

Pullback / vjp rule of scalar multiplication

$$f(x, y) = x \cdot y = z$$

$$f: \mathbb{R} \times \mathbb{R} \rightarrow \mathbb{R}$$

$$\bar{x} = \bar{z} \frac{\partial f}{\partial x} = \bar{z} y$$

$$\bar{y} = \bar{z} \frac{\partial f}{\partial y} = \bar{z} x$$

$$\mathcal{B}(\cdot, (x, y), (\bar{z})) = (\underbrace{(x \cdot y)}_z, (\underbrace{\bar{z} y}_x, \underbrace{\bar{z} x}_y))$$