

Topics

I. Iterator and Iterable

A. Import statements:

1. import java.lang.Iterable → implicit, not very involved, only requires one method to be implemented
2. import java.util.Iterator → explicit, very involved, requires the creation of a class with several methods that must be implemented

B. Code demo

```
import java.lang.Iterable;
import java.util.Iterator;
public class LinkedList<Type> implements Iterable<Type> {
    private Node<Type> head;
    /** constructor omitted **/

    public Iterator<Type> iterator() { // for Iterable
        return new LLit(this);
    }

    private class LLit implements Iterator<Type> {
        private Node<Type> current;
        private LLit(LinkedList list) {
            current = head; // gives us starting point
        }
        public boolean hasNext() {
            return current != null;
        }
        public Type next() {
            Node<Type> tmp = null;
            if(hasNext()) {
                tmp = current;
                current = current.next;
                return tmp.data;
            } else {
                return null;
            }
        }
    }

    /** private inner Node class omitted **/
}
```

- C. Iterable - requires the iterator() method to be overridden which returns the iterator
- D. Iterator - an object which iterates through the structure
 - 1. Our iterator will be similar to the loops we've used to manually traverse through the list
 - 2. Requires two methods to be overridden: next() and hasNext()
 - a) hasNext() → returns if current is NOT null (if the iterator *has* a *next* data element to return)
 - b) next() → returns the *next* data the iterator has yet to give you (the data from the current node) and moves current to the next node

E. Code demo: using the iterator

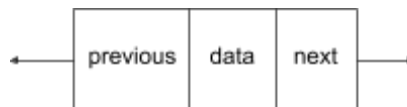
```
/** in some main method */
LinkedList<String> courses = new LinkedList();
courses.add("1332"); // add some more courses...

// implicitly use iterator
for (String course: courses) {
    System.out.println(course);
}
// explicitly use iterator
Iterator<String> courseit = courses.iterator();
while(courseit.hasNext()){
    System.out.println(courseit.next());
}
```

- 1. Iterators are implicitly called when using for-each loops - there's no stopping it and you can't really use it to alter list values
- 2. You can explicitly use the iterator by instantiating an Iterator to step through the linked list and have more control over each step

II. Doubly Linked Lists

- A. Generally always have both a head and tail pointer
- B. A doubly linked node is going to have next and previous pointers and data.



- C. For a DLL of size 0, both the head and tail point to null
- D. For a DLL of size 1, both the head and tail point to the single node
- E. For a DLL of size > 1:
 - 1. Adding to the front:
 - a) Create the new node
 - b) Connect the node to the LL → set the new node's next to the head
 - c) Connect the LL to the node → set the head's prev to the new node
 - d) Point the head to the new node
 - 2. Adding to the back:
 - a) Create the new node

- b) Connect the node to the LL → set the new node's prev to the tail
 - c) Connect the LL to the node → set the tail's next to the new node
 - d) Point the tail to the new node
- 3. Make sure you always change the head/tail after everything else has been connected, we do not want to lose these references!
- 4. Removing from the back:
 - a) Set the tail to tail's previous
 - b) Set the tail's next to null
- 5. Removing from the front:
 - a) Set the head to head's next
 - b) Set the head's previous to null
- 6. Edge case: removing from a list of length 1 → set head and tail to null

III. Circular Singly Linked Lists

- A. The last node in the list points back to the head.
- B. We can no longer use `current == null` to check if we've reached the end of our list
 - 1. We must use `current == head` (reference equality) to terminate our loop
- C. How to NOT add to the front:
 - 1. Create a new node, point it to the head, and move the head
 - 2. Resetting the last node to point to the new head would be $O(n)$ because we would have to iterate through the list to find it
- D. Adding to the front in $O(1)$ (the correct way):
 - 1. Create a new, empty node
 - 2. Connect the node to the CLL → set the new node's next to head's next
 - 3. Connect the CLL to the node → set head's next to the new node
 - 4. Put the data from the head into the new node
 - 5. Put the data we want to add into the head node
- E. Adding to the back in $O(1)$:
 - 1. Perform the steps to add to the front
 - 2. Now, just move the head to head's next and the data you just added is now at the back of the list
- F. Removing from the front in $O(1)$ (when size > 1):
 - 1. Save the data from the head somewhere to return later
 - 2. Copy the data from head's next into the head
 - 3. Set head's next pointer to head's next's next (essentially cutting the node at index 1 out of the list)
- G. Unfortunately, removing from the back cannot be optimized with a data manipulation trick → it will be $O(n)$ to iterate to the node before the last one

Wednesday

Topics

- I. Recursion Basics
 - A. Definition: a method repeatedly calls itself

B. Must have:

1. Base case/terminating condition (can have multiple)
2. Recursive call to function (can have multiple)
3. A parameter that advances toward termination (can have several)

C. Termination is very important to prevent infinite recursion

D. Basic structure:

```
rFunction (parameter)
    if (parameter meets terminating condition)
        return value
    else
        return rFunction(changed parameter)
    // self-call can be before return but not after
```

II. Math-based recursion - classic examples: factorial, fibonacci

A. Example: compound interest $A = P(1 + (r/n))^n$

B. Function: recursive IRA

```
rIRA(p, r, t) // principle, rate, time
    if (t <= 1)
        return p;
    else
        return Math.pow((1+r/4),4) * rIRA(p,r,t-1) + p;
```

C. Investing \$2000 a year with an 8% growth rate...

1. From 40 to 70: ~\$240,000
2. From 30 to 70: ~\$550,000
3. From 20 to 70: \$1,250,000 (\$100,000 of your own money was invested)

III. LinkedList recursion

A. Example: a LL contains all data in sorted order so all duplicates are contiguous, now remove all the duplicates

B. Function: remove all duplicates

```
rRemove(c) // current node
    if (c == null)
        return null;
    else
        c.next = rRemove(c.next);
        if (c.next != null && c.data == c.next.data)
            return c.next; // cut out a duplicate
        else
            return c; // makes no changes to the list
```

C. How it works: starting from the end of the list, this function “collapses” duplicate chains; the last duplicate in the chain is technically the one that stays in the list

D. Trace through code with the following example:

1. head → [2] → [3] → [3] → null

Topics

I. Stacks Intro: Array, SLL, and DLL operation review

Time Complexity	Access	Search	Add (to front)	Remove (from front)
Array	$O(1)$	$O(n)$	$O(n)$	$O(n)$
SLL	$O(n)$	$O(n)$	$O(1)$	$O(1)$
DLL	$O(n)$	$O(n)$	$O(1)$	$O(1)$

- A. Access - accessing an element at a given index
 - 1. Arrays - we can access data at a given index in constant time
 - 2. LL - even if we have index information (eg. storing index as an attribute of the node), we cannot access that index without iterating to it
- B. Search - accessing an element at an unknown index
 - 1. Always $O(n)$ for unsorted structures
- C. Add (to front)
 - 1. Arrays - we must shift everything to create an empty spot
 - 2. LL - easily add to front with head pointer
- D. Remove (from front)
 - 1. Arrays - we must shift everything to fill empty spot
 - 2. LL - easily move the head pointer over one
- E. Remove (from back, with tail)
 - 1. SLL - $O(n)$; DLL - $O(1)$

II. Stacks

- A. Abstract Data Type (ADT) - a conceptual outline for how a data structure should be implemented (eg. expected behaviors)
 - 1. Data structures are the concrete implementations of ADTs
 - 2. Multiple implementations exist with different backing structures
- B. A stack can be backed by an Array, a SLL, or a DLL.
- C. What does a stack do?
 - 1. Examples: a Pringles can, the recursive stack, a laundry pile
 - 2. To add, we'll "push" items onto the stack
 - 3. To remove, we'll "pop" from the stack, but we can only access what was pushed last: "Last In, First Out," a.k.a. LIFO
 - 4. We cannot access anything other than what is at the top of the stack
 - 5. Stacks are very linear and are implemented with linear structures: Arrays and LinkedLists (Singly or Doubly)
- D. Stack operations - implementation depends on backing structure
 - 1. void push(x) - add
 - 2. x pop() - remove
 - 3. x top()/peek() - returns the next item to pop without actually removing it
 - 4. bool isEmpty()

5. void clear()

III. SLL-backed stack

- A. When the stack is empty, the SLL's head is null
- B. When you push, you add to the front → push 1,3,3,2
 - 1. head → [2] → [3] → [3] → [1] → null
- C. When you pop, you remove from the front → pop 2,3,3,1
- D. All stack operations deal with the head (to clear the stack → set head to null)

IV. Array-backed stack

- A. When the stack is empty, the array size is 0
- B. When you push, add first element to index 0, where do we put the next element?
 - 1. We could add to the front, but this is $O(n)$
 - 2. Instead, we will add and remove from the back (at index = size)
 - a) It is important to keep track of size and capacity (resize)
- C. The "top" of the stack is at index size - 1
- D. When you pop, you'll remove from index size - 1
 - 1. Option 1: decrement size and then remove from index size.
 - 2. Option 2: remove from index size - 1 and then decrement size
- E. Clearing the stack
 - 1. Option 1: reset size to 0 and just overwrite old data ($O(1)$)
 - 2. Option 2: reset size to 0 and delete everything in the array ($O(n)$)
 - 3. Option 3: reset size to 0 and reassign backing array to new array ($O(1)$)

Stacks	SLL	Array
push	$O(1)$ - head	$O(1)$ (amortized) - size
pop	$O(1)$ - head	$O(1)$ - size - 1
top	$O(1)$ - head	$O(1)$ - size - 1
isEmpty	$O(1)$ - head	$O(1)$ - size
size	$O(1)$	$O(1)$
clear	$O(1)$ - head	Depends on implementation
resize	$O(1)$ - just add a new node	$O(n)$

V. DLL- backed

- A. Just like SLL-backed but you can add/remove from the head or tail (make sure whichever end you add to you also remove from)