

$$1. g = 6xz + 4yz + xy = 72$$

$$f = xyz$$

$$\Delta \nabla f = \langle yz, xz, xy \rangle$$

$$\nabla g = \langle 6z+y, 4z+x, 6x+4y \rangle$$

$$yz = \lambda (6z+y)$$

$$xz = \lambda (4z+x)$$

$$xy = \lambda (6x+4y)$$

$$\left. \begin{array}{l} yz = \lambda (6z+y) \\ xz = \lambda (4z+x) \\ xy = \lambda (6x+4y) \end{array} \right\} \begin{array}{l} y=6z, x=4z, 72z^2=72 \\ 6xz+4yz+xy=72 \end{array} \Rightarrow z=1, x=4, y=6$$