The group G is isomorphic to the group labelled by [72, 22] in the Small Groups library. Ordinary character table of $G \cong (C6 \times S3)$: C2:

| | 1a | 2a | 2b | 3a | 6a | 2c | 4a | 6b | 6c | 3b | 6d | 6e | 6f | 3c | 6g |
|-------------|----|----|----|----|----|----|----|------------------|------------------|----|----|------------------|------------------|----|----|
| χ_1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| χ_2 | 1 | 1 | -1 | 1 | 1 | -1 | 1 | -1 | -1 | 1 | 1 | -1 | -1 | 1 | 1 |
| χ_3 | 1 | 1 | -1 | 1 | 1 | 1 | -1 | 1 | 1 | 1 | 1 | -1 | -1 | 1 | 1 |
| χ_4 | 1 | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | 1 | 1 | 1 | 1 | 1 | 1 |
| χ_5 | 2 | 2 | -2 | 2 | 2 | 0 | 0 | 0 | 0 | -1 | -1 | 1 | 1 | -1 | -1 |
| χ_6 | 2 | 2 | 2 | 2 | 2 | 0 | 0 | 0 | 0 | -1 | -1 | -1 | -1 | -1 | -1 |
| χ_7 | 2 | -2 | 0 | 2 | -2 | 0 | 0 | 0 | 0 | 2 | -2 | 0 | 0 | 2 | -2 |
| χ_8 | 2 | 2 | 0 | -1 | -1 | -2 | 0 | 1 | 1 | 2 | 2 | 0 | 0 | -1 | -1 |
| χ_9 | 2 | 2 | 0 | -1 | -1 | 2 | 0 | -1 | -1 | 2 | 2 | 0 | 0 | -1 | -1 |
| χ_{10} | 2 | -2 | 0 | -1 | 1 | 0 | 0 | $-E(3) + E(3)^2$ | $E(3) - E(3)^2$ | 2 | -2 | 0 | 0 | -1 | 1 |
| χ_{11} | 2 | -2 | 0 | -1 | 1 | 0 | 0 | $E(3) - E(3)^2$ | $-E(3) + E(3)^2$ | 2 | -2 | 0 | 0 | -1 | 1 |
| χ_{12} | 2 | -2 | 0 | 2 | -2 | 0 | 0 | 0 | 0 | -1 | 1 | $-E(3) + E(3)^2$ | $E(3) - E(3)^2$ | -1 | 1 |
| χ_{13} | 2 | -2 | 0 | 2 | -2 | 0 | 0 | 0 | 0 | -1 | 1 | $E(3) - E(3)^2$ | $-E(3) + E(3)^2$ | -1 | 1 |
| χ_{14} | 4 | 4 | 0 | -2 | -2 | 0 | 0 | 0 | 0 | -2 | -2 | 0 | 0 | 1 | 1 |
| χ_{15} | 4 | -4 | 0 | -2 | 2 | 0 | 0 | 0 | 0 | -2 | 2 | 0 | 0 | 1 | -1 |

| Trivial source character table of $G \cong (C6 \times S3)$: C2 at $p = 3$: | | | | | | | | | | | |
|--|--|------------------------|---|-----------------------|--|--|--|--|--|--|--|
| Normalisers N_i | N_1 | N_2 | N_3 | N_4 | N_5 | | | | | | |
| p-subgroups of G up to conjugacy in G | P_1 | P_2 | P_3 | P_4 | P_5 | | | | | | |
| Representatives $n_j \in N_i$ | 1a $2a$ $2b$ $2c$ $4a$ | 1a $2c$ $2a$ $2b$ $4a$ | $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | 4a $2a$ $4b$ | 1a $2c$ $2a$ $2b$ $4a$ | | | | | | |
| $0 \cdot \chi_1 + 0 \cdot \chi_2 + 1 \cdot \chi_3 + 0 \cdot \chi_4 + 1 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 1 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 1 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | 9 	 9 	 -3 	 3 	 -1 | 0 0 0 0 0 | 0 0 0 0 0 | 0 0 0 | 0 0 0 0 0 | | | | | | |
| $0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 1 \cdot \chi_6 + 0 \cdot \chi_7 + 1 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 1 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | 9 	 9 	 3 	 -3 	 -1 | 0 0 0 0 0 | | $0 \qquad 0 \qquad 0$ | | | | | | | |
| $0 \cdot \chi_1 + 1 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 1 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 1 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 1 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | 9 	 9 	 -3 	 -3 	 1 | 0 0 0 0 0 | | $0 \qquad 0 \qquad 0$ | | | | | | | |
| $1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 1 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 1 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 1 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | 9 9 3 3 1 | 0 0 0 0 0 | | $0 \qquad 0 \qquad 0$ | | | | | | | |
| $0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 1 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 1 \cdot \chi_{10} + 1 \cdot \chi_{11} + 1 \cdot \chi_{12} + 1 \cdot \chi_{13} + 0 \cdot \chi_{14} + 2 \cdot \chi_{15}$ | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | 0 0 0 0 0 | | $0 \qquad 0 \qquad 0$ | | | | | | | |
| $0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 1 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 1 \cdot \chi_{10} + 1 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | 6 -6 0 0 0 | 6 0 -6 0 0 | 0 0 0 0 0 | 0 0 0 | 0 0 0 0 0 | | | | | | |
| $0 \cdot \chi_1 + 1 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 1 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | 3 3 -1 -3 1 | 3 -3 3 -1 1 | | $0 \qquad 0 \qquad 0$ | | | | | | | |
| $0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 1 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | 3 -3 3 1 -1 | | $0 \qquad 0 \qquad 0$ | | | | | | | |
| $1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 1 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | 3 3 1 3 1 | 3 3 3 1 1 | | $0 \qquad 0 \qquad 0$ | | | | | | | |
| $0 \cdot \chi_1 + 0 \cdot \chi_2 + 1 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 1 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | 3 3 3 -1 -1 | | $0 \qquad 0 \qquad 0$ | | | | | | | |
| $0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 1 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 1 \cdot \chi_{12} + 1 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | 0 0 0 0 0 | 6 0 -6 0 0 0 | 0 0 0 | 0 0 0 0 0 | | | | | | |
| $0 \cdot \chi_1 + 1 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 1 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | 3 3 -3 -1 1 | 0 0 0 0 0 | $\begin{vmatrix} 3 & -1 & 3 & -3 & 1 & 0 \end{vmatrix}$ | $0 \qquad 0 \qquad 0$ | | | | | | | |
| $0 \cdot \chi_1 + 0 \cdot \chi_2 + 1 \cdot \chi_3 + 0 \cdot \chi_4 + 1 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | 0 0 0 0 0 | $\begin{vmatrix} 3 & 1 & 3 & -3 & -1 & 0 \end{vmatrix}$ | $0 \qquad 0 \qquad 0$ | | | | | | | |
| $1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 1 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | 3 3 3 1 1 | 0 0 0 0 0 | 3 1 3 3 1 0 | $0 \qquad 0 \qquad 0$ | | | | | | | |
| $0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 1 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | 0 0 0 0 0 | $\begin{vmatrix} 3 & -1 & 3 & 3 & -1 & 0 \end{vmatrix}$ | $0 \qquad 0 \qquad 0$ | | | | | | | |
| $0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 1 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 1 \cdot \chi_{15}$ | 6 -6 0 0 0 | 0 0 0 0 0 | 0 0 0 0 3 | E(4) -3 $-E(4)$ | 0 0 0 0 0 | | | | | | |
| $0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 1 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 1 \cdot \chi_{15}$ | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | 0 0 0 0 0 | | -E(4) -3 $E(4)$ | | | | | | | |
| $1 \cdot \chi_1 + 1 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 1 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | 0 0 0 0 0 | | 1 3 1 | | | | | | | |
| $0 \cdot \chi_1 + 0 \cdot \chi_2 + 1 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 1 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | 0 0 0 0 0 | | -1 3 -1 | | | | | | | |
| $1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | 1 1 1 1 1 | 1 1 1 1 1 | 1 1 1 1 1 1 | 1 1 1 | 1 1 1 1 1 | | | | | | |
| $0 \cdot \chi_1 + 0 \cdot \chi_2 + 1 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | 1 1 1 -1 -1 | 1 1 1 -1 -1 1 | -1 1 -1 | 1 1 1 -1 -1 | | | | | | |
| $0 \cdot \chi_1 + 1 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | 1 -1 1 -1 1 | 1 -1 1 -1 1 1 | 1 1 1 | 1 -1 1 -1 1 | | | | | | |
| $0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | 1 -1 1 1 -1 | 1 -1 1 1 -1 1 | -1 1 -1 | 1 -1 1 1 -1 | | | | | | |
| $0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 1 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15}$ | 2 -2 0 0 0 | 2 0 -2 0 0 | $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | 0 -2 0 | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | | | | | | |

```
P_1 = Group([()]) \cong 1
```

 $P_2 = Group([(1,3,2)]) \cong C3$

 $P_3 = Group([(4,6,5)]) \cong C3$

 $P_4 = Group([(1,3,2)(4,6,5)]) \cong C3$

 $P_5 = Group([(1,3,2),(4,6,5)]) \cong C3 \times C3$

 $N_1 = Group([(5,6)(8,10),(2,3)(7,8)(9,10),(7,9)(8,10),(1,2,3),(4,5,6)]) \cong (C6 \times S3) : C2$

 $N_2 = Group([(5,6)(8,10),(2,3)(7,8)(9,10),(7,9)(8,10),(1,2,3),(4,5,6)]) \cong (C6 \times S3) : C2$

 $N_3 = Group([(5,6)(8,10),(2,3)(7,8)(9,10),(7,9)(8,10),(1,2,3),(4,5,6)]) \cong (C6 \times S3) : C2$

 $N_4 = Group([(1,3,2)(4,6,5),(2,3)(4,5)(7,8,9,10),(4,6,5),(7,9)(8,10)]) \cong (C3 \times C3) : C4$ $N_5 = Group([(5,6)(8,10),(2,3)(7,8)(9,10),(7,9)(8,10),(1,2,3),(4,5,6)]) \cong (C6 \times S3) : C2$