

1. This problem is similar to the example given in section 10.9, except for the polarization. Instead of (10.110), the incident electric field is

$$\mathbf{E}_i = E_0 \epsilon_2 e^{ik(z \cos \alpha + x \sin \alpha)} \quad (1)$$

Then accordingly, (10.111), (10.112), (10.113) becomes

$$(\mathbf{n} \times \mathbf{E}_i)_{z=0} = -E_0 \epsilon_1 e^{ikx' \sin \alpha} \quad (2)$$

$$\mathbf{E}(\mathbf{x}) = -\frac{ie^{ikr} E_0}{2\pi r} (\mathbf{k} \times \epsilon_1) \int_0^a \rho d\rho \int_0^{2\pi} d\beta e^{ik\rho [\sin \alpha \cos \beta - \sin \theta \cos(\phi - \beta)]} \quad (3)$$

$$\mathbf{E}(\mathbf{x}) = -\frac{e^{ikr}}{r} a^2 E_0 (\mathbf{k} \times \epsilon_1) \frac{J_1(ka\xi)}{ka\xi} \quad (4)$$

giving the power per unit solid angle

$$\frac{dP}{d\Omega} = P_i \frac{(ka)^2}{4\pi} \left(\frac{\cos^2 \theta + \sin^2 \phi \sin^2 \theta}{\cos \alpha} \right) \left| \frac{2J_1(ka\xi)}{ka\xi} \right|^2 \quad (5)$$

2. Both (5) and (10.114) have azimuthal dependence (apart from that contained in ξ), unlike results (10.119) from the *scalar* Kirchhoff approximation. With normal incidence $\alpha = 0$, and for a special observation location at $\phi = \pi/4$, (5) and (10.114) produce the same θ -distribution, as it should due to the symmetry in this configuration.