Answer:

$$p(y;\lambda) = \frac{e^{-\lambda}\lambda^y}{y!} = (1/y!)\exp(y\log\lambda - \lambda)$$
 i.e.
$$T(y) = y; \; \eta = \log\lambda; \; a(\eta) = e^{\eta}; \; b(y) = (1/y!)$$
 in the form
$$p(y;\lambda) = p(y;\eta) = b(y)\exp(\eta^T T(y) = a(\eta))$$