

Team notebook

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1 DP

1.1 DivideAndConquer

```
#include <bits/stdc++.h>
using namespace std;

typedef long long ll;
#define repx(i, a, b) for (int i = (int)a; i < (int)b; i++)
#define ff first
#define ss second

ll cost(int i, int j) { return ; }

vector<ll> last, now;

void compute(int l, int r, int optl, int optr)
{
    if (l > r) return;

    int mid = (l + r) / 2;
    pair<ll, int> best = {cost(0, mid), -1};

    repx(k, max(1, optl), min(mid, optr) + 1)
        best = min(best, {last[k - 1] + cost(k, mid), k});

    now[mid] = best.ff;

    compute(l, mid - 1, optl, best.ss);
    compute(mid + 1, r, best.ss, optr);
}
```

1.2 KnuthOptimization

```
#include <bits/stdc++.h>
using namespace std;

#define rep(i, n) for (int i = 0; i < (int)n; i++)
#define repx(i, a, b) for (int i = (int)a; i < (int)b; i++)

int N;
vector<vector<int>>> DP, OPT;
vector<int> A;

int main()
{
    DP.assign(N + 1, vector<int>(N + 1));
    OPT.assign(N + 1, vector<int>(N + 1));

    rep(i, N) DP[i][i + 1] = A[i + 1] - A[i], OPT[i][i + 1] = i;
```

```
repx(d, 2, N + 1) rep(l, N + 1 - d)
{
    int r = l + d, l_ = OPT[l][r - 1], r_ = OPT[l + 1][r];
    DP[l][r] = 1e9;
    repx(i, l_, r_ + 1)
    {
        int aux = DP[l][i] + DP[i][r] + A[r] - A[l];
        if (aux < DP[l][r]) DP[l][r] = aux, OPT[l][r] = i;
    }
}
```

1.3 LIS

```
#include <bits/stdc++.h>
using namespace std;

int LIS(vector<int> &v)
{
    vector<int> L; int S = 0;
    for(int x : v)
    {
        int i = upper_bound(L.begin(), L.end(), x) - L.begin();
        if(i == S) L.push_back(x), S++;
        else L[i] = x;
    }
    return S;
}
```

2 Geometry

2.1 2D

```
#include <bits/stdc++.h>
using namespace std;

#define rep(i, n) for (int i = 0; i < (int)n; i++)

const double PI = acos(-1.0L);
const double EPS = 1e-12;

// POINT 2D

typedef double T; struct P
{
    T x, y;
    P() {} P(T x, T y) : x(x), y(y) {}

    P operator+(const P &p) const { return P(x + p.x, y + p.y); }
```

```

P operator-(const P &p) const { return P(x - p.x, y - p.y); }
P operator*(const double &c) const { return P(x * c, y * c); }
P operator/(const double &c) const { return P(x / c, y / c); }
T operator^(const P &p) const { return x * p.y - y * p.x; }
T operator*(const P &p) const { return x * p.x + y * p.y; }
bool operator==(const P &p) const
{
    return abs(x - p.x) + abs(y - p.y) < EPS;
}
bool operator<(const P &p) const
{
    return abs(x - p.x) > EPS ? p.x - x > EPS : p.y - y > EPS;
}

T norm2() const { return x * x + y * y; }
double norm() const { return sqrt(norm2()); }
double ang()
{
    double a = atan2(y, x);
    if (a < 0) a += 2. * PI;
    return a;
}
P unit() { return (*this) / norm(); }
P perp() { return P(-y, x); }
P rot(P r) { return P((*this) ^ r, (*this) * r); }
P rot(double a){ return rot(P(sin(a), cos(a))); }
};
P polar(double r, double a) { return P(r * cos(a), r * sin(a)); }
istream &operator>>(istream &s, P &p) { return s >> p.x >> p.y; }
ostream &operator<<(ostream &s, const P &p)
{
    return s << '(' << p.x << ", " << p.y << ')';
}

double ang(double a)
{
    while (a >= 2. * PI) a -= 2. * PI;
    while (a < 0) a += 2. * PI;
    return a;
}

T turn(P &a, P &b, P &c) { return (b - a) ^ (c - a); }

bool isConvex(vector<P> p)
{
    int n = p.size();
    bool hasPos = false, hasNeg = false, hasCol = false;
    rep(i, n)
    {
        int o = turn(p[i], p[(i + 1) % n], p[(i + 2) % n]);
        if (o > 0) hasPos = true;
        if (o < 0) hasNeg = true;
        if (o == 0) hasCol = true;
    }
    return !(hasPos && hasNeg) && !hasCol;
}

```

```

}

bool half(P &p) { return p.y > 0 || (p.y == 0 && p.x > 0); }

void polarSort(vector<P> &v)
{
    sort(v.begin(), v.end(), [](P &p1, P &p2)
    {
        int h1 = half(p1), h2 = half(p2);
        return h1 != h2 ? h1 > h2 : (p1 ^ p2) > 0;
    });
}

// LINE

struct L
{
    P v; T c;
    L() {} L(P v, T c) : v(v), c(c) {}
    L(T a, T b, T c) : v(P(b, -a)), c(c) {}
    L(P p, P q) : v(q - p), c(v ^ p) {}

    T side(P p) { return (v ^ p) - c; }
    double dist(P p) { return abs(side(p) / v.norm()); }
    double dist2(P p) { return side(p) * side(p) / (double)v.norm2(); }
    L perp(P p) { return L(p, p + v.perp()); }
    L translate(P t) { return L(v, c + (v ^ t)); }
    P proj(P p) { return p - v.perp() * side(p) / v.norm2(); }
    P refl(P p) { return p - v.perp() * 2 * side(p) / v.norm2(); }
};

bool parallel(L l1, L l2) {return abs(l1.v ^ l2.v) < EPS; }

// only if not parallel
P inter(L l1, L l2) { return (l2.v * l1.c - l1.v * l2.c) / (l1.v ^ l2.v); }

L bisector(L l1, L l2, bool in)
{
    double sign = in ? 1 : -1;
    return L(l2.v / l2.v.norm() + l1.v / l1.v.norm() * sign,
            l2.c / l2.v.norm() + l1.c / l1.v.norm() * sign);
}

typedef long long ll;
struct HASH // Hashing for integer coordinates lines
{
    ll a, b, c;
    HASH(const P &p1, const P &p2)
    {
        a = p1.y - p2.y, b = p2.x - p1.x;
        c = p1.x * (p2.y - p1.y) - p1.y * (p2.x - p1.x);
        ll sgn = (a < 0 or (a == 0 and b < 0)) ? -1 : 1;
        ll g = __gcd(abs(a), __gcd(abs(b), abs(c))) * sgn;
        a /= g, b /= g, c /= g;
    }
}

```

```

    bool operator<((const HASH &h) const
    {
        return a < h.a or (a == h.a and (b < h.b or (b == h.b and c < h.c)));
    }
};

// SEGMENT

bool inDisk(P &a, P &b, P &p) { return (a - p) * (b - p) <= 0; }

bool onSegment(P &a, P &b, P &p)
{
    return abs(turn(a, b, p)) < EPS && inDisk(a, b, p);
}

bool properInter(P &a, P &b, P &c, P &d, P &out)
{
    T ta = turn(c, d, a), tb = turn(c, d, b),
    tc = turn(a, b, c), td = turn(a, b, d);
    out = (a * tb - b * ta) / (tb - ta);
    return (ta * tb < 0 && tc * td < 0);
}

set<P> inter(P &a, P &b, P &c, P &d)
{
    P out;
    if (properInter(a, b, c, d, out)) return {out};
    set<P> ans;
    if (onSegment(c, d, a)) ans.insert(a);
    if (onSegment(c, d, b)) ans.insert(b);
    if (onSegment(a, b, c)) ans.insert(c);
    if (onSegment(a, b, d)) ans.insert(d);
    return ans;
}

double segPoint(P &a, P &b, P &p)
{
    if ((p - a) * (b - a) >= 0 && (p - b) * (a - b) >= 0)
        return abs(((b - a) ^ (p - a)) / (b - a).norm());
    return min((p - a).norm(), (b - a).norm());
}

double segSeg(P &a, P &b, P &c, P &d)
{
    P aux;
    if (properInter(a, b, c, d, aux)) return 0;
    return min({segPoint(a, b, c), segPoint(a, b, d),
        segPoint(c, d, a), segPoint(c, d, b)});
}

// POLYGONS

double areaTriangle(P &a, P &b, P &c)
{
    return abs((b - a) ^ (c - a)) / 2.;
}

```

```

}

double areaPolygon(vector<P> &p)
{
    double ans = 0; int n = p.size();
    rep(i, n) ans += p[i] ^ p[(i + 1) % n];
    return abs(ans) / 2.;
}

bool above(P &a, P &p) { return p.y >= a.y; }

bool crossesRay(P &a, P &p, P &q)
{
    return (above(a, q) - above(a, p)) * turn(a, p, q) > 0;
}

// if strict, returns false when a is on the boundary
bool inPolygon(vector<P> &p, P &a, bool strict = true)
{
    int c = 0, n = p.size();
    rep(i, n)
    {
        if (onSegment(p[i], p[(i + 1) % n], a)) return !strict;
        c += crossesRay(a, p[i], p[(i + 1) % n]);
    }
    return c & 1;
}

#define ff first
#define ss second
double areaPolygonUnion(vector<vector<P>> &pol) // Slow  $O((NE)^2 \log(NE))$ 
{
    double area = 0;
    rep(i, pol.size()) rep(j, pol[i].size())
    {
        int m = pol[i].size();
        P p1 = pol[i][j], p2 = pol[i][(j + 1) % m];

        vector<pair<double, int>> s; s.emplace_back(1., 0);

        rep(ii, pol.size()) if (ii != i) rep(jj, pol[ii].size())
        {
            int mm = pol[ii].size();
            P p3 = pol[ii][jj], p4 = pol[ii][(jj + 1) % mm];

            double t1 = turn(p1, p2, p3), t2 = turn(p1, p2, p4),
            t3 = turn(p3, p4, p1), t4 = turn(p3, p4, p2);
            if (!t1 && !t2 && (p2 - p1) * (p4 - p3) > 0 && i > ii)
            {
                s.emplace_back((p3 - p1) * (p2 - p1).unit(), 1);
                s.emplace_back((p4 - p1) * (p2 - p1).unit(), -1);
            }
            if (t1 >= 0 && t2 < 0) s.emplace_back(t3 / (t3 - t4), 1);
            if (t1 < 0 && t2 >= 0) s.emplace_back(t3 / (t3 - t4), -1);
        }
    }
}

```

```

    sort(s.begin(), s.end());

    int c = 0;
    double last = 0, f = 0;
    for (auto e : s)
    {
        double now = min(1., max(0., e.ff));
        if (c == 0) f += now - last;
        c += e.ss, last = now;
    }

    area += (p1 ^ p2) * f;
}

return area;
}

vector<P> convexHull(vector<P> &p)
{
    int n = p.size(), k = 0;
    vector<P> H(2 * n); sort(p.begin(), p.end());
    rep(i, n)
    {
        while (k >= 2 && turn(H[k - 2], H[k - 1], p[i]) <= 0) k--;
        H[k++] = p[i];
    }
    for (int i = n - 2, t = k + 1; i >= 0; i--)
    {
        while (k >= t && turn(H[k - 2], H[k - 1], p[i]) <= 0) k--;
        H[k++] = p[i];
    }
    H.resize(k - 1);
    return H;
}

// MISCELLANEOUS

// Smallest Enclosing circle

P bary(P &A, P &B, P &C, double a, double b, double c)
{
    return (A * a + B * b + C * c) / (a + b + c);
}

P circum(P &A, P &B, P &C)
{
    double a = (B - C).norm2(), b = (C - A).norm2(), c = (A - B).norm2();
    return bary(A, B, C, a * (b + c - a), b * (c + a - b), c * (a + b - c));
}

pair<P, double> smallestEnclosingCircle(vector<P> &p)
{
    random_shuffle(p.begin(), p.end());
    P c = p[0]; double r = 0; int N = p.size();

```

```

    rep(i, N) if (i && (p[i] - c).norm() > r + EPS)
    {
        c = p[i]; r = 0;
        rep(j, i) if ((p[j] - c).norm() > r + EPS)
        {
            c = (p[i] + p[j]) * 0.5;
            r = (p[i] - c).norm();
            rep(k, j) if ((p[k] - c).norm() > r + EPS)
            {
                c = circum(p[i], p[j], p[k]);
                r = (p[k] - c).norm();
            }
        }
    }

    return {c, r};
}

// Closest pair of points from array "a" (mindist: squared mindist)

#define repx(i, a, b) for (int i = (int)a; i < (int)b; i++)
const int MAXN = 1000010;

int n; T mindist;
pair<P, P> best;
P a[MAXN], t[MAXN];

T sq(T x) { return x * x; }

bool cmpY(P &a, P &b) { return a.y < b.y; }

void update(P &p1, P &p2)
{
    T aux = (p1 - p2).norm2();
    if (aux < mindist) { mindist = aux; best = {p1, p2}; }
}

// sort "a" before usage (P must have default operator<)
void closest(int l, int r)
{
    if (r - l <= 3)
    {
        repx(i, l, r) repx(j, i + 1, r) update(a[i], a[j]);
        sort(a + l, a + r, cmpY);
        return;
    }

    int m = (l + r) >> 1, xm = a[m].x;
    closest(l, m); closest(m, r);

    merge(a + l, a + m, a + m, a + r, t, cmpY);
    copy(t, t + r - l, a + l);

    int tsz = 0;
    repx(i, l, r) if (sq(a[i].x - xm) < mindist)

```

```

    {
        for (int j = tsz - 1; j >= 0 && sq(a[i].y - t[j].y) < mindist; --j)
            update(a[i], a[j]);
        t[tsz++] = a[i];
    }
}

```

2.2 3D

```

#include <bits/stdc++.h>
using namespace std;

const double PI = acos(-1.0L);
const double EPS = 1e-12;

// POINT 3D

struct P
{
    double x, y, z;
    P() {}
    P(double x, double y, double z) : x(x), y(y), z(z) {}

    P operator+(const P &p) const { return P(x + p.x, y + p.y, z + p.z); }
    P operator-(const P &p) const { return P(x - p.x, y - p.y, z - p.z); }
    P operator*(const double &c) const { return P(x * c, y * c, z * c); }
    P operator/(const double &c) const { return P(x / c, y / c, z / c); }
    P operator^(const P &p) const
    {
        return P(y * p.z - z * p.y,
                z * p.x - x * p.z,
                x * p.y - y * p.x);
    }
    double operator*(const P &p) const { return x * p.x + y * p.y + z * p.z; }
    double operator%(const P &p) const
    {
        return acos((*this) * p) / (norm() * p.norm());
    }
    bool operator==(const P &p) const
    {
        return abs(x - p.x) + abs(y - p.y) + abs(z - p.z) < EPS;
    }

    double norm() const { return sqrt(norm2()); }
    double norm2() const { return x * x + y * y + z * z; }
    P unit() { return (*this) / norm(); }
};

P polar(double r, double a, double b)
{
    return P(r * cos(a) * cos(b), r * cos(a) * sin(b), r * sin(a));
}

istream &operator>>(istream &s, P &p) { return s >> p.x >> p.y >> p.z; }

```

```

ostream &operator<<(ostream &s, const P &p)
{
    return s << '(' << p.x << ", " << p.y << ", " << p.z << ')';
}

// ARCS

bool in_arc(P &a, P &b, P &n, P &p)
{
    double ab = a % b;
    double ap = a % p;
    P c = (a * cos(ap) + (n ^ a) * sin(ap));
    return ab > ap && p == c;
}

bool find_intersection(P &a1, P &b1, P &a2, P &b2, double &angle)
{
    P n1 = (a1 ^ b1).unit(), n2 = (a2 ^ b2).unit(), i = (n1 ^ n2);
    if (i.norm() < EPS) return false;
    i = i.unit() * a1.norm();
    if (in_arc(a1, b1, n1, i) and in_arc(a2, b2, n2, i))
    {
        angle = a1 % i;
        return true;
    }
    i = i * -1.;
    if (in_arc(a1, b1, n1, i) and in_arc(a2, b2, n2, i))
    {
        angle = a1 % i;
        return true;
    }
    return false;
}

```

3 Graphs

3.1 BFS

```

#include <bits/stdc++.h>
using namespace std;

int n;
vector<vector<int>>> g;
vector<int> depth;

void bfs(int s)
{
    queue<int> q; q.push(s);
    depth.assign(n, -1); depth[s] = 0;
    while (!q.empty())
    {
        int u = q.front(); q.pop();
    }
}

```

```

    for (int v : g[u]) if (depth[v] == -1)
    {
        depth[v] = depth[u] + 1;
        q.push(v);
    }
}
}

```

3.2 BellmanFord

```

#include <bits/stdc++.h>
using namespace std;

#define rep(i, n) for (int i = 0; i < (int)n; i++)

const int INF = 1e9;

struct Edge
{
    int v, w;
    Edge(int v, int w) : v(v), w(w) {}
};

int n;
vector<vector<Edge>> g;
vector<int> D;

bool bellmanFord(int s)
{
    D.assign(n, INF); D[s] = 0;
    rep(i, n - 1) rep(j, n) for (Edge e : g[j])
        D[e.v] = min(D[e.v], D[j] + e.w);

    bool neg = false;
    rep(i, n) for (Edge e : g[i]) if (D[e.v] > D[i] + e.w) neg = true;

    return neg;
}

```

3.3 DFS

```

#include <bits/stdc++.h>
using namespace std;

int n;
vector<vector<int>> g;
vector<bool> visited;

// Recursive (set visited before)
void dfs(int u)

```

```

{
    visited[u] = true;
    for(int v : g[u]) if(!visited[v]) dfs(v);
}

// Iterative
void dfs(int root)
{
    stack<int> s;
    s.push(root);
    visited.assign(n, false);
    visited[root] = true;
    while (!s.empty())
    {
        int u = s.top(); s.pop();
        for (int v : g[u]) if (!visited[v])
        {
            visited[u] = true;
            s.push(v);
        }
    }
}

```

3.4 Dijkstra

```

#include <bits/stdc++.h>
using namespace std;

const int INF = 1e9;

struct Edge
{
    int v, w; // CHECK FOR OVERFLOW
    Edge(int v, int w) : v(v), w(w) {}
    bool operator<(const Edge &e) const { return w > e.w; }
};

int n;
vector<vector<Edge>> G;

int dijkstra(int s, int t)
{
    vector<int> C(n, INF); C[s] = 0; // CHECK FOR OVERFLOW
    priority_queue<Edge> q; q.emplace(s, 0);
    while (!q.empty())
    {
        int u = q.top().v, w = q.top().w; q.pop(); // CHECK FOR OVERFLOW
        if (C[u] < w) continue;
        for (auto e : G[u]) if (C[e.v] > e.w + w)
            C[e.v] = e.w + w, q.emplace(e.v, C[e.v]);
    }
    return C[t];
}

```

}

3.5 Dinic

```
#include <bits/stdc++.h>
using namespace std;

typedef long long ll;

class Dinic
{
    struct Edge { int to, rev; ll f, c; };
    int n, t_; vector<vector<Edge>> G;
    vector<ll> D; vector<int> q, W;

    bool bfs(int s, int t)
    {
        W.assign(n, 0); D.assign(n, -1); D[s] = 0;
        int f = 0, l = 0; q[l++] = s;
        while (f < l)
        {
            int u = q[f++];
            for (const Edge &e : G[u]) if (D[e.to] == -1 && e.f < e.c)
                D[e.to] = D[u] + 1, q[l++] = e.to;
        }
        return D[t] != -1;
    }

    ll dfs(int u, ll f)
    {
        if (u == t_) return f;
        for (int &i = W[u]; i < (int)G[u].size(); ++i)
        {
            Edge &e = G[u][i]; int v = e.to;
            if (e.c <= e.f || D[v] != D[u] + 1) continue;
            ll df = dfs(v, min(f, e.c - e.f));
            if (df > 0) { e.f += df, G[v][e.rev].f -= df; return df; }
        }
        return 0;
    }

public:
    Dinic(int N) : n(N), G(N), D(N), q(N) {}
    void addEdge(int u, int v, ll cap)
    {
        G[u].push_back({v, (int)G[v].size(), 0, cap});
        G[v].push_back({u, (int)G[u].size() - 1, 0, 0}); // cap if bidirectional
    }
    ll maxFlow(int s, int t)
    {
        t_ = t; ll ans = 0;
        while (bfs(s, t)) while (ll dl = dfs(s, LLONG_MAX)) ans += dl;
        return ans;
    }
};
```

}
};

3.6 FloydWarshall

```
#include <bits/stdc++.h>
using namespace std;

#define rep(i, n) for (int i = 0; i < (int)n; i++)

const int INF = 1e9;

int n;
vector<vector<int>> D;

//D is an adjacency matrix at the beginning
void floydWarshall ()
{
    rep(k, n) rep(i, n) rep(j, n) if (D[i][k] < INF && D[k][j] < INF)
        D[i][j] = min(D[i][j], D[i][k] + D[k][j]);

    // opcional, si hay ciclos negativos
    rep(k, n) rep(i, n) rep(j, n) if (D[i][k] < INF && D[k][j] < INF &&
        D[k][k] < 0)
        D[i][j] = -INF;
}
```

3.7 HeavyLightDecomposition

```
#include <bits/stdc++.h>
using namespace std;

#define rep(i, n) for (int i = 0; i < (int)n; i++)

template <class ST, class node>
class HLD
{
    ST st;
    vector<int> A, H, D, R, P;

    int dfs(vector<vector<int>> &G, int u)
    {
        int ans = 1, M = 0, s;
        for (int v : G[u]) if (v != A[u])
        {
            A[v] = u, D[v] = D[u] + 1;
            s = dfs(G, v), ans += s;
            if (s > M) H[u] = v, M = s;
        }
        return ans;
    }
};
```



```

}
template <class OP>
void path(int u, int v, OP op)
{
    for (; R[u] != R[v]; v = A[R[v]])
    {
        if (D[R[u]] > D[R[v]]) swap(u, v);
        op(P[R[v]], P[v] + 1);
    }
    if (D[u] > D[v]) swap(u, v);
    op(P[u], P[v] + 1);          // VALUES ON VERTEX
    // op(P[u] + 1, P[v] + 1);    // VALUES ON EDGE
}

public:
HLD(vector<vector<int>> &G, int n) : A(n), st(n), D(n), R(n), P(n)
{
    H.assign(n, -1); A[0] = -1, D[0] = 0; dfs(G, 0); int p = 0;
    rep(i, n) if (A[i] == -1 || H[A[i]] != i)
        for (int j = i; j != -1; j = H[j]) R[j] = i, P[j] = p++;
}
void set(int v, const node &x) { st.set(P[v], x); } // VALUES ON VERTEX
// void set(int u, int v, const node &x)           // VALUES ON EDGE
// {
//     if (D[u] > D[v]) swap(u, v);
//     st.set(P[v], x);
// }
void update(int u, int v, const node& x)           // OPTIONAL FOR RANGE
    UPDATES
{ path(u, v, [this, &x](int l, int r) { st.update(l, r, x); }); }
node query(int u, int v)
{
    node ans = node();
    path(u, v, [this, &ans](int l, int r) { ans = node(ans, st.query(l, r)); });
    return ans;
}
};

// USAGE: HLD<ST<Node>, Node> hld(G, N);

//// NON COMMUTATIVE QUERIES :

template <class ST, class node>
class HLD
{
    ST st;
    vector<int> A, H, D, R, P;

    int dfs(vector<vector<int>> &G, int u)
    {
        int ans = 1, M = 0, s;
        for (int v : G[u]) if (v != A[u])
        {
            A[v] = u, D[v] = D[u] + 1;

```

```

            s = dfs(G, v), ans += s;
            if (s > M) H[u] = v, M = s;
        }
        return ans;
    }

public:
    node path(int u, int v)
    {
        node ans1, ans2; bool d = 0;
        for (; R[u] != R[v]; v = A[R[v]])
        {
            if (D[R[u]] > D[R[v]]) swap(u, v), d = !d;
            if (d) ans1 = node(st.query(P[R[v]], P[v] + 1), ans1);
            else ans2 = node(st.query(P[R[v]], P[v] + 1), ans2);
        }
        if (D[u] > D[v]) swap(u, v), d = !d;
        if (d) ans1 = node(st.query(P[u], P[v] + 1), ans1);
        else ans2 = node(st.query(P[u], P[v] + 1), ans2);
        ans1.sw(); return node(ans1, ans2);
    }
    HLD(vector<vector<int>> &G, int n) : A(n), st(n), D(n), R(n), P(n)
    {
        H.assign(n, -1); A[0] = -1, D[0] = 0; dfs(G, 0); int p = 0;
        rep(i, n) if (A[i] == -1 || H[A[i]] != i)
            for (int j = i; j != -1; j = H[j]) R[j] = i, P[j] = p++;
    }
    void set(int v, const node &x) { st.set(P[v], x); }
};

```

3.8 HopcroftKarp

```

#include <bits/stdc++.h>
using namespace std;

```

```

class Hopcroft
{
    vector<vector<int>> g;
    vector<int> U, dist;
    int inf = 1e9;

    bool bfs() {
        queue<int> q;
        for (int u : U) if (match[u] == nil) dist[u] = 0, q.push(u);
        else dist[u] = inf;
        dist[nil] = inf;
        while (!q.empty())
        {
            int u = q.front(); q.pop();
            if (u != nil) for (int v : g[u]) if (dist[match[v]] == inf)
            {
                dist[match[v]] = dist[u] + 1;

```

```

        q.push(match[v]);
    }
}
return (dist[nil] != inf);
}

bool dfs(int u) {
    if (u == nil)
        return true;
    for (int v : g[u]) if (dist[match[v]] == dist[u]+1 and dfs(match[v]))
    {
        match[v] = u, match[u] = v;
        return true;
    }
    dist[u] = inf;
    return false;
}

public:
    vector<int> match;
    int nil, isPerfect, matchSize = 0;

    // gg is a bidirectional graph, UU has the nodes in the left partition
    Hopcroft(vector<vector<int>> &gg, vector<int> &UU)
    {
        g = gg; U = UU; nil = g.size();
        match.assign(g.size() + 1, nil);
        dist.assign(g.size() + 1, inf);
        while (bfs()) for (int u : U) if (match[u] == nil and dfs(u))
            matchSize++;
        isPerfect = (matchSize == U.size() and g.size() == U.size() * 2);
    }
};

```

3.9 Hungarian

```

#include <bits/stdc++.h>
using namespace std;

#define rep(i, n) for (int i = 0; i < (int)n; i++)
#define repx(i, a, b) for (int i = (int)a; i < (int)b; i++)

template<class T>
class Hungarian
{
    T inf = numeric_limits<T>::max() / 2;
    bool maxi, swapped = false;
    vector<vector<T>> cost;
    vector<int> p, way;
    vector<T> u, v;
    int l, r;

```

```

public:
    // left/right == partition sizes
    Hungarian(int left, int right, bool maximizing)
    {
        l = left, r = right, maxi = maximizing;
        if (swapped = l > r) swap(l, r);
        cost.assign(l + 1, vector<T>(r + 1, 0));
        u.assign(l + 1, 0); v.assign(r + 1, 0);
        p.assign(r + 1, 0); way.assign(r + 1, 0);
    }

    void add_edge(int l, int r, T w)
    {
        assert(l and r); // indices start from 1 !!
        if (swapped) swap(l, r);
        cost[l][r] = maxi ? -w : w;
    }

    // execute after all edges were added
    void calculate()
    {
        repx(i, 1, l + 1)
        {
            vector<bool> used(r+1, false);
            vector<T> minv(r+1, inf);
            int j0 = 0, p[0] = i;

            while (p[j0])
            {
                int j1, i0 = p[j0], used[j0] = true;
                T delta = inf;
                repx(j, 1, r + 1) if (not used[j])
                {
                    T cur = cost[i0][j] - u[i0] - v[j];
                    if (cur < minv[j]) minv[j] = cur, way[j] = j0;
                    if (minv[j] < delta) delta = minv[j], j1 = j;
                }
                rep(j, r + 1)
                {
                    if (used[j]) u[p[j]] += delta, v[j] -= delta;
                    else minv[j] -= delta;
                }
                j0 = j1;
            }

            while (j0) p[j0] = p[way[j0]], j0 = way[j0];
        }
    }

    // execute after executing calculate()
    T answer() { return maxi ? v[0] : -v[0]; }

    bool are_matched(int l, int r)
    {
        if (swapped) swap(l, r);
    }

```

```

    }
    return p[r] == 1;
};

```

3.10 LCA

```

#include <bits/stdc++.h>
using namespace std;

#define rep(i, n) for (int i = 0; i < (int)n; i++)

struct LCA
{
    int N, LOG;
    vector<int> A, D;
    vector<vector<int>> G;
    int &anc(int u, int l) { return A[l * N + u]; }
    LCA(vector<vector<int>> &G, int N, int root) : G(G), N(N)
    {
        D.assign(N, -1); A.resize(N * (LOG + 1));
        dfs(root, -1, 0), LOG = 31 - __builtin_clz(N);
        rep(l, LOG + 1) if (l) rep(u, N)
        {
            int a = anc(u, l - 1);
            anc(u, l) = (a == -1 ? -1 : anc(a, l - 1));
        }
    }
    void dfs(int u, int p, int depth)
    {
        anc(u, 0) = p, D[u] = depth;
        for (int v : G[u]) if (D[v] == -1) dfs(v, u, depth + 1);
    }
    int raise(int u, int k)
    {
        for (int l = 0; k; l++, k >>= 1) if (k & 1) u = anc(u, l);
        return u;
    }
    int lca(int u, int v)
    {
        if (D[u] < D[v]) swap(u, v);
        u = raise(u, D[u] - D[v]);
        if (u == v) return u;
        for (int l = LOG; l >= 0; l--) if (anc(u, l) != anc(v, l))
            u = anc(u, l), v = anc(v, l);
        return anc(u, 0);
    }
    int dist(int u, int v) { return D[u] + D[v] - 2 * D[lca(u, v)]; }
    int raise_in_path(int u, int v, int k)
    {
        if (D[u] - D[lca(u, v)] >= k) return raise(u, k);
        return raise(v, dist(u, v) - k);
    }
};

```

```

int add_child(int p, int u)
{
    G[p].push_back(u);
    D[u] = D[p] + 1, anc(u, 0) = p;
    rep(l, LOG) if (l)
    {
        p = anc(p, l - 1);
        if (p == -1) break;
        anc(u, l) = p;
    }
};

```

3.11 MST

```

#include <bits/stdc++.h>
using namespace std;

#define rep(i, n) for (int i = 0; i < (int)n; i++)

// PRIM //

struct Edge
{
    int u, v, w;
    Edge(int u, int v, int w) : u(u), v(v), w(w) {}
    bool operator>(const Edge &e) const { return w > e.w; }
};

int find_mst(vector<vector<Edge>> &g, vector<vector<Edge>> &T)
{
    int n = g.size();
    vector<bool> V(n, 0);
    T.assign(n, {});

    int ans = 0, c = 1; V[0] = 1;
    priority_queue<Edge, vector<Edge>, greater<Edge>> q;
    for (Edge &p : g[0]) q.emplace(0, p.v, p.w);

    while (!q.empty())
    {
        Edge e = q.top(); q.pop();

        if (V[e.v]) continue;

        int u = e.u, v = e.v, w = e.w;
        V[v] = true, ans += w;
        T[u].emplace_back(u, v, w);
        T[v].emplace_back(v, u, w);

        if (++c == n) break;
    }
};

```

```

    for (Edge &p : g[v]) if (!V[p.v]) q.emplace(v, p.v, p.w);
}

return ans;
}

```

3.12 MinCostMaxFlow

```

#include <bits/stdc++.h>
using namespace std;

#define rep(i, n) for (int i = 0; i < (int)n; i++)
#define ff first
#define ss second

template <class T>
class MCMF
{
    typedef pair<T, T> pTT;
    T INF = numeric_limits<T>::max();
    struct Edge
    {
        int v; T c, w;
        Edge(int v, T c, T w) : v(v), c(c), w(w) {}
    };

    int n; vector<vector<int>> E;
    vector<Edge> L; vector<int> F; vector<T> D, P; vector<bool> V;

    bool dij(int s, int t)
    {
        D.assign(n, INF); F.assign(n, -1); V.assign(n, false);
        D[s] = 0;
        rep(_, n)
        {
            int best = -1;
            rep(i, n) if (!V[i] && (best == -1 || D[best] > D[i])) best = i;
            if (D[best] >= INF) break;
            V[best] = true;
            for (int e : E[best])
            {
                Edge ed = L[e];
                if (ed.c == 0) continue;
                T toD = D[best] + ed.w + P[best] - P[ed.v];
                if (toD < D[ed.v]) D[ed.v] = toD, F[ed.v] = e;
            }
        }
        return D[t] < INF;
    }

    pTT augment(int s, int t)
    {
        pTT flow(L[F[t]].c, 0);

```

```

        for (int v = t; v != s; v = L[F[v] ^ 1].v)
            flow.ff = min(flow.ff, L[F[v]].c), flow.ss += L[F[v]].w;
        for (int v = t; v != s; v = L[F[v] ^ 1].v)
            L[F[v]].c -= flow.ff, L[F[v] ^ 1].c += flow.ff;
        return flow;
    }

public:
    MCMF(int n) : n(n), E(n), D(n), P(n, 0), V(n, 0) {}
    pTT mcmf(int s, int t)
    {
        pTT ans(0, 0);
        if (!dij(s, t)) return ans;
        rep(i, n) if (D[i] < INF) P[i] += D[i];
        while (dij(s, t))
        {
            auto flow = augment(s, t);
            ans.ff += flow.ff, ans.ss += flow.ff * flow.ss;
            rep(i, n) if (D[i] < INF) P[i] += D[i];
        }
        return ans;
    }
    void addEdge(int u, int v, T c, T w)
    {
        E[u].push_back(L.size()); L.emplace_back(v, c, w);
        E[v].push_back(L.size()); L.emplace_back(u, 0, -w);
    }
};

```

3.13 SCC

```

#include <bits/stdc++.h>
using namespace std;

#define rep(i, n) for (int i = 0; i < (int)n; i++)

int N, id;
vector<vector<int>> G; // Directed Graph
vector<int> D, L, I; stack<int> S;

void dfs(int u)
{
    D[u] = L[u] = id++, I[u] = 1; S.push(u);
    for (int v : G[u])
    {
        if (D[v] == -1) { dfs(v); L[u] = min(L[v], L[u]); }
        else if (I[v]) L[u] = min(L[v], L[u]);
    }
    if (L[u] == D[u]) while (1) // SCC FOUND
    {
        int x = S.top(); S.pop(); I[x] = 0;
        if (x == u) break;
    }
}

```

```

    }
}

void find_sccs()
{
    D.assign(N, -1); L.resize(N); I.assign(N, 0);
    id = 0; rep(u, N) if (D[u] == -1) dfs(u);
}

```

3.14 Tarjan

```

#include <bits/stdc++.h>
using namespace std;

vector<vector<int>>> G;
vector<int> D, L;

void dfs(int u, int p, int d)
{
    D[u] = L[u] = d;
    for(int v : G[u]) if (v != p)
    {
        if (D[v] == -1)
        {
            dfs(v, u, d + 1);
            if (L[v] > D[u]) {} // (u - v) cut edge
            L[u] = min(L[u], L[v]);
        }
        else L[u] = min(L[u], D[v]);
    }
}

int rc = 0;
void dfs(int u, int p, int d)
{
    D[u] = L[u] = d;
    for(int v : G[u]) if (v != p)
    {
        if (D[v] == -1)
        {
            dfs(v, u, d + 1);
            if ((p == -1 && ++rc == 2) || (p != -1 && L[v] >= d)) {} // u is AP
            L[u] = min(L[u], L[v]);
        }
        else if (D[v] < d) L[u] = min(L[u], D[v]);
    }
}

stack<pair<int, int>>> S;
void dfs(int u, int p, int d)
{
    D[u] = L[u] = d;

```

```

for(int v : G[u]) if (v != p)
{
    if (D[v] == -1)
    {
        S.emplace(u, v); dfs(v, u, d + 1);
        if (p == -1 or L[v] >= d) while (1) // BCC found
        {
            pair<int, int> e = S.top(); S.pop();
            if (e == make_pair(u, v)) break;
        }
        L[u] = min(L[u], L[v]);
    }
    else if (D[v] < d) { S.emplace(u, v); L[u] = min(L[u], D[v]); }
}
}

```

4 Math

4.1 BinaryExp

```

#include <bits/stdc++.h>
using namespace std;

int binexp(int b, int p, int M)
{
    b %= M;
    int ans = 1;
    while (p > 0)
    {
        if (p & 1) ans = (ans * b) % M;
        b = (b * b) % M;
        p >>= 1;
    }
    return ans;
}

```

4.2 FFT

```

#include <bits/stdc++.h>
using namespace std;

#define rep(i, n) for (int i = 0; i < (int)n; i++)
#define repx(i, a, b) for (int i = (int)a; i < (int)b; i++)

#define PI acos(-1.0L)

typedef complex<double> C;
typedef vector<double> vd;
void fft(vector<C> &a)

```

```

{
    int n = a.size(), L = 31 - __builtin_clz(n);
    static vector<complex<long double>> R(2, 1);
    static vector<C> rt(2, 1);
    for (static int k = 2; k < n; k *= 2)
    {
        R.resize(n); rt.resize(n);
        auto x = polar(1.0L, PI / k);
        repx(i, k, 2 * k) rt[i] = R[i] = i & 1 ? R[i / 2] * x : R[i / 2];
    }
    vector<int> rev(n);
    rep(i, n) rev[i] = (rev[i / 2] | (i & 1) << L) / 2;
    rep(i, n) if (i < rev[i]) swap(a[i], a[rev[i]]);
    for (int k = 1; k < n; k *= 2) for (int i = 0; i < n; i += 2 * k) rep(j, k)
    {
        auto x = (double *)&rt[j + k], y = (double *)&a[i + j + k];
        C z(x[0] * y[0] - x[1] * y[1], x[0] * y[1] + x[1] * y[0]);
        a[i + j + k] = a[i + j] - z, a[i + j] += z;
    }
}

vd conv(const vd &a, const vd &b)
{
    if (a.empty() || b.empty()) return {};
    vd res(a.size() + b.size() - 1);
    int L = 32 - __builtin_clz(res.size()), n = 1 << L;
    vector<C> in(n), out(n);
    copy(a.begin(), a.end(), in.begin());
    rep(i, b.size()) in[i].imag(b[i]);
    fft(in); for (auto &x : in) x *= x;
    rep(i, n) out[i] = in[-i & (n - 1)] - conj(in[i]);
    fft(out); rep(i, res.size()) res[i] = imag(out[i]) / (4 * n);
    return res;
}

typedef long long ll;
typedef vector<ll> vl;
vl convMod(const vl &a, const vl &b, int M)
{
    if (a.empty() || b.empty()) return {};
    vl res(a.size() + b.size() - 1);
    int B = 32 - __builtin_clz(res.size()), n = 1 << B, cut = int(sqrt(M));
    vector<C> L(n), R(n), outs(n), outl(n);
    rep(i, a.size()) L[i] = C((int)a[i] / cut, (int)a[i] % cut);
    rep(i, b.size()) R[i] = C((int)b[i] / cut, (int)b[i] % cut);
    fft(L), fft(R);
    rep(i, n)
    {
        int j = -i & (n - 1);
        outl[j] = (L[i] + conj(L[j])) * R[i] / (2.0 * n);
        outs[j] = (L[i] - conj(L[j])) * R[i] / (2.0 * n) / ii;
    }
    fft(outl), fft(outs);
    rep(i, res.size())
    {

```

```

        ll av = ll(real(outl[i]) + .5), cv = ll(imag(outs[i]) + .5);
        ll bv = ll(imag(outl[i]) + .5) + ll(real(outs[i]) + .5);
        res[i] = ((av % M * cut + bv) % M * cut + cv) % M;
    }
    return res;
}

```

4.3 PrimeFactorization

```

#include <bits/stdc++.h>
using namespace std;

vector<int> P;

vector<int> factor(int x)
{
    vector<int> ans;
    for (int d : P)
    {
        if (d * d > x) break;
        while (x % d == 0)
        {
            ans.push_back(d);
            if ((x /= d) == 1) return ans;
        }
    }
    if (x > 1) ans.push_back(x);
    return ans;
}

```

4.4 Sieve

```

#include <bits/stdc++.h>
using namespace std;

#define rep(i, n) for (int i = 0; i < (int)n; i++)

template<int SZ> struct Sieve
{
    bitset<SZ> I; vector<int> P;
    Sieve()
    {
        I.set(); I[0] = I[1] = 0;
        for (int i = 4; i < SZ; i += 2) I[i] = 0;
        for (int i = 3; i * i < SZ; i += 2) if (I[i])
            for (int j = i * i; j < SZ; j += i * 2) I[j] = 0;
        rep(i, SZ) if (I[i]) P.push_back(i);
    }
};

```

```
Sieve<320000> S;
```

5 Strings

5.1 AhoCorasick

```
#include <bits/stdc++.h>
using namespace std;

#define rep(i, n) for (int i = 0; i < (int)n; i++)

struct AC
{
    static const int MAX = 1e4, ASZ = 26;
    int N[MAX][ASZ] = {0}, L[MAX] = {0}, E[MAX] = {0}, c = 0;
    void add(string s)
    {
        int p = 0;
        for (char l : s)
        {
            int t = l - 'a';
            if (!N[p][t]) N[p][t] = ++c;
            p = N[p][t];
        } E[p] = 1;
    }
    void init()
    {
        queue<int> q; q.push(0); L[0] = -1;
        while (!q.empty())
        {
            int p = q.front(); q.pop();
            rep(c, ASZ)
            {
                int u = N[p][c]; if (!u) continue;
                L[u] = L[p] == -1 ? 0 : N[L[p]][c], q.push(u);
            }
            if (p) rep(c, ASZ) if (!N[p][c]) N[p][c] = N[L[p]][c];
        }
    }
};
```

5.2 Hash

```
#include <bits/stdc++.h>
using namespace std;

typedef long long ll;
#define rep(i, n) for (int i = 0; i < (int)n; i++)
```

```
struct RH
{
    int B = 1777771, M[2] = {999727999, 1070777777}, P[2] = {325255434, 10018302};
    vector<int> H[2], I[2];
    RH(string &s)
    {
        int N = s.size(); rep(k, 2)
        {
            H[k].resize(N + 1), I[k].resize(N + 1);
            H[k][0] = 0, I[k][0] = 1; ll b = 1;
            rep(i, N + 1) if (i)
            {
                H[k][i] = (H[k][i - 1] + b * s[i - 1]) % M[k];
                I[k][i] = (1LL * I[k][i - 1] * P[k]) % M[k];
                b = (b * B) % M[k];
            }
        }
    }
    ll get(int l, int r) // inclusive - exclusive
    {
        ll h0 = (H[0][r] - H[0][l] + M[0]) % M[0];
        h0 = (1LL * h0 * I[0][l]) % M[0];
        ll h1 = (H[1][r] - H[1][l] + M[1]) % M[1];
        h1 = (1LL * h1 * I[1][l]) % M[1];
        return (h0 << 32) | h1;
    }
};
```

5.3 KMP

```
#include <bits/stdc++.h>
using namespace std;

#define rep(i, n) for (int i = 0; i < (int)n; i++)

int match(string &p, string &t)
{
    int n = p.size(), m = t.size(), L[n]; L[0] = 0;
    rep(j, n - 1)
    {
        int i = L[j]; while (p[i] != p[j + 1] && i) i = L[i - 1];
        L[j + 1] = (p[i] == p[j + 1] ? i + 1 : 0);
    }
    int ans = 0, i = 0; rep(j, m)
    {
        while (p[i] != t[j] && i) i = L[i - 1];
        if (p[i] == t[j] && ++i == n) i = L[n - 1], ans++;
    }
    return ans;
}
```

5.4 Manacher

```
#include <bits/stdc++.h>
using namespace std;

int n;
string s;

int main()
{
    vector<int> d1(n); // odd sized palindromes
    for (int i = 0, l = 0, r = -1; i < n; i++) {
        int k = (i > r) ? 1 : min(d1[l + r - i], r - i + 1);
        while (0 <= i - k && i + k < n && s[i - k] == s[i + k]) k++;
        d1[i] = k--;
        if (i + k > r) l = i - k, r = i + k;
    }
    vector<int> d2(n); // even sized palindromes (center to the right)
    for (int i = 0, l = 0, r = -1; i < n; i++) {
        int k = (i > r) ? 0 : min(d2[l + r - i + 1], r - i + 1);
        while (0 <= i - k - 1 && i + k < n && s[i - k - 1] == s[i + k]) k++;
        d2[i] = k--;
        if (i + k > r) l = i - k - 1, r = i + k;
    }
}
```

5.5 SuffixArray

```
#include <bits/stdc++.h>
using namespace std;

#define rep(i, n) for (int i = 0; i < (int)n; i++)
#define repx(i, a, b) for (int i = (int)a; i < (int)b; i++)

struct SA
{
    int n; vector<int> C, R, R_, sa, sa_, lcp;
    inline int gr(int i) { return i < n ? R[i] : 0; }
    void csort(int maxv, int k)
    {
        C.assign(maxv + 1, 0); rep(i, n) C[gr(i + k)]++;
        repx(i, 1, maxv + 1) C[i] += C[i - 1];
        for (int i = (int)n - 1; i >= 0; i--) sa_[-C[gr(sa[i] + k)]] = sa[i];
        sa.swap(sa_);
    }
    void getSA(vector<int>& s)
    {
        R = R_ = sa = sa_ = vector<int>(n); rep(i, n) sa[i] = i;
        sort(sa.begin(), sa.end(), [&s](int i, int j) { return s[i] < s[j]; });
        int r = R[sa[0]] = 1;
        repx(i, 1, n) R[sa[i]] = (s[sa[i]] != s[sa[i - 1]]) ? ++r : r;
        for (int h = 1; h < n && r < n; h <= 1)

```

```

        {
            csort(r, h); csort(r, 0); r = R_[sa[0]] = 1;
            repx(i, 1, n)
            {
                if (R[sa[i]] != R[sa[i - 1]] || gr(sa[i] + h) != gr(sa[i - 1] + h))
                    r++;
                R_[sa[i]] = r;
            } R.swap(R_);
        }
    }
    void getLCP(vector<int>& s)
    {
        lcp.assign(n, 0); int k = 0;
        rep(i, n)
        {
            int r = R[i] - 1;
            if (r == n - 1) { k = 0; continue; }
            int j = sa[r + 1];
            while (i + k < n && j + k < n and s[i + k] == s[j + k]) k++;
            lcp[r] = k; if (k) k--;
        }
    }
    SA(vector<int>& s) { n = s.size(); getSA(s); getLCP(s); }
};

```

5.6 SuffixAutomaton

```
#include <bits/stdc++.h>
using namespace std;

#define rep(i, n) for (int i = 0; i < (int)n; i++)

// vector implementation
struct SA
{
    int sz, l; vector<int> L, Lk, S, C, T;
    vector<vector<int>>> N, Ilk;

    SA(string s, int n) : L(2 * n), Lk(2 * n), C(2 * n), N(2 * n, vector<int>(26, -1))
    {
        l = L[0] = 0, Lk[0] = -1, sz = 1; int p;
        for (char c : s) p = extend(c - 'A');
        Ilk.resize(sz); S.assign(sz, -1);
        rep(i, sz) if (i) Ilk[Lk[i]].push_back(i);
        T.assign(sz, 0); while (p != -1) T[p] = 1, p = Lk[p];
    }
    int extend(char c)
    {
        int cur = sz++, p = 1; C[cur] = 0, L[cur] = L[1] + 1;
        while (p != -1 && N[p][c] == -1) N[p][c] = cur, p = Lk[p];
        if (p == -1) { Lk[cur] = 0, l = cur; return cur; }
    }

```

```

    int q = N[p][c];
    if (L[p] + 1 == L[q]) { Lk[cur] = q, l = cur; return cur; }
    int w = sz++; C[w] = 1, L[w] = L[p] + 1, Lk[w] = Lk[q], N[w] = N[q];
    while (p != -1 && N[p][c] == q) N[p][c] = w, p = Lk[p];
    Lk[q] = Lk[cur] = w, l = cur; return cur;
}
int size(int p)
{
    if (S[p] != -1) return S[p];
    for (int i : Ilk[p]) S[p] += size(i);
    return S[p] += (1 - C[p]) + 1;
}
};

```

// 101 vector implementation

```

struct SA
{
    int sz, l; vector<int> L, Lk;
    vector<vector<int>> N, Ilk;

    SA(string s, int n) : L(2 * n), Lk(2 * n), N(2 * n, vector<int>(26, -1))
    {
        l = L[0] = 0, Lk[0] = -1, sz = 1; int p;
        for (char c : s) p = extend(c - 'A');
    }
    int extend(char c)
    {
        int cur = sz++, p = l; L[cur] = L[l] + 1;
        while (p != -1 && N[p][c] == -1) N[p][c] = cur, p = Lk[p];
        if (p == -1) { Lk[cur] = 0, l = cur; return cur; }
        int q = N[p][c];
        if (L[p] + 1 == L[q]) { Lk[cur] = q, l = cur; return cur; }
        int w = sz++; L[w] = L[p] + 1, Lk[w] = Lk[q], N[w] = N[q];
        while (p != -1 && N[p][c] == q) N[p][c] = w, p = Lk[p];
        Lk[q] = Lk[cur] = w, l = cur; return cur;
    }
};

```

// 101 map implementation

```

struct SA
{
    int sz, l; vector<int> L, Lk;
    vector<map<char, int>> N;

    SA(string s, int n) : L(2 * n), Lk(2 * n), N(2 * n)
    {
        l = L[0] = 0, Lk[0] = -1, sz = 1;
        for (char c : s) extend(c);
    }
    void extend(char c)
    {
        int cur = sz++, p = l; L[cur] = L[l] + 1;
        while (p != -1 && !N[p].count(c)) N[p][c] = cur, p = Lk[p];
        if (p == -1) { Lk[cur] = 0, l = cur; return; }
        int q = N[p][c];
    }
};

```

```

    if (L[p] + 1 == L[q]) { Lk[cur] = q, l = cur; return; }
    int w = sz++; L[w] = L[p] + 1, Lk[w] = Lk[q], N[w] = N[q];
    while (p != -1 && N[p][c] == q) N[p][c] = w, p = Lk[p];
    Lk[q] = Lk[cur] = w, l = cur;
}
};

```

5.7 Trie

```

#include <bits/stdc++.h>
using namespace std;

```

```

struct Trie
{
    static const int MAX = 1e6;
    int N[MAX][26] = {0}, S[MAX] = {0}, c = 0;
    void add(string s, int a = 1)
    {
        int p = 0; S[p] += a;
        for (char l : s)
        {
            int t = l - 'a';
            if (!N[p][t]) N[p][t] = ++c;
            S[p = N[p][t]] += a;
        }
    }
};

#define rep(i, n) for (int i = 0; i < (int)n; i++)

struct TrieXOR
{
    static const int MAX = 1e6;
    int N[MAX][2] = {0}, S[MAX] = {0}, c = 0;
    void add(int x, int a = 1)
    {
        int p = 0; S[p] += a;
        rep(i, 31)
        {
            int t = (x >> (30 - i)) & 1;
            if (!N[p][t]) N[p][t] = ++c;
            S[p = N[p][t]] += a;
        }
    }
    int get(int x)
    {
        if (!S[0]) return -1;
        int p = 0; rep(i, 31)
        {
            int t = ((x >> (30 - i)) & 1) ^ 1;
            if (!N[p][t] || !S[N[p][t]]) t ^= 1;
            p = N[p][t]; if (t) x ^= (1 << (30 - i));
        }
    }
};

```

```

    }
    return x;
}
};

```

6 Structures

6.1 FenwickTree

```

#include <bits/stdc++.h>
using namespace std;

// 1 - indexed / inclusive - inclusive
struct FT
{
    vector<int> t;
    FT(int N) { t.resize(N + 1, 0); }
    int query(int i)
    {
        int ans = 0;
        for (; i; i -= i & (-i)) ans += t[i];
        return ans;
    }
    int query(int i, int j) { return query(j) - query(i - 1); }
    void update(int i, int v)
    {
        int s = query(i, i); // Sets
        for (; i < t.size(); i += i & (-i)) t[i] += v - s;
    }
    void update(int i, int j, int v)
    {
        update(i, v); update(j + 1, -v);
    }
};

```

6.2 FenwickTree2D

```

#include <bits/stdc++.h>
using namespace std;

// 0 - indexed / inclusive - inclusive
template <class T>
class FT2D
{
    vector<vector<T>>> t;
    int n, m;

public:
    FT2D() {}

```

```

FT2D(int n, int m)
{
    t.assign(n, vector<T>(m, 0));
    this->n = n;
    this->m = m;
}

void add(int r, int c, T value)
{
    for (int i = r; i < n; i |= i + 1)
        for (int j = c; j < m; j |= j + 1)
            t[i][j] += value;
}

T sum(int r, int c)
{
    T res = 0;
    for (int i = r; i >= 0; i = (i & (i + 1)) - 1)
        for (int j = c; j >= 0; j = (j & (j + 1)) - 1)
            res += t[i][j];
    return res;
}

T sum(int r1, int c1, int r2, int c2)
{
    return sum(r2, c2) - sum(r1 - 1, c2) - sum(r2, c1 - 1) +
           sum(r1 - 1, c1 - 1);
}

T get(int r, int c) { return sum(r, c, r, c); }

void set(int r, int c, T value) { add(r, c, -get(r, c) + value); }
};

```

6.3 LineContainer

```

#include <bits/stdc++.h>
using namespace std;

typedef long long ll;

struct Line
{
    mutable ll k, m, p;
    bool operator<(const Line &o) const { return k < o.k; }
    bool operator<(ll x) const { return p < x; }
};

// (for doubles, use inf = 1/.0, div(a,b) = a/b)
struct LineContainer : multiset<Line, less<>>
{

```

```

const ll inf = LLONG_MAX;
ll div(ll a, ll b) { return a / b - ((a ^ b) < 0 && a % b); }
bool isect(iterator x, iterator y)
{
    if (y == end()) { x->p = inf; return false; }
    if (x->k == y->k) x->p = x->m > y->m ? inf : -inf;
    else x->p = div(y->m - x->m, x->k - y->k);
    return x->p >= y->p;
}
void add(ll k, ll m)
{
    auto z = insert({k, m, 0}), y = z++, x = y;
    while (isect(y, z)) z = erase(z);
    if (x != begin() && isect(--x, y)) isect(x, y = erase(y));
    while ((y = x) != begin() && (--x)->p >= y->p) isect(x, erase(y));
}
ll query(ll x)
{
    assert(!empty());
    auto l = *lower_bound(x);
    return l.k * x + l.m;
}
};

```

6.4 MoQueries

```

#include <bits/stdc++.h>
using namespace std;

int S; // Size of buckets (generally sqrt(N))

struct Query
{
    int l, r, id;
    Query(int l, int r, int id) : l(l), r(r), id(id) {}
    bool operator<(Query &q)
    {
        return l / S < q.l / S or (l / S == q.l / S and r < q.r);
    }
};

```

6.5 PersistentSegmentTree

```

#include <bits/stdc++.h>
using namespace std;

struct Node
{
    int v, l, r;
    Node() : v(0), l(0), r(0) {}
};

```

```

Node(int v) : v(v) {}
Node(const Node &a, const Node &b, int l, int r) : l(l), r(r)
{ v = a.v + b.v; }
};

// 0 - indexed / inclusive - inclusive
template <class node>
struct PST
{
    int cnt = 0, n, rc = 0;
    vector<node> st; vector<int> rt;

    node query(int u, int a, int b, int i, int j)
    {
        if (j < a || b < i) return node();
        if (a <= i && j <= b) return st[u];
        int m = (i + j) / 2, l = st[u].l, r = st[u].r;
        return node(query(l, a, b, i, m), query(r, a, b, m + 1, j), l, r);
    }
    int update(int u, int p, node v, int i, int j)
    {
        if (j < p || p < i) return u;
        st[cnt] = st[u]; int x = cnt++, m = (i + j) / 2;
        if (i == j) { st[x] = v; return x; }
        int l = st[x].l = update(st[x].l, p, v, i, m);
        int r = st[x].r = update(st[x].r, p, v, m + 1, j);
        st[x] = node(st[l], st[r], l, r); return x;
    }
    int build(vector<node> &arr, int i, int j)
    {
        int u = cnt++, m = (i + j) / 2;
        if (i == j) { st[u] = arr[i]; return u; }
        int l = st[u].l = build(arr, i, m);
        int r = st[u].r = build(arr, m + 1, j);
        st[u] = node(st[l], st[r], l, r); return u;
    }

    PST(vector<node> &arr) : st(1e7), rt(1e5)
    { n = arr.size(); rt[rc++] = build(arr, 0, n - 1); }
    void update(int t, int p, node v) { rt[rc++] = update(rt[t], p, v, 0, n - 1); }
    node query(int t, int a, int b) { return query(rt[t], a, b, 0, n - 1); }
};

// Init with null's (no build) (requires l = r = 0 as default)
template <class node>
struct PST
{
    int cnt = 1, n, rc = 1;
    vector<node> st; vector<int> rt;

    node query(int u, int a, int b, int i, int j)
    {
        if (j < a || b < i) return node();
        if (a <= i && j <= b) return st[u];
    }
};

```

```

    int m = (i + j) / 2, l = st[u].l, r = st[u].r;
    return node(query(l, a, b, i, m), query(r, a, b, m + 1, j), l, r);
}
int update(int u, int p, node v, int i, int j)
{
    if (j < p || p < i) return u;
    st[cnt] = st[u]; int x = cnt++; m = (i + j) / 2;
    if (i == j) { st[x] = v; return x; }
    int l = st[x].l = update(st[x].l, p, v, i, m);
    int r = st[x].r = update(st[x].r, p, v, m + 1, j);
    st[x] = node(st[l], st[r], l, r); return x;
}

PST(int N) : st(1e7), rt(1e5), n(N) {}
void update(int t, int p, node v) { rt[rc++] = update(rt[t], p, v, 0, n - 1); }
node query(int t, int a, int b) { return query(rt[t], a, b, 0, n - 1); }
};

```

6.6 PersistentSegmentTreeLazy

```

#include <bits/stdc++.h>
using namespace std;

struct Node
{
    int v, l = 0, r = 0, lzv = 0;
    bool lz = false;
    Node() : v(0) {}
    Node(int x) : v(x) {}
    Node(const Node &a, const Node &b, int l, int r) : v(a.v + b.v), l(l), r(r) {}
    Node(int x, int i, int j, const Node &b) : l(b.l), r(b.r)
    { v = b.v + (j - i + 1) * x; }
};

// 0 - indexed / inclusive - inclusive
template <class node>
struct PSTL
{
    int cnt = 0, n, rc = 0;
    vector<node> st; vector<int> rt;

    void push(int u, int v, int i, int j)
    {
        st[u] = node(v, i, j, st[u]);
        if (i == j) return;
        st[cnt] = st[st[u].l]; int l = cnt++;
        st[cnt] = st[st[u].r]; int r = cnt++;
        st[u].l = l, st[l].lz = 1, st[l].lzv += v;
        st[u].r = r, st[r].lz = 1, st[r].lzv += v;
    }

    node query(int u, int a, int b, int i, int j)

```

```

{
    if (j < a || b < i) return node();
    if (st[u].lz) push(u, st[u].lzv, i, j);
    if (a <= i && j <= b) return st[u];
    int m = (i + j) / 2, l = st[u].l, r = st[u].r;
    return node(query(l, a, b, i, m), query(r, a, b, m + 1, j), l, r);
}
int update(int u, int a, int b, int v, int i, int j)
{
    if (st[u].lz) push(u, st[u].lzv, i, j);
    if (j < a || b < i) return u;
    st[cnt] = st[u]; int x = cnt++, m = (i + j) / 2;
    if (a <= i && j <= b) { push(x, v, i, j); return x; }
    int l = st[x].l = update(st[x].l, a, b, v, i, m);
    int r = st[x].r = update(st[x].r, a, b, v, m + 1, j);
    st[x] = node(st[l], st[r], l, r); return x;
}
int build(vector<node> &arr, int i, int j)
{
    int u = cnt++, m = (i + j) / 2;
    if (i == j) { st[u] = arr[i]; return u; }
    int l = st[u].l = build(arr, i, m);
    int r = st[u].r = build(arr, m + 1, j);
    st[u] = node(st[l], st[r], l, r); return u;
}

PSTL(vector<node> &arr) : st(1e7), rt(1e5)
{ n = arr.size(); rt[rc++] = build(arr, 0, n - 1); }
void update(int t, int a, int b, int v)
{ rt[rc++] = update(rt[t], a, b, v, 0, n - 1); }
node query(int t, int a, int b) { return query(rt[t], a, b, 0, n - 1); }
};

// Direct accumulate (No Push) Faster and shorter
struct Node
{
    int v = 0, l = 0, r = 0, lzv = 0;
    bool lz = false;
    Node() {}
    Node(int x) : v(x) {}
    Node(const Node &a, const Node &b, int l, int r) : v(a.v + b.v), l(l), r(r) {}
    Node(int x, int i, int j, const Node &b)
    { *this = b; v += (j - i + 1) * x; } // *this = b needed in this variant
    (keeps lazy)
};

template <class node>
struct PSTL
{
    int cnt = 0, n, rc = 0;
    vector<node> st; vector<int> rt;

    node query(int u, int a, int b, int i, int j, ll acc)
    {
        if (j < a || b < i) return node();

```

```

    if (st[u].lz) acc += st[u].lzv;
    int m = (i + j) / 2, l = st[u].l, r = st[u].r;
    if (a <= i && j <= b) return node(acc, i, j, st[u]);
    return node(query(l, a, b, i, m, acc), query(r, a, b, m + 1, j, acc), l,
                r);
}
int update(int u, int a, int b, int v, int i, int j)
{
    if (j < a || b < i) return u;
    st[cnt] = st[u]; int x = cnt++, m = (i + j) / 2;
    if (a <= i && j <= b) { st[x].lz = 1, st[x].lzv += v; return x; }
    int l = st[x].l = update(st[x].l, a, b, v, i, m);
    int r = st[x].r = update(st[x].r, a, b, v, m + 1, j);
    st[x] = node(v, max(i, a), min(j, b), st[x]); return x;
}
int build(vector<node> &arr, int i, int j)
{
    int u = cnt++, m = (i + j) / 2;
    if (i == j) { st[u] = arr[i]; return u; }
    int l = st[u].l = build(arr, i, m);
    int r = st[u].r = build(arr, m + 1, j);
    st[u] = node(st[l], st[r], l, r); return u;
}

PSTL(vector<node> &arr) : st(5e6), rt(2e5)
{ n = arr.size(); rt[rc++] = build(arr, 0, n - 1); }
int update(int t, int a, int b, int v)
{ rt[rc] = update(rt[t], a, b, v, 0, n - 1); return rc++; }
node query(int t, int a, int b) { return query(rt[t], a, b, 0, n - 1, 0); }
};

```

6.7 PolicyBased

```

#include <bits/stdc++.h>
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>

using namespace __gnu_pbds;
using namespace std;

template <typename T, typename Comparator = less<T>>
using super_set = tree<T, null_type, Comparator, rb_tree_tag,
                      tree_order_statistics_node_update>;

// order_of_key(T x)
// -> returns the number of elements strictly smaller than x

// find_by_order(size_t i)
// -> returns iterator to i-th largest element (counting from 0)

```

6.8 SegmentTree

```

#include <bits/stdc++.h>
using namespace std;

struct Node
{
    int v;
    Node() { v = 0; } // neutro
    Node(int v) : v(v) {}
    Node(const Node &a, const Node &b) { v = a.v + b.v; }
};

// 0 - indexed / inclusive - exclusive
template <class node>
struct ST
{
    vector<node> t; int n;

    ST(vector<node> &arr, int N) : n(N), t(N * 2)
    {
        copy(arr.begin(), arr.end(), t.begin() + n);
        for (int i = n - 1; i > 0; --i) t[i] = node(t[i << 1], t[i << 1 | 1]);
    }
    void set(int p, const node &value)
    {
        for (t[p += n] = value; p >>= 1;)
            t[p] = node(t[p << 1], t[p << 1 | 1]);
    }
    node query(int l, int r)
    {
        node ans1, ansr;
        for (l += n, r += n; l < r; l >>= 1, r >>= 1)
        {
            if (l & 1) ans1 = node(ans1, t[l++]);
            if (r & 1) ansr = node(t[--r], ansr);
        }
        return node(ans1, ansr);
    }
};

```

6.9 SegmentTreeLazy

```

#include <bits/stdc++.h>
using namespace std;

struct Node
{
    int v, lzv = 0;
    bool lz = false;
    Node() : v(0) {}
    Node(int x) : v(x) {}
};

```

```

Node(const Node &a, const Node &b) : v(a.v + b.v) {}
Node(int x, int i, int j, const Node &b)
{
    v = b.v + (j - i + 1) * x;
}
};

// 0 - indexed / inclusive - inclusive
template <class node>
struct STL
{
    vector<node> st; int n;

    void build(int u, int i, int j, vector<node> &arr)
    {
        if (i == j) { st[u] = arr[i]; return; }
        int m = (i + j) / 2, l = u * 2 + 1, r = u * 2 + 2;
        build(l, i, m, arr), build(r, m + 1, j, arr);
        st[u] = node(st[l], st[r]);
    }
    void push(int u, int i, int j, int x)
    {
        st[u] = node(x, i, j, st[u]);
        if (i == j) return;
        st[u * 2 + 1].lz = 1, st[u * 2 + 1].lzv += x;
        st[u * 2 + 2].lz = 1, st[u * 2 + 2].lzv += x;
    }
    node query(int a, int b, int u, int i, int j)
    {
        if (j < a || b < i) return node();
        int m = (i + j) / 2, l = u * 2 + 1, r = u * 2 + 2;
        if (st[u].lz) push(u, i, j, st[u].lzv);
        if (a <= i && j <= b) return st[u];
        return node(query(a, b, l, i, m), query(a, b, r, m + 1, j));
    }
    void update(int a, int b, int v, int u, int i, int j)
    {
        if (st[u].lz) push(u, i, j, st[u].lzv);
        if (j < a || b < i) return;
        int m = (i + j) / 2, l = u * 2 + 1, r = u * 2 + 2;
        if (a <= i && j <= b) { push(u, i, j, v); return; }
        update(a, b, v, l, i, m); update(a, b, v, r, m + 1, j);
        st[u] = node(st[l], st[r]);
    }

    STL(vector<node> &v, int N) : n(N), st(N * 4 + 5) { build(0, 0, n - 1, v); }
    node query(int a, int b) { return query(a, b, 0, 0, n - 1); }
    void update(int a, int b, int v) { update(a, b, v, 0, 0, n - 1); }
};

```

6.10 SparseTable

```

#include <bits/stdc++.h>
using namespace std;

template <class t>
class ST
{
    int n;
    vector<int> memo, *arr;

public:
    ST(vector<int> &_arr)
    {
        arr = &_amp; n = arr->size();
        int maxlog = 31 - __builtin_clz(n);
        memo.assign(n * (maxlog + 1), -1);
    }
    int dp(int i, int e)
    {
        int &ans = memo[e * n + i];
        if (ans != -1) return ans;
        if (e == 0) return ans = (*arr)[i];
        return ans = t::merge(dp(i, e - 1), dp(i + (1 << (e - 1)), e - 1));
    }

    int query_01(int l, int r)
    {
        int e = 31 - __builtin_clz(r - l + 1);
        return t::merge(dp(l, e), dp(r - (1 << e) + 1, e));
    }

    int query_0logn(int l, int r)
    {
        int ans = t::neutro;
        int d = r - l + 1;
        for (int e = 0; d; e++, d >>= 1) if (d & 1)
        {
            ans = t::merge(ans, dp(l, e));
            l += 1 << e;
        }
        return ans;
    }
};

struct OP
{
    static const int neutro = 0;
    static int merge(int x, int y) { return x + y; }
};

```

6.11 Treap

```

#include <bits/stdc++.h>

```

```

using namespace std;

mt19937 gen(chrono::high_resolution_clock::now().time_since_epoch().count());

typedef pair<int, int> ii;
#define ff first
#define ss second

// 101 Treap //

struct Node
{
    int p, sz = 0, v, acc, l = -1, r = -1;
    Node() : v(0), acc(0) {}
    Node(int x): p(gen()), sz(1), v(x), acc(x) {}
    void recalc(const Node &a, const Node &b)
    {
        sz = a.sz + b.sz + 1;
        acc = v + a.acc + b.acc;
    }
};

template <class node>
struct Treap
{
    vector<node> t; int n, r = -1;

    node get(int u) { return u != -1 ? t[u] : node(); }
    void recalc(int u) { t[u].recalc(get(t[u].l), get(t[u].r)); }
    int merge(int l, int r)
    {
        if (min(l, r) == -1) return l != -1 ? l : r;
        int ans = (t[l].p < t[r].p) ? l : r;
        if (ans == l) t[l].r = merge(t[l].r, r), recalc(l);
        if (ans == r) t[r].l = merge(l, t[r].l), recalc(r);
        return ans;
    }
    ii split(int u, int id)
    {
        if (u == -1) return {-1, -1};
        int szl = get(t[u].l).sz;
        if (szl >= id)
        {
            ii ans = split(t[u].l, id);
            t[u].l = ans.ss; recalc(u);
            return {ans.ff, u};
        }
        ii ans = split(t[u].r, id - szl - 1);
        t[u].r = ans.ff; recalc(u);
        return {u, ans.ss};
    }

    Treap(vector<int> &v) : n(v.size())
    { for (int i = 0; i < n; i++) t.emplace_back(v[i]), r = merge(r, i); }
};

```

```

// Complete Treap with Lazy propagation //

struct Node
{
    int p, sz = 0, v, acc, l = -1, r = -1, par = -1, lzv = 0;
    bool lz = false, f = false;
    Node() : v(0), acc(0) {}
    Node(int x): p(gen()), sz(1), v(x), acc(x) {}
    void recalc(const Node &a, const Node &b)
    {
        sz = a.sz + b.sz + 1;
        acc = v + a.acc + b.acc;
    }
    void upd_lazy(int x) { lz = 1, lzv += x; }
    void lazy() { v += lzv, acc += sz * lzv, lz = 0, lzv = 0; }
    void flip() { swap(l, r), f = 0; }
};

template <class node>
struct Treap
{
    vector<node> t; int n, r = -1;

    node get(int u) { return u != -1 ? t[u] : node(); }
    void recalc(int u)
    {
        int l = t[u].l, r = t[u].r;
        push(l); push(r); flip(l); flip(r);
        t[u].recalc(get(l), get(r));
    }
    void push(int u)
    {
        if (u == -1 || !t[u].lz) return;
        int l = t[u].l, r = t[u].r;
        if (l != -1) t[l].upd_lazy(t[u].lzv);
        if (r != -1) t[r].upd_lazy(t[u].lzv);
        t[u].lazy();
    }
    void flip(int u)
    {
        if (u == -1 || !t[u].f) return;
        int l = t[u].l, r = t[u].r;
        if (l != -1) t[l].f ^= 1;
        if (r != -1) t[r].f ^= 1;
        t[u].flip();
    }
    int merge(int l, int r)
    {
        if (min(l, r) == -1) return l != -1 ? l : r;
        push(l); push(r); flip(l); flip(r);
        int ans = (t[l].p < t[r].p) ? l : r;
        if (ans == l) t[l].r = merge(t[l].r, r), recalc(l);
        if (ans == r) t[r].l = merge(l, t[r].l), recalc(r);
    }
};

```

```

    if (t[ans].l != -1) t[t[ans].l].par = ans; // optional only if parent
        needed
    if (t[ans].r != -1) t[t[ans].r].par = ans; // optional only if parent
        needed
    return ans;
}
ii split(int u, int id)
{
    if (u == -1) return {-1, -1};
    push(u); flip(u);
    int szl = get(t[u].l).sz;
    if (szl >= id)
    {
        ii ans = split(t[u].l, id);
        if (ans.ss != -1) t[ans.ss].par = u; // optional only if parent needed
        if (ans.ff != -1) t[ans.ff].par = -1; // optional only if parent needed
        t[u].l = ans.ss; recalc(u);
        return {ans.ff, u};
    }
    ii ans = split(t[u].r, id - szl - 1);
    if (ans.ff != -1) t[ans.ff].par = u; // optional only if parent needed
    if (ans.ss != -1) t[ans.ss].par = -1; // optional only if parent needed
    t[u].r = ans.ff; recalc(u);
    return {u, ans.ss};
}
int update(int u, int l, int r, int v)
{
    ii a = split(u, l), b = split(a.ss, r - l + 1);
    t[b.ff].upd_lazy(v);
    return merge(a.ff, merge(b.ff, b.ss));
}
void print(int u)
{
    if (u == -1) return;
    push(u); flip(u);
    print(t[u].l);
    cout << t[u].v << ' ';
    print(t[u].r);
}

Treap(vector<int> &v) : n(v.size())
{ for (int i = 0; i < n; i++) t.emplace_back(v[i]), r = merge(r, i); }
};

```

6.12 UnionFind

```

#include <bits/stdc++.h>
using namespace std;

#define rep(i, n) for (int i = 0; i < (int)n; i++)

struct DSU

```

```

{
    vector<int> p;
    DSU(int N) : p(N, -1) {}
    int get(int x) { return p[x] < 0 ? x : p[x] = get(p[x]); }
    bool sameSet(int a, int b) { return get(a) == get(b); }
    int size(int x) { return -p[get(x)]; }
    void unite(int x, int y)
    {
        if ((x = get(x)) == (y = get(y))) return;
        if (p[x] > p[y]) swap(x, y);
        p[x] += p[y], p[y] = x;
    }
};

```

6.13 WaveletTree

```

#include <bits/stdc++.h>
using namespace std;

class WT
{
    typedef vector<int>::iterator iter;
    vector<vector<int>> r0;
    vector<int> arrCopy;
    int n, s;

    void build(iter b, iter e, int l, int r, int u)
    {
        if (l == r) return;
        int m = (l + r) / 2;
        r0[u].reserve(e - b + 1);
        r0[u].push_back(0);
        for (iter it = b; it != e; ++it)
            r0[u].push_back(r0[u].back() + (*it <= m));
        iter p = stable_partition(b, e, [=](int i) { return i <= m; });
        build(b, p, l, m, u * 2); build(p, e, m + 1, r, u * 2 + 1);
    }

    int q, w;
    int range(int a, int b, int l, int r, int u)
    {
        if (r < q or w < l) return 0;
        if (q <= l and r <= w) return b - a;
        int m = (l + r) / 2, za = r0[u][a], zb = r0[u][b];
        return range(za, zb, l, m, u * 2) +
            range(a - za, b - zb, m + 1, r, u * 2 + 1);
    }

public:
    // arr[i] in [0, sigma)
    WT(vector<int> arr, int sigma)
    {

```



```

    n = arr.size(); s = sigma; r0.resize(s * 2);
    arrCopy = arr;
    build(arr.begin(), arr.end(), 0, s - 1, 1);
}

// k in [1,n], [a,b] is 0-indexed, -1 if error
int quantile(int k, int a, int b)
{
    // extra conditions disabled
    if (/*a < 0 or b > n or*/ k < 1 or k > b - a) return -1;
    int l = 0, r = s - 1, u = 1, m, za, zb;
    while (l != r)
    {
        m = (l + r) / 2;
        za = r0[u][a], zb = r0[u][b], u *= 2;
        if (k <= zb - za) a = za, b = zb, r = m;
        else k -= zb - za, a -= za, b -= zb, l = m + 1, ++u;
    }
    return r;
}

// counts numbers in [x,y] in positions [a,b]
int range(int x, int y, int a, int b)
{
    if (y < x or b <= a) return 0;
    q = x, w = y;
    return range(a, b, 0, s - 1, 1);
}

// count occurrences of x in positions [0,k)
int rank(int x, int k)
{
    int l = 0, r = s - 1, u = 1, m, z;
    while (l != r)
    {
        m = (l + r) / 2;
        z = r0[u][k], u *= 2;
        if (x <= m) k = z, r = m;
        else k -= z, l = m + 1, ++u;
    }
    return k;
}

// x in [0,sigma)
void push_back(int x)
{
    int l = 0, r = s - 1, u = 1, m, p;
    ++n;

```

```

    while (l != r)
    {
        m = (l + r) / 2;
        p = (x <= m);
        r0[u].push_back(r0[u].back() + p);
        u *= 2;
        if (p) r = m;
        else l = m + 1, ++u;
    }
}

// doesn't check if empty
void pop_back()
{
    int l = 0, r = s - 1, u = 1, m, p, k;
    --n;
    while (l != r)
    {
        m = (l + r) / 2;
        k = r0[u].size(), p = r0[u][k - 1] - r0[u][k - 2];
        r0[u].pop_back();
        u *= 2;
        if (p) r = m;
        else l = m + 1, ++u;
    }
}

// swap arr[i] with arr[i+1], i in [0,n-1)
void swap_adj(int i)
{
    int &x = arrCopy[i], &y = arrCopy[i + 1];
    int l = 0, r = s - 1, u = 1;
    while (l != r)
    {
        int m = (l + r) / 2, p = (x <= m), q = (y <= m);
        if (p != q)
        {
            r0[u][i + 1] ^= r0[u][i] ^ r0[u][i + 2];
            break;
        }
        u *= 2;
        if (p) r = m;
        else l = m + 1, ++u;
    }
    swap(x, y);
}
};

```