1-10的奇数题,11-20的偶数题 9.1 Pf: f(0) = 0 & $f(\pi)$ is continuous at 0. 9.3 Pf: fix) = constant Suppose that f is a periodic function s.t. S f(x+T)=f(x), YXEIR for some T>0

Lim f(x)= C exists. Then fIX+NT) YNEN = lim fixthT) = lim +1x) = C YX EIR A. 9.5. Obvious 9.7 1. (1). (1) xE/N f(0) = f(0) + f(0) => f(0) =0 $\forall x > 1, f(x) = f(\sum_{k=1}^{\infty} 1) = \sum_{k=1}^{\infty} f(x) = x \cdot \alpha$ ②ガ(及) If $x \le 0$, then $f(x) + f(-x) = f(0) \Rightarrow f(x) = f(0) - f(-x) = f(0) - \alpha \cdot (-x) = \alpha x$

 $f(p) = f(q \cdot \frac{p}{q}) = q \cdot f(\frac{p}{q}) \Rightarrow f(\frac{p}{q}) = \frac{1}{q} \cdot f(p) = \frac{1}{q} \cdot p \cdot \alpha = \frac{p}{q} \alpha$

3 7= PEQ

(2) Since Q is dense in |R|, $\forall \pi \in |R|$, $\exists \{\pi_n\} \subseteq Q \text{ s.t. } \forall n \neq \pi$, then $f(\pi) = \lim_{\pi \to \pi} d \cdot \pi = d \cdot \pi.$

9.9

Pt: Obvious

9.12.

Pf. Xty Sin X

9.14

14: Since lim fix = lim fix = +00, = M>0 s.t.

f(x) > f(o), 4 /2/ > M

 \Rightarrow f(x) > inf f(x), $\forall x \in \mathbb{R}$

=) inf fix) = inf xerminj fix)

which can be achived at some point xoet-M,M].

9.lb.

Pf: Since fig is continuous, Y x1, x2 e1R, I t1, t2 e[011] s.t.

(1/2)= fit2)+x29(t2).

9(1/1) - 9(1/2) = f(t) + x, g(t) - f(t) - x2 g(t)

= f(ti)+729(ti)-f(ti)-129(ti)+719(ti)-729(t)

= fiti)+ 1/2 glti) - gup (fit)+2/9 pt) + (7/1-7/2) glti)

(1/1)- (1/12) = f(t)+7,9(t)-f(t)-729(t) = Sup fit)+ x1 gtt) - (fiti)+x1giti) +(x1-x1) giti) > - Sup | 9(t) | · / x1 - x2 14(x1) - 4(x2) = sup g · / x1 - x2), /x1, x2 & 12 \Rightarrow 0 9.18 Pt: Define f: S O Q 9.20. #: f is uniformly continuous => For &=1, 3 8>0 S.t. 7/21-72/<8, we have |f/x1)-f/22)/</ Yn>0, ∃ Re/N s.t. 76[ks, (b+1)8], then /f17) - f10) = |f1x|-flp&) + | = f(1k+1)&)-flp&) $\leq |+k\cdot| = k+| = \frac{k+1}{ks} \cdot ks \leq \frac{k+1}{ks} \cdot \pi \leq \frac{\pi}{s}$ In a similar way, \ta<0, |fix)-fix) \leq \frac{2}{5}. Has = 1/10) + (2) =) **口** .