

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Introduction

COMP90049 COMP30018 Knowledge Technologies

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THE UNIVERSITY OF
MELBOURNE

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Week 3:

- Approximate String Search and Matching
- Common Applications
- Methods:
 - Neighbourhood Search
 - Edit Distance
 - N-Gram Distance
 - [Phonetic methods]
- Evaluation
- [Genomics]

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

Consider:

- Given a string, is some substring contained within it?
- Given a string (document), find all occurrences of some substring

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

For example, find Exxon in:

In exes for foxes rex dux mixes a pox of waxed luxes.

An axe, and an axon, to exo Exxon max oxen.

Grexit or Brexit as quixotic haxxers with buxom rex taxation.

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

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Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

Consider:

- Given a string, is some substring contained within it?
- Given a string (document), find all occurrences of some substring

Not (really) a Knowledge Technology!

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

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Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

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In exes for foxes rex dux mixes a pox of waxed luxes.

An axe, and an axon, to exo Exxon max oxen.

Grexit or Brexit as quixotic haxxers with buxom rex taxation.

Not present!

...But what is the “closest” or “best” match?

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

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In exes for foxes rex dux mixes a pox of waxed luxes.

An axe, and an axon, to exo Exxon max oxen.

Grexit or Brexit as quixotic haxxers with buxom rex taxation.

Not present!

...But what is the “closest” or “best” match?

This is a Knowledge Technology!

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

Two main applications for Approximate String Search:

- Spelling correction
- Computational Genomics

Spelling Correction

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate

Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics



Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

Need the notion of a **dictionary**:

- Here, a list of words

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

Need the notion of a **dictionary**:

- Here, a list of ~~words~~ entries that are “correct” with respect to our (expectations of our) language

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

Need the notion of a **dictionary**:

- Here, a list of ~~words~~ entries that are “correct”
- We can break our input into ~~words~~ substrings that we wish to match, and compare each of them against the entries in the dictionary

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

Need the notion of a **dictionary**:

- Here, a list of ~~words~~ entries that are “correct”
- We can break our input into ~~words~~ substrings that we wish to match, and compare each of them against the entries in the dictionary
- A ~~word~~ item in the input which *doesn't* appear in the dictionary is *misspelled*

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

Need the notion of a **dictionary**:

- Here, a list of ~~words~~ entries that are “correct”
- We can break our input into ~~words~~ substrings that we wish to match, and compare each of them against the entries in the dictionary
- A ~~word~~ item in the input which *doesn't* appear in the dictionary is *misspelled*
- A ~~word~~ item in the input which *does* appear in the dictionary might be correctly spelled *or* misspelled

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

Need the notion of a **dictionary**:

- Here, a list of **words** entries that are “correct”
- We can break our input into **words** substrings that we wish to match, and compare each of them against the entries in the dictionary
- A **word** item in the input which *doesn't* appear in the dictionary is *misspelled*
- A **word** item in the input which *does* appear in the dictionary might be correctly spelled *or* misspelled (probably slightly beyond the scope of this subject)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

Therefore, the problem here:

Given some item of interest — which does not appear in our dictionary
— which entry from the dictionary was truly intended?

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

Therefore, the problem here:

Given some item of interest — which does not appear in our dictionary
— which entry from the dictionary was truly intended?

Depends on the person who wrote the original string!

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

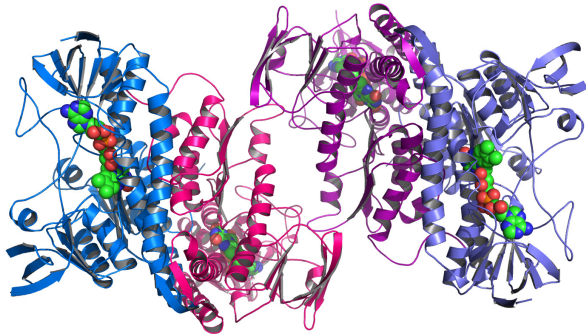
Phonetics

Evaluation

References

Genomics

Computational Genomics (later, if we have time)



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Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate

Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

- Name matching, for example:

The name *Gorbachev* is spelled (at least) 20 different ways in a corpus of newswire text!

Gorbachev, Gorbacahev, Gorbahev, Gorbatchev, Gorbechev,
Gorbachov, Gorachev, Gorbacheva, Gorbechyeve, Gorbacev,
Gorbachyov, Gorabchev, Grobachev, ...

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

- Computational Genomics (later, if we have time)
- Name matching
- Query repair
- Phonetic matching (later, if we have time)
- Data cleaning
- ...

What's a “best” match?

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Find approximate match(es) for exon in:

In exes for foxes rex dux mixes a pox of waxed luxes.

An axe, and an axon, to exo Exxon max oxen.

Grexit or Brexit as quixotic haxxers with buxom rex taxation.

What's a “best” match?

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Find approximate match(es) for `exon` in:

In exes for foxes rex dux mixes a pox of waxed luxes.

An axe, and an axon, to exo **Exxon** max oxen.

Grexit or Brexit as quixotic haxxers with buxom rex taxation.

Insert `x` (and fold case)

What's a “best” match?

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Find approximate match(es) for `exon` in:

In exes for foxes rex dux mixes a pox of waxed luxes.

An axe, and an axon, to **exo** Exxon max oxen.

Grexit or Brexit as quixotic haxxers with buxom rex taxation.

Delete `n`

What's a “best” match?

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Find approximate match(es) for exon in:

In exes for foxes rex dux mixes a pox of waxed luxes.

An axe, and an **axon**, to exo Exxon max oxen.

Grexit or Brexit as quixotic haxxers with buxom rex taxation.

Replace e with a
(Sometimes **Substitute**)

What's a “best” match?

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Find approximate match(es) for exon in:

In exes for foxes rex dux mixes a pox of waxed luxes.

An axe, and an axon, to exo Exxon max **oxen**.

Grexit or Brexit as quixotic haxxers with buxom rex taxation.

Transpose e and o

(Beyond the scope of this subject.)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

For a given string w of interest:

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

For a given string w of interest:

- Generate all variants of w that utilise at most k changes (Insertions/Deletions/Replacements) — **neighbours**

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

For a given string w of interest:

- Generate all variants of w that utilise at most k changes (Insertions/Deletions/Replacements) — **neighbours**
- Check whether generated variants exist in dictionary

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

For a given string w of interest:

- Generate all variants of w that utilise at most k changes (Insertions/Deletions/Replacements) — **neighbours**
- Check whether generated variants exist in dictionary
- **All** results found in dictionary are returned

Unix command-line utility `agrep` is an efficient mechanism for finding these.

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

For example:

... proceed if you can see no **ther** option ...

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

For example:

... proceed if you can see no **ther** option ...

Intended word: other

Requires 1 insertion (o) so intended word will be found using neighbourhood search (and some unintended words...)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

With a careful implementation, Neighbourhood search is suprisingly fast!

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Neighbourhood search is suprisingly fast!

Consider: alphabet size is Σ , length of string is $|w|$:

For 1 edit, roughly $\mathcal{O}(\Sigma \cdot |w|)$ neighbours

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Neighbourhood search is suprisingly fast!

Consider: alphabet size is Σ , length of string is $|w|$:

For 2 edits, roughly $\mathcal{O}(\Sigma^2 \cdot |w|^2)$ neighbours

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Neighbourhood search is suprisingly fast!

Consider: alphabet size is Σ , length of string is $|w|$:

For k edits, roughly $\mathcal{O}(\Sigma^k \cdot |w|^k)$ neighbours

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Neighbourhood search is surprisingly fast!

Consider: alphabet size is Σ , length of string is $|w|$:

For k edits, roughly $\mathcal{O}(\Sigma^k \cdot |w|^k)$ neighbours

...But Σ is a small constant, string of interest is usually short, and k is usually small

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

Neighbourhood search is suprisingly fast!

Consider: alphabet size is Σ , length of string is $|w|$:

For k edits, roughly $\mathcal{O}(\Sigma^k \cdot |w|^k)$ neighbours

...But Σ is a small constant, string of interest is usually short, and k is usually small

For each neighbour, need a dictionary read (dict has D entries):
Binary search yields $\mathcal{O}(|w|^k \log D)$ string comparisons

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

So, efficiency isn't our problem.

(agrep example)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Alternative methods:

Scan through each dictionary entry looking for the “best” match

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Global Edit Distance:

Transform the string of interest into each dictionary entry, using the operations Insert, Delete, Replace, and Match (character)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Global Edit Distance:

Transform the string of interest into each dictionary entry, using the operations Insert, Delete, Replace, and Match (character)

Each operation is associated with a score;
Best match is the dictionary entry with best aggregate **score**

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

For example:

Item of interest: `crat`

Dictionary: `cart, arts`

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

For example:

Item of interest: `crat`

Dictionary: `cart`, `arts`

`crat` \rightarrow `cart`:

Match `c`, Delete `r`, Match `a`, Insert `r`, Match `t`

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

For example:

Item of interest: `crat`

Dictionary: `cart`, `arts`

`crat` → `cart`:

Match `c`, Delete `r`, Match `a`, Insert `r`, Match `t`

`crat` → `arts`:

Replace `c` with `a`, Match `r`, Delete `a`, Match `t`, Insert `s`

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

For example:

Item of interest: `crat`

Dictionary: `cart`, `arts`

Score: Match +1, Insert -1, Delete -1, Replace -1

`crat` → `cart`:

Match `c`, Delete `r`, Match `a`, Insert `r`, Match `t`

`crat` → `arts`:

Replace `c` with `a`, Match `r`, Delete `a`, Match `t`, Insert `s`

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

For example:

Item of interest: `crat`

Dictionary: `cart`, `arts`

Score: Match +1, Insert -1, Delete -1, Replace -1

`crat` → `cart`:

Match `c` (+1), Delete `r` (-1), Match `a` (+1), Insert `r` (-1), Match `t` (+1) = +1

`crat` → `arts`:

Replace `c` with `a` (-1), Match `r` (+1), Delete `a` (-1), Match `t` (+1), Insert `s` (-1) = -1

`cart` is the better match

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Confusingly, Global Edit Distance isn't a "distance"

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Confusingly, Global Edit Distance isn't a "distance"

...But depends on parameter

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Match (0), Insert (+1), Delete (+1), Replace (+1)

This is the Levenshtein Distance (which is a “distance”): it counts the number of edits required to transform one string into the other

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

For example:

Item of interest: `crat`

Dictionary: `cart`, `arts`

Score: Match 0, Insert +1, Delete +1, Replace +1

`crat` → `cart`:

Match `c` (0), Replace `r` with `a` (+1), Replace `a` with `r` (+1), Match `t` (0) = +2

`crat` → `arts`:

Replace `c` with `a` (+1), Match `r` (0), Replace `a` with `t` (+1), Replace `t` with `s` (+1) = +3

`cart` is the better match (2 “changes”, rather than 3 “changes”)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Hypothetically, any parameter is possible!

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Hypothetically, any parameter is possible!

But some choices make no sense, e.g.:

Match (+4), Insert (-2), Delete (+8), Replace (0)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Hypothetically, any parameter is possible!

But some choices make no sense, e.g.:

Match (+4), Insert (-2), Delete (+8), Replace (0)

Consider aba: which corresponds to best match?

- foo
- aba
- cb

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Hypothetically, any parameter is possible!

But some choices make no sense, e.g.:

Match (+4), Insert (-2), Delete (+8), Replace (0)

aba: Which corresponds to best match?

- foo: Delete, Delete, Replace, Insert, Insert
- aba: Match, Match, Match
- cb: Replace, Match, Delete

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Hypothetically, any parameter is possible!

But some choices make no sense, e.g.:

Match (+4), Insert (-2), Delete (+8), Replace (0)

aba: Which corresponds to best match?

- foo: Delete, Delete, Replace, Insert, Insert = +12
- aba: Match, Match, Match = +12
- cb: Replace, Match, Delete = +12

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Often, “direction” doesn’t matter: Insert = Delete (“Indel”)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Sometimes, score of Replace depends on which character is being replaced:

Consider:

Is faxing more likely to be facing or faking?

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Computer can't find best sequence of operations by inspection

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

From string f to string t , given array of $|f| + 1$ columns and $|t| + 1$ rows, we can solve using the Needleman–Wunsch algorithm:

Global Edit Distance Algorithm

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

From string f to string t , given array A of $|f| + 1$ columns and $|t| + 1$ rows, we can solve using the Needleman–Wunsch algorithm:

```
lf = strlen(f); lt = strlen(t);
A[0][0]=0;
for (j=1; j<=lt; j++) A[j][0] = j * i;
for (k=1; k<=lf; k++) A[0][k] = k * d;

for (j=1; j<=lt; j++)
    for (k=1; k<=lf; k++)
        A[j][k] = max3( //Or min3 if m<i,d,r
            A[j][k-1] + d, //Deletion
            A[j-1][k] + i, //Insertion
            A[j-1][k-1] + equal(f[k-1],t[j-1])); //Replace or match
```

`equal()` returns m if characters match, r otherwise

Final score is at $A[|t|][|f|]$

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from `crat` to `arts`, Match (+1), Insert/Delete/Replace (-1)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

	ϵ	c	r	a	t
ϵ					
a					
r					
t					
s					

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

Initialise table:

	ϵ	c	r	a	t
ϵ	0	-1	-2	-3	-4
a	-1				
r	-2				
t	-3				
s	-4				

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, consider three neighbours:

	ϵ	c	r	a	t
ϵ	0	-1	-2	-3	-4
a	-1	?			
r	-2				
t	-3				
s	-4				

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, Delete c:

	ϵ	c	r	a	t
ϵ	0	-1	-2	-3	-4
a	-1	-2			
r	-2				
t	-3				
s	-4				

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, Insert a:

	ϵ	c	r	a	t
ϵ	0	-1	-2	-3	-4
a	-1	-2			
r	-2				
t	-3				
s	-4				

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, Replace c with a:

	ϵ	c	r	a	t
ϵ	0	-1	-2	-3	-4
a	-1	-1			
r	-2				
t	-3				
s	-4				

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

And so on:

	ϵ	c	r	a	t
ϵ	0	-1	-2	-3	-4
a	-1	-1	-2		
r	-2				
t	-3				
s	-4				

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

And so on:

	ϵ	c	r	a	t
ϵ	0	-1	-2	-3	-4
a	-1	-1	-2	-1	
r	-2				
t	-3				
s	-4				

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

And so on:

	ε	c	r	a	t
ε	0	-1	-2	-3	-4
a	-1	-1	-2	-1	-2
r	-2	-2	0	-1	-2
t	-3	-3	-1	-1	0
s	-4	-4	-2	-2	-1

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from `crat` to `arts`, Match (+1), Insert/Delete/Replace (-1)

And so on:

	ε	c	r	a	t
ε	0	-1	-2	-3	-4
a	-1	-1	-2	-1	-2
r	-2	-2	0	-1	-2
t	-3	-3	-1	-1	0
s	-4	-4	-2	-2	-1

Global Edit Distance: -1 (Replace, Match, Delete, Match, Insert)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Algorithm actually depends on parameter!

More parameter concerns

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

```
A[j][k] = max3(  
    A[j][k-1] + d, //Deletion  
    A[j-1][k] + i, //Insertion  
    A[j-1][k-1] + equal(f[k-1],t[j-1])); //Replace or match
```

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

```
A[j][k] = max3(  
    A[j][k-1] + d, //Deletion  
    A[j-1][k] + i, //Insertion  
    A[j-1][k-1] + equal(f[k-1],t[j-1])); //Replace or match
```

→ Match score greater than Insert/Delete/Replace

e.g. Match (+1), Insert/Delete/Replace (-1)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

```
A[j][k] = min3(  
    A[j][k-1] + d, //Deletion  
    A[j-1][k] + i, //Insertion  
    A[j-1][k-1] + equal(f[k-1],t[j-1])); //Replace or match
```

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

```
A[j][k] = min3(  
    A[j][k-1] + d, //Deletion  
    A[j-1][k] + i, //Insertion  
    A[j-1][k-1] + equal(f[k-1],t[j-1])); //Replace or match
```

→ Match score less than Insert/Delete/Replace

e.g. Match (0), Insert/Delete/Replace (+1)

(Levenshtein Distance)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Local Edit Distance is like Global Edit Distance, but we are searching for the best substring match

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Local Edit Distance is like Global Edit Distance, but we are searching for the best substring match

Particularly suitable when comparing two strings of very different lengths, e.g. a word and a sentence, or a sentence and an entire document

Local Edit Distance Algorithm

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

From string f to string t , given array A of $|f| + 1$ columns and $|t| + 1$ rows, we can solve using the Smith–Waterman algorithm:

```
lf = strlen(f); lt = strlen(t);
A[0][0]=0;
for (j=1; j<=lt; j++) A[j][0] = 0;
for (k=1; k<=lf; k++) A[0][k] = 0;

for (j=1; j<=lt; j++)
    for (k=1; k<=lf; k++)
        A[j][k] = max4( //0r min4 if m<i,d,r
            0,
            A[j][k-1] + d, //Deletion
            A[j-1][k] + i, //Insertion
            A[j-1][k-1] + equal(f[k-1],t[j-1])); //Replace or match
```

`equal()` returns m if characters match, r otherwise

Final score is greatest value in the entire table (or least value, if $m < i, d, r$)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from `cart` to `arts`, Match (+1), Insert/Delete/Replace (-1)

(For Local Edit Distance, Match must have different $+/-$ sign to Insert/Delete/Replace)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

	ϵ	c	a	r	t
ϵ					
a					
r					
t					
s					

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

Initialise table:

	ϵ	c	a	r	t
ϵ	0	0	0	0	0
a	0				
r	0				
t	0				
s	0				

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, consider three neighbours:

	ϵ	c	a	r	t
ϵ	0	0	0	0	0
a	0	?			
r	0				
t	0				
s	0				

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, Delete c:

	ϵ	c	a	r	t
ϵ	0	0	0	0	0
a	0	-1			
r	0				
t	0				
s	0				

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, Insert a:

	ϵ	c	a	r	t
ϵ	0	0	0	0	0
a	0	-1			
r	0				
t	0				
s	0				

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, Replace c with a:

	ϵ	c	a	r	t
ϵ	0	0	0	0	0
a	0	-1			
r	0				
t	0				
s	0				

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, 0 is better:

	ϵ	c	a	r	t
ϵ	0	0	0	0	0
a	0	0			
r	0				
t	0				
s	0				

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

For a-a correspondence (Match), 1 is better:

	ϵ	c	a	r	t
ϵ	0	0	0	0	0
a	0	0	1		
r	0				
t	0				
s	0				

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

For a-r correspondence, back to 0:

	ϵ	c	a	r	t
ϵ	0	0	0	0	0
a	0	0	1	0	0
r	0	0	0	1	0
t	0	0	0	0	1
s	0	0	0	0	0

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

And so on:

	ε	c	a	r	t
ε	0	0	0	0	0
a	0	0	1	0	0
r	0	0	0	2	1
t	0	0	0	1	3
s	0	0	0	0	2

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

And so on:

	ϵ	c	a	r	t
ϵ	0	0	0	0	0
a	0	0	1	0	0
r	0	0	0	2	1
t	0	0	0	1	3
s	0	0	0	0	2

Best match: art with art (+3); ties are possible.

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

For strings f and t , Both algorithms above are $\mathcal{O}(|f||t|)$ in both space and time. (Space can be improved, but time (probably) cannot.)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

When approximate matching, we have a constant string f which we want to compare to each string in the dictionary:

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

When approximate matching, we have a constant string f which we want to compare to each string t in the dictionary D :

$$\mathcal{O}(\sum_{t \in D} |f||t|)$$

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

When approximate matching, we have a constant string f which we want to compare to each string t in the dictionary D :

$$\mathcal{O}(|f| \sum_{t \in D} |t|)$$

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

When approximate matching, we have a constant string f which we want to compare to each string t in the dictionary D :

Hence, integer comparisons are roughly the number of characters in the dictionary. Whether this is feasible depends on the size of the dictionary.

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

N-Gram Distance has same goal as Edit Distance: compare two strings to determine “best” match

A true “distance”

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

N-Gram Distance has same goal as Global Edit Distance, but much simpler

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

(character) n -gram: substring of length n

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

n -gram: substring of length n

2-grams of crat: cr, ra, at

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

n -gram: substring of length n

2-grams of crat: #c, cr, ra, at, t# (sometimes)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

n -gram: substring of length n

3-grams of crat: #cr, cra, rat, at#

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

n-gram: substring of length *n*

2-grams of crat: #c, cr, ra, at, t#

2-grams of cart: #c, ca, ar, rt, t#

2-grams of arts: #a, ar, rt, ts, s#

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

n -gram: substring of length n

2-grams of crat: #c, cr, ra, at, t#

2-grams of cart: #c, ca, ar, rt, t#

2-grams of arts: #a, ar, rt, ts, s#

N-Gram Distance between n -grams of string s ($G_n(s)$) and t ($G_n(t)$):

$$|G_n(s)| + |G_n(t)| - 2 \times |G_n(s) \cap G_n(t)|$$

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

n-gram: substring of length *n*

2-grams of crat: #c, cr, ra, at, t#

2-grams of cart: #c, ca, ar, rt, t#

2-grams of arts: #a, ar, rt, ts, s#

2-Gram Distance between crat and cart:

$$\begin{aligned} & |G_2(\text{crat})| + |G_2(\text{cart})| - 2 \times |G_2(\text{crat}) \cap G_2(\text{cart})| \\ &= 5 + 5 - 2 \times 2 = 6 \end{aligned}$$

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

n -gram: substring of length n

2-grams of crat: #c, cr, ra, at, t#

2-grams of cart: #c, ca, ar, rt, t#

2-grams of arts: #a, ar, rt, ts, s#

2-Gram Distance between crat and cart:

$$|G_2(\text{crat})| + |G_2(\text{cart})| - 2 \times |G_2(\text{crat}) \cap G_2(\text{cart})| \\ = 5 + 5 - 2 \times 2 = 6$$

2-Gram Distance between crat and arts:

$$|G_2(\text{crat})| + |G_2(\text{arts})| - 2 \times |G_2(\text{crat}) \cap G_2(\text{arts})| \\ = 5 + 5 - 2 \times 0 = 10$$

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

n -gram: substring of length n

2-grams of crat: #c, cr, ra, at, t#

2-grams of cart: #c, ca, ar, rt, t#

2-grams of arts: #a, ar, rt, ts, s#

2-Gram Distance between crat and cart:

$$|G_2(\text{crat})| + |G_2(\text{cart})| - 2 \times |G_2(\text{crat}) \cap G_2(\text{cart})| \\ = 5 + 5 - 2 \times 2 = 6 \text{ (better)}$$

2-Gram Distance between crat and arts:

$$|G_2(\text{crat})| + |G_2(\text{arts})| - 2 \times |G_2(\text{crat}) \cap G_2(\text{arts})| \\ = 5 + 5 - 2 \times 0 = 10$$

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

Occasionally useful as a simpler variant of (Global) Edit Distance

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

Occasionally useful as a simpler variant of Edit Distance

More sensitive to long substring matches, less sensitive to relative ordering of strings (matches can be anywhere!)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

Occasionally useful as a simpler variant of Edit Distance

More sensitive to long substring matches, less sensitive to relative ordering of strings (matches can be anywhere!)

Despite its simplicity, takes roughly the same time to compare entire dictionary

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

Occasionally useful as a simpler variant of Edit Distance

More sensitive to long substring matches, less sensitive to relative ordering of strings (matches can be anywhere!)

Despite its simplicity, takes roughly the same time to compare entire dictionary

Quite useless for very long strings and/or very small alphabets (Why?)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Salient concern in speech-to-text systems, e.g.:
Georgia Conal

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Salient concern in speech-to-text systems, e.g.:

Georgia Conal

George O'Connell

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Salient concern in speech-to-text systems, e.g.:

You wreck a nice beach

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Salient concern in speech-to-text systems, e.g.:

You wreck a nice beach

You recognize speech

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Salient concern in speech-to-text systems, e.g.:
Lowe

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Salient concern in speech-to-text systems, e.g.:

Low

Lo

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Salient concern in speech-to-text systems, e.g.:

Lowe

Lo

Lho

Loan

Loe

Loew

Lough

Low ...

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Also relevant in spelling correction (English can be very difficult to spell correctly!)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

One (ineffectual) mechanism: Soundex

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

One mechanism: Soundex

Translation table:	aehiouwy	→	0 (vowels)
	bpfv	→	1 (labials)
	cgjksxz	→	2 (misc: fricatives, velars, etc.)
	dt	→	3 (dentals)
	l	→	4 (lateral)
	mn	→	5 (nasals)
	r	→	6 (rhotic)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

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	dt	→	3 (dentals)
	l	→	4 (lateral)
	mn	→	5 (nasals)
	r	→	6 (rhotic)

Four step process:

- 1 Except for initial character, translate string characters according to table
- 2 Remove duplicates (e.g. 4444 → 4)
- 3 Remove 0s
- 4 Truncate to four symbols

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

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	dt	→	3 (dentals)
	l	→	4 (lateral)
	mn	→	5 (nasals)
	r	→	6 (rhotic)

Four step process:

king	kyngge
k052	k05220
k052	k0520
k52	k52
k52	k52

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

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	dt	→	3 (dentals)
	l	→	4 (lateral)
	mn	→	5 (nasals)
	r	→	6 (rhotic)

Four step process:

knight	night
k50203	n0203
k50203	n0203
k523	n23
k523	n23

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact

Approximate

Application

Methods

Neighbourhood

Edit Distance

N-Gram Distance

Phonetics

Evaluation

References

Genomics

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	cgjkqsz	→	2 (misc: fricatives, velars, etc.)
	dt	→	3 (dentals)
	l	→	4 (lateral)
	mn	→	5 (nasals)
	r	→	6 (rhotic)

Four step process:

loan	loew	lough	lewicks
1005	1000	10020	1000222
105	10	1020	102
15	1	12	12
15	1	12	12

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Better phonetic methods make use of the fact that some letters sounds alike in certain contexts, and different in other contexts

Editex uses the Edit Distance to compare strings based on a similar translation table to Soundex

Ipadist uses a text-to-sound algorithm to represent tokens according to the International Phonetic Alphabet (but context matters a lot)

There are also worse variants, like Phonix.

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Evaluation: consider whether the system is effective at solving the user's problem

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Evaluation: consider whether the system is effective at solving the user's problem

In this case: for a misspelled word, does the system identify the correct word?

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

To evaluate, we need:

- A number of cases of misspelled words

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

To evaluate, we need:

- A number of cases of misspelled words
- The intended (correct) word for each case

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

To evaluate, we need:

- A number of cases of misspelled words
- The intended (correct) word for each case
- An **evaluation metric**

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

We have some cases:

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Misspelled Word	Correct Word
ther	other
corridr	corridor
cracheyt	crotchety
...	...

Evaluation Metrics for Spelling Correction

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Misspelled Word	Correct Word	Predicted Word
ther	other	there
corridr	corridor	corridor
cracheyt	crotchety	cachet
...

Evaluation Metrics for Spelling Correction

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Misspelled Word	Correct Word	Predicted Word	Right/Wrong?
ther	other	there	×
corridr	corridor	corridor	✓
cracheyt	crotchety	cachet	×
...

Evaluation Metrics for Spelling Correction

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Misspelled Word	Correct Word	Predicted Word	Right/Wrong?
ther	other	there	×
corridr	corridor	corridor	✓
cracheyt	crotchety	cachet	×
...

Accuracy: fraction of correct responses ($\frac{1}{3}$)

Evaluation Metrics for Spelling Correction

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Misspelled Word	Correct Word	Predicted Word	Right/Wrong?
ther	other	there	×
corridr	corridor	corridor	✓
cracheyt	crotchety	cachet	×
...

Accuracy: $\frac{\text{Number of correct predictions}}{\text{Total number of words}}$

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

More realistic situation:

Misspelled Word	Correct Word	Predicted Word
ther	other	there other their
corridr	corridor	corridor carrier
cracheyt	crotchety	???
...

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

More realistic situation:

Misspelled Word	Correct Word	Predicted Word	Right/Wrong?
ther	other	there	×
		other	✓
		their	×
corridr	corridor	corridor	✓
		carrier	×
cracheyt	crotchety	???	???
...	

Evaluation Metrics for Spelling Correction

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Misspelled Word	Correct Word	Predicted Word	Right/Wrong?
ther	other	there	×
		other	✓
		their	×
corridr	corridor	corridor	✓
		carrier	×
cracheyt	crotchety	???	—
...	

Precision: fraction of correct responses among attempted responses
 $(\frac{2}{5})$

Evaluation Metrics for Spelling Correction

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Misspelled Word	Correct Word	Predicted Word	Right/Wrong?
ther	other	there	×
		other	✓
		their	×
corridr	corridor	corridor	✓
		carrier	×
cracheyt	crotchety	???	—
...	

Recall: proportion of words with a correct response (somewhere) ($\frac{2}{3}$)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References
Genomics

Typically, the value of the evaluation metric has little intrinsic meaning

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References
Genomics

Typically, the value of the evaluation metric has little intrinsic meaning

“This system gets 81% accuracy” — useful for users, or not?

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

The evaluation metric allows us to compare systems:

“The system based on the Global Edit Distance gets 81% accuracy, whereas the system based on the N-Gram Distance gets 84% accuracy”

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

The evaluation metric allows us to compare systems:

“The basic system gets 81% accuracy, but after making some changes, the accuracy becomes 74%”

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Typically, comparison is more difficult:

“System A gets 45% precision and 80% recall;
System B gets 95% precision and 10% recall”

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Typically, comparison is more difficult:

“System A gets 45% precision and 80% recall;
System B gets 95% precision and 10% recall”
— Which one should we use? (Also: why?)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

The answer depends on the problem (and the user)!

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

- What is approximate string search?
- What are some common applications of approximate string search; why are they hard?
- What are some methods for finding an approximate match to a string? What do we need to generate them?
- How can we evaluate a typical approximate matching system?

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

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Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

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Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Typical Genomics problem:

- Given a nucleotide/amino acid sequence (substring)
- Find whether the sequence occurs within a larger sequence (string)
- Possibly with “errors” (nucleotide/amino acid changes)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Typical Genomics problem:

- Given a substring, find whether the sequence occurs within a larger string, possibly with “errors”
- Almost the same as spelling correction, flipped around

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Typical Genomics problem:

- Given a substring, find whether the sequence occurs within a larger string, possibly with “errors”
- Almost the same as spelling correction
- But **much** larger strings: a small genomics problem might involve comparing perhaps 1K character sequence against several 100K character sequences; alphabet is smaller

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Recall: we have a “short” ($\sim 1\text{K}$ character) nucleotide/amino acid sequence to compare against many long ($\sim 100\text{K}$ character) chromosomes/genes/proteins/etc.

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Recall: we have a “short” ($\sim 1\text{K}$ character) string to compare against many long ($\sim 100\text{K}$ character) strings

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Recall: we have a “short” ($\sim 1\text{K}$ character) string to compare against many long ($\sim 100\text{K}$ character) strings

For example, if some member of the population has 99% of the sequence of interest, they might be susceptible to some medical condition

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Recall: we have a “short” ($\sim 1\text{K}$ character) string to compare against many long ($\sim 100\text{K}$ character) strings

We're allowed ~ 10 errors; alphabet is ~ 4 or ~ 20 characters

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Neighbourhood search:

Roughly $4^{10} \times 1000^{10}$ possible neighbours.

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Neighbourhood search:

Roughly $4^{10} \times 1000^{10}$ possible neighbours.

... Forget it.

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Global Edit Distance:

One string is $\sim 1\text{K}$ characters, other is $\sim 100\text{K}$ characters.

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Global Edit Distance:

One string is $\sim 1\text{K}$ characters, other is $\sim 100\text{K}$ characters.

... Every string comparison involves $\sim 99\text{K}$ insertions.

→ Prefers shorter chromosomes (not intended behaviour)

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Local Edit Distance:

One string is $\sim 1\text{K}$ characters, other is $\sim 100\text{K}$ characters.

... Seems like the right idea.

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Local Edit Distance:

One string is $\sim 10\text{K}$ characters, other is $\sim 1\text{G}$ characters.

... Can't fit table into memory.

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

Local Edit Distance:

One string is $\sim 10K$ characters, other is $\sim 1G$ characters.

... Requires approximate solutions with heuristics, e.g. BLAST, FASTA

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

N-Gram Distance:

With huge n (e.g. 80% of length of shorter string) can (almost) work!

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

N-Gram Distance:

Surprisingly, can (almost) work!

Tends to prefer shorter chromosomes like Global Edit Distance

Introduction

COMP90049
COMP30018
Knowledge
Technologies

String Search

Exact
Approximate
Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonetics

Evaluation

References

Genomics

N-Gram Distance:

But better methods for using n -gram information, e.g. de Bruijn graphs