3 Problem 1

-3

-3

(6)
$$E_{\times}$$
 ind = $\frac{1}{3} \cdot \frac{3}{5} \cdot \frac{15}{5} + \frac{2}{3} \cdot \frac{15}{2} = 8$

(c) Var (ind 1 marten) =
$$(0-8)^2 \cdot \frac{2}{5} + (15-8)^2 \cdot \frac{3}{5}$$

= $E_X(in)^2 | marten) - E_X(ind 1 marten)^2$
= $\frac{3}{5} \cdot 15^2 tall - \frac{3}{2} = 54$

Problem 2 (a) $Pr(L|C) = \frac{Pr(C|L)}{Pr(C)} = \frac{1}{2} \cdot \frac{1}{3} = \frac{1}{4}$ (b) $E_{\times}(WXX) = E_{\times}(W|C) Pr(C) + E_{\times}(W|C\cap L) Pr(C\cap L)$ +Ex (WIZAL) Pr(WIZAL) -> Ex(w(c) = 7-1/4 Problem 3 (a) (Rank of nA, Suit of nA) 3 3 52.57.50.49/ 48 (52)

(b) (Rank of Tincluded, Suit of Tincluded,

Rank of 4) (0) 4.13.12.11.40.391.41 13.4.12 521 $\binom{52}{5}$

SC1 /1-624 $\begin{pmatrix} 52 \\ 5 \end{pmatrix}$

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Problem 4

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$$(a) \frac{6}{9} \cdot 3 = 2 = E \times (T)$$

$$Var(T) = 3 \cdot \frac{2}{3} (1 - \frac{2}{3}) = \frac{2}{3}$$

(b) 2/3. Linearity of Ex Joes not depend on inder

Problem 5

$$\frac{(a) n^2}{(2)-2n}$$

(b)
$$(1-\frac{n}{(2^n)-2n})^{-1}$$

Problem 6

The

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1

7

7

3

7

7

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7

3

$$T_{h,n} = H_{h-1} + S_{h-1} + C_{h-1}$$

$$T_{h-1} = H_{h-1} = S_{h-1} + C_{h-1} = H_{h}$$

$$(d) H_{h} = 2^{h-1} - H_{h-1}$$

2008 Final (cntd.)

Problem 7 (cntd.)

(d) Hn=2 - Hn-1

Hom Sol: x+1=0-> x=-1

Part

-

Bran Sol: Q2+ Q2-1= 1/2(2)

 $a_{2}^{n} + a_{2}^{n} = a_{2}^{1} + a_{2}^{n}$

 $a + \frac{a}{2} = \frac{1}{2}$

a = 1/3

Gen Sol: Hn=A(-1) + 1/32

Bdry chds: Ho=0 -> A = -13 ->

-> Hn=(-1/2)(-1)+1/22

Problem 8 (a) No (b) Yes (c) Ses (d) Yes Yes (E) N/B (f) Yes Problem 9 A Since the graph is finite, by wor, consider 4 the longest path. Consider the last hode. -9 Vn if Vn-> Vm7n then the Path is longer. -> Vn -> Vich therefor Vi ... Vn .. V; Fra 3 0

Problem 18 Proof (by invariance) tarp(h):= * of inversions is odd. J.S. if we have a iversions. We have mor 6-22. V D