

1)

- a)  $f = \Theta(g)$   $c \cdot f(n)$  can be  $\geq / \leq c \cdot g(n)$
- b)  $f = O(g)$   $n^{2/3}$  will always be larger eventually, no matter what  $C \cdot f(n)$  equals
- c)  $f = \Theta(g)$   $n > \log(n)^x$ , which results in just  $c \cdot n$
- d)  $f = \Theta(g)$  just constants result in  $c \cdot n$
- e)  $f = \Theta(g)$  just constants result in  $c \cdot \log(n)$ , for both  $f(n)$  and  $g(n)$
- f)  $f = \Theta(g)$   $\log(n^2) = 2\log(n)$ , which results in both being  $c \cdot \log(n)$ , and thus being theta.

2)

- a) if  $c < 1$ , then  $\lim$  of  $g(n) = 1$ , resulting in  $g(n) = \Theta(1)$ . Any constant applied can result in an upper or lower bound.
- b) if  $c = 1$ , then  $\lim$  of  $g(n) = \infty$ , and  $\lim$  of  $(n) = \infty$ . This results in any constant can be applied to  $(n)$  to upper or lower bound  $g(n)$
- c) if  $c > 1$ , then the  $\lim$  of  $(g)n = c^n$ , which is the same as  $c^n$ . Any constant can be applied to upper or lower bound  $g(n)$  in that case.

3.a)

```
def fibExp(n):
    if n == 0:
        return 1
    if n == 1:
        return 1
    if n == 2:
        return 1
    return (fibExp(n-1) + fibExp(n-2) * fibExp(n-3))

print (fibExp(10))
```

$f^n$  due to the function being ran to the power of  $n$ . The more  $N$  exists, the more it recurses down, exponentially.

b)

```
def fabLinear(n):
    if n == 0:
        return 1
    if n == 1:
        return 1
    if n == 2:
        return 1
    array = [1,1,1]
    for x in range(3, n + 1):
        array.append(x)
    for x in range(3, n + 1):
```

```
    array[x] = array[x-1] + array[x-2] * array[x-3]
    add = (len(array) - 3) * 2
    mult = (len(array) - 3)
    return array[n], add, mult
```

add and mult returns the number of additions and multiplications, respectively