

### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Exact Approximate

Methods

Edit Distance

......

References

Ganomic

## Introduction

COMP90049 COMP30018 Knowledge Technologies

Jeremy Nicholson and Justin Zobel and Karin Verspoor

Semester 2, 2018





# Summary

#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Application

Neighbourhood
Edit Distance

Phoneti

Evaluatio

Reference

`anami

## Week 3:

- Approximate String Search and Matching
- Common Applications
- Methods:
  - Neighbourhood Search
  - Edit Distance
  - N-Gram Distance
  - [Phonetic methods]
- Evaluation
- [Genomics]



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

## String Searc

Approxima

Methods Neighbourhood

Edit Distance
N-Gram Distance

Phonet

Evaluation

Reference

enomic

### Consider:

- Given a string, is some substring contained within it?
- Given a string (document), find all occurrences of some substring



### Introduction

COMP30049 COMP30018 Knowledge Technologies

## String Searc

Approxim Application

Methods

Neighbourhood
Edit Distance
N-Gram Distance

Phonet

Evaluation

References

Genomi

## For example, find Exxon in:

In exes for foxes rex dux mixes a pox of waxed luxes. An axe, and an axon, to exo Exxon max oxen. Grexit or Brexit as quixotic haxxers with buxom rex taxation.



### Introduction

COMP90049 COMP30018 Knowledge Technologies

#### String Searc Exact

Approxim

Methods
Neighbourhood
Edit Distance

Edit Distance N-Gram Distance

Phoneti

Evaluation

References

Genomi

## For example, find Exxon in:

In exes for foxes rex dux mixes a pox of waxed luxes. An axe, and an axon, to exo **Exxon** max oxen. Grexit or Brexit as quixotic haxxers with buxom rex taxation.



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

#### String Searc Exact

Application

Methods Neighbourhood Edit Distance

...

Evaluation

References

Genomic

### Consider:

- Given a string, is some substring contained within it?
- Given a string (document), find all occurrences of some substring

Not (really) a Knowledge Technology!



# Approximate String Search

#### Introduction

COMP90049 COMP30018 Knowledge Technologies

# String Searc

Approximate Application

Methods
Neighbourhood
Edit Distance
N-Gram Distance

Phoneti

Evaluation

References

icici ciic

### Find exon in:

In exes for foxes rex dux mixes a pox of waxed luxes. An axe, and an axon, to exo Exxon max oxen. Grexit or Brexit as quixotic haxxers with buxom rex taxation.



# Approximate String Search

#### Introduction

COMP90049 COMP30018 Knowledge Technologies

# Exact Approximate

Application

Methods

Neighbourhood Edit Distance N-Gram Distance

Phonet

Evaluation

References

Find exon in:

In exes for foxes rex dux mixes a pox of waxed luxes. An axe, and an axon, to exo Exxon max oxen. Grexit or Brexit as quixotic haxxers with buxom rex taxation.

Not present!

...But what is the "closest" or "best" match?



# Approximate String Search

#### Introduction

Knowledge Technologies

Approximate

References

## Find exon in:

In exes for foxes rex dux mixes a pox of waxed luxes. An axe, and an axon, to exo Exxon max oxen. Grexit or Brexit as quixotic haxxers with buxom rex taxation.

## Not present!

...But what is the "closest" or "best" match?

This is a Knowledge Technology!



# Important problems

#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Application

Methods

Edit Distance

Dhonoti

Evaluation

Reference

Genomi

Two main applications for Approximate String Search:

- Spelling correction
- Computational Genomics



#### Introduction

Knowledge **Technologies** 

Application

3:44 PM Optus 3G Messages Edit xyzzy 14/09/2013 3:44 PM В corridor × You are in a maze of dark and twisty corridr Send W Е R U 0 P Q S D F G Н K A X В M X .?123 space return



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Sear

Approximate

Application

Neighbourhood Edit Distance

N-Gram Distance

Evaluatio

References

Need the notion of a **dictionary**:

Here, a list of words



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Application

Application

Neighbourhood Edit Distance

Phonei

Evaluatio

Reference

Senomic

## Need the notion of a dictionary:

 Here, a list of words entries that are "correct" with respect to our (expectations of our) language



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Application

Methods Neighbourhood Edit Distance

Phonet

Evaluation

References

Genomi

- Here, a list of words entries that are "correct"
- We can break our input into words substrings that we wish to match, and compare each of them against the entries in the dictionary



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Application

Methods Neighbourhood Edit Distance

Phonei

Evaluation

References

Senomi

- Here, a list of words entries that are "correct"
- We can break our input into words substrings that we wish to match, and compare each of them against the entries in the dictionary
- A word item in the input which doesn't appear in the dictionary is misspelled



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searcl Exact

Application

Methods
Neighbourhood
Edit Distance
N-Gram Distance

Phonet

Evaluatio

References

- Here, a list of words entries that are "correct"
- We can break our input into words substrings that we wish to match, and compare each of them against the entries in the dictionary
- A word item in the input which doesn't appear in the dictionary is misspelled
- A werd item in the input which does appear in the dictionary might be correctly spelled or misspelled



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Application

Methods
Neighbourhood
Edit Distance
N-Gram Distance

Phoneti

Evaluatio

References

- Here, a list of words entries that are "correct"
- We can break our input into words substrings that we wish to match, and compare each of them against the entries in the dictionary
- A word item in the input which doesn't appear in the dictionary is misspelled
- A word item in the input which does appear in the dictionary might be correctly spelled or misspelled (probably slightly beyond the scope of this subject)



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Application

Application

Neighbourhood Edit Distance

Dhonoi

Evaluation

Reference

Senomi

Therefore, the problem here:

Given some item of interest — which does not appear in our dictionary — which entry from the dictionary was truly intended?



#### Introduction

Knowledge Technologies

Application

References

Therefore, the problem here:

Given some item of interest — which does not appear in our dictionary - which entry from the dictionary was truly intended?

Depends on the person who wrote the original string!



## Other Problems of Interest

#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Application

Methods

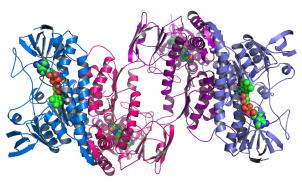
Edit Distance

Phonet

Evaluation

Reference

Computational Genomics (later, if we have time)



"Genomics", Wikipedia, used under CC BY-SA 2.0 https://creativecommons.org/licenses/by-sa/2.0/deed.en



## Other Problems of Interest

#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searcl Exact

Application

Neighbourhood
Edit Distance
N-Gram Distance

Phoneti

Evaluation

References

Name matching, for example:

The name *Gorbachev* is spelled (at least) 20 different ways in a corpus of newswire text!

Gorbachev, Gorbachev, Gorbahev, Gorbatchev, Gorbechev, Gorbachov, Gorachev, Gorbacheva, Gorbachev, Gorbachev, Gorbachev, Gorbachev, ...



## Other Problems of Interest

#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search
Exact

Application

Application

Neighbourhood

N-Gram Distance

Phonet

Evaluation

Reference

enomic

- Computational Genomics (later, if we have time)
- Name matching
- Query repair
- Phonetic matching (later, if we have time)
- Data cleaning
- ...



## Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search
Exact
Approximate

Methods Neighbourhood

Edit Distance N-Gram Distance

Phoneti

Evaluation

References

Find approximate match(es) for exon in:

In exes for foxes rex dux mixes a pox of waxed luxes. An axe, and an axon, to exo Exxon max oxen. Grexit or Brexit as quixotic haxxers with buxom rex taxation.



#### Introduction

Knowledge **Technologies** 

Methods

References

Find approximate match(es) for exon in:

In exes for foxes rex dux mixes a pox of waxed luxes. An axe, and an axon, to exo Exxon max oxen.

Grexit or Brexit as quixotic haxxers with buxom rex taxation.

Insert x (and fold case)



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Approximate

Application

#### Methods

Edit Distance

Dhanatia

Contrastina

Deference

Genomi

Find approximate match(es) for exon in:

In exes for foxes rex dux mixes a pox of waxed luxes. An axe, and an axon, to **exo** Exxon max oxen. Grexit or Brexit as quixotic haxxers with buxom rex taxation.

Delete n



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc Exact

Application

Methods

Edit Distance

N-Gram Distar

Phonet

Evaluation

References

Genomi

Find approximate match(es) for exon in:

In exes for foxes rex dux mixes a pox of waxed luxes. An axe, and an **axon**, to exo Exxon max oxen. Grexit or Brexit as quixotic haxxers with buxom rex taxation.

Replace e with a (Sometimes Substitute)



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc Exact

Application

## Methods

Edit Distance

Diameter.

References

Ganomic

Find approximate match(es) for exon in:

In exes for foxes rex dux mixes a pox of waxed luxes.

An axe, and an axon, to exo Exxon max **oxen**.

 ${\tt Grexit}$  or  ${\tt Brexit}$  as quixotic haxxers with buxom rex taxation.

**Transpose** e and o (Beyond the scope of this subject.)



### Introduction

COMP30018 Knowledge Technologies

String Searc

Exact Approximate

Methods

#### Neighbourhood

L-Gram Dietane

Dhanatia

i ilonetic.

Deference

Genomi

For a given string w of interest:



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Methods Neighbourhood

Edit Distance
N-Gram Distance

Phonet

Evaluatio

References

Conomi

## For a given string w of interest:

 Generate all variants of w that utilise at most k changes (Insertions/Deletions/Replacements) — neighbours



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Methods

Neighbourhood Edit Distance

N-Gram Distance

Phonotics

Evaluatio

References

Genomi

## For a given string w of interest:

- Generate all variants of w that utilise at most k changes (Insertions/Deletions/Replacements) — neighbours
- Check whether generated variants exist in dictionary



#### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Searce Exact Approximate

Application

Neighbourhood

Edit Distance N-Gram Distanc

Phonetic

Evaluatio

References

For a given string *w* of interest:

- Generate all variants of w that utilise at most k changes (Insertions/Deletions/Replacements) — neighbours
- Check whether generated variants exist in dictionary
- All results found in dictionary are returned

Unix command-line utility agrep is an efficient mechanism for finding these.



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

### String Searcl

Exact Approximate

Method

#### Neighbourhood

alt Distance

N-Gram Distan

Evaluatio

Reference

Distance

## For example:

 $\dots$  proceed if you can see no  $ther\ \mbox{\rm option}\ \dots$ 



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Methods

Neighbourhood Edit Distance

N-Gram Distan

\_\_\_\_\_\_

Evaluation

References

Genomic

## For example:

... proceed if you can see no **ther** option ...

Intended word: other

Requires 1 insertion (o) so intended word will be found using neighbourhood search (and some unintended words...)



# Neighbourhood Search Efficiency

#### Introduction

COMP30018 Knowledge Technologies

### String Searc

Exact Approximate

Method

#### Neighbourhood

Edit Distance

N-Gram Distance

**Phonetics** 

Reference

Genomi

With a careful implementation, Neighbourhood search is suprisingly fast!



# Neighbourhood Search Efficiency

#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Applicat

Neighbourhood

Edit Distance

N-Gram Distanc

...

Evaluation

Reference

Genomi

Neighbourhood search is suprisingly fast!

Consider: alphabet size is  $\Sigma$ , length of string is |w|:

For 1 edit, roughly  $\mathcal{O}(\Sigma \cdot |w|)$  neighbours



# Neighbourhood Search Efficiency

#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Applicatio

Neighbourhood

Edit Distance

N-Gram Distant

...

Frankristis

neierence

Neighbourhood search is suprisingly fast!

Consider: alphabet size is  $\Sigma$ , length of string is |w|:

For 2 edits, roughly  $\mathcal{O}(\Sigma^2 \cdot |w|^2)$  neighbours



# Neighbourhood Search Efficiency

#### Introduction

Knowledge **Technologies** 

Neighbourhood

Neighbourhood search is suprisingly fast!

Consider: alphabet size is  $\Sigma$ , length of string is |w|:

For *k* edits, roughly  $\mathcal{O}(\Sigma^k \cdot |w|^k)$  neighbours



# Neighbourhood Search Efficiency

#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc Exact

Methods

Neighbourhood Edit Distance

N-Gram Distan

Dhanatian

Evaluation

References

Genomi

Neighbourhood search is suprisingly fast!

Consider: alphabet size is  $\Sigma$ , length of string is |w|:

For k edits, roughly  $\mathcal{O}(\Sigma^k \cdot |w|^k)$  neighbours

...But  $\Sigma$  is a small constant, string of interest is usually short, and  $\emph{k}$  is usually small



# Neighbourhood Search Efficiency

#### Introduction

COMP90049 COMP30018 Knowledge Technologies

Exact Approximate

pproximate

Neighbourhood

Edit Distance N-Gram Distance

Phoneti

Evaluation

References

Neighbourhood search is suprisingly fast!

Consider: alphabet size is  $\Sigma$ , length of string is |w|:

For k edits, roughly  $\mathcal{O}(\Sigma^k \cdot |w|^k)$  neighbours

...But  $\Sigma$  is a small constant, string of interest is usually short, and k is usually small

For each neighbour, need a dictionary read (dict has D entries): Binary search yields  $\mathcal{O}(|w|^k \log D)$  string comparisons



# Neighbourhood Search Effectiveness

#### Introduction

COMP30018 Knowledge Technologies

String Searc

Approximate

Method

Neighbourhood

N Crom Distance

N-Gram Distan

**Phonetics** 

Evaluation

Reference

So, efficiency isn't our problem.

 $({\tt agrep}\ example)$ 



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Approximate

Bankha da

Neighbourhoo

Edit Distance

N-Gram Distai

\_ . . .

B. /.....

Alternative methods:

Scan through each dictionary entry looking for the "best" match



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searcl

Exact
Approximate
Application

Neighbourhood Edit Distance

N-Gram Distar

FIIOHELIC

Evaluation

References

enomic

#### Global Edit Distance:

Transform the string of interest into each dictionary entry, using the operations Insert, Delete, Replace, and Match (character)



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Methods Neighbourhood Edit Distance

N-Gram Dista

. ......

References

O---:

#### Global Edit Distance:

Transform the string of interest into each dictionary entry, using the operations Insert, Delete, Replace, and Match (character)

Each operation is associated with a score;
Best match is the dictionary entry with best aggregate **score** 



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Approximate Application

Methods

Edit Distance

N-Gram Distance

Frankria i

Lvaidatio

Reference

For example:

Item of interest: crat

Dictionary: cart, arts



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Application

Methods

Edit Distance

N-Gram Distan

N-Grain Dista

Frankrickie

**~** . .. . . . . . .

For example:

Item of interest: crat

Dictionary: cart, arts

 $\mathtt{crat} o \mathtt{cart}$ :

Match c, Delete r, Match a, Insert r, Match t



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Approximate

Methods

Edit Distance

N-Gram Distance

Division

Evaluatio

References

Genomi

For example:

Item of interest: crat

Dictionary: cart, arts

 $\mathtt{crat} \to \mathtt{cart}$ :

Match c, Delete r, Match a, Insert r, Match t

 $\mathtt{crat} \to \mathtt{arts}$ :

Replace c with a, Match r, Delete a, Match t, Insert s



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Methods Neighbourh

Edit Distance N-Gram Distance

N-Grain Dista

Evaluatio

References

Genomic

For example:

Item of interest: crat

Dictionary: cart, arts

Score: Match +1, Insert -1, Delete -1, Replace -1

 $\mathtt{crat} \to \mathtt{cart}$ :

Match c, Delete r, Match a, Insert r, Match t

 $\mathtt{crat} \to \mathtt{arts}$ :

Replace c with a, Match r, Delete a, Match t, Insert s



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searce Exact Approximate

Methods Neighbourhoo

Edit Distance

Phonotic

Evaluatio

Reference

For example:

Item of interest: crat

Dictionary: cart, arts

Score: Match +1, Insert -1, Delete -1, Replace -1

 $\mathtt{crat} \to \mathtt{cart}$ :

Match c (+1), Delete r (-1), Match a (+1), Insert r (-1), Match t (+1) = +1

 $\mathtt{crat} o \mathtt{arts}$ :

Replace c with a (-1), Match r (+1), Delete a (-1), Match t (+1), Insert s (-1) = -1

cart is the better match



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Exact Approximate

Methods

Edit Distance

N-Gram Distance

Phonetic:

Evaluation

References

Confusingly, Global Edit Distance isn't a "distance"



#### Introduction

COMP90049 COMP30018

Technologies

String Searc Exact

Applicatio

Methode

Edit Distance

N-Gram Dietan

N-Gram Distar

Phonetics

Evaluatio

Reference

...But depends on parameter

Confusingly, Global Edit Distance isn't a "distance"



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search
Exact
Approximate

Neighbourhood Edit Distance

Edit Distance N-Gram Distan

Filonetic

Evaluation

References

Match (0), Insert (+1), Delete (+1), Replace (+1)

This is the Levenshtein Distance (which is a "distance"): it counts the number of edits required to transform one string into the other



### Introduction

COMP90049 COMP30018 Knowledge Technologies

Exact
Approximate

Neighbourhood

Edit Distance

Phonotic

Evaluatio

References

For example:

Item of interest: crat

Dictionary: cart, arts

Score: Match 0, Insert +1, Delete +1, Replace +1

 $\mathtt{crat} o \mathtt{cart}$ :

Match c (0), Replace r with a (+1), Replace a with r (+1), Match t (0) = +2

 $\mathtt{crat} \to \mathtt{arts}$ :

Replace c with a (+1), Match r (0), Replace a with t (+1), Replace t with s (+1) = +3

cart is the better match (2 "changes", rather than 3 "changes")



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Exact Approximate

Mothode

Neighbourhoo

Edit Distance

· Honetice

\_\_\_\_\_

i cici ci i ci

Hypothetically, any parameter is possible!



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Applicatio

Methods

Neighbour

Edit Distance

Tr Gram Bista

Lvaidatio

Reference

Hypothetically, any parameter is possible!

But some choices make no sense, e.g.:

Match (+4), Insert (-2), Delete (+8), Replace (0)



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc Exact

Approximate Application

Methods

Edit Distance

N-Gram Distanc

Phonetic

Evaluatio

References

aenomic

Hypothetically, any parameter is possible!

But some choices make no sense, e.g.:

Match (+4), Insert (-2), Delete (+8), Replace (0)

Consider aba: which corresponds to best match?

- foo
- aba
- cb



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

Exact Approximate

Application

Neighbourhood Edit Distance

N-Gram Distan

Phoneti

References

Hypothetically, any parameter is possible!

But some choices make no sense, e.g.:

Match (+4), Insert (-2), Delete (+8), Replace (0)

aba: Which corresponds to best match?

■ foo: Delete, Delete, Replace, Insert, Insert

aba: Match, Match, Match

■ cb: Replace, Match, Delete



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

Exact Approximate

Application

Neighbourhood Edit Distance

Edit Distance N-Gram Distance

Phonet

Evaluation

References

Hypothetically, any parameter is possible!

But some choices make no sense, e.g.:

Match (+4), Insert (-2), Delete (+8), Replace (0)

aba: Which corresponds to best match?

- foo: Delete, Delete, Replace, Insert, Insert = +12
- aba: Match, Match, Match = +12
- cb: Replace, Match, Delete = +12



#### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Searc

Exact Approximate

Methods

Edit Distance

N-Gram Distanc

Phonetics

\_ .

Genomi

Often, "direction" doesn't matter: Insert = Delete ("Indel")



#### Introduction

Knowledge **Technologies** 

**Edit Distance** 

Consider:

Sometimes, score of Replace depends on which character is being replaced:

Is faxing more likely to be facing or faking?



# Global Edit Distance Algorithm

#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Exact Approximate

Methods

Neighbourhoo Edit Distance

N-Gram Distance

**Phonetics** 

Evaluation

References

Genomi

Computer can't find best sequence of operations by inspection



# Global Edit Distance Algorithm

#### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Searc

Approximate

Application

Neighbourhood Edit Distance

N-Gram Distance

Phonetic

Evaluation

Reference

. . . . . . . . . .

From string f to string t, given array of |f|+1 columns and |t|+1 rows, we can solve using the Needleman–Wunsch algorithm:



# Global Edit Distance Algorithm

#### Introduction

COMP90049 COMP30018 Knowledge Technologies

Exact
Approximate

Neighbourhood Edit Distance

N-Gram Dista

Evaluation

Reference

From string t to string t, given array A of |t|+1 columns and |t|+1 rows, we can solve using the Needleman–Wunsch algorithm:

equal() returns *m* if characters match, *r* otherwise

Final score is at A[It][If]



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Exact Approximate

Аррисанс

Neighbourho

Edit Distance

N-Gram Distan

Phonetic:

Evaluation

References

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Application

Methods

Edit Distance

N-Gram Distance

Evaluatio

References

Conomio

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

	ε	С	r	a	t
ε					
a					
r					
t					
s					



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Application

Neighbourhood Edit Distance

N-Gram Distai

Frankrickie

Genomi

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

Initialise table:

	ε	С	r	a	t
$\varepsilon$	0	-1	-2	-3	-4
a	-1				
r	-2				
t	-3				
s	-4		-2		



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search
Exact

Application

Neighbourhood Edit Distance

N-Gram Distan

Evaluatio

Reference

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, consider three neighbours:

	$\varepsilon$	С	r	a	t
ε	0	-1	-2	-3	-4
a	-1	?	-2		
r	-2				
t	-3				
s	-4				



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Application

Neighbourho

Edit Distance N-Gram Distance

N-Grain Dista

Evaluatio

Reference

Referenc

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, Delete c:

	$\varepsilon$	С	r	a	t
ε	0	-1	-2	-3	-4
a	-1	-1 -2			
r	-2				
t	-3				
s	-4				



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search
Exact

Approximate
Application

Neighbourhoo

Edit Distance N-Gram Distance

Evaluatio

Reference

Genomi

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, Insert a:

	$\varepsilon$	С		a	t
ε	0	-1	-2	-3	-4
a	-1	-1 -2			
r	-2				
t	-3				
s	-4				



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Approximate Application

Neighbourhood Edit Distance

N-Gram Distan

Phonetics

Evaluatio

Reference

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, Replace c with a:

		С	r	a	t
ε	0	-1	-2	-3	-4
a	-1	-1	-2		
r	-2				
t	-3				
s	-4				



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search
Exact

Methods Neighbourh

Edit Distance

N-Gram Dista

Frankrickie

Lvaidatio

neierence

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

And so on:

	$\varepsilon$	С	r	a	t
ε	0	-1	-2	-3	-4
a	-1	-1	-2		
r	-2				
t	-3				
s	-4		-2 -2		



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search
Exact

Approximate

Methods

Edit Distance

N-Gram Distan

Filoneti

Evaluatio

Reference

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

And so on:

	ε	С	r	a	t
$\varepsilon$	0	-1	-2	-3	-4
a	-1	-1	- <mark>2</mark> -2	-1	
r	-2				
t	-3				
s	-4				



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search
Exact

Methods Neighbourhoo

Edit Distance N-Gram Distance

DI. . . . . . . . . . .

Evaluatio

Reference

Senomic

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

And so on:

	$\varepsilon$	С	r	a	t
$\varepsilon$	0	-1	-2	-3	-4
a	-1	-1	-2	-1	-2
r	-2	-2	0	-3 -1 -1 -1 -2	-2
t	-3	-3	-1	-1	0
s	-4	-4	-2	-2	-1



## Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search
Exact
Approximate

Methods Neighbourhood

Edit Distance N-Gram Distan

Phoneti

Evaluatio

neierence

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

And so on:

	ε	С	r	a	t
ε	0	-1	-2	-3	-4
a	-1	-1 -1 -2 -3 -4	-2	-1	-2
r	-2	-2	0	-1	-2
t	-3	-3	-1	-1	0
s	-4	-4	-2	-2	-1

Global Edit Distance: -1 (Replace, Match, Delete, Match, Insert)



#### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Searc

Exact Approximate

Methods

Neighbourhood Edit Distance

N-Gram Distance

i ilonetic.

\_ .

Genomi

Algorithm actually depends on parameter!



### Introduction

COMP90049 COMP30018 Knowledge Technologies

Exact

Approximate Application

Methods

Edit Distance

N-Gram Distan

N-Grain Dist

\_ . . .

Lvaidatio

Reference

A[j][k] = max3(
 A[j][k-1] + d, //Deletion
 A[j-1][k] + i, //Insertion
 A[j-1][k-1] + equal(f[k-1],t[j-1])); //Replace or match



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Applicatio

Methods

Edit Distance

N-Gram Distar

Phonetic

Lvaidatio

References

Genomic

```
A[j][k] = max3(
    A[j][k-1] + d, //Deletion
    A[j-1][k] + i, //Insertion
    A[j-1][k-1] + equal(f[k-1],t[j-1])); //Replace or match
```

→ Match score greater than Insert/Delete/Replace

```
e.g. Match (+1), Insert/Delete/Replace (-1)
```



### Introduction

COMP30049 COMP30018 Knowledge Technologies

Exact
Approximate

Approximate Application

Methods

Edit Distance

N-Gram Distan

N-Grain Dist

\_ . . .

Ticici ciioc

```
A[j][k] = min3(
   A[j][k-1] + d, //Deletion
   A[j-1][k] + i, //Insertion
   A[j-1][k-1] + equal(f[k-1],t[j-1])); //Replace or match
```



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Approximate

Methods

Neighbourhood Edit Distance

N-Gram Distan

Contrastia

References

Genomic

```
A[j][k] = min3(
    A[j][k-1] + d, //Deletion
    A[j-1][k] + i, //Insertion
    A[j-1][k-1] + equal(f[k-1],t[j-1])); //Replace or match
```

→ Match score less than Insert/Delete/Replace

```
e.g. Match (0), Insert/Delete/Replace (+1)
```

(Levenshtein Distance)



# **Local Edit Distance**

### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Searcl

Application

Application

Neighbourhood

Edit Distance N-Gram Distance

DI. . . . . . . . . . . .

Evaluatio

Reference

Genomi

Local Edit Distance is like Global Edit Distance, but we are searching for the best substring match



## **Local Edit Distance**

### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

....

Edit Distance

N-Gram Distan

Evaluation

References

Genomi

Local Edit Distance is like Global Edit Distance, but we are searching for the best substring match

Particularly suitable when comparing two strings of very different lengths, e.g. a word and a sentence, or a sentence and an entire document



# Local Edit Distance Algorithm

lf = strlen(f); lt = strlen(t);

## Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search
Exact
Approximate

Methods
Neighbourhood
Edit Distance

N-Gram Distan

Evaluation

References

Genomic

From string f to string t, given array A of |f|+1 columns and |t|+1 rows, we can solve using the Smith–Waterman algorithm:

equal() returns m if characters match, r otherwise

Final score is greatest value in the entire table (or least value, if m < i, d, r)

4 D > 4 P > 4 E > 4 E > 9 Q P



## Introduction

Knowledge **Technologies** 

**Edit Distance** 

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

(For Local Edit Distance, Match must have different +/- sign to Insert/Delete/Replace)



## Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Application

Methods

Edit Distance

N-Gram Distan

\_ . . .

Canami

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

	ε	С	a	r	t
ε					
a					
r					
t					
s					



## Introduction

**Technologies** 

**Edit Distance** 

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1) Initialise table:

	ε	С	a	r	t
$\varepsilon$	0	0	0	0	0
arepsilon a	0 0 0				
r	0				
t	0				
s	0				



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search
Exact

Methods

Edit Distance

N-Gram Distan

Phoneti

Evaluatio

Reference

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, consider three neighbours:

	ε	С	a	r	t
$\varepsilon$	0	0	0	0	0
a r t	0 0 0	?			
r	0				
	0				
s	0				



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Methods

Edit Distance

N-Gram Distar

\_ . . .

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, Delete c:

	$\varepsilon$	С	a	r	t
ε	0	0 -1	0	0	0
arepsilon arts	0 0 0 0	-1			
r	0				
t	0				
s	0				



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search
Exact

Approximate

Application

Neighbourhood
Edit Distance

N-Gram Distai

Evaluatio

Reference

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, Insert a:

	$\varepsilon$	С	a	r	t
ε	0	0	0	0	0
$\varepsilon$ a r t	0 0 0 0	-1			
r	0				
t	0				
s	0				



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search
Exact
Approximate

Methods Neighbourl

Edit Distance

N-Grain Dista

Evaluatio

Reference

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, Replace c with a:

	$\varepsilon$	С	a	r	t
ε	0	0	0	0	0
a	0	-1			
r	0				
t	0				
s	0	0 -1			



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Methods

Edit Distance

N-Gram Distar

\_ . . .

Genomi

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

For c-a correspondence, 0 is better:

	ε	С	a	r	t
ε	0	0	0	0	0
$\varepsilon$ a r t	0000	0			
r	0				
t	0				
s	0				



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Methods

Edit Distance

N-Gram Distan

DI. . . . . . . . . . . .

Evaluatio

Reference

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

For a-a correspondence (Match), 1 is better:

	ε	С	a	r	t
ε	0	0	0	0	0
$\varepsilon$ a r t s	00000	0 0	1		
r	0				
t	0				
s	0				



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search Exact

Application

Neighbou

Edit Distance

N-Gram Distar

Lvaidatio

Reference

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

For a-r correspondence, back to 0:

	ε	С		r	t
ε	0	0	0	0	0
a	0	0	1	0	
r	0				
t	0				
S	0				



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Methods
Neighbourhood
Edit Distance

N-Gram Dista

Evaluatio

Reference

Genomic

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

And so on:

	ε	С	a	r	t
$\overline{\varepsilon}$	0	0	0	0	
a	0	0	1	0	0
a r t	0	0	0	2	1
t	0	0	0	1	3
s	0	0 0 0 0	0	0	2



## Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Application

Neighbourhood Edit Distance

N-Gram Dista

Europeania.

Reference

Genomi

In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

And so on:

	$\varepsilon$	С	a	r	t
$\varepsilon$	0	0	0	0	0
a	0	0	1	0	0
r	0	0	0	2	1
t	0	0	0	1	3
s	0	0	0	0 0 2 1 0	2

Best match: art with art (+3); ties are possible.



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searcl

Approximat

Application

Neighbourhood Edit Distance

N-Gram Distance

Evaluatio

Reference

For strings f and t, Both algorithms above are  $\mathcal{O}(|f||t|)$  in both space and time. (Space can be improved, but time (probably) cannot.)



## Introduction

COMP30049 COMP30018 Knowledge Technologies

String Searc

Approximate

Application

Neighbourhood Edit Distance

N-Gram Distance

Evaluatio

Reference

When approximate matching, we have a constant string f which we want to compare to <u>each</u> string in the dictionary:



## Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Exact
Approximate
Application

Neighbourhood Edit Distance

N-Gram Distance

-----

Evaluation

Reference

Genomi

When approximate matching, we have a constant string f which we want to compare to each string t in the dictionary D:

$$\mathcal{O}(\sum_{t \in D} |f||t|)$$



## Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Exact Approximate

Neighbourhood Edit Distance

N-Gram Distance

\_\_\_\_\_\_

Evaluation

Reference

Genomi

When approximate matching, we have a constant string f which we want to compare to each string t in the dictionary D:

$$\mathcal{O}(|f|\sum_{t\in D}|t|)$$



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc Exact Approximate

Methods Neighbourhood

Edit Distance

N-Gram Distai

References

When approximate matching, we have a constant string f which we want to compare to each string t in the dictionary D:

Hence, integer comparisons are roughly the number of characters in the dictionary. Whether this is feasible depends on the size of the dictionary.



## Introduction

COMP30018 Knowledge Technologies

## String Search

Exact
Approximate
Application

Neighbourhoo

#### N-Gram Distance

\_. .

Evaluatio

Reference

Genomi

N-Gram Distance has same goal as Edit Distance: compare two strings to determine "best" match

A true "distance"



### Introduction

COMP30018 Knowledge Technologies

## String Search

Approximat

Application

Edit Dietance

#### N-Gram Distance

\_. .

Reference

Genomi

N-Gram Distance has same goal as Global Edit Distance, but much simpler



### Introduction

COMP30018 Knowledge Technologies

## String Search

Exact Approximate

Application

Methods Neighbourhoo

N-Gram Distance

Phonetics

Evaluation

References

Genomic

(character) *n*-gram: substring of length *n* 



### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Search

Application

Application

Edit Dietan

N-Gram Distance

Frankricki.

\_ .

n-gram: substring of length n

2-grams of crat: cr, ra, at



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Approximat

Markerde

Edit Dieta

N-Gram Distance

Contrastia

*n*-gram: substring of length *n* 

2-grams of crat: #c, cr, ra, at, t# (sometimes)



## Introduction

COMP30018 Knowledge Technologies

String Search

Approximat Application

Markerde

Edit Distanc

N-Gram Distance

Dhanatian

Evaluatio

Reference

Genomic

n-gram: substring of length n

3-grams of crat: #cr, cra, rat, at#



### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Search

Approximate

Applicat

Edit Distance

N-Gram Distance

\_ \_

n-gram: substring of length n

2-grams of crat: #c, cr, ra, at, t#

2-grams of cart: #c, ca, ar, rt, t#

2-grams of arts: #a, ar, rt, ts, s#

### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Searc Exact

Application

Neighbour

N-Gram Distance

\_ . . .

References

Ganomic

*n*-gram: substring of length *n* 

2-grams of crat: #c, cr, ra, at, t#

2-grams of cart: #c, ca, ar, rt, t#

2-grams of arts: #a, ar, rt, ts, s#

N-Gram Distance between *n*-grams of string  $s\left(G_{n}(s)\right)$  and  $t\left(G_{n}(t)\right)$ :

$$|G_n(s)|+|G_n(t)|-2\times |G_n(s)\cap G_n(t)|$$

### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Applicati

Method

Edit Distance

N-Gram Distance

References

Genomi

*n*-gram: substring of length *n* 

2-grams of crat: #c, cr, ra, at, t#

2-grams of cart: #c, ca, ar, rt, t#

2-grams of arts: #a, ar, rt, ts, s#

2-Gram Distance between crat and cart:

 $|\textit{G}_{2}(\texttt{crat})| + |\textit{G}_{2}(\texttt{cart})| - 2 \times |\textit{G}_{2}(\texttt{crat}) \cap \textit{G}_{2}(\texttt{cart})|$ 

$$=5+5-2\times 2=6$$

### Introduction

COMP90049 COMP30018 Knowledge Technologies

Exact
Approximate

Neighbourhoo Edit Distance

N-Gram Distance

iv didiii bist

Europeanie

References

Genomi

*n*-gram: substring of length *n* 

2-grams of crat: #c, cr, ra, at, t#

2-grams of cart: #c, ca, ar, rt, t#

2-grams of arts: #a, ar, rt, ts, s#

2-Gram Distance between crat and cart:

$$|G_2(\operatorname{crat})| + |G_2(\operatorname{cart})| - 2 \times |G_2(\operatorname{crat}) \cap G_2(\operatorname{cart})|$$

$$=5+5-2\times2=6$$

2-Gram Distance between crat and arts:

$$|G_2(\text{crat})| + |G_2(\text{arts})| - 2 \times |G_2(\text{crat}) \cap G_2(\text{arts})|$$
  
= 5 + 5 - 2 × 0 = 10

### N-Gram Distance

#### Introduction

COMP90049 COMP30018 Knowledge Technologies

Exact Approximate

Methods Neighbourhoo

N-Gram Distance

iv didiii bist

\_ . . .

References

Genomi

*n*-gram: substring of length *n* 

2-grams of crat: #c, cr, ra, at, t#

2-grams of cart: #c, ca, ar, rt, t#

2-grams of arts: #a, ar, rt, ts, s#

2-Gram Distance between crat and cart:

$$|\mathit{G}_{2}(\mathtt{crat})| + |\mathit{G}_{2}(\mathtt{cart})| - 2 imes |\mathit{G}_{2}(\mathtt{crat}) \cap \mathit{G}_{2}(\mathtt{cart})|$$

$$= 5 + 5 - 2 \times 2 = 6$$
 (better)

2-Gram Distance between crat and arts:

$$|G_2(\text{crat})| + |G_2(\text{arts})| - 2 \times |G_2(\text{crat}) \cap G_2(\text{arts})|$$
  
= 5 + 5 - 2 × 0 = 10



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searcl

Exact Approximate

Application

Neighbourho

N-Gram Distance

I-Gram Distanc

Phonetic:

Evaluation

References

icici ciic

Occasionally useful as a simpler variant of (Global) Edit Distance



#### Introduction

Knowledge Technologies

N-Gram Distance

References

Occasionally useful as a simpler variant of Edit Distance

More sensitive to long substring matches, less sensitive to relative ordering of strings (matches can be anywhere!)



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Methods

Edit Distance

N-Gram Distance

England.

References

Ganomi

Occasionally useful as a simpler variant of Edit Distance

More sensitive to long substring matches, less sensitive to relative ordering of strings (matches can be anywhere!)

Despite its simplicity, takes roughly the same time to compare entire dictionary



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searce Exact Approximate

Neighbourhoo

N-Gram Distance

**Evaluatio** 

References

Genomi

Occasionally useful as a simpler variant of Edit Distance

More sensitive to long substring matches, less sensitive to relative ordering of strings (matches can be anywhere!)

Despite its simplicity, takes roughly the same time to compare entire dictionary

Quite useless for very long strings and/or very small alphabets (Why?)



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

### String Searcl

Exact Approximate

Application

Neighbourhood Edit Distance

#### Phonetics

i ilolictic.

Reference

Genomi

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Application

Methods Neighbourhood

N-Gram Distance

**Phonetics** 

Evaluatio

Reference

Genomi

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Salient concern in speech—to—text systems, e.g.: Georgia Conal



#### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Searc

Applicatio

Methods Neighbourhood

Edit Distance
N-Gram Distance

**Phonetics** 

Evaluation

Reference

Genomi

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Salient concern in speech—to—text systems, e.g.: Georgia Conal George O'Connell



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc Exact

Methods Neighbourhood

Edit Distance
N-Gram Distance

#### **Phonetics**

Evaluation

References

Genomi

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Salient concern in speech-to-text systems, e.g.:
You wreck a nice beach



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searcl Exact

Applicatio

Methods Neighbourhood

Edit Distance N-Gram Distance

**Phonetics** 

Evaluation

References

Genomi

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Salient concern in speech—to—text systems, e.g.: You wreck a nice beach You recognize speech



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Application

Methods
Neighbourhood
Edit Distance

Phonetics

Evelvetie.

Reference

Genom

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Salient concern in speech-to-text systems, e.g.: Lowe



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Applicatio

Methods Neighbourhood

Edit Distance N-Gram Distanc

**Phonetics** 

Evaluation

References

Genomi

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Salient concern in speech-to-text systems, e.g.:

Lowe

Lo



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search
Exact

Application

Methods Neighbourhood

N-Gram Distance

Phonetics

Evaluation

References

Genomi

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Salient concern in speech-to-text systems, e.g.:

Lowe

Lo

Lho

Loan

Loe

Loew

Lough

Low ...



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Methods

Neighbourhood Edit Distance N-Gram Distance

**Phonetics** 

Evaluation

Reference

In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Also relevant in spelling correction (English can be very difficult to spell correctly!)



#### Introduction

COMP30049 COMP30018 Knowledge Technologies

#### String Search

Exact Approximate

Applicatio

Neighbourhood

N-Gram Distance

#### **Phonetics**

Lvaiuation

Reference

Genomic

One (ineffectual) mechanism: Soundex



#### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Search

Application

Application

Neighbourhood

N-Gram Distance

#### **Phonetics**

Evaluation

Reference

......

One mechanism: Soundex

```
\mathtt{aehiouwy} \quad \rightarrow \quad 0 \; (vowels)
```

 $\mathtt{bpfv} \quad \rightarrow \quad \textbf{1 (labials)}$ 

 $\texttt{cgjkqsxz} \quad \rightarrow \quad \text{2 (misc: fricatives, velars, etc.)}$ 

Translation table: dt  $\rightarrow$  3 (dentals)

 $1 \rightarrow 4$  (lateral)

mn  $\rightarrow$  5 (nasals)

 $r \rightarrow 6$  (rhotic)



#### Introduction

Knowledge Technologies

**Phonetics** 

References

One mechanism: Soundex

aehiouwy  $\rightarrow$  0 (vowels)

 $bpfv \rightarrow 1$  (labials) cgjkqsxz  $\rightarrow$  2 (misc: fricatives, velars, etc.)

Translation table: 3 (dentals)  $\mathtt{dt} \quad o$ 

 $\rightarrow$  4 (lateral)

 $\rightarrow$  5 (nasals) mn

 $\rightarrow$  6 (rhotic) r

### Four step process:

- Except for initial character, translate string characters according to table
- Remove duplicates (e.g. 4444 → 4)
- Remove 0s
- Truncate to four symbols



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search
Exact

Application

Neighbourhood Edit Distance

N-Gram Distance

### Phonetics

Evaluatio

References

Genomi

### One mechanism: Soundex

 $\texttt{aehiouwy} \quad \rightarrow \quad 0 \; (\texttt{vowels})$ 

 $\mathtt{bpfv} \quad \rightarrow \quad \textbf{1 (labials)}$ 

 $cgjkqsxz \rightarrow 2$  (misc: fricatives, velars, etc.)

Translation table:  ${\tt dt} \quad \to \quad {\tt 3} \; ({\tt dentals})$ 

 $1 \rightarrow 4$  (lateral)

mn  $\rightarrow$  5 (nasals)

 $r \rightarrow 6$  (rhotic)

### Four step process:

king kyngge

k052 k05220

k052 k0520

k52 k52

k52 k52



### Introduction

Knowledge Technologies

#### **Phonetics**

References

### One mechanism: Soundex

aehiouwy  $\rightarrow$  0 (vowels)

 $bpfv \rightarrow 1 (labials)$ 

cgjkqsxz → 2 (misc: fricatives, velars, etc.)

Translation table: 3 (dentals) dt  $\rightarrow$ 

> 4 (lateral) 1  $\rightarrow$

5 (nasals) mn  $\rightarrow$ 6 (rhotic)

 $\rightarrow$ r

### Four step process:

knight night k50203 n0203 k50203 n0203 k523 n23 k523 n23



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search Exact

Application

Neighbourhood Edit Distance

#### **Phonetics**

Evaluatio

References

Genomi

### One mechanism: Soundex

 $\texttt{aehiouwy} \quad \rightarrow \quad 0 \; (\texttt{vowels})$ 

 $\mathtt{bpfv} \quad \rightarrow \quad \textbf{1 (labials)}$ 

 $cgjkqsxz \rightarrow 2$  (misc: fricatives, velars, etc.)

Translation table:  $dt \rightarrow 3$  (dentals)

 $\text{1} \quad \rightarrow \quad \text{4 (lateral)}$ 

mn  $\rightarrow$  5 (nasals)

 $\texttt{r} \quad \rightarrow \quad \text{6 (rhotic)}$ 

### Four step process:

loan	loew	lough	lewicks
1005	1000	10020	1000222
105	10	1020	102
15	1	12	12
15	1	12	12



### Other Phonetic Methods

#### Introduction

Knowledge **Technologies** 

#### **Phonetics**

References

Better phonetic methods make use of the fact that some letters sounds alike in certain contexts, and different in other contexts

Editex uses the Edit Distance to compare strings based on a similar translation table to Soundex

**Ipadist** uses a text-to-sound algorithm to represent tokens according to the International Phonetic Alphabet (but context matters a lot)

There are also worse variants, like Phonix.



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

#### String Searcl

Approximate

Application

Neighbourhood Edit Distance

N-Gram Distance

Phonet

#### **Evaluation**

Reference

Genomic

Evaluation: consider whether the system is effective at solving the user's problem



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Exact

Approximate

Methods Neighbourhood

Edit Distance
N-Gram Distance

Phonet

Evaluation

Reference

Evaluation: consider whether the system is effective at solving the user's problem

In this case: for a misspelled word, does the system identify the correct word?



### Introduction

COMP30018 Knowledge Technologies

String Searc

Approxima Application

Application

Edit Distance

N-Gram Distan

Phonet

#### **Evaluation**

Reference

Genomic

To evaluate, we need:

A number of cases of misspelled words



### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Searc

Approximate Application

Neighbourhood

Edit Distance N-Gram Distance

Phonet

**Evaluation** 

Reference

Genomic

### To evaluate, we need:

- A number of cases of misspelled words
- The intended (correct) word for each case



### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Searc

Applicati

Methods

Edit Distance

Phoneti

**Evaluation** 

Reference

enomic

### To evaluate, we need:

- A number of cases of misspelled words
- The <u>intended</u> (correct) word for each case
- An evaluation metric



### Introduction

COMP30018 Knowledge Technologies

#### String Searcl

Exact Approximate

Methods

Neighbourhoo

N-Gram Distan

\_\_\_\_\_\_

#### Evaluation

References

Genomic

We have some cases:



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searcl

Application

Application

Methods

Edit Distance

Phonet

Evaluation

References

Genomic

Misspelled Word	Correct Word	
ther	other	
corridr	corridor	
cracheyt	crotchety	



### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Search

Application

Mathade

Edit Distance

N-Gram Distan

Phonei

Evaluation

Reference

Genomic

Misspelled Word	Correct Word	Predicted Word
ther	other	there
corridr	corridor	corridor
cracheyt	crotchety	cachet



### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Search
Exact

Application

Methods Neighbourhoo

N-Gram Distance

Phone

Evaluation

Reference

Misspelled Word	Correct Word	Predicted Word	Right/Wrong?
ther	other	there	×
corridr	corridor	corridor	✓
cracheyt	crotchety	cachet	×



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search Exact

Methods

Neighbourhood Edit Distance N-Gram Distance

Phonet

Evaluation

Reference

aenomic

Misspelled Word	Correct Word	Predicted Word	Right/Wrong?
ther	other	there	×
corridr	corridor	corridor	✓
cracheyt	crotchety	cachet	×

**Accuracy**: fraction of correct responses  $(\frac{1}{3})$ 



#### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Searcl Exact

Methods

Neighbourhood Edit Distance N-Gram Distance

Phonet

Evaluation

Reference

Renomic

Misspelled Word	Correct Word	Predicted Word	Right/Wrong?
ther	other	there	×
corridr	corridor	corridor	✓
cracheyt	crotchety	cachet	×

Accuracy: Number of correct predictions
Total number of words



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search
Exact
Approximate

Methods
Neighbourhood
Edit Distance
N-Gram Distance

Phonet

Evaluation

Reference

Genomic

### More realistic situation:

Misspelled Word	Correct Word	Predicted Word
		there
ther	other	other
		their
corridr	corridor	corridor
Corriar	COLLIGOL	carrier
cracheyt	crotchety	???



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc
Exact
Approximate
Application

Methods
Neighbourhood
Edit Distance
N-Gram Distance

Phonet

Evaluation

Reference

D-6----

### More realistic situation:

Misspelled Word	Correct Word	Predicted Word	Right/Wrong?
		there	×
ther	other	other	✓
		their	×
corridr	corridor	corridor	✓
COLLIGI	COILIGOI	carrier	×
cracheyt	crotchety	???	???
•••			



#### Introduction

COMP30049 COMP30018 Knowledge Technologies

Exact
Approximate

Application

Neighbourhood Edit Distance N-Gram Distance

Phonet

**Evaluation** 

Reference

Genomic

Misspelled Word	Correct Word	Predicted Word	Right/Wrong?
		there	×
ther	other	other	✓
		their	×
corridr	corridor	corridor	<b>√</b>
		carrier	×
cracheyt	crotchety	???	_

**Precision**: fraction of correct responses among attempted responses  $(\frac{2}{5})$ 



#### Introduction

COMP90049 COMP30018 Knowledge Technologies

Exact
Approximate
Application

Methods
Neighbourhood
Edit Distance

Dhonotic

Evaluation

Reference

enomic

Misspelled Word	Correct Word	Predicted Word	Right/Wrong?
		there	×
ther	other	other	✓
		their	×
corridr	corridor	corridor	<b>√</b>
Corriar	COILIGOI	carrier	×
cracheyt	crotchety	???	_

**Recall**: proportion of words with a correct response (somewhere)  $(\frac{2}{3})$ 



### Introduction

COMP30049 COMP30018 Knowledge Technologies

### String Searcl

Exact Approximate

Application

Neighbourhood

N-Gram Distance

Tr Gram Brota

## Evaluation

Reference

Canami

Typically, the value of the evaluation metric has little intrinsic meaning



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Approximat

Neighbourhood Edit Distance

N-Gram Dista

Phonet

**Evaluation** 

Reference

Typically, the value of the evaluation metric has little intrinsic meaning

"This system gets 81% accuracy" — useful for users, or not?



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Methods

Neighbourhood Edit Distance N-Gram Distance

Phonet

Evaluation

References

-- The evaluation metric allows us to <u>compare</u> systems:

"The system based on the Global Edit Distance gets 81% accuracy, whereas the system based on the N-Gram Distance gets 84% accuracy"



### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Searc

Approximate
Application

Neighbourhood Edit Distance

N-Gram Distan

**Phonet** 

Evaluation

Reference

enomi

The evaluation metric allows us to <u>compare</u> systems:

"The basic system gets 81% accuracy, but after making some changes, the accuracy becomes 74%"



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Approximate

Application

Neighbourhood

Edit Distance N-Gram Distance

Phonet

Evaluation

Reference

terenc

Typically, comparison is more difficult:

"System A gets 45% precision and 80% recall; System B gets 95% precision and 10% recall"



### Introduction

Knowledge **Technologies** 

Evaluation

References

Typically, comparison is more difficult:

"System A gets 45% precision and 80% recall; System B gets 95% precision and 10% recall"

— Which one should we use? (Also: why?)



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searcl

Exact Approximate

Application

Neighbourhoo

Edit Distance

ir drain biotai

Evaluation

Poforonco

-----

The answer depends on the problem (and the user)!



# Summary

### Introduction

COMP90049 COMP30018 Knowledge Technologies

### String Searc Exact

Methods Neighbourhood

Neighbourhood Edit Distance N-Gram Distance

Phoneti

#### **Evaluation**

References

ielelelik

- What is approximate string search?
- What are some common applications of approximate string search; why are they hard?
- What are some methods for finding an approximate match to a string? What do we need to generate them?
- How can we evaluate a typical approximate matching system?



# Background Readings

# Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searce Exact Approximate Application

Methods Neighbourhood Edit Distance N-Gram Distanc

Phonet

References

Genomic

Needleman, Saul B. and Wunsch, Christian D. (1970). "A general method applicable to the search for similarities in the amino acid sequence of two proteins". Journal of Molecular Biology 48 (3): 44353. doi:10.1016/0022-2836(70)90057-4

(Originally in Russian, published in English as:) Levenshtein, Vladimir I. (1966). "Binary codes capable of correcting deletions, insertions, and reversals". Soviet Physics Doklady 10 (8): 707710.

Smith, Temple F. and Waterman, Michael S. (1981). "Identification of Common Molecular Subsequences". Journal of Molecular Biology 147: 195197. doi:10.1016/0022-2836(81)90087-5

Kondrak, Grzegorz (2005). "N-Gram Similarity and Distance". In Proceedings of the 12th international conference on String Processing and Information Retrieval (SPIRE'05), pp. 115-126, Buenos Aires, Argentina.

Zobel, Justin and Dart, Philip (1996). "Phonetic String Matching: Lessons from Information Retrieval". In Proceedings of the 19th annual international ACM SIGIR conference on Research and development in information retrieval (SIGIR'96), pp. 166-172, New York, USA.



# Extension Readings

#### Introduction

Knowledge Technologies

References

Whitelaw, Casey and Hutchison, Ben and Chung, Grace Y and Ellis, Gerard (2009). "Using the Web for Language Independent Spellchecking and Autocorrection". In Proceedings of the 2009 Conference on Empirical Methods in Natural Language Processing (EMNLP 2009), pp. 890-899, Singapore, Singapore.

Ahmad, Faroog and Kondrak, Grzegorz (2005). "Learning a Spelling Error Model from Search Query Logs". In Proceedings of the Human Technology Conference and Conference on Empirical Methods in Natural Language Processing (HLT/EMNLP 2005), pp. 955-962. Vancouver, Canada.



# Computational Genomics

### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Methods

Neighbourhood
Edit Distance

Dhonot

Evaluation

References

Genomics

## Typical Genomics problem:

- Given a nucleotide/amino acid sequence (substring)
- Find whether the sequence occurs within a larger sequence (string)
- Possibly with "errors" (nucleotide/amino acid changes)



## Computational Genomics

### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Application

Methods

Neighbourhood Edit Distance N-Gram Distance

Phoneti

Evaluation

Reference

Genomics

## Typical Genomics problem:

- Given a substring, find whether the sequence occurs within a larger string, possibly with "errors"
- Almost the same as spelling correction, flipped around



## **Computational Genomics**

#### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc Exact Approximate

Methods Neighbourhood

Neighbourhood Edit Distance N-Gram Distance

**Phonet** 

Evaluation

References

Genomics

## Typical Genomics problem:

- Given a substring, find whether the sequence occurs within a larger string, possibly with "errors"
- Almost the same as spelling correction
- But much larger strings: a small genomics problem might involve comparing perhaps 1K character sequence against several 100K character sequences; alphabet is smaller



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searcl

Approximat Application

Neighbourhood Edit Distance

N-Gram Distar

**Phonet** 

Evaluatio

References

Genomics

Recall: we have a "short" ( $\sim$ 1K character) nucleotide/amino acid sequence to compare against many long ( $\sim$ 100K character) chromosomes/genes/proteins/etc.



### Introduction

COMP30049 COMP30018 Knowledge Technologies

## String Searc

Approximat

Methods

Edit Distance

DI .....

Evaluatio

Reference

Genomics

Recall: we have a "short" ( $\sim$ 1K character) string to compare against many long ( $\sim$ 100K character) strings



### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Searc Exact

Application

**/lethods** Neighbourhood

Edit Distance N-Gram Distance

Phonet

Evaluatio

References

Genomics

Recall: we have a "short" ( $\sim$ 1K character) string to compare against many long ( $\sim$ 100K character) strings

For example, if some member of the population has 99% of the sequence of interest, they might be susceptible to some medical condition



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc Exact

Methods

Edit Distance
N-Gram Distance

Phonet

Evaluation

References

Genomics

Recall: we have a "short" ( $\sim$ 1K character) string to compare against many long ( $\sim$ 100K character) strings

We're allowed  $\sim$ 10 errors; alphabet is  $\sim$ 4 or  $\sim$ 20 characters



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Approximat

Application

Neighbourhood Edit Distance

N-Gram Distance

Phonet

Evaluation

Reference

Genomics

Neighbourhood search:

Roughly  $4^{10}\times 1000^{10}$  possible neighbours.



### Introduction

Knowledge **Technologies** 

Genomics

Roughly  $4^{10} \times 1000^{10}$  possible neighbours.

... Forget it.

Neighbourhood search:



### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Search

Approximat Application

Application

Edit Distance

N-Gram Distan

Phonet

Evaluation

Reference

Genomics

### Global Edit Distance:

One string is  $\sim$ 1K characters, other is  $\sim$ 100K characters.



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc Exact

Methods

Neighbourhood Edit Distance N-Gram Distance

Phonet

**Evaluatio** 

Reference

Genomics

### Global Edit Distance:

One string is  $\sim 1 \text{K}$  characters, other is  $\sim 100 \text{K}$  characters.

- ... Every string comparison involves ~99K insertions.
- → Prefers shorter chromosomes (not intended behaviour)



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Applicatio

Methods Neighbourhood

Edit Distance N-Gram Distan

Phoneti

Evaluatio

Reference

Genomics

### Local Edit Distance:

One string is  $\sim$ 1K characters, other is  $\sim$ 100K characters.

... Seems like the right idea.



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc

Applicatio

Methods Neighbourhood

Edit Distance N-Gram Distance

Phoneti

Evaluatio

Reference

Genomics

## Local Edit Distance:

One string is  $\sim$ 10K characters, other is  $\sim$ 1G characters.

... Can't fit table into memory.



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Searc Exact

Methods

Neighbourhood Edit Distance N-Gram Distance

Phonetic

**Evaluatio** 

Reference

Genomics

### Local Edit Distance:

One string is  $\sim$ 10K characters, other is  $\sim$ 1G characters.

... Requires approximate solutions with heuristics, e.g. BLAST, FASTA



### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Searc

Approximat Application

Application

Neighbourhood Edit Distance

N-Gram Dista

Phonet

Evaluation

Reference

Genomics

### N-Gram Distance:

With huge *n* (e.g. 80% of length of shorter string) can (almost) work!



### Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Applicatio

Methods

Neighbourhood Edit Distance

Dhanat

**Evaluatio** 

Reference

Genomics

N-Gram Distance:

Surprisingly, can (almost) work!

Tends to prefer shorter chromosomes like Global Edit Distance



### Introduction

COMP30049 COMP30018 Knowledge Technologies

String Searc

Approximat Application

Neighbourhood

Edit Distance N-Gram Distance

Phonet

Evaluation

Reference

Genomics

### N-Gram Distance:

But better methods for using *n*-gram information, e.g. de Bruijn graphs