

Decision-Tree for Classification

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Course Overview

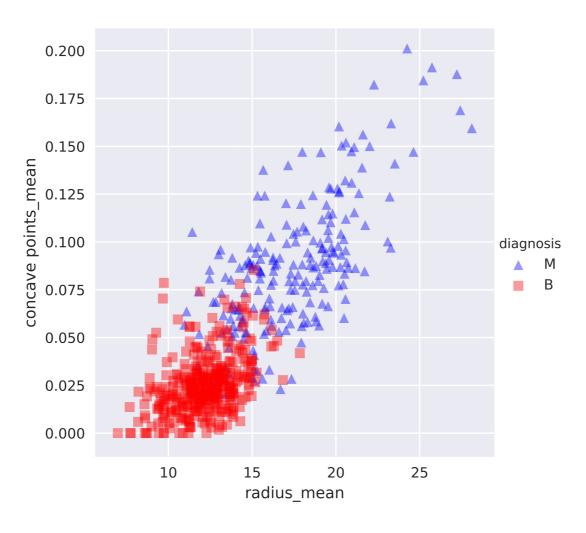
- Chap 1: Classification And Regression Tree (CART)
- Chap 2: The Bias-Variance Tradeoff
- Chap 3: Bagging and Random Forests
- Chap 4: Boosting
- Chap 5: Model Tuning

Classification-tree

- Sequence of if-else questions about individual features.
- Objective: infer class labels.
- Able to capture non-linear relationships between features and labels.
- Don't require feature scaling (ex: Standardization, ..)

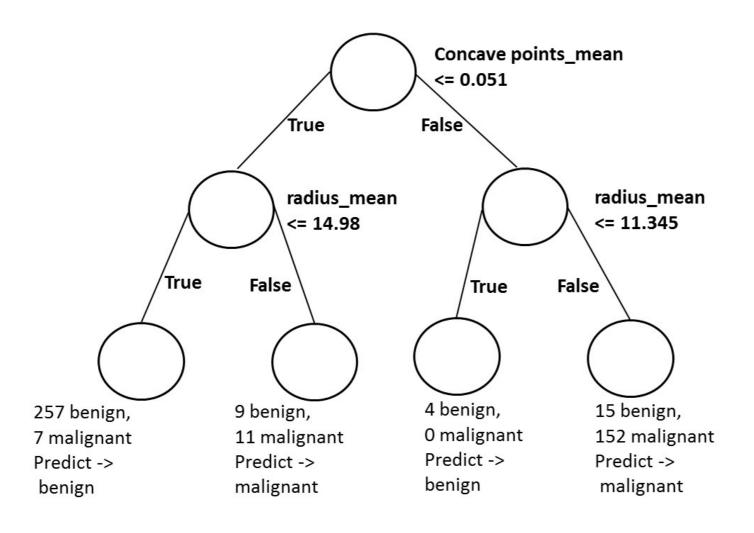


Breast Cancer Dataset in 2D





Decision-tree Diagram





Classification-tree in scikit-learn

```
# Import DecisionTreeClassifier
In [1]: from sklearn.tree import DecisionTreeClassifier

# Import train_test_split
In [2]: from sklearn.model_selection import train_test_split

# Import accuracy_score
In [3]: from sklearn.metrics import accuracy_score

# Split dataset into 80% train, 20% test
In [4]: X_train, X_test, y_train, y_test= train_test_split(X, y, test_size=0.2, stratify=y, random_state=1)

# Instantiate dt
In [5]: dt = DecisionTreeClassifier(max_depth=2, random_state=1)
```



Classification-tree in scikit-learn

```
# Fit dt to the training set
In [6]: dt.fit(X_train, y_train)

# Predict test set labels
In [7]: y_pred = dt.predict(X_test)

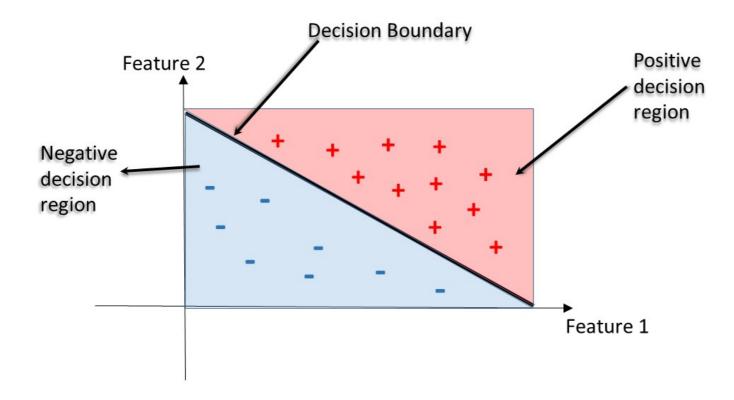
# Evaluate test-set accuracy
In [8]: accuracy_score(y_test, y_pred)

Out[8]: 0.90350877192982459
```

Decision Regions

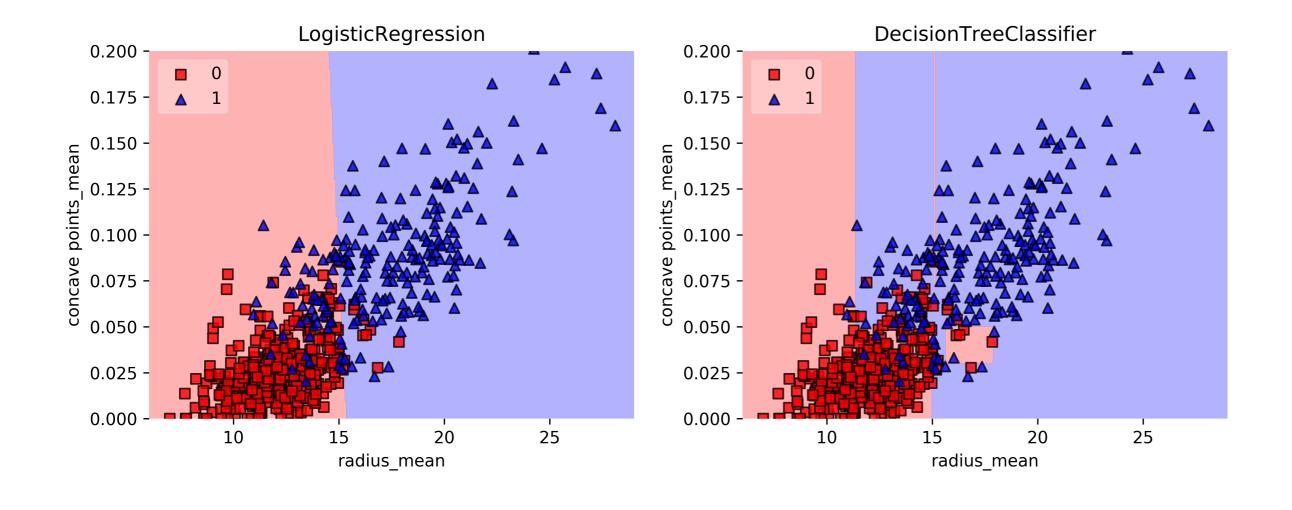
Decision region: region in the feature space where all instances are assigned to one class label.

Decision Boundary: surface separating different decision regions.





Decision Regions: CART vs. Linear Model







Let's practice!





Classification-Tree Learning

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Building Blocks of a Decision-Tree

• **Decision-Tree**: data structure consisting of a hierarchy of nodes.

Node: question or prediction.



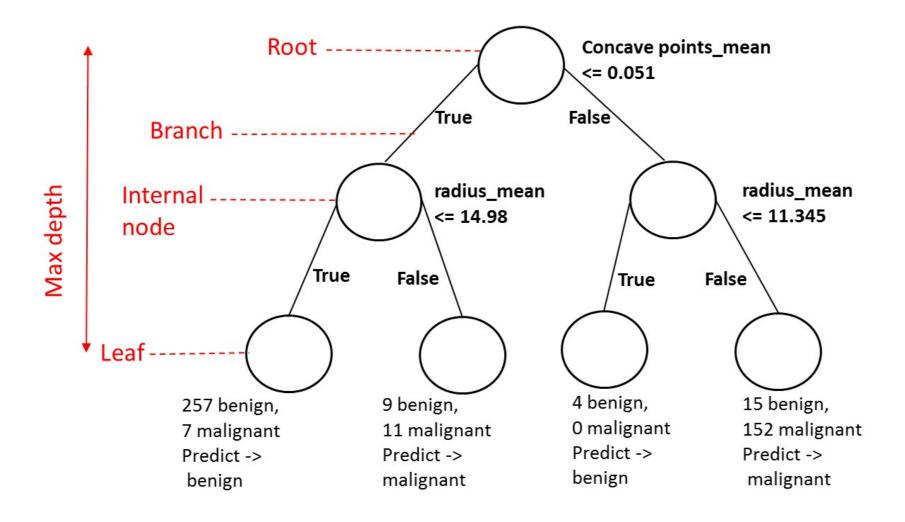
Building Blocks of a Decision-Tree

Three kinds of nodes:

- Root: no parent node, question giving rise to two children nodes.
- Internal node: one parent node, question giving rise to two children nodes.
- Leaf: one parent node, no children nodes --> prediction.

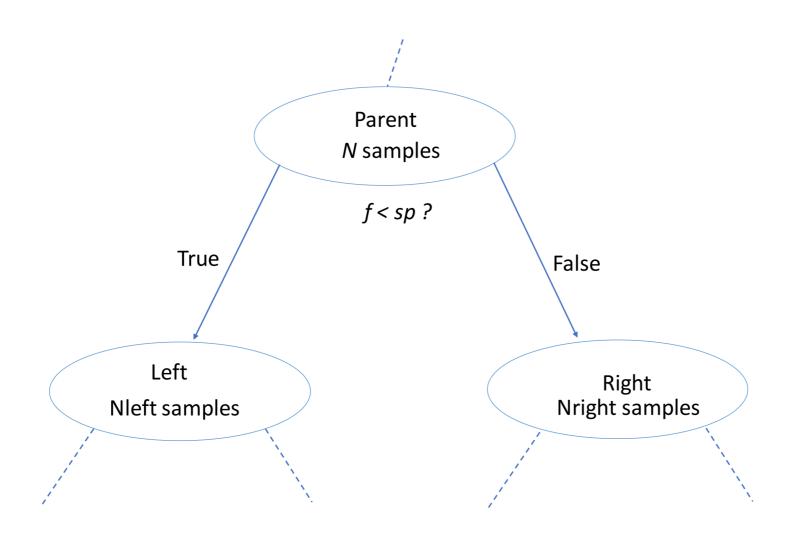


Prediction





Information Gain (IG)



Information Gain (IG)

$$IG(\underbrace{f}_{feature\ split-point}, \underbrace{sp}_{split-point}) = I(parent) - \left(\frac{N_{left}}{N}\ I(left) + \frac{N_{right}}{N}\ I(right)\right)$$

Criteria to measure the impurity of a node I(node):

- gini index,
- entropy. ...

Classification-Tree Learning

- Nodes are grown recursively.
- At each node, split the data based on:
 - feature f and split-point sp to maximize IG(node).
- If IG(node) = 0, declare the node a leaf.

...



Information Criterion in scikit-learn (Breast Cancer dataset)

```
# Import DecisionTreeClassifier
In [1]: from sklearn.tree import DecisionTreeClassifier
# Import train test split
In [2]: from sklearn.model selection import train test split
# Import accuracy score
In [3]: from sklearn.metrics import accuracy_score
# Split dataset into 80% train, 20% test
In [4]: X train, X test, y train, y test= train test split(X, y,
                                                    test size=0.2,
                                                     stratify=y,
                                                     random state=1)
# Instantiate dt, set 'criterion' to 'gini'
In [5]: dt = DecisionTreeClassifier(criterion='gini', random state=1)
```



Information Criterion in scikit-learn

```
# Fit dt to the training set
In [6]: dt.fit(X_train,y_train)

# Predict test-set labels
In [7]: y_pred= dt.predict(X_test)

# Evaluate test-set accuracy
In [8]: accuracy_score(y_test, y_pred)

Out[8]: 0.92105263157894735
```





Let's practice!



Decision-Tree for Regression

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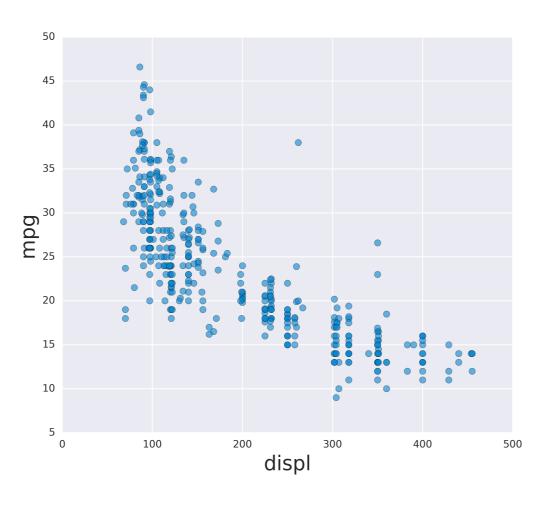


Auto-mpg Dataset

	mpg	displ	hp	weight	accel	origin	size
0	18.0	250.0	88	3139	14.5	US	15.0
1	9.0	304.0	193	4732	18.5	US	20.0
2	36.1	91.0	60	1800	16.4	Asia	10.0
3	18.5	250.0	98	3525	19.0	US	15.0
4	34.3	97.0	78	2188	15.8	Europe	10.0
5	32.9	119.0	100	2615	14.8	Asia	10.0



Auto-mpg with one feature





Regression-Tree in scikit-learn

```
# Import DecisionTreeRegressor
In [1]: from sklearn.tree import DecisionTreeRegressor
# Import train test split
In [2]: from sklearn.model selection import train test split
# Import mean squared error as MSE
In [3]: from sklearn.metrics import mean squared error as MSE
# Split data into 80% train and 20% test
In [4]: X train, X test, y train, y test= train test split(X, y,
                                                            test size=0.2,
                                                            random state=3)
# Instantiate a DecisionTreeRegressor 'dt'
In [5]: dt = DecisionTreeRegressor(max depth=4,
                                   min samples leaf=0.1,
                                   random state=3)
```



Regression-Tree in scikit-learn

```
# Fit 'dt' to the training-set
In [6]: dt.fit(X_train, y_train)

# Predict test-set labels
In [7]: y_pred = dt.predict(X_test)

# Compute test-set MSE
In [8]: mse_dt = MSE(y_test, y_pred)

# Compute test-set RMSE
In [9]: rmse_dt = mse_dt**(1/2)

# Print rmse_dt
In [10]: print(rmse_dt)
Out[10]: 5.1023068889
```

Information Criterion for Regression-Tree

$$I(\mathsf{node}) = \underbrace{\mathsf{MSE}(\mathsf{node})}_{mean-squared-error} = \frac{1}{N_{node}} \sum_{i \in node} (y^{(i)} - \hat{y}_{node})^2$$

$$\hat{y}_{node} = \frac{1}{N_{node}} \sum_{i \in node} y^{(i)}$$

$$mean-target-value$$

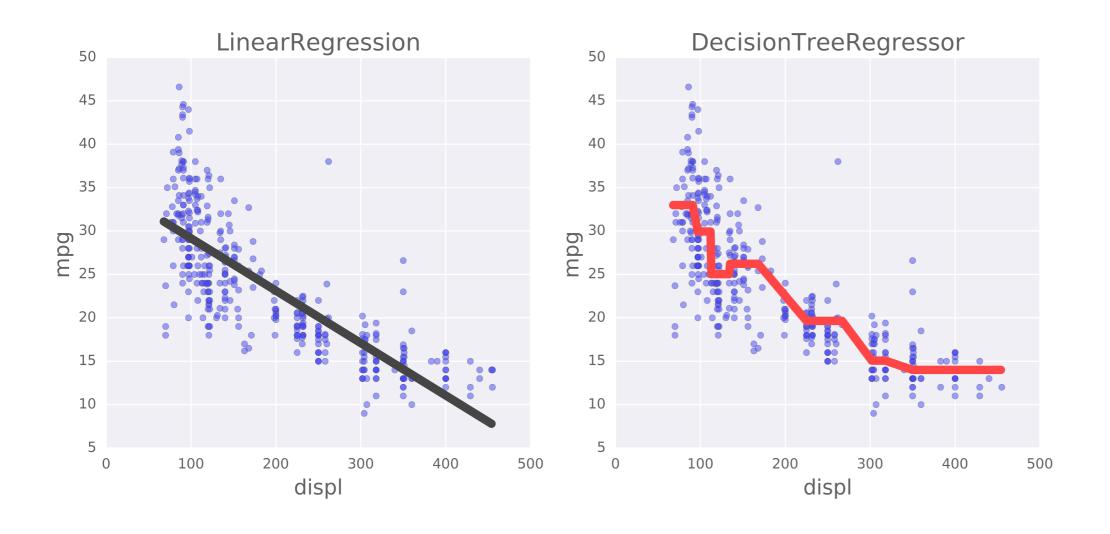


Prediction

$$\hat{y}_{pred}(leaf) = \frac{1}{N_{leaf}} \sum_{i \in leaf} y^{(i)}$$



Linear Regression vs. Regression-Tree







Let's practice!