Languages and Compilers (SProg og Oversættere)

Lecture 4 Language specifications

Bent Thomsen

Department of Computer Science

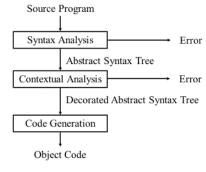
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Learning goals

- A deeper understanding of programming language specifications
- Introduction to context free grammars
- Introduction to BNF and EBNF
- Overview of formal specifications notations

Programming Language Specification

- Why?
 - A communication device between people who need to have a common understanding of the PL:
 - language designer, language implementor, language user
- What to specify?
 - Specify what is a 'well formed' program
 - syntax
 - contextual constraints (also called static semantics):
 - scope rules
 - type rules
 - Specify what is the meaning of (well formed) programs
 - semantics (also called runtime semantics)



Programming Language Specification

- Why?
- What to specify?
- How to specify?
 - Formal specification: use some kind of precisely defined formalism
 - Informal specification: description in English.
 - Usually a mix of both (e.g. Java specification)
 - Syntax => formal specification using RE and CFG
 - Contextual constraints and semantics => informal
 - Formal semantics has been retrofitted though
 - But trend towards more formality (C#, Fortress)
 - fortress.pdf
 - <u>Ecma-334.pdf</u>

Fortress definition p. 71 and p. 181

13.4 Dotted Method Invocations

```
Syntax:
```

```
\begin{array}{lll} \textit{Primary} & ::= & \textit{Primary} . \textit{Id StaticArgs? ParenthesisDelimited} \\ \textit{ParenthesisDelimited} & ::= & \textit{Parenthesized} \\ & & | & \textit{ArgExpr} \\ & & | & () \\ \textit{Parenthesized} & ::= & (\textit{Expr}) \\ \textit{ArgExpr} & ::= & \textit{TupleExpr} \\ & | & ((\textit{Expr},)^* \textit{Expr} ...) \\ \textit{TupleExpr} & ::= & ((\textit{Expr},)^+ \textit{Expr}) \\ \end{array}
```

A dotted method invocation consists of a subexpression (called the receiver expression), followed by '.', followed by an identifier, an optional list of static arguments (described in Chapter 9) and a subexpression (called the argument expression). Unlike in function calls (described in Section 13.6), the argument expression must be parenthesized, even if it is not a tuple. There must be no whitespace on the left-hand side of the '.' and the left-hand side of the left parenthesis of the argument expression. The receiver expression evaluates to the receiver of the invocation (bound to the self parameter (discussed in Section 10.2) of the method). A method invocation may include explicit instantiations of static parameters but most method invocations do not include them.

The receiver and arguments of a method invocation are each evaluated in parallel in a separate implicit thread (see Section 5.4). After this thread group completes normally, the body of the method is evaluated with the parameter of the method bound to the value of the argument expression (thus evaluation of the body occurs after evaluation of the receiver and arguments in dynamic program order). The value and the type of a dotted method invocation are the value and the type of the method body.

We say that methods or functions (collectively called as functionals) may be applied to (also "invoked on" or "called with") an argument. We use "call", "invocation", and "application" interchangeably.

$$[\text{R-METHOD}] \quad \frac{ \text{object } O_- \left(\overrightarrow{x : -}\right)_- \text{ end } \in p \qquad mbody_p(f[\![\overrightarrow{\tau'}]\!], O[\![\overrightarrow{\tau'}]\!]) = \{(\overrightarrow{x'}) \to e\} }{ p \vdash E[O[\![\overrightarrow{\tau'}]\!](\overrightarrow{v'}).f[\![\overrightarrow{\tau'}]\!](\overrightarrow{v'})] \longrightarrow E[[\![\overrightarrow{v}/\overrightarrow{x}]\!][O[\![\overrightarrow{\tau'}]\!](\overrightarrow{v})/\text{self}][\![\overrightarrow{v'}/\overrightarrow{x'}]e] }$$

The C89 standard – 519 pages

6.8 Statements and blocks

Syntax

1 statement:

labeled-statement compound-statement expression-statement selection-statement iteration-statement jump-statement

Semantics

- 2 A statement specifies an action to be performed. Except as indicated, statements are executed in sequence.
- A *block* allows a set of declarations and statements to be grouped into one syntactic unit. The initializers of objects that have automatic storage duration, and the variable length array declarators of ordinary identifiers with block scope, are evaluated and the values are stored in the objects (including storing an indeterminate value in objects without an initializer) each time the declaration is reached in the order of execution, as if it were a statement, and within each declaration in the order that declarators appear.
- A full expression is an expression that is not part of another expression or of a declarator. Each of the following is a full expression: an initializer; the expression in an expression statement; the controlling expression of a selection statement (if or switch); the controlling expression of a while or do statement; each of the (optional) expressions of a for statement; the (optional) expression in a return statement. The end of a full expression is a sequence point.

Forward references: expression and null statements (6.8.3), selection statements (6.8.4), iteration statements (6.8.5), the **return** statement (6.8.6.4).

6.8.3 Expression and null statements

Syntax

1 expression-statement: expression_{opt};

Semantics

- 2 The expression in an expression statement is evaluated as a void expression for its side effects. (134)
- 3 A *null statement* (consisting of just a semicolon) performs no operations.
- 4 EXAMPLE 1 If a function call is evaluated as an expression statement for its side effects only, the discarding of its value may be made explicit by converting the expression to a void expression by means of a cast:

```
int p(int);
/* ... */
(void)p(0);
```

134) Such as assignments, and function calls which have side effects.

5 EXAMPLE 2 In the program fragment

```
char *s;

/* ... */

while (*s++ != '\0')

;
```

a null statement is used to supply an empty loop body to the iteration statement.

6 EXAMPLE 3 A null statement may also be used to carry a label just before the closing } of a compound statement.

Programming Language Specification

A language specification need to address:

- Syntax
 - Token grammar: Regular Expressions
 - Context Free Grammar: BNF or EBNF
- Contextual constraints
 - Scope rules (static semantics)
 - Often informal, but can be formalized
 - Type rules (static semantics)
 - Informal or Formal
- Semantics (dynamic semantics)
 - Informal or Formal

Syntax Analysis

- The syntax analysis portion of a language processor nearly always consists of two parts:
 - A low-level part called a lexical analyzer
 (mathematically, a finite automaton based on a regular grammar)
 - A high-level part called a syntax analyzer, or parser (mathematically, a push-down automaton based on a context-free grammar, or BNF)

The General Problem of Describing Syntax: Terminology

- A sentence is a string of characters over some alphabet
- A language is a set of sentences
- A lexeme is the lowest level syntactic unit of a language (e.g., *, sum, begin)
- A token is a category of lexemes (e.g., identifier)

Definition of Tokens/lexemes

- Tokens are often specified using regular expressions
- Remember:

```
Regular Expression
Terminal
floatdcl
intdcl
           "p"
print
id
          [a-e] | [g-h] | [j-o] | [q-z]
assign
plus
minus
          [0-9]^{+}
inum
          [0-9]^+ . [0-9]^+
fnum
blank
```

Figure 2.3: Formal definition of ac tokens.

Note: In most languages id is a sequence of letters and numbers starting With a letter defined as [a-z]([a-z] | [0-9])*

Formal Definition of Languages

Generators

- A device that generates sentences of a language
- One can determine if the syntax of a particular sentence is syntactically correct by comparing it to the structure of the generator

Recognizers

- A recognition device reads input strings over the alphabet of the language and decides whether the input strings belong to the language
- Example: syntax analysis part of a compiler

BNF and Context-Free Grammars

Context-Free Grammars

- Developed by Noam Chomsky in the mid-1950s
- Language generators, meant to describe the syntax of natural languages
- Define a class of languages called context-free languages
- Backus-Naur Form (1959)
 - Invented by John Backus to describe Algol 58
 - Modified by Peter Naur to describe Algol 60
 - BNF is equivalent to context-free grammars

Syntax is specified using "Context Free Grammars":

- A finite set of terminal symbols (or tokens)
- A finite set of non-terminal symbols
- A start symbol
- A finite set of production rules

A CFG defines a set of strings

This is called the language of the CFG.

Backus-Naur Form

Usually CFG are written in BNF notation.

A production rule in BNF notation is written as:

 $N := \alpha$ where N is a non terminal and α a sequence of terminals and non-terminals $N := \alpha \mid \beta \mid ...$ is an abbreviation for several rules with N as left-hand side.

Sometimes non terminals are represented in angel brackets: $\langle N \rangle$ and ::= is replaced with \rightarrow

15

Example:

Q: What is the "language" defined by this grammar?

Note: a sequence of letters and numbers starting with a letter defined in RE as [a-z]([a-z] | [0-9])*

What is the "language" defined by this grammar?

```
identifier::= available-identifier
            a identifier-or-keyword
available-identifier::= identifier-or-keyword (that is not a keyword)
identifier-or-keyword::=identifier-start-character identifier-part-characters_{opt}
identifier-start-character::= letter-character
                         _ (the underscore character U+005F)
identifier-part-characters::= identifier-part-character
                          identifier-part-characters identifier-part-character
identifier-part-character::= letter-character
                         decimal-digit-character
                        connecting-character combining-character
                        formatting-character
letter-character::= A Unicode character of classes Lu, Ll, Lt, Lm, Lo, or Nl
   A unicode-escape-sequence representing a character of classes Lu, Ll, Lt, Lm, Lo, or Nl
combining-character::= A Unicode character of classes Mn or Mc
   A unicode-escape-sequence representing a character of classes Mn or Mc
decimal-digit-character::= A Unicode character of the class Nd
   A unicode-escape-sequence representing a character of the class Nd
connecting-character::= A Unicode character of the class Pc
   A unicode-escape-sequence representing a character of the class Pc
formatting-character::= A Unicode character of the class Cf
   A unicode-escape-sequence representing a character of the class Cf
```

What is the "language" defined by this grammar?

3.8. Identifiers

An identifier is an unlimited-length sequence of Java letters and Java digits, the first of which must be a Java letter.

```
Identifier:

IdentifierChars but not a Keyword or BooleanLiteral or NullLiteral

IdentifierChars:

JavaLetter {JavaLetterOrDigit}

JavaLetter:

any Unicode character that is a "Java letter"

JavaLetterOrDigit:

any Unicode character that is a "Java letter-or-digit"
```

A "Java letter" is a character for which the method Character.isJavaIdentifierStart(int) returns true.

A "Java letter-or-digit" is a character for which the method Character.isJavaIdentifierPart(int) returns true.

The "Java letters" include uppercase and lowercase ASCII Latin letters A=Z (\\\u00041-\\\u0005a), and a=z (\\\u00051-\\\u0007a), and, for historical reasons, the ASCII underscore (_, or \\\\u0005£) and dollar sign (\$, or \\\\u00024). The \$\$ sign should be used only in mechanically generated source code or, rarely, to access pre-existing names on legacy systems.

The "Java digits" include the ASCII digits 0-9 (\u0030-\u0039).

Letters and digits may be drawn from the entire Unicode character set, which supports most writing scripts in use in the world today, including the large sets for Chinese, Japanese, and Korean. This allows programmers to use identifiers in their programs that are written in their native languages.

An identifier cannot have the same spelling (Unicode character sequence) as a keyword (§3.9), boolean literal (§3.10.3), or the null literal (§3.10.7), or a compile-time error occurs.

Two identifiers are the same only if they are identical, that is, have the same Unicode character for each letter or digit. Identifiers that have the same external appearance may yet be different.

Spot the syntax error

```
{
x = 1;
y = 2;
z = 1+2
```

Subtle example 1:

```
Block ::= { Statements }
Statements ::= Statement ; Statements
               Statement
Statement ::= V-name = Expression
              Identifier (Expression)
```

Subtle example 2:

```
Block ::= { Statements }
Statements ::= Statement Statements
              Statement
Statement := V-name = Expression;
             Identifier (Expression);
```

Subtle example 3:

Table 1.1 Language evaluation criteria and the characteristics that affect them

Characteristic	CRITERIA		
	READABILITY	WRITABILITY	RELIABILITY
Simplicity	•	•	•
Orthogonality	•	•	•
Data types	11.01	•	•
Syntax design	•	•	•
Support for abstraction		•	•
Expressivity		•	•
Type checking			•
Exception handling			•
Restricted aliasing			•

Subtle example 4:

Bad example 4:

BNF Fundamentals

- In BNF, abstractions are used to represent classes of syntactic structures—they act like syntactic variables (also called *nonterminal symbols*, or just *nonterminals*)
- Terminals are lexemes or tokens
- A rule has a left-hand side (LHS), which is a nonterminal, and a right-hand side (RHS), which is a string of terminals and/or nonterminals
- Nonterminals are often enclosed in angle brackets
 - Examples of BNF rules:
 <ident_list> → identifier | identifier, <ident_list>
 <if stmt> → if <logic expr> then <stmt>
- Grammar: a finite non-empty set of rules
- A start symbol is a special element of the nonterminals of a grammar

Note: terminals/lexemes like if and then are often used in CFG instead of tokens if_token and then_token

BNF Rules

 An abstraction (or nonterminal symbol) can have more than one RHS

```
<stmt> → <single_stmt>
<stmt> → begin <stmt_list> end
```

Describing Lists

Syntactic lists are described using recursion

 A derivation is a repeated application of rules, starting with the start symbol and ending with a sentence (all terminal symbols)

Pause

An Example Grammar

An Example Derivation

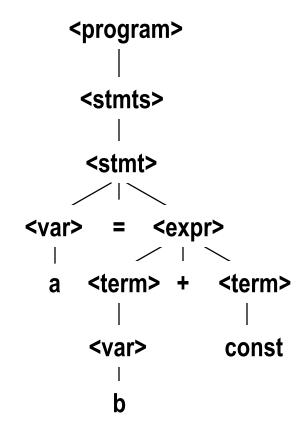
```
<stmt> → <stmt> | <stmt> ; <stmt> 
    <stmt> → <stmt> | <stmt> ; <stmt> 
    <stmt> → <var> = <expr> 
    <var> → a | b | c | d 
    <expr> → <term> + <term> | <term> - <term> 
    <term> → <var> | const
```

Derivations

- Every string of symbols in a derivation is a sentential form
- A sentence is a sentential form that has only terminal symbols
- A leftmost derivation is one in which the leftmost nonterminal in each sentential form is the one that is expanded
- A rightmost derivation is one in which the rightmost nonterminal in each sentential form is the one that is expanded
- A derivation may be neither leftmost nor rightmost

Parse Tree

A hierarchical representation of a derivation

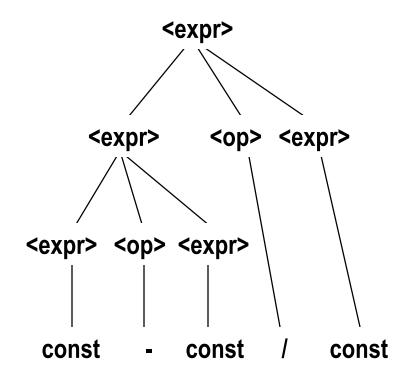


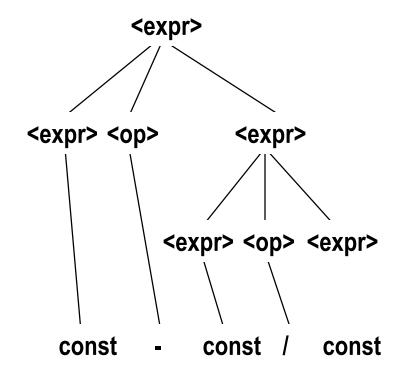
Ambiguity in Grammars

 A grammar is ambiguous if and only if it generates a sentential form that has two or more distinct parse trees

An Ambiguous Expression Grammar

$$\rightarrow$$
 | const
 \rightarrow / | -

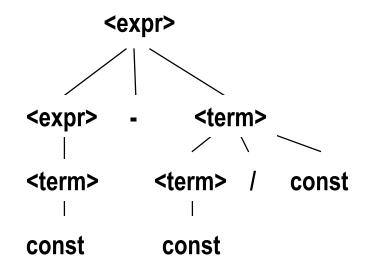




An Unambiguous Expression Grammar

 If we use the parse tree to indicate precedence levels of the operators, we cannot have ambiguity

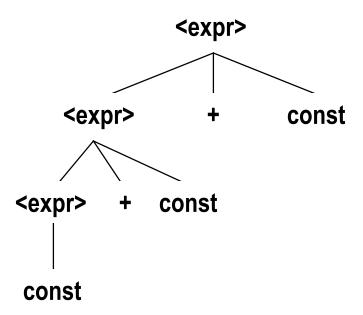
```
<expr> → <expr> - <term> | <term>
<term> → <term> / const| const
```



Associativity of Operators

Operator associativity can also be indicated by a grammar

```
<expr> -> <expr> + <expr> | const (ambiguous)
<expr> -> <expr> + const | const (unambiguous)
```



Extended BNF

Optional parts are placed in brackets []

```
call> -> ident [(<expr_list>)]
```

 Alternative parts of RHSs are placed inside parentheses and separated via vertical bars

```
\langle \text{term} \rangle \rightarrow \langle \text{term} \rangle (+|-) \text{ const}
```

Repetitions (0 or more) are placed inside braces { }

```
<ident> → letter {letter|digit}
```

BNF and **EBNF**

BNF

EBNF

```
<expr> → <term> { (+ | -) <term>}
<term> → <factor> { (* | /) <factor>}
```

Recent Variations in EBNF

- Alternative RHSs are put on separate lines
- Use of a colon or = or := instead of \rightarrow
- Use of opt for optional parts
- Use of one of for choices
- Sometimes terminal (lexems or tokens) are written in " " or ` ` or in bold or color ..
- Sometimes given in a seperate grammar and the non-terminals from this grammer is used as terminal in the CFG
- Sometimes ()* is used for { } and ? for []

BNF and **EBNF**

BNF

EBNF

```
\langle expr \rangle \rightarrow \langle term \rangle ((+ | -) \langle term \rangle) *
\langle term \rangle \rightarrow \langle factor \rangle ((* | /) \langle factor \rangle) *
```

EBNF in EBNF

```
Production = production_name "=" [ Expression ] "." .

Expression = Alternative { "|" Alternative } .

Alternative = Term { Term } .

Term = production_name | token [ "..." token ] | Group | Option | Repetition .

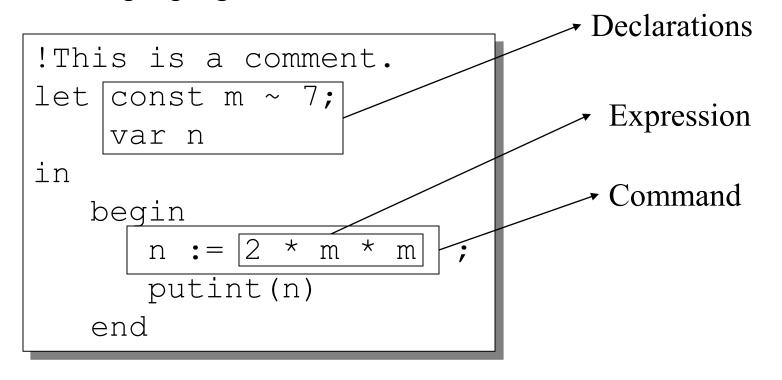
Group = "(" Expression ")" .

Option = "[" Expression "]" .

Repetition = "{" Expression "}" .
```

An Example Language Specification

Mini Triangle is a very simple Pascal-like language introduced in Brown & Watt's book: Language Processors in Java An example program:



Syntax of Mini Triangle

```
Program ::= single-Command
single-Command
      ::= V-name := Expression
          Identifier (Expression)
          if Expression then single-Command
                        else single-Command
          while Expression do single-Command
          let Declaration in single-Command
          begin Command end
Command ::= single-Command
            Command ; single-Command
```

Syntax of Mini Triangle (continued)

```
Expression
  ::= primary-Expression
      Expression Operator primary-Expression
primary-Expression
  ::= Integer-Literal
      V-name
     Operator primary-Expression
      (Expression)
V-name ::= Identifier
Identifier ::= Letter
               Identifier Letter
               Identifier Digit
Integer-Literal ::= Digit
                    Integer-Literal Digit
Operator ::= + | - | * | / | < | > |
```

Syntax of Mini Triangle (continued)

```
Declaration
    ::= single-Declaration
    | Declaration ; single-Declaration
    single-Declaration
    ::= const Identifier ~ Expression
    | var Identifier ::= Type-denoter
Type-denoter ::= Identifier
```

```
Comment ::= ! CommentLine eol

CommentLine ::= Graphic CommentLine

Graphic ::= any printable character or space
```

Concrete Syntax of Commands

```
single-Command
      ::= V-name := Expression
          Identifier (Expression)
          if Expression then single-Command
                        else single-Command
          while Expression do single-Command
          let Declaration in single-Command
          begin Command end
Command ::= single-Command
            Command ; single-Command
```

Abstract Syntax of Commands

An abstract syntax, like the above, is often used in the definition of the formal semantics

Even more Abstract Syntax of Commands

Command

- ::= V-name Expression AssignCmd
 - Identifier Expression CallCmd
 - | Expression Command Command IfCmd
 - Expression Command WhileCmd

 - | Command Command

SequentialCmd

An abstract syntax, like the above, may form the basis for the design of the AST

Contextual Constraints

Syntax rules alone are not enough to specify the format of well-formed programs.

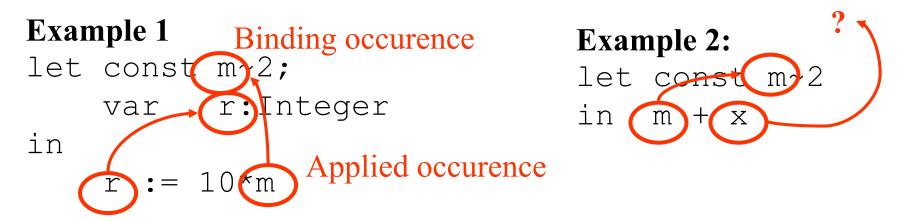
Example 1:



Example 2:

Scope Rules

Scope rules regulate visibility of identifiers. They relate every **applied occurrence** of an identifier to a **binding occurrence**



Terminology:

Static binding vs. dynamic binding

Type Rules

Type rules regulate the expected types of arguments and types of returned values for the operations of a language.

Examples

```
Type rule of < :
    E1 < E2 is type correct and of type Boolean
    if E1 and E2 are type correct and of type Integer

Type rule of while:
    while E do C is type correct
    if E of type Boolean and C type correct</pre>
```

Terminology:

Static typing vs. dynamic typing

Specification of semantics is concerned with specifying the "meaning" of well-formed programs.

Terminology:

Expressions are evaluated and yield values (and may or may not perform side effects)

Commands are executed and perform side effects.

Declarations are elaborated to produce bindings

Side effects:

- change the values of variables
- perform input/output

Example: The semantics of expressions.

An expression is evaluated to yield a value.

An (integer literal expression) IL yields the integer value of IL

The (variable or constant name) expression V yields the value of the variable or constant named V

The (binary operation) expression $E1 \circ E2$ yields the value obtained by applying the binary operation \circ to the values yielded by (the evaluation of) expressions E1 and E2

etc.

Example: The semantics of declarations.

A declaration is elaborated to produce bindings. It may also have the side effect of allocating (memory for) variables.

The constant declaration const $I \sim E$ is elaborated by binding the identifier value I to the value yielded by E

The constant declaration **var** *I*: *T* is elaborated by binding *I* to a newly allocated variable, whose initial value is undefined. The variable will be deallocated on exit from the let containing the declaration.

The sequential declaration D1; D2 is elaborated by elaborating D1 followed by D2 combining the bindings produced by both. D2 is elaborated in the environment of the sequential declaration overlaid by the bindings produced by D1

Example: The (informally specified) semantics of commands in Mini Triangle.

Commands are executed to update variables and/or perform input output.

```
The assignment command V := E is executed as follows:

first the expression E is evaluated to yield a value \mathbf{v}

then \mathbf{v} is assigned to the variable named V

The sequential command C1; C2 is executed as follows:
```

first the command C1 is executed then the command C2 is executed

etc.

Structured operational semantics

$$[ass_{ns}] \qquad \langle x := a, s \rangle \rightarrow s[x \mapsto \mathcal{A}[\![a]\!]s]$$

$$[skip_{ns}] \qquad \langle akip, s \rangle \rightarrow s$$

$$[comp_{ns}] \qquad \frac{\langle S_1, s \rangle \rightarrow s', \langle S_2, s' \rangle \rightarrow s''}{\langle S_1; S_2, s \rangle \rightarrow s'}$$

$$[if^{tt}_{ns}] \qquad \frac{\langle S_1, s \rangle \rightarrow s'}{\langle if \ b \ then \ S_1 \ else \ S_2, \ s \rangle \rightarrow s'} \ if \ \mathcal{B}[\![b]\!]s = \mathbf{tt}$$

$$[if^{ff}_{ns}] \qquad \frac{\langle S_2, s \rangle \rightarrow s'}{\langle if \ b \ then \ S_1 \ else \ S_2, \ s \rangle \rightarrow s'} \ if \ \mathcal{B}[\![b]\!]s = \mathbf{ff}$$

$$[while^{tt}_{ns}] \qquad \frac{\langle S, s \rangle \rightarrow s', \langle while \ b \ do \ S, \ s' \rangle \rightarrow s''}{\langle while \ b \ do \ S, \ s \rangle \rightarrow s''} \ if \ \mathcal{B}[\![b]\!]s = \mathbf{tt}$$

$$[while^{ff}_{ns}] \qquad \langle while \ b \ do \ S, \ s \rangle \rightarrow s \ if \ \mathcal{B}[\![b]\!]s = \mathbf{ff}$$

- There is no single widely acceptable notation or formalism for describing semantics
- Several needs for a methodology and notation for semantics:
 - Programmers need to know what statements mean
 - Compiler writers must know exactly what language constructs do
 - Correctness proofs would be possible
 - Compiler generators would be possible
 - Designers could detect ambiguities and inconsistencies

Semantic styles

Structural Operational Semantics

- Sebesta's book has a very narrow view
- Much better view in
 - Transitions and Trees: An introduction to structural operational semantics, Cambridge University Press

Denotational Semantics

- Based on recursive function theory
- Originally developed by Scott and Strachey (1970)

Axiomatic Semantics

- Sometimes called Hoare Logic
- Original purpose: formal program verification

Important!

- Syntax is the visible part of a programming language
 - Programming Language designers can waste a lot of time discussing unimportant details of syntax
 - But syntax <u>is</u> important syntax should convey the meaning intutively
- The language paradigm is the next most visible part
 - The choice of paradigm, and therefore language, depends on how humans best think about the problem
 - Imperative, Object Oriented, Functional, ..
 - There are no <u>right</u> models of computations just different models of computations, some more suited for certain classes of problems than others
- The most invisible part is the language semantics
 - Clear semantics usually leads to simple and efficient implementations

Before Language definition

- Write programs!!
- Serves as inspiration for language specification
 - Syntax
 - Tokens
 - CFG
 - Static semantics
 - Scope rules
 - Type rules
 - Semantics
 - Informal
 - Formal
- Serves as test case for compiler !!
- Read language specifications: C, C#, Java, ...