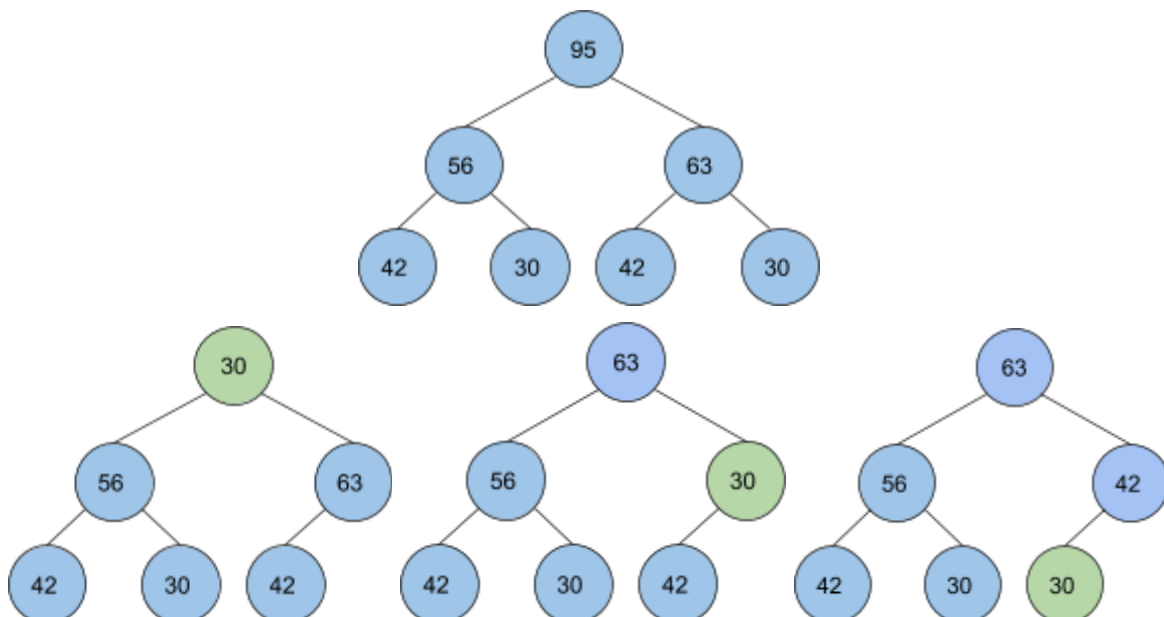


Topics

- I. Heaps review
 - A. Heaps are binary trees that are complete; children are either greater than their parents (min-heap) or less than their parents (max-heaps)
- II. Removing from a Heap
 - A. We'll only ever remove the root of the heap (the min or max element)
 - B. Just like adding, we'll maintain the shape before handling the order
 - C. Algorithm:
 1. Remove the data from the root (save it somewhere to be returned)
 2. Move the last element in the array (the element at index size) to the root
 3. Heapify-down (down-heap)
 - a) Compare the new data at the root to its children
 - b) If this data is not in the correct order, swap with its minimum (min-heap)/maximum (max-heap) child
 - (1) You also need to handle conditions where the node only has one left child (because the tree is complete, a node will never have just a right child)
 - c) Repeat until the data falls back in line with the order property or it has no children/becomes a leaf node



- D. For the purposes of this course, assume we'll never ask you to handle duplicate values in a heap
- III. Build Heap
 - A. The build heap algorithm takes a collection of data and builds a heap from it

- B. How not to: iterate through the collection & call add on every element ($O(n \log n)$)
- C. How to:
 - 1. Drop everything as-is into the backing array (just like before, we're prioritizing the shape property over the order property)
 - 2. Starting at index $n = \text{size}/2$ (the first node to have children), heapify-down
 - 3. Decrement n and heapify-down the node at that index
 - a) Repeat until $n = 0$
- D. Efficiency: $O(n)$ ([proof](#))

No Content - Wednesday

Friday

Topics

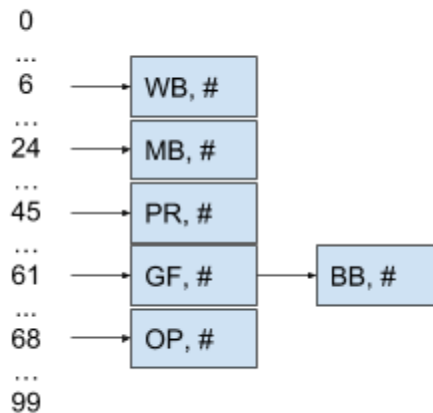
I. Maps

- A. Maps are...
 - 1. ...collections of <key, value> pairs
 - 2. ...searchable
 - 3. ...unordered
- B. Keys are unique (no duplicate keys can exist in one Map) and cannot be changed, i.e. you can't change the key of an entry currently in the map
- C. Maps store and retrieve using the key to identify entries
- D. Values can change, you can change the value of an entry
- E. Values can have duplicates
 - 1. The entries <A, 3> and <B, 3> can exist in the same map, but the entries <A, 3> and <A, 5> cannot exist in the same map
- F. Hash function
 - 1. What it returns - an integer value (the hashCode) that represents the key
 - 2. Why we need it - the hashCode is used to place the map entry into the backing array and then used to search for an entry when the key is known
 - 3. How we get it - every Object has a .hashCode() method; this method can be customized for any Object you create, but make sure they are relatively unique (i.e. don't return 1 for every instance)
 - 4. How to use it - compress the hashCode to fit within the bounds of the backing array: $\text{index} = \text{hashCode} \% \text{backing array length}$
- G. Collision strategies → what if 2+ entries hash & compress to the same index?
 - 1. External chaining - uses a singly linked list at each index so everything that hashes to the same index will be in a linked list at that index
 - a) Example - we want to put <phone number, athletic department> key-value pairs into a map with a backing array of length 100

v - value	H(k) - hashCode	H(k) % 100 - index
Men's Basketball	4424	24

Women's Basketball	5406	06
Baseball	2261	61
Public Relations	5445	45
Operations	6668	68
Golf	0961	61

Index



- b) We don't want everything to be stored at the same index, so we need to periodically resize when we hit a certain max load factor
 - (1) Load factor = size / capacity = (the number of map entries in the map) / (the capacity of the backing array)
 - (2) Usually the maximum load factor is around 75%
 - (3) Make the capacity of the array prime to reduce collisions

2. Probing Collision Strategies

- a) Linear probing
- b) Quadratic probing
- c) Double hashing

II. HashMaps

- A. HashMaps are subsets of Maps, they inherit all the behaviors and qualities of Maps