

$$\oint \oint \oint \frac{G m_0 \int \int \int z \rho \sin \phi \, d\rho \, d\phi \, d\theta}{\rho^3}$$
$$= G m_0 \pi a^2 / 3$$