

the center of an structure is obtained through averaging the centers of its subparts.

the center of a single L:

$$\left(\frac{1}{2} + \frac{n}{2}\right)/2 = \frac{n+1}{4} = c_1$$

the center of h Ls:

$$\begin{aligned} C_h &= c_1 + (c_1+1) + (c_1+2) + \dots + (c_1+(h-1))/h \\ &= (hc_1 + \frac{h(h-1)}{2})/h = c_1 + \frac{h-1}{2} \end{aligned}$$

every c_i for $i \neq 1$ should be $c_i \leq \underbrace{n-1}_{\text{length of base}}$
(base starts at -1)

for c_k it should be:

(we shift frame) $n^{-1} \lceil k \rceil n$

$$\rightarrow (n+1)/4 + (k-1)/2 \leq n-1/2 \quad \begin{cases} \text{for odd } n \\ \text{we have } 2 \text{ choices} \end{cases}$$

$$\rightarrow n-1 \leq (n+1)/4 + (k-1)/2 \leq n$$

$$\rightarrow \frac{3n-3}{2} \leq k \leq \frac{3n-1}{2}$$

Subject:

Year:

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$$\bullet \sum_{k=1}^n H_k = \sum_{k=1}^n \sum_{j=1}^k \frac{1}{j}$$

$$\bullet \sum_{k=1}^n H_k \text{ is similar to } \int_1^n 1/h = h | h - \frac{h}{1}$$

	j	1	2	3	4	...	h
	k						
1	1						
2	1	1/2					
3	1	1/2	1/3				
4	1	1/2	1/3	1/4			
	...						
n	1	1/2	1/3	1/4	...	1/h	

$$\bullet \sum_{j=1}^n \sum_{k=j}^h \frac{1}{j}$$

$$\bullet \sum_{j=1}^n \frac{1}{j} \sum_{k=j}^n 1 = \sum_{j=1}^n \frac{1}{j} (h-j+1)$$

$$= \sum_{j=1}^n \frac{h-j+1}{j} = \sum_{j=1}^n \frac{h+1}{j} - \sum_{j=1}^n 1$$

$$= (h+1) \sum_{j=1}^n \frac{1}{j} - h = (n+1) H_h - h$$