Module 6: Fellegi-Sunter Method

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joint with Olivier Binette

Reading

- Binette and Steorts (2020)
- Newcombe et al. (1959)
- Fellegi and Sunter (1969)

Agenda

- Soundex algorithm
- Newcombe algorithm
- Fellegi and Sunter method

Load R Packages

```r
knitr::opts_chunk$set(echo = TRUE,
                      fig.width=4, fig.height=3,
                      fig.align="center")
library(RecordLinkage)
library(blink)
library(phonics)
source("../../code/runFS.R")
source("../../code/evaluationMetrics.R")
source("../../code/evaluate.R")
```

Background

- Soundex algorithm
- Likelihood ratio tests (LRT)

Soundex

Soundex is a phonetic algorithm for indexing names by sound, as pronounced in English.

- The goal is for similar words to be encoded to the same representation so that they can be matched despite minor differences in spelling.
- The Soundex algorithm was one of the first types of blocking used to our knowledge since it's intuitive and easy to use.

Example of Soundex algorithm

```r
soundex("Rebecca")
```

```
## [1] "R120"
```

```r
soundex("Rebekah")
```

```
## [1] "R120"
```

Example of Soundex algorithm

```r
soundex("Beka")
```

```
## [1] "B200"
```

```r
soundex("Becca")
```

```
## [1] "B200"
```

```r
soundex("Becky")
```

```
## [1] "B200"
```

Likelihood ratio test (LRT)

Please review or learn about LRTs if you are not familiar with these as these are the backbone of the Fellegi and Sunter method (1969).

https://www.sciencedirect.com/topics/computer-science/likelihood-ratio

Newcombe's Automatic Linkage of Vital Records

Newcombe et al. (1959). Published in *Science*:

Automatic Linkage of Vital Records*

Computers can be used to extract "follow-up" statistics of families from files of routine records.

H. B. Newcombe, J. M. Kennedy, S. J. Axford, A. P. James

Newcombe's Automatic Linkage of Vital Records

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The authors did the following:

- Stated record linkage as a statistical problem, proposing the first unsupervised probabilistic record linkage method.
- Illustrated that it could be implemented on a computer.

Newcombe's Automatic Linkage of Vital Records

Goal: Link **34,138 birth records** from 1955 in British Columbia **to 114,471 marriage records** in the preceding ten year period.

	Marriage record	Birth record
Husband's family name	Ayad	Ayot
Wife's family name	Barr	Barr
Husband's initials	J Z	J Z
Wife's initials	M T	B T
Husband's birth province	AB	AB
Wife's birth province	PE	PE

Table 1: Example of identity information from comparing marriage and birth records. This is adapted and translated from Table I of Newcombe (1969). AB and PE represent the Canadian provinces of Alberta and Prince Edward Island.

Newcombe's Automatic Linkage of Vital Records

Main contributions:

1. Sort records by the Soundex algorithm of family names.
2. When the Soundex coding agrees, an informal likelihood ratio test (LRT) determines if the record are matches/non-matches.

Newcombe's Automatic Linkage of Vital Records

The **performance of the method** was as follows:

- 10 record pairs were processed per minutes
- About 98.3% of the true matches were detected, and about 0.7% of the linked records were not actual matches.
- "by far the largest part of the effort" was the preparation of punched card files reproducing marriage records in an adequate format.

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- "by far the largest part of the effort" was the preparation of punched card files reproducing marriage records in an adequate format.

Unfortunately, we do not know exactly how the probabilities for the likelihood ratio test were computed in all cases.

Probabilistic Record Linkage

The work of Newcombe et al. (1959) led to one of the most seminal papers in the literature — Fellegi and Sunter (1969).

The Fellegi-Sunter model

Fellegi and Sunter (1969). Published in JASA:

A THEORY FOR RECORD LINKAGE*

IVAN P. FELLEGI AND ALAN B. SUNTER
Dominion Bureau of Statistics

A mathematical model is developed to provide a theoretical framework for a computer-oriented solution to the problem of recognizing those records in two files which represent identical persons, objects or events (said to be *matched*).

The Fellegi-Sunter model

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Given a pair of records, Fellegi and Sunter (1969) considers three possible actions:

- to *link* the record pairs;
- to *possibly link* the record pairs; or
- to *not link* the record pairs.

An "optimal" decision rule is proposed for this.

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We will focus on the **model** (rather than the decision-theoretic framework).

The Fellegi-Sunter model

Basic elements:

- Two *databases* A and B
  - Duplication *across* but not within databases (bipartite record linkage).
- *Records* with corresponding *attributes* or *fields*
  - Name, age, address, SSN, etc.

The Fellegi-Sunter model

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How we'll do that:

- We will consider **record pairs** from databases A and B to obtain multidimensional measures of similarity.
- Based on these **measures of similarity**, we will group records together that refer to the same entity.

The Fellegi-Sunter model

Record no.	Field 1 First name	Field 2 Last name	Field 3 Age
1	Olivier	Binette	25
2	Peter	Hoff	NA
$\vdots$	$\vdots$	$\vdots$	$\vdots$
N_1	Beka	Steorts	NA

Record no.	Field 1 First name	Field 2 Last name	Field 3 Age
1	Oliver	Binette	26
2	Brian	K	NA
$\vdots$	$\vdots$	$\vdots$	$\vdots$
N_2	Frances	Hung	NA

Is Olivier Binette the same person as Oliver Binette?

The Fellegi-Sunter model

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$$i = 1, 2, \ldots, N_1 \times N_2$$

enumerate the set of all record pairs in $A \times B$.

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- Each γ_i^j compares the jth field of the records.

Example: Let the jth field be "age." Then $\gamma_i^j = 0$ if all ages are the same and $\gamma_i^j = 1$ if ages different.

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How they're obtained:

- You choose!
- Use string distance functions to compare names.

The Fellegi-Sunter model

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Next component of the model:

- The **matching configuration** $r = \{r_j\}_{j=1}^{N_1 \times N_2}$, with $r_j = 1$ if the jth record pair matches, and $r_j = 0$ otherwise.
  - This is the adjacency list representation. We can also use a matching configuration matrix.
- This is not a very efficient representation for bipartite matching. Sadinle (2017) instead uses a *matching labeling*.

The Fellegi-Sunter model

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- For record pairs that are a ***m**atch* ($r_j = 1$), we assume that $\gamma \sim m$ independently.
- For record pairs that are ***u**nmatched* ($r_j = 0$), we assume that $\gamma \sim u$ independently.
- More precisely,

$$p\left(\{\gamma_j\}_{j=1}^{N_1 \times N_2} \mid r, m, u\right) = \left(\prod_{j\,:\,r_j=1} m(\gamma_j)\right) \times \left(\prod_{j\,:\,r_j=0} u(\gamma_j)\right).$$

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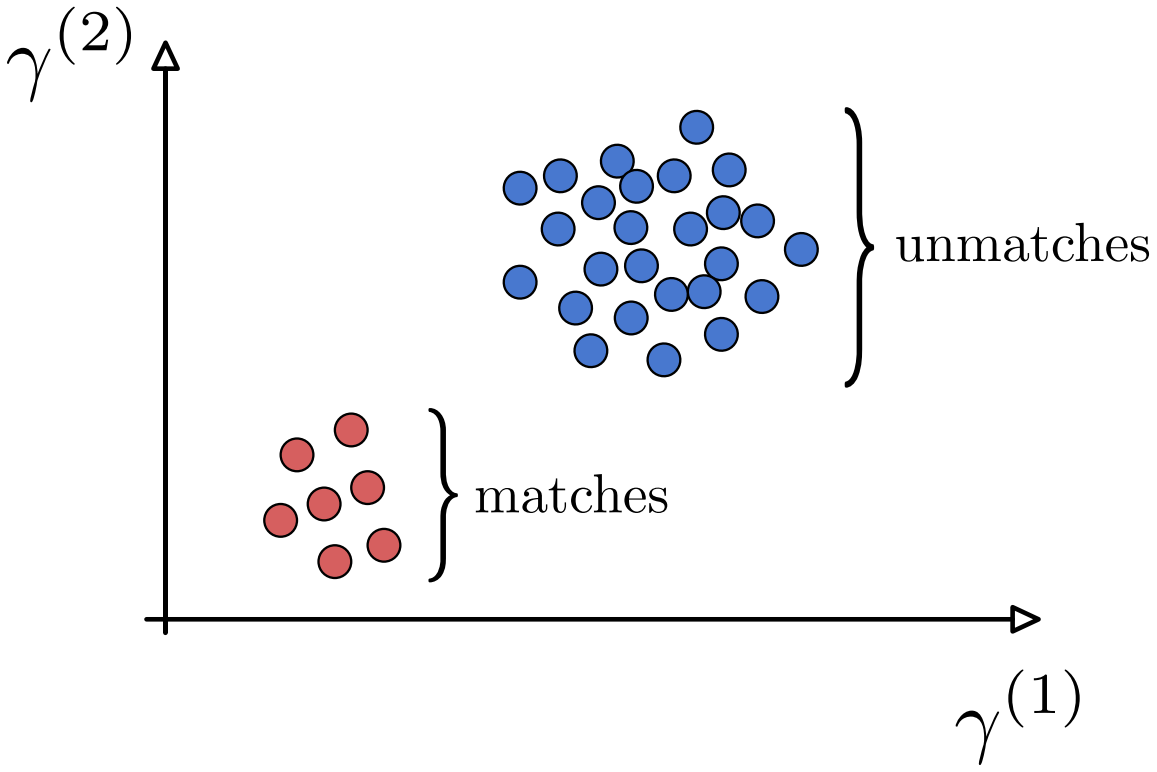

The Fellegi-Sunter model

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- Estimate model parameters.
- Define a prior $p(r, m, u)$.
- Obtain a posterior

$$
\begin{aligned}
p(r \mid \{\gamma_j\}_{j=1}^{N_1 \times N_2}) &= \int p(r, m, u \mid \{\gamma_j\}_{j=1}^{N_1 \times N_2})\, dm\, du \\
&\propto \int p(\{\gamma_j\}_{j=1}^{N_1 \times N_2} \mid r, m, u) p(r, m, u)\, dm\, du
\end{aligned}
$$

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- Then, define the log-likelihood ratio (**matching weight**)

$$W(\gamma_j) = \log \frac{m(\gamma_j)}{u(\gamma_j)}.$$

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- Originally, FS proposed to estimate m and u on their own.
- Then, define the log-likelihood ratio (**matching weight**)

$$W(\gamma_j) = \log \frac{m(\gamma_j)}{u(\gamma_j)}.$$

- Say that the jth pair is a match if $W(\gamma_j)$ is large, that they're not a match if $W(\gamma_j)$ is small: this is a likelihood ratio test.

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- You could link records a and b, and b and c, and yet say that a and c are not a match. This is incoherent.

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What's the problem with the original FS approach?

- You consider all record pairs independently.
- You could link records a and b, and b and c, and yet say that a and c are not a match. This is incoherent.
- In the *bipartite record linkage* framework, we want to specify a prior on r which reflects the fact that there is duplication across but not within databases.