

l) $A + ((B - C * D) / E) + F - G / H$

1- Infix to Postfix

1- Convert

Token	Operation	Stack	Postfix
A	Pass operand to out		A
+	Pass operator to stack if stack is empty	+	A
(Pass left parenthesis into stack	+, (A
(Pass left parenthesis into stack	+, (, (A
B	Pass operand to out	+, (, (A B
-	Pass all operators down to first left parenthesis that have higher or equal precedence into stack and push token into stack	+, (, (, -	A B
C	Pass operand to out	+, (, (, -	A B C
*	Pass all operators down to first left parenthesis that have higher or equal precedence into stack and push token into stack	+, (, (, -, *	A B C
D	Pass operand to out	+, (, (, -, *	A B C D
)	Pass all operators down to first left parenthesis to out	+, (A B C D * -
/	Pass all operators down to first left parenthesis that have higher or equal precedence into stack and push token into stack	+, (, /	A B C D * -
E	Pass operand to out	+, (, /	A B C D * - E
)	Pass all operators down to first left parenthesis to out	+	A B C D * - E /
+	Pass all operators down to first left parenthesis that have higher or equal precedence into stack and push token into stack	+	A B C D * - E / +
F	Pass operand to out	+	A B C D * - E / + F
-	Pass all operators down to first left parenthesis that have higher or equal precedence into stack and push token into stack	-	A B C D * - E / + F +
G	Pass operand to out	-	A B C D * - E / + F + G
/	Pass all operators down to first left parenthesis that have higher or equal precedence into stack and push token into stack	- /	A B C D * - E / + F + G
H	Pass operand to out	- /	A B C D * - E / + F + G H
			A B C D * - E / + F + G H / -

2- Evaluate

Infix notation: $A + ((B - C * D) / E) + F - G / H$

Postfix notation: $A B C D * - E / + F + G H / -$

Let $A = 6$, $B = 12$, $C = 2$, $D = 1$, $E = 5$, $F = 8$, $G = 9$, $H = 3$

Infix notation: $6 + ((12 - 2 * 1) / 5) + 8 - 9 / 3$

Postfix notation: $6 12 2 1 * - 5 / + 8 + 9 3 / -$

$6 12 2 1 * - 5 / + 8 + 9 3 / -$	$2 1 *$	$6 12 \textcolor{red}{2} - 5 / + 8 + 9 3 / -$
$6 12 2 - 5 / + 8 + 9 3 / -$	$12 2 -$	$6 \textcolor{red}{10} 5 / + 8 + 9 3 / -$
$6 10 5 / + 8 + 9 3 / -$	$10 5 /$	$6 \textcolor{red}{2} + 8 + 9 3 / -$
$6 2 + 8 + 9 3 / -$	$6 2 +$	$\textcolor{red}{8} 8 + 9 3 / -$
$8 8 + 9 3 / -$	$8 8 +$	$\textcolor{red}{16} 9 3 / -$
$16 9 3 / -$	$9 3 /$	$16 \textcolor{red}{3} -$
$16 3 -$	$16 3 -$	$\textcolor{red}{13}$

2- Infix to Prefix

1- Convert

Reverse infix: $H / G - F + (E / (D * C - B)) + A$

Token	Operation	Stack	Postfix
H	Pass operand to out		H
/	Pass operator to stack if stack is empty	/	H
G	Pass operand to out	/	H G
-	Pass all operators down to first left parenthesis that have higher or equal precedence into stack and push token into stack	-	H G /
F	Pass operand to out	-	H G / F
+	Pass all operators down to first left parenthesis that have higher or equal precedence into stack and push token into stack	+	H G / F -
(Pass left parenthesis into stack	+, (H G / F -
E	Pass operand to out	+, (H G / F - E
/	Pass all operators down to first left parenthesis that have higher or equal precedence into stack and push token into stack	+, (/	H G / F - E
(Pass left parenthesis into stack	+, (/ (H G / F - E
D	Pass operand to out	+, (/ (H G / F - E D
*	Pass all operators down to first left parenthesis that have higher or equal precedence into stack and push token into stack	+, (/ (*	H G / F - E D
C	Pass operand to out	+, (/ (*	H G / F - E D C
-	Pass all operators down to first left parenthesis that have higher or equal precedence into stack and push token into stack	+, (/ (-	H G / F - E D C *
B	Pass operand to out	+, (/ (-	H G / F - E D C * B
)	Pass all operators down to first left parenthesis to out	+, (/	H G / F - E D C * B -
)	Pass all operators down to first left parenthesis to out	+	H G / F - E D C * B - /
+	Pass all operators down to first left parenthesis that have higher or equal precedence into stack and push token into stack	+	H G / F - E D C * B - / +
A	Pass operand to out	+	H G / F - E D C * B - / + A
			H G / F - E D C * B - / + A +

Reverse expression: $+ A + / - B * C D E - F / G H$

2- Evaluate

Infix notation: $A + ((B - C * D) / E) + F - G / H$

Prefix notation: $+ A + / - B * C D E - F / G H$

Let $A = 6$, $B = 12$, $C = 2$, $D = 1$, $E = 5$, $F = 8$, $G = 9$, $H = 3$

Infix notation: $6 + ((12 - 2 * 1) / 5) + 8 - 9 / 3$

Prefix notation: $+ 6 + / - 12 * 2 1 5 - 8 / 9 3$

$+ 6 + / - 12 * 2 1 5 - 8 / 9 3$	$/ 9 3$	$+ 6 + / - 12 * 2 1 5 - 8 \textcolor{red}{3}$
$+ 6 + / - 12 * 2 1 5 - 8 3$	$- 8 3$	$+ 6 + / - 12 * 2 1 \textcolor{red}{5}$
$+ 6 + / - 12 * 2 1 5 5$	$* 2 1$	$+ 6 + / - 12 \textcolor{red}{2} 5 5$
$+ 6 + / - 12 2 5 5$	$- 12 2$	$+ 6 + / \textcolor{red}{10} 5 5$
$+ 6 + / 10 5 5$	$/ 10 5$	$+ 6 + \textcolor{red}{2} 5$
$+ 6 + 2 5$	$+ 2 5$	$+ 6 \textcolor{red}{7}$
$+ 6 7$	$+ 6 7$	$\textcolor{red}{13}$

II) ! (A && ! ((B < C) || (C > D))) || (C < E)

1- Infix to Postfix

1- Convert

Token	Operation	Stack	Postfix
!	Pass operator to stack	!	
(Pass left parenthesis into stack	!, (
A	Pass operand to out	!, (A
&&	Pass operator to stack	!, (, &&	A
!	Pass operator to stack	!, (, &&, !	A
(Pass left parenthesis into stack	!, (, &&, !, (A
(Pass left parenthesis into stack	!, (, &&, !, (, (A
B	Pass operand to out	!, (, &&, !, (, (A B
<	Pass operator to stack	!, (, &&, !, (, (, <	A B
C	Pass operand to out	!, (, &&, !, (, (, <	A B C
)	Pass all operators down to first left parenthesis to out	!, (, &&, !, (A B C <
	Pass operator to stack	!, (, &&, !, (,	A B C <
(Pass left parenthesis into stack	!, (, &&, !, (, , (A B C <
C	Pass operand to out	!, (, &&, !, (, , (A B C < C
>	Pass operator to stack	!, (, &&, !, (, , (, >	A B C < C
D	Pass operand to out	!, (, &&, !, (, , (, >	A B C < C D
)	Pass all operators down to first left parenthesis to out	!, (, &&, !, (,	A B C < C D >
)	Pass all operators down to first left parenthesis to out	!, (, &&	A B C < C D > !
)	Pass all operators down to first left parenthesis to out		A B C < C D > ! && !
	Pass operator to stack		A B C < C D > ! && !
(Pass left parenthesis into stack	, (A B C < C D > ! && !
C	Pass operand to out	, (A B C < C D > ! && ! C
<	Pass operator to stack	, (, <	A B C < C D > ! && ! C
E	Pass operand to out	, (, <	A B C < C D > ! && ! C E
)	Pass all operators down to first left parenthesis to out		A B C < C D > ! && ! C E <
			A B C < C D > ! && ! C E <

2- Evaluate

Infix notation: $!(A \&\& !((B < C) \parallel (C > D))) \parallel (C < E)$

Postfix notation: $A B C < C D > \parallel ! \&\& ! C E < \parallel$

Let $A = 1, B = 2, C = 3, D = 5, E = 3$

Infix notation: $!(1 \&\& !((2 < 3) \parallel (3 > 5))) \parallel (3 < 3)$

Postfix notation: $1 2 3 < 3 5 > \parallel ! \&\& ! 3 3 < \parallel$

1 2 3 < 3 5 > $\parallel ! \&\& ! 3 3 < \parallel$	2 3 <	1 1 3 5 > $\parallel ! \&\& ! 3 3 < \parallel$
1 1 3 5 > $\parallel ! \&\& ! 3 3 < \parallel$	3 5 >	1 1 0 $\parallel ! \&\& ! 3 3 < \parallel$
1 1 0 $\parallel ! \&\& ! 3 3 < \parallel$	1 0 \parallel	1 1 $\&\& ! 3 3 < \parallel$
1 1 $\&\& ! 3 3 < \parallel$	1 !	1 0 $\&\& ! 3 3 < \parallel$
1 0 $\&\& ! 3 3 < \parallel$	1 0 $\&\&$	0 $\&\& ! 3 3 < \parallel$
0 $\&\& ! 3 3 < \parallel$	0 !	1 $\&\& ! 3 3 < \parallel$
1 3 3 < \parallel	3 3 <	1 0 \parallel
1 0 \parallel	1 0 \parallel	1

2- Infix to Prefix

1- Convert

Reverse infix: (E > C) || !((D < C) || (C > B)) && A

Token	Operation	Stack	Postfix
(Pass left parenthesis into stack	(
E	Pass operand to out	(E
>	Pass operator to stack	(, >	E
C	Pass operand to out	(, >	E C
)	Pass all operators down to first left parenthesis to out		E C >
	Pass operator to stack		E C >
!	Pass operator to stack	, !	E C >
(Pass left parenthesis into stack	, !, (E C >
!	Pass operator to stack	, !, (, !	E C >
(Pass left parenthesis into stack	, !, (, !, (E C >
(Pass left parenthesis into stack	, !, (, !, (, (E C >
D	Pass operand to out	, !, (, !, (, (E C > D
<	Pass operator to stack	, !, (, !, (, (, <	E C > D
C	Pass operand to out	, !, (, !, (, (, <	E C > D C
)	Pass all operators down to first left parenthesis to out	, !, (, !, (E C > D C <
	Pass operator to stack	, !, (, !, (,	E C > D C <
(Pass left parenthesis into stack	, !, (, !, (, , (E C > D C <
C	Pass operand to out	, !, (, !, (, , (E C > D C < C
>	Pass operator to stack	, !, (, !, (, , (, >	E C > D C < C
B	Pass operand to out	, !, (, !, (, , (, >	E C > D C < C B
)	Pass all operators down to first left parenthesis to out	, !, (, !, (,	E C > D C < C B >
)	Pass all operators down to first left parenthesis to out	, !, (E C > D C < C B > !
&&	Pass operator to stack	, !, (, &&	E C > D C < C B > !
A	Pass operand to out	, !, (, &&	E C > D C < C B > ! A
)	Pass all operators down to first left parenthesis to out		E C > D C < C B > ! A && !
			E C > D C < C B > ! A && !

Reverse expression: || ! && A ! || < B C > C D < C E

2- Evaluate

Infix notation: $!(A \&\& !((B < C) || (C > D))) || (C < E)$

Prefix notation: $|| ! \&\& A ! || < B C > C D < C E$

Let $A = 1, B = 2, C = 3, D = 5, E = 3$

Infix notation: $!(1 \&\& !((2 < 3) || (3 > 5))) || (3 < 3)$

Prefix notation: $|| ! \&\& 1 ! || < 2 3 > 3 5 < 3 3$

$! \&\& 1 ! < 2 3 > 3 5 < 3 3$	$< 3 3$	$! \&\& 1 ! < 2 3 > 3 5 \textcolor{red}{0}$
$! \&\& 1 ! < 2 3 > 3 5 0$	$> 3 5$	$! \&\& 1 ! < 2 3 \textcolor{red}{0} 0$
$! \&\& 1 ! < 2 3 0 0$	$< 2 3$	$! \&\& 1 ! \textcolor{red}{1} 0 0$
$! \&\& 1 ! 1 0 0$	$ 1 0$	$! \&\& 1 ! \textcolor{red}{1} 0$
$! \&\& 1 ! 1 0$	$! 1$	$! \&\& 1 \textcolor{red}{0} 0$
$! \&\& 1 0 0$	$\&\& 1 0$	$! \textcolor{red}{0} 0$
$! 0 0$	$! 0$	$ \textcolor{red}{1} 0$
$ 1 0$	$ 1 0$	$\textcolor{red}{1}$