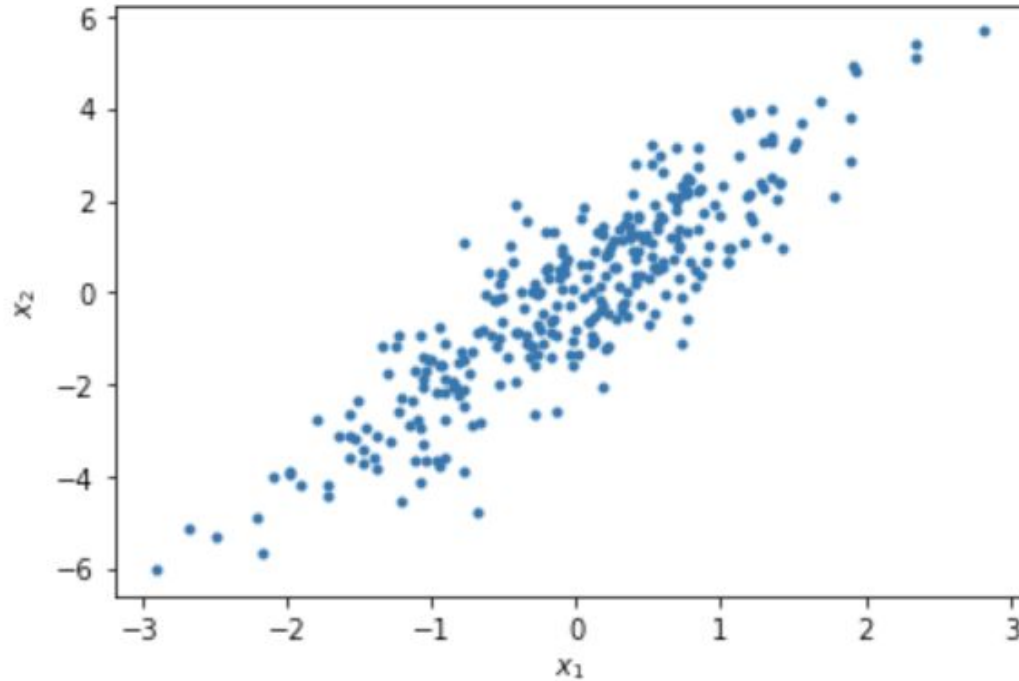


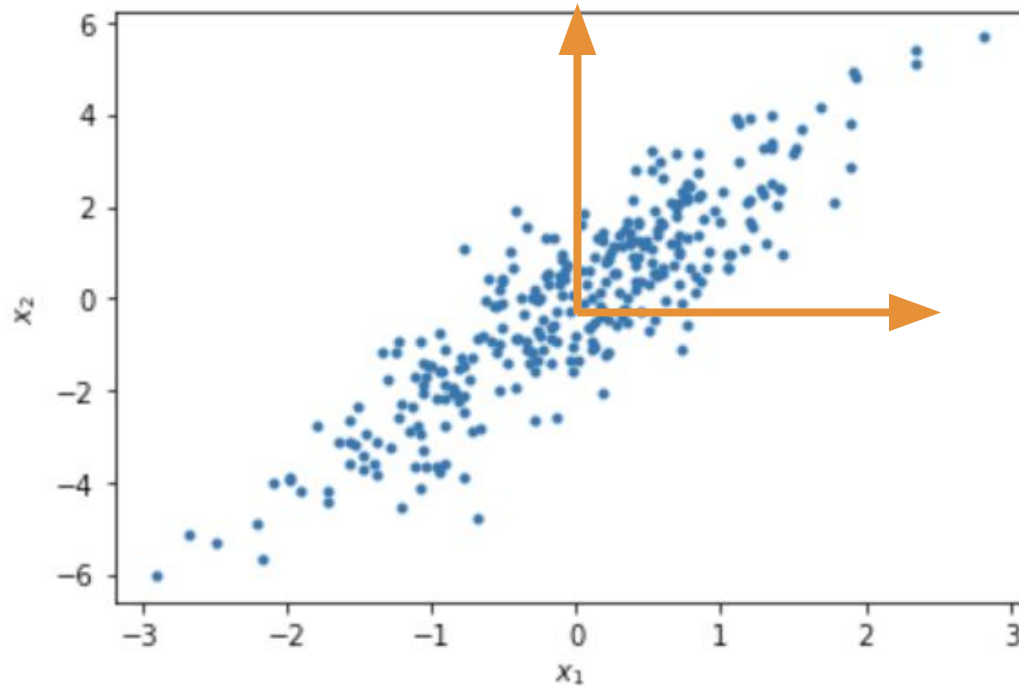
Last time:

Principal component analysis (PCA)



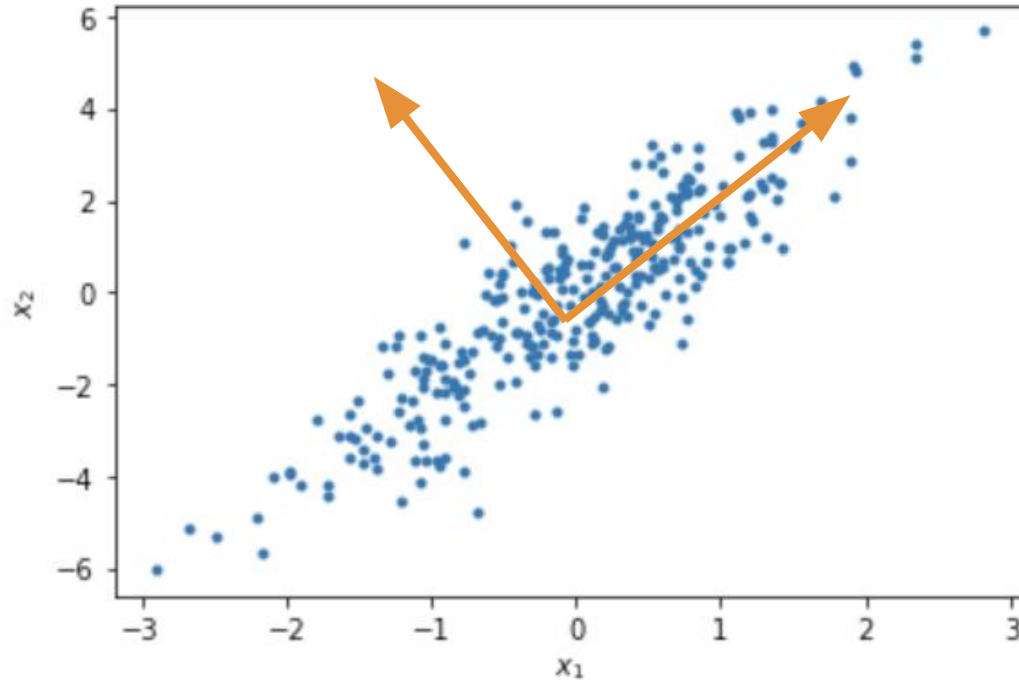
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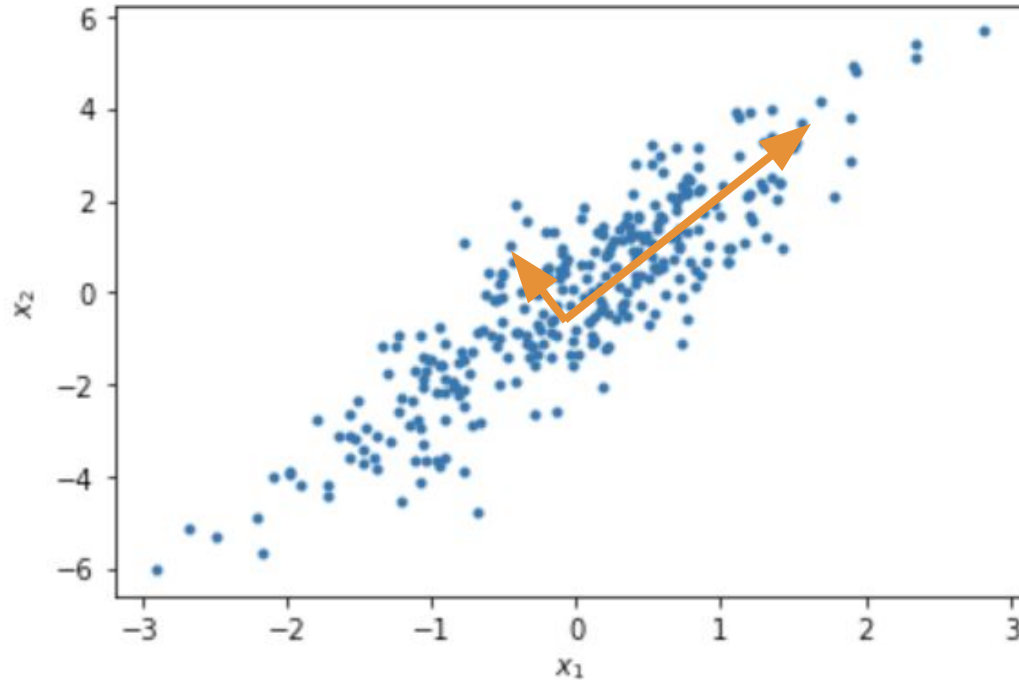
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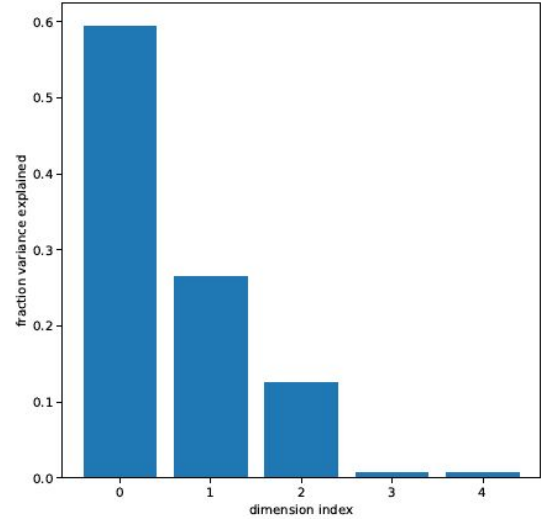
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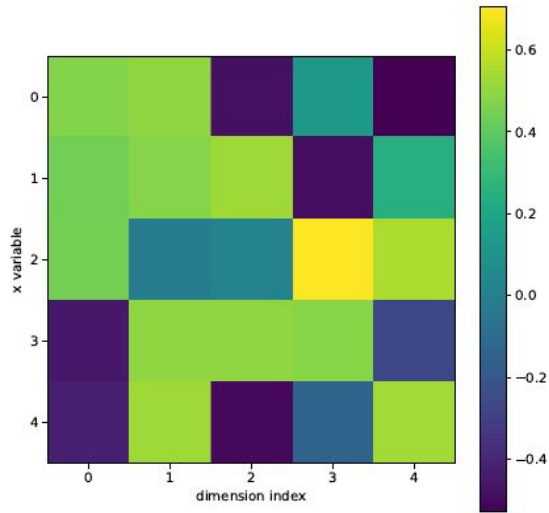


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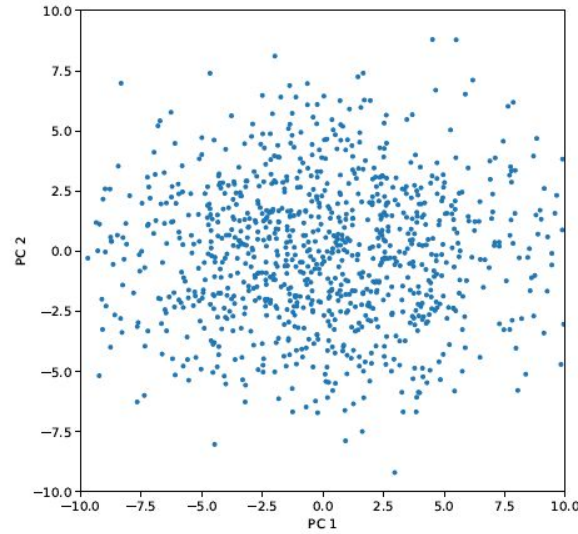
fraction explained variance



loadings



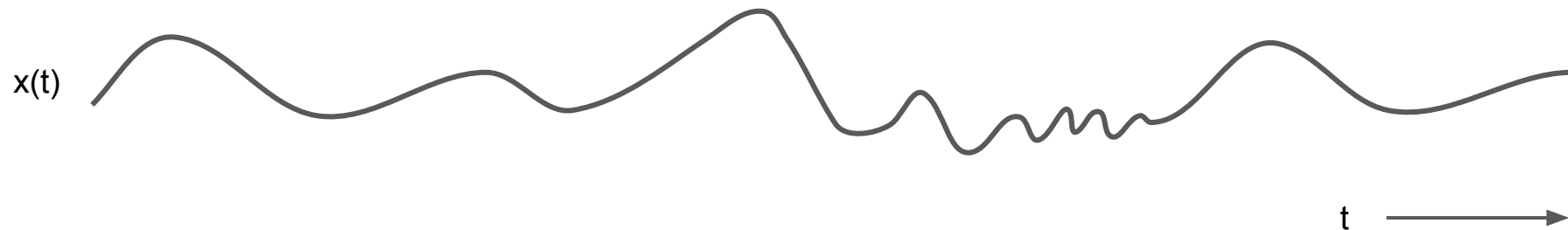
principal components



Today:

- PCA for time series
- tSNE (nonlinear dimensionality reduction)

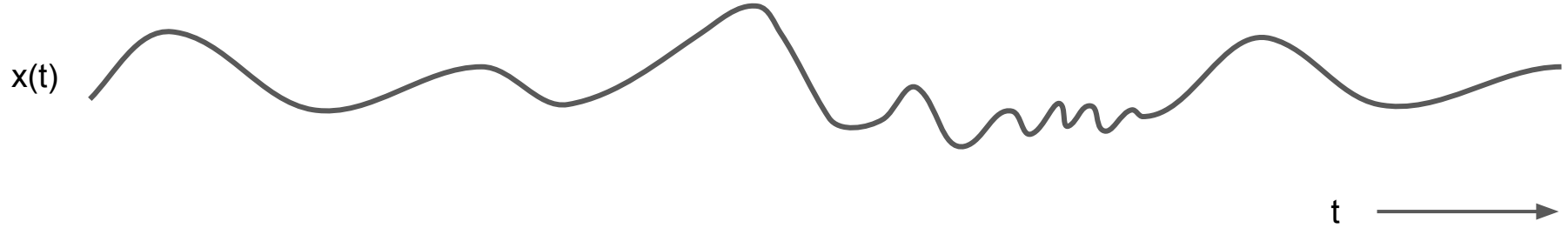
A time series is the output of a variable over time.



The graph shows a function $x(t)$ plotted against time t . The horizontal axis is labeled t with an arrow pointing to the right. The vertical axis is labeled $x(t)$. The function starts with a smooth, low-frequency oscillation. At a certain point, it drops sharply and enters a region of high-frequency, high-amplitude oscillations. After this region, it returns to a smooth, low-frequency oscillation.

Usually, we treat “samples” as being independent.
(e.g., subjects in a study, trials of an experiment)

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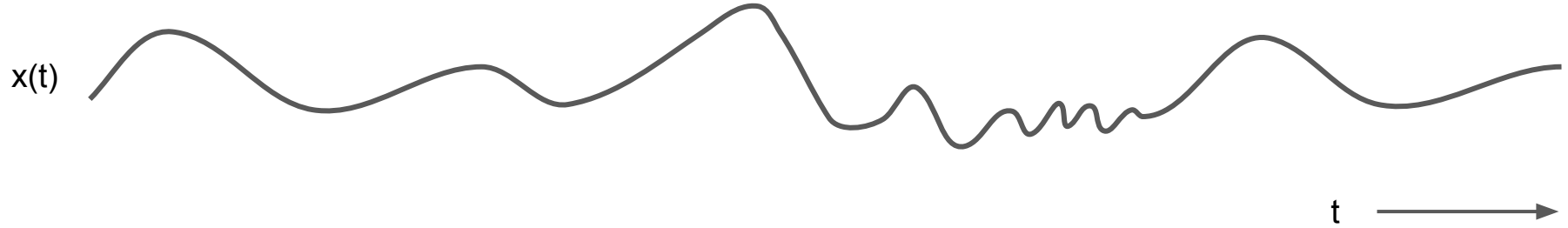


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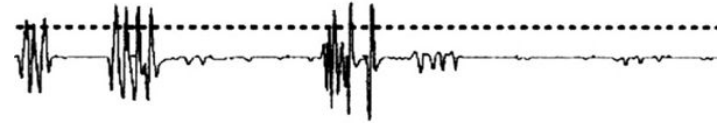
→ We should take advantage of its properties!

An important property:

The value of two nearby timepoints should be similar (smoothness).

Often in neuroscience, we work with time series.

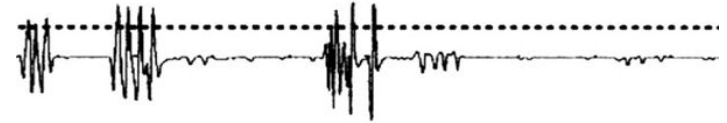
Examples:



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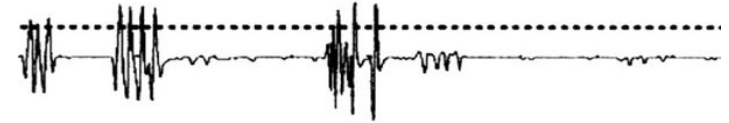
- EMG activity of arm reaches
- EEG activity
- action potential/spike waveforms
- pupil diameter trace
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- auditory signals
- any type of dynamics



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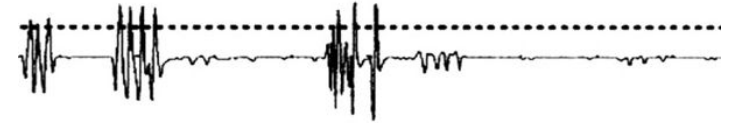
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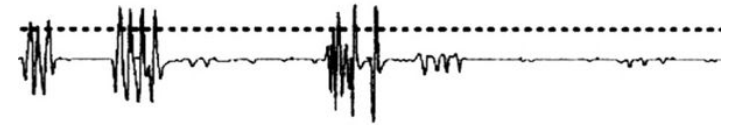
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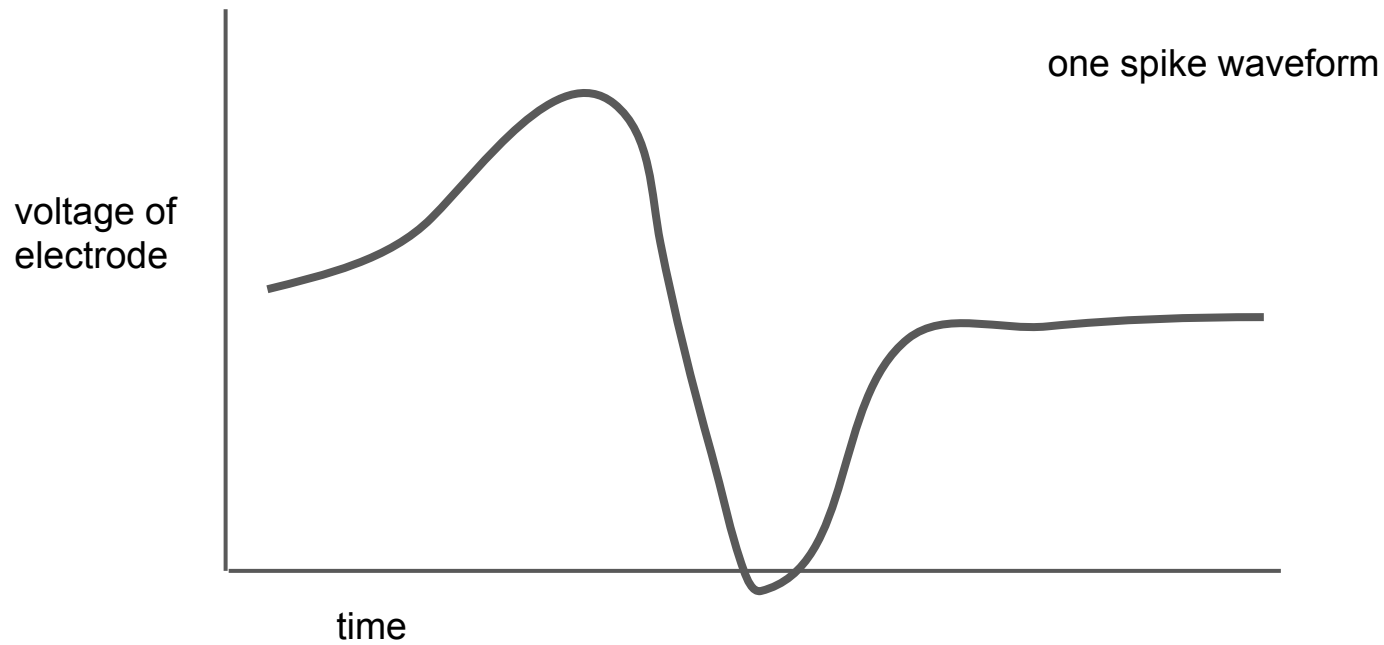
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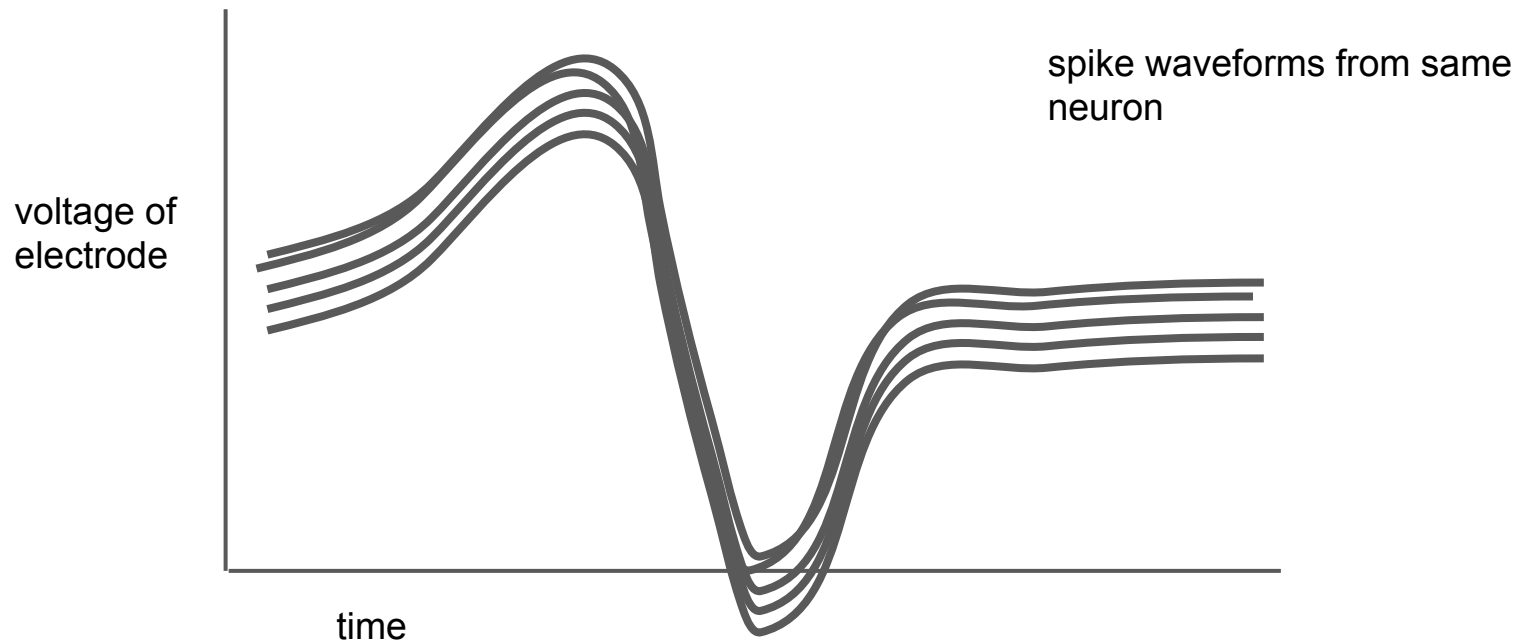
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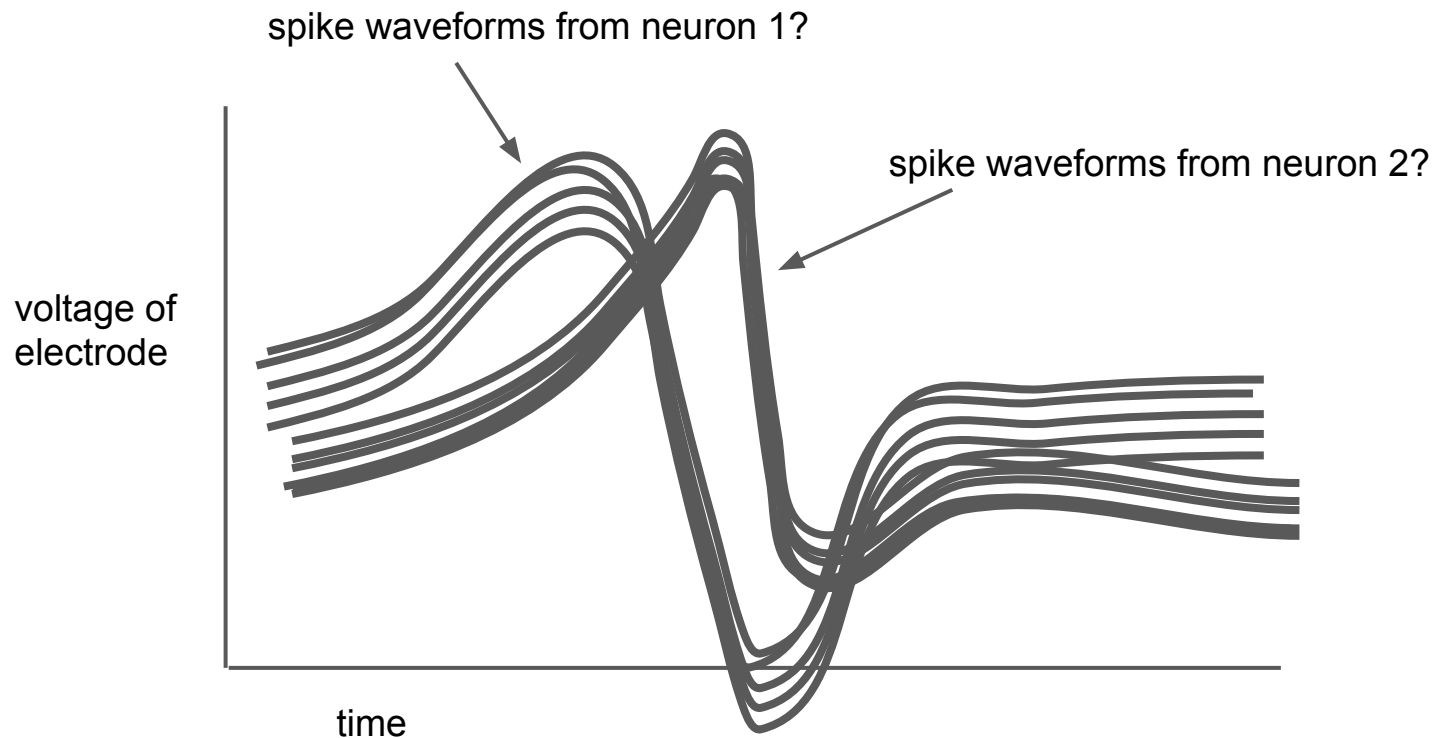


Solution: Identify “templates” of spike waveforms.
Each template corresponds to a different neuron!









PCA to the rescue!

Idea:

1. Treat each time point as a variable.
2. Treat each spike waveform as an observation.
3. Apply PCA (with time points as features)
4. Look at loadings of PCA

---> Colab Notebook

tSNE

high-d space (2-d):



tSNE reduced space (1-d):



tSNE

- short for “t-distributed stochastic neighbor embedding”

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tSNE

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- nonlinear dimensionality reduction: takes K features and maps datapoints to 2 or 3 dimensions
- key idea: nearby distances between datapoints in reduced-space are similar to distances in high-d space

high-d space (2-d):



tSNE reduced space (1-d):



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Note: tSNE has some hyperparameters that we are ignoring for this class (knobs that may be important in defining clusters)

Colab notebook:

t-SNE on a simple problem (together)

t-SNE with increasing number of clusters (on your own)

