

The group G is isomorphic to the projective special linear group $\text{PSL}(3,2)$.
 Ordinary character table of $G \cong \text{PSL}(3,2)$:

	$1a$	$2a$	$3a$	$4a$	$7a$	$7b$
χ_1	1	1	1	1	1	1
χ_2	3	−1	0	1	$E(7) + E(7)^2 + E(7)^4$	$E(7)^3 + E(7)^5 + E(7)^6$
χ_3	3	−1	0	1	$E(7)^3 + E(7)^5 + E(7)^6$	$E(7) + E(7)^2 + E(7)^4$
χ_4	6	2	0	0	−1	−1
χ_5	7	−1	1	−1	0	0
χ_6	8	0	−1	0	1	1

Trivial source character table of $G \cong \text{PSL}(3,2)$ at $p = 2$:

Normalisers N_i	N_1						N_2	N_3		N_4		N_5	N_6
p -subgroups of G up to conjugacy in G	P_1						P_2	P_3		P_4		P_5	P_6
Representatives $n_j \in N_i$	$1a$	$3a$	$7a$			$7b$	$1a$	$1a$	$3a$	$1a$	$3a$	$1a$	$1a$
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 1 \cdot \chi_5 + 0 \cdot \chi_6$	8	2	1			1	0	0	0	0	0	0	0
$0 \cdot \chi_1 + 1 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 1 \cdot \chi_5 + 0 \cdot \chi_6$	16	1	$2 * E(7) + 2 * E(7)^2 + E(7)^3 + 2 * E(7)^4 + E(7)^5 + E(7)^6$			$E(7) + E(7)^2 + 2 * E(7)^3 + E(7)^4 + 2 * E(7)^5 + 2 * E(7)^6$	0	0	0	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 1 \cdot \chi_3 + 1 \cdot \chi_4 + 1 \cdot \chi_5 + 0 \cdot \chi_6$	16	1	$E(7) + E(7)^2 + 2 * E(7)^3 + E(7)^4 + 2 * E(7)^5 + 2 * E(7)^6$			$2 * E(7) + 2 * E(7)^2 + E(7)^3 + 2 * E(7)^4 + E(7)^5 + E(7)^6$	0	0	0	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 1 \cdot \chi_6$	8	−1	1			1	0	0	0	0	0	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 2 \cdot \chi_4 + 1 \cdot \chi_5 + 0 \cdot \chi_6$	20	2	−1			−1	4	0	0	0	0	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 1 \cdot \chi_5 + 0 \cdot \chi_6$	14	2	0			0	2	2	2	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6$	6	0	−1			−1	2	2	−1	0	0	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 1 \cdot \chi_5 + 0 \cdot \chi_6$	14	2	0			0	2	0	0	2	2	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6$	6	0	−1			−1	2	0	0	2	−1	0	0
$1 \cdot \chi_1 + 1 \cdot \chi_2 + 1 \cdot \chi_3 + 2 \cdot \chi_4 + 1 \cdot \chi_5 + 0 \cdot \chi_6$	26	2	−2			−2	2	0	0	0	0	2	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6$	1	1	1			1	1	1	1	1	1	1	1

$$P_1 = Group([(())]) \cong 1$$

$$P_2 = Group([(2,3)(6,7)]) \cong \text{C2}$$

$$P_3 = Group([(4,5)(6,7), (2,3)(6,7)]) \cong \text{C2 x C2}$$

$$P_4 = Group([(4,6)(5,7), (4,5)(6,7)]) \cong \text{C2 x C2}$$

$$P_5 = Group([(2,3)(4,7,5,6), (4,5)(6,7)]) \cong \text{C4}$$

$$P_6 = Group([(4,5)(6,7), (2,3)(6,7), (4,6)(5,7)]) \cong \text{D8}$$

$$N_1 = Group([(2,4)(3,5), (1,2,3)(5,6,7)]) \cong \text{PSL}(3,2)$$

$$N_2 = Group([(2,3)(6,7), (4,5)(6,7), (2,3)(4,5), (2,6)(3,7)]) \cong \text{D8}$$

$$N_3 = Group([(2,3)(6,7), (4,5)(6,7), (4,7)(5,6), (2,4,7)(3,5,6)]) \cong \text{S4}$$

$$N_4 = Group([(4,5)(6,7), (4,6)(5,7), (1,3)(5,7), (1,2)(5,6)]) \cong \text{S4}$$

$$N_5 = Group([(2,3)(4,7,5,6), (4,5)(6,7), (2,3)(6,7)]) \cong \text{D8}$$

$$N_6 = Group([(4,6)(5,7), (2,3)(6,7), (4,5)(6,7)]) \cong \text{D8}$$