

**Question 1.** (a) Each bundles have 6 recommendations.



I choose the bundle "Between Spring". Since it is a bundle related to seasons and flower, I guess the top five recommendations are:

1. The bouqs.
2. Spring rose.
3. Hello spring.
4. Autumn.
5. 2014 summer.

(b) First, I use `read_csv` to read the file since I can't install the package `data.table` due to a R version issue.

```
1 library(tidyverse)
2 library(lsa) # cosine()
3
4 # Question 1
5 ac_bundles_dt <- read_csv('piccollage_accounts_bundles.csv')
6 ac_bundles_matrix <- as.matrix(ac_bundles_dt[, -1, with=FALSE])
7 rm(ac_bundles_dt)
```

(i) The cosine recommendation matrix can be computed by the following code:

```
1 # Question 1 (b-i)
2 top_5_recommend_cos <- function(ac_bundles_matrix){
3   cos_matrix <- cosine(ac_bundles_matrix) # Obtain cosine similarity
4   sorted_names_matrix <- c() # construct a empty matrix
```

```

5
6   for (i in colnames(cos_matrix)){ # extract every column names
7     temp_vector <- cos_matrix[,i] # extract a column of cos matrix
8     # sort the similarities decreasingly
9     temp_vector_sorted <- data.frame(sort(temp_vector, decreasing=TRUE))
10    # the rownames are sorted according to the cosine similarity, too
11    names_vector <- rownames(temp_vector_sorted)
12    # combine the result to get a full recommendation matrix
13    sorted_names_matrix <- cbind(sorted_names_matrix, names_vector)
14  }
15
16  # assign the column names to the sorted names matrix
17  colnames(sorted_names_matrix) <- colnames(cos_matrix)
18  # We only want top 5 (omit each bundle itself)
19  recommand_matrix <- sorted_names_matrix[2:6,]
20
21  return(recommand_matrix)
22 }
23
24 recommand_matrix_cos <- top_5_recommnd_cos(ac_bundles_matrix)

```

---

Use the command

```
> recommand_matrix_cos[, "betweenspring"]
```

The console returns the following bundles:

```
"OddAnatomy" "supersassy" "word" "KLL" "xoxo"
```

(ii) The correlation recommendation matrix can be computed by the following code:

---

```

1 # Question 1 (b-ii)
2 mean_centering_col <- function(ac_bundles) {
3   bundle_means <- apply(ac_bundles, 2, mean)
4   bundle_means_matrix <- t(replicate(nrow(ac_bundles), bundle_means))
5   # Subtract each row with its mean
6   ac_bundles_mc_b <- ac_bundles - bundle_means_matrix
7
8   return(ac_bundles_mc_b)
9 }
10
11 ac_bundles_matrix_centered <- mean_centering_col(ac_bundles_matrix)
12 recommand_matrix_cor <- top_5_recommnd_cos(ac_bundles_matrix_centered)
13 rm(ac_bundles_matrix_centered)

```

---

Use the command

```
> recommand_matrix_cor[, "betweenspring"]
```

The console returns the following bundles:

```
"OddAnatomy" "supersassy" "word" "xoxo" "KLL"
```

(iii) The adjusted-cosine based recommendation matrix can be computed by the following code:

---

```

1 # Question 1 (b-iii)
2 mean_centering_row <- function(ac_bundles) {
3   bundle_means <- apply(ac_bundles, 1, mean)
4   bundle_means_matrix <- t(replicate(ncol(ac_bundles), bundle_means))
5   # Subtract each row with its mean
6   ac_bundles_mc_b <- ac_bundles - t(bundle_means_matrix)
7

```

```

8   return(ac_bundles_mc_b)
9 }
10
11 # for adjust cosine
12 ac_bundles_matrix_ad <- mean_centering_row(ac_bundles_matrix)
13 recommand_matrix_ad <- top_5_recommnd_cos(ac_bundles_matrix_ad)
14 rm(ac_bundles_matrix_ad)

```

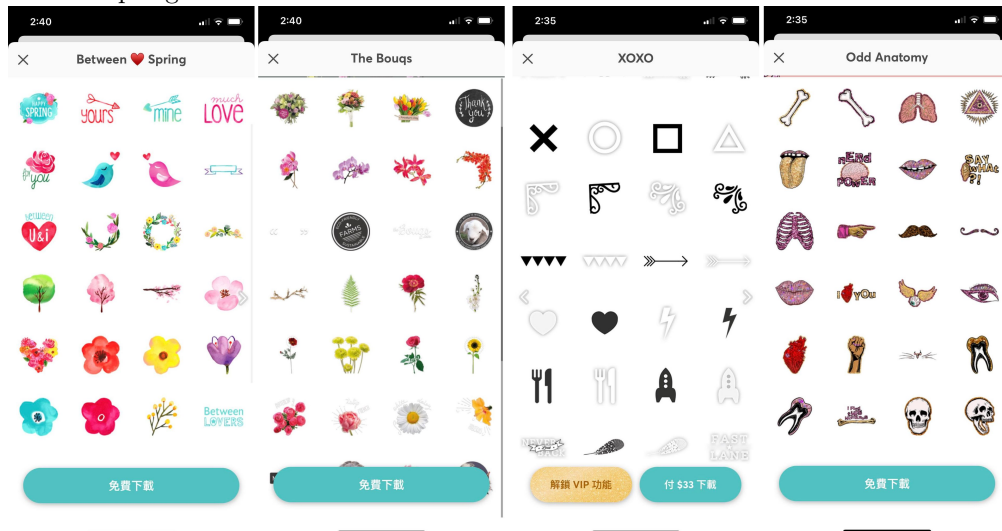
Use the command

```
> recommand_matrix_ad[, "betweenspring"]
```

The console returns the following bundles:

```
"OddAnatomy" "thebouqs" "xoxo" "word" "between"
```

(c) However, I have found some of the recommended bundles which is in the dataset. They share some features with the bundle "between spring". Such as flowers or words



(d) Basically, I think cosine similarity, correlation, and adjusted-cosine are the same things. We try to define similarities in a inner product space ( $\mathbb{R}^n$ ) by generalized the cos function. The main difference is that we view data as vectors centralized at different points: cosine similarity is centered at 0, adjusted-cosine is centered at the mean of all data, and correlation is centered at 0, but we subtract each vector with the mean of its components. ■

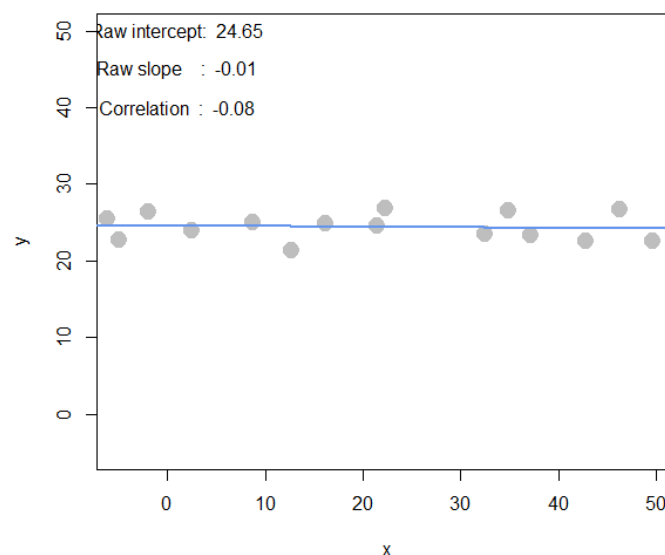
**Question 2.** Use the command

```
source("demo_simple_regression.R")
```

```
interactive_regression()
```

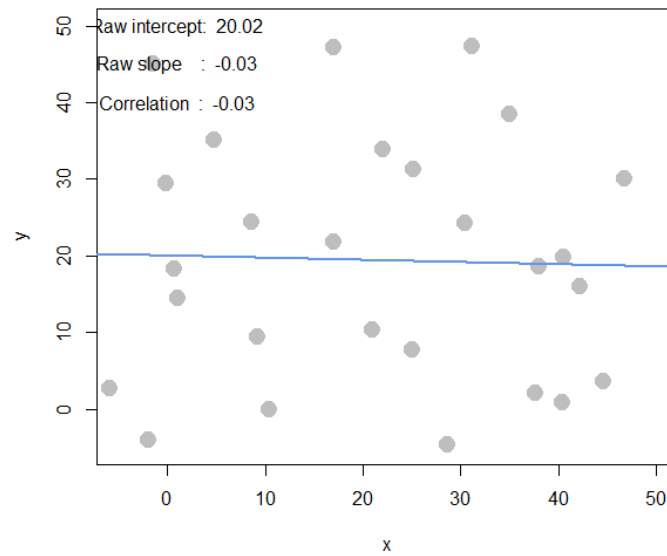
to conduct simulations.

(a) Create a horizontal set of random points, with a relatively narrow but flat distribution.



- The slope of  $x$  and  $y$  I expect  $m = 0$
- The correlation of  $x$  and  $y$  that I expect  $r(x, y) = 0$

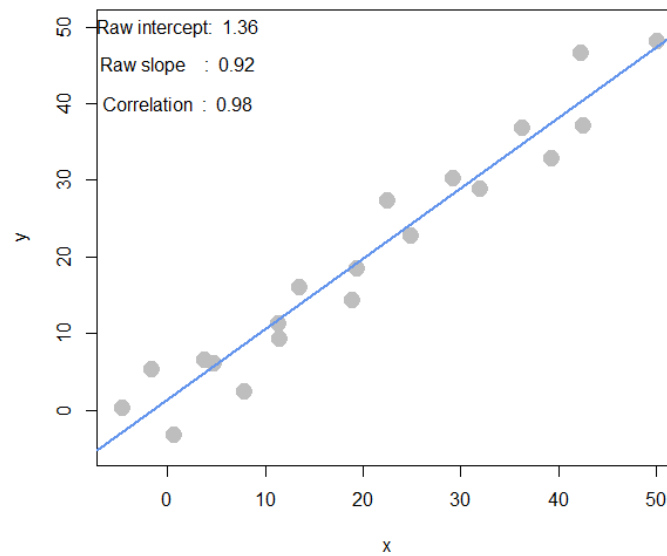
(b) Create a completely random set of points to fill the entire plotting area, along both  $x$ -axis and  $y$ -axis



- The slope of  $x$  and  $y$  I expect  $m = 0$
- The correlation of  $x$  and  $y$  that I expect  $r(x, y) = 0$

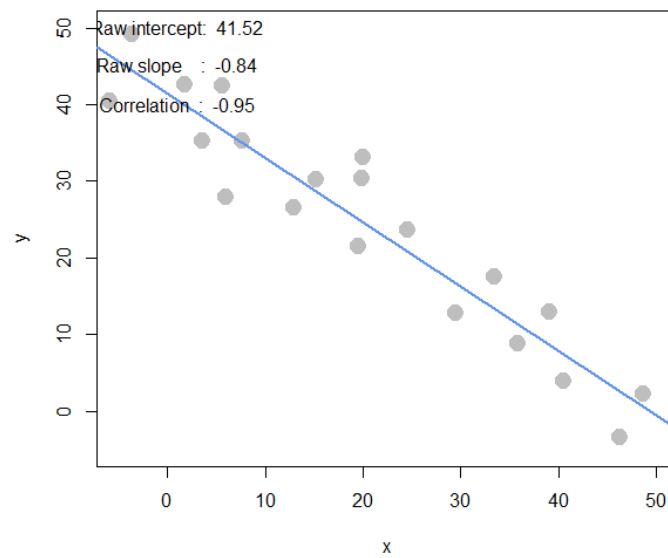
(c) Create a diagonal set of random points trending upwards at 45 degrees

- The slope of  $x$  and  $y$  I expect  $m = 1$
- The correlation of  $x$  and  $y$  that I expect  $r(x, y) = 1$

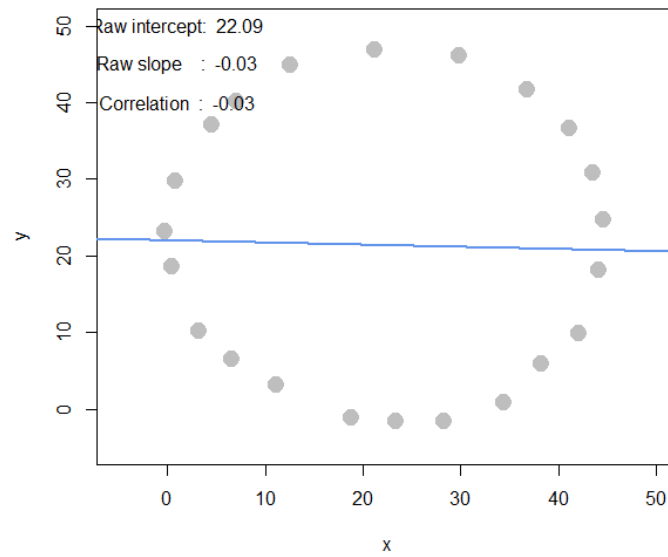


(d) Create a diagonal set of random trending downwards at 45 degrees

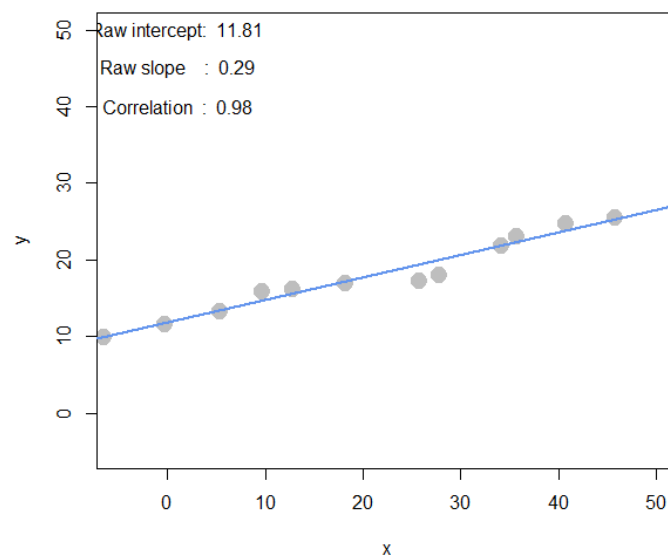
- The slope of  $x$  and  $y$  I expect  $m = -1$
- The correlation of  $x$  and  $y$  that I expect  $r(x, y) = 1$



(e) I found that when all data points are on a circle, the correlation would be 0, too.



(f) I found that when all data points are on a straight line whose slope is nonzero, then the correlation would be 1.



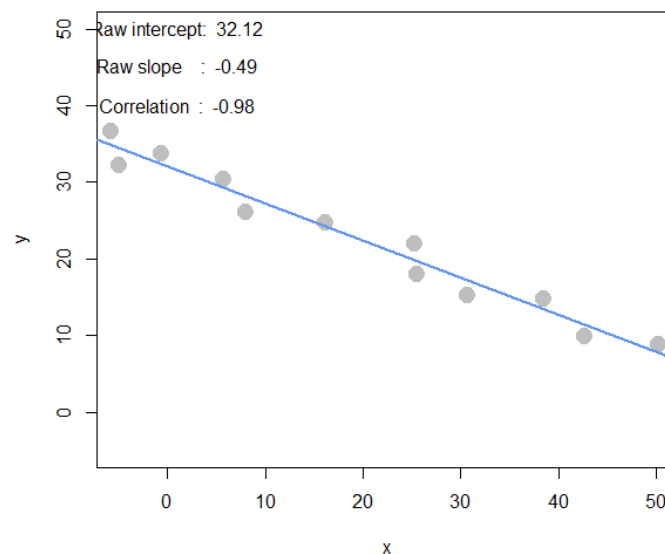
(g) The code of this problem:

---

```
1 # Question 2 (g)
2 source("demo_simple_regression.R")
3 pts <- interactive_regression() # run the simulation and record the points
4 slope <- summary(lm(pts$y~pts$x)) # estimate the regression intercept and slope
5 cor_pts <- cor(pts) # estimate the correlation
6 pts_std <- scale(pts) # standardize
7 slope_std <- summary(lm(pts_std[, "y"]~pts_std[, "x"])) # regression slope
8 cor_pts_std <- cor(pts_std) # correlation
```

---

(i) The points generated:



(ii) The regression intercept is  $k = 32.12312$  and slope  $m = -0.48548$ .

(iii)  $r = -0.9834927$ .

(iv) The regression intercept of the standardized values is  $k = 0$  and slope  $m = -0.9835$ .

(v) It suggests that the correlation is the slope of the regression model of standardized values.

