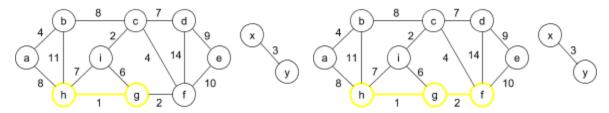
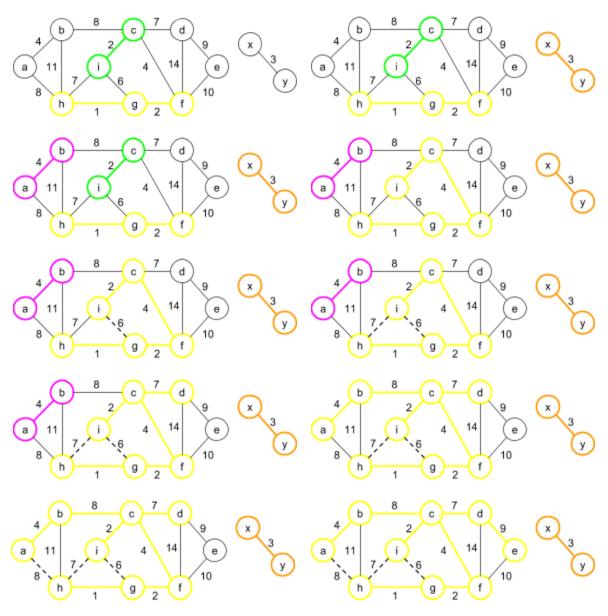
11/19/18

Topics

- I. Kruskal's MST Algorithm
 - A. Minimum Spanning Tree (MST)
 - 1. Spanning trees are acyclic, undirected, and connected
 - a) Minimum spanning trees also minimize the total weight of the edges in the spanning tree
 - 2. MSTs of graphs are not necessarily unique, especially when some edges have the same weight
 - 3. For a graph with v vertices, the MST will be composed of (v-1) undirected edges, or 2(v-1) directed edges (where each undirected edge is represented by two directed edges)
 - B. Requirements
 - 1. Priority Queue holds all the edges in the edge list
 - 2. Disjoint Set hold "clusters" of vertices to keep track of which vertices have already been connected in the MST
 - a) find(v) finds the "root" of the subset vertex v is in
 - b) union(v, u) combines the clusters containing v and u
 - 3. MST Set holds the edges in the MST we're creating
 - C. Algorithm
 - 1. Initialize Priority Queue (PQ) with all the edges from the graph
 - 2. Initialize Disjoint Set (DS) with all the vertices from the graph
 - 3. Initialize empty MST Edge Set (MST)
 - 4. While PQ is not empty and MST size is not valid yet
 - a) $e \leftarrow PQ.remove()$
 - b) if find(e.u) does not equal find(e.v)
 - (1) union(e.u, e.v)
 - (2) add e to the MST (if the graph is undirected, add the opposite edge as well: edge(e.v, e.u))
 - 5. Check if the MST is valid
 - a) If the size is valid \rightarrow return the list
 - b) If the size is less than what it should be \rightarrow throw it out
 - D. Example: each color represents a different cluster in the disjoint set





E. Valid MST? No, there are only 9 edges in the MST when there should be 10.

Thanksgiving Break - 11/21/18 Thanksgiving Break - 11/23/18