Int64,1}:
          1
          4
```

Arrays can be of any type, specified by the type parameter. One interesting thing is that this means that arrays can be of arrays:

```
In [12]: a = Vector{Vector{Float64}}(3)
          a[1] = [1;2;3]
          a[2] = [1;2]
          a[3] = [3;4;5]
          a

Out[12]: 3-element Array{Array{Float64,1},1}:
          [1.0,2.0,3.0]
          [1.0,2.0]
          [3.0,4.0,5.0]
```

---

**Question 1** Can you explain the following behavior? Julia's community values consistency of the rules, so all of the behavior is deducible from simple rules. (Hint: I have noted all of the rules involved here).

```
In [14]: b = a
          b[1] = [1;4;5]
          a

Out[14]: 3-element Array{Array{Float64,1},1}:
          [1.0,4.0,5.0]
          [1.0,2.0]
          [3.0,4.0,5.0]
```

---

To fix this, there is a recursive copy function: `deepcopy`

```
In [16]: b = deepcopy(a)
          b[1] = [1;2;3]
          a

Out[16]: 3-element Array{Array{Float64,1},1}:
          [1.0,4.0,5.0]
          [1.0,2.0]
          [3.0,4.0,5.0]
```

For high performance, Julia provides mutating functions. These functions change the input values that are passed in, instead of returning a new value. By convention, mutating functions tend to be defined with a `!` at the end and tend to mutate their first argument. An example of a mutating function in `scale!` which scales an array by a scalar (or array)

```
In [19]: a = [1;6;8]
          scale!(a,2) # a changes

Out[19]: 3-element Array{Int64,1}:
           2
          12
          16
```

The purpose of mutating functions is that they allow one to reduce the number of memory allocations which is crucial for achieving high performance.

## 0.2 Control Flow

Control flow in Julia is pretty standard. You have your basic for and while loops, and your if statements. There's more in the documentation.

```
In [16]: for i=1:5 #for i goes from 1 to 5
          println(i)
        end

        t = 0
        while t<5
            println(t)
            t+=1 # t = t + 1
        end

        school = :UCI

        if school==:UCI
            println("ZotZotZot")
        else
            println("Not even worth discussing.")
        end
```

```
1
2
3
4
5
0
1
2
3
4
ZotZotZot
```

One interesting feature about Julia control flow is that we can write multiple loops in one line:

```
In [17]: for i=1:2, j=2:4
          println(i*j)
        end
```

```
2
3
4
4
6
8
```

### 0.3 Function Syntax

```
In [20]: f(x,y) = 2x+y # Create an inline function
```

```
Out[20]: f (generic function with 1 method)
```

```
In [22]: f(1,2) # Call the function
```

```
Out[22]: 4
```

```
In [24]: function f(x)
           x+2
       end # Long form definition
```

```
WARNING: Method definition f(Any) in module Main at In[23]:2 overwritten at In[24]:
```

```
Out[24]: f (generic function with 2 methods)
```

By default, Julia functions return the last value computed within them.

```
In [26]: f(2)
```

```
Out[26]: 4
```

A key feature of Julia is multiple dispatch. Notice here that there is “one function”, `f`, with two methods. Methods are the actionable parts of a function. Here, there is one method defined as `(::Any, ::Any)` and `(::Any)`, meaning that if you give `f` two values then it will call the first method, and if you give it one value then it will call the second method.

Multiple dispatch works on types. To define a dispatch on a type, use the `::Type` signifier:

```
In [35]: f(x::Int, y::Int) = 3x+2y
```

```
WARNING: Method definition f(Int64, Int64) in module Main at In[28]:1 overwritten a
```

```
Out[35]: f (generic function with 4 methods)
```

Julia will dispatch onto the strictest acceptable type signature.

```
In [30]: f(2,3) # 3x+2y
```

```
Out[30]: 12
```

```
In [32]: f(2.0,3) # 2x+y since 2.0 is not an Int
```

```
Out[32]: 7.0
```

Types in signatures can be parametric. For example, we can define a method for “two values are passed in, both Numbers and having the same type”. Note that `<:` means “a subtype of”.

```
In [3]: f{T<:Number}(x::T, y::T) = 4x+10y
```

```
Out[3]: f (generic function with 1 method)
```

```
In [37]: f(2,3) # 3x+2y since (::Int,::Int) is stricter
```

```
Out[37]: 12
```

```
In [4]: f(2.0,3.0) # 4x+10y
```

```
Out[4]: 38.0
```

Note that type parameterizations can have as many types as possible, and do not need to declare a supertype. For example, we can say that there is an  $x$  which must be a `Number`, while  $y$  and  $z$  must match types:

```
In [5]: f{T<:Number,T2}(x::T,y::T2,z::T2) = 5x + 5y + 5z
```

```
Out[5]: f (generic function with 1 method)
```

We will go into more depth on multiple dispatch later since this is the core design feature of Julia. The key feature is that Julia functions specialize on the types of their arguments. This means that  $f$  is a separately compiled function for each method (and for parametric types, each possible method). The first time it is called it will compile.

---

## Question 2 Can you explain these timings?

```
In [6]: f(x,y,z,w) = x+y+z+w
         @time f(1,1,1,1)
         @time f(1,1,1,1)
         @time f(1,1,1,1)
         @time f(1,1,1,1.0)
         @time f(1,1,1,1.0)

0.003880 seconds (387 allocations: 21.150 KB)
0.000002 seconds (4 allocations: 160 bytes)
0.000001 seconds (3 allocations: 144 bytes)
0.002570 seconds (1.33 k allocations: 69.866 KB)
0.000001 seconds (4 allocations: 160 bytes)
```

```
Out[6]: 4.0
```

---

Note that functions can also feature optional arguments:

```
In [42]: function test_function(x,y;z=0) #z is an optional argument
        if z==0
            return x+y,x*y #Return a tuple
        else
            return x*y*z,x+y+z #Return a different tuple
            #whitespace is optional
        end #End if statement
    end #End function definition
```

```
Out[42]: test_function (generic function with 1 method)
```

Here, if  $z$  is not specified, then it's 0.

```
In [45]: x,y = test_function(1,2)
```

```
Out[45]: (3,2)
```

```
In [46]: x,y = test_function(1,2;z=3)
```

```
Out[46]: (6,6)
```

Notice that we also featured multiple return values.

```
In [47]: println(x); println(y)
```

```
6
6
```

The return type for multiple return values is a Tuple. The syntax for a tuple is  $(x, y, z, \dots)$  or inside of functions you can use the shorthand  $x, y, z, \dots$  as shown.

Note that functions in Julia are “first-class”. This means that functions are just a type themselves. Therefore functions can make functions, you can store functions as variables, pass them as variables, etc. For example:

```
In [7]: function function_playtime(x) #z is an optional argument
        y = 2+x
        function test()
            2y # y is defined in the previous scope, so it's available here
        end
        z = test() * test()
        return z,test
    end #End function definition
    z,test = function_playtime(2)
```

```
WARNING: Method definition function_playtime{Any} in module Main at In[6]:2 overwri
```

```
Out[7]: (64,test)
```

```
In [14]: test()
```

```
Out[14]: 8
```

Notice that `test()` does not get passed in `y` but knows what `y` is. This is due to the function scoping rules: an inner function can know the variables defined in the same scope as the function. This rule is recursive, leading us to the conclusion that the top level scope is global. Yes, that means

```
In [18]: a = 2
```

```
Out[18]: 2
```

defines a global variable. We will go into more detail on this.

Lastly we show the anonymous function syntax. This allows you to define a function inline.

```
In [20]: g = (x,y) -> 2x+y
```

```
Out[20]: (::#5) (generic function with 1 method)
```

Unlike named functions, `g` is simply a function in a variable and can be overwritten at any time:

```
In [21]: g = (x) -> 2x
```

```
Out[21]: (::#7) (generic function with 1 method)
```

An anonymous function cannot have more than 1 dispatch. However, as of v0.5, they are compiled and thus do not have any performance disadvantages from named functions.

## 0.4 Type Declaration Syntax

A type is what in many other languages is an “object”. If that is a foreign concept, think of a type as a thing which has named components. A type is the idea for what the thing is, while an instantiation of the type is a specific one. For example, you can think of a car as having an make and a model. So that means a Toyota RAV4 is an instantiation of the car type.

In Julia, we would define the car type as follows:

```
In [48]: type Car
           make
           model
       end
```

We could then make the instance of a car as follows:

```
In [49]: mycar = Car("Toyota", "Rav4")
```

```
Out[49]: Car("Toyota", "Rav4")
```

Here I introduced the string syntax for Julia which uses “...” (like most other languages, I’m glaring at you MATLAB). I can grab the “fields” of my type using the `.` syntax:



```
In [51]: mycar.make
```

```
Out[51]: "Toyota"
```

To “enhance Julia’s performance”, one usually likes to make the typing stricter. For example, we can define a `WorkshopParticipant` (notice the convention for types is capital letters, Camel-Case) as having a name and a field. The name will be a string and the field will be a `Symbol` type, (defined by `:Symbol`, which we will go into plenty more detail later).

```
In [52]: type WorkshopParticipant
          name::String
          field::Symbol
        end
        tony = WorkshopParticipant("Tony", :physics)
```

```
Out[52]: WorkshopParticipant("Tony", :physics)
```

As with functions, types can be set “parametrically”. For example, we can have an `StaffMember` have a name and a field, but also an age. We can allow this age to be any `Number` type as follows:

```
In [1]: type StaffMember{T<:Number}
          name::String
          field::Symbol
          age::T
        end
        ter = StaffMember("Terry", :football, 17)
```

```
Out[1]: StaffMember{Int64}("Terry", :football, 17)
```

The rules for parametric typing is the same as for functions. Note that most of Julia’s types, like `Float64` and `Int`, are natively defined in Julia in this manner. This means that there’s no limit for user defined types, only your imagination. Indeed, many of Julia’s features first start out as a prototyping package before it’s ever moved into `Base` (the Julia library that ships as the `Base` module in every installation).

Lastly, there exist abstract types. These types cannot be instantiated but are used to build the type hierarchy. You’ve already seen one abstract type, `Number`. We can define one for `Person` using the `Abstract` keyword

```
In [15]: abstract Person
```

Then we can set types as a subtype of person

```
In [16]: type Student <: Person
          grade
        end
```

---

**Question 3** Can you make a function `k(x)` where `x` has to be a `Person`?

---

Another “version” of type is `immutable`. When one uses `immutable`, the fields of the type cannot be changed. However, Julia will automatically stack allocate immutable types, whereas standard types are heap allocated. If this is unfamiliar terminology, then think of this as meaning that immutable types are able to be stored closer to the CPU and have less cost for memory access (this is a detail not present in many scripting languages). Many things like Julia’s built-in `Number` types are defined as `immutable` in order to give good performance.

```
In [63]: immutable Field
           name
           school
       end
           ds = Field(:DataScience, [:PhysicalScience; :ComputerScience])
```

```
WARNING: Method definition (::Type{Main.Field})(Any, Any) in module Main at In[58]:
```

```
Out [63]: Field(:DataScience, Symbol[:PhysicalScience, :ComputerScience])
```

---

**Question 4** Can you explain this interesting quirk? Thus `Field` is immutable, meaning that `ds.name` and `ds.school` cannot be changed:

```
In [64]: ds.name = :ComputationalStatistics
```

```
LoadError: type Field is immutable
while loading In[64], in expression starting on line 1
```

However, the following is allowed:

```
In [65]: push!(ds.school, :BiologicalScience)
           ds.school
```

```
Out [65]: 3-element Array{Symbol,1}:
           :PhysicalScience
           :ComputerScience
           :BiologicalScience
```

(Hint: recall that an array is not the values itself, but a pointer to the memory of the values)

---

One important detail in Julia is that everything is a type (and every piece of code is an Expression type, more on this later). Thus functions are also types, which we can access the fields of. Not only is everything compiled down to C, but all of the “C parts” are always accessible. For example, we can, if we so choose, get a function pointer:

```
In [46]: foo(x) = 2x
         first(methods(foo)).lambda_template.fptr
```

```
Out[46]: Ptr{Void} @0x0000000000000000
```

## 0.5 Documentation and “Hunting”

The main source of information is the [Julia Documentation](#). Julia also provides lots of built-in documentation and ways to find out what’s going on. The number of tools for “hunting down what’s going on / available” is too numerous to explain in full detail here, so instead this will just touch on what’s important. For example, the `?`  gets you to the documentation for a type, function, etc.

```
In [23]: ?copy
```

```
search: copy copy! copysign deepcopy unsafe_copy! cospi complex Complex
```

```
Out[23]:
```

```
copy(x)
```

Create a shallow copy of `x`: the outer structure is copied, but not all internal values. For example, copying an array produces a new array with identically-same elements as the original.

To find out what methods are available, we can use the `methods` function. For example, let’s see how `+` is defined:

```
In [25]: methods(+)
```

```
Out[25]: # 163 methods for generic function "+":
          +(x::Bool, z::Complex{Bool}) at complex.jl:136
          +(x::Bool, y::Bool) at bool.jl:48
          +(x::Bool) at bool.jl:45
          +{T<:AbstractFloat}(x::Bool, y::T) at bool.jl:55
          +(x::Bool, z::Complex) at complex.jl:143
          +(x::Bool, A::AbstractArray{Bool,N<:Any}) at arraymath.jl:91
          +(x::Float32, y::Float32) at float.jl:239
          +(x::Float64, y::Float64) at float.jl:240
          +(z::Complex{Bool}, x::Bool) at complex.jl:137
          +(z::Complex{Bool}, x::Real) at complex.jl:151
          +(a::Float16, b::Float16) at float16.jl:136
          +(x::Char, y::Integer) at char.jl:40
          +(c::BigInt, x::BigFloat) at mpfr.jl:240
```

```

+(a::BigInt, b::BigInt, c::BigInt, d::BigInt, e::BigInt) at gmp.jl:298
+(a::BigInt, b::BigInt, c::BigInt, d::BigInt) at gmp.jl:291
+(a::BigInt, b::BigInt, c::BigInt) at gmp.jl:285
+(x::BigInt, y::BigInt) at gmp.jl:255
+(x::BigInt, c::Union{UInt16,UInt32,UInt64,UInt8}) at gmp.jl:310
+(x::BigInt, c::Union{Int16,Int32,Int64,Int8}) at gmp.jl:326
+(a::BigFloat, b::BigFloat, c::BigFloat, d::BigFloat, e::BigFloat) at mpfr.jl:381
+(a::BigFloat, b::BigFloat, c::BigFloat, d::BigFloat) at mpfr.jl:381
+(a::BigFloat, b::BigFloat, c::BigFloat) at mpfr.jl:375
+(x::BigFloat, c::BigInt) at mpfr.jl:236
+(x::BigFloat, y::BigFloat) at mpfr.jl:205
+(x::BigFloat, c::Union{UInt16,UInt32,UInt64,UInt8}) at mpfr.jl:212
+(x::BigFloat, c::Union{Int16,Int32,Int64,Int8}) at mpfr.jl:220
+(x::BigFloat, c::Union{Float16,Float32,Float64}) at mpfr.jl:228
+{T}(B::BitArray{2}, J::UniformScaling{T}) at linalg/uniformscaling.jl:38
+(a::Base.Pkg.Resolve.VersionWeights.VWPreBuildItem, b::Base.Pkg.Resolve.VersionWeights.VWPreBuildItem) at base/pkg_resolve/version_weights/vw_prebuilditem.jl:10
+(a::Base.Pkg.Resolve.VersionWeights.VWPreBuild, b::Base.Pkg.Resolve.VersionWeights.VWPreBuild) at base/pkg_resolve/version_weights/vw_prebuild.jl:10
+(a::Base.Pkg.Resolve.VersionWeights.VersionWeight, b::Base.Pkg.Resolve.VersionWeights.VersionWeight) at base/pkg_resolve/version_weights/version_weight.jl:10
+(a::Base.Pkg.Resolve.MaxSum.FieldValues.FieldValue, b::Base.Pkg.Resolve.MaxSum.FieldValues.FieldValue) at base/pkg_resolve/max_sum/field_values/field_value.jl:10
+(x::Base.Dates.CompoundPeriod, y::Base.Dates.CompoundPeriod) at dates/compoundperiod.jl:10
+(x::Base.Dates.CompoundPeriod, y::Base.Dates.Period) at dates/periods.jl:10
+(x::Base.Dates.CompoundPeriod, y::Base.Dates.TimeType) at dates/periods.jl:10
+(dt::DateTime, z::Base.Dates.Month) at dates/arithmetic.jl:37
+(dt::DateTime, y::Base.Dates.Year) at dates/arithmetic.jl:13
+(x::DateTime, y::Base.Dates.Period) at dates/arithmetic.jl:64
+(x::Date, y::Base.Dates.Day) at dates/arithmetic.jl:62
+(x::Date, y::Base.Dates.Week) at dates/arithmetic.jl:60
+(dt::Date, z::Base.Dates.Month) at dates/arithmetic.jl:43
+(dt::Date, y::Base.Dates.Year) at dates/arithmetic.jl:17
+(y::AbstractFloat, x::Bool) at bool.jl:57
+{T<Union{Int128,Int16,Int32,Int64,Int8,UInt128,UInt16,UInt32,UInt64,UInt8}}(x::T, y::T) at union.jl:10
+(x::Integer, y::Ptr) at pointer.jl:108
+(z::Complex, w::Complex) at complex.jl:125
+(z::Complex, x::Bool) at complex.jl:144
+(x::Real, z::Complex{Bool}) at complex.jl:150
+(x::Real, z::Complex) at complex.jl:162
+(z::Complex, x::Real) at complex.jl:163
+(x::Rational, y::Rational) at rational.jl:199
+(x::Integer, y::Char) at char.jl:41
+{N}(i::Integer, index::CartesianIndex{N}) at multidimensional.jl:58
+(c::Union{UInt16,UInt32,UInt64,UInt8}, x::BigInt) at gmp.jl:314
+(c::Union{Int16,Int32,Int64,Int8}, x::BigInt) at gmp.jl:327
+(c::Union{UInt16,UInt32,UInt64,UInt8}, x::BigFloat) at mpfr.jl:216
+(c::Union{Int16,Int32,Int64,Int8}, x::BigFloat) at mpfr.jl:224
+(c::Union{Float16,Float32,Float64}, x::BigFloat) at mpfr.jl:232
+(x::Irrational, y::Irrational) at irrationals.jl:88
+(x::Number) at operators.jl:115
+{T<Number}(x::T, y::T) at promotion.jl:255

```

```

+(x::Number, y::Number) at promotion.jl:190
+(r1::OrdinalRange, r2::OrdinalRange) at operators.jl:505
+{T<:AbstractFloat}(r1::FloatRange{T}, r2::FloatRange{T}) at operators.jl:
+{T<:AbstractFloat}(r1::LinSpace{T}, r2::LinSpace{T}) at operators.jl:531
+(r1::Union{FloatRange,LinSpace,OrdinalRange}, r2::Union{FloatRange,LinSpa
+(x::Ptr, y::Integer) at pointer.jl:106
+(A::BitArray, B::BitArray) at bitarray.jl:1042
+(A::Array{T<:Any,2}, B::Diagonal) at linalg/special.jl:121
+(A::Array{T<:Any,2}, B::Bidiagonal) at linalg/special.jl:121
+(A::Array{T<:Any,2}, B::Tridiagonal) at linalg/special.jl:121
+(A::Array{T<:Any,2}, B::SymTridiagonal) at linalg/special.jl:130
+(A::Array{T<:Any,2}, B::Base.LinAlg.AbstractTriangular) at linalg/special
+(A::Array, B::SparseMatrixCSC) at sparse/sparsematrix.jl:1711
+{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period}}(x::Union{Base.Res
+(A::AbstractArray{Bool,N<:Any}, x::Bool) at arraymath.jl:90
+(A::SymTridiagonal, B::SymTridiagonal) at linalg/tridiag.jl:96
+(A::Tridiagonal, B::Tridiagonal) at linalg/tridiag.jl:494
+(A::UpperTriangular, B::UpperTriangular) at linalg/triangular.jl:357
+(A::LowerTriangular, B::LowerTriangular) at linalg/triangular.jl:358
+(A::UpperTriangular, B::Base.LinAlg.UnitUpperTriangular) at linalg/triang
+(A::LowerTriangular, B::Base.LinAlg.UnitLowerTriangular) at linalg/triang
+(A::Base.LinAlg.UnitUpperTriangular, B::UpperTriangular) at linalg/triang
+(A::Base.LinAlg.UnitLowerTriangular, B::LowerTriangular) at linalg/triang
+(A::Base.LinAlg.UnitUpperTriangular, B::Base.LinAlg.UnitUpperTriangular)
+(A::Base.LinAlg.UnitLowerTriangular, B::Base.LinAlg.UnitLowerTriangular)
+(A::Base.LinAlg.AbstractTriangular, B::Base.LinAlg.AbstractTriangular) at
+(Da::Diagonal, Db::Diagonal) at linalg/diagonal.jl:110
+(A::Bidiagonal, B::Bidiagonal) at linalg/bidiag.jl:256
+(UL::UpperTriangular, J::UniformScaling) at linalg/uniformscaling.jl:55
+(UL::Base.LinAlg.UnitUpperTriangular, J::UniformScaling) at linalg/unifor
+(UL::LowerTriangular, J::UniformScaling) at linalg/uniformscaling.jl:55
+(UL::Base.LinAlg.UnitLowerTriangular, J::UniformScaling) at linalg/unifor
+(A::Diagonal, B::Bidiagonal) at linalg/special.jl:120
+(A::Bidiagonal, B::Diagonal) at linalg/special.jl:121
+(A::Diagonal, B::Tridiagonal) at linalg/special.jl:120
+(A::Tridiagonal, B::Diagonal) at linalg/special.jl:121
+(A::Diagonal, B::Array{T<:Any,2}) at linalg/special.jl:120
+(A::Bidiagonal, B::Tridiagonal) at linalg/special.jl:120
+(A::Tridiagonal, B::Bidiagonal) at linalg/special.jl:121
+(A::Bidiagonal, B::Array{T<:Any,2}) at linalg/special.jl:120
+(A::Tridiagonal, B::Array{T<:Any,2}) at linalg/special.jl:120
+(A::SymTridiagonal, B::Tridiagonal) at linalg/special.jl:129
+(A::Tridiagonal, B::SymTridiagonal) at linalg/special.jl:130
+(A::SymTridiagonal, B::Array{T<:Any,2}) at linalg/special.jl:129
+(A::Diagonal, B::SymTridiagonal) at linalg/special.jl:138
+(A::SymTridiagonal, B::Diagonal) at linalg/special.jl:139
+(A::Bidiagonal, B::SymTridiagonal) at linalg/special.jl:138
+(A::SymTridiagonal, B::Bidiagonal) at linalg/special.jl:139

```

```

+(A::Diagonal, B::UpperTriangular) at linalg/special.jl:150
+(A::UpperTriangular, B::Diagonal) at linalg/special.jl:151
+(A::Diagonal, B::Base.LinAlg.UnitUpperTriangular) at linalg/special.jl:151
+(A::Base.LinAlg.UnitUpperTriangular, B::Diagonal) at linalg/special.jl:151
+(A::Diagonal, B::LowerTriangular) at linalg/special.jl:150
+(A::LowerTriangular, B::Diagonal) at linalg/special.jl:151
+(A::Diagonal, B::Base.LinAlg.UnitLowerTriangular) at linalg/special.jl:151
+(A::Base.LinAlg.UnitLowerTriangular, B::Diagonal) at linalg/special.jl:151
+(A::Base.LinAlg.AbstractTriangular, B::SymTridiagonal) at linalg/special.jl:151
+(A::SymTridiagonal, B::Base.LinAlg.AbstractTriangular) at linalg/special.jl:151
+(A::Base.LinAlg.AbstractTriangular, B::Tridiagonal) at linalg/special.jl:151
+(A::Tridiagonal, B::Base.LinAlg.AbstractTriangular) at linalg/special.jl:151
+(A::Base.LinAlg.AbstractTriangular, B::Bidiagonal) at linalg/special.jl:151
+(A::Bidiagonal, B::Base.LinAlg.AbstractTriangular) at linalg/special.jl:151
+(A::Base.LinAlg.AbstractTriangular, B::Array{T<:Any,2}) at linalg/special.jl:151
+{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period}}(Y::Union{Base.ReshapedArray{T<:Any,1,A<:DenseArray{MI<:Tuple{Vararg{Base.Dates.Period}},N}})) at dates/periods.jl:70
+{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period},Q<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period}}(Y::Union{Base.ReshapedArray{T<:Any,1,A<:DenseArray{MI<:Tuple{Vararg{Base.Dates.Period}},N}})) at dates/periods.jl:70
+{T<:Base.Dates.TimeType,P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period}}(r::Range{T},x::Base.Dates.Period) at dates/range.jl:8
+{Tv1,Ti1,Tv2,Ti2}(A_1::SparseMatrixCSC{Tv1,Ti1},A_2::SparseMatrixCSC{Tv2,Ti2}) at sparse/sparsematrix.jl:1709
+(A::SparseMatrixCSC, B::Array) at sparse/sparsematrix.jl:1709
+(A::SparseMatrixCSC, J::UniformScaling) at sparse/sparsematrix.jl:3811
+(x::AbstractSparseArray{Tv<:Any,Ti<:Any,1},y::AbstractSparseArray{Tv<:Any,Ti<:Any,1}) at sparse/sparsematrix.jl:3811
+(x::Union{Base.ReshapedArray{T<:Any,1,A<:DenseArray{MI<:Tuple{Vararg{Base.Dates.Period}},N}},AbstractSparseArray{Tv<:Any,Ti<:Any,1}},y::Union{Base.ReshapedArray{T<:Any,1,A<:DenseArray{MI<:Tuple{Vararg{Base.Dates.Period}},N}},AbstractSparseArray{Tv<:Any,Ti<:Any,1}})) at sparse/sparsematrix.jl:3811
+{T<:Number}(x::AbstractArray{T,N<:Any}) at abstractarraymath.jl:91
+{R,S}(A::AbstractArray{R,N<:Any},B::AbstractArray{S,N<:Any}) at arraymath.jl:94
+(A::AbstractArray,x::Number) at arraymath.jl:94
+(x::Number,A::AbstractArray) at arraymath.jl:95
+{N}(index1::CartesianIndex{N},index2::CartesianIndex{N}) at multidimensional.jl:57
+{N}(index::CartesianIndex{N},i::Integer) at multidimensional.jl:57
+(J1::UniformScaling,J2::UniformScaling) at linalg/uniformscaling.jl:37
+(J::UniformScaling,B::BitArray{2}) at linalg/uniformscaling.jl:39
+(J::UniformScaling,A::AbstractArray{T<:Any,2}) at linalg/uniformscaling.jl:41
+(J::UniformScaling,x::Number) at linalg/uniformscaling.jl:41
+(x::Number,J::UniformScaling) at linalg/uniformscaling.jl:42
+{TA,TJ}(A::AbstractArray{TA,2},J::UniformScaling{TJ}) at linalg/uniformscaling.jl:42
+{T}(a::Base.Pkg.Resolve.VersionWeights.HierarchicalValue{T},b::Base.Pkg.Resolve.VersionWeights.HierarchicalValue{T}) at dates/periods.jl:70
+{P<:Base.Dates.Period}(x::P,y::P) at dates/periods.jl:70
+(x::Base.Dates.Period,y::Base.Dates.Period) at dates/periods.jl:311
+(y::Base.Dates.Period,x::Base.Dates.CompoundPeriod) at dates/periods.jl:311
+(y::Base.Dates.Period,x::Base.Dates.TimeType) at dates/arithmetic.jl:66
+{T<:Base.Dates.TimeType}(x::Base.Dates.Period,r::Range{T}) at dates/range.jl:8
+(x::Union{Base.Dates.CompoundPeriod,Base.Dates.Period}) at dates/periods.jl:70
+{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period}}(x::Union{Base.Dates.CompoundPeriod,Base.Dates.Period}) at dates/periods.jl:70
+(x::Base.Dates.TimeType) at dates/arithmetic.jl:8
+(a::Base.Dates.TimeType,b::Base.Dates.Period,c::Base.Dates.Period) at dates/arithmetic.jl:8
+(a::Base.Dates.TimeType,b::Base.Dates.Period,c::Base.Dates.Period,d::Base.Dates.Period) at dates/arithmetic.jl:8

```

```

+(x::Base.Dates.TimeType, y::Base.Dates.CompoundPeriod) at dates/periods.jl:4
+(x::Base.Dates.Instant) at dates/arithmetic.jl:4
+{T<:Base.Dates.TimeType}(x::AbstractArray{T,N<:Any}, y::Union{Base.Dates.TimeType,Base.Dates.Instant}) at dates/arithmetic.jl:4
+{T<:Base.Dates.TimeType}(y::Union{Base.Dates.CompoundPeriod,Base.Dates.Period}) at dates/arithmetic.jl:4
+{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period}}(y::Base.Dates.TimeType) at dates/arithmetic.jl:4
+(a, b, c, xs...) at operators.jl:138

```

We can inspect a type by finding its fields with `fieldnames`

```
In [40]: fieldnames(LinSpace)
```

```

Out[40]: 4-element Array{Symbol,1}:
 :start
 :stop
 :len
 :divisor

```

and find out which method was used with the `@which` macro:

```
In [43]: @which copy([1,2,3])
```

```
Out[43]: copy{T<:Array{T,N}}(a::T) at array.jl:70
```

Notice that this gives you a link to the source code where the function is defined.

Lastly, we can find out what type a variable is with the `typeof` function:

```
In [44]: a = [1;2;3]
         typeof(a)
```

```
Out[44]: Array{Int64,1}
```

## 0.6 Some Basic Types

Julia provides many basic types. Indeed, you will come to know Julia as a system of multiple dispatch on types, meaning that the interaction of types with functions is core to the design.

### 0.6.1 Lazy Iterator Types

While MATLAB or Python has easy functions for building arrays, Julia tends to side-step the actual “array” part with specially made types. One such example are ranges. To define a range, use the `start:stepsize:end` syntax. For example:

```
In [45]: a = 1:5
         println(a)
         b = 1:2:10
         println(b)
```

```
1:5
```

```
1:2:9
```

We can use them like any array. For example:

```
In [47]: println(a[2]); println(b[3])

2
5
```

But what is b?

```
In [50]: println(typeof(b))

StepRange{Int64,Int64}
```

b isn't an array, it's a StepRange. A StepRange has the ability to act like an array using its fields:

```
In [52]: fieldnames(StepRange)

Out[52]: 3-element Array{Symbol,1}:
          :start
          :step
          :stop
```

Note that at any time we can get the array from these kinds of type via the `collect` function:

```
In [55]: c = collect(a)

Out[55]: 5-element Array{Int64,1}:
          1
          2
          3
          4
          5
```

The reason why lazy iterator types are preferred is that they do not do the computations until it's absolutely necessary, and they take up much less space. We can check this with `@time`:

```
In [7]: @time a = 1:100000
         @time a = 1:100
         @time b = collect(1:100000);

0.000005 seconds (6 allocations: 240 bytes)
0.000003 seconds (5 allocations: 192 bytes)
0.007849 seconds (189 allocations: 792.844 KB)
```

Notice that the amount of time the range takes is much shorter. This is mostly because there is a lot less memory allocation needed: only a StepRange is built, and all that holds is the three numbers. However, b has to hold 100000 numbers, leading to the huge difference.



**Question 4** If you know `start`, `step`, and `stop`, how do you calculate the `i`th value? Can you create a function `MyRange` which where for `a` being a `MyRange`, `value(a, i) == a[i]` for `a` a `StepRange`? (I will show you how to make the `a[i]` syntax available for your own types later. As noted before, all of these Julia types are implemented in Julia, and therefore you have the power to implement it yourself).

## 0.6.2 Dictionaries

Another common type is the Dictionary. It allows you to access (key,value) pairs in a named manner. For example:

```
In [1]: d = Dict{:test=>2, "silly"=>:suit}
        println(d{:test})
        println(d["silly"])

2
suit
```

## 0.6.3 Tuples

Tuples are immutable arrays. That means they can't be changed. However, they are super fast. They are made with the `(x, y, z, ...)` syntax and are the standard return type of functions which return more than one object.

```
In [4]: tup = (2., 3) # Don't have to match types
        x, y = (3.0, "hi") # Can separate a tuple to multiple variables

Out[4]: (3.0, "hi")
```

## 0.7 Metaprogramming

Metaprogramming is a huge feature of Julia. The key idea is that every statement in Julia is of the type `Expression`. Julia operators by building an Abstract Syntax Tree (AST) from the Expressions. You've already been exposed to this a little bit: a `Symbol` (like `:PhysicalSciences` is not a string because it is part of the AST, and thus is part of the parsing/expression structure. One interesting thing is that symbol comparisons are  $O(1)$  while string comparisons, like always, are  $O(n)$  is part of this, and macros (the weird functions with an `@`) are functions on expressions.

Thus you can think of metaprogramming as "code which takes in code and outputs code". One basic example is the `@time` macro:

```
In [85]: macro my_time(ex)
        return quote
            local t0 = time()
            local val = $ex
            local t1 = time()
            println("elapsed time: ", t1-t0, " seconds")
            val
        end
    end
```

```
LoadError: error in method definition: function Base.@time must be explicit
while loading In[85], in expression starting on line 1
```

This takes in an expression `ex`, gets the time before and after evaluation, and prints the elapsed time between (the real time macro also calculates the allocations as seen earlier). Note that `$ex` “interpolates” the expression into the macro. Going into detail on metaprogramming is a large step from standard scripting and will be a later session.

Why macros? One reason is because it lets you define any syntax you want. Since it operates on the expressions themselves, as long as you know how to parse the expression into working code, you can “choose any syntax” to be your syntax. A case study will be shown later. Another reason is because these are done at “parse time” and those are only called once (before the function compilation).