

A) Service times

S_k WebService:

 $B_k / C_k = 86400 / 432 000 = 12 960 / 432 000 = 0.03$

S_k Authentication Server:

- 1) $V_k = C_k / C$. V_k here is 1.0286 and C is 432 000 $\Leftrightarrow C_k = V_k * C = 1.0286 * 432 000 = 444 355$
- 2) $B_k = 86400 * 0.512 = 44237$
- 3) $S_k = B_k / C_k = 44 237 / 444 355 = 0.09956$

S_k Application Server:

Using Little's law we have N = XR so X = N/R = 1.766/0.0618Then U = X*S / c so S = c U / X = 2*(0.5714 / 28.576) = 0.03999

S_k Map Server

We consider that all the requests went through the map server as it was observed that 432 000 were completed. Hence we have C_k = C = 432 000

 $B_k = 21600$

So $S_k = 21\ 600\ /\ 432\ 000 = 0.05$

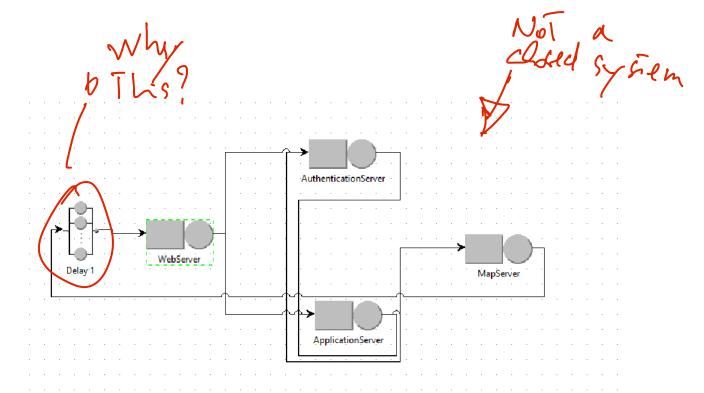
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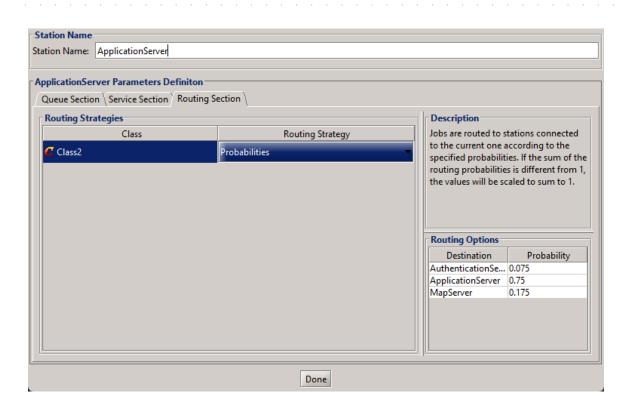
Service Centre	Service Time (S _k)
WebServer	0.03
AuthorizationServer	0.09956
ApplicationServer	0.039
MapServer	0.05

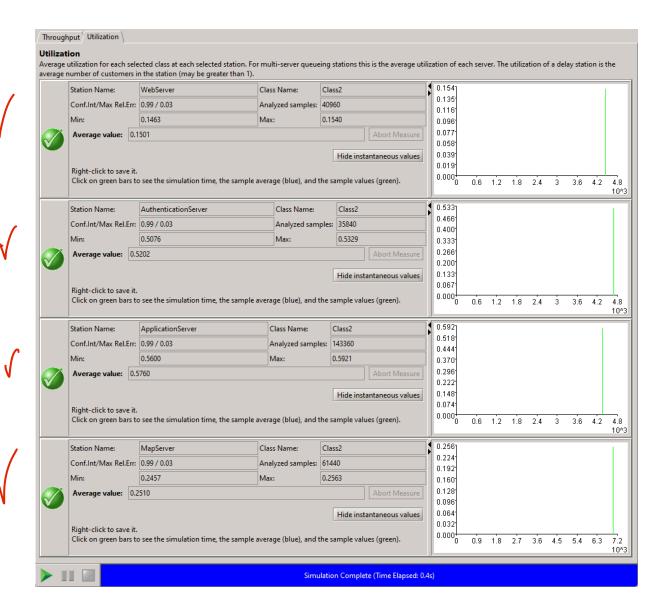
B) Simulation results

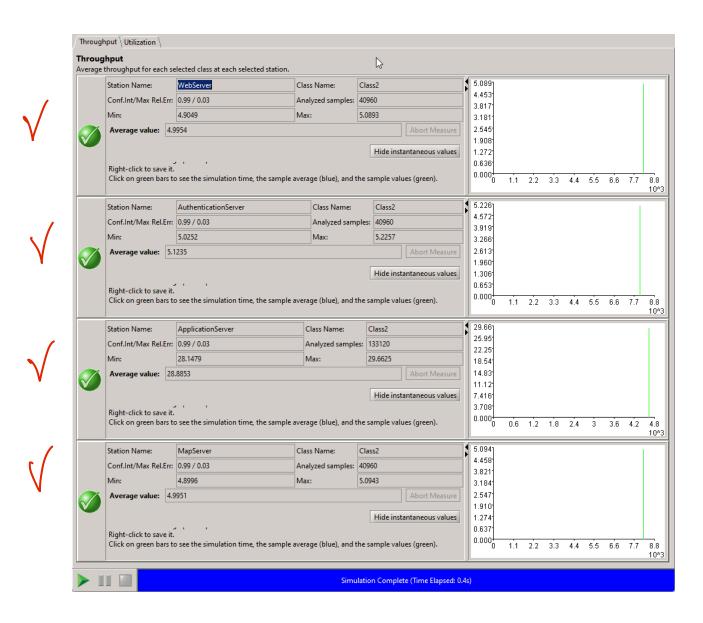
WebServer - exp(33.333) AuthenticationServer - exp (10.044) MapServer - exp(20)

ApplicationServer - exp(25.006)









Name of service center	Utilization	Throughput
WebServer	0,1501	4,9954
AuthorizationServer	0,5202	5,1235
ApplicationServer	0,5760	28.8853
MapServer	0,2510	4.9951

Average System Response Time: 0.6505

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C) System upgrade

Web server

The new throughput will be:

 X_k : 1 296 000 / 86400 = 15

We then have the $U_k = X_k * S_k = 15 * 0.03 = 0.45$

0.45 < 1 so the web server do not need any upgrade.

Authentication server:

The average number of request will be: 1 296 000 * 1.0286 = 1 333 066

The new throughput will be:

 X_k : 1 333 066 / 86400 = 15.42

We then have $U_k = (X_k * S_k) / c = 15.42 * 0.09956 = 1.54$

or U_k < 1 We need to divide U_k by two, hence doubling the number of servers.

1.54 / 2 = 0.77. Here, $U_k = (X_k * S_k) / c$ for c = 2.

This corresponds to our findings.

Application Server:

We have the new average jobs which is 3*1.766 = 5.298

According to Little's law, we have N = X*R. N is 5.298 and R is 0.0618.

We have $5.298=X*0.0618 \Leftrightarrow X=5.298/0.0618 = 85.72$

This corresponds to our findings.

Going further, we see that $U_k = V_k * S_k / c = (85.72*0.04) / 2$

Hence, $2U_k = 3,488 \Leftrightarrow U_k = 1.744$

For $U_k < 1$ We need to divide U_k by two, hence doubling the number of servers, coming from 2 to 4.

Then, we would have $U_k = (85.72*0.04) / 2*2 = 0.872$.

This corresponds to our findings.

Map Server:

 $X_k = C_k / T \rightarrow 1296000 / 86400 = 15$

 $U_k = (X_k S_k) \rightarrow 15 * 0.05 = 0.75 < 1$

0.75 < 1 so the web server do not need any upgrade.



Name of service center	Minimum number of resources	Utilization	Throughput
WebServer	1	0.4496	14.9457
AuthorizationServer	2	0,7703	15.3760
ApplicationServer	4	0.8503	84.5606
MapServer	1	0,7462	14.9056

Average System Response Time (do not worry if you got the red cross next to some result during the simulation, as long as the blue line in the graph of the chart on the right is stable): 0,9958

