# Quantitative Exercise

Marine Collery and Benjamin Seregi 10/30/2017

```
library(knitr)
opts_chunk$set(tidy.opts=list(width.cutoff=60),tidy=TRUE)
```

#### Introduction

We are looking at the Monty Hall problem.

#### Dataset

The dataset is generated by a C program that save the samples in a CSV files.

Setting the directory to the data directory.

```
getwd()
## [1] "/Users/Marine/Documents/1_KTH/4_Courses/3_RMSW/Assignments/Quantitative"
setwd("/Users/Marine/Documents/1_KTH/4_Courses/3_RMSW/Assignments/Quantitative")
getwd()
```

## [1] "/Users/Marine/Documents/1\_KTH/4\_Courses/3\_RMSW/Assignments/Quantitative" Read in data frame.

```
## [1] "CarDoor" "Selected" "S" "NS"
summary(mdf)
```

```
CarDoor
                        Selected
                                             S
##
                                        Length: 100000
## Length:100000
                      Length:100000
## Class :character
                      Class : character
                                        Class : character
## Mode :character Mode :character
                                        Mode :character
##
        NS
## Length:100000
## Class :character
## Mode :character
```

We can then factorize the data.

```
# factorize the data

mdf$Sf = as.factor(mdf$S)
```

```
mdf$NSf = as.factor(mdf$NS)
# summary(mdf)
```

The function countWin will count when the player wins and has changed his mind and when he has win without changing his mind.

```
# Count all the wins in 2 sets : Switch or No Switch
countWin <- function(df) {</pre>
    # df is a dataframe
    11 <- length(df$NS)</pre>
    sumWinS <- 0</pre>
    sumWinNS <- 0
    for (i in 1:11) {
         if (df$S[i] == "W" & df$NS[i] == "L") {
             sumWinS <- sumWinS + 1</pre>
             df$sumWinSwitched[i] <- sumWinS</pre>
             # Not changed:
             df$sumWinNotSwitched[i] <- sumWinNS</pre>
         } else if (df$S[i] == "L" & df$NS[i] == "W") {
             sumWinNS <- sumWinNS + 1</pre>
             df$sumWinNotSwitched[i] <- sumWinNS</pre>
             # Not changed:
             df$sumWinSwitched[i] <- sumWinS</pre>
         }
    }
    return(df)
}
mdf <- countWin(mdf)</pre>
summary(mdf)
```

```
##
     CarDoor
                         Selected
                                               S
##
   Length:100000
                       Length:100000
                                          Length: 100000
##
   Class :character
                       Class : character
                                          Class : character
   Mode :character
                       Mode :character
                                          Mode :character
##
##
##
         NS
                                 NSf
                                            sumWinNotSwitched sumWinSwitched
##
                       Sf
   Length: 100000
                       L:33212
                                 L:66788
                                           Min. : 1
                                                              Min. :
##
                                           1st Qu.: 8424
                                                              1st Qu.:16577
   Class : character
                       W:66788
                                 W:33212
   Mode :character
##
                                           Median :16736
                                                              Median :33264
##
                                           Mean
                                                 :16690
                                                              Mean
                                                                     :33310
##
                                           3rd Qu.:25012
                                                              3rd Qu.:49988
##
                                           Max.
                                                  :33212
                                                              Max.
                                                                     :66788
```

### Variables

We only have very few variables for this problem that are relevant for the analysis. Those variables are:

- S : (equal to "W" or "L") this variable represent whether the player has Win or Lose IF he has Switch.
- NS : (equal to "W" or "L") this variable represent whether the player has Win or Lose IF he has Not Switch.

NS and S are dependent of each other: if one is "W" the other is "L". We could have kept only one of them but keeping both facilitates the comprehension and the display of the result.

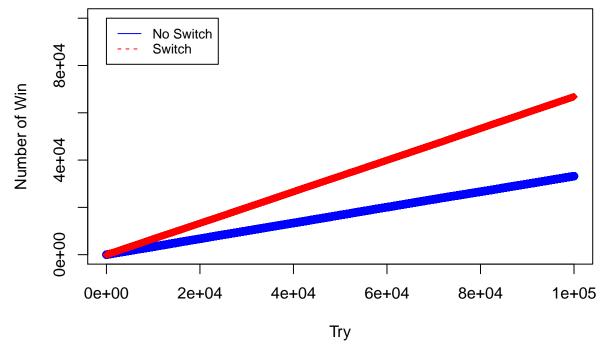
The other attributes of the data frame or either to the facilitate the analysis (sumWinSwitched and sumWinNotSwitched) or are required to understand the problem (CarDoor and Selected). The last ones are required for the generation.

## Analysis

```
# Plot Win without switch
plot(mdf$sumWinNotSwitched, xlim = c(0, length(mdf$NS)), ylim = c(0,
    length(mdf$NS)), xlab = "Try", ylab = "Number of Win", col = "blue",
    type = "b", lty = 1)

# Add Win with switch
lines(mdf$sumWinSwitched, pch = 18, col = "red", type = "b",
    lty = 2)

# Legend
legend(0, length(mdf$NS) - 1, legend = c("No Switch", "Switch"),
    col = c("blue", "red"), lty = 1:2, cex = 0.8)
```



The probability of winning with a switch is in theory 2/3.

# probWinWithSwitch = mdf\$sumWinSwitched[length(mdf\$NS)]/(length(mdf\$NS))

We have for those samples the probability:

# ${\tt probWinWithSwitch}$

## ## [1] 0.66788

We can then conclude that our samples have the expected properties.