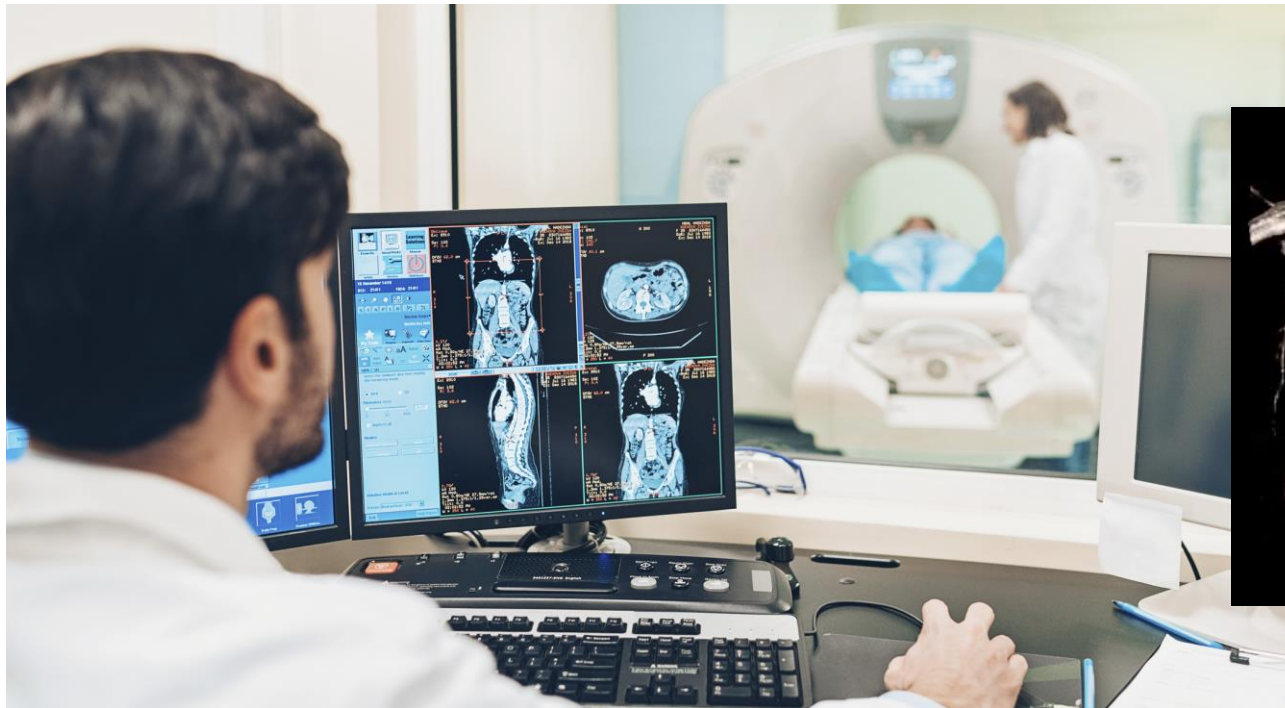


MRI simulation

Carlos Castillo Passi

What is MRI



How does MRI work?

GRADE 2
Playing Time 4:05

CONDUCTOR

CONCERT PIECE FOR STRINGS

by Elliot A. Del Borgo

With vigor $\text{♩} = 132$

1st VIOLIN

2nd VIOLIN

VIOLA (3rd Violin
part included)

CELLO

BASS



The musical score is for a string ensemble and is written in 4/4 time. It begins with a dynamic marking of *f* (forte). The notation for each instrument is as follows:

- 1st VIOLIN:** Treble clef, starting with a quarter note G4, followed by eighth notes A4, B4, C5, and a half note D5.
- 2nd VIOLIN:** Treble clef, starting with a quarter note F#4, followed by eighth notes G4, A4, B4, C5, and a half note D5.
- VIOLA (3rd Violin part included):** Alto clef, starting with a quarter note E4, followed by eighth notes F4, G4, A4, and a half note B4.
- CELLO:** Bass clef, starting with a quarter note E3, followed by eighth notes F3, G3, A3, and a half note B3.
- BASS:** Bass clef, starting with a quarter note D3, followed by eighth notes E3, F3, G3, and a half note A3.

The score shows the first four measures of the piece, with a circled page number (9) at the bottom right.

How does MRI work?

Sequence

GRADE 2
Playing Time 4:05

CONCERT PIECE FOR STRINGS by Elliot A. Del Borgo

CONDUCTOR

With vigor $\text{♩} = 132$

1st VIOLIN

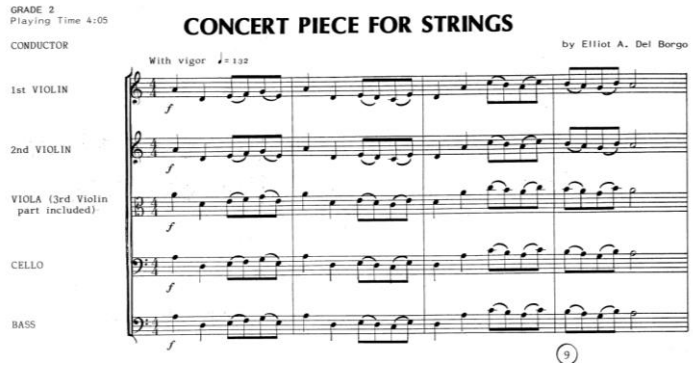
2nd VIOLIN

VIOLA (3rd Violin part included)

CELLO

BASS

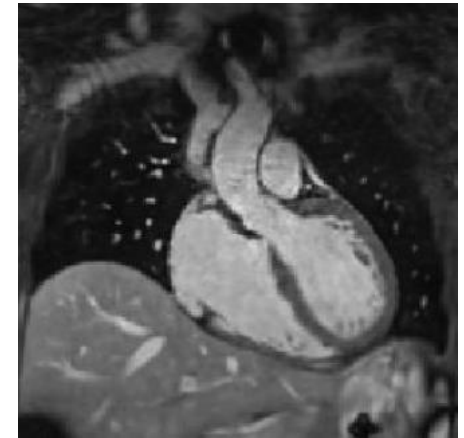
(9)



Scanner



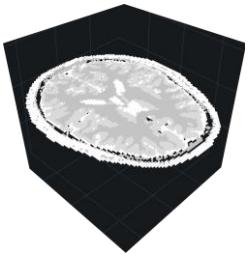
Image



Virtual MRI experiment

Phantom

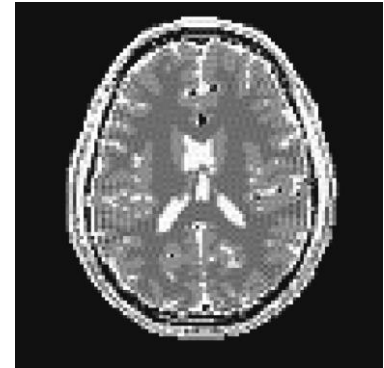
M_0, T_1, T_2, \dots



Scanner



Image



Sequence

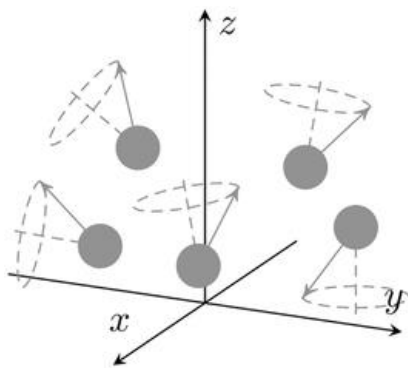
B



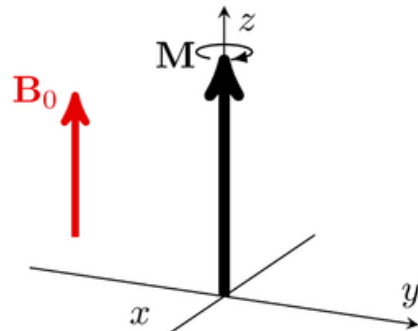
We have indirect measurements of the object

Bloch equation:

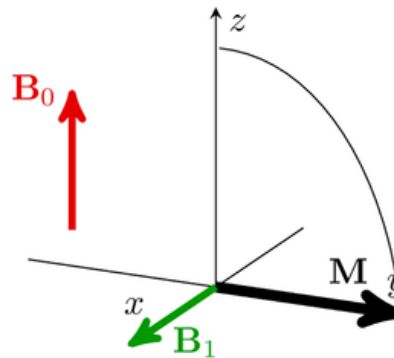
$$\frac{d\mathbf{M}}{dt} = \gamma \mathbf{M} \times \mathbf{B} + \frac{(M_0 - M_z)\hat{\mathbf{z}}}{T_1} - \frac{M_x\hat{\mathbf{x}} + M_y\hat{\mathbf{y}}}{T_2}$$



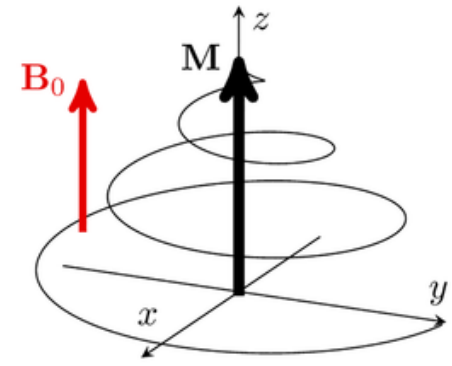
(a) Rest



(b) Equilibrium



(c) Excitation



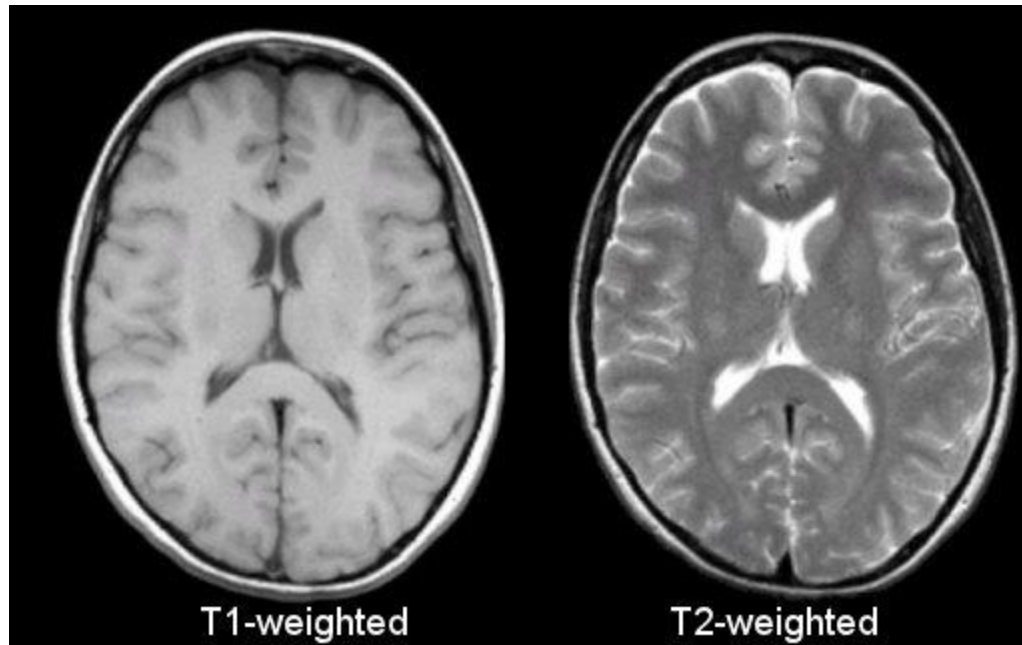
(d) Relaxation

Difference in magnetic prop. generate contrast

$$\frac{d\mathbf{M}}{dt} = \gamma \mathbf{M} \times \mathbf{B} + \frac{(M_0 - M_z)\hat{z}}{T_1} - \frac{M_x\hat{x} + M_y\hat{y}}{T_2}$$

Sequence #1

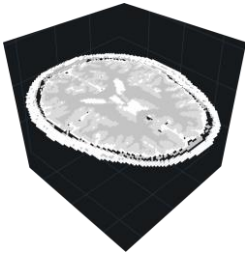
Sequence #2



MRI simulation

Phantom

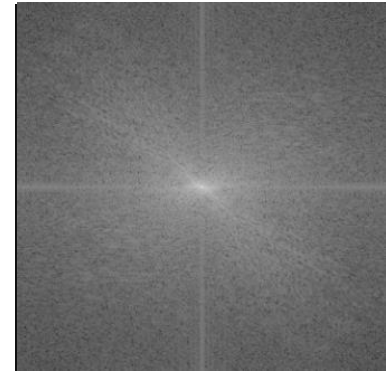
M_0, T_1, T_2, \dots



Scanner



Data

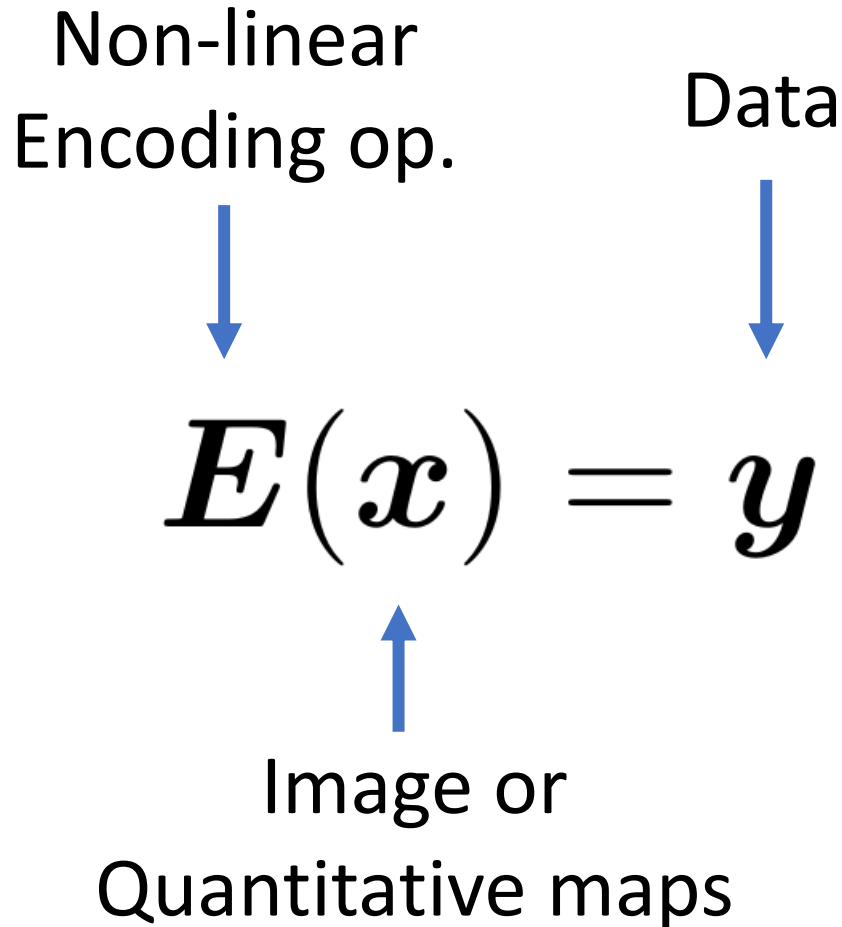


Sequence

B



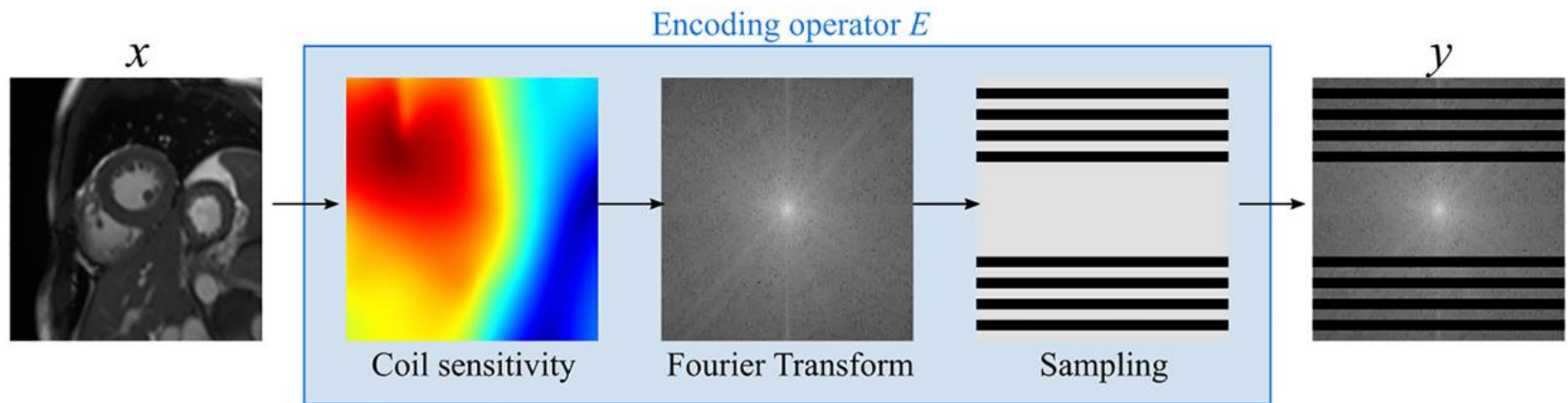
Simulation: Forward problem



Reconstruction: Inverse problem

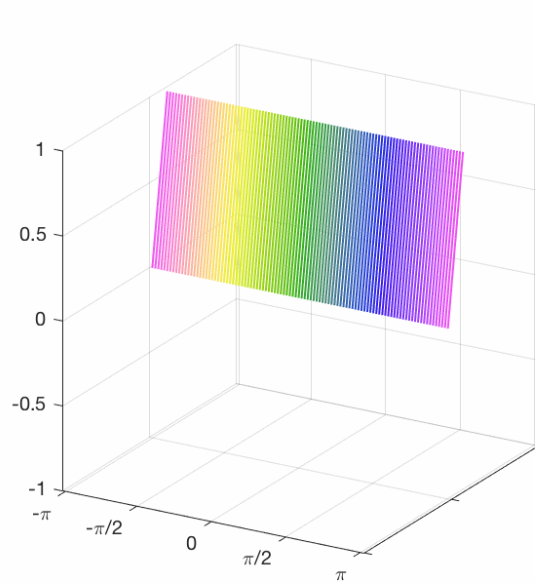
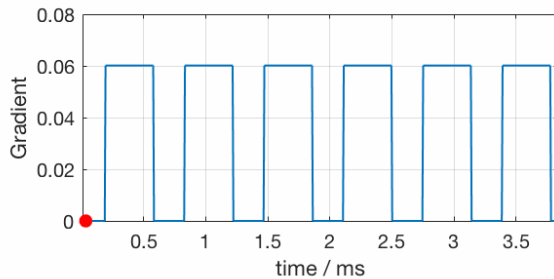
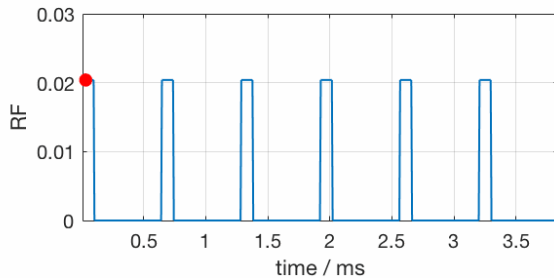
A **simplification** of the MRI system is used to enable **rapid reconstruction**

$$\mathbf{E}(x) \approx \mathbf{E} x \Rightarrow \min_x \frac{1}{2} \|\mathbf{E}x - \mathbf{y}\|_2^2 + \lambda R(x)$$

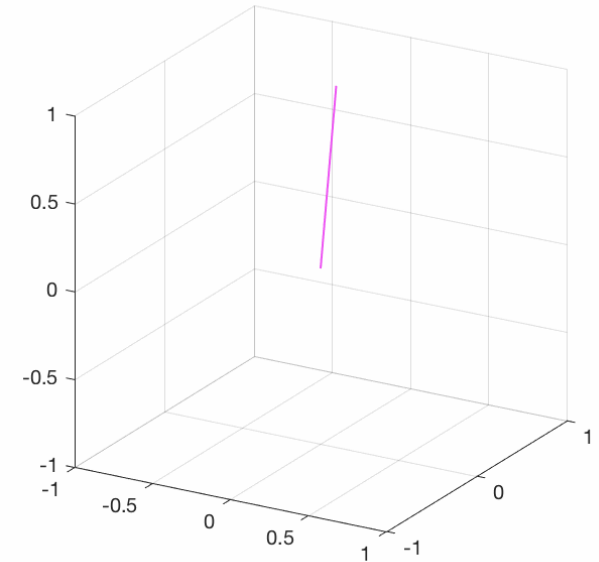


Simulation methods: Bloch

$$\frac{d\mathbf{M}}{dt} = \gamma \mathbf{M} \times \mathbf{B} + \frac{(M_0 - M_z)\hat{\mathbf{z}}}{T_1} - \frac{M_x\hat{\mathbf{x}} + M_y\hat{\mathbf{y}}}{T_2}$$



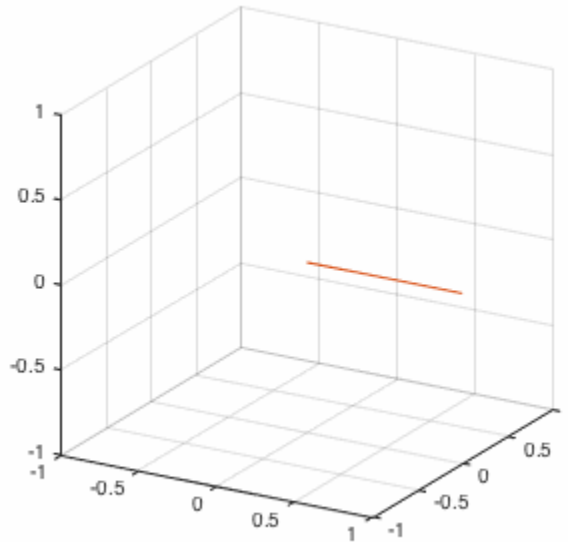
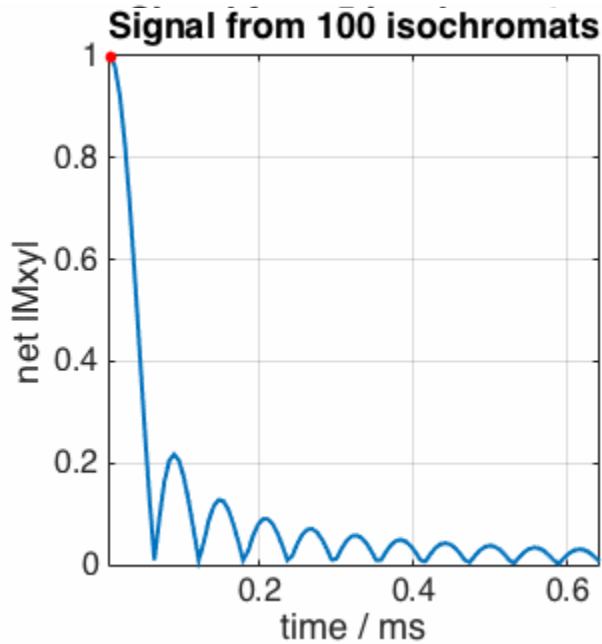
Spins along the x-axis



Spins on top of each other

Isochromat: Spins that precess at different frequencies

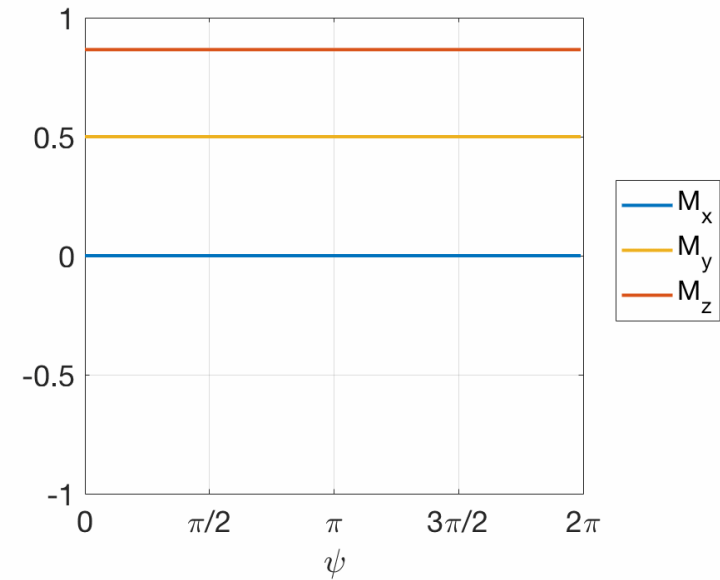
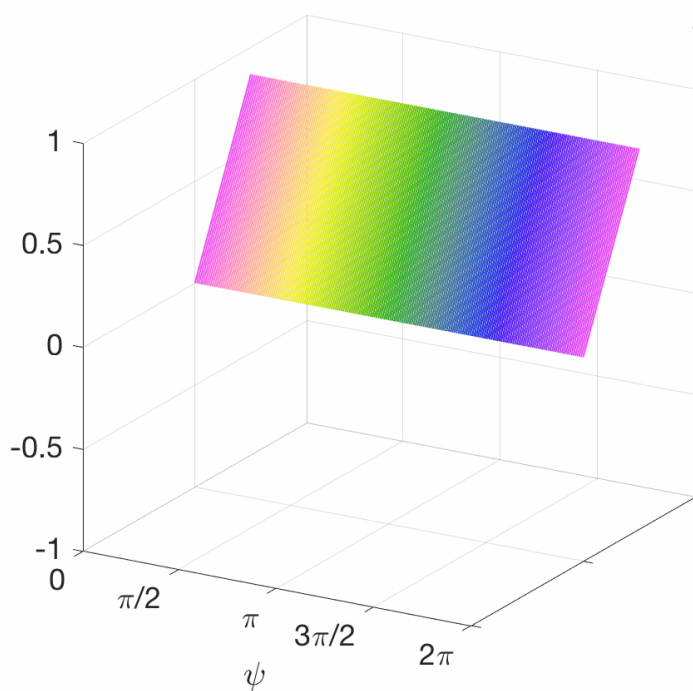
- Effect of a big gradient on a spin ensemble with a low number of isochromats



Not realistic spurious echoes

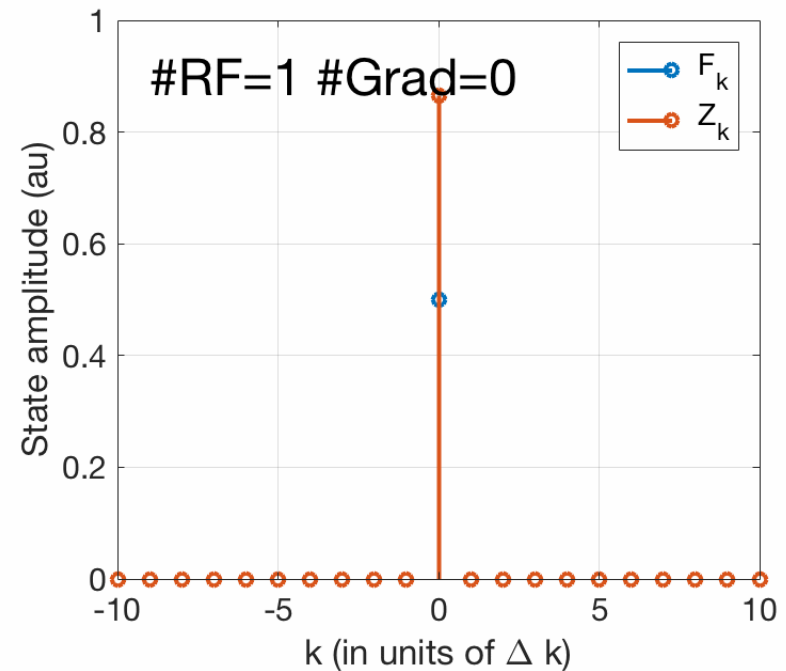
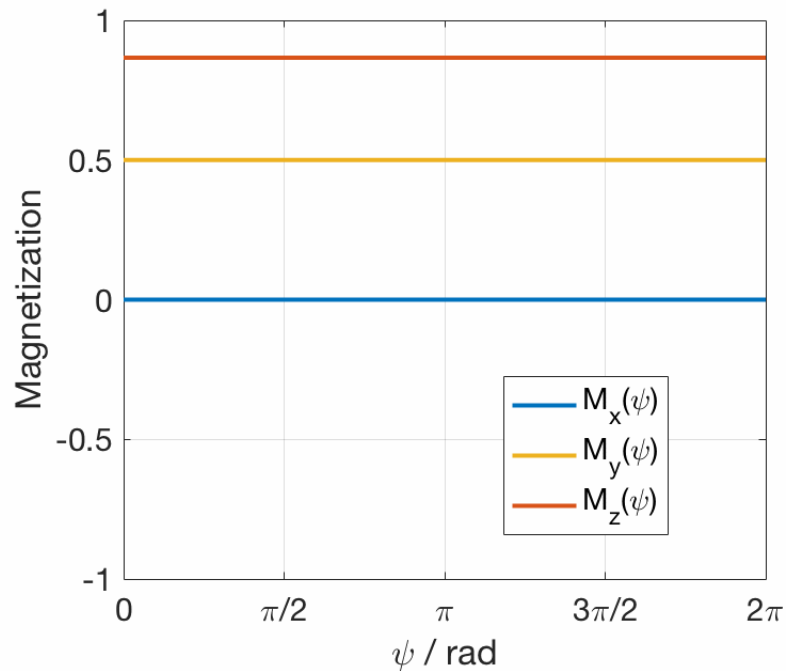
Simulation method: EPG

- Let's look at the previous example in another way



Simulation method: EPG

- Let's look at the previous example in another way



Instead of 100 isochromats
we can use just a few Fourier components!

Operator splitting method

- How do you deal with **relaxation**?

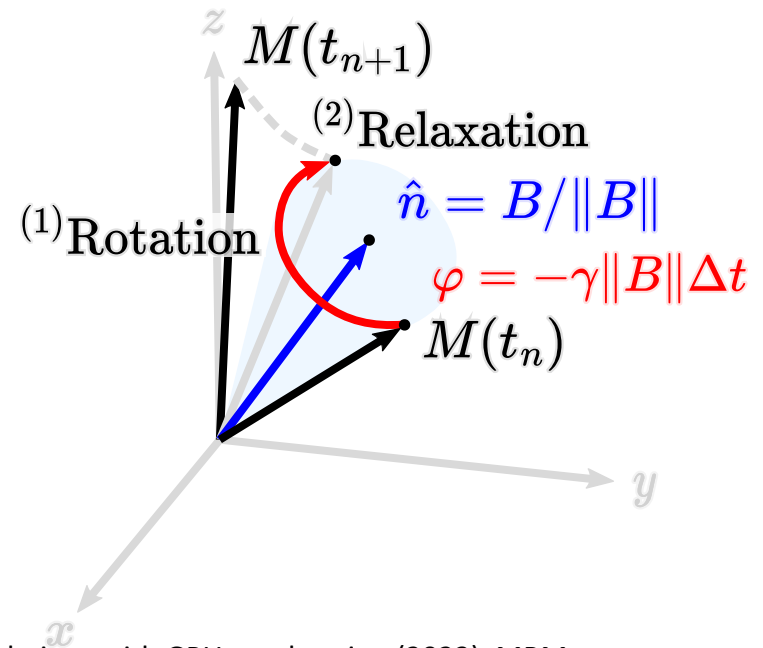
$$\frac{d\mathbf{M}}{dt} = \underbrace{\gamma \mathbf{M} \times \mathbf{B}}_{\text{Precession}} + \underbrace{\frac{(M_0 - M_z)\hat{\mathbf{z}}}{T_1}}_{\text{Relaxation}} - \frac{M_x \hat{\mathbf{x}} + M_y \hat{\mathbf{y}}}{T_2}$$

No general solution

$$\frac{d\mathbf{M}^{(1)}}{dt} = \begin{bmatrix} 0 & \gamma B_z & -\gamma B_y \\ -\gamma B_z & 0 & \gamma B_x \\ \gamma B_y & -\gamma B_x & 0 \end{bmatrix} \mathbf{M}^{(1)}, \quad (3)$$

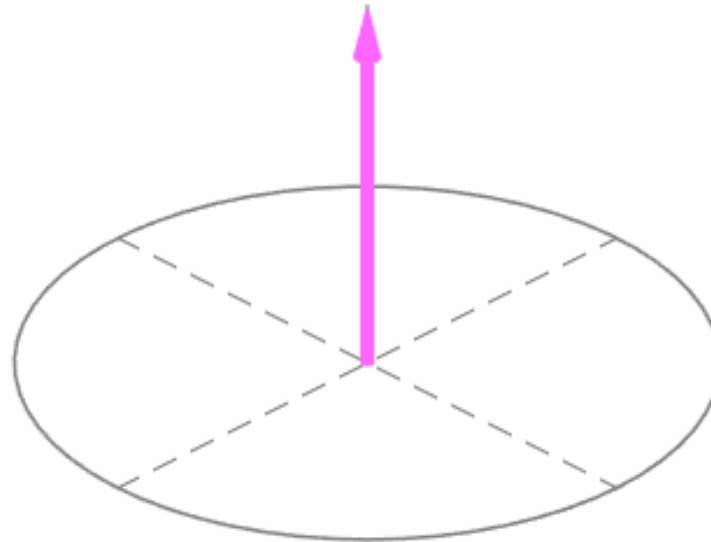
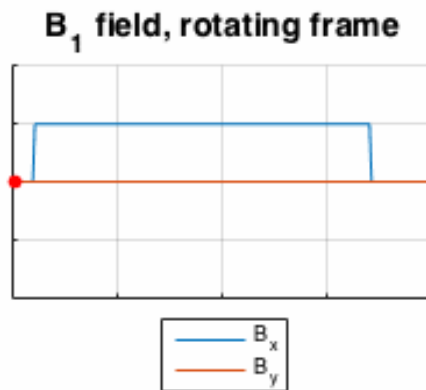
with initial condition $\mathbf{M}^{(1)}(t_n) = \mathbf{M}(t_n)$, and the relaxation is described by

$$\frac{d\mathbf{M}^{(2)}}{dt} = \begin{bmatrix} -\frac{1}{T_2} & 0 & 0 \\ 0 & -\frac{1}{T_2} & 0 \\ 0 & 0 & -\frac{1}{T_1} \end{bmatrix} \mathbf{M}^{(2)} + \begin{bmatrix} 0 \\ 0 \\ \frac{M_0}{T_1} \end{bmatrix}, \quad (4)$$



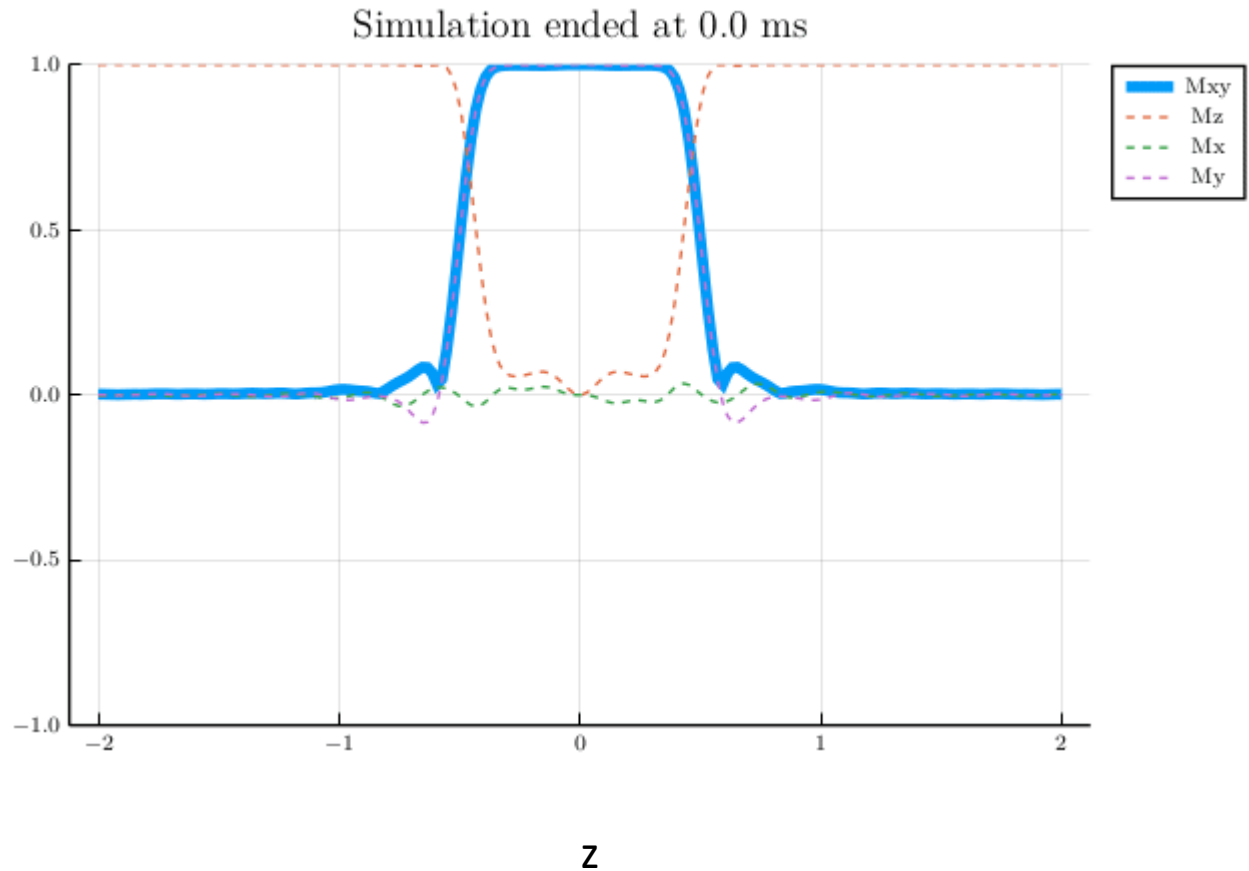
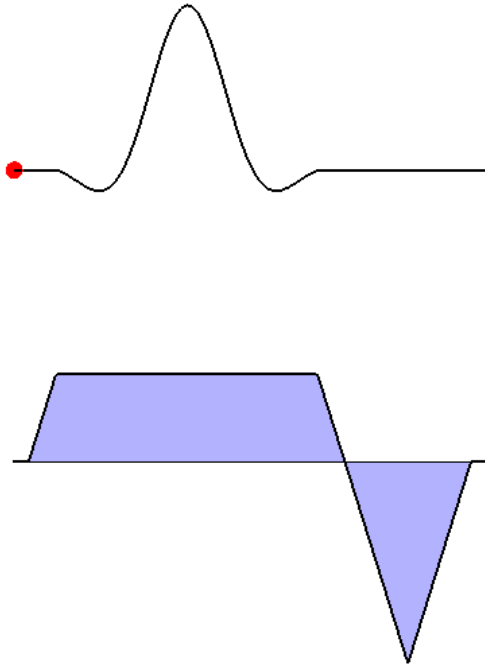
Simulation examples

- Slice selectivity



Simulation examples

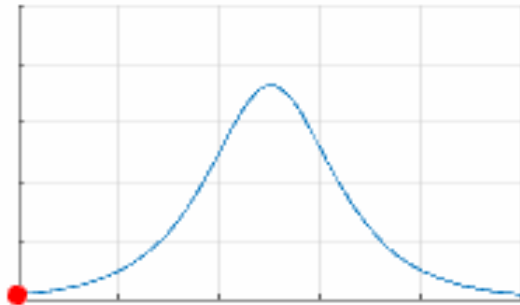
- Slice selectivity



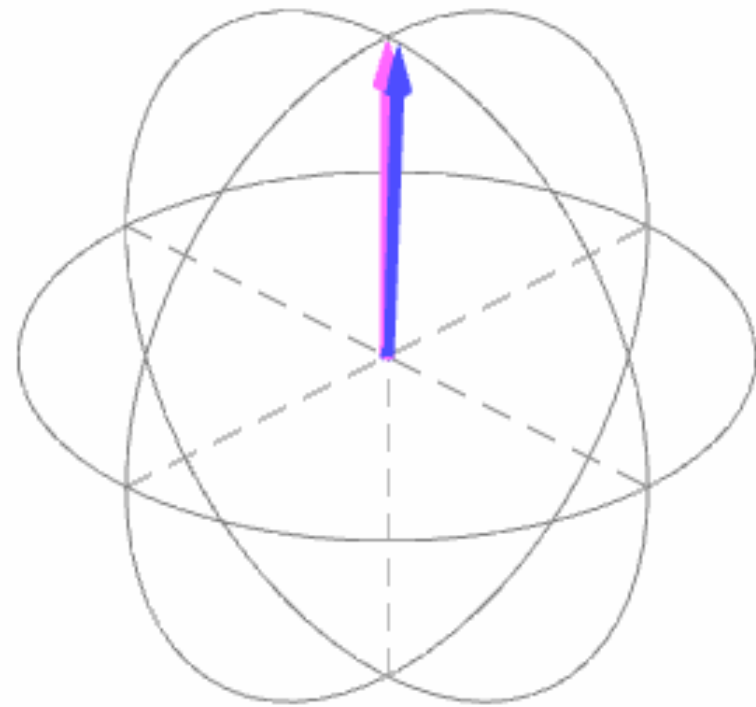
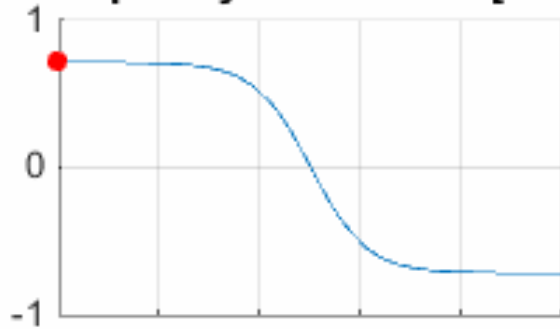
Simulation examples

- Adiabatic RF pulses

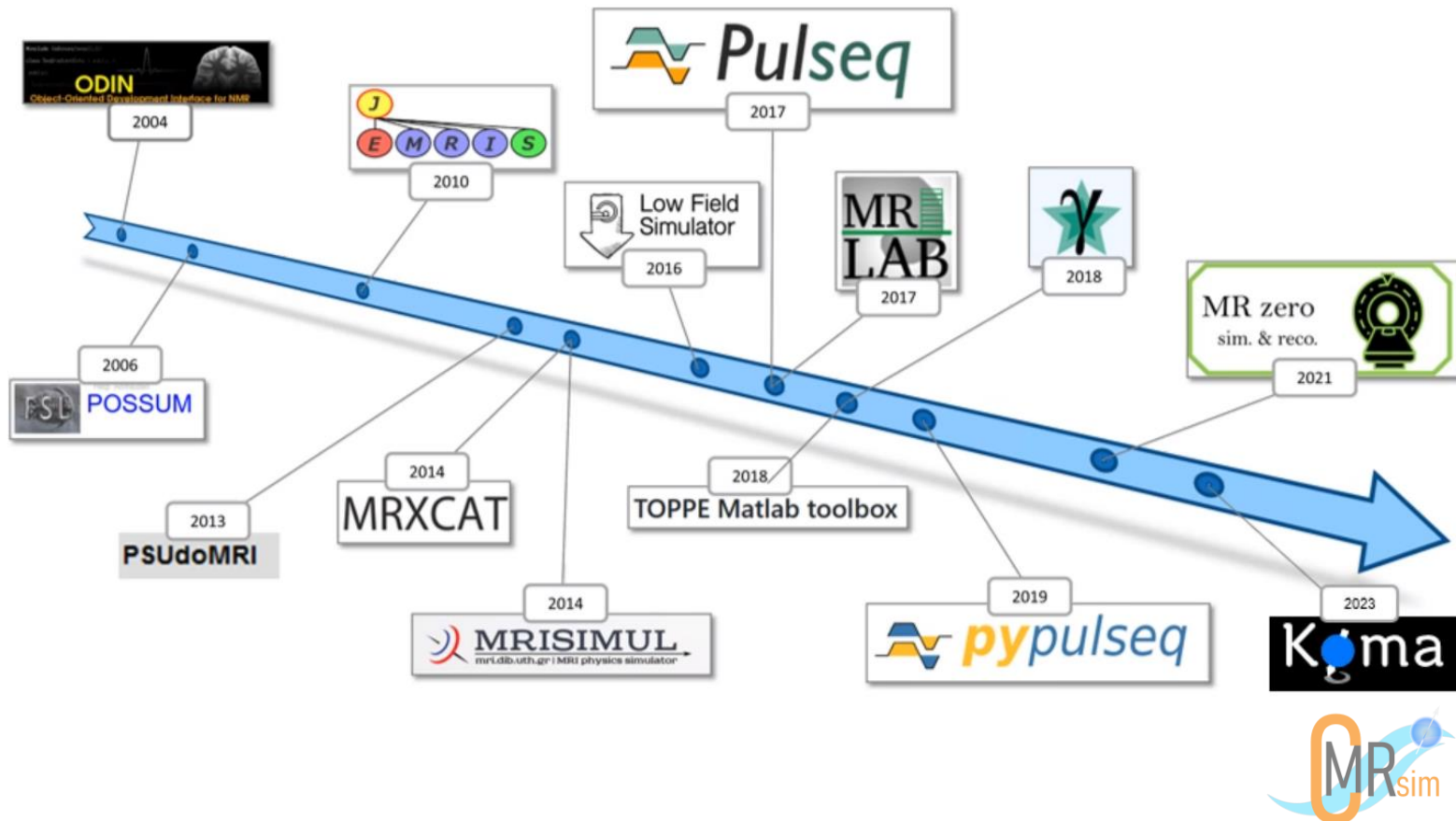
Pulse Amplitude



Frequency Modulation [kHz]

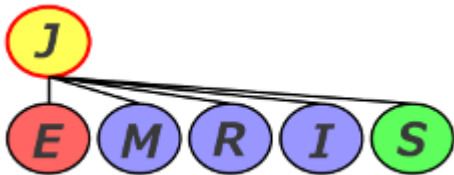


MRI simulation landscape

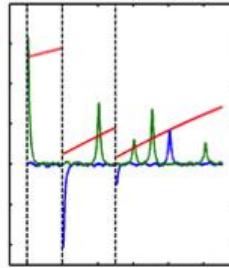


JEMRIS (2010)

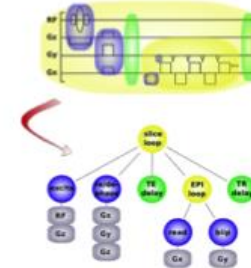
- MATLAB GUI
- CPU Multithreading
- C++



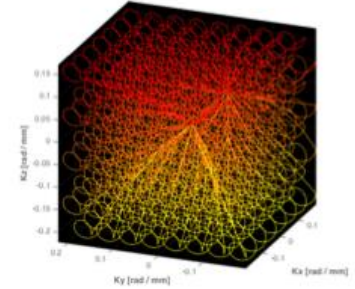
3-Pulse echo simulation



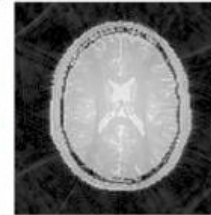
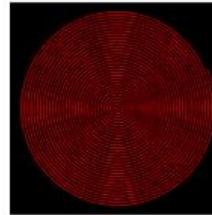
Sequence Tree Concept



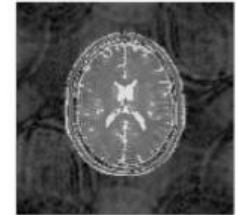
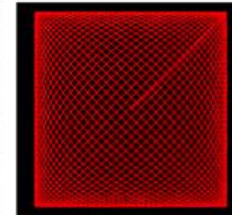
Wave-CAIPI k-space



Spiral Trajectory Acquisition



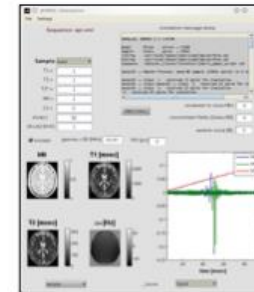
Lissajous Trajectory Acquisition



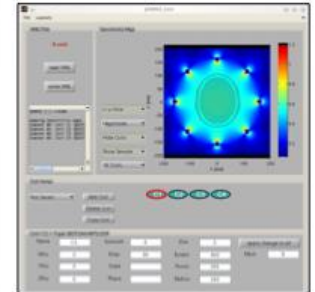
Sequence GUI



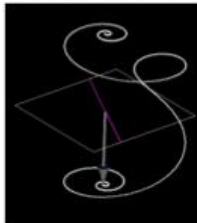
Simulation GUI



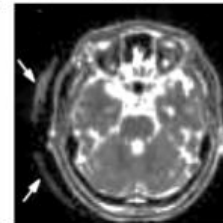
Coil Layout GUI



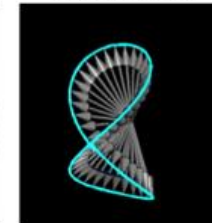
Adiabatic Inversion



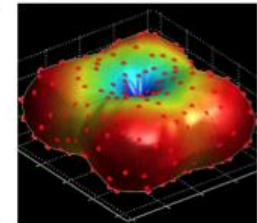
Fat shift



Eight-Ball Echo

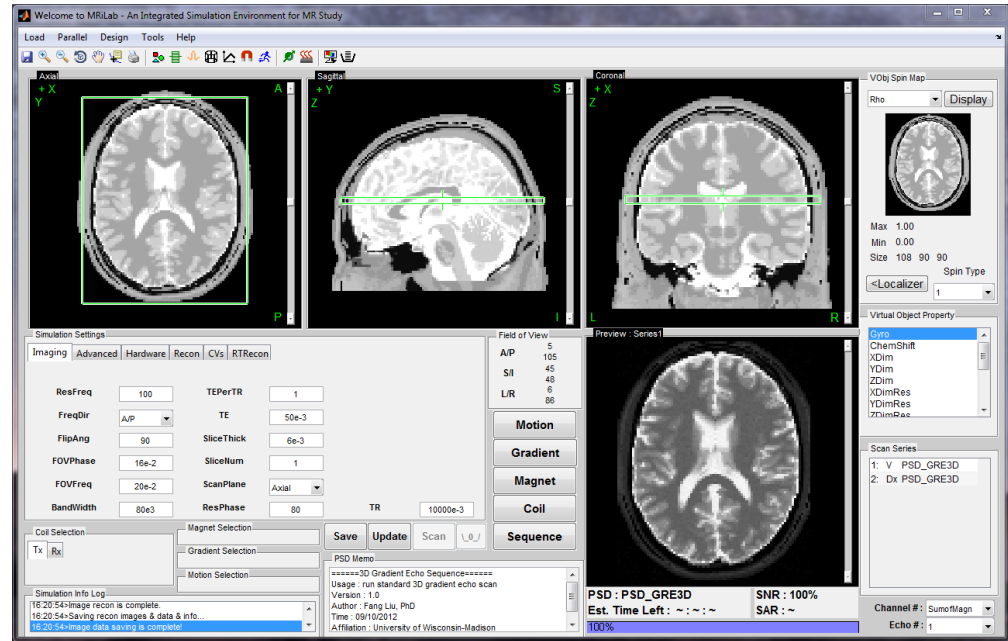


Diffusion Signal Profile



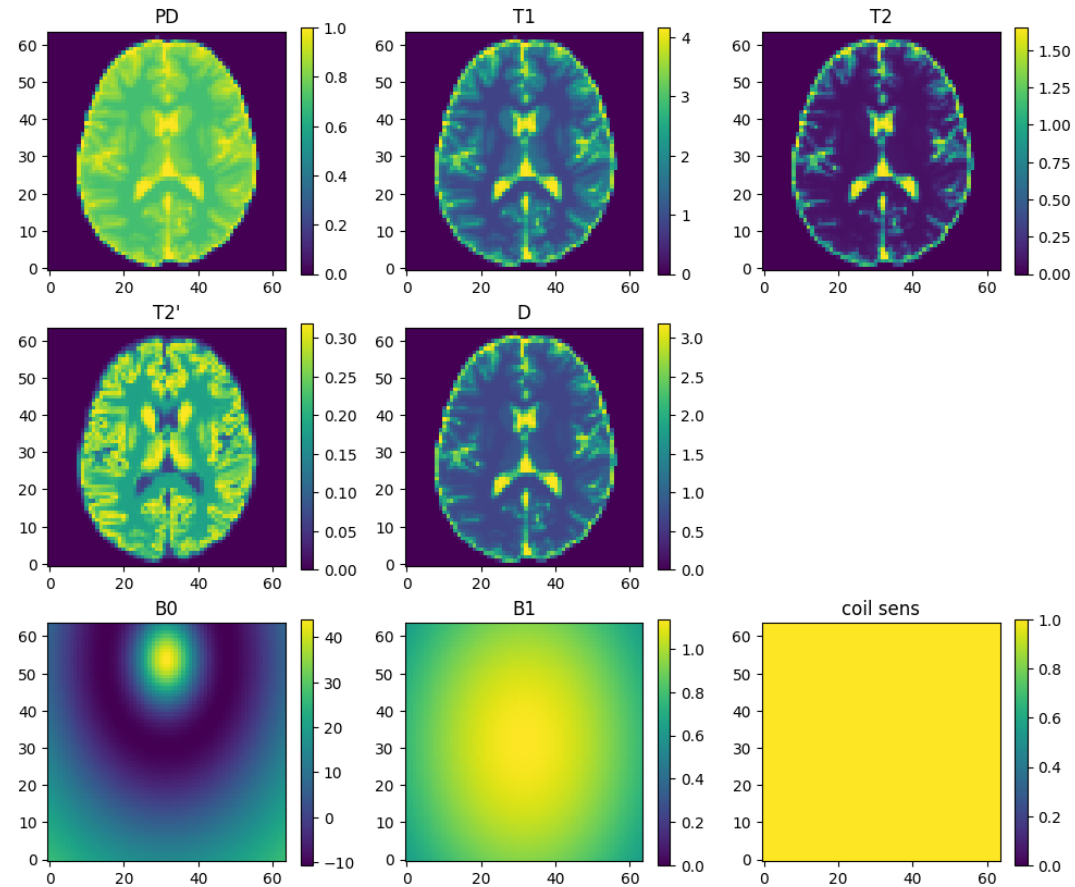
MRiLab (2017)

- MATLAB GUI
- CPU Multithreading
- GPU acceleration
- C++ and CUDA



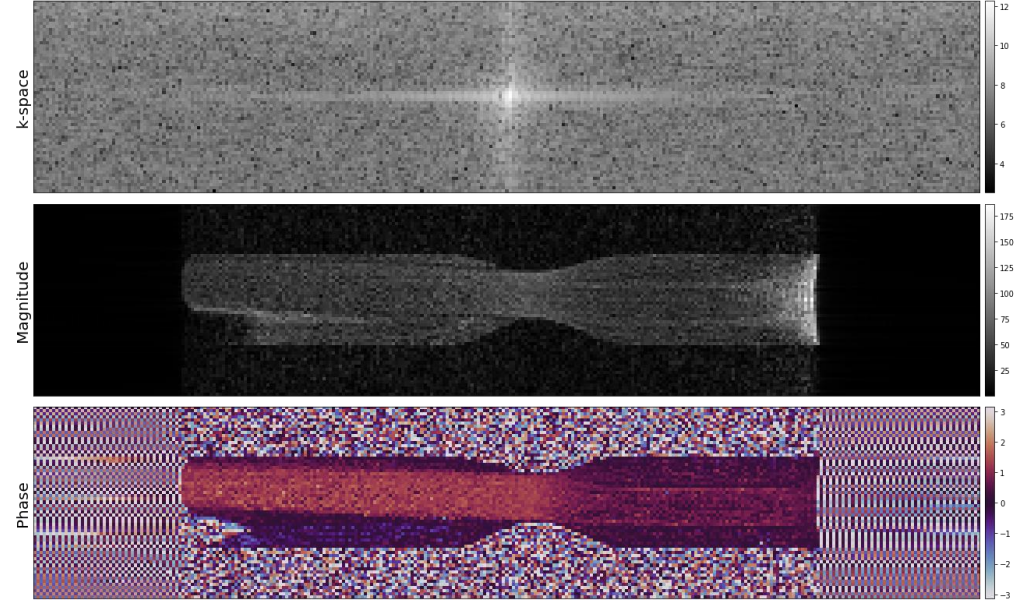
MRZero (2021)

- No GUI
- GPU acceleration
- Pure Python
- Pulseseq compatible
- PyTorch based



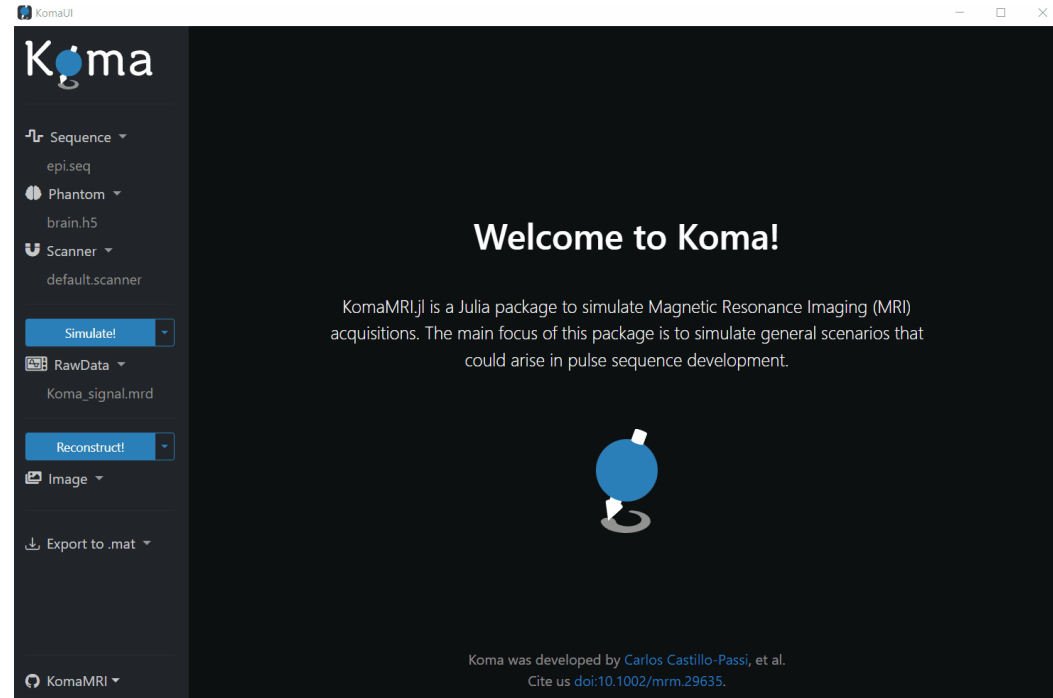
CMRsim (2023)

- No GUI
- GPU acceleration
- Pure Python
- TensorFlow2 based



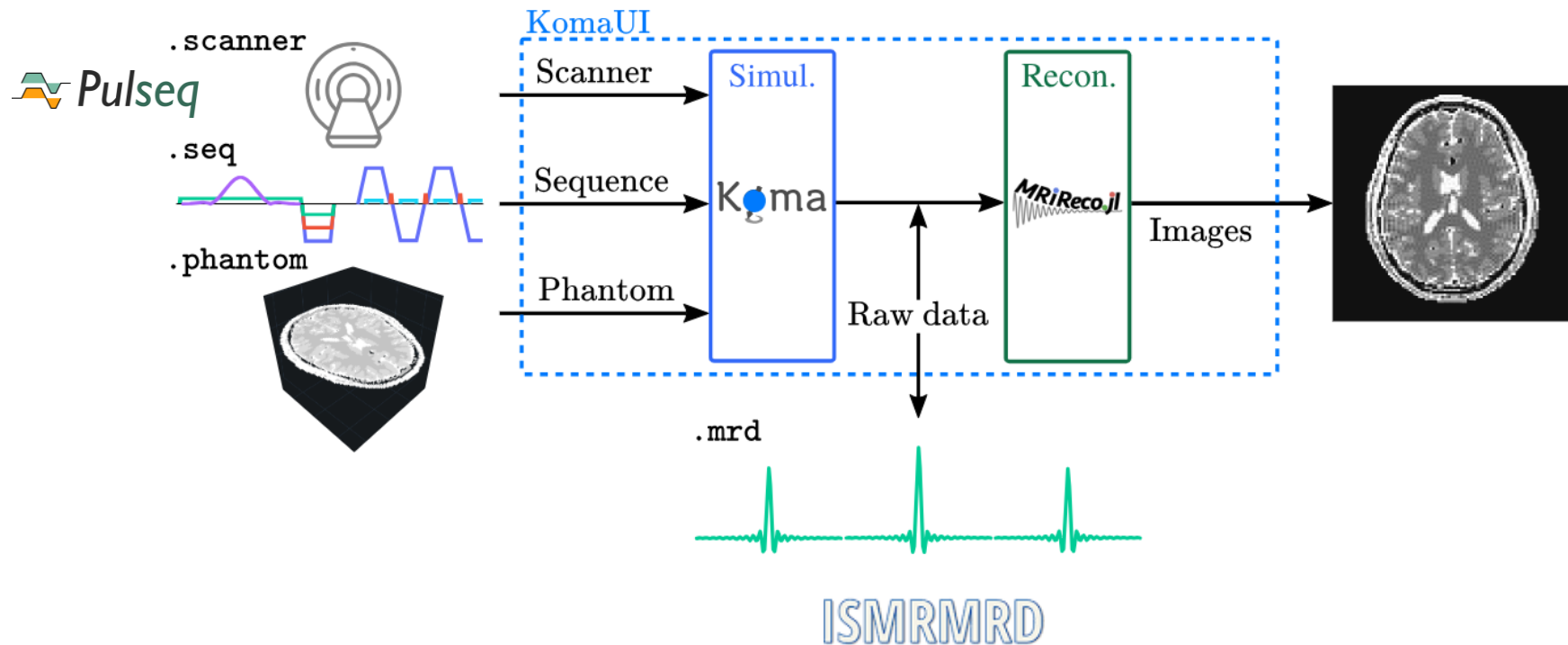
KomaMRI (2023)

- Web GUI
- CPU Multithreading
- GPU acceleration
- Pure Julia
- Pulseq compatible

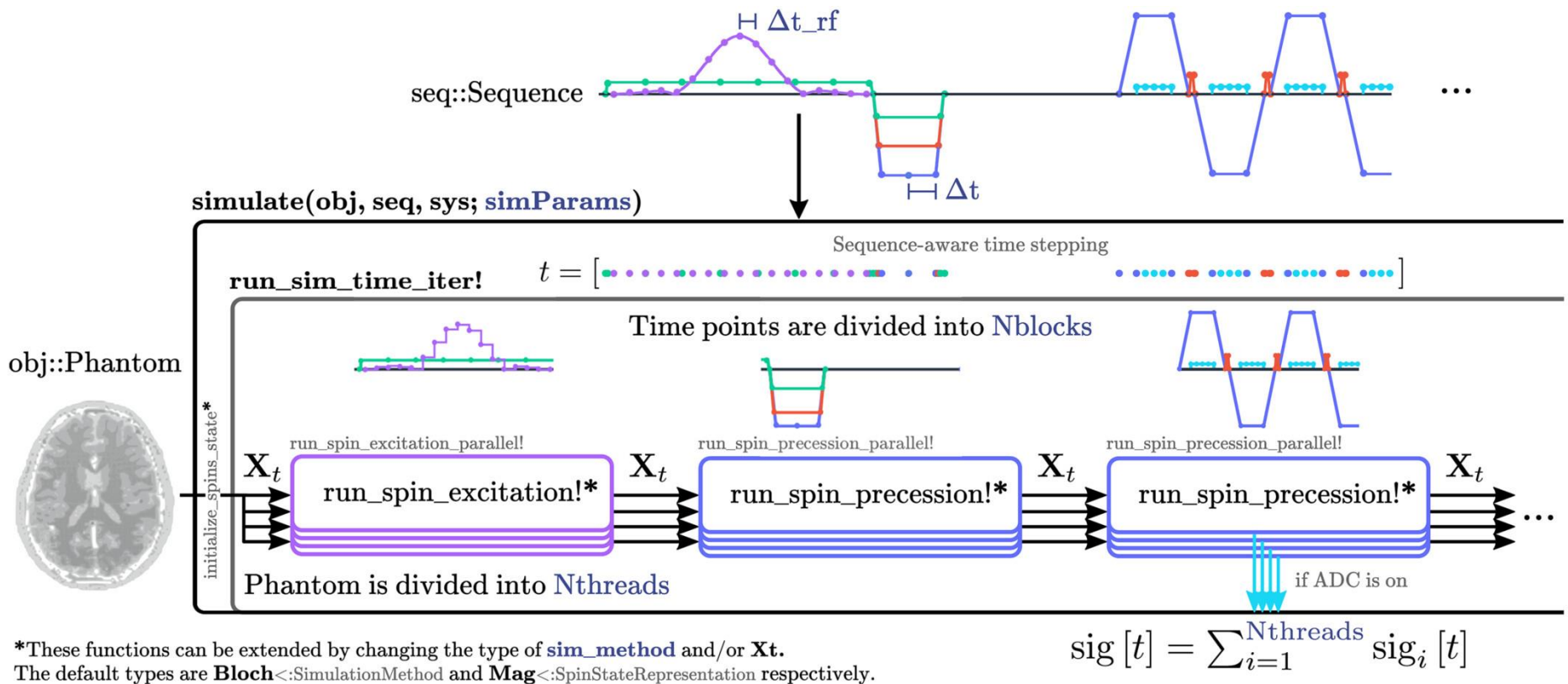


Koma

KomaMRI.jl

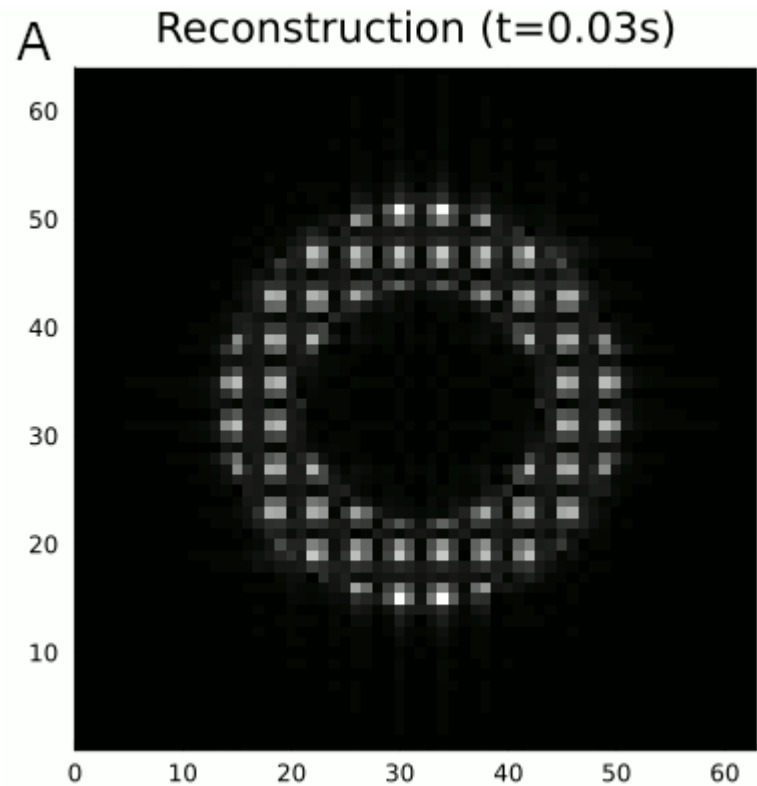
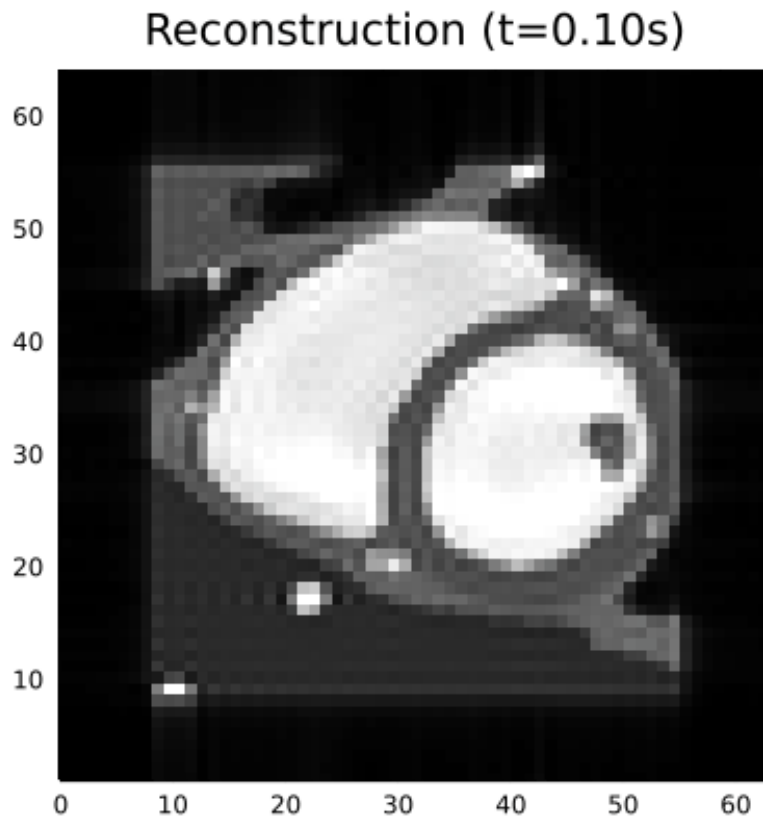


Parallelization and extensibility



A KomaMRI Phantom Extension for Integrated Dynamic Imaging

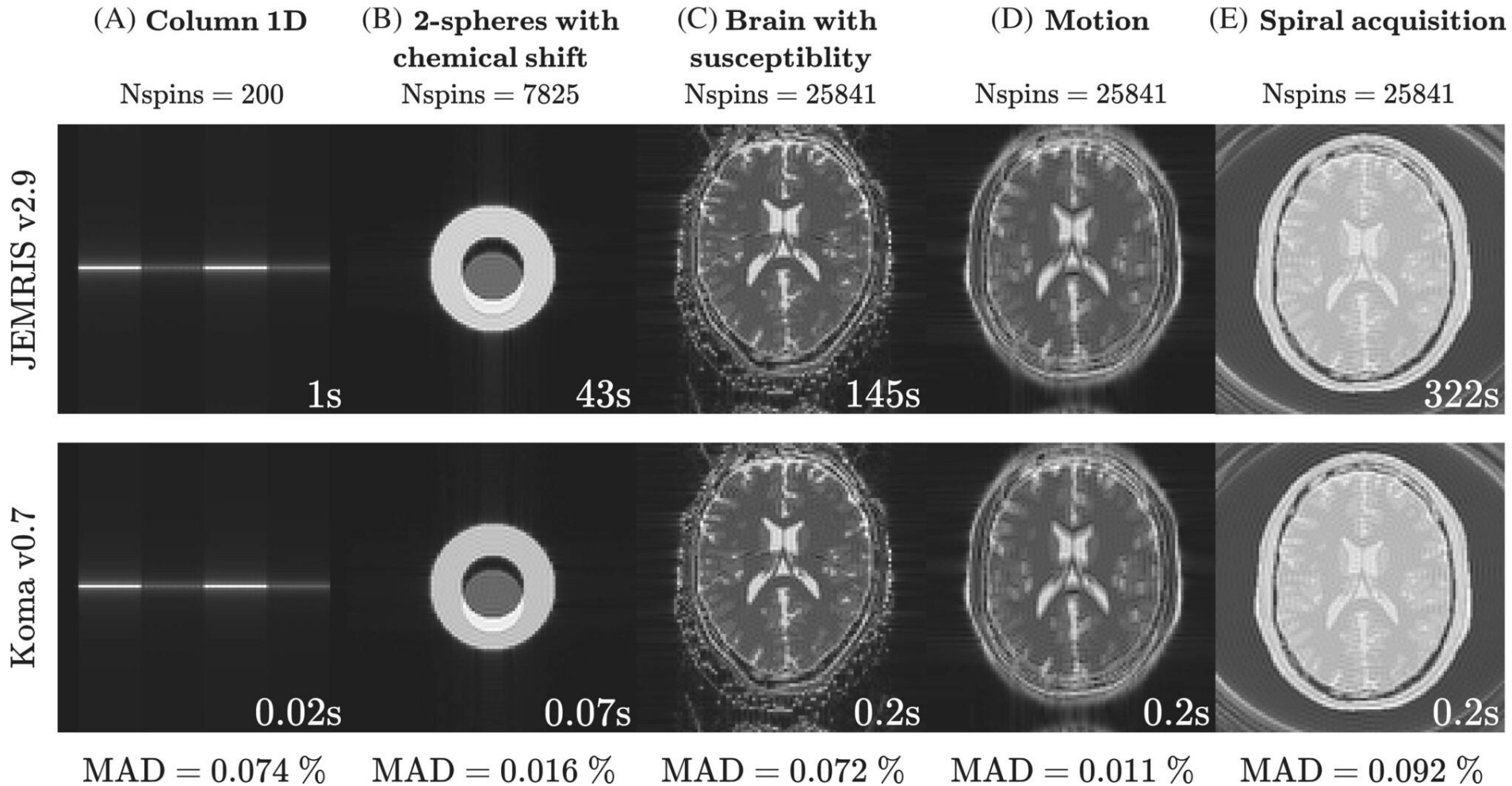
Pablo Villacorta Aylagas, Carlos Castillo-Passi, Rosa María Menchón-Lara, Pablo Irarrazaval, Carlos Alberola-López



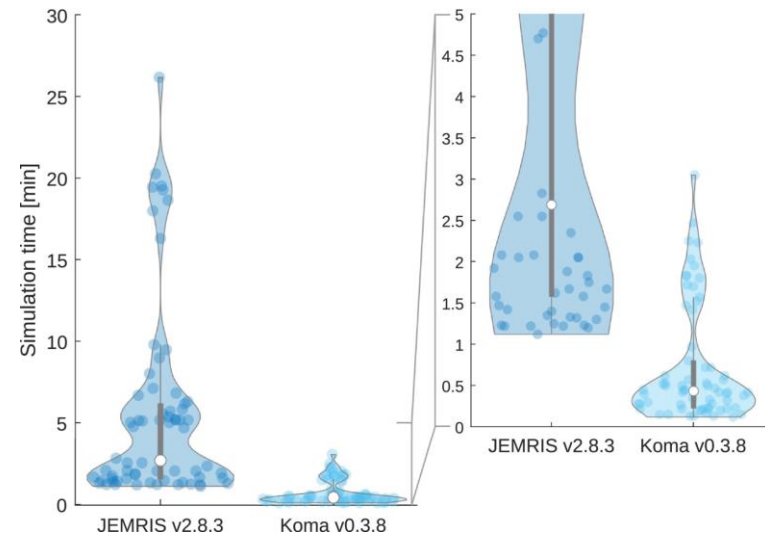
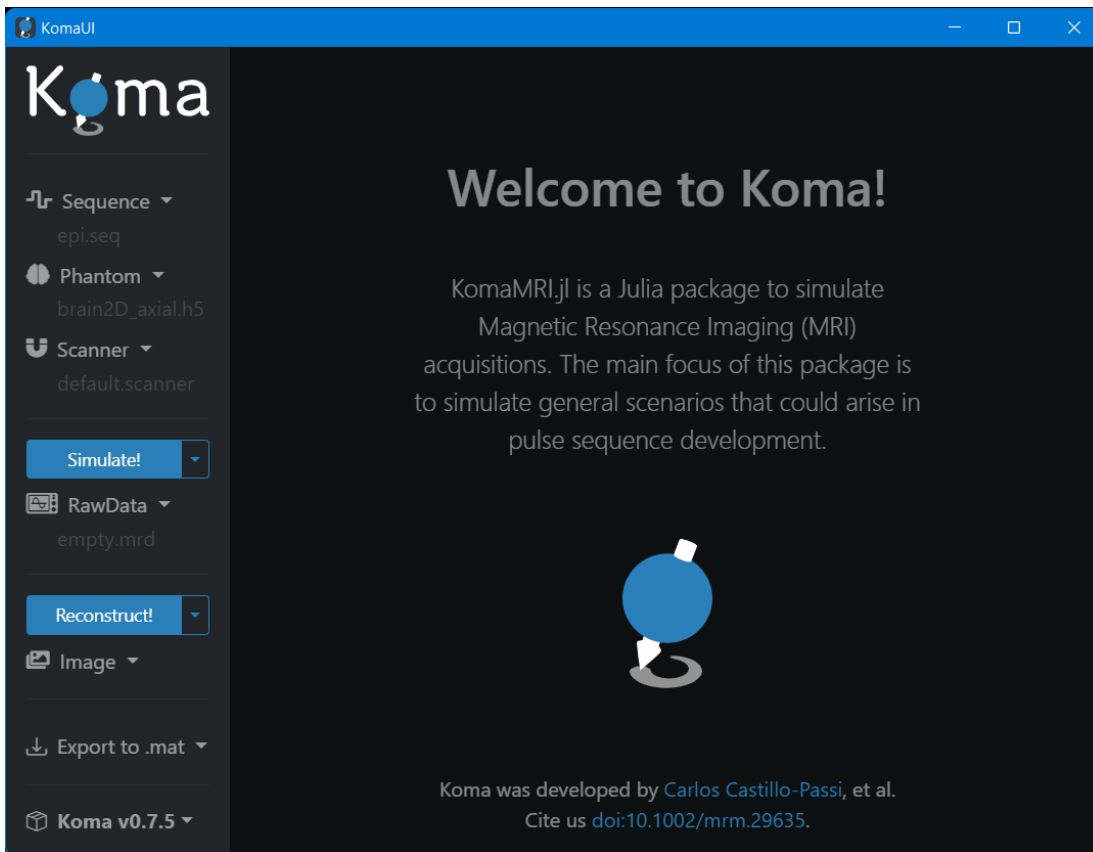
Speed: Comparing simulation speed

Name	CPU	GPU	
	Intel i7-1165G7	GTX 1650 Ti	RTX 2080 Ti
JEMRIS	$\approx 7 \text{ min}$	-	-
MRiLab	$1.56 \text{ s} \pm 0.07 \text{ s}$	$0.84 \text{ s} \pm 0.02 \text{ s}$	$0.91 \text{ s} \pm 0.02 \text{ s}$
Koma	$1.82 \text{ s} \pm 0.17 \text{ s}$	$0.32 \text{ s} \pm 0.02 \text{ s}$	$0.15 \text{ s} \pm 0.01 \text{ s}$

Acc: Comparing simulation accuracy with JEMRIS



Easy-to-use: Students' experience (beta testers)



User experience

Students reported no problem installing Julia (mean 4.7/5), Koma (mean 4.2/5), JEMRIS (mean 3.8/5), and MRILab (mean 4.3/5). Regarding the time taken to install each simulator, most of the students were able to install Koma (mean 13.2 min), JEMRIS (mean 33.8 min), and MRILab (mean 16.9 min) in less than 40 min.

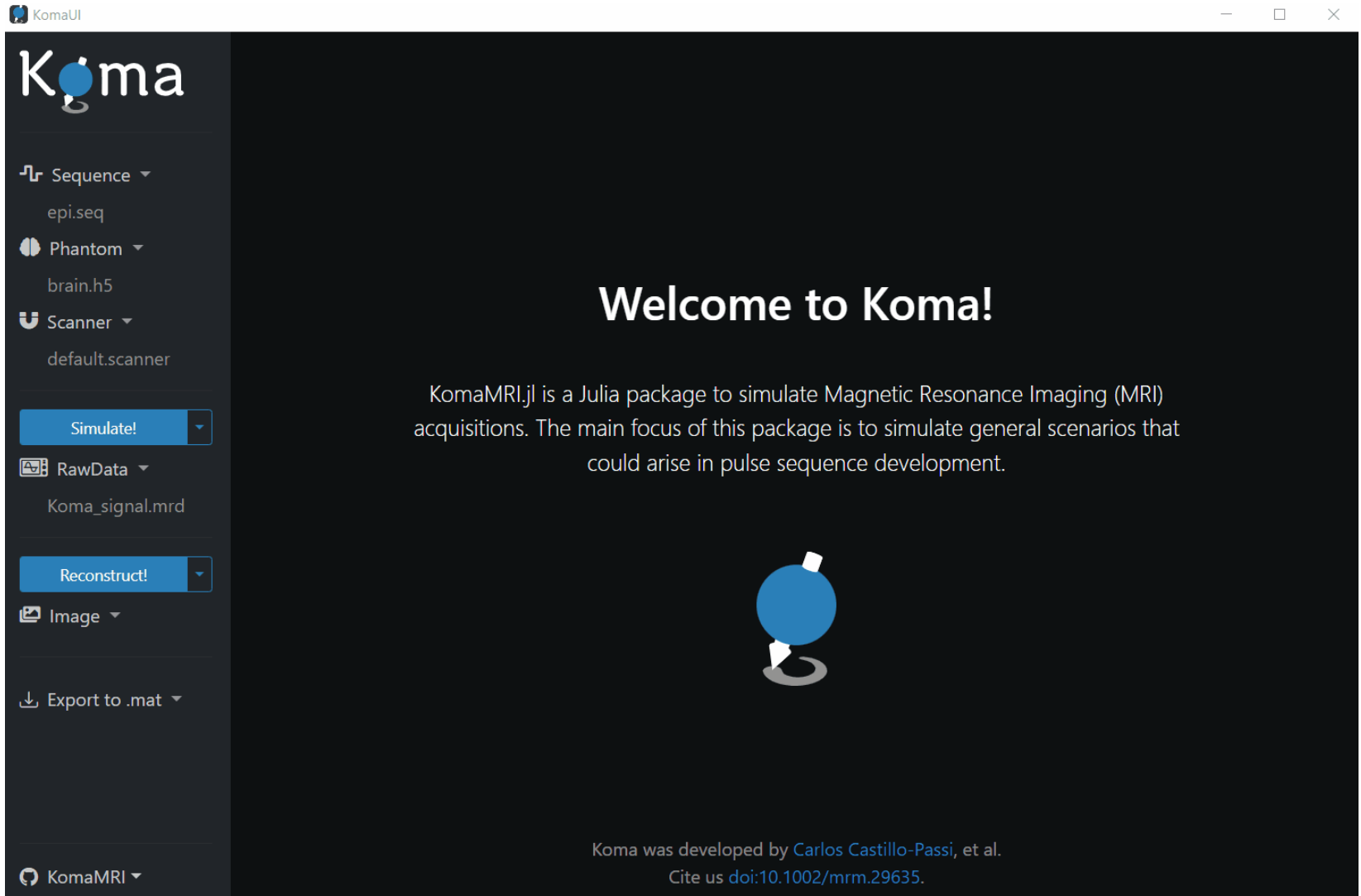
Their first simulation took them more time in JEMRIS (mean 19 min) and MRILab (mean 13.9 min) than in Koma (mean 5.7 min). 31% of the students could not simulate on MRILab (six students using Mac OS), so we decided to only use Koma and JEMRIS for the rest of the activities.

Blink.jl + PlotlyJS.jl powered



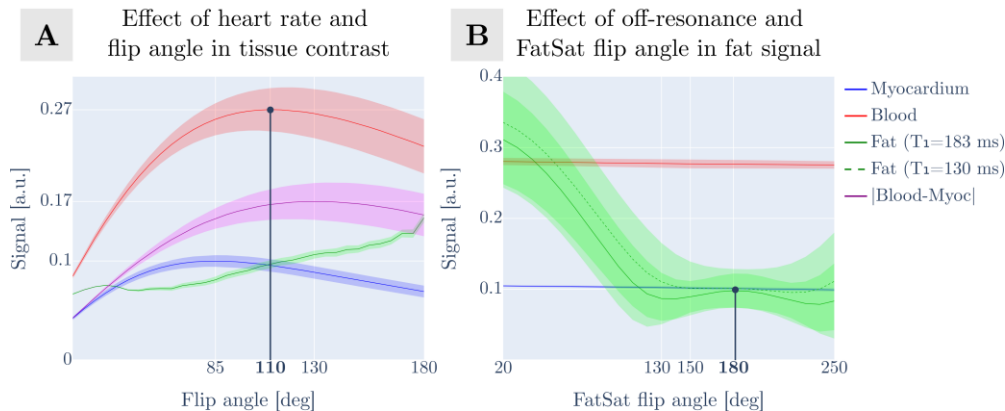
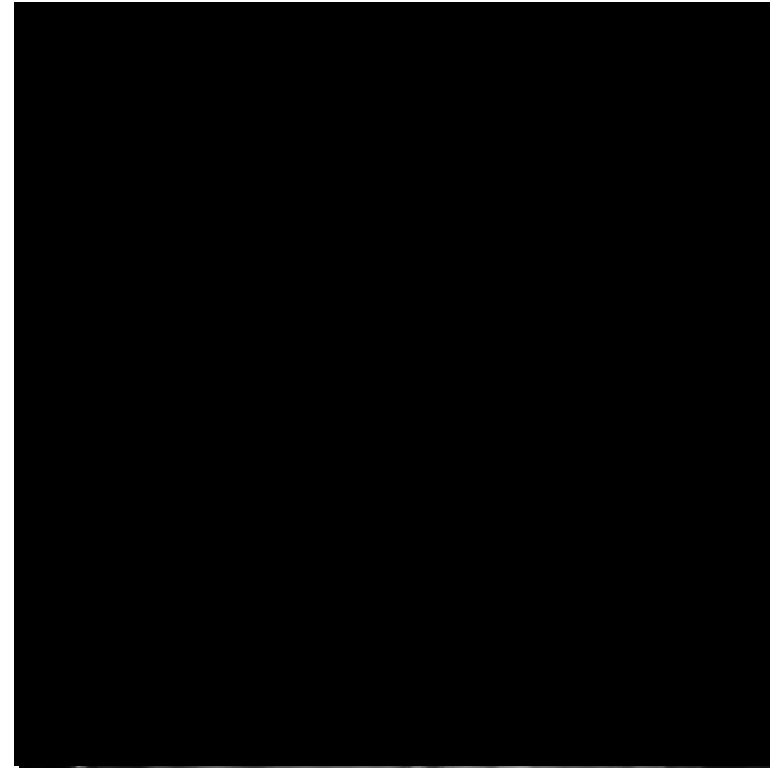
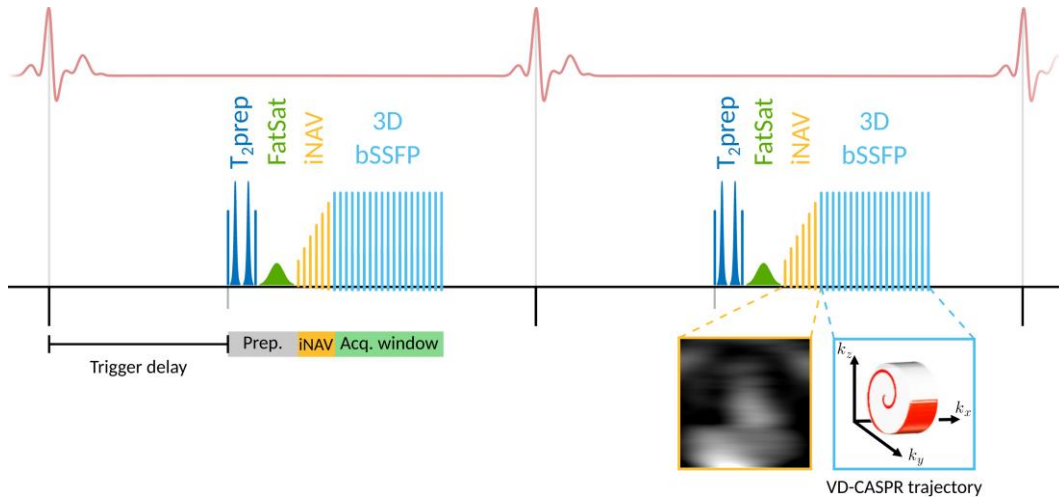
You can export your sequence to an interactive HTML! :)

Using KomaMRI's GUI



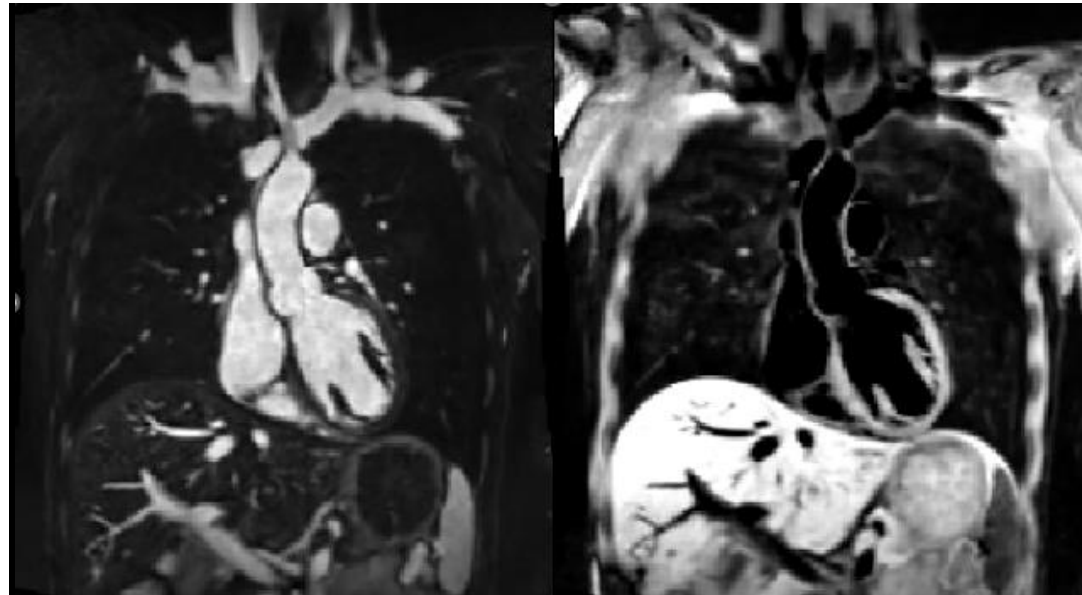
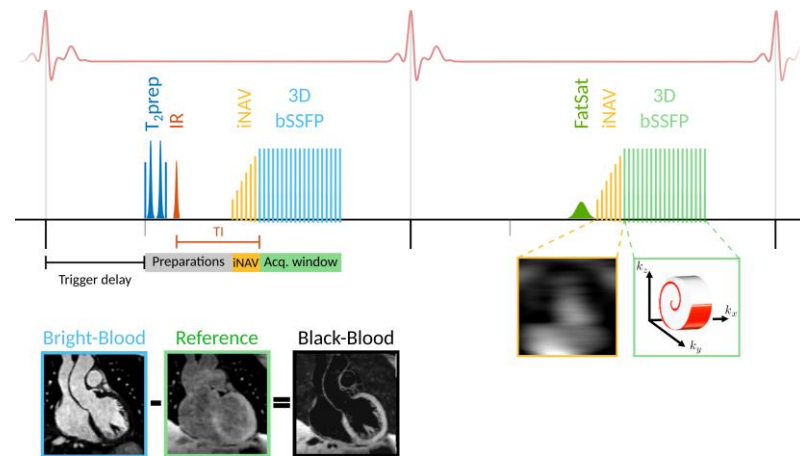
Whole-Heart Cardiovascular MRA with iNAV-based Non-Rigid Motion-Corrected Reconstruction at 0.55T

Carlos Castillo-Passi, Michael Crabb, Camila Munoz, Karl P. Kunze, Radhouene Neji, Pablo Irrarrazaval, René M. Botnar, and Claudia Prieto



Simultaneous iNAV-based 3D Whole-Heart Bright-Blood and Black-Blood Imaging at 0.55T

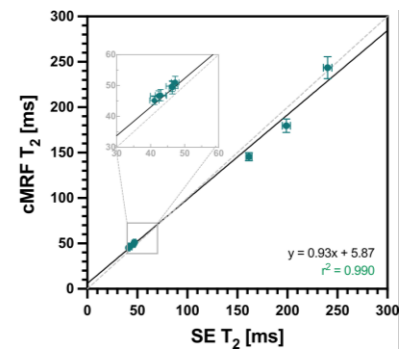
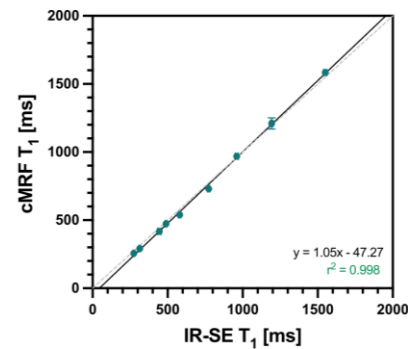
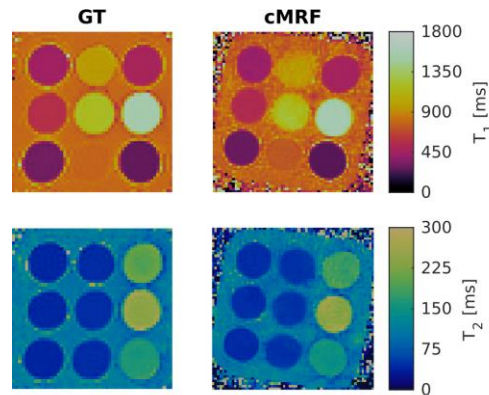
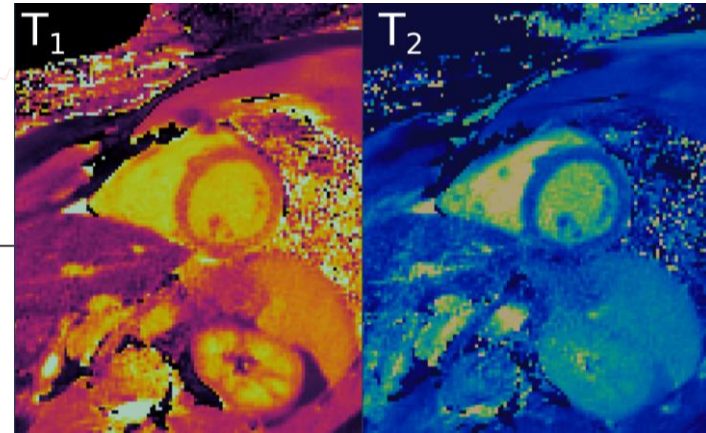
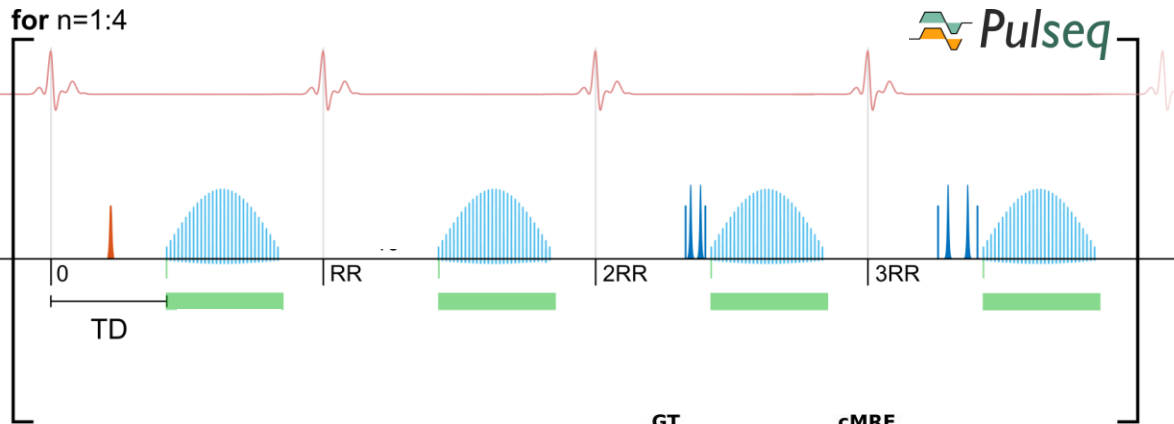
Carlos Castillo-Passi, Karl P. Kunze, Michael Crabb, Camila Munoz, Radhouene Neji, Pablo Irrazaval, René M. Botnar, and Claudia Prieto



Cardiac Magnetic Resonance Fingerprinting for Simultaneous T1 and T2 Mapping at 0.55T

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for n=1:4



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