CENG 201 Veri Yapıları 5: Dengeli Ağaçlar

Öğr.Gör. Şevket Umut ÇAKIR

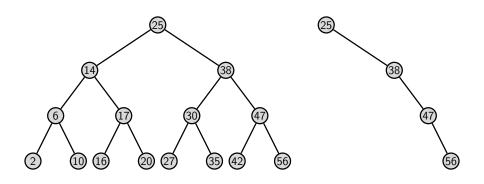
Pamukkale Üniversitesi

Hafta 5

Anahat

AVL Ağaçları AVL Ağaçları Tanım AVL Ağacı Ekleme Silme

Dengeli Ağaçlar



 Yukardaki n elemanlı ikili arama ağaçlarda arama ve ekleme işlemleri en iyi ve en kötü durumda kaç adımda yapılır?

- İsmini geliştiricileri olan Adelson-Velskii ve Landis'den almıştır
- Dengeli bir ikili arama ağacıdır
- Dengeleme işlemi ekleme ve silme sırasında yapılır
- Her düğüm için denge faktörü -1'den küçük veya 1'den büyük olamaz
- Denge faktörü bir düğümün hangi yöne yatık olduğunu gösterir

Denge Faktörü

Yükseklik

Bir düğümün yüksekliği düğüm ile soyundan gelen yapraklardan en uzağı arasındaki mesafedir.

Denge Faktörü

Sağ çocuğun yüksekliği ile sol çocuğun yüksekliği arasındaki farktır.

AVL Ağaçları Tanım

Denge Faktörü/Balance Factor

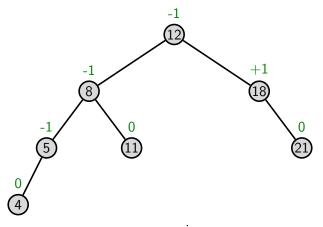


Figure: AVL Ağacı(Dengeli İkili Arama Ağacı)

Denge Faktörü/Balance Factor

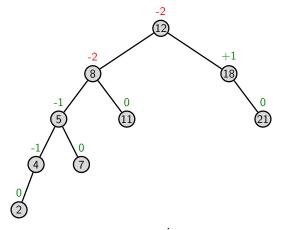
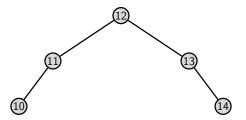


Figure: AVL Ağacı(Dengeli İkili Arama Ağacı)



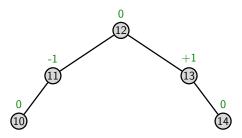
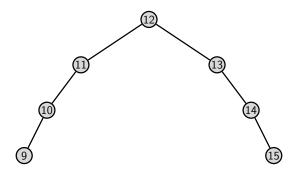


Figure: AVL Ağacıdır



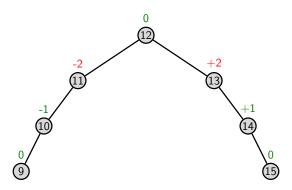


Figure: AVL Ağacı değildir

Ekleme

- Ekleme işlemi ikili arama ağaçlarındaki gibidir
- Ekleme işlemi sırasında denge bozulabilir
- Dengesi bozulan düğümler eklenen düğümden köke kadarki yolda olacaktır
- Dengenin tekrar sağlanması için döndürme işlemleri yapılır
- 4 farklı durum ortaya çıkabilir
- Tekli veya ikili döndürme ile ağaç tekrar dengelenir

Ekleme

- 4 farklı ekleme biçiminden ötürü denge bozulmuş olabilir:
 - \bullet 'nın sol çocuğunun soluna ekleme
 - $\mathbf{2} \alpha$ 'nın sol çocuğunun sağına ekleme
 - $oldsymbol{3}$ lpha'nın sağ çocuğunun soluna ekleme
 - $\mathbf{4}$ α 'nın sağ çocuğunun sağına ekleme
- Durum 1 ve 4 tekli döndürme ile düzeltilebilir
- Durum 2 ve 3 için çift döndürme gereklidir

Tekli Döndürme(Sağa)

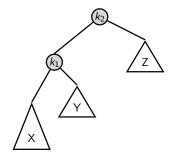


Figure: Durum 1'in çözümü

Tekli Döndürme(Sağa)

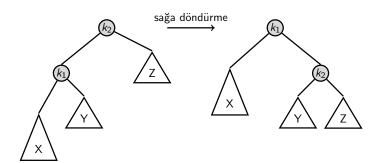
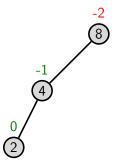
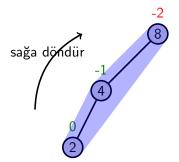
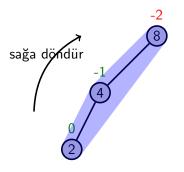
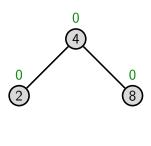


Figure: Durum 1'in çözümü









Tekli Döndürme(Sola)

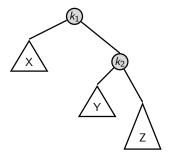


Figure: Durum 4'ün çözümü

Tekli Döndürme(Sola)

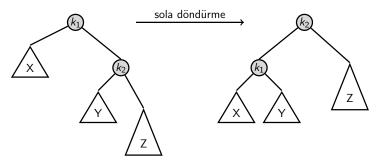
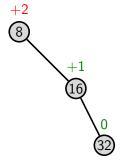
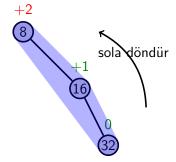
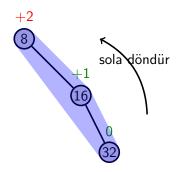
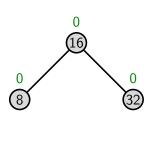


Figure: Durum 4'ün çözümü









Çift Döndürme(sol, sağ)

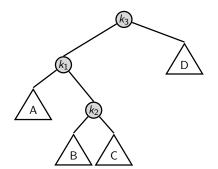


Figure: Durum 2'nin çözümü

Çift Döndürme(sol, sağ)

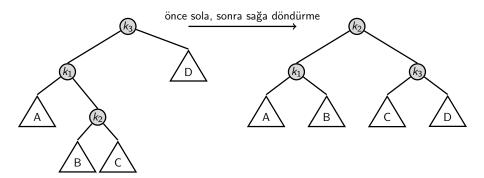
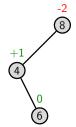
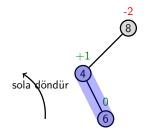
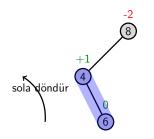
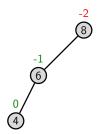


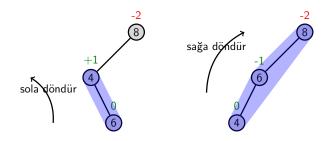
Figure: Durum 2'nin çözümü

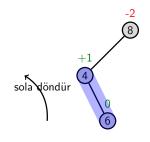


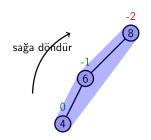


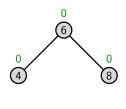












Çift Döndürme(sağ, sol)

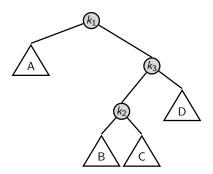


Figure: Durum 3'ün çözümü

Çift Döndürme(sağ, sol)

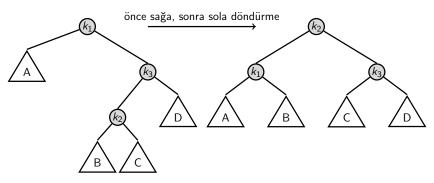
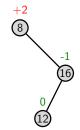
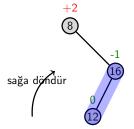
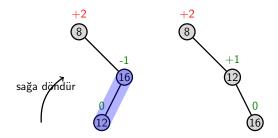
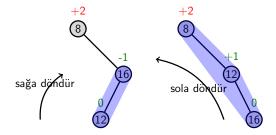


Figure: Durum 3'ün çözümü

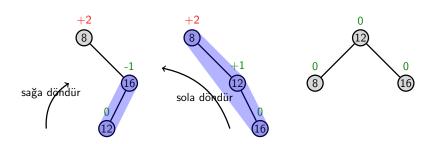








Durum 3 Örnek



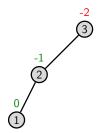
Bir AVL ağacına 3, 2, 1, 4, 5, 6, 7, 16, 15, 14, 13, 12, 11, 10, 8, 9 değerlerini sırasıla ekleyelim.



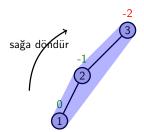
AVL Ağacı Ekleme

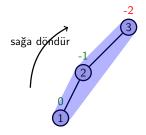


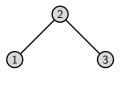
AVL Ağacı Ekleme

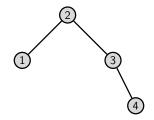


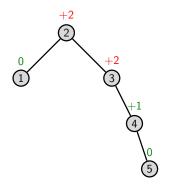
AVL Ağacı Ekleme

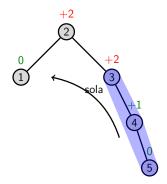


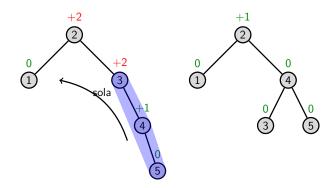












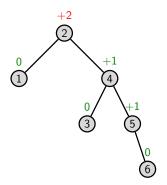


Figure: Sola döndür

AVL Ağacı Ekleme

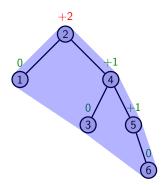


Figure: Sola döndür

AVL Ağacı Ekleme

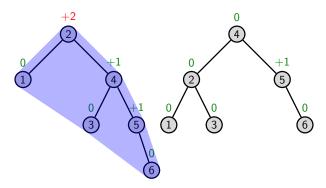


Figure: Sola döndür

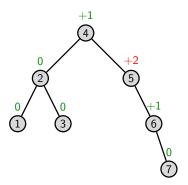


Figure: Sola döndür

AVL Ağacı Ekleme

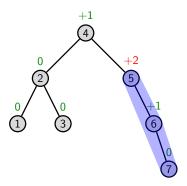


Figure: Sola döndür

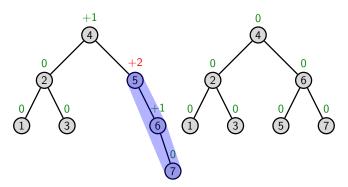
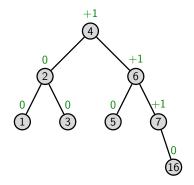


Figure: Sola döndür



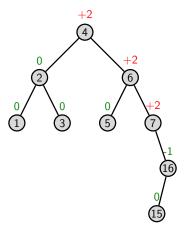
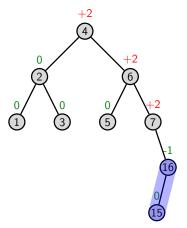


Figure: Mavi sağa, sonra kırmızı sola 🗇 🗀 👢 🗸 🔍 🤉 🕻



AVL Ağacı Ekleme

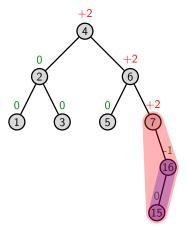
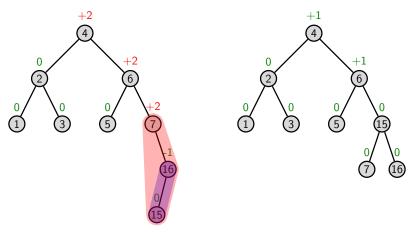


Figure: Mavi sağa, sonra kırmızı sola



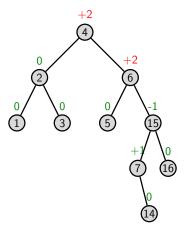
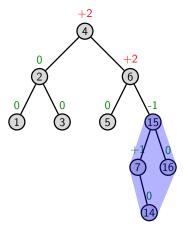


Figure: Mavi sağa, sonra kırmızı sola



AVL Ağacı Ekleme

14 Ekle

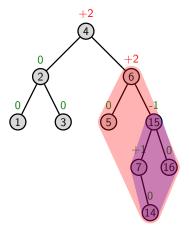
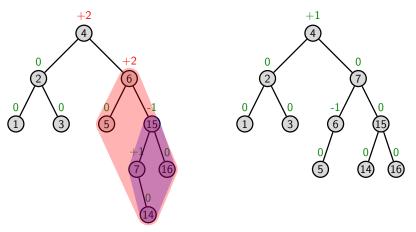


Figure: Mavi sağa, sonra kırmızı sola



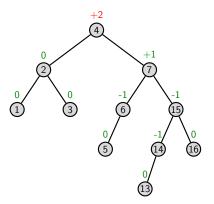


Figure: Tüm ağacı sola döndür

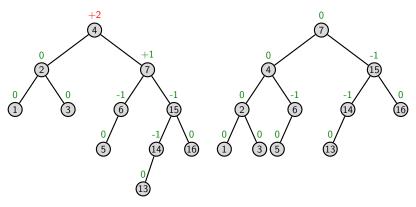


Figure: Tüm ağacı sola döndür

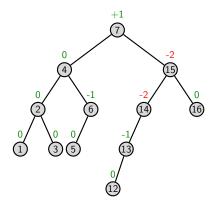


Figure: Sağa döndür

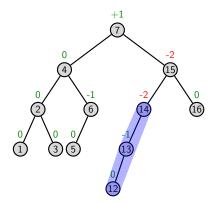


Figure: Sağa döndür

AVL Ağacı Ekleme

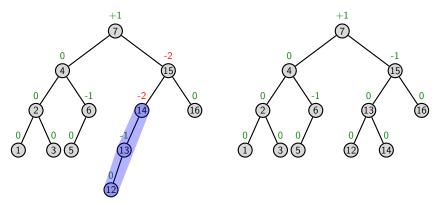


Figure: Sağa döndür

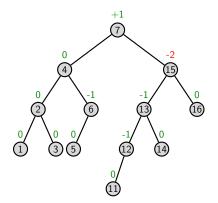


Figure: Sağa döndür

AVL Ağacı Ekleme

11 Ekle

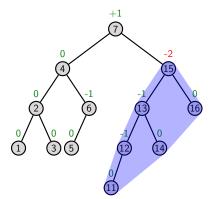


Figure: Sağa döndür

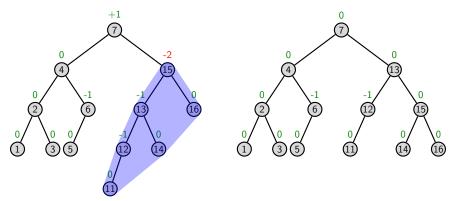


Figure: Sağa döndür

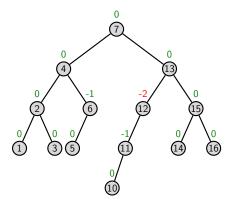


Figure: Sağa döndür

AVL Ağacı Ekleme 10 Ekle

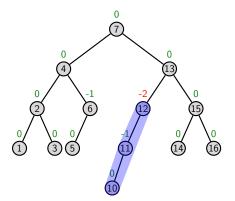


Figure: Sağa döndür

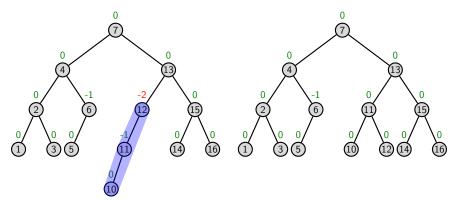


Figure: Sağa döndür

AVL Ağacı Ekleme

8 Ekle

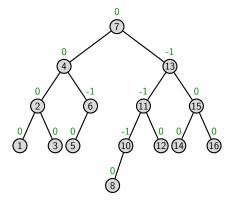
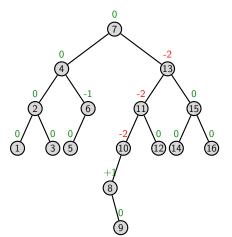
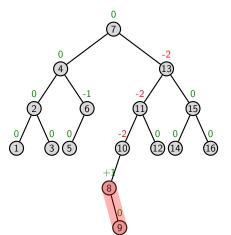
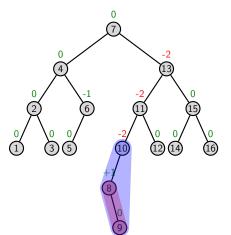
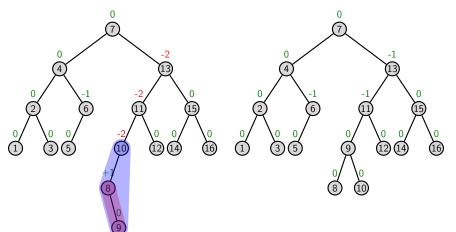


Figure: Sağa döndür









Soru

13, 21, 45, 8, 10, 65, 7, 4, 16, 46, 15 değerlerini sırasıyla AVL ağacına ekleyin.

AVL Ağacı Ekleme

Soru

13, 21, 45, 8, 10, 65, 7, 4, 16, 46, 15 değerlerini sırasıyla AVL ağacına ekleyin.

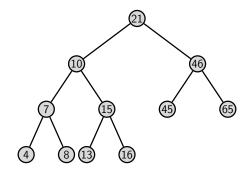


Figure: Değerler eklenince ortaya çıkan AVL Ağacı

Silme İşlemi

- Silinecek düğüm w olsun
- w düğümünü ikili arama ağacındaki gibi sil
- w'dan köke doğru ilk dengesiz z düğümünü bul
- y, z'nin yüksek çocuğu olsun
- x, y'nin yüksek çocuğu olsun
- 4 farklı durum ortaya çıkmaktadır

Sol'un solu durumu

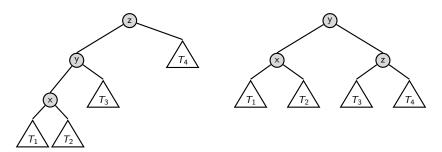


Figure: Sağa döndürme

Sol'un sağı durumu

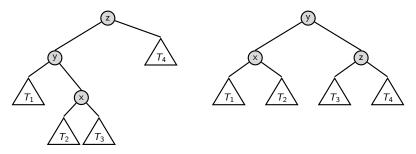


Figure: Önce sola sonra sağa döndürme

Sağ'ın sağı durumu

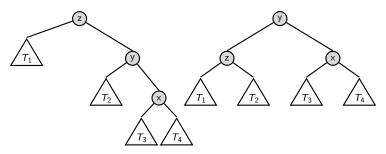


Figure: Sola döndürme

Sağ'ın solu durumu

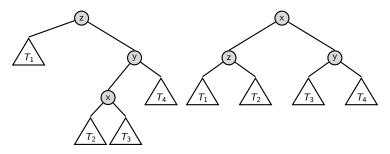
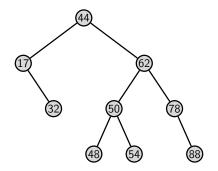


Figure: Önce sağa sonra sola döndürme



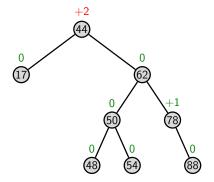


Figure: Sola döndürme

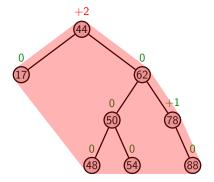


Figure: Sola döndürme

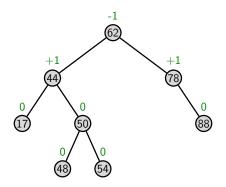


Figure: 32 silindikten sonra ağaç dengelendi

Görselleştirme

- https: //www.cs.usfca.edu/~galles/visualization/AVLtree.html
- https://visualgo.net/bn/bst

Silme

THE MAIN PRINCIPLES OF SOFTWARE ENGINEERING

PART 1

