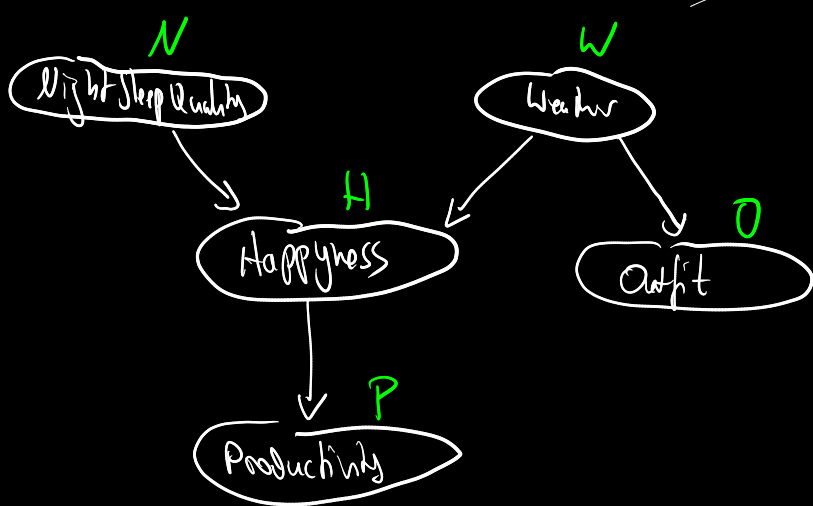


# Directed Graphical Models

## D-Separated / Conditional Independence

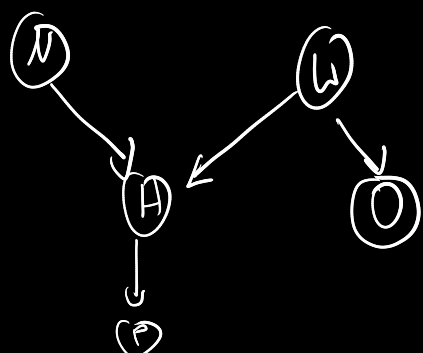
(latent & observed nodes)



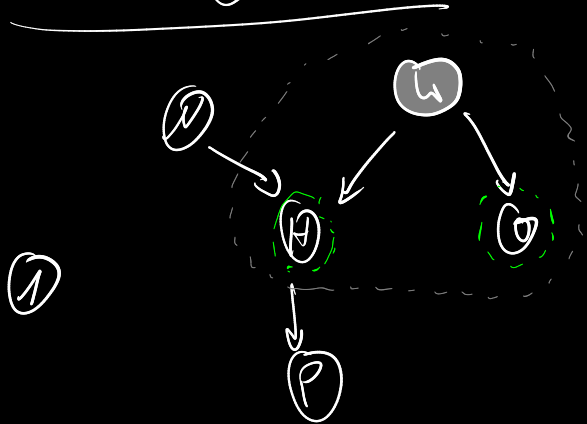
DGM

↳ factorize the joint

distributions between nodes in the graph?



question: if we only observe  $W$   
can we say sth about relationships between other nodes

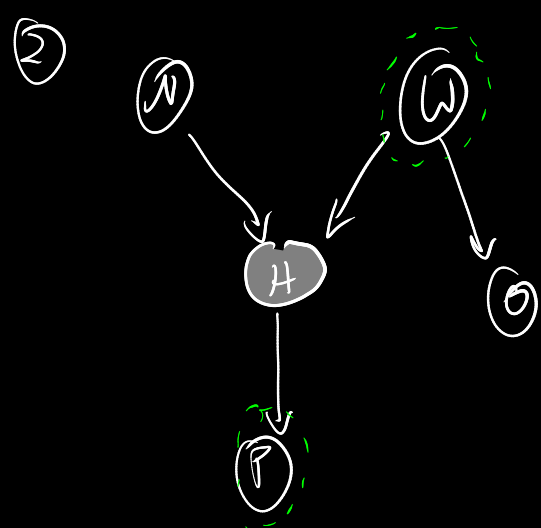


→ conditional independence between  $H$  and  $O$  given  $W$   
(→ d-separated)

$$p(H, O | W) = p(H | W) p(O | W)$$

[not marginal independence  
 $p(H, O) \neq p(H) p(O)$ ]

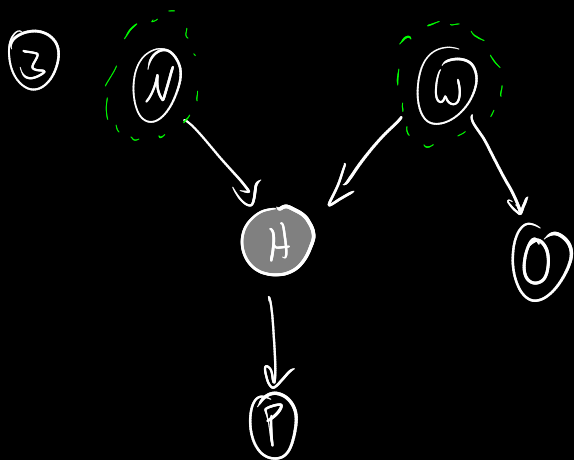
$p(N, W, H, O, P)$   
marginalization



$W$  is conditionally independent of  $P$  given  $H$

$$p(W, P | H) = p(W | H) p(P | H)$$

express by Bayes Rule

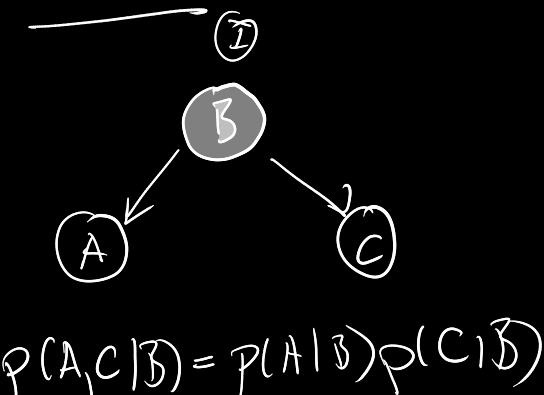


$$p(N, W | H) \neq p(N | H) p(W | H)$$

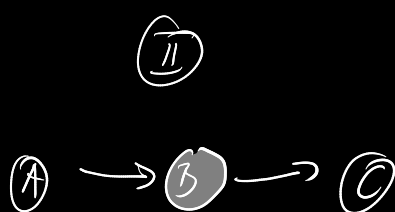
↳ Simpson's Paradox  
(→ read Wikipedia)

if we know the random variable caused by two other, then those two are no longer independent

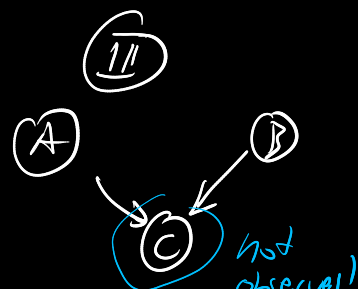
### Basic Rules



$$p(A, C | B) = p(A | B) p(C | B)$$



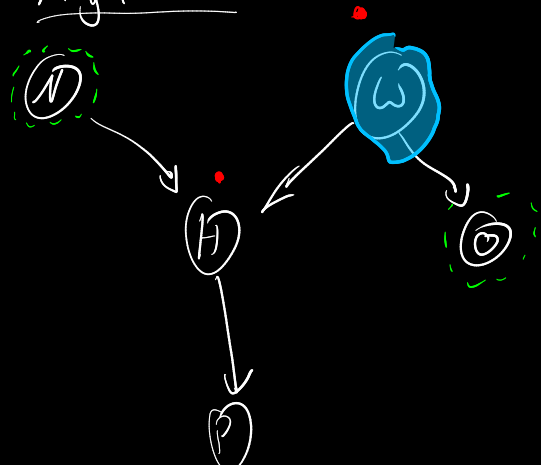
$$p(A, C | B) = p(A | B) p(C | B)$$



$$p(A, B) = p(A) p(B)$$

"both A & B are roots"

### Algorithm



① Mark the givens  
e.g.  $W$

② Apply Basic rules to all tripts

③ check if there is a path between random variables that is not blocked (undirected)  
e.g.  $N$  &  $P$  are d-separated given  $W$