

Force, density, Pressure

Force is rate of change of momentum.

There are two groups of force:-

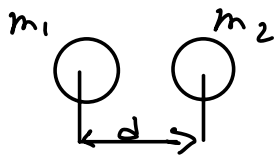
- 1) Contact force
- 2) Non contact force

Effect of force

- 1) Change speed
- 2) Change direction
- 3) Change shape
- 4) Cause a body to rotate about an axis.

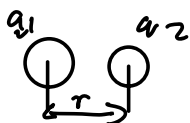
Different type of Forces

- 1) Gravitational force \rightarrow Every object attracts other object with a force.



$$F \propto \frac{m_1 m_2}{d^2}$$

- 2) Electrostatic force \rightarrow Force between two charged particles



$$F \propto \frac{q_1 q_2}{r^2}$$

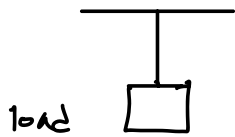
Contact force

1) Normal Contact Force



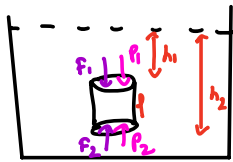
2) Friction

3) Tension



For load tension is upwards.
for ceiling tension is downwards.

4) Upthrust



$$P_1 = h_1 \rho g$$

$$P_2 = h_2 \rho g$$

$$P_1 = \frac{F_1}{A}$$

$$P_2 = \frac{F_2}{A}$$

$$F_1 = P_1 A$$

$$F_2 = P_2 A$$

$$P_2 > P_1 \quad F_2 > F_1$$

$$F_2 - F_1 = \text{resultant force upwards}$$

$$F_2 - F_1 = \text{upthrust}$$

$$h_2 \rho g A - h_1 \rho g A = \text{upthrust}$$

$$\rho g A (h_2 - h_1) = \text{upthrust}$$

$$\rho g A l = \text{upthrust}$$

$$\rho g V_s = \text{upthrust}$$

$$\rho g V_p = \text{upthrust}$$

$$m_l g = \text{upthrust}$$

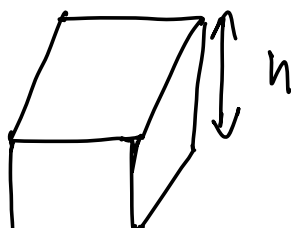
$$m_l g = \text{weight of the liquid displaced} = \text{upthrust}$$

Archimedes principle which states

→ upthrust acting on a body immersed in a fluid is equal to the weight of the fluid displaced.

* Show that pressure $P = h\rho g$ *

Solⁿ Consider a section of fluid in the form of a cuboid.



~~_____~~
Volume of cuboid $V = A \times h$

Its mass $m = V \times \rho$ (density of fluid)

$$m = A h \rho$$

$$\text{weight} = mg = A h \rho g$$

$$\text{Pressure} = \frac{\text{Force}}{\text{Area}} = \frac{A h \rho g}{A} = h \rho g$$

$$P = h \rho g$$

* Points to remember

Solid : Liquid : gas

density ratio $\longrightarrow S : L : G = 1000 : 1000 : 1$

Spacing ratio $\longrightarrow S : L : G = 1 : 1 : 10$

$$\text{spacing } n = \sqrt[3]{V}$$

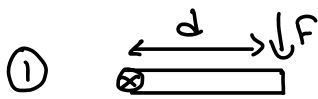
and

$$n \propto \sqrt[3]{\frac{1}{\rho}}$$

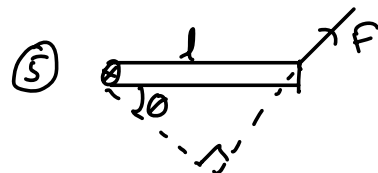
Moments

Moment \rightarrow The turning effect of a force is called moment

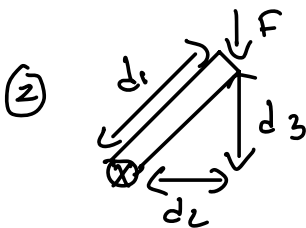
Moment = Force \times perpendicular distance from pivot.
SI unit = Nm



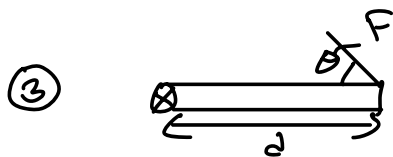
Moment = $F \times d$



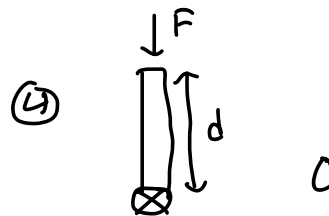
$l \cos \theta F$



$F \times d_2$

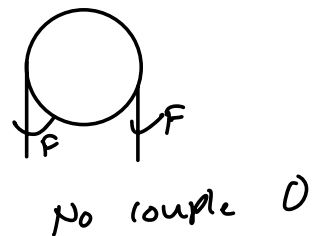
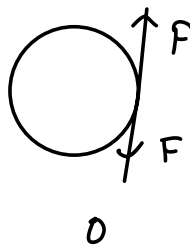
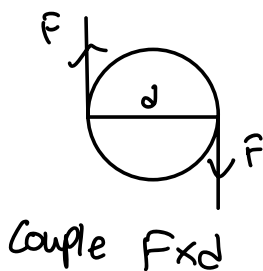


$F \sin \theta d$

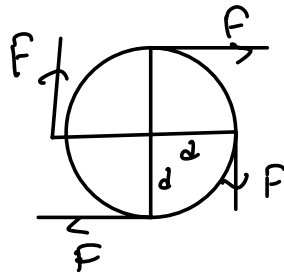


0

Couple: A couple is a pair of forces equal in magnitude, opposite in direction and are not in the same line of action.



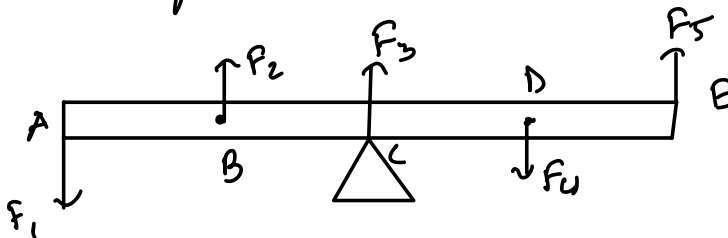
Torque: The total moment produced by a couple is called torque



$$\text{Torque} = Fd + Fd \\ 2Fd$$

The Principle of moment

For an object to be in equilibrium the sum of clockwise moment is equal to the sum of anticlockwise about the same point.

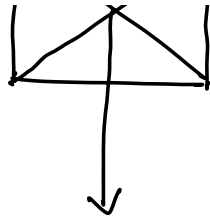


About C sum of CWM = sum of ACWM

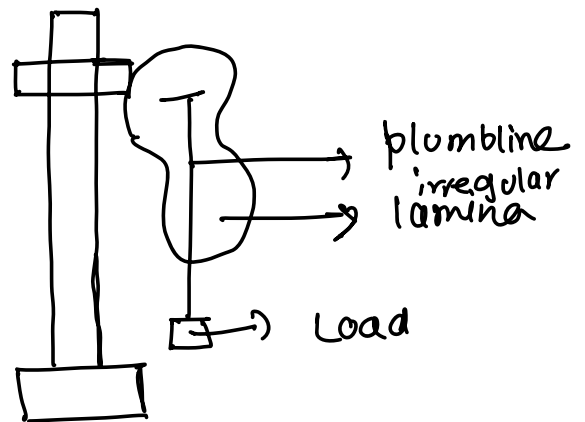
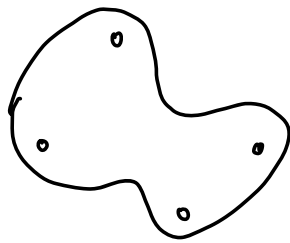
$$(F_4 \times CD) + (F_2 \times BC) = (F_1 \times AC) + (F_5 \times CE)$$

Centre of gravity → It is the point on the body where all its weight seems to act.





Finding centre of gravity of irregular lamina (Plumbline method)

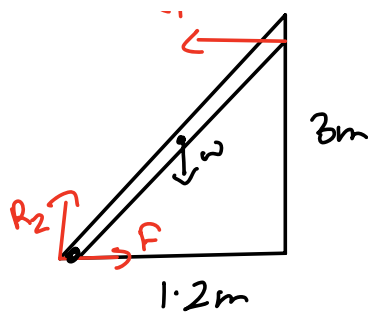


Equilibrium \rightarrow For an object to be in equilibrium

1) The sum of forces in any direction must be zero.

2) The sum of the moments of the forces about any point must be zero.

Figure shows a ladder leaned against the wall at rest.



$$W = 50$$

Resultant force = 0

upward force = downward force

$$R_2 = W$$

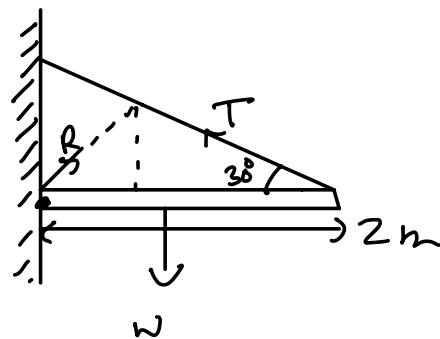
$$F = R_1$$

Comparing moments

$$W \times 0.6 = R_1 \times 3$$

$$50 \times 0.6 = R_1 \times 3$$

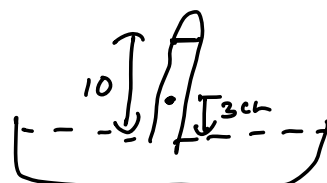
$$R_1 = 10 \text{ N}$$



$$W \times 1 = T \sin 30 \times 2$$

(the line of forces will have to intersect at one point if the object is in equilibrium)

Barometer → It measures atmospheric pressure



Atmospheric pressure = $h \rho g$
(760mm of H_g)

If pressure for
10cm is P .

Pressure at $x = \frac{z}{6} P$