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	$\begin{vmatrix} \chi_9 \end{vmatrix} = 2 - 2 = 0 = 0 = 0 = E(8) - E(8)^3 = -E(8) + E(8)^3 = E(8) - E(8)^3 = -E(8) + E(8)^3 = 2 - 2 = 0 = 0 = 0 = E(8) - E(8)^3 = -E(8) + E(8)^3 = 0 = 0 = 0 = 0 = 0 = 0 = 0 = 0 = 0 = $
	$\left \begin{array}{cccccccccccccccccccccccccccccccccccc$
	$ \begin{vmatrix} \chi_{11} \\ \chi_{11} \end{vmatrix} 2 - 2 & 0 & 0 & 0 & -E(24)^{17} + E(24)^{19} & E(24)^{17} - E(24)^{19} & -E(24)^{11} & E(24) - E(24)^{11} & -E(12)^{7} - E(12)^{11} & -E(12)^{7} + E(12)^{11} & E(8) - E(8)^{3} & -E(8) + E(8)^{3} $
	$\left \begin{array}{cccccccccccccccccccccccccccccccccccc$
	$\left \begin{array}{cccccccccccccccccccccccccccccccccccc$
	$\left \begin{array}{cccccccccccccccccccccccccccccccccccc$
	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
Trivial source character table of $G \cong C3$ : Q16 at $p = 2$ :	
$p$ -subgroups of $G$ up to conjugacy in $G$ $P_1$ $P_2$ $P_3$ $P_4$ $P_5$ $P_6$ $P_7$ $P_8$ $P_9$	
Representatives $n_j \in N_i$ $1a  3a  1a  3a  1a  1a  1a  1a  $	
$\boxed{1 \cdot \chi_1 + 1 \cdot \chi_2 + 1 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 2 \cdot \chi_7 + 2 \cdot \chi_8 + 2 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15} & 16 & 16 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & $	
$\left  \ 0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 1 \cdot \chi_5 + 1 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 1 \cdot \chi_{10} + 1 \cdot \chi_{11} + 1 \cdot \chi_{12} + 1 \cdot \chi_{13} + 1 \cdot \chi_{14} + 1 \cdot \chi_{15} \right  \ 16 \ \ -8 \ \left  \ 0 \ \ 0 \ \ \right  \ 0 \ \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \left  \ 0 \ \ \right  \ \left  \ 0 \ \ \left  \ $	
$1 \cdot \chi_1 + 1 \cdot \chi_2 + 1 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 2 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15} \begin{vmatrix} 8 & 8 & 8 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{vmatrix}$	
$\boxed{0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 1 \cdot \chi_5 + 1 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 1 \cdot \chi_{14} + 1 \cdot \chi_{15}  8  -4  8  -4  0  0  0  0  0  0  0  0}$	

$P_1$ =	$=Group([()])\cong 1$
	$C_{1}$ $C_{1}$ $C_{1}$ $C_{2}$ $C_{3}$

 $P_2 = Group([(1,5)(2,9)(3,12)(4,14)(6,16)(7,19)(8,21)(10,23)(11,25)(13,27)(15,29)(17,31)(18,32)(20,34)(22,36)(24,38)(26,39)(28,41)(30,42)(33,43)(35,45)(37,46)(40,47)(44,48)]) \cong C2(3,32)(3,32)(4,33$ 

 $1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 1 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15} \begin{vmatrix} 4 & 4 & 4 & 4 & 0 & 0 \end{vmatrix} \begin{vmatrix} 2 & 0 & 0 & 0 & 0 \end{vmatrix} \begin{vmatrix} 0 & 0 & 0 & 0 \end{vmatrix} \begin{vmatrix} 0 & 0 & 0 & 0 \end{vmatrix} \end{vmatrix}$  $1 \cdot \chi_1 + 0 \cdot \chi_2 + 1 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 1 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15} \begin{vmatrix} 4 & 4 & 4 & 4 & 0 & 0 & 0 & 2 & 0 & 0 & 0 \end{vmatrix}$  $\begin{vmatrix} 0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 1 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11} + 0 \cdot \chi_{12} + 0 \cdot \chi_{13} + 0 \cdot \chi_{14} + 0 \cdot \chi_{15} \end{vmatrix} \begin{vmatrix} 2 & -1 & 2 & -1 & 2 & -1 & 0 & 0 & 2 & -1 & 0 & 0 & 0 \end{vmatrix}$ 

 $P_3 = Group([(1,5)(2,9)(3,12)(4,14)(6,16)(7,19)(8,21)(10,23)(11,25)(13,27)(15,29)(17,31)(18,32)(20,34)(22,36)(24,38)(26,39)(28,41)(30,42)(33,43)(35,45)(37,46)(40,47)(44,48), (1,14,5,4)(2,21,9,8)(3,25,12,11)(6,29,16,15)(7,32,19,18)(10,36,23,22)(13,39,27,26)(17,42,31,30)(20,43,34,33)(24,46,38,37)(28,47,41,40)(35,48,45,44)]) \cong C4$ 

 $P_4 = Group([(1,5)(2,9)(3,12)(4,14)(6,16)(7,19)(8,21)(10,23)(11,25)(13,27)(15,29)(17,31)(18,32)(20,34)(22,36)(24,38)(26,39)(28,41)(30,42)(33,43)(35,45)(37,46)(40,47)(44,48), (1,2,5,9)(3,18,12,32)(4,21,14,8)(6,24,16,38)(7,25,19,11)(10,31,23,17)(13,44,27,48)(15,46,29,37)(20,47,34,40)(22,30,36,42)(26,35,39,45)(28,33,41,43)]) \cong C4$ 

 $P_6 = Group([(1,5)(2,9)(3,12)(4,14)(6,16)(7,19)(8,21)(10,23)(11,25)(13,27)(15,29)(24,34)(22,36)(24,38)(26,39)(28,41)(30,42)(33,43)(24,46,38,37)(28,47,41,40)(35,48,45,47)(15,29)(17,31)(18,32)(20,34)(22,36)(24,38)(26,39)(28,41)(30,42)(33,43)(35,45)(37,46)(40,47)(44,48), (1,14,5,4)(2,19,8)(24,38)(26,39)(28,41)(30,42)(33,43)(35,45)(37,46)(40,47)(44,48), (1,14,5,4)(2,19,8)(24,38)(26,39)(28,41)(30,42)(33,43)(35,45)(37,46)(40,47)(44,48), (1,14,5,4)(2,19,8)(24,38)(26,39)(28,41)(30,42)(33,43)(35,45)(37,46)(40,47)(44,48), (1,14,5,4)(21,19,8)(24,38)(26,39)(28,41)(30,42)(33,43)(35,45)(37,46)(40,47)(44,48), (1,14,5,4)(21,19,8)(24,38)(26,39)(28,41)(30,42)(33,43)(35,45)(37,46)(40,47)(44,48), (1,14,5,4)(21,19,8)(24,48)(33,43)(35,48)(35,48)(35,48)(35,48)(35,48)(35,48)(36,48)(3$ 

 $P_7 = Group([(1,5)(2,9)(3,12)(4,14)(6,16)(7,19)(8,21)(10,23)(11,25)(13,27)(15,29)(17,31)(18,32)(20,34)(22,36)(24,38)(25,12,11)(6,29,16,15)(7,32,19,18)(10,36,23,22)(13,39,27,26)(17,42,31,30)(20,43,44,33)(24,46,38,37)(28,47,41,40)(25,36,42)(26,35,39,45)(28,37,46)(40,47)(44,48), \\ (1,14,5,4)(2,21,9,8)(3,25,12,11)(6,29,16,15)(7,32,19,18)(10,36,23,22)(13,39,27,26)(17,42,31,30)(20,43,43)(24,48,38,37)(28,47,41,40)(25,36,42)(26,35,39,45)(28,33,41,43)(26,36,39)(28,41,43)(28,36,39)(28,41,43)(28,36,39)(28,41,43)(28,36,39)(28,41,43)(28,36,39)(28,36,3$ 

 $P_8 = Group([(1,5)(2,9)(3,12)(4,14)(6,16)(7,19)(8,21)(10,23)(11,25)(13,27)(15,29)(17,31)(18,32)(20,34)(22,36)(24,38)(26,39)(28,41)(30,42)(33,43)(24,48,34,34)(20,43,43)(24,48,34,34)(20,43,43)(24,48,34,34)(24,48,3$ 

 $|\chi_2|$  1 1 1 -1 -1  $|\chi_3|$  1 1 1 -1 1  $|\chi_4|111111-1$ 

 $N_5 = Group([(1,18,5,32)(2,25,9,11)(3,8,12,21)(4,7,14,19)(6,44,16,48)(10,47,23,40)(13,37,27,46)(15,35,29,45)(17,33,31,43)(20,42,34,30)(22,41,36,28)(24,39,38,26), \\ (1,5)(2,9)(3,12)(4,14)(6,16)(7,19)(8,21)(10,23)(11,25)(13,27)(15,29)(17,31)(18,32)(20,34,30)(22,41,36,28)(24,39,38,26), \\ (1,5)(2,9)(3,12)(4,14)(6,16)(7,19)(8,21)(10,23)(11,25)(13,27)(15,29)(17,31)(18,32)(20,34,30)(22,41,36,28)(24,39,38,26), \\ (1,5)(2,9)(3,12)(4,14)(6,16)(7,19)(8,21)(10,23)(11,25)(13,27)(15,29)(17,31)(18,32)(20,34,30)(22,41,36,28)(24,39,38,26), \\ (1,5)(2,9)(3,12)(4,14)(6,16)(7,19)(8,21)(10,23)(11,25)(13,27)(15,29)(17,31)(18,32)(20,34,30)(22,41,36,28)(24,39,38,26), \\ (1,5)(2,9)(3,12)(4,14)(6,16)(17,32$ 

 $N_4 = Group([(1,2,5,9)(3,18,12,32)(4,21,14,8)(6,24,16,38)(7,25,19,11)(10,31,23,17)(13,44,27,48)(22,33,36)(23,43)(24,37,38,46)(28,40,41,47)(23,43,43)(24,37,38,46)(28,40,41,47)(23,43,43)(24,37,38,46)(28,40,41,47)(35,44,45,48)] \\ \cong Q_8 = Q_8$ 

 $N_8 = Group([(1,18,5,32)(2,25,9,11)(3,42,21,4,36)(22,41,36,23)(22,41,36,24)(13,34)(22,41,36,24)(13,34,34)(24,46,38,37)(28,47,41,40)(35,48,45,44), (1,5)(2,9)(3,12)(4,14,16,16)(7,19)(8,21)(10,23)(11,25)(13,27)(15,29)(17,31)(18,32)(20,34,32)(21,34,34)(22,36,34,34,34)(22,36,34,34,34)(22,36,34,34)(22,36,34,34)(22,36,34,34)(22,36,34,34)(22,36,34,34)(22,36,34$ 

 $N_9 = Group([(1,2,5,9)(3,18,12,32)(4,21,14,8)(6,24,16,38)(7,25,12,11)(6,29,16,15)(7,32,19,18)(10,36,23,22)(13,39,27,26)(17,42,31,30)(20,43,44,27,48)(15,46,29,37)(20,47,34,40)(22,30,36,42)(23,34,22,33)(17,28,42,47,31,41,30,40)(24,35,46,48,38,45,37,44),\\ N_9 = Group([(1,2,5,9)(3,12)(4,14)(6,16)(7,19)(8,21)(10,23)(11,25)(13,27)(15,29)(17,31)(18,32)(20,34)(22,36)(24,38)(26,39)(28,41)(30,42)(33,43)(24,46,38,37)(28,47,41,40)(24,36,48)(24,46,38,37)(28,47,41,40)(24,48,48)(2$