

Development of a new Baseline Assessment for the South African Hake resource, Incorporating catch-at-length information

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INTRODUCTION

Results are presented for a proposed new baseline assessment for the South African hake resource, incorporating catchat-length (CAL) information in the fit of the model. In years for which age-length keys are not available, CAL information is used instead of catches-at-age (CAA) which had been previously based on averages of age-length keys for other years (a problematic and potentially biased approach). Further changes to the model and the data that have been made are described below.

DATA and METHODOLOGY

The data used in the new proposed baseline, but not in the 2008 baseline (as described in Rademeyer and Butterworth, 2008) are listed in Appendix A.

Updates to the model from the 2008 baseline assessment:

I. Using Pope's approximation

To speed model fitting, Pope's approximation for the catch equations was used rather than Baranov's equation.

II. Incorporating catch-at-length information

Appendix B sets out how CAL information is taken into account in the model fitting.

III. Estimating west coast winter survey selectivity for M. paradoxus

In previous assessments, the selectivity-at-age for this survey and species was assumed to be the same as that for the west coast summer survey because no west coast winter survey CAA data for *M. paradoxus* were available. Some age and length data are now available for these west coast surveys so that a different selectivity is estimated for the two seasons for *M. paradoxus* (as is done for *M. capensis*).

IV. Fitting to commercial coast-specific information

Previously, the model fit was coast-specific only for the survey data, while GLM-standardized CPUE, commercial catches and CAA information were combined across the two coasts and a single selectivity-at-age vector (for each fleet) was assumed to apply. The model is now fit to coast-specific commercial information. This was carried out by treating the offshore trawl fleet on the south and west coasts as two different fleets, with potentially different selectivities-at-age, and similarly for the longline fleet. The model therefore now includes six fleets:

- 1) west coast offshore fleet (catching M. paradoxus and M. capensis);
- 2) south coast offshore fleet (catching M. paradoxus and M. capensis);
- 3) south coast inshore fleet (catching *M. capensis* only);

- 4) west coast longline fleet (catching *M. paradoxus* and *M. capensis*);
- 5) south coast longline fleet (catching M. capensis only); and
- 6) south coast handline fleet (catching *M. capensis* only).

The annual catches of each species assumed for each of these six fleets are shown in Table App.A.1, while the commercial age and length information is shown in Tables App.A.11-15. As age/length information is not available disaggregated by species and therefore not available for each species/fleet combination, fishing selectivity-at-age cannot be estimated directly for all fleets and some assumptions have to be made. Details of the fishing selectivities used in the assessment are shown in Table 1.

V. Different selectivity for the Africana surveys with new gear

A different selectivity is estimated for the *Africana* with new gear, for the west coast summer and south coast (spring and autumn) surveys. As for the other survey selectivities, the *Africana* new gear selectivity is estimated separately for each age, from age 0 to 5+/7+ for *M. paradoxus* and *M. capensis* respectively. However, because the information available is length-based and only 3 or 4 years of data are available, a smoothing penalty was added to the negative log-likelihood in the fitting process to prevent unrealistically large variations in selectivity from one age to the next:

S_penalty =
$$\sum_{a=1}^{z-1} 3(S_{a-1} - 2S_a + S_{a+1})^2$$
 (1)

The initial 3 multiplicative factor is a somewhat arbitrary weighting to ensure reasonable smoothness of the selectivity. For consistency, this smoothing penalty was also used for the old gear selectivity.

VI. Further three years of offshore commercial catch-at-length

Offshore trawl (species combined) CAL information has become available for 2005 to 2007 and has been taken into account in fitting the model. This is however only available combined across coasts, and is therefore compared to the predicted coast combined CAL, weighted by the actual catch on each coast.

RESULTS AND DISCUSSION

Table 2 compares estimates of management quantities for the 2008 baseline and the proposed new baseline assessment, while Fig. 1 plots the spawning biomass trajectories. For both *M. paradoxus* and *M. capensis*, the spawning biomass in absolute terms is estimated to be larger in the proposed new baseline assessment than in the 2008 baseline assessment. Relative to pre-exploitation levels however, spawning biomass is not much affected by the changes made.

Fig. 2 plots the estimated selectivities-at-age for the commercial fleets and the surveys. The new gear on the *Africana* is estimated to catch slightly smaller fish than the old gear, particularly for *M. capensis*.

Figs 3 and 4 show the fits the CPUE and survey abundance series. The fits to these data are generally good.

The fits to the commercial CAA and CAL data are show in Fig. 5. The fits are poor for certain CAL (West Coast Offshore, Both Coasts Offshore particularly, and the inshore *M. capensis* CAA). The likely reason for this is a conflict between the CAA and CAL information. For example, for the offshore trawl fleet (west coast and both coasts) the observed length distribution of the catch is very narrow compared to a relatively wide range of ages observed in the CAA.

As described in Appendix B, a selectivity-at-length effect had to be incorporated to allow for a reasonable fit of the survey CAL data. The effects on the estimated CAL distributions by age are shown in Fig. 6 for each species and survey. For both species, the effect is negligible for the south coast spring survey and greatest on the west coast surveys. The actual fits to the survey CAA and CAL are shown in Fig. 7. The fits are particularly poor for the *M. capensis* west coast summer CAL and south coast *M. paradoxus*, again likely due to a conflict between the CAA and CAL information. Note that the selectivity on the south coast is assumed to be the same for the spring and autumn surveys.

Fig. 8 plots the standardised stock-recruitment residuals and the estimated stock-recruitment relationships for M. paradoxus and M. capensis. Note that the "SR2" option is still used, with σ_R linearly decreasing from 0.25 to 0.1 over the 2004 to 2008 period.

The spawning biomass trajectories for two retrospective assessments are compared to those estimated in the proposed new baseline assessment (Fig. 9). For the retrospective analysis, the assessments are still run to 2008 but are fitted to data up to 2007 ("data to 2007") and 2006 ("data to 2006"). A small retrospective pattern is apparent for *M. capensis* but not for *M. paradoxus*. There is a slight upturn in spawning biomass for both species from 2006 to 2007, which is likely a reflection of better recruitment indicated for recent years compared to the low values from the mid-1990s to 2003 (see Fig. 8).

An interesting feature of the new baseline assessment is that the estimates of natural mortality at age (see Table 2) are lower, which seems more realistic biologically.

The proposed new baseline assessment will be used for the sensitivities analyses to be conducted in the light of discussions during the WG meetings. While this new baseline is not entirely satisfactory given the misfits to some of the catch-at-length data, this does seem to be arising primarily from data conflicts which alternative models will not resolve at this stage. Further resolution attempts seem better to wait for analyses that treat the age readings in a better statistical manner, perhaps also distinguishing the sexes with their different growth curves.

REFERENCES

Rademeyer RA and Butterworth DS. 2008. 2008 routine update of the South African hake baseline assessment. Unpublished report, Marine and Coastal Management, South Africa. MCM/2008/SEPT/SWG-DEM/48. (13pp)

Table 1: Details for the commercial selectivity-at-age for each fleet and species combination, as well as indications of what data are available, for the proposed new baseline assessment.

		M. paradoxus	M. capensis	data available
1. West coast offshore	1917-1976	set equal to 1989	set equal to 1989	
	1977-1984	logistic, two parameters estimated slope estimated	same shift as paradoxus zero slope	species combined
	1985-1992	linear change between 1	984 and 1993 selectivity	species combined
	1993-2008	logistic, two parameters estimated slope estimated	same as SC inshore but shifted to the right by 1 year, zero slope	species combined
2. South coast offshore	1917-1976	set equal to 1989	set equal to 1989	
	1977-1984	same shift as west coast slope as 1993-2008	same shift as paradoxus zero slope	species combined
	1985-1992	linear change between 1	984 and 1993 selectivity	species combined
	1993-2008	logistic, two parameters estimated slope estimated	same as SC inshore but shifted to the right by 1 year, zero slope	species combined
3. South coast inshore			logistic, two parameters estimated slope estimated	capensis
4. West coast longline		logistic, two parameters estimated zero slope	same as South coast longline	species combined
5. South coast longline			logistic, two parameters estimated zero slope	capensis
6. South coast handline			average of South coast longline and inshore	

Table 2: Comparison of management quantities for the 2008 baseline assessment (D) and the proposed new baseline assessment. Note that the negative log likelihoods shown are not comparable as they are based on different data sets. Note that the fitting criteria used includes a penalty to encourage $M_2 > M_5$.

			2008 baseline (D)	new baseline
	-lnL total		-192.1	-40.9
	K^{sp}		1407	1821
	h		0.95	0.95
	MSY		116	114
	Bsp ₂₀₀₈ /Ksp		216	265
Si	B^{sp}_{2008}/K^{sp}		0.15	0.15
охи	$B^{sp}_{2008}/MSYL^{sp}$		0.64	0.82
M. paradoxus	MSYL sp		0.24	0.18
1. pa	MSIL M	0	0.52	0.36
N	M	0	0.52	0.36
		1	0.52	0.36
		2	0.32	0.35
		4	0.38	0.34
		5+	0.35	0.33
	K^{sp}		692	871
	h		0.95	0.95
	MSY		81	86
	B^{sp}_{2008}		434	501
	B^{sp}_{2008}/K^{sp}		0.63	0.57
S.	$B^{sp}_{2008}/MSYL^{sp}$		2.01	2.31
sua	$MSYL^{sp}$		0.31	0.25
M. capensis	M	0	1.00	0.40
, c		1	1.00	0.40
Z		2	1.00	0.40
		3	0.73	0.40
		4	0.57	0.41
		5	0.46	0.41
		6	0.46	0.41
		7+	0.46	0.41
	SC survey q		0.59	0.49
	2008 species ratio	B^{sp}	2.07	1.89
	(paradoxus/capensis)	B^{2+}	1.84	1.66

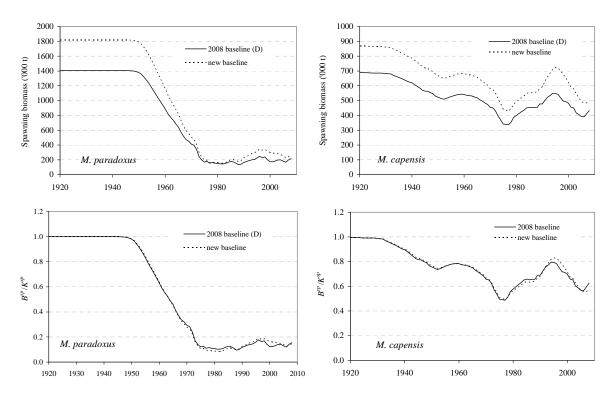


Fig. 1: *M. paradoxus* and *M. capensis s*pawning biomass trajectories for the 2008 baseline and proposed new baseline assessments.

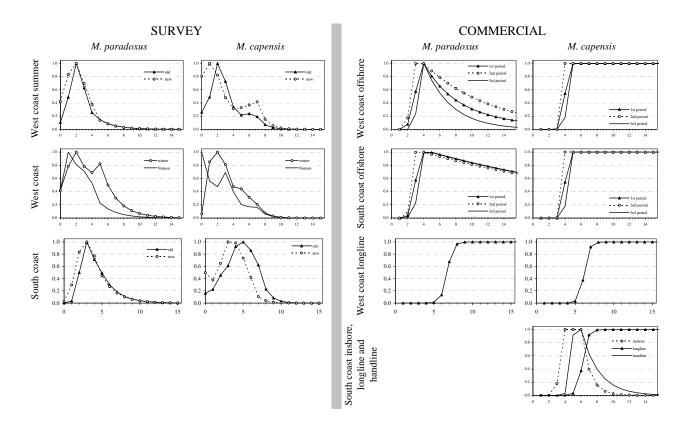


Fig. 2: Estimated survey and commercial fishing selectivities-at-age for the proposed new baseline assessment.

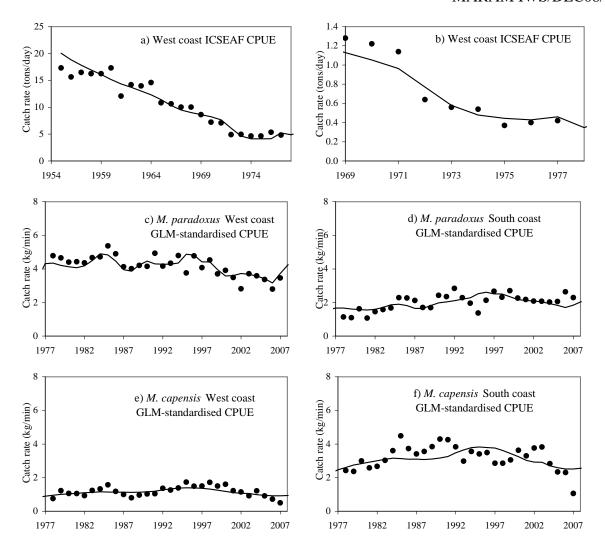


Fig. 3: Fits to the CPUE abundance indices for the proposed new baseline assessment. The historic (pre-1978) CPUE data are for both *M. capensis* and *M. paradoxus* combined.

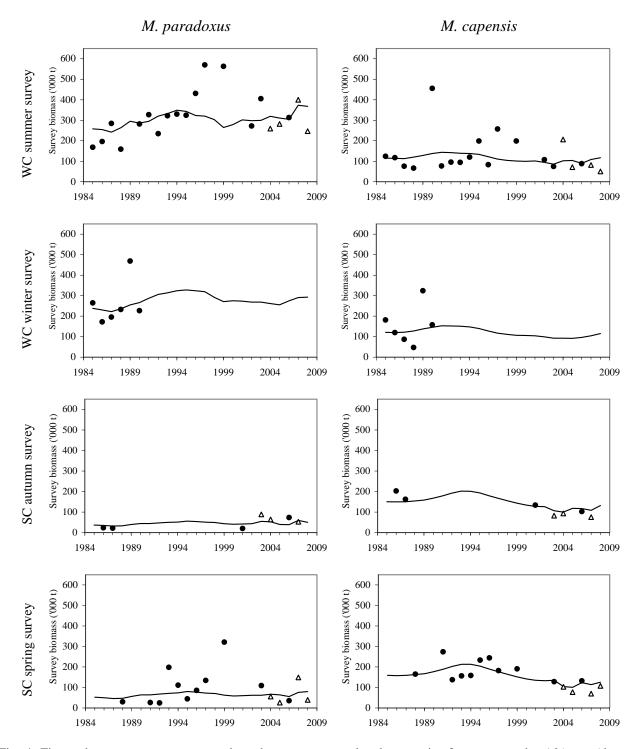


Fig. 4: Fits to the west coast summer and south coast autumn abundance series from surveys by *Africana* (the two longest series) for the proposed new baseline assessment. The observed values shown as Δ were conducted by the *Africana* with the new gear and have been rescaled by the agreed calibration factor for the species concerned (0.95 and 0.8 for *M. paradoxus* and *M. capensis* respectively). Note: the estimated survey biomass trends incorporate the change in selectivity between the old and new *Africana* gear.

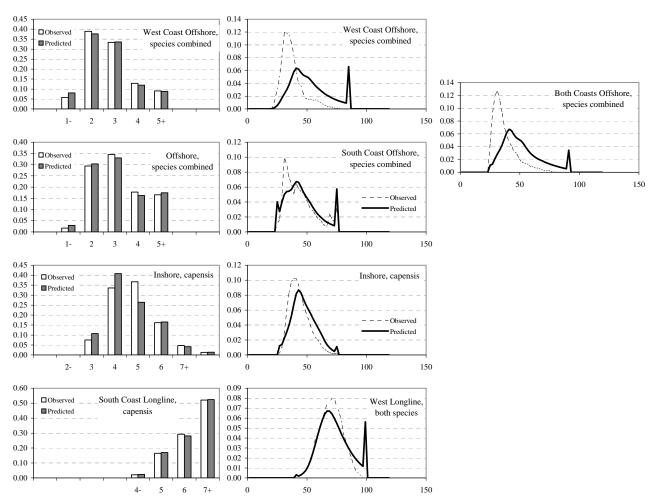


Fig. 5: Fit to the commercial CAA and CAL data for the proposed new baseline assessment.

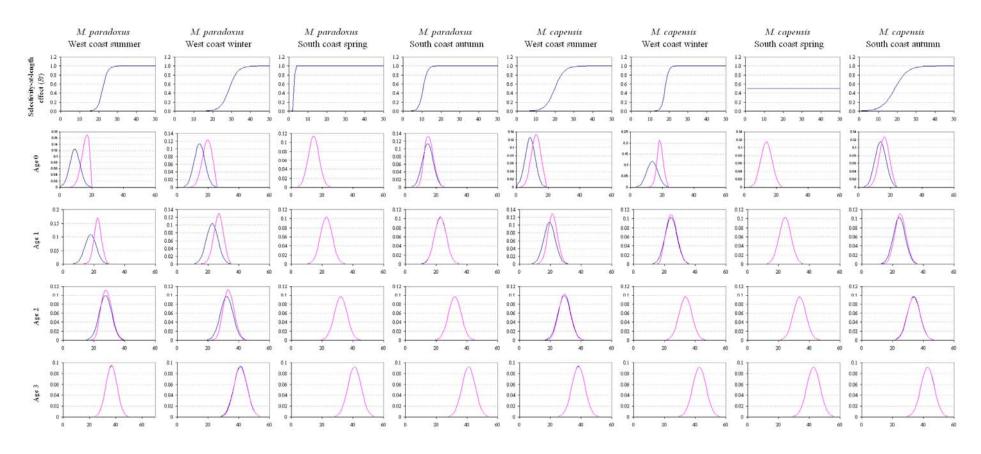


Fig 6: Survey selectivity-at-length effect in the proposed new baseline assessment (see Appendix B for details). The first row shows the R_l factor (see equation B.7), and the remaining rows show the consequent shifts in the catch-at-length distributions by age. The length units are cm.

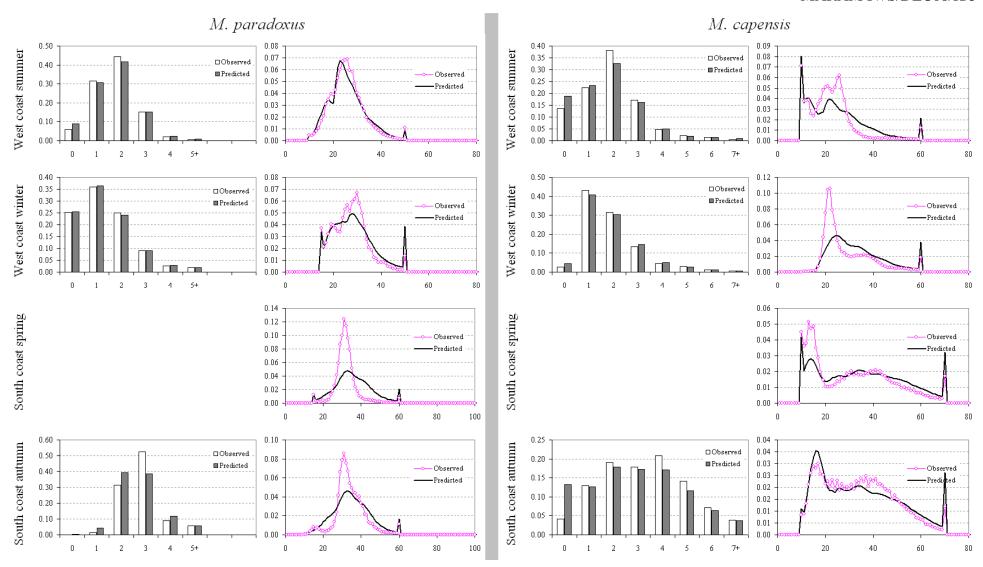


Fig. 7: Fit to survey CAA and CAL for *M. paradoxus* for the proposed new baseline assessment.

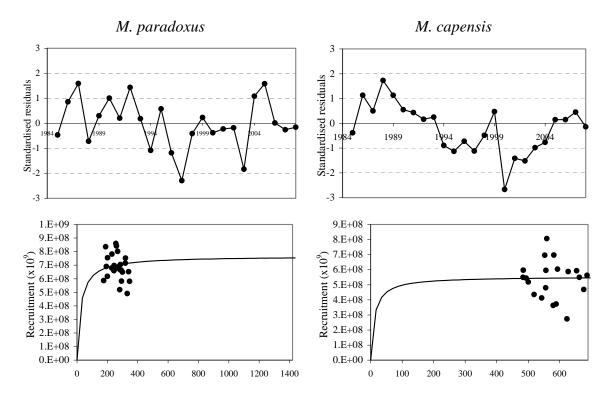


Fig. 8: Time series of standardised stock-recruitment residuals and estimated stock-recruitment relationships for the proposed new baseline assessment.

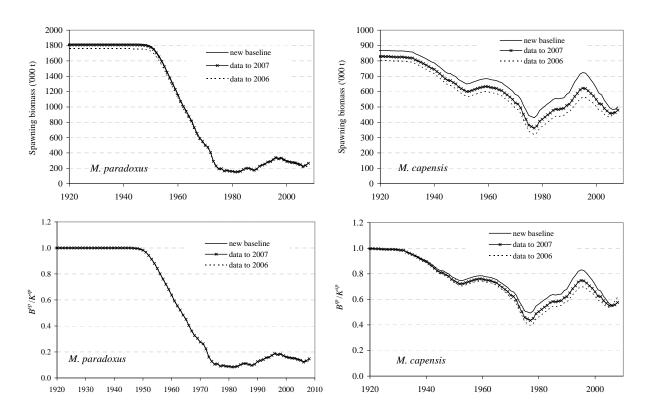


Fig. 9: *M. paradoxus* and *M. capensis s*pawning biomass trajectories for the proposed new baseline and two retrospective assessments.

Appendix B – Age data used

Table App.A.1: Assumed annual catches disaggregated by species, fleet and coast in thousand tons.

		M. paradoxus				M. caj	pensis		
	Offs	shore South Coast	Longline		shore South Coast	Inshore	Lor	igline . South Coast	Handline
1917	-	-	-	1.000	-	-	-	-	-
1918 1919	-	-	-	1.100 1.900	-	-	-	-	-
1920	-	-	-	0.000	-	-	-	-	-
1921	-	-	-	1.300	-	-	-	-	-
1922 1923	-	-	-	1.000 2.500	-	-	-	-	-
1924	-	-	-	1.500	-	-	-	-	-
1925 1926	-		-	1.900 1.400			-	-	-
1927	-	-	-	0.800	-	-	-	-	-
1928 1929	-	-	-	2.600 3.800	-	-	-	-	-
1930	-	-	-	4.400	-	-	-	-	-
1931	-	-	-	2.800	-	-	-	-	-
1932 1933	-	-	-	14.300 11.100	-	-	-	-	-
1934	-	-	-	13.800	-	-	-	-	-
1935 1936	0.001 0.001		-	14.999 17.699	-	-	-	-	-
1937	0.003		-	20.197	-	-	-	-	-
1938	0.005	-	-	21.095	-	-	-	-	-
1939 1940	0.010 0.028		-	19.990 28.572	-	-		-	-
1941	0.057	-	-	30.543	-	-	-	-	-
1942 1943	0.126 0.268	-	-	34.374 37.632	-	-	-	-	-
1944	0.465	-	-	33.635	=	-	-	-	-
1945	0.763	÷	-	28.437	÷	=	-	-	-
1946 1947	1.991 3.743	=	-	38.409 37.657	-	-	-	-	-
1948	9.304	-	-	49.496	-	-	-	-	-
1949 1950	14.770 27.306		-	42.630 44.694	-	-	-	-	-
1951	44.856	-	-	44.644	-	-	-	-	-
1952	53.304	-	-	35.496 31.034	-	-	-	-	-
1953 1954	62.466 74.752	-	-	30.648	-	-	-	-	-
1955	84.517	-	-	30.883	-	-	-	-	-
1956 1957	88.043 94.982	-	-	30.157 31.418	-	-	-	-	-
1958	98.660	-	-	32.040	-	-	-	-	-
1959	110.468	-	-	35.532	-	-	-	-	-
1960 1961	121.131 112.716	-	-	38.769 35.984	-	1.000 1.308	-	-	-
1962	111.918	-	-	35.682	-	1.615	-	-	-
1963 1964	128.545 123.095	-	-	40.955 39.205	-	1.923 2.231	-	-	-
1965	153.970	-	-	49.030	-	2.538	-	-	-
1966 1967	147.905 134.026	- 5.661	-	47.095 42.674	8.525	2.846 3.154	-	-	-
1968	108.921	11.136	-	34.679	16.772	3.462	-	-	-
1969	125.229	15.136	-	39.871	22.795	3.769	-	-	-
1970 1971	108.087 153.218	9.466 12.017	-	34.413 48.782	14.257 18.098	4.077 4.385	-	-	-
1972	185.025	18.633	-	58.908	28.062	4.692	-	-	-
1973 1974	119.679 93.296	28.873 36.254	-	38.103 29.704	43.483 54.599	5.000 10.056	-	-	-
1975	67.975	26.920	-	21.642	40.543	6.372	-	-	-
1976 1977	109.144 77.616	20.722 14.753	-	34.750 24.712	31.208 22.219	5.740 3.500	-	-	-
1977	104.093	4.017	-	23.414	3.574	4.931	-	-	-
1979	95.374	2.759	-	38.149	4.161	6.093	-	-	-
1980 1981	100.766 91.599	2.948 1.301	-	32.766 29.333	3.508 4.182	9.121 9.400	-		-
1982	84.990	4.240	-	28.359	7.118	8.089	-	-	-
1983 1984	71.202 81.804	6.124 4.843	0.161 0.256	23.231 29.451	6.392 6.092	7.672 9.035	0.069 0.110	0.016	-
1985	91.090	10.442	0.817	33.980	9.574	9.203	0.350	0.292	0.065
1986 1987	103.405	10.214	0.965 2.500	30.401	5.751	8.724	0.413	0.302	0.084
1987	94.724 82.964	9.269 7.424	3.628	22.801 23.601	6.415 7.108	8.607 8.417	1.071 1.555	0.353	0.096 0.071
1989	82.543	7.619	0.203	24.653	11.355	10.038	0.087	0.032	0.137
1990 1991	76.684 86.151	11.995 13.997	0.270	26.884 20.288	10.865 8.087	10.012 8.206	0.116	3.000	0.348 1.270
1992	81.782	20.020	-	21.503	6.444	9.252	-	1.500	1.099
1993	101.964	11.086	-	16.100	3.175	8.870	-	0.626	0.278
1994 1995	104.326 93.332	7.601 4.552	1.130 0.670	19.541 27.564	3.451 2.598	9.569 10.630	0.484 0.287	0.626 0.650	0.449 0.756
1996	109.817	9.759	1.676	19.358	3.530	11.062	0.718	1.828	1.515
1997 1998	99.873 110.854	11.904 10.796	1.806 0.647	17.281 16.799	3.932 3.357	8.834 8.283	0.774 0.277	1.872 1.471	1.404 1.738
1999	87.507	12.435	1.963	16.254	2.911	8.595	0.841	4.144	2.749
2000	96.180	7.800	3.456	23.058	4.193	10.906	1.481	2.077	5.500
2001 2002	108.121 89.560	6.107 12.637	2.793 4.772	16.693 19.223	2.832 2.095	11.836 9.581	1.197 2.045	1.688 3.945	7.300 3.500
2003	98.976	16.342	4.668	11.837	3.255	9.883	2.000	4.878	3.000
2004 2005	91.749 89.185	23.254 21.896	3.758	14.067 9.712	3.931	10.004 7.881	1.611	4.429 4.559	1.600 0.700
2005	90.074	14.524	4.172 3.592	9.712	3.720 3.142	5.524	1.788 1.539	4.032	0.400
2007	97.210	15.675	3.151	9.920	3.391	6.350	1.350	3.834	0.400
2008	89.792	14.479	2.910	9.163	3.132	5.865	1.247	3.541	0.369

Table App.A.2: South and west coast historic and GLM standardized CPUE data (Glazer, 2008) for *M. paradoxus* and *M. capensis*. The historic CPUE series are for *M. capensis* and *M. paradoxus* combined.

	ICSEAF CP	UE (tons/hr)		GLM CPU	JE (kg/min)	GLM CPU	JE (kg/min)
	Species-a	ggregated		M. capensis	M. paradoxus	M. capensis	M. paradoxus
Year	South Coast	West Coast	Year	Wes	t coast	South	h coast
1955		17.31	1978	0.75	4.79	2.42	1.14
1956		15.64	1979	1.22	4.66	2.37	1.10
1957		16.47	1980	1.06	4.40	3.00	1.63
1958		16.26	1981	1.05	4.43	2.58	1.07
1959		16.26	1982	0.93	4.36	2.67	1.45
1960		17.31	1983	1.24	4.67	3.03	1.58
1961		12.09	1984	1.32	4.72	3.61	1.68
1962		14.18	1985	1.57	5.37	4.49	2.29
1963		13.97	1986	1.18	4.90	3.73	2.27
1964		14.60	1987	0.99	4.13	3.41	2.13
1965		10.84	1988	0.80	4.01	3.56	1.70
1966		10.63	1989	0.96	4.21	3.85	1.70
1967		10.01	1990	1.03	4.15	4.30	2.42
1968		10.01	1991	1.04	4.93	4.25	2.36
1969	1.28	8.62	1992	1.37	4.16	3.83	2.84
1970	1.22	7.23	1993	1.26	4.34	2.98	2.29
1971	1.14	7.09	1994	1.38	4.80	3.56	1.96
1972	0.64	4.90	1995	1.73	3.76	3.41	1.38
1973	0.56	4.97	1996	1.49	4.78	3.49	2.14
1974	0.54	4.65	1997	1.50	4.08	2.86	2.67
1975	0.37	4.66	1998	1.72	4.54	2.85	2.31
1976	0.40	5.35	1999	1.50	3.70	3.06	2.70
1977	0.42	4.84	2000	1.60	3.91	3.63	2.27
			2001	1.22	3.50	3.30	2.18
			2002	1.15	2.82	3.76	2.08
			2003	0.92	3.72	3.82	2.08
			2004	1.21	3.59	2.83	2.02
			2005	0.91	3.37	2.33	2.06
			2006	0.71	2.80	2.31	2.64
			2007	0.50	3.46	1.06	2.29

Table App.A.3: Summer survey catches-at-age (proportions) of *M. capensis* and *M. paradoxus* on the west coast for the 0-500m depth range. Here and in the following tables, the data to which the proposed new baseline assessment (with CAL) is NOT fitted to are shown in light grey. Data that were not included in the 2008 baseline assessment (D) (Rademeyer and Butterworth, 2008) are shaded.

				М. сај	pensis						M. par	adoxus		
Age	0	1	2	3	4	5	6	7+	0	1	2	3	4	5+
1986	0.034	0.230	0.603	0.085	0.023	0.014	0.008	0.003	-	-	-	-	-	-
1987	0.024	0.113	0.465	0.223	0.139	0.022	0.010	0.004	-	-	-	-	-	-
1988	0.280	0.483	0.135	0.059	0.018	0.015	0.009	0.002	0.234	0.568	0.171	0.014	0.004	0.009
1989	-	-	-	-	-	-	-	-	-	-	-	-	-	-
1990	0.004	0.325	0.635	0.023	0.009	0.003	0.001	0.000	0.029	0.310	0.492	0.158	0.009	0.002
1991	0.072	0.122	0.644	0.097	0.038	0.017	0.009	0.002	0.018	0.278	0.561	0.107	0.024	0.008
1992	0.131	0.260	0.313	0.162	0.078	0.025	0.019	0.010	0.010	0.383	0.485	0.082	0.023	0.012
1993	0.038	0.176	0.207	0.399	0.088	0.057	0.024	0.011	0.009	0.200	0.547	0.187	0.044	0.010
1994	0.081	0.253	0.208	0.262	0.075	0.054	0.048	0.020	0.011	0.244	0.551	0.166	0.017	0.008
1995	0.001	0.147	0.739	0.066	0.021	0.018	0.005	0.003	0.065	0.191	0.444	0.258	0.028	0.010
1996	0.065	0.368	0.205	0.237	0.066	0.023	0.025	0.011	0.057	0.394	0.302	0.210	0.030	0.005
1997	0.036	0.141	0.384	0.407	0.014	0.010	0.004	0.003	0.006	0.171	0.546	0.256	0.016	0.003
1998	-	-	-	-	-	-	-	-	-	-	-	-	-	-
1999	0.867	0.059	0.024	0.026	0.011	0.008	0.005	0.001	0.161	0.410	0.336	0.081	0.008	0.003
2000	-	-	-	-	-	-	-	-	-	-	-	-	-	-
2001	-	-	-	-	-	-	-	-	-	-	-	-	-	-
2002	0.198	0.441	0.230	0.070	0.032	0.019	0.007	0.002	0.076	0.373	0.380	0.132	0.028	0.012
2003	0.247	0.209	0.254	0.156	0.046	0.047	0.032	0.009	0.063	0.322	0.400	0.181	0.023	0.012
2004	0.110	0.457	0.359	0.064	0.007	0.002	0.001	0.001	0.175	0.307	0.321	0.152	0.035	0.011
2005	0.679	0.092	0.133	0.076	0.012	0.005	0.002	0.001	0.218	0.493	0.208	0.069	0.009	0.003
2006	0.446	0.325	0.169	0.042	0.008	0.005	0.003	0.001	0.073	0.321	0.440	0.144	0.017	0.005
2007	0.057	0.144	0.533	0.236	0.018	0.006	0.003	0.003	0.074	0.341	0.372	0.175	0.031	0.008

Table App.A.4: Winter survey catches-at-age (proportions) of *M. capensis* and *M. paradoxus* on the west coast for the 0-500m depth range.

				М. сај	pensis						M. par	adoxus		
Age	0	1	2	3	4	5	6	7+	0	1	2	3	4	5+
1986	0.005	0.305	0.267	0.318	0.051	0.027	0.017	0.010	-	-	-	-	-	-
1987	0.010	0.477	0.202	0.171	0.072	0.048	0.011	0.009	-	-	-	-	-	-
1988	0.031	0.432	0.388	0.063	0.042	0.029	0.012	0.004	0.176	0.431	0.298	0.077	0.013	0.006
1989	0.079	0.676	0.213	0.022	0.008	0.001	0.001	0.000	-	-	-	-	-	-
1990	0.006	0.267	0.514	0.098	0.052	0.042	0.013	0.008	0.329	0.290	0.202	0.105	0.041	0.032

Table App.A.5: *Nansen* summer survey catches-at-age (proportions) of *M. capensis* and *M. paradoxus* on the west coast for the 0-500m depth range.

				М. сар	pensis					M. par	adoxus			
Age	0	1	2	3	4	5	6	7+	0	1	2	3	4	5+
2000	0.393	0.336	0.147	0.111	0.007	0.004	0.002	0.001	0.261	0.460	0.204	0.056	0.015	0.004
2001	0.493	0.109	0.157	0.157	0.050	0.018	0.009	0.007	0.199	0.378	0.237	0.143	0.031	0.011

Table App.A.6: Spring survey catches-at-age (proportions) of *M. capensis* and *M. paradoxus* on the south coast for the 0-500m depth range.

				М. са	pensis						M. par	adoxus		
Age	0	1	2	3	4	5	6	7+	0	1	2	3	4	5+
2001	0.158	0.106	0.091	0.171	0.264	0.139	0.039	0.033	0.007	0.085	0.518	0.369	0.015	0.006
2002	-	-	-	-	-	-	-	-	-	-	-	-	-	-
2003	0.192	0.139	0.151	0.163	0.170	0.117	0.039	0.029	0.000	0.026	0.448	0.463	0.035	0.029
2004	0.457	0.103	0.109	0.122	0.104	0.067	0.021	0.016	0.034	0.034	0.358	0.499	0.042	0.033

Table App.B.7: Autumn survey catches-at-age (proportions) of *M. capensis* and *M. paradoxus* on the south coast for the 0-500m depth range.

				М. сар	pensis						M. par	adoxus		
Age	0	1	2	3	4	5	6	7+	0	1	2	3	4	5+
1991	0.011	0.111	0.126	0.173	0.215	0.181	0.112	0.073	0.004	0.010	0.522	0.292	0.116	0.056
1992	0.015	0.203	0.358	0.145	0.118	0.110	0.038	0.014	0.000	0.001	0.370	0.541	0.065	0.024
1993	0.001	0.083	0.120	0.171	0.373	0.143	0.068	0.042	0.000	0.005	0.416	0.544	0.026	0.010
1994	0.061	0.140	0.123	0.219	0.137	0.159	0.116	0.045	0.005	0.090	0.656	0.186	0.017	0.046
1995	0.019	0.121	0.225	0.189	0.202	0.149	0.066	0.029	0.000	0.000	0.124	0.773	0.089	0.014
1996	0.005	0.104	0.188	0.192	0.288	0.131	0.061	0.031	0.000	0.000	0.097	0.749	0.100	0.054
1997	0.064	0.134	0.105	0.187	0.216	0.175	0.067	0.052	0.000	0.001	0.111	0.581	0.105	0.202
1998	-	-	-	-	-	-	-	-	-	-	-	-	-	-
1999	0.159	0.140	0.281	0.145	0.117	0.087	0.040	0.030	0.000	0.014	0.216	0.527	0.190	0.054
2000	-	-	-	-	-	-	-	-	-	-	-	-	-	-
2001	0.149	0.112	0.085	0.175	0.279	0.137	0.036	0.027	0.006	0.053	0.444	0.462	0.027	0.007
2002	-	-	-	-	-	-	-	-	-	-	-	-	-	-
2003	0.109	0.214	0.195	0.142	0.161	0.116	0.035	0.028	0.008	0.023	0.385	0.530	0.034	0.020
2004	0.130	0.103	0.132	0.187	0.228	0.141	0.045	0.034	0.029	0.115	0.350	0.438	0.060	0.008
2005	0.110	0.159	0.169	0.161	0.216	0.126	0.035	0.023	0.065	0.142	0.240	0.370	0.130	0.053
2006	0.030	0.072	0.194	0.264	0.232	0.123	0.047	0.037	0.001	0.012	0.314	0.582	0.073	0.018
2007	0.250	0.250	0.169	0.157	0.112	0.044	0.011	0.008	0.050	0.039	0.191	0.501	0.197	0.022

Table App.A.8: Offshore trawl fleet catches-at-age (M. capensis and M. paradoxus combined) for west and south coasts.

			West	coast, spe	ecies con	nbined					Sou	th coast, sp	ecies comb	ined		
Age	0	1	2	3	4	5	6	7+	0	1	2	3	4	5	6	7+
1978	0.000	0.072	0.716	0.152	0.039	0.016	0.005	0.001	0.000	0.058	0.570	0.249	0.073	0.028	0.013	0.009
1979	0.000	0.114	0.545	0.215	0.064	0.046	0.013	0.004	0.000	0.000	0.077	0.235	0.256	0.240	0.111	0.082
1980	0.000	0.056	0.472	0.289	0.112	0.048	0.017	0.008	0.000	0.027	0.419	0.272	0.144	0.067	0.039	0.032
1981	0.004	0.235	0.492	0.158	0.068	0.026	0.011	0.006	0.000	0.024	0.270	0.331	0.227	0.085	0.040	0.024
1982	0.037	0.290	0.484	0.114	0.040	0.023	0.009	0.003	0.000	0.056	0.399	0.205	0.128	0.106	0.070	0.035
1983	0.001	0.121	0.488	0.238	0.085	0.044	0.016	0.007	0.000	0.031	0.376	0.302	0.136	0.088	0.049	0.017
1984	0.000	0.063	0.483	0.275	0.097	0.046	0.024	0.012	0.009	0.085	0.387	0.232	0.154	0.071	0.040	0.022
1985	0.000	0.008	0.350	0.395	0.133	0.069	0.030	0.016	0.000	0.005	0.339	0.343	0.139	0.099	0.049	0.027
1986	0.000	0.014	0.339	0.467	0.104	0.040	0.022	0.015	0.000	0.003	0.226	0.366	0.177	0.115	0.077	0.035
1987	0.000	0.023	0.524	0.276	0.103	0.048	0.016	0.009	0.000	0.002	0.398	0.258	0.135	0.111	0.065	0.032
1988	0.000	0.021	0.589	0.266	0.059	0.036	0.021	0.009	0.000	0.009	0.414	0.264	0.136	0.103	0.053	0.021
1989	0.000	0.014	0.434	0.402	0.090	0.036	0.018	0.006	0.000	0.002	0.352	0.392	0.114	0.082	0.045	0.013
1990	0.000	0.002	0.313	0.496	0.137	0.034	0.013	0.005	0.000	0.002	0.216	0.416	0.233	0.084	0.035	0.015
1991	0.000	0.003	0.253	0.357	0.233	0.087	0.049	0.019	0.000	0.003	0.281	0.414	0.181	0.066	0.040	0.015
1992	0.000	0.012	0.405	0.303	0.145	0.088	0.035	0.013	0.000	0.005	0.333	0.377	0.156	0.077	0.035	0.017
1993	0.000	0.003	0.146	0.378	0.307	0.128	0.029	0.009	0.000	0.000	0.166	0.485	0.229	0.070	0.035	0.016
1994	0.000	0.001	0.140	0.464	0.200	0.157	0.030	0.008	0.000	0.001	0.209	0.477	0.165	0.091	0.039	0.019
1995	0.000	0.001	0.109	0.552	0.207	0.075	0.044	0.012	0.000	0.002	0.100	0.473	0.252	0.070	0.067	0.037
1996	0.000	0.002	0.120	0.554	0.221	0.063	0.029	0.011	0.000	0.000	0.054	0.477	0.342	0.073	0.037	0.018

Table App.A.9: Longline fleet catches-at-age (assumed to consist of *M. capensis* only) on the south coast.

				М. са	pensis			
Age	0	1	2	3	4	5	6	7+
1994	0.000	0.000	0.000	0.001	0.030	0.248	0.404	0.318
1995	0.000	0.000	0.000	0.000	0.006	0.093	0.262	0.638
1996	0.000	0.000	0.000	0.000	0.007	0.134	0.297	0.561
1997	0.000	0.000	0.000	0.002	0.036	0.201	0.298	0.464
1998	-	-	-	-	-	-	-	-
1999	-	-	-	-	-	-	-	-
2000	0.000	0.000	0.001	0.003	0.020	0.148	0.203	0.626

Table App.A.10: Inshore fleet catches-at-age (assumed to consist of M. capensis only) on the south coast.

		_					• /	
				М. сар	pensis			
Age	0	1	2	3	4	5	6	7+
1989	0.000	0.000	0.081	0.478	0.285	0.109	0.039	0.008
1990	0.000	0.000	0.055	0.279	0.439	0.171	0.045	0.011
1991	0.000	0.000	0.053	0.281	0.367	0.219	0.067	0.014
1992	0.000	0.001	0.151	0.371	0.237	0.184	0.048	0.009
1993	0.000	0.000	0.026	0.332	0.457	0.139	0.039	0.006
1994	0.000	0.000	0.060	0.380	0.304	0.183	0.067	0.007
1995	0.000	0.000	0.015	0.232	0.455	0.209	0.072	0.018
1996	0.000	0.000	0.024	0.327	0.457	0.140	0.043	0.008
1997	0.000	0.000	0.034	0.369	0.394	0.159	0.034	0.011
1998	0.000	0.008	0.166	0.377	0.284	0.116	0.034	0.015
1999	0.000	0.012	0.190	0.365	0.248	0.116	0.044	0.024
2000	0.000	0.000	0.022	0.244	0.476	0.196	0.034	0.028

Table App.A.11: Summer survey catches-at-length of *M. capensis* and *M. paradoxus* on the west coast for the 0-500m depth range.

	Merluccius capensis							Merluccius paradoxus										
Size 5	1985 0	2002	2003	2004	2005 1459	2006 829	2007	2008	1985 0	1986 0	1987	2002	2003	2004	2005	2006 179	2007	2008 134
6	0	33	145	263	567	114	126	40	0	0	0	53	114	25	625	83	6	192
7 8	0	264 207	194 121	263 790	2775 29016	3109 10776	142 271	1013 5140	66 99	46 0	0 28	97 112	114 73	340 3020	1887 6125	552 841	14 31	914 1479
9	33	322	1134	5267	61400	77981	1036	24126	0	501	69	376	406	7697	11844	1891	135	3730
10 11	874 3768	1997 6757	1849 3442	12082 9476	98507 148231	142083 98087	2119 2928	22989 11297	0 462	1123 1230	27 524	391 710	994 2413	19017 30499	11316 21238	3062 7874	262 632	5137 5911
12	4291	8323	2865	6478	181576	48989	4077	14412	2937	1567	1402	1451	3359	34618	31895	12237	727	6440
13 14	6156 9085	12044 19963	6148 8028	10305 12471	154653 44648	36423 24123	6809 3705	16917 15809	2310 2624	2719 3977	1717 1920	4315 9503	7608 18332	44643 42228	57570 98045	20104 20334	1246 1081	9992 11794
15	6930	27476	10334	26543	16120	18795	3156	12136	2943	7388	3620	20343	35838	59307	152402	31172	1812	18558
16 17	9554	33810	8865 7814	51689	8503	29516	3261 4594	20700	4067 5704	10857	11996 24785	35649	45088	51215 44736	199473	32572	2908 6327	24195
18	19185 18716	27711 31263	7814 4804	104378 101521	4013 5713	56105 104067	5021	22589 20684	7429	13894 16269	36591	64498 73398	68632 79475	39644	313472 353043	42462 45898	7244	30860 32651
19 20	12828 10120	50054	4455	120375 164185	2474 3028	129719 115425	9260 8953	29992 23158	7475 13508	18377 16129	35915 43171	92989 96974	106960 125805	39986 54835	312403 190489	65672 85065	10800	42940
21	7025	73365 85993	4244 6141	258401	3687	66152	12256	13407	9878	16632	55617	102797	135974	73065	146668	112530	9920 11986	46108 52942
22 23	12510 27118	54843 35261	5357 8528	343338 304247	5976 9010	66556 23327	13819 24246	5379 4542	20763 28038	30772 41038	101281 156442	117648 127712	162204 154510	86290 95674	109809 107701	123524 136442	11352 11521	88706 91839
24	74648	22216	8089	192796	10592	38688	45507	3831	60711	61058	180095	120136	129395	96728	117153	142667	10352	109501
25 26	128636 140536	19594 14012	11548 10598	130971 82630	20765 31827	24364 43519	57076 63067	2840 3534	72235 97571	71954 95753	182512 173105	120053 99996	119462 103738	94182 74908	140720 130094	151954 139877	11331 11411	70570 66646
27	107548	14480	10336	48469	38928	13826	49281	2988	66682	81678	146862	93348	124981	77431	106727	131033	11746	40452
28 29	66789 38360	12426 7824	8564 8080	30845 20374	33528 22637	21935 6434	37885 29192	4394 3564	63808 44600	69172 48456	118232 82836	83682 65711	173777 184740	63075 60510	69212 56174	174646 145090	11457 9924	43962 48905
30	24232	5765	5563	13899	14802	6594	19243	4585	44401	43928	55436	50064	139379	48651	48281	126561	7824	53069
31	14032	4524	5411	8766	9624	4671	19441	4065	32551	51787	45092	35412	132428	43659	39005	91340	8525	49025
32 33	12268 6696	3500 2729	3250 3542	6819 6506	6358 4805	3705 2997	10426 10335	3727 2997	33759 27802	48761 41115	48826 37705	26914 24908	89752 73602	33988 36805	32577 29647	58327 34126	5786 5596	45090 38395
34	7972	2504	2664	4002	3855	2448	5591	3142	24661	40665	27616	18601	46877	26108	25990	24418	3464	29433
35 36	4547 4242	2912 2635	2908 1041	3437 1958	3072 1816	2251 1939	5223 2786	2434 2033	15682 17569	31242 25224	25885 22031	18391 15117	39610 23652	22297 18351	22470 21503	15071 13256	3622 2585	34255 31016
37 38	4053 1871	2326 1971	1350 1300	1985 1732	1905 1707	1714 1362	2620 1320	1717 1621	13227 14276	17113 11811	17309 20288	13382 10592	23139 18188	21789 16061	17511 11544	12317 9271	2877 1972	31707 27601
39	2324	1747	1041	1625	1361	1302	1163	1497	9882	7076	10872	7666	15330	17237	10035	8511	2022	24643
40 41	1720 2150	1883 1601	605 674	1885 1603	984 816	1110 1192	710 575	2041 1929	10041 6185	6231 4119	10686 8611	8415 5821	11942 8438	12906 10777	7425 5117	6641 6560	1460 1581	17071 12685
42	1321	1413	658	1513	1043	1204	413	3113	6113	3064	8571	5367	7654	9331	3761	6279	1003	11282
43 44	1502 1867	2012 1951	653 520	1598 1395	766 905	897 762	370 353	2340 2662	3859 3998	2201 2805	5291 4132	5051 3860	6960 4998	6959 5732	3433 2468	4688 5082	1258 737	12663 7545
45	723	2043	579	1363	1049	629	426	3771	2439	1646	4390	4025	5487	5399	2489	4204	840	4971
46 47	1730 1110	2043 2302	600 749	973 1149	1139 1257	456 736	319 378	2768 2677	3410 2077	1228 1157	3464 2671	3512 4186	4010 4293	5736 4672	2110 1911	3273 2766	536 524	4358 5021
48	1203	1581	721	1042	1182	714	298	2363	2280	890	2574	2869	3445	3529	1365	2527	327	2204
49 50	1018 1013	2061 1773	1036 993	1001 1019	1278 941	643 616	263 231	2121 2237	1599 1130	833 783	2535 2166	3346 2586	3191 2790	2386 2333	1595 772	1801 1711	339 319	1952 1931
51	743	2040	1358	833	1078	1008	375	1414	1417	612	790	2448	2509	2064	890	1657	277	864
52 53	813 670	1585	993 1206	659 666	934 745	1060 777	220 328	1140 917	1112 1043	641 679	792 581	2065 1644	2795 2677	1558 1447	738 604	1207 999	214 185	829 1071
54	739	1431 2010	1312	568	621	657	313	505	1214	423	962	1342	2242	1258	757	970	190	413
55 56	319 232	1818 1718	1461 1320	489	560 422	723 509	384 245	482 246	751 890	407 750	530 555	1902 1436	2909 2313	1105 1133	610 563	904 941	123 117	425 333
57	248	1959	1411	345 369	422	577	344	234	751	321	782	1533	3135	1066	458	599	117	616
58 59	274 249	1445	1241 1415	345 215	251 352	495 455	232 234	167 78	709 369	333 378	737 351	1178 1345	1792 2275	921 885	392 394	684 595	126	320
60	359	1469 1316	1339	227	290	496	155	114	688	460	262	911	1477	1011	346	432	73 75	383 492
61 62	210 115	1112 487	1835 1359	250 242	333 307	1237 541	245 129	68 22	367 337	731 178	233 111	830 501	1893 1094	713 599	329 200	488 231	55 50	329 154
63	74	652	1280	270	366	580	226	58	351	329	98	637	1339	955	178	349	21	204
64 65	277 242	399 406	1257 1172	328 180	220 257	510 268	83 189	45 57	412 333	239 327	186 387	544 403	1105 1441	374 772	207 223	210 276	31 30	208 188
66	263	319	922	256	189	337	274	124	236	445	70	345	910	442	289	154	51	326
67 68	243 68	230 188	692 549	315 325	132 145	285 176	241 140	77 67	276 279	151 233	70 63	269 237	829 335	337 230	174 253	179 207	14 18	164 113
69	55	170	524	215	135	94	189	78	343	225	199	314	608	318	90	171	11	298
70 71	40 97	154 174	378 504	212 222	103 67	147 81	94 106	47 102	424 144	286 139	62 49	201 207	392 441	173 252	101 150	83 133	7 29	74 51
72	52	97	261	224	34	309	167	34	212	346	90	213	245	264	124	14	10	91
73 74	55 44	90 56	375 156	223 116	65 0	151 13	45 37	33 45	133 72	147 198	57 82	134 163	250 135	166 66	58 76	127 51	7 6	51 11
75	37	112	123	33	76	29	73	58	124	51	215	150	184	140	27	59	2	94
76 77	73 111	100 128	76 179	183 70	74 22	27 28	35 48	45 11	137 9	45 55	396 499	105 82	78 123	23 119	86 29	26 22	3 2	31 100
78	15	51	38	36	11	13	24	34	119	31	68	68	78	32	27	14	4	11
79 80	32 15	44 12	65 25	44 24	42 47	0 27	13 13	11 11	12 12	20 20	289 27	53 29	102 60	0	39 39	26 0	2 0	20 11
81	16	96	57	56	31	0	0	11	0	35	14	30	85	22	18	22	0	0
82 83	16 16	72 34	0 50	23 55	45 11	29 68	0	11 11	61 18	20 35	14 109	24 19	28 28	0 11	27 27	0	3 1	0
84	0	20	13	0	57	13	13	11	0	45	14	10	61	32	0	0	0	0
85 86	15 16	0 14	0	0	22 21	27 0	0	136 24	9	10 84	14 0	14 0	57 0	57 11	0	0	1	0
87	30	34	13	0	11	0	0	11	9	0	0	0	0	0	0	0	0	0
88	0	0 10	13 25	0	11 0	0	0 11	0	0 61	20 0	0	0	0	12 22	0	0	1	0
90	0	0	0	0	0	147	0	12	9	14	0	39	0	12	9	0	0	0
91 92	0	14 10	0 13	0 11	0	0	0	0	0	0 10	0 14	0	0	0	0	0	0	0
93	0	0	0	22	0	0	0	11	0	0	0	0	0	0	0	0	0	0
94 95	0	10 10	0	0	0	0	0	0	0	0	14 0	0 24	0	0	0	0	0	0
96	0	22	0	0	0	0	0	0	0	0	14	0	0	0	0	0	0	0
97 98	0 15	0	13 0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
99	0	0	0	0	0	0	0	0	16	0	0	0	0	0	0	0	0	0
100	0	0	0	0	0	0	0	0	0	0	0	0	0	65 0	0	0	0	0
101	U	U	V	U	- 0	U	U	U		V	V	U	U	V	U	U	U	V

Table App.A.12: Winter survey catches-at-length of *M. capensis* and *M. paradoxus* on the west coast for the 0-500m depth range.

		ıccius cap		Merluccius paradoxus							
Size 5	1985	1986 0	1987 0	1985	1986 0	1987	1989				
6	0	0	0	14	0	0	0				
7	0 42	0	0	28 196	16 112	0	58 87				
9	0	32	0	211	272	37	192				
10 11	42 156	96 352	0 295	98 190	784 1536	223 1443	1203 2510				
12	28	384	463	364	1453	4512	7771				
13	113	288	166	1067	2579	7926	27694				
14 15	453 1076	160 162	626 886	3036 4643	3733 7828	12290 20410	58366 99068				
16	2633	129	795	4754	15670	23759	107783				
17	10716	146	2459	6828	28611	32773	83410				
18 19	21541 75443	480 1370	7725 13706	9365 14197	45754 68036	53277 59200	61986 59923				
20	109270	7704	24043	21577	59250	58377	55435				
21 22	152455 132880	12362 22549	32234 30631	32146 34215	45989 41562	54724 43618	57052 59486				
23	98769	25638	15389	37210	42842	35457	61196				
24 25	76139	23449	8757	44965	53271	54048	96122				
26	44864 31247	17376 13985	5934 5336	54962 57436	52078 48345	63029 63657	127838 167468				
27	17301	11061	7082	55353	40357	56770	158154				
28 29	22426 15838	9362 9344	6128 5544	62718 83998	44408 42374	75713 71586	167888 157416				
30	12597	10093	4438	96043	43062	85780	156045				
31 32	10718 11336	10808 11435	4044 3680	99807 83911	42731 35546	55477 42091	126820 121659				
33	11287	12443	3876	80392	27926	24361	81775				
34	9455	13405	3137	57443	18722	18881	59161				
35 36	8321 8332	13932 13654	3435 4646	41560 31001	10836 11419	15575 13753	53662 55573				
37	6549	13295	4298	25788	8763	7190	28920				
38 39	7453 7522	12145 10249	5146 5352	22051 11000	9084 5891	6764 9196	25202 23189				
40	6963	8412	4952	12556	6926	8346	16221				
41	6370	6986	4943	14604	5455	7448	21931				
42 43	6142 5293	5045 3701	4769 4599	13469 8864	5355 4111	7224 4400	13944 9128				
44	4268	2953	3519	6337	4751	4139	8927				
45 46	3454 3386	2451 1541	2682 2615	3762 3003	2841 2587	2661 5578	6153 8658				
47	2482	1532	2689	2542	1777	2189	5835				
48 49	2720 2175	1315 1019	3072 2257	1828 1764	1896 1585	2454 1959	5000 4553				
50	2397	1248	2578	1138	1261	1726	4784				
51	1954	931	2901	778	962	1301	3009				
52 53	2021 1505	1227 1273	2253 2186	842 898	906 1053	1715 1009	3959 1469				
54	1845	1305	2185	673	872	1138	1553				
55 56	1674 1538	1289 1297	1300 1112	715 575	970 635	1056 782	1743 1143				
57	1743	1024	1386	358	1036	540	1362				
58	1729	1189	904	481	848	743	1373				
59 60	1192 1484	1139 885	891 481	323 393	807 610	675 531	1154 2009				
61	862	1015	570	516	602	361	773				
62 63	847 587	849 693	308 435	386 291	651 651	388 259	1764 1589				
64	479	708	388	235	614	302	582				
65 66	367 503	558 396	346 386	186 249	463 696	345 263	1317 850				
67	302	483	211	309	344	217	990				
68	461	510	195	253	356	68	1680				
69 70	323 285	253 444	236 253	270 130	344 246	187 133	602 1612				
71	158	292	194	67	270	254	622				
72 73	449 320	287 187	230 223	60 161	258 184	189 144	296 58				
74	242	261	70	49	111	146	0				
75	169	130	116	42	110	131	25				
76 77	227 188	144 103	17 97	84 42	98 98	41 98	38 0				
78	146	33	17	53	49	168	0				
79 80	263 193	66 119	48 49	35 18	86 61	123 59	0				
81	135	90	132	18	86	41	0				
82	33	91	48	18	0	0	0				
83 84	67 14	58 33	17 50	0	131 37	29 14	0				
85	25	25	17	25	49	14	0				
86 87	14 0	29 82	52 17	0	49 0	14 0	0				
88	0	17	0	0	0	0	0				
89	0	17	17	0	0	0	0				
90 91	19 14	0 12	17 32	18	0	0	0				
92	83	0	19	0	25	14	246				
93 94	0	0	31 0	0	0	0	0				
94 95	0	0	0 17	0	0	0 16	0				
96	0	0	17	0	0	0	0				
97 98	0	0 29	0	_ 0	0	0	0				
99	0	0	0	7.	17	0	0				
100	14 0	0	0 50	0	0	0	0				
101	U	U	DU	U	V	U	U				

Table App.A.13: Spring survey catches-at-length of *M. capensis* and *M. paradoxus* on the south coast for the 0-500m depth range.

Qina	1986	1987	Merls 2001	uccius cap 2003		2004	2007	1986	1987	Merlu 2001	ccius para	adoxus 2004	2004	2007
Size 5	0	0	0	0	2004	2006 562	2007 64	0	0	0	0	10	2006	0
6	0	10	35	41	328	633	96	0	0	0	0	21	0	0
7 8	212 0	27 68	189 215	249 570	1283 4257	1815 3494	721 989	0	0	0	27 0	42 106	0	0
9	121	301	1114	1472	12946	5977	3459	0	0	0	54	125	0	0
10 11	298 925	618 2004	2226 4543	3003 5469	30434 39084	6248 8158	4940 9783	0	0	0 67	53 299	102 337	0	0 13
12	2591	5156	6514	6768	28934	9486	10682	133	0	67	292	392	0	26
13	10704	8576	9127	6111	22470	14704	26015	213	0	245	439	2078	0	13
14 15	18941 28348	9346 7012	6964 7406	5163 5277	14178 7065	14548 15565	22072 25247	1010 2154	0	67 83	699 487	3293 2219	55 0	0
16	32129	4866	5173	4122	4138	10445	11588	1915	0	16	284	933	0	0
17 18	29698 20937	3446 2527	4431 3176	3735 3325	2793 1511	7026 4268	8316 4677	1250 1117	45 0	0	176 27	122 202	0 22	26 13
19	9114	2946	2698	3307	1569	3644	3887	1250	134	ō	149	0	556	497
20	4860	2628	2316	2425	1648	3061	2126	2043	0	0	41	42	584	549
21 22	3490 2566	2481 2946	1771 1837	2246 2146	1692 1750	4464 4667	2604 2584	948 1808	67 45	0	150 111	0 200	266 441	666 1032
23	1467	2195	1225	2627	2195	6663	2795	2454	0	289	146	484	811	327
24 25	2462 2030	2378 1829	1060 1007	2977 3004	2323 3835	7406 9027	2382 4702	6312 7103	89 89	588 1682	314 1977	1319 1262	697 3598	627 693
26	2633	2316	1580	3154	3942	7969	3429	8251	911	3730	2915	3354	3377	209
27 28	3009	1915	1573	3030	4680	8638	6876	4275	2636	6254	11697 16166	7334 15002	12268 20587	2509
29	5259 5327	2666 2962	1939 2223	2604 2560	4794 5759	6654 7576	5494 8769	3028 2325	5450 8316	7538 8244	29715	19470	36512	3444 7947
30	6706	3867	2196	2261	6522	5471	7520	2741	10351	7971	31326	25330	34253	14401
31 32	6960 7621	4095 4059	2669 2789	3048 2411	6523 5892	6214 4388	9244 7179	4218 4700	10454 9026	8417 9435	51083 47244	30996 26635	43203 26485	19000 23332
33	6169	3958	2942	3517	5114	5649	7565	5634	6292	7171	42205	20634	27196	17630
34 35	7477 6548	4108 3839	3616 3793	2623 3428	5044 3649	4837 6431	5765 5468	5416 3994	3894 2308	6278 4197	26324 17522	17851 16330	17153 11729	22075 10630
36	7878	3865	4310	2797	3129	5885	4939	4575	1256	2569	9386	8419	5202	10262
37	6892	3916	5301	3351	3044	7460	4797	3467	1211	1033	4705	6065	3740	7988
38 39	8380 7041	4818 5323	6103 6875	2155 3035	3078 3249	5570 7020	4305 4416	3305 1752	974 569	1256 312	2409 1355	3013 2547	2363 1527	4625 3789
40	7074	6611	7343	2388	3203	5556	3943	2739	387	277	1181	1250	1128	1829
41	6439 5604	5845 5967	8180 8506	3547 2888	3068 3516	6287 4910	3779 2970	1442 1096	636 622	178 223	776 379	545 1165	840 629	1863 810
43	4887	5111	9203	3741	3777	4930	3703	861	857	111	486	1436	618	395
44 45	4691 3489	4656 3920	8093 7518	3007 3369	4182 3701	3999 4032	2583 3195	924 588	776 1059	178 45	459 565	668 824	284 270	836 287
46	3705	3930	6892	2548	3923	2908	1930	675	1013	134	534	229	247	157
47	3297	3294	6340	2948	3406	3363	2238	380	901	0	551	261	205	157
48 49	4093 3131	4216 3545	4921 4499	2206 2707	3467 3277	1987 2526	1651 2011	380 283	598 617	178 0	354 770	386 469	191 124	157 235
50	4265	4097	3745	2617	3164	1783	1388	349	490	111	534	146	90	105
51 52	3509 4277	3698 3541	3819 2877	2807 2025	2761 2191	2066 1219	1460 1000	131 109	294 283	0 22	551 508	219 188	157 126	118 39
53	4226	3352	2911	2255	2177	1667	1258	22	194	22	503	198	104	131
54 55	4551 4789	3422 3068	2387 2536	1563 1947	1960 1880	1217 1606	843 1012	65 109	237 178	0 22	647 384	219 219	135 124	91 78
56	4043	3006	2478	1481	1448	1017	700	109	122	0	551	323	124	91
57	4346	2737	2148	1862	1495	1437	916	44	83	22	408	449	194	91
58 59	3913 3827	2639 2380	1579 1660	1161 1205	1161 1283	1050 966	602 461	0 44	99 128	0 22	312 360	490 449	146 79	118 78
60	3919	2360	1135	1024	2279	667	508	0	99	0	360	480	11	39
61 62	3176 3287	2288 2209	940 887	827 730	862 742	962 780	782 428	0 65	150 39	0 45	264 288	501 417	112 112	157 26
63	2707	2089	961	736	969	778	586	22	22	0	324	407	34	105
64 65	2752 1889	1742 1383	690 873	410 656	597 578	592 691	323 260	0 44	61 0	22 0	252 204	449 522	90 79	91 52
66	1732	1414	697	558	479	683	242	65	ō	22	108	323	101	13
67 68	1601 1457	1817 1151	629 398	575 384	619 330	618 511	365 330	22	16 0	0 22	144 120	469 271	292 56	13 39
69	1572	1266	636	368	438	415	221	0	45	0	84	198	0	26
70	1107	1086	512	354	322	397	200	44	22	45	36	94	45	13
71 72	1205 989	872 903	465 269	297 284	242 317	289 329	142 118	22	0 22	0	48 24	115 115	34 45	13 0
73	1093	843	267	394	176	369	185	22	0	111	12	219	22	13
74 75	1158 472	662 778	292 152	282 305	290 121	253 184	73 76	0	0	45 22	36 12	63 63	0	0 13
76	741	575	171	225	334	149	146	44	0	0	60	31	45	13
77 78	271 581	403 288	241 136	167 126	45 164	137 180	127 54	0	0	0	60 12	83 42	11 34	13 13
79	296	288 294	104	51	155	180	54 45	0	0	0	12	63	0	0
80	306	446	66	75	57	56	38	0	0	22	36	52	0	0
81 82	392 27	298 120	143 50	61 51	25 23	37 75	38 16	0	0	0	12 36	21 52	0	0
83	117	221	91	50	82	0	16	0	0	0	0	10	22	0
84 85	136 123	193 165	0 67	39 51	55 21	59 37	0	0	0	0	0	0	0	0
86	152	122	16	0	12	0	0	0	0	0	0	0	0	0
87	75	70	0	12	0	23	0	0	0	0	0	10	0	0
88 89	97 80	141 45	28 16	27 0	36 48	7 0	32 0	0	0	0	0 12	0 10	11 0	0
90	102	120	16	0	11	0	0	0	0	0	0	10	0	0
91 92	80 48	39 104	38 28	27 0	0 12	0	0	0	0	0	0	0 10	0	0
93	0	0	0	0	0	0	0	0	0	0	0	0	0	0
94	47	67	0	0	0	0	0	0	0	0	0	0	0	0
95 96	27 0	10 0	16 0	0	0	11 0	0	0	0	0	0	0	0	0
97	0	0	0	0	0	0	0	0	0	0	0	0	0	0
98 99	27 0	22 0	0	0	0	0 14	0 Q	0	0	0	0	0	0	0
100	0	0	0	0	0	0	18	0	0	0	0	0	0	0
101	0	0	0	0	0	0	16	0	0	0	0	0	0	0

Table App.A.14: Autumn survey catches-at-length of *M. capensis* and *M. paradoxus* on the south coast for the 0-500m depth range.

			Moris	иссіия сар	ancie		Merluccius paradoxus									
Size	1988	2003	2004	2005	2006	2007	2008	1988	2003	2004	2005	2006	2007	2008		
5	0	0	0	170	0	176	0	0	0	0	20	0	0	0		
6	165	0	34	268	0	22	139	0	0	0	0	0	0	0		
7 8	688 682	39 39	169 65	133 518	29 0	33 493	80 115	0	0	0	139 0	0	0	0		
9	711	58	350	729	14	1121	286	ő	13	ŏ	139	14	ō	ō		
10	767	299	560	894	35	2505	224	0	0	69	41	0	47	0		
11	1276 2944	1248 1605	1664 2838	1814 1339	197 289	6575 10998	570 1041	0	27 0	54 236	41	0	239 508	128 224		
13	5454	2506	5026	1503	875	17226	1523	0	0	201	111 497	18	4055	336		
14	7455	4088	4621	2287	1753	19737	2247	0	13	646	567	14	7907	304		
15	8824	6220	3960	3041	2556	19115	3208	0	13	3264	1353	0	7848	416		
16 17	8687 8296	7135 11514	4062 3939	4061 4839	2427 3187	14569 11698	3523 2837	0	27 44	3897 4641	1223 2039	0	3705 1430	96 160		
18	8445	9808	2185	4316	1946	11486	2284	39	54	3334	1790	0	438	112		
19	9180	12560	1561	4129	2561	7431	2380	97	0	1871	1263	32	438	96		
20	7507	9262	1761	4181	2247	4625	3256	19	0	1280	1194	0	729	240		
21 22	7395 8153	9594 6101	1886 1541	4092 3832	2544 2676	4853 4504	4316 4520	136 97	40 42	1962 3932	448 557	0	1634 1284	0 32		
23	9134	6732	1879	4290	3353	5002	5111	234	523	5014	239	0	875	80		
24	8761	5190	2387	2735	2873	3805	5022	175	188	7467	656	57	934	306		
25 26	7777 7483	6576 4041	2482 2298	3123 1980	3854 3979	4722 3315	6625 6317	136 58	1998 3799	6461 6477	877 1852	252 482	636 1237	722 2333		
27	6757	3796	2656	2596	4849	4558	7633	195	10862	6092	3038	1676	4353	3919		
28	7006	3284	2185	1906	5028	4263	6588	331	33436	10965	3312	3829	5846	5634		
29	8007	2505	2160	1688	5803	5511	6577	457	60606	21570	3214	7076	13431	5872		
30 31	8673 9570	1853 2247	2119 1980	1277 1610	5187 6201	5348 6600	6676 5984	951 2250	75364 69515	28940 27204	2746 2935	9121 11804	13833 20782	5812 6298		
32	10136	1965	2369	1059	5617	5188	5515	2977	46696	21155	1739	12764	19994	7582		
33	10659	2387	3357	1636	7275	6502	4744	3649	24458	14909	2451	12390	24137	6944		
34 35	10739 9644	3078 3822	3133 3157	1357 2486	6952 7710	4517 5309	4978 5054	3610 4181	14269 7949	11445 11083	2310 2888	9899 6717	16790 18179	6248 6141		
36	9644 8607	4260	3591	2505	7017	3871	2024 4645	4714	6620	8955	2888	4798	16108	6092		
37	7187	4614	3885	3282	7619	5134	5229	4521	4914	7658	3354	3572	18010	6383		
38	6284	3666	3465	3308	5733	3167	4632	5280	2710	8091	2608	2752	16808	4134		
39 40	5247 5150	4240 3653	3425 4039	3867 3483	6658 6453	4921 3840	5891 6189	4699 4447	2205 1447	4813 5054	2758 2632	2110 1525	27592 21425	5160 3055		
41	4910	3555	4120	4440	6092	4126	6399	3372	1037	3448	1681	810	24057	4128		
42	4961	3030	4151	3593	5732	3073	5998	2935	955	1846	1014	646	20195	2380		
43 44	5247 5292	2908 3629	4091 4764	3905 3435	4993 4692	3318 2806	6207 5212	2163 1977	1135 983	1474 1751	1165 653	820 572	19827 5555	2678 2132		
45	4805	3861	4237	3261	4301	3106	4314	1784	619	724	696	307	8566	1678		
46	5832	3795	3725	2804	3952	2563	4521	2184	1356	912	578	586	3985	1214		
47	5519	4215	4209	2758	3487	2654	3966	1252	697	179	676	602	3063	1282		
48 49	4685 4358	3690 4003	3209 3825	2538 3085	2700 3408	1764 1722	3424 3369	1275 776	1255 981	211 244	588 549	404 322	1575 764	842 1062		
50	4415	3588	3581	2491	2988	1498	3249	1022	1207	116	250	387	969	466		
51	4194	3849	2658	2148	2651	1811	2939	565	626	85	179	301	286	470		
52	4424	3092	3041	1961	2341	1080	2784	370	1007	35	239	258	525	352		
53 54	3372 3667	2700 2657	2922 2457	1921 1567	2461 2293	978 828	2570 2158	285 347	829 1123	164 244	209 169	158 186	694 566	242 144		
55	3284	2365	2291	1551	2528	1010	2262	409	614	15	328	229	496	176		
56	3258	1937	2147	1712	1820	731	2045	234	1320	0	280	158	321	80		
57 58	2827 2839	2000 1715	2252 1201	1416 1058	2116 1884	852 489	1714 1506	156 211	850 1310	12 15	269 279	315 229	438 292	18 32		
59	2546	1267	1630	1089	2116	637	936	117	777	107	398	215	263	64		
60	2337	1292	1751	823	1840	491	818	117	858	46	179	229	379	112		
61	1964	1242	1317	789	2167	594	902	19	506	122	338	158	233	0		
62 63	1557 1418	869 968	981 837	556 640	1421 1450	265 461	676 676	136 74	473 381	0 107	279 224	244 143	467 233	0 16		
64	1379	905	879	541	1190	237	740	58	404	107	149	164	117	32		
65	1321	650	743	433	998	293	648	97	296	46	91	143	117	32		
66 67	1383 953	734 554	682 486	229 373	818 998	319 253	399 317	19 19	205 134	15 0	60 70	57 72	584 233	32 32		
68	849	526	480 610	373 315	485	193	189	19	107	0	90	43	32.1	32.		
69	594	438	479	317	870	209	277	19	67	46	70	57	146	48		
70	529	473	461	105	525	121	248	58	67	46	50	86	29	0		
71 72	471 351	352 291	472 250	151 213	549 330	173 100	169 72	0	40 67	0 183	20 30	29 57	88 175	16 0		
73	404	304	233	81	345	124	143	0	13	46	0	43	117	80		
74	397	219	286	67	208	46	12	0	27	0	0	14	58	0		
75 76	350 213	157 199	180 152	167 95	231 144	13 93	116 84	0	0 13	0	10 0	14 29	88 88	0 32		
77	135	158	219	82	122	69	53	0	0	46	21	29	29	0		
78	128	158	494	68	101	67	49	0	27	0	0	0	0	0		
79	242	56 122	88	22	82	44	0	0	0	0	0	0	29	0		
80 81	105 243	133 74	128 87	12 23	87 198	35 33	42 24	0	0	0	0	0	0	0		
82	210	15	38	35	68	11	0	0	0	46	0	14	0	ō		
83	70	132	88	48	58	22	0	0	0	0	0	14	0	0		
84 85	32 32	58 73	13 36	35 0	72 43	11 11	0	0	13 0	0	0	0	0 29	0		
86	35	30	36	12	14	22	0	0	0	0	10	0	29	0		
87	67	0	15	12	0	0	12	0	13	0	0	29	0	0		
88	72	73	28	24	14	0	0	0	0	0	0	0	0	0		
89 90	24 63	74 41	38 28	24 0	21 0	24 0	12 0	0	0 15	0	0	0 14	0	0		
91	56	30	13	35	14	0	24	0	0	ő	0	0	ő	ő		
92	16	15	28	0	0	0	12	0	0	0	0	0	0	0		
93 94	48 32	29 15	0	11 0	0	0	0	0	0	0	0	0	0	0		
94	32	0	0	0	0	11	0	0	0	0	0	0	0	0		
96	24	0	0	11	0	0	12	0	0	0	0	0	0	0		
97	0	0	0	0	0	0	12	0	0	0	0	0	0	0		
98 99	0	0	13 0	0	14 0	0	0	0	0	0	0	0	0	0		
100	0	12	0	0	0	0	0	0	0	0	0	0	0	0		
101	0	15	0	12	0	0	0	0	0	0	0	0	0	0		

 Table App.A.15:
 Commercial catches-at-length (species combined).

	Offs	Offshore trawl Offshore trawl					0	ffshore trav	d I	Inshore trawl									Longline			
	West Coast South Coast					Both Coasts South coast										West Coast						
		th specie			Both species			Both species		M. capensis								Both species				
Length	1997	1998	1999	1975	1976	1977	2005	2006	2007	1981	1982	1983	1984	1985	1986	1987	1988	1994	1995	1996	1997	
19	36	26	16	0	0	Ω	15320	0	0	0	0	0	0	0	0	0	0	Ω.	0	0	0	
21	575	418	265	0	753275	8256	146700	340993	ō	0	0	0	0	0	0	0	ō	0	0	0	0	
23	3109	2281	1406	0	1027193	4128	1947301	2420009	329913	0	0	0	0	0	201	0	812	0	0	0	0	
25	7080	5322	3394	149765		74306		10114184	3341151	14616	16062	1284	0	313	1602	0	7356	o o	0	Ů.	0	
27	10636	8525	5780	688919		90818		19878889		43847	96373	4397	7510	1731	6750	3785	68805	o o	0	Ů.	0	
29	16979	13788	9978		16914437	499501		25382280		204618	497928	43819	42362	17424	49482	34644	256192	0	0	0	0	
31	22842	21168	15156		31158173	1515017		28909583			1365287	191172	235286	63890	208646	113552	622506	0	0	0	0	
33	20830	22423	15365		24858059	1671885		25782332		1023088		419654	681695	174492	520621	329855	1148827	7	0	0	0	
35	19531	22565	15069	3584377	16982916	1948468	23060176	20993022	21195853	1476170	2312957	683207	1180629	381287	880580	688169	1190681	55	0	68	0	
37	17087	20516	13485	4263312	9929528	2423201	14081990	15576440	18526775	1710019	2007775	873549	1564328	580814	1100662	1124012	1143296	145	0	68	0	
39	14006	16694	10952	3424628	4999004	2472738	11226958	11396663	16293899	1739250	1798966	960018	1817904	725458	1039693	1247484	1043460	290	151	204	0	
41	9239	11404	7376	5032106	7464266	2617222	8381432	9452470	13611807	1505401	1413474	1011188	1906240	878907	975200	1534650	1015551	642	227	511	668	
43	6425	8039	5235	5181871	5478360	2299358	9589056	8144595	10702986	1373861	1076167	1064233	1666818	1068546	779643	1274141	995372	980	113	1498	3339	
45	5769	7292	4825	5181871	4999004	2055799	7778592	7113076	7348419	1096166	835234	1088795	1138668	1233793	720842	969945	844254	1180	605	2519	2893	
47	3693	4738	3289	5711041	5957717	1407686	8649677	6120703	6379690	876933	610364	995056	803947	1130354	642917	735431	761449	1477	794	2927	7345	
49	2428	3219	2394	5101996	4725086	1205408	5482530	4830979	5267271	716162	465804	830025	592794	1030908	585256	623045	637884	1801	1852	4867	10906	
51	2177	2906	2268	5181871	2739180	1003131	4637750	4108786	3334680	526160	369431	632843	479697	924507	596237	524386	580651	2423	3591	7897	15135	
53	2254	3050	2374	4193421	1232631	891672	4123671	3555076	2520877	453082	256995	479038	382114	667560	563458	455587	438897	3299	6993	13105	26264	
55	1927	2588	2064	4193421	684795	875160	4033206	3250875	2605755	306926	192746	330390	306103	483651	511108	355258	378324	4728	8278	20831	27822	
57	2069	2780	2201	3354737	479357	747188	3821585	3002475	1908180	248464	160622	233878	242642	345335	453663	292439	301004	6074	16782	31315	45405	
59	1804	2358	1958	2366288	273918	730676	2943441	1978579	1299511	219233	112435	160384	214044	270558	390459	282002	263996	6937	15837	44896	46296	
61	1438	1844	1570	1827134	342398	800854	2808123	1804417	1470292	160771	96373	111543	158277	208466	269362	261303	238268	7716	20071	56299	45183	
63	1169	1438	1288	1218089	205439	606832	1947249	1680277	1084712	116924	64249	87219	118168	153740	180754	153010	119120	8579	24455	63039	58760	
65	847	976	965	988449	136959	367402	2089726	1394477	1105531	87693	48187	61463	79663	108274	114094	108928	91704	9525	21696	84959	67218	
67	602	681	682	988449	205439	317865	1451537	1210351	859275	58462	32124	43058	49378	67904	74811	63570	63129	11816	28273	80228	74340	
69	472	517	545	838684	136959	2064055	1138007	905966	815793	43847	32124	28891	33978	45175	47366	40858	38916	13514	26799	80704	70334	
71	409	440	471	459279	136959	1490248	775412	757464	524991	29231	16062	19882	18260	28132	30239	30355	22497	13935	28689	83870	76121	
73	206	219	230	459279	68480	1168255	614793	439740	919148	14616	16062	16144	12982	20409	20971	18270	18390	14660	31372	73216	77456	
75	159	169	177	379405	68480	1498504	306312	293611	782060	14616	0	10668	8631	11917	13171	11837	10979	13983	23624	68757	68553	
77	88	89	105	379405	0	722419	217081	154424	152939	14616	0	6510	5822	9037	11994	11188	8588	12424	26081	58988	65437	
79	66	69	75 54	379405	0	24769	105159	83279	128618	14616	0	5112	4413	4880	7442	6010	4509	10588	22603	50342	49857	
81	46	48	54	379405	0	33025	174162	72984	62199	0	0	2908	2150	4141	4872	4690	3368	7710	18370	39859	38283	
83	25	27	29	229640	0	1120	19449	44491	35991	0	0	1704	1512	3724	3107	3669	3477	7026	15535	30736	29603	
85	12 8	11	14	229640	0	4128 0	27914	31774	29354	0	0	466	1553	2164	2250	1254	155	4410	12020	25222	25819	
87	6	8 6	10 6	149765 149765	0	12384	7397 56178	9825 9428	25463 32283	0	0	704	905	866 358	864	1233	1150 283	3037 2015	10508 6312	15726	24038	
91	5	6	5	79875	0	12364 8256	15428	26237	5740	0	0	648 136	658 288	358 478	477 693	328 394	283	1256	3251	11062 7761	11574 6010	
93	3	/	2	19015	0	6230 0	2497	1318	5740	0	0	114	288 82	119	37	430	73	1001	2419	4119	3561	
95	1	1	1	0	n	0	2497	2277	10401	0	0	57	237	30	521	430	0	435	983	2757	2003	
97	1	2	1	0	0	n	ľ	2936	10401	0	0	80	237	97	0.0	0	0	242	643	1123	668	
99	0	0	0	0	0	n	l o	2930	4661	0	0	0	134	97	0	0	٥	97	189	579	668	
101	ľ	n	0	0	0	0	n	563	1001	0	0	0	0	0	0	0	0	69	113	374	000	
103	1	1	1	0	0	0	n	0	n	0	0	0	0	119	0	0	ő	7	0	204	n	
105	1	1	1	0	Ő	o	o o	2277	ő	0	0	0	0	0	0	0	ő	7	0	34	0	

Appendix B – Incorporation of catch-at-length information in fitting an ASPM

To be able to incorporate the proportion at length information, the proportions at age predicted by the model ($\hat{p}_{y,a}$) (with is based upon age-specific selectivity) are converted to proportions at length ($\hat{p}_{y,l}$) using the von Bertalanffy growth equation, assuming that the length-at-age distribution remains constant over time:

$$\hat{p}_{y,l} = \sum_{a} \hat{p}_{y,a} A_{a,l} \tag{B.1}$$

where $A_{a,l}$ is the proportion of fish of age a that fall in the length group l (i.e., $\sum_{l} A_{a,l} = 1$ for all ages a). The matrix A

is calculated under the assumption that length-at-age is normally distributed about a mean given by the von Bertalanffy equation, i.e.:

$$L_a \sim N \left[L_\infty \left(1 - e^{-\kappa (a - t_0)} \right); \theta_a^2 \right]$$
 (B.2)

where θ_a is the standard deviation of length-at-age a, which is modelled as a function of the expected length at age a, i.e.:

$$\theta_a = \beta \left[L_{\infty} \left(1 - e^{-\kappa (a - t_0)} \right) \right]^{\gamma} \tag{B.3}$$

 β and γ are estimated in the fitting process. The resultant term added to $-\ln L$ in the fitting process is:

$$-\ln L^{\text{length}} = 0.1 \sum_{y} \sum_{l} \left[\ln \left(\sigma_{len} / \sqrt{p_{y,l}} \right) + p_{y,l} \left(\ln p_{y,l} - \ln \hat{p}_{y,l} \right)^{2} / 2 \left(\sigma_{len} \right)^{2} \right]$$
 (B.4)

where σ_{len} is the standard deviation associated with the length-at-age data, which is estimated in the fitting procedure by:

$$\hat{\sigma}_{len} = \sqrt{\sum_{y} \sum_{l} p_{y,l} \left(\ln p_{y,l} - \ln \hat{p}_{y,l} \right)^2 / \sum_{y} \sum_{l} 1}$$
 (B.5)

The initial 0.1 multiplicative factor is a somewhat arbitrary downweighting to allow for correlation between proportions in adjacent length groups.

Age 0 correction:

To allow for the fact that zero-year old fish are not available to the trawl fishery throughout their first year of life the mean length at age 0 is computed as:

$$L_0 = L_{\infty} \left(1 - e^{-\kappa (A_0 - t_0)} \right) \tag{B.6}$$

where A_0 is estimated in the model fitting procedure (for each species separately).

Selectivity-at-length effect for the surveys

Although the model, and therefore the fishing selectivity, is age-based, many selectivity effects are in fact length-based. This applies particularly to the small fish that can escape through the mesh. A selectivity-at-length effect was therefore included when fitting to the survey catch-at-length information. This correction was applied only to the survey data, as the commercial fleets do not catch enough of the very young fish for this effect to be important.

The selectivity-at-length effect is included by estimating a logistic function to model the proportion of fish of length l actually retained by the gear:

$$R_{l} = \frac{1}{1 + e^{-(l - L_{l})/\Delta}} \tag{B.7}$$

where L_1 and L_2 are estimated in the model fitting procedure for each survey and species separately.

The proportion of fish of age a caught that fall in length group l is computed as:

$$A_{a,l}' = \frac{A_{a,l} R_l}{\sum_{l} A_{a,l} R_l}$$
 (B.8)