Exercise 1

Let us consider the following CCS definition of a coffee machine.

$$CM \stackrel{\text{def}}{=} coin.\overline{coffee}.CM$$

• Give a CCS process which describes a coffee machine that may behave like CM but may also steal the money it receives and fail at any time.

Exercise 2

Which of the following expressions are correctly built CCS expressions? Why? (Assume that A, B are process constants and a, b are channel names.)

- 1. a.b.A + B
- 2. $(a.Nil + \overline{a}.A) \setminus \{a,b\}$
- 3. $(a.Nil \mid \overline{a}.A) \setminus \{a, \tau\}$
- 4. a.B + [a/b]
- 5. $\tau.\tau.B + Nil$
- 6. (a.B + b.B)[a/b, b/a]
- 7. $(a.B + \tau.B)[a/\tau, b/a]$
- 8. $(a.B + \tau.B)[\tau/a]$
- 9. $(a.b.A + \overline{a}.Nil) \mid B$
- 10. $(a.b.A + \overline{a}.Nil).B$
- 11. $(a.b.A + \overline{a}.Nil) + B$
- 12. $(Nil \mid Nil) + Nil$

Exercise 3*

By using the SOS rules for CCS, prove the existence of the following transitions (assume that A is a CCS constant with defining equation $A \stackrel{\text{def}}{=} b.a.B$):

- $(A \mid \overline{b}.Nil) \setminus \{b\} \xrightarrow{\tau} (a.B \mid Nil) \setminus \{b\}$
- $(A \mid \overline{b}.a.B) + (\overline{b}.A)[a/b] \xrightarrow{\overline{b}} (A \mid a.B)$
- $(A \mid \overline{b}.a.B) + (\overline{b}.A)[a/b] \xrightarrow{\overline{a}} A[a/b]$

Exercise 4*

Consider the following CCS defining equations:

$$CM \stackrel{\mathrm{def}}{=} coin. \overline{coffee}. CM$$
 $CS \stackrel{\mathrm{def}}{=} \overline{pub}. \overline{coin}. coffee. CS$
 $Uni \stackrel{\mathrm{def}}{=} (CM \mid CS) \setminus \{coin, coffee\}$

Use the rules of the SOS semantics for CCS to derive the labelled transition system for the process Uni defined above. The proofs can be omitted and a drawing of the resulting LTS is enough.

$$(CM \mid \overline{coin}. coffee. CS) \setminus \{coin, coffee\}$$

$$\downarrow^{\tau}$$

$$(\overline{coffee}. CM \mid coffee. CS) \setminus \{coin, coffee\}$$

Exercise 5

Draw (part of) the labelled transition system for the process constant A defined by

$$A \stackrel{\text{def}}{=} (a.A) \setminus \{b\}.$$

The resulting LTS should have infinitely many reachable states. Can you think of a CCS term that generates a finite LTS and intuitively has the same behaviour as A?

Exercise 6 (optional)

1. Draw the transition graph for the process name Mutex₁ whose behaviour is given by the following defining equations.

$$\begin{array}{ccc} \mathsf{Mutex}_1 & \stackrel{\mathrm{def}}{=} & (\mathsf{User} \mid \mathsf{Sem}) \setminus \{p,v\} \\ \mathsf{User} & \stackrel{\mathrm{def}}{=} & \bar{p}.\mathsf{enter.exit.} \bar{v}.\mathsf{User} \\ \mathsf{Sem} & \stackrel{\mathrm{def}}{=} & p.v.\mathsf{Sem} \end{array}$$

2. Draw the transition graph for the process name Mutex₂ whose behaviour is given by the defining equation

$$\mathsf{Mutex}_2 \stackrel{\mathrm{def}}{=} ((\mathsf{User}|\mathsf{Sem})|\mathsf{User}) \setminus \{p,v\}$$

where User and Sem are defined as before. Would the behaviour of the process change if User was defined as

User
$$\stackrel{\text{def}}{=} \bar{p}$$
.enter. \bar{v} .exit.User ?

3. Draw the transition graph for the process name FMutex whose behaviour is given by the defining equation

$$\mathsf{FMutex} \stackrel{\mathrm{def}}{=} ((\mathsf{User} \mid \mathsf{Sem}) \mid \mathsf{FUser}) \setminus \{p,v\}$$

where User and Sem are defined as before, and the behaviour of FUser is given by the defining equation

$$FUser \stackrel{\text{def}}{=} \bar{p}.enter.(exit.\bar{v}.FUser + exit.\bar{v}.Nil)$$

Do you think that Mutex₂ and FMutex are offering the same behaviour? Can you argue informally for your answer?