

Problem 1 Benjamin Jazayeri

Problem 2

(a) $f_1, f_5, f_3, f_8, f_7, f_6, f_4, f_{\frac{3}{2}} \checkmark$

$$(b) h = n$$

$$\left. \begin{array}{c} n \\ n/3 \\ n/3 \\ n/3 \\ n/3 \\ n/3 \\ \vdots \\ \vdots \\ n \end{array} \right\} \Theta(h \lg_3 h)$$

(c) $\lg n = \lg n \quad \Theta(\lg n) \checkmark$

$$\lg n^{\frac{1}{2}} = \frac{1}{2} \lg n$$

$$\lg n^{\frac{1}{4}} = \frac{1}{4} \lg n$$

$$\vdots$$

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Problem 3

- (a) F ✓
- (b) T ✓
- (c) F ✓
- (d) F X -2
- (e) F ✓
- (f) F ✓
- (g) T X -2
- (h) T X -2
- (i) T ✓

Problem 4

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 m, h

$$(a) T(m, h) = 3h + T\left(\frac{m}{2}, h\right) = \Theta(h \log m) \quad \times$$

(b) The algorithm is correct. \times

We provide a 2 part Proof.

1. The Algorithm will terminate.

each Sub Problem has size

$$\left\lfloor \frac{m}{2} \right\rfloor \times h \text{ or } m - \left\lfloor \frac{m}{2} \right\rfloor \times h \text{ empty.}$$

so either returns or negatively

for empty, $m=1 \rightarrow \max$ will be Peak ✓

2. The returned Value will be

Peak. assume for \nexists it beingPassed up steps being peak $\rightarrow b$ isadjacent to middle column s.t. $a < b$ and c is max on there $\rightarrow b < c$ and $d > c$ but a is max \nexists \square

Problem 5

(a) $\binom{n}{k}$ leaves. ✓

$$\binom{n}{k} = n \binom{n-1}{k-1} + \binom{n-1}{k} = k \binom{n-1}{k-1}$$

(b) divide into $n/2$, test, recurseinto positive worst case $k \binom{n}{k}$. ✓

Problem 6 dict = {} ✓

(a) for i in multisets(k, P):
dict[sum(i)] = i

(b) return dict[S]

dict = {} ✓

(b) for i in multisets(k/2, P):

dict[sum(i)] = i

for i in multisets(k/2, P):

if S - sum(i) in dict: S - sum(i)

return i + dict[{}]

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Problem 7

(a) if $A[i] < \min$: ✓
 $\min = A[i]$

(b) ~~Binary Search for min $[i:j] < A[j]$~~
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$$\frac{7}{\cancel{3}9/12_0} = 65\%$$