

① Laplace of

$$\sin(at) = \frac{a}{s^2 + a^2} = 5 \left(\frac{2\pi}{s^2 + 4\pi^2} \right)$$

$$f(t) = 3 \times \delta(t) + 5 \sin(2\pi t)$$

$$= \frac{3}{s} e^{-s} + \frac{10\pi}{s^2 + 4\pi^2}$$

$$= \frac{3e^{-s}}{s} + \frac{10\pi}{s^2 + 4\pi^2}$$

② inverse Laplace

$$\frac{z}{s^2 + 8s + 15} = \frac{1}{s+3} - \frac{1}{s+5} = e^{-3t} - e^{-5t}$$