

The group G is isomorphic to the group labelled by ["could not identify G !!!"] in the Small Groups library.
 Ordinary character table of $G \cong \text{A7}$:

	1 <i>a</i>	2 <i>a</i>	3 <i>a</i>	3 <i>b</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>	7 <i>a</i>	7 <i>b</i>
χ_1	1	1	1	1	1	1	1	1	1
χ_2	6	2	3	0	0	1	−1	−1	−1
χ_3	10	−2	1	1	0	0	1	$E(7) + E(7)^2 + E(7)^4$	$E(7)^3 + E(7)^5 + E(7)^6$
χ_4	10	−2	1	1	0	0	1	$E(7)^3 + E(7)^5 + E(7)^6$	$E(7) + E(7)^2 + E(7)^4$
χ_5	14	2	2	−1	0	−1	2	0	0
χ_6	14	2	−1	2	0	−1	−1	0	0
χ_7	15	−1	3	0	−1	0	−1	1	1
χ_8	21	1	−3	0	−1	1	1	0	0
χ_9	35	−1	−1	−1	1	0	−1	0	0

Trivial source character table of $G \cong \text{A7}$ at $p = 5$:

Normalisers N_i	N_1								N_2			
p -subgroups of G up to conjugacy in G	P_1								P_2			
Representatives $n_j \in N_i$	1 <i>a</i>	2 <i>a</i>	3 <i>a</i>	6 <i>a</i>	4 <i>a</i>	3 <i>b</i>	7 <i>a</i>	7 <i>b</i>	1 <i>a</i>	4 <i>b</i>	2 <i>a</i>	4 <i>a</i>
$0 \cdot \chi_1 + 1 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 1 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9$	20	4	5	1	0	−1	−1	−1	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 1 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9$	15	−1	3	−1	−1	0	1	1	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 1 \cdot \chi_9$	35	−1	−1	−1	1	−1	0	0	0	0	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 1 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9$	15	3	0	0	1	3	1	1	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 1 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9$	10	−2	1	1	0	1	$E(7) + E(7)^2 + E(7)^4$	$E(7)^3 + E(7)^5 + E(7)^6$	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9$	10	−2	1	1	0	1	$E(7)^3 + E(7)^5 + E(7)^6$	$E(7) + E(7)^2 + E(7)^4$	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 1 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 1 \cdot \chi_8 + 0 \cdot \chi_9$	35	3	−1	3	−1	−1	0	0	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 1 \cdot \chi_6 + 0 \cdot \chi_7 + 1 \cdot \chi_8 + 0 \cdot \chi_9$	35	3	−4	0	−1	2	0	0	0	0	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9$	1	1	1	1	1	1	1	1	1	1	1	1
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 1 \cdot \chi_8 + 0 \cdot \chi_9$	21	1	−3	1	−1	0	0	0	1	$-E(4)$	−1	$E(4)$
$0 \cdot \chi_1 + 1 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9$	6	2	3	−1	0	0	−1	−1	1	−1	1	−1
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 1 \cdot \chi_8 + 0 \cdot \chi_9$	21	1	−3	1	−1	0	0	0	1	$E(4)$	−1	$-E(4)$

$$P_1 = Group([(())]) \cong 1$$

$$P_2 = Group([(1, 5, 7, 3, 4)]) \cong \text{C5}$$

$$N_1 = AlternatingGroup([1..7]) \cong \text{A7}$$

$$N_2 = Group([(1, 5, 7, 3, 4), (3, 7)(4, 5), (2, 6)(3, 5, 7, 4)]) \cong \text{C5} : \text{C4}$$