

Tutorial -6

SOEN-321

Problem-1

Let $x=111$ and $y=19301$. Factor $n=21311$ using the fact that $x^2 \equiv y^2 \pmod n$.

$$x^2 - y^2 = 0 \pmod n$$

$$x^2 - y^2 = Kn$$

$$(x + y)(x - y) = k_1 k_2 n$$

$$(x + y)(x - y) = k_1 p k_2 q$$

$$\gcd(x \pm y, n) = p \text{ or } q$$

$$\gcd(111 + 19301, 21311)$$

$$\gcd(19412, 21311)$$

$$21311 = 19412 + 1899$$

$$19412 = 10 \times 1899 + 422$$

$$1899 = 4 \times 422 + 211$$

$$422 = 2 \times 211 + 0$$

$$\gcd(19412, 21311) = p = 211$$

$$q = \frac{n}{p} = \frac{21311}{211} = 101$$

Problem 2

Suppose Bob has an RSA Cryptosystem with a large modulus n for which the factorization cannot be found in a reasonable amount of time. Suppose Alice sends a message to Bob by representing each alphabetic character as an integer between 0 and 25 (i.e., $A \leftrightarrow 0$, $B \leftrightarrow 1$, etc.), and then encrypting each residue modulo n as a separate plaintext character.

Describe how Eve can easily decrypt a message which is encrypted in this way.

Eve can construct a lookup table for all the valid 26 ciphertexts by encrypting the letters A to Z using Bob's public key.

Then Eve can use this table (or more precisely the inverse of this table) to decrypt any ciphertext encrypted by Alice

m	$c = m^e \bmod n$
$A = 0$	$c = 0$
$B = 1$	$c = 1$
...	...
$Z = 25$...