

**Lecture 18:
Feature Selection**

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Filtering methods

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Common Issues

Practical
considerations

Summary

Lecture 18: Feature Selection

COMP90049 Knowledge Technologies

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Semester 2, 2018



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We want to get knowledge out of a data set:

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Data set:

Outlook	Temperature	Humidity	Windy	Play
sunny	hot	high	FALSE	no
sunny	hot	high	TRUE	no
overcast	hot	high	FALSE	yes
rainy	mild	high	FALSE	yes
rainy	cool	normal	FALSE	yes
rainy	cool	normal	TRUE	no
:	:	:	:	:

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Summary

Instances:

Outlook	Temperature	Humidity	Windy	Play
INSTANCE ₁	INSTANCE ₁	INSTANCE ₁	INSTANCE ₁	INSTANCE ₁
sunny	hot	high	FALSE	no
INSTANCE ₂	INSTANCE ₂	INSTANCE ₂	INSTANCE ₂	INSTANCE ₂
sunny	hot	high	TRUE	no
overcast	hot	high	FALSE	yes
rainy	mild	high	FALSE	yes
rainy	cool	normal	FALSE	yes
rainy	cool	normal	TRUE	no
⋮	⋮	⋮	⋮	⋮

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Summary

Attributes:

Outlook	Temperature	Humidity	Windy	Play
sunny	hot	high	FALSE	no
sunny	hot	high	TRUE	no
overcast	hot	high	FALSE	yes
rainy	mid	high	FALSE	yes
rainy	cool	normal	FALSE	yes
rainy	cool	normal	TRUE	no
		:	:	:

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Summary

We want to get knowledge out of a data set:

- Where do instances come from?
 - Examples from real world data

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Summary

We want to get knowledge out of a data set:

- Where do instances come from?
 - Examples from real world data
- Where do attributes come from?
 - ???

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Summary

We want to get knowledge out of a data set:

- Where do instances come from?
 - Examples from real world data
- Where do attributes come from?
 - (Hopefully) meaningful features of the problem
 - Anything that might capture regularity in the data

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Outlook	Temperature	Humidity	Windy	Play
sunny	hot	high	FALSE	no
sunny	hot	high	TRUE	no
overcast	hot	high	FALSE	yes
rainy	mild	high	FALSE	yes
rainy	cool	normal	FALSE	yes
rainy	cool	normal	TRUE	no
:	:	:	:	:

- Windy seems like a good predictor of Play
- Humidity seems like a less good predictor of Play

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Summary

We want to get knowledge out of a data set:

- Where do instances come from?
 - Examples from real world data
- Where do attributes come from?
 - (Hopefully) meaningful features of the problem
 - Anything that might capture regularity in the data
- Where do models come from?
 - ???

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Models:



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Summary

We want to get knowledge out of a data set:

- Where do instances come from?
 - Examples from real world data
- Where do attributes come from?
 - (Hopefully) meaningful features of the problem
 - Anything that might capture regularity in the data
- Where do models come from?
 - Need to choose a model suitable for our data set

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Summary

How to do Machine Learning:

1 Pick a feature representation

2

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6

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Summary

How to do Machine Learning:

- 1 Pick a feature representation
- 2 Compile data
- 3
- 4
- 5
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Summary

How to do Machine Learning:

- 1 Pick a feature representation
- 2 Compile data
- 3 Pick a (suitable) algorithm for building a model
- 4
- 5
- 6

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Summary

How to do Machine Learning:

- 1 Pick a feature representation
- 2 Compile data
- 3 Pick a (suitable) algorithm for building a model
- 4 Train the model
- 5
- 6

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Summary

How to do Machine Learning:

- 1 Pick a feature representation
- 2 Compile data
- 3 Pick a (suitable) algorithm for building a model
- 4 Train the model
- 5 Classify development data, evaluate results
- 6

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Summary

How to do Machine Learning:

- 1 Pick a feature representation
- 2 Compile data
- 3 Pick a (suitable) algorithm for building a model
- 4 Train the model
- 5 Classify development data, evaluate results
- 6 Probably: *go to (1)*

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Summary

How to do Machine Learning:

- 1 [0.] Get hired!
- 2 Pick a feature representation
- 3 Compile data
- 4 Pick a (suitable) algorithm for building a model
- 5 Train the model
- 6 Classify development data, evaluate results
- 7 Probably: *go to (1)*

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Summary

Our job as Machine Learning experts:

- Choose an algorithm suitable for classifying the data according to the attributes
- Choose attributes suitable for classifying the data according to the model

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Summary

Our job as Machine Learning experts:

- Choose an algorithm suitable for classifying the data according to the attributes
- Choose attributes suitable for classifying the data according to the model
 - Inspection
 - Intuition

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Summary

Our job as Machine Learning experts:

- Choose an algorithm suitable for classifying the data according to the attributes
- Choose attributes suitable for classifying the data according to the model
 - Inspection
 - Intuition
 - Neither possible in practice

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Summary

Our job as Machine Learning experts:

- Choose an algorithm suitable for classifying the data according to the attributes
- Choose attributes suitable for classifying the data according to the model
 - Inspection
 - Intuition
 - Neither possible in practice
 - Throw everything we can think of at the problem and let the algorithm decide!

What makes features good?

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Summary

Better models!

- Better performance according to some evaluation metric

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Summary

Better models!

- Better performance according to some evaluation metric

Side-goal:

- Tell us interesting things about the problem

What makes features good?

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Summary

Better models!

- Better performance according to some evaluation metric

Side-goal:

- Tell us interesting things about the problem

Side-goal:

- Fewer features \rightarrow smaller models \rightarrow faster answer

What makes features good?

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Summary

Better models!

- Better performance according to some evaluation metric

Side-goal:

- Tell us interesting things about the problem

Side-goal:

- Fewer features \rightarrow smaller models \rightarrow faster answer
 - More accurate answer \gg faster answer

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“Wrapper” methods:

- Choose subset of attributes that give best performance on the development data

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Summary

“Wrapper” methods:

- Choose subset of attributes that give best performance on the development data
- For example: for the Weather data set:
 - Train model on {Outlook}

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Summary

“Wrapper” methods:

- Choose subset of attributes that give best performance on the development data
- For example: for the Weather data set:
 - Train model on {Outlook}
 - Train model on {Temperature}
 - ...

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Summary

“Wrapper” methods:

- Choose subset of attributes that give best performance on the development data
- For example: for the Weather data set:
 - Train model on {Outlook}
 - Train model on {Temperature}
 - ...
 - Train model on {Outlook, Temperature}
 - ...
 - Train model on {Outlook, Temperature, Humidity}
 - ...
 - Train model on {Outlook, Temperature, Humidity, Windy}

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Summary

“Wrapper” methods:

- Choose subset of attributes that give best performance on the development data
- For example: for the Weather data set:
 - Evaluate model on {Outlook}
 - Evaluate model on {Temperature}
 - ...
 - Evaluate model on {Outlook, Temperature}
 - ...
 - Evaluate model on {Outlook, Temperature, Humidity}
 - ...
 - Evaluate model on {Outlook, Temperature, Humidity, Windy}

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Summary

“Wrapper” methods:

- Choose subset of attributes that give best performance on the development data
- For example: for the Weather data set:
 - Evaluate model on {Outlook}
 - Evaluate model on {Temperature}
 - ...
 - Evaluate model on {Outlook, Temperature}
 - ...
 - Evaluate model on {Outlook, Temperature, Humidity}
 - ...
 - Evaluate model on {Outlook, Temperature, Humidity, Windy}
- Best performance on data set → best feature set

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Summary

“Wrapper” methods:

- Choose subset of attributes that give best performance on the development data
- Advantages:
 - Feature set with optimal performance on development data

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Summary

“Wrapper” methods:

- Choose subset of attributes that give best performance on the development data
- Advantages:
 - Feature set with optimal performance on development data
- Disadvantages:
 - Takes a **long** time

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Summary

Assume we have a fast method (e.g. Naive Bayes) over a data set of non-trivial size ($\sim 10K$ instances):

- Assume: train–evaluate cycle takes 10 sec to complete

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Summary

Assume we have a fast method (e.g. Naive Bayes) over a data set of non-trivial size ($\sim 10K$ instances):

- Assume: train–evaluate cycle takes 10 sec to complete

How many cycles? For m features:

- 2^m subsets = $\frac{2^m}{6}$ minutes

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Assume we have a fast method (e.g. Naive Bayes) over a data set of non-trivial size ($\sim 10K$ instances):

- Assume: train–evaluate cycle takes 10 sec to complete

How many cycles? For m features:

- 2^m subsets = $\frac{2^m}{6}$ minutes
- $m = 10 \rightarrow 3$ hours

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Summary

Assume we have a fast method (e.g. Naive Bayes) over a data set of non-trivial size ($\sim 10K$ instances):

- Assume: train-evaluate cycle takes 10 sec to complete

How many cycles? For m features:

- 2^m subsets = $\frac{2^m}{6}$ minutes
- $m = 10 \rightarrow 3$ hours
- $m = 60 \rightarrow$ heat death of universe

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Assume we have a fast method (e.g. Naive Bayes) over a data set of non-trivial size ($\sim 10K$ instances):

- Assume: train–evaluate cycle takes 10 sec to complete

How many cycles? For m features:

- 2^m subsets = $\frac{2^m}{6}$ minutes
- $m = 10 \rightarrow 3$ hours
- $m = 60 \rightarrow$ heat death of universe

Only practical for very small data sets.

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Summary

Greedy approach:

- Train and evaluate model on each single attribute
- Choose best attribute

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Summary

Greedy approach:

- Train and evaluate model on each single attribute
- Choose best attribute
- Until convergence:
 - Train and evaluate model on best attribute(s), plus each remaining single attribute
 - Choose best attribute out of the remaining set
- Iterate until performance (e.g. accuracy) stops increasing

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Summary

Greedy approach:

- Bad news:
 - Takes $\frac{1}{2}m^2$ cycles, for m attributes
 - In theory, 386 attributes \rightarrow days

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Summary

Greedy approach:

- **Bad** Good news:
 - Takes $\frac{1}{2}m^2$ cycles, for m attributes
 - In practice, converges much more quickly than this

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Summary

Greedy approach:

- ~~Bad~~ Good ~~Bad~~ news:
 - Takes $\frac{1}{2}m^2$ cycles, for m attributes
 - In practice, converges much more quickly than this
 - Converges to a sub-optimal (and often very bad) solution

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Summary

“Ablation” approach:

- Start with all attributes
- Remove one attribute, train and evaluate model

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Summary

“Ablation” approach:

- Start with all attributes
- Remove one attribute, train and evaluate model
- Until divergence:
 - From remaining attributes, remove each attribute, train and evaluate model
 - Remove attribute that causes least performance degradation
- Termination condition usually: performance (e.g. accuracy) starts to degrade by more than ϵ

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Summary

“Ablation” approach:

- Good news:
 - Mostly removes irrelevant attributes (at the start)

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Summary

“Ablation” approach:

- Good news:
 - Mostly removes irrelevant attributes (at the start)
- Bad news:
 - Assumes independence of attributes (both approaches; worse than Naive Bayes!)
 - Actually does take $O(m^2)$ time; cycles are slower with more attributes

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Summary

“Embedded” methods:

- Some models actually perform feature selection as part of the algorithm!

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Summary

“Embedded” methods:

- Some models actually perform feature selection as part of the algorithm!
 - Most notably, linear classifiers
 - To some degree: Decision Trees
- (More on these models in later lectures.)

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Summary

“Embedded” methods:

- Some models actually perform feature selection as part of the algorithm!
 - Most notably, linear classifiers
 - To some degree: Decision Trees
- Often benefit from other feature selection approaches anyway

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Summary

Intuition: possible to evaluate “goodness” of each feature, separate from other features

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Summary

Intuition: possible to evaluate “goodness” of each feature, separate from other features

- Consider each feature separately: linear time in number of attributes
- Typically most popular strategy
- Possible (but difficult) to control for inter-dependence of features

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What makes a feature set good?

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What makes a feature set good?

- Better models!

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Summary

What makes a ~~feature set~~ single feature good?

- Better models!

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Summary

What makes a ~~feature set~~ single feature good?

- ~~Better models!~~
- Well correlated with class

Toy example

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Summary

a_1	a_2	c
Y	Y	Y
Y	N	Y
N	Y	N
N	N	N

Which of a_1 , a_2 is good?

Toy example

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Summary

a_1	a_2	c
Y	Y	Y
Y	N	Y
N	Y	N
N	N	N

a_1 is probably good.

Toy example

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Summary

a_1	a_2	c
Y	Y	Y
Y	N	Y
N	Y	N
N	N	N

a_2 is probably not good.

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Summary

Recall independence:

$$P(A, C) = P(A)P(C)$$

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Summary

Recall independence:

$$P(A, C) = P(A)P(C)$$

This formula holds if attribute is independent from class.

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Summary

Recall independence:

$$\frac{P(A, C)}{P(A)P(C)} = 1$$

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Summary

Recall independence:

$$\frac{P(A, C)}{P(A)P(C)} = 1$$

- If LHS ~ 1 , attribute and class occur together as often as we would expect from random chance
- If LHS $\gg 1$, attribute and class occur together much more often than randomly.
- (If LHS $\ll 1$, attribute and class are negatively correlated. More on this later.)

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Summary

Pointwise mutual information:

$$PMI(A, C) = \log_2 \frac{P(A, C)}{P(A)P(C)}$$

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Summary

Pointwise mutual information:

$$PMI(A, C) = \log_2 \frac{P(A, C)}{P(A)P(C)}$$

Attributes with greatest PMI: best attributes

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Summary

a_1	a_2	c
Y	Y	Y
Y	N	Y
N	Y	N
N	N	N

Calculate PMI of a_1 , a_2 with respect to c

Toy example, revisited

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Summary

a_1	a_2	c
Y	Y	Y
Y	N	Y
N	Y	N
N	N	N

$$P(a_1) = \frac{2}{4}; P(c) = \frac{2}{4}; P(a_1, c) = \frac{2}{4}$$

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Summary

a_1	a_2	c
Y	Y	Y
Y	N	Y
N	Y	N
N	N	N

$$\begin{aligned} PMI(a_1, c) &= \log_2 \frac{\frac{1}{2}}{\frac{1}{2} \cdot \frac{1}{2}} \\ &= \log_2(2) = 1 \end{aligned}$$

Toy example, revisited

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Summary

a_1	a_2	c
Y	Y	Y
Y	N	Y
N	Y	N
N	N	N

$$P(a_2) = \frac{2}{4}; P(c) = \frac{2}{4}; P(a_2, c) = \frac{1}{4}$$

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Summary

a_1	a_2	c
Y	Y	Y
Y	N	Y
N	Y	N
N	N	N

$$\begin{aligned} PMI(a_2, c) &= \log_2 \frac{\frac{1}{4}}{\frac{1}{2} \cdot \frac{1}{2}} \\ &= \log_2(1) = 0 \end{aligned}$$

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Summary

What makes a single feature good?

- Well correlated with class

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Summary

What makes a single feature good?

- Well correlated with class
 - Knowing a lets us predict c with more confidence

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Summary

What makes a single feature good?

- Well correlated with class
 - Knowing a lets us predict c with more confidence
- **Reverse correlated** with class
 - Knowing \bar{a} lets us predict c with more confidence
 - Just as good

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Summary

What makes a single feature good?

- Well correlated with class
 - Knowing a lets us predict c with more confidence
- Reverse correlated with class
 - Knowing \bar{a} lets us predict c with more confidence
- Well correlated (or reverse correlated) with not class
 - Knowing a lets us predict \bar{c} with more confidence
 - Usually not quite as good, but still useful

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Summary

Mutual information: combine each a , \bar{a} , c , \bar{c} PMI

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Summary

Contingency tables: compact representation of these frequency counts

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Summary

Contingency tables: compact representation of these frequency counts

	a	\bar{a}
c	$\sigma(a, c)$	$\sigma(\bar{a}, c)$
\bar{c}	$\sigma(a, \bar{c})$	$\sigma(\bar{a}, \bar{c})$

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Summary

Contingency tables: compact representation of these frequency counts

	a	\bar{a}	Total
c	$\sigma(a, c)$	$\sigma(\bar{a}, c)$	$\sigma(c)$
\bar{c}	$\sigma(a, \bar{c})$	$\sigma(\bar{a}, \bar{c})$	$\sigma(\bar{c})$
Total	$\sigma(a)$	$\sigma(\bar{a})$	N

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Summary

Contingency tables: compact representation of these frequency counts

	a	\bar{a}	Total
c	$\sigma(a, c)$	$\sigma(\bar{a}, c)$	$\sigma(c)$
\bar{c}	$\sigma(a, \bar{c})$	$\sigma(\bar{a}, \bar{c})$	$\sigma(\bar{c})$
Total	$\sigma(a)$	$\sigma(\bar{a})$	N

$$P(a, c) = \frac{\sigma(a, c)}{N}, \text{ etc.}$$

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Contingency tables for toy example:

a_1	a_2	c
Y	Y	Y
Y	N	Y
N	Y	N
N	N	N

a_1	$a = Y$	$a = N$	Total
$c = Y$	2	0	2
$c = N$	0	2	2
Total	2	2	4

a_2	$a = Y$	$a = N$	Total
$c = Y$	1	1	2
$c = N$	1	1	2
Total	2	2	4

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Summary

$$MI(A, C) = P(a, c)PMI(a, c) + P(\bar{a}, c)PMI(\bar{a}, c) + P(a, \bar{c})PMI(a, \bar{c}) + P(\bar{a}, \bar{c})PMI(\bar{a}, \bar{c})$$

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Summary

$$\begin{aligned} MI(A, C) = & P(a, c) \log_2 \frac{P(a, c)}{P(a)P(c)} + P(\bar{a}, c) \log_2 \frac{P(\bar{a}, c)}{P(\bar{a})P(c)} + \\ & P(a, \bar{c}) \log_2 \frac{P(a, \bar{c})}{P(a)P(\bar{c})} + P(\bar{a}, \bar{c}) \log_2 \frac{P(\bar{a}, \bar{c})}{P(\bar{a})P(\bar{c})} \end{aligned}$$

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Summary

Often written more compactly as:

$$MI(A, C) = \sum_{i \in \{a, \bar{a}\}} \sum_{j \in \{c, \bar{c}\}} P(i, j) \log_2 \frac{P(i, j)}{P(i)P(j)}$$

(This representation can be extended to different types of attributes more intuitively.)

Note that $0 \log 0 \equiv 0$.

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Summary

Contingency table for toy example:

a_1	a_2	c
Y	Y	Y
Y	N	Y
N	Y	N
N	N	N

a_1	$a=Y$	$a=N$	Total
$c=Y$	2	0	2
$c=N$	0	2	2
Total	2	2	4

$$P(a, c) = \frac{2}{4}; P(a) = \frac{2}{4}; P(c) = \frac{2}{4}$$

$$P(\bar{a}, \bar{c}) = \frac{2}{4}; P(\bar{a}) = \frac{2}{4}; P(\bar{c}) = \frac{2}{4}$$

$$P(\bar{a}, c) = 0; P(a, \bar{c}) = 0$$

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Summary

$$\begin{aligned} MI(A_1, C) &= P(a_1, c) \log_2 \frac{P(a_1, c)}{P(a_1)P(c)} + P(\bar{a}_1, c) \log_2 \frac{P(\bar{a}_1, c)}{P(\bar{a}_1)P(c)} + \\ &\quad P(a_1, \bar{c}) \log_2 \frac{P(a_1, \bar{c})}{P(a_1)P(\bar{c})} + P(\bar{a}_1, \bar{c}) \log_2 \frac{P(\bar{a}_1, \bar{c})}{P(\bar{a}_1)P(\bar{c})} \\ &= \frac{1}{2} \log_2 \frac{\frac{1}{2}}{\frac{1}{2} \frac{1}{2}} + 0 \log_2 \frac{0}{\frac{1}{2} \frac{1}{2}} + 0 \log_2 \frac{0}{\frac{1}{2} \frac{1}{2}} + \frac{1}{2} \log_2 \frac{\frac{1}{2}}{\frac{1}{2} \frac{1}{2}} \\ &= \frac{1}{2}(1) + 0 + 0 + \frac{1}{2}(1) = 1 \end{aligned}$$

Mutual Information Example

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Summary

Contingency table for toy example:

a_1	a_2	c
Y	Y	Y
Y	N	Y
N	Y	N
N	N	N

a_2	$a=Y$	$a=N$	Total
$c=Y$	1	1	2
$c=N$	1	1	2
Total	2	2	4

$$P(a, c) = \frac{1}{4}; P(a) = \frac{2}{4}; P(c) = \frac{2}{4}$$

$$P(\bar{a}, \bar{c}) = \frac{1}{4}; P(\bar{a}) = \frac{2}{4}; P(\bar{c}) = \frac{2}{4}$$

$$P(\bar{a}, c) = \frac{1}{4}; P(a, \bar{c}) = \frac{1}{4}$$

Mutual Information Example

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Summary

$$\begin{aligned} MI(A_2, C) &= P(a_2, c) \log_2 \frac{P(a_2, c)}{P(a_2)P(c)} + P(\bar{a}_2, c) \log_2 \frac{P(\bar{a}_2, c)}{P(\bar{a}_2)P(c)} + \\ &\quad P(a_2, \bar{c}) \log_2 \frac{P(a_2, \bar{c})}{P(a_2)P(\bar{c})} + P(\bar{a}_2, \bar{c}) \log_2 \frac{P(\bar{a}_2, \bar{c})}{P(\bar{a}_2)P(\bar{c})} \\ &= \frac{1}{4} \log_2 \frac{\frac{1}{4}}{\frac{1}{2} \frac{1}{2}} + \frac{1}{4} \log_2 \frac{\frac{1}{4}}{\frac{1}{2} \frac{1}{2}} + \frac{1}{4} \log_2 \frac{\frac{1}{4}}{\frac{1}{2} \frac{1}{2}} + \frac{1}{4} \log_2 \frac{\frac{1}{4}}{\frac{1}{2} \frac{1}{2}} \\ &= \frac{1}{4}(0) + \frac{1}{4}(0) + \frac{1}{4}(0) + \frac{1}{4}(0) = 0 \end{aligned}$$

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Summary

Check the value we actually observed $O(W)$ with the expected value $E(W)$:

- If the observed value is much greater than the expected value, a occurs more often with c than we would expect at random — predictive
- If the observed value is much lesser than the expected value, a occurs less often with c than we would expect at random — predictive
- If the observed value is close to the expected value, a occurs as often with c as we would expect randomly — not predictive

Similarly with X , Y , Z

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Summary

Actual calculation (written more compactly):

$$\chi^2 = \sum_{i=1}^r \sum_{j=1}^c \frac{(O_{i,j} - E_{i,j})^2}{E_{i,j}}$$

(i sums over rows and j sums over columns.)

In practice, there are simpler ways to calculate this for 2×2 contingency tables.

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Summary

So far, we've only looked at binary (Y/N) attributes:

- Nominal attributes
- Continuous attributes
- Ordinal attributes

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Summary

Nominal attributes (e.g. `Outlook={sunny, overcast, rainy}`).
Two common strategies:

- 1 Treat as multiple binary attributes:
 - e.g. `sunny=Y, overcast=N, rainy=N`, etc.
 - Can just use the formulae as given
 - Results often difficult to interpret
 - For example, `Outlook=sunny` is useful, but `Outlook=overcast` and `Outlook=rainy` are not useful... Should we use `Outlook`?
- 2 Modify contingency tables (and formulae)

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Summary

Modified contingency table:

0	s	o	r
$c=Y$	U	V	W
$c=N$	X	Y	Z

Modified MI:

$$\begin{aligned}
 MI(O, C) &= \sum_{i \in \{s, o, r\}} \sum_{j \in \{c, \bar{c}\}} P(i, j) \log_2 \frac{P(i, j)}{P(i)P(j)} \\
 &= P(s, c) \log_2 \frac{P(s, c)}{P(s)P(c)} + P(s, \bar{c}) \log_2 \frac{P(s, \bar{c})}{P(s)P(\bar{c})} + \\
 &\quad P(o, c) \log_2 \frac{P(o, c)}{P(o)P(c)} + P(o, \bar{c}) \log_2 \frac{P(o, \bar{c})}{P(o)P(\bar{c})} + \\
 &\quad P(r, c) \log_2 \frac{P(r, c)}{P(r)P(c)} + P(r, \bar{c}) \log_2 \frac{P(r, \bar{c})}{P(r)P(\bar{c})}
 \end{aligned}$$

- Biased towards attributes with many values. (Why?)

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Summary

Continuous attributes:

- Usually dealt with by estimating probability based on a Gaussian (normal) distribution
- With a large number of values, most random variables are normally distributed due to the **Central Limit Theorem**
- For small data sets or pathological features, we typically need to use messy binomial/multinomial distributions

All of this is (unsurprisingly) beyond the scope of this subject

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Summary

Ordinal attributes (e.g. low, med, high or 1,2,3,4).
Three possibilities, roughly in order of popularity:

- 1 Treat as binary
 - Particularly appropriate for frequency counts where events are low-frequency (e.g. words in tweets)
- 2 Treat as nominal (i.e. throw away ordering)
- 3 Treat as continuous
 - The fact that we haven't *seen* any intermediate values is usually not important
 - Does have all of the technical downsides of continuous attributes, however

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Summary

So far, we've only looked at binary (Y/N) classification tasks.

What makes a single feature good?

- Highly correlated with class
- Highly reverse correlated with class
- Highly correlated (or reverse correlated) with not class

... What if there are many classes?

Multiclass (e.g., RightTroll, LeftTroll, and Other) classification tasks are usually much more difficult.

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Summary

What makes a feature **bad**?

- Irrelevant

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Summary

What makes a feature **bad**?

- Irrelevant
- Correlated with other features

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Summary

What makes a feature **bad**?

- Irrelevant
- Correlated with other features
- Good at only predicting one class (but is this truly bad?)

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Summary

Consider multi-class problem over R, L, O:

- PMI, MI, χ^2 are all calculated *per-class*
- (Some other feature selection metrics, e.g. Information Gain, work for all classes at once)
- Need to make a point of selecting (hopefully uncorrelated) features for *each* class to give our classifier the best chance of predicting everything correctly.

Multi-class problems—Example 1

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Summary

Actual example (MI):

R	L	O
breaking	the	the
maga	and	to
rtamerica	a	is
retweet	black	a
beeth	i	and
bbbsp	is	this
tcot	news	rt
obama	to	of
hillary	blacklivesmatter	breaking
pjnet	this	on

Multi-class problems—Example 1

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Summary

Actual example (χ^2):

R	L	O
breaking	the	the
maga	and	to
rtamerica	a	is
retweet	black	a
beeth	i	and
tcot	is	of
bbbsp	blacklivesmatter	this
obama	this	rt
hillary	to	on
rt	amp	dallas

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Summary

Actual example (MI):

B	H	Se	SD	W
boston	houston	seattle	diego	dc
diego	diego	diego	san	diego
san	jupdicom	wa	chargers	san
httpbitlyczmk	tx	san	sd	obama
ma	san	cheezburger	sdut	health
redsox	httpbitlycdqk	boston	seattle	washington
seattle	seattle	bellevue	sandiego	bill

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Summary

Intuitive features:

B	H	Se	SD	W
boston	houston	seattle	diego	dc
diego	diego	diego	san	diego
san	jupdicom	wa	chargers	san
httpbitlyczmk	tx	san	sd	obama
ma	san	cheezburger	sdut	health
redsox	httpbitlycdqk	boston	seattle	washington
seattle	seattle	bellevue	sandiego	bill

Lecture 18: Feature Selection

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Machine Learning

Feature Selection

Wrappers
Embedded
Filters

Filtering methods

PMI
MI
 χ^2

Common Issues

Practical
considerations

Summary

Features for predicting not class (MI):

B	H	Se	SD	W
boston	houston	seattle	diego	dc
diego	diego	diego	san	diego
san	jupdicom	wa	chargers	san
httpbitlyczmk	tx	san	sd	obama
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Unintuitive features:

B	H	Se	SD	W
boston	houston	seattle	diego	dc
diego	diego	diego	san	diego
san	jupdicom	wa	chargers	san
httpbitlyczmk	tx	san	sd	obama
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Summary

Mutual Information is biased toward rare, uninformative features

- All probabilities: no notion of the raw frequency of events
- If a feature is seen rarely, but always with a given class, it will be seen as “good”
- For example: `httpbitlyczmk` occurs 447 times out of 750K instances, but often with B. Is this meaningful?
- Best features in the Twitter dataset only had MI of about 0.1 bits; 100th best for a given class had MI of about 0.0001 bits

So... Give up on feature selection then?

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Summary

No way!

- Even marginally relevant features usually a vast improvement on an unfiltered data set
- Some models **need** feature selection
 - k-Nearest Neighbour, hugely
 - Naive Bayes, Decision Trees, and SVM to a lesser extent
- Machine learning experts (us!) need to think about the data!

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Summary

- Wrappers vs. Embedded methods vs. Filters
- Popular filters: PMI, MI, χ^2 , how should we use them and what are the results going to look like
- Importance of feature selection for different methods (even though it often isn't the solution we were hoping for)

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