

$$1. \frac{\partial w}{\partial r} = \frac{\partial w}{\partial x} \frac{\partial x}{\partial r} + \frac{\partial w}{\partial y} \frac{\partial y}{\partial r}$$

$$= (3x^2y + y^3) \cos \theta + (3y^2x + x^3) \sin \theta$$

$$2. dw = W_x dx + W_y dy$$

$$= W_x (x_r dr + x_\theta d\theta) + W_y (y_r dr + y_\theta d\theta)$$

$$= W_x (\cos \theta dr - r \sin \theta d\theta) + W_y (\sin \theta dr + r \cos \theta d\theta)$$

$$3. x|_{(2, \pi/4)} = \sqrt{2}$$

$$y|_{(2, \pi/4)} = \sqrt{2}$$

$$\frac{\partial w}{\partial r} \Big|_{(2, \pi/4)} = 16$$