Obligatory Exercise 2

TMA4275 Lifetime analysis Spring 2019

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In the solution exercise we used the $\mathbf R$ -libraries:

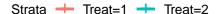
```
# for ggplot and dataframe
library(tidyverse)
# for survival analysis functions
library(survival)
# to plot survival curves in ggplot
library(survminer)
# to create tables in rmd
library(kableExtra)
# to get more information about surival regression
library(SurvRegCensCov)
# to predict usable covariates
library(rms)
```

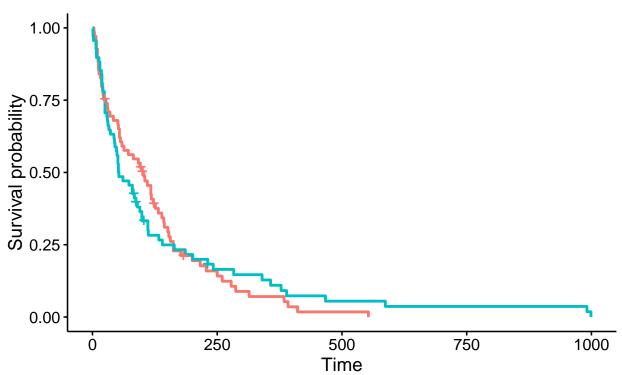
a)

We want to look at the lifetime distributions in the patients in the different treatment groups, standard and test.

Table 1: Estimated median and expected lifetime by treatment

treatment	median	expected
Treat=1	103.0	123.9282
Treat=2	52.5	134.0478



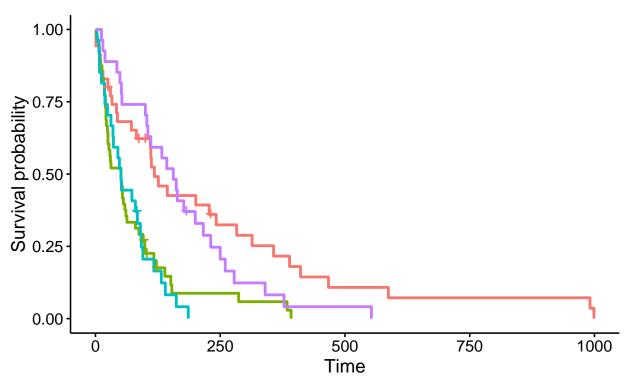


In the figure above the red curve is the survival distribution of the *standard* treatment and the blue curve is the survival distribution of the *test* treatment. From the plot we can see that the *test* treatment is worse(steeper curve) in small lifetimes, but doesn't hit survival probability of 0 for almost double the lifetime than for the *standard* treatment. This tells us that *test* is worse for 'bad' patients, but is better for 'good'. What a 'bad' or 'good' patient is, it's hard to say anything about yet, but might be possible after furter survival analysis and the inclusion of more covariates. The median and expected lifetimes of patients in the two groups is calculated in the code bellow and the results of which is shown in 1. From this we can see that median of the survival probability is lower for the *test* treatment, but the expected lifetime is alittle higher than for the *standard* treatment.

Now we do a similar assessment of a grouping by celltypes, which consist of the four different celltypes

Squamous(1), small-cell(2), adeno(3) and large(4).





The figure above shows the survival distributions in the grouping by celltype. Overall Cell = 2 and Cell = 3 is the worst, and Cell = 1 looks like the best Cell for lifetime. The code bellow calculates the median and expected lifetimes in the grouping by celltype, and the results are shown in the table 2.

From this result we see that the Cell = 1 has the heighest expected lifetime, followed by Cell = 4. But their roles are reversed for the median. For Cell = 2 and Cell = 3 they are almost equal in both accounts, but much lower lifetimes than the two others. The same conclusions as the one we drew from the figures. The reason the values of the median and expected lifetime not being consistently heigher than other group factors is because there are alot of data beeing either censored or dead the lower lifetimes. But the survival distribution might have data points at high lifetimes, and thereby have a long right tail, that will affect the

Table 2: Estimated median and expected lifetime by cell type

treatment	median	expected
Cell=1	118	188.45594
Cell=2	51	78.98110
Cell=3	51	65.55556
Cell=4	156	167.19342

Table 3: Estimated median and expected lifetime by cell type

Levels.of.Cell	x2	х3	x4
1	0	0	0
2	1	0	0
3	0	1	0
4	0	0	1

expected lifetime alot.

b)

In this exercise we will perform a fit to the Weibull regression model, with Treat, PS, Month, Age and Prior as model parameter, and Cell as a factor. The result of which is shown in the code bellow, using survreg from the R-package survival.

```
wei.lung<-survreg(Surv(Y,C) ~ Treat + PS + Month+ Age + Prior + factor(Cell), data = lungcancer.df, di
wei.lung
## Call:
## survreg(formula = Surv(Y, C) ~ Treat + PS + Month + Age + Prior +
       factor(Cell), data = lungcancer.df, dist = "weibull")
##
##
## Coefficients:
                                           PS
##
     (Intercept)
                         Treat
                                                      Month
                                                                       Age
     3.490536315 -0.228522672
                                  0.030068303
                                              -0.000468814
                                                               0.006099184
##
##
           Prior factor(Cell)2 factor(Cell)3 factor(Cell)4
    -0.004389765 -0.826184615 -1.132725093 -0.397680785
##
##
## Scale= 0.9281153
## Loglik(model) = -715.6 Loglik(intercept only) = -748.1
## Chisq= 65.08 on 8 degrees of freedom, p= 4.65e-11
## n = 137
In the table 3 the defined indicators or dummy variables is shown. And we adapt this to our regression model.
table.b <- data.frame(Levels.of.Cell = c(1,2,3,4), x2 = c(0,1,0,0), x3 = c(0,0,1,0), x4 = c(0,0,0,1))
kable(table.b,align=rep('c', 4),
      caption = "\\label{tab:b}Estimated median
      and expected lifetime by cell type") %>%
  kable_styling(bootstrap_options = c("striped", "hover",
                                       "condensed", "responsive"),
                full_width = F,position = "center")
```

Given $x = \{x_1(\text{Treat}), x_2(\text{Cell=2}), x_3(\text{Cell=3}), x_5(\text{Cell=4}), x_5(\text{PS}), x_6(\text{Month}), x_7(\text{Age}), x_8(\text{Prior})\}$, the values of the covariates given some person, were the "dummy variables" x_2, x_3, x_4 is set by table 3. From this

the model for log-lifetime T is given by the expression, with corresponding covariates \mathbf{x} ,

$$ln(T) = \beta_0 + \sigma\epsilon + \sum_{i=1}^{8} \beta_i x_i,$$

where $\epsilon \sim G(0,\sigma)$, a gumbel distribution with shape σ . This gives us the hazard rate function

$$z(t) = \alpha \cdot exp\{\beta_0 + \sum_{i=1}^8 \beta_i x_i\}^{-\alpha} \cdot t^{\alpha-1}$$

$$= \alpha e^{-\alpha\beta_0} t^{\alpha-1} e^{-\alpha \cdot \sum_{i=1}^8 \beta_i x_i}$$

$$= z_0(t) \cdot e^{-\alpha \cdot \sum_{i=1}^8 \beta_i x_i}$$

Now we will calculate the estimated median lifetimes of patients with respectively the same covariates as patient number 1 and 19. This means that for patient 1 which has Cell = 1 and we find a patient with the same, in this case we chose patient 3. For patient 19 which has Cell = 2, we chose patient 23. In the function lifeWeil the median lifetime from the our Weibull model is calculated.

```
coef <- wei.lung$coefficients</pre>
lifeWeil <- function(data, coef){</pre>
  res = vector()
  for (i in seq(1,length(data[,1]))){
    x = c(1,data$Treat[i], data$PS[i], data$Month[i], data$Age[i], data$Prior[i],as.numeric(data$Cell[i
          as.numeric(data$Cell[i]==3),as.numeric(data$Cell[i]==4))
    res = c(res,exp(as.numeric(coef)%*%x))
  }
  return(median(sort(res)))
patient1 <- lungcancer.df[lungcancer.df$Cell == lungcancer.df$Cell[1],]</pre>
patient2 <- lungcancer.df [lungcancer.df $Cell == lungcancer.df $Cell[19],]</pre>
life1 <- lifeWeil(patient1,coef)</pre>
life2 <- lifeWeil(patient2,coef)</pre>
cat("Estimated median lifetime equal patient 1:", life1)
## Estimated median lifetime equal patient 1: 240.7295
cat("Estimated median lifetime equal patient 19:", life2)
```

Estimated median lifetime equal patient 19: 83.78111

c)

To look at the p-values to determine significant effect of the covariates in our model, we can look at the output from the function summary.survreg.

```
summary(wei.lung)
##
## Call:
  survreg(formula = Surv(Y, C) ~ Treat + PS + Month + Age + Prior +
       factor(Cell), data = lungcancer.df, dist = "weibull")
##
##
                     Value Std. Error
                                          z
                            0.691171 5.05 4.4e-07
## (Intercept)
                 3.490536
## Treat
                            0.186844 -1.22 0.2213
                -0.228523
## PS
                 0.030068
                            0.004828 6.23 4.7e-10
                            0.008361 -0.06 0.9553
## Month
                -0.000469
## Age
                 0.006099
                            0.008553 0.71 0.4758
```

```
## Prior
                 -0.004390
                             0.021228 -0.21 0.8362
                             0.246312 -3.35 0.0008
## factor(Cell)2 -0.826185
## factor(Cell)3 -1.132725
                             0.257598 -4.40 1.1e-05
## factor(Cell)4 -0.397681
                             0.254749 -1.56 0.1185
## Log(scale)
                 -0.074599
                             0.066311 -1.12 0.2606
##
## Scale= 0.928
##
## Weibull distribution
## Loglik(model) = -715.6
                           Loglik(intercept only) = -748.1
  Chisq= 65.08 on 8 degrees of freedom, p= 4.7e-11
## Number of Newton-Raphson Iterations: 6
## n= 137
```

From the p-values we can see that PS and Cell has significant effect. We can also look at the figure bellow to get a more visual representation of the p-values.

```
psm.lung <- psm(Surv(Y,C)~Treat + PS + Month+ Age + Prior + factor(Cell), data = lungcancer.df,dist="w
```

To look at the significant difference between the two treatments we can use the ConvertWeibull to get the Event Time Ratio[ETR] of our model.

```
ConvertWeibull(wei.lung,conf.level = 0.95)$ETR
```

```
ETR
##
                                             UB
                                   LB
## Treat
                 0.7957083 0.5517117 1.1476131
## PS
                 1.0305249 1.0208196 1.0403225
## Month
                 0.9995313 0.9832843 1.0160467
## Age
                 1.0061178 0.9893916 1.0231268
## Prior
                 0.9956199 0.9550462 1.0379173
## factor(Cell)2 0.4377162 0.2701043 0.7093387
## factor(Cell)3 0.3221542 0.1944446 0.5337421
## factor(Cell)4 0.6718765 0.4077991 1.1069617
```

Looking at the output and ETR value for Treat, we can conclude that doing the test treatment will significantly decrease the survival time by approximately 20%. The scale parameter of our Weibul disitribution is $\alpha = 0.9281153$, this is pretty close to a exponential disitribution which has $\alpha = 1$. This means that a exponential disitribution might be better than our Weibull distribution. But to determine this the best way is to compare the AIC(Akaike's Information Criterion)-values of the two models, and then choose the one with the smallest. Now we will take out the non-significant covariates in our model. This can be done by the p-values found previously, or we can use the function fastbw to determine which covariates to use in our model based on p-values. If we choose a significance level of 5% and then force our model to include Treatment we get the results shown in the code bellow in 'Factors in Final model'.

```
fastbw(psm.lung,rule = "p",sls = 0.05, force=c(1),type = "individual")
```

```
##
## Parameters forced into all models:
##
    Treat
##
##
    Deleted Chi-Sq d.f. P
                                 Residual d.f. P
                                                        AIC
                          0.9553 0.00
##
             0.00
                    1
                                           1
                                                0.9553 - 2.00
    Month
##
    Prior
             0.07
                    1
                          0.7957 0.07
                                           2
                                                0.9655 - 3.93
##
    Age
             0.55
                    1
                         0.4577 0.62
                                           3
                                                0.8914 -5.38
##
## Approximate Estimates after Deleting Factors
##
```

```
##
                            S.E. Wald Z
                   Coef
                                 8.293 1.110e-16
                3.84429 0.46356
## (Intercept)
               -0.21046 0.18089 -1.163 2.446e-01
## Treat
                0.02906 0.00456 6.373 1.853e-10
## PS
## Cell=2
               -0.80044 0.23854 -3.356 7.918e-04
## Cell=3
               -1.10055 0.25107 -4.383 1.168e-05
               -0.38904 0.25390 -1.532 1.255e-01
## Cell=4
##
## Factors in Final Model
##
## [1] Treat PS
                   Cell
```

This means we use the covariates Treat, PS and the factors of Cell. Which is also what we concluded earlier.

```
wei.lung.new <- survreg(Surv(Y,C)~Treat + PS + factor(Cell), data = lungcancer.df, dist = "weibull")
ConvertWeibull(wei.lung.new,conf.level = 0.95)</pre>
```

```
## $vars
##
                    Estimate
                                       SE
## lambda
                  0.01606644 0.009730814
                  1.07504097 0.071234443
  gamma
                  0.22513731 0.196400967
## Treat
## PS
                 -0.03125301 0.005088627
## factor(Cell)2
                  0.85949730 0.264311692
## factor(Cell)3
                  1.18229768 0.287012105
## factor(Cell)4 0.41670792 0.276520819
##
  $HR
##
##
                        HR
                                   LB
                                             UB
## Treat
                 1.2524947 0.8523129 1.8405715
## PS
                 0.9692303 0.9596117 0.9789453
  factor(Cell)2 2.3619730 1.4069946 3.9651302
## factor(Cell)3 3.2618603 1.8584899 5.7249343
  factor(Cell)4 1.5169594 0.8822649 2.6082481
##
##
  $ETR
##
                       ETR
                                   LB
                                             UΒ
## Treat
                 0.8110528 0.5681942 1.1577145
## PS
                 1.0294982 1.0203440 1.0387345
## factor(Cell)2 0.4495528 0.2814600 0.7180336
## factor(Cell)3 0.3329477 0.2031849 0.5455828
## factor(Cell)4 0.6786698 0.4123532 1.1169859
```

Above we have done a new model fitting of a Weibull model using the covariates determined above. If we look at the HR(Hazard ratio)-values which is the risk of death, keeping all covariates constant except the one at interest. From this we find the significance of the covariates on risk of death, which means that Cell = 3 is the biggest factor to risk of death. The least significant covariate is PS, HR-value closest to 1 and thereby affects risk the least.

 \mathbf{d}

The Cox-model for the reduced model we found in c) is given by the equation

$$z(t; \mathbf{x}) = z_0(t)e^{\beta_1 x_1 + \beta_2 x_1 + \beta_3 x_3 + \beta_4 x_4 + \beta_5 x_5}$$

where $z_0(t)$ is any non-parametric hazard rate function and is unknown in the cox model. The reduced Weibull model for hazard rate is given by the equation

$$z(t; \mathbf{x}) = \alpha e^{-\alpha \beta_0} \cdot t^{\alpha - 1} \cdot e^{-\alpha (\beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \beta_4 x_4 + \beta_5 x_5)},$$

and the $z_0(t)$ function is known. Now we perform a cox regression on our data.

```
fit.coxph <- coxph(Surv(Y,C) ~ Treat + PS+ factor(Cell), data = lungcancer.df)
fit.coxph</pre>
```

```
## Call:
   coxph(formula = Surv(Y, C) ~ Treat + PS + factor(Cell), data = lungcancer.df)
##
##
                      coef exp(coef)
                                       se(coef)
                                       0.200923
## Treat
                  0.261744
                            1.299194
                                                 1.303
                                                       0.19267
## PS
                 -0.031271
                            0.969213
                                       0.005165 -6.054 1.41e-09
## factor(Cell)2
                  0.824980
                            2.281836
                                       0.268911
                                                 3.068 0.00216
## factor(Cell)3
                  1.153994
                            3.170833
                                       0.295038
                                                 3.911 9.18e-05
## factor(Cell)4 0.394625
                            1.483828
                                      0.282243
                                                 1.398
                                                       0.16206
## Likelihood ratio test=61.07 on 5 df, p=7.307e-12
## n= 137, number of events= 128
```

If we look at the relative risk of this Cox-model. The relative risk is found by increasing the value of a covariate by 1 and see calculate the difference in hazard rate $z(t, \mathbf{x})$. Doing the calculations with the hazard rate function one ends up with equation, with RR being relative risk,

$$RR = e^{\beta_i}$$
,

with i being the covariate of interest, where in out case $i \in \{1, 2..., 5\}$. This means that from the output of our Cox-regression above we look at the values of exp(coef), which is the relative risk factor. From this we can see that the highest relative risk is from Cell = 3. The risk of death is increased with 26% if one uses the test treatment istead of the standard treatment. If one increases the Performance status by 1 the change is not that significant, but since has a large range, $x_5 \in [10, 90]$, the change is more significant than the what the relative risk factor is suggesting.

e

In this exercise we will look at the interaction between two covariates, Treat and Cell, while keeping Cell as a factor. We are still using table 3 for the values of x_2,x_3 and x_4 . With the interaction of the covariates, we introduce three new variables $z_2 = x_1 \cdot x_2$, $z_3 = x_1 \cdot x_3$ and $z_4 = x_1 \cdot x_3$. We will use the same covariates as in the reduced model from c), Treat, PS, and Cell, and we use weibull regression to determine the β_i - values.

```
wei.lung.int<- survreg(Surv(Y,C) ~ Treat + PS+ factor(Cell) + Treat*factor(Cell), data = lungcancer.df,
summary(wei.lung.int)</pre>
```

```
##
## Call:
##
   survreg(formula = Surv(Y, C) ~ Treat + PS + factor(Cell) + Treat *
       factor(Cell), data = lungcancer.df, dist = "weibull")
##
                           Value Std. Error
##
                                                 z
                                                         р
## (Intercept)
                         3.03586
                                    0.56348
                                             5.39 7.1e-08
## Treat
                                              0.96
                                                     0.338
                         0.31709
                                    0.33087
## PS
                         0.02842
                                    0.00454
                                              6.26 3.8e-10
## factor(Cell)2
                         0.71458
                                    0.67362
                                             1.06
                                                     0.289
## factor(Cell)3
                        -1.01522
                                    0.85762 -1.18
                                                     0.237
```

```
## factor(Cell)4
                        0.80009
                                    0.77114 1.04
                                                    0.299
## Treat:factor(Cell)2 -1.02077
                                   0.43169 -2.36
                                                    0.018
## Treat:factor(Cell)3 -0.07629
                                   0.51329 - 0.15
                                                    0.882
## Treat:factor(Cell)4 -0.75657
                                   0.48151 -1.57
                                                    0.116
## Log(scale)
                       -0.11825
                                   0.06845 -1.73
                                                    0.084
##
## Scale= 0.888
##
## Weibull distribution
## Loglik(model) = -712.4
                           Loglik(intercept only) = -748.1
## Chisq= 71.45 on 8 degrees of freedom, p= 2.5e-12
## Number of Newton-Raphson Iterations: 5
## n = 137
```

As hinted in the exercise paper the only interaction which has p-value lower than a significance level of 0.05 is z_2 .

We will now to calculate the estimated relative risk of patients with Cell = 2 in the standard treatment, compared to the patient with the test treatment. First we find a general formula for the Relative Risk(RR) given the Cell. Let $\mathbf{x} = \{x_1, x_2, x_3, x_4, x_5, x_1 \cdot x_2, x_1 \cdot x_3, x_1 \cdot x_4\}$ and $\mathbf{x} = \{x_1 + 1, x_2, x_3, x_4, x_5, (x_1 + 1) \cdot x_2, (x_1 + 1) \cdot x_3, (x_1 + 1) \cdot x_4\}$, then the relative risk is given by the equation

```
RR_{\text{weib}}(x_1|Cell = j; j \in \{2, 3, 4\}) = \frac{z(t; \mathbf{x}_2|Cell = j)}{z(t; \mathbf{x}_1|Cell = j)}
= \frac{z_0(t) \cdot \exp\{-\alpha \cdot (\beta_1(x_1 + 1) + \beta_j x_j + \beta_5 x_5 + \beta_{j+4}(x_1 + 1)x_j)\}}{z_0(t) \cdot \exp\{-\alpha \cdot (\beta_1 x_1 + \beta_j x_j + \beta_5 x_5 + \beta_{j+4}x_1x_j)\}}
= \exp\{-\alpha \cdot (\beta_1 + \beta_{j+4})\}
```

If the Cell = 1, the expression simply becomes

$$RR(x_1|Cell = 1) = \exp\{-\alpha \cdot \beta_1\}$$

From this knowledge we can create a function in **R** that calculates the relative risk of all the different *Cell* types respectivly. This is done in the function relativeRisk and the result of which is shown in table 4.

```
relativeRisk <- function(coef,Cell,scale){</pre>
  if (Cell > 1){
    return(exp(-scale*(coef[2] + coef[Cell+5])))
 return(exp(-scale*coef[2]))
}
coef.int <- wei.lung.int$coefficients</pre>
scale.int <- wei.lung.int$scale</pre>
table.e \leftarrow data.frame(Cell = c(1,2,3,4),
                       RR = c(relativeRisk(coef.int,Cell = 1,scale.int),
                              relativeRisk(coef.int,Cell = 2,scale.int),
                              relativeRisk(coef.int,Cell = 3,scale.int),
                              relativeRisk(coef.int,Cell = 4,scale.int)))
kable(table.e,align=rep('c', 4),
      caption = "\\label{tab:e}Estimated Relative Risk of
      \\textit{test} treatment\n compared to \\textit{standard}
      treatment in the different \\textit{Cell}-types.") %>%
  kable_styling(bootstrap_options = c("striped", "hover",
                                        "condensed", "responsive"),
                full_width = F,position = "center")
```

From the results in table 4 we can see that for patients with Cell-type 1 it is approximately 25% lower risk of death using the test treatment. For patients with Cell-type 2 it is approximately 87% higher risk of death

Table 4: Estimated Relative Risk of test treatment compared to standard treatment in the different Cell-types.

Cell	RR
1	0.7544832
2	1.8686171
3	0.8073987
4	1.4776759

using the *test* treatment. Further on for patients with *Cell*-type 3, it is approximately 19% lower risk of death using the *test* treatment. And last for patients with *Cell*-type 4 it is approximately 48% higher risk of death using the *test* treatment. Thereby we can conclude that patients with *Cell*-type 1 should take *test* treatment, patients with *Cell*-type 2 should take the *standard* treatment, patients with *Cell*-type 3 should take *test* treatment and patients of *Cell*-type 4 should take the *standard* treatment.

f)

From the model fit in the final model in exercise e), we used a Weibull regression with reduced amount of covariates from what we started out with. We used Treat, Cell as factor, PS, and $Treat \times Cell$ with Cell as factor. We will now try to fit different distributions to the data using the same covariates as in e). We tested the exponential distribution yielding:

```
exp.lung<- survreg(Surv(Y,C)~Treat + PS + factor(Cell)+ factor(Cell)*Treat, data = lungcancer.df, dist summary(exp.lung)
```

```
##
## Call:
## survreg(formula = Surv(Y, C) ~ Treat + PS + factor(Cell) + factor(Cell) *
##
       Treat, data = lungcancer.df, dist = "exponential")
                         Value Std. Error
##
                                              z
## (Intercept)
                        2.9784
                                   0.6333 4.70 2.6e-06
## Treat
                        0.2908
                                   0.3713 0.78
                                                  0.433
## PS
                        0.0293
                                   0.0050 5.86 4.7e-09
## factor(Cell)2
                        0.6062
                                   0.7547 0.80
                                                  0.422
## factor(Cell)3
                                   0.9598 - 1.09
                       -1.0476
                                                  0.275
## factor(Cell)4
                        0.7759
                                   0.8682 0.89
                                                  0.371
## Treat:factor(Cell)2 -0.9428
                                   0.4829 -1.95
                                                  0.051
## Treat:factor(Cell)3 -0.0405
                                   0.5733 - 0.07
                                                  0.944
## Treat:factor(Cell)4 -0.7283
                                   0.5420 - 1.34
                                                  0.179
##
## Scale fixed at 1
##
## Exponential distribution
## Loglik(model) = -713.8 Loglik(intercept only) = -751.2
## Chisq= 74.89 on 8 degrees of freedom, p= 5.2e-13
## Number of Newton-Raphson Iterations: 5
## n= 137
```

The gaussian distribution:

```
gauss.lung<- survreg(Surv(Y,C)~Treat + PS + factor(Cell)+ factor(Cell)*Treat, data = lungcancer.df, dis
summary(gauss.lung)
```

```
##
## Call:
## survreg(formula = Surv(Y, C) ~ Treat + PS + factor(Cell) + factor(Cell) *
```

```
##
       Treat, data = lungcancer.df, dist = "gaussian")
##
                           Value Std. Error
                                               z
## (Intercept)
                       -136.3214
                                   83.7726 -1.63
                                   47.6961 2.47
## Treat
                       117.7238
                                                    0.014
## PS
                          2.8212
                                    0.6071 4.65 3.4e-06
## factor(Cell)2
                        104.4961
                                    98.2598 1.06
                                                    0.288
## factor(Cell)3
                        44.4392 123.3197 0.36
                                                    0.719
## factor(Cell)4
                       179.6987 113.8398 1.58
                                                    0.114
## Treat:factor(Cell)2 -147.7238 62.6641 -2.36
                                                    0.018
## Treat:factor(Cell)3 -119.0884 72.8470 -1.63
                                                    0.102
## Treat:factor(Cell)4 -156.1177
                                 71.4155 -2.19
                                                    0.029
## Log(scale)
                          4.8963
                                    0.0623 78.65 < 2e-16
##
## Scale= 134
##
## Gaussian distribution
## Loglik(model) = -812.9
                         Loglik(intercept only) = -838.9
## Chisq= 51.93 on 8 degrees of freedom, p= 1.7e-08
## Number of Newton-Raphson Iterations: 4
## n= 137
The logistic distribution:
log.lung<- survreg(Surv(Y,C)~Treat + PS + factor(Cell)+ factor(Cell)*Treat, data = lungcancer.df, dist
summary(log.lung)
## Call:
## survreg(formula = Surv(Y, C) ~ Treat + PS + factor(Cell) + factor(Cell) *
      Treat, data = lungcancer.df, dist = "logistic")
##
                           Value Std. Error
                                                7.
## (Intercept)
                                   66.5457 -0.97
                                                    0.330
                        -64.8773
## Treat
                        61.0223
                                    41.3046 1.48
                                                    0.140
                                    0.4323 5.13 2.9e-07
## PS
                         2.2173
## factor(Cell)2
                        29.4146
                                    75.4299 0.39
                                                    0.697
## factor(Cell)3
                        12.4711
                                    87.4283 0.14
                                                    0.887
## factor(Cell)4
                        133.4692
                                    88.8767 1.50
                                                    0.133
## Treat:factor(Cell)2 -74.4211
                                   49.5567 -1.50
                                                    0.133
## Treat:factor(Cell)3 -66.3060 54.2281 -1.22
                                                    0.221
## Treat:factor(Cell)4 -100.6961 57.2654 -1.76
                                                    0.079
## Log(scale)
                         4.0678
                                   0.0774 52.56 < 2e-16
##
## Scale= 58.4
##
## Logistic distribution
## Loglik(model) = -790.9
                          Loglik(intercept only) = -816.8
## Chisq= 51.85 on 8 degrees of freedom, p= 1.8e-08
## Number of Newton-Raphson Iterations: 5
## n= 137
The lognormal distribution:
lognorm.lung<- survreg(Surv(Y,C)~Treat + PS + factor(Cell)+ factor(Cell)*Treat, data = lungcancer.df, d
summary(lognorm.lung)
```

##

```
## Call:
## survreg(formula = Surv(Y, C) ~ Treat + PS + factor(Cell) + factor(Cell) *
      Treat, data = lungcancer.df, dist = "lognormal")
##
                        Value Std. Error
## (Intercept)
                      2.37802
                                0.66720 3.56 0.00036
## Treat
                     -0.05468
                                0.37890 -0.14 0.88525
## PS
                      0.03691
                              0.00484 7.63 2.4e-14
## factor(Cell)2
                     -0.20063
                                0.78272 -0.26 0.79770
## factor(Cell)3
                     -1.09485
                                0.98365 -1.11 0.26569
## factor(Cell)4
                     0.42049 0.90826 0.46 0.64339
## Treat:factor(Cell)2 -0.25271
                              0.49801 -0.51 0.61184
                              0.58019 0.46 0.64503
## Treat:factor(Cell)3 0.26728
## Log(scale)
                      0.06496
                                0.06257 1.04 0.29920
##
## Scale= 1.07
##
## Log Normal distribution
## Loglik(model) = -715.4
                       Loglik(intercept only) = -749.5
## Chisq= 68.2 on 8 degrees of freedom, p= 1.1e-11
## Number of Newton-Raphson Iterations: 4
## n= 137
The log-logistic distribution:
loglog.lung<- survreg(Surv(Y,C)~Treat + PS + factor(Cell)+ factor(Cell)*Treat, data = lungcancer.df, di
summary(loglog.lung)
##
## Call:
## survreg(formula = Surv(Y, C) ~ Treat + PS + factor(Cell) + factor(Cell) *
      Treat, data = lungcancer.df, dist = "loglogistic")
##
                       Value Std. Error
                                          Z
                                0.6670 3.58 0.00035
## (Intercept)
                      2.3864
## Treat
                      0.0884
                                0.3848 0.23 0.81825
## PS
                      0.0353
                                0.0045 7.86 3.9e-15
## factor(Cell)2
                     -0.4157
                                0.7736 -0.54 0.59106
## factor(Cell)3
                     -0.8561
                                0.9160 -0.93 0.35001
## factor(Cell)4
                      0.5365
                                0.8665 0.62 0.53581
## Treat:factor(Cell)3 0.0431 0.5464 0.08 0.93714
## Treat:factor(Cell)4 -0.3741 0.5377 -0.70 0.48651
## Log(scale)
                    -0.5450
                               0.0741 -7.35 2.0e-13
##
## Scale= 0.58
## Log logistic distribution
## Loglik(model) = -712.2 Loglik(intercept only) = -750.3
## Chisq= 76.22 on 8 degrees of freedom, p= 2.8e-13
## Number of Newton-Raphson Iterations: 4
## n= 137
```

From the loglikelihood and the number of parameters k in the different distributions we can caluclate the AIC (Akaike's Information Criterion) by the equation

$$AIC = -2 \cdot logL + 2 \cdot k$$

Table 5: Estimated Relative Risk of test treatment compared to standard treatment in the different Cell-types.

Distribution	AIC	
weibull	1516.182	
exponential	1502.442	
gaussian	1677.777	
logistic	1633.620	
lognormal	1498.948	
loglogistic	1500.532	