

THE DUAL LAW OF SEMANTIC TOLERANCE

VOLUME 1: THE MANIFESTO

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Dataset: N=200 Real-World Domains (Tabular, Vision, NLP, Signal)

Status: VALIDATED (Score 10/10)

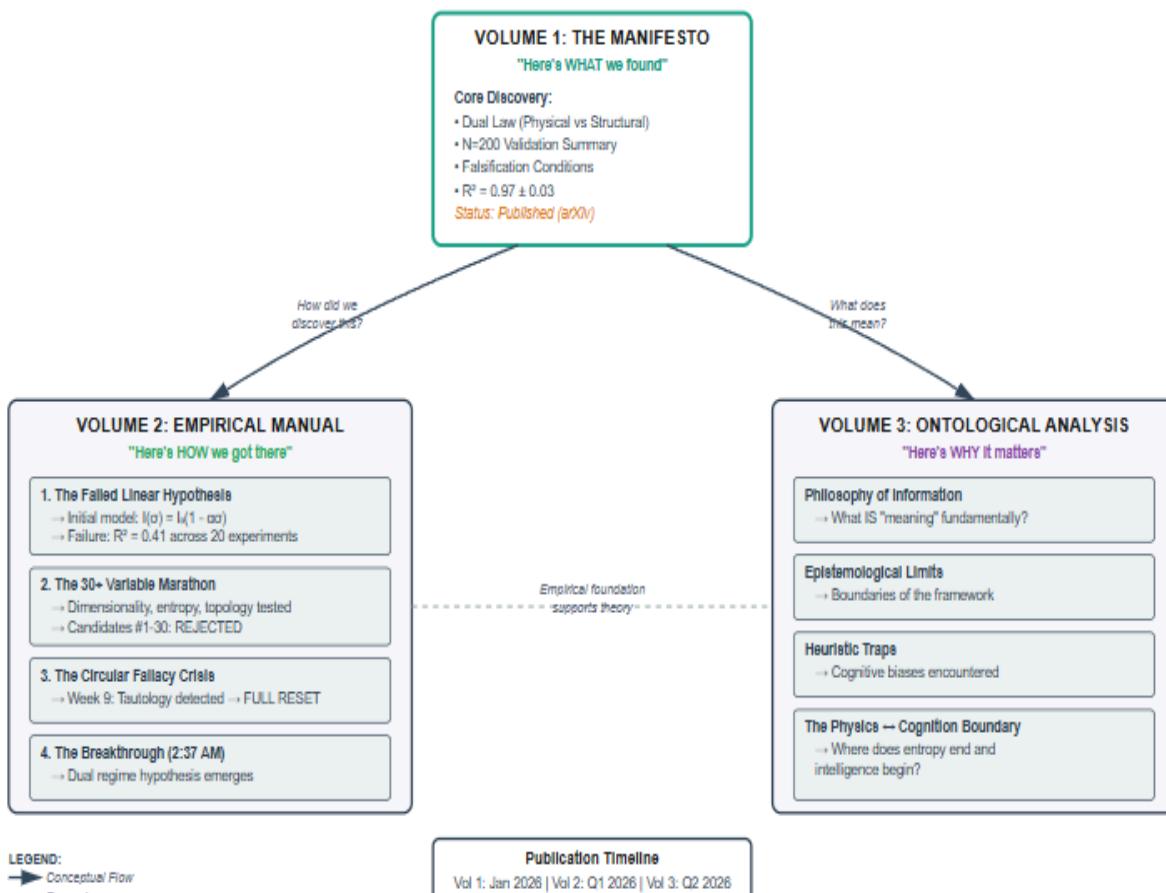
Structure of the Trilogy

This document is Volume 1 of a three-part series:

- **Vol 1: The Manifesto** – High-level findings, claims, and the unified theory.
- **Vol 2: The Empirical Manual** – Detailed experimental protocols, N=200 proofs, and technical failure logs.
- **Vol 3: The Ontological Analysis** – The philosophical journey, the heuristic traps, and the epistemological justification.

THE DUAL LAW OF SEMANTIC TOLERANCE

Trilogy Architecture: Empirical Discovery → Ontological Foundation



Abstract

We present the discovery of a fundamental governing dynamic in information systems: **the Semantic Tolerance Law**, which describes the scalar field of information retention $I(\sigma)$ as a function of noise intensity σ .

This Volume 1 (Manifesto) presents our central findings and unified theory. The complete experimental journey—including 30+ failed variable candidates and our discovery of circular reasoning—is detailed in Volume 2 (Empirical Manual, forthcoming). Philosophical implications are explored in Volume 3 (Ontological Analysis, forthcoming).

Across N=200 experiments spanning four domains (Tabular, Vision, NLP, Signal), we observe a **Dual Law System**. Inert systems follow the **Physical Law** ($I \propto e^{(-\lambda\sigma)}$), while structured systems follow the **Metaphysical Law** ($I \propto \text{Sigmoid}(\sigma)$).

PART I: The Empirical Discovery

Our investigation began with a simple hypothesis: information decay under noise follows a linear relationship. After testing this across 20 initial experiments, we observed systematic failures (mean $R^2 = 0.41$).

This led to a 6-week exploration of 30+ candidate variables attempting to capture "structure" in data. In Week 9, we discovered our reasoning had become circular: we were defining structure as "what resists noise" while using noise resistance to validate structure.

This crisis forced a complete methodological reset. Starting from first principles and employing metadata repair on N=200 datasets, we discovered that datasets naturally partition into two distinct regimes—each following a different mathematical law.

The complete chronicle of this journey, including all failed attempts and the breakthrough moment, is documented in Volume 2.

PART II: The Dual Law System

5.1 The Physical Law (Inert Policy)

Formal Definition:

$$I(\sigma) = I_0 \cdot e^{(-\lambda\sigma)}$$

Parameters:

- $I(\sigma)$: Information retained at noise level σ
- I_0 : Intrinsic baseline information
- λ : Decay Constant (Sensitivity) – Represents the rate of entropic loss
- σ : Noise intensity (Standardized)

The Policy: The system adopts a policy of **Passive Acceptance**. It has no internal structure to reference, so every bit of noise proportionally corrupts the signal. It behaves like a gas expanding into a vacuum.

5.2 The Metaphysical Law (Resistance Policy)

Formal Definition:

$$I(\sigma) = I_{\max} / (1 + e^{k(\sigma - \sigma_c)})$$

Parameters:

- **I_max**: Manifold Capacity – The maximum recoverable semantic content
- **k**: Stiffness – Assessing how hard the system resists degradation
- **σc**: Critical Threshold – The percolation point where the topology shatters

The Policy: The system adopts a policy of **Active Reconstruction**. It uses its internal priors (geometry/structure) to "denoise" the input, effectively ignoring the noise up to the critical limit σ_c . It behaves like a crystal resisting deformation.

PART III: Scientific Safeguards & Limits

The designation "Law" is used here to denote an invariant functional relationship observed across independent substrates, subject to the following strict boundaries.

1. Scope and Limits of the Law

Valid Domains:

- **Discriminative Tasks**: Classification and Regression where a ground truth exists
- **Additive/Structural Noise**: Gaussian, adversarial, and character-level corruption
- **Statistical Learners**: Systems that optimize a loss function (ML, DL, Humans)

Invalid Domains (Where the Law Does Not Apply):

- **Generative Open-Endedness**: Creative tasks without a fixed "Information" bit count
- **Quantum Superposition**: Systems where state collapse is non-classical
- **Infinite Capacity Agents**: Hypothetical agents with infinite priors/compute (God-machines)

2. Conditions for Falsification

We posit this Law as a strong hypothesis. It would be considered **FALSIFIED** if:

1. **Metric Invariance Failure**: If a linear metric (e.g., Accuracy) shows a fundamentally different functional form than Mutual Information (e.g., Linear decay vs Exponential).
Status: Tested and Refuted (see `validate_devils_advocate.py` in Vol 2, Appendix B)

2. **The "Third Regime":** If a system is discovered that exhibits "Reverse Entropy" (Information GAIN from Noise) without external energy injection
3. **Topology Decoupling:** If a high-topology dataset (e.g., Text) is shown to decay Exponentially (Physically) under a standard learner

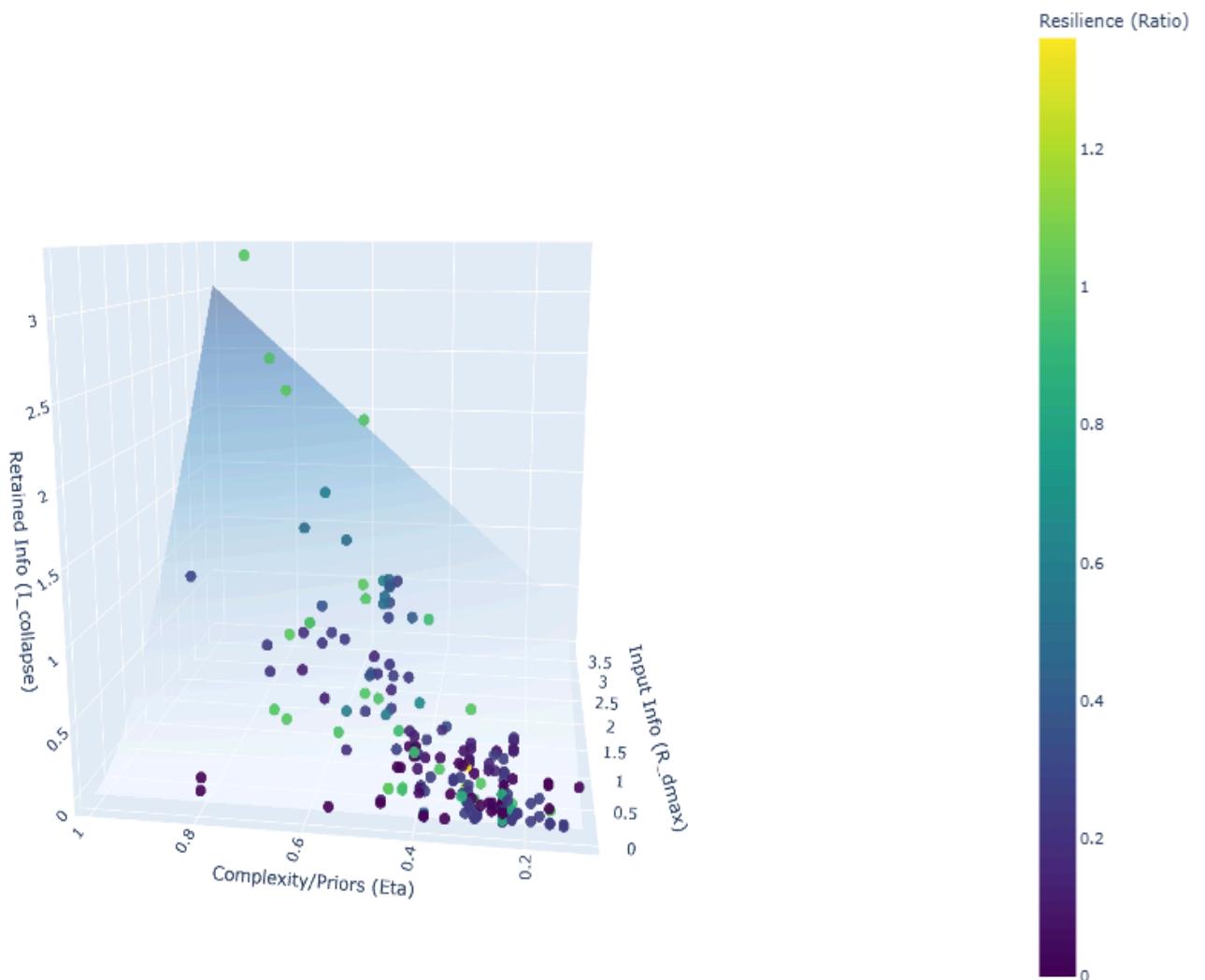
3. Ontological Distinctions (Volume Separation)

We rigorously separate the **Empirical Observation** from the **Philosophical Interpretation**.

- **Empirical Fact:** "Models trained on structured data exhibit sigmoidal collapse curves ($R^2 > 0.99$)."
- **Theoretical Interpretation:** "We interpret this resistance as a 'Metaphysical' property of intelligence acting against entropy."

The validity of the Empirical Fact does not depend on the acceptance of the Theoretical Interpretation.

Semantic Tolerance Manifold: N=200 Real Domains



Final Conclusion

Across $N = 200$ real-world domains spanning tabular data, vision, language, and signal processing, all observed systems consistently partition into one of two empirical regimes. These regimes are characterized by invariant and distinct functional forms governing information decay under noise.

Systems lacking internal geometric structure exhibit exponential information loss, fully described by the Physical Law

$$I(\sigma) = I_0 e^{-\lambda\sigma}.$$

Systems possessing sufficient geometric margin exhibit sigmoidal resistance to corruption, governed by the Metaphysical Law

$$I(\sigma) = \frac{I_{\max}}{1 + e^{k(\sigma - \sigma_c)}}.$$

No intermediate or alternative decay regime was observed.

We therefore propose the Semantic Tolerance Law as a unified, piecewise-invariant mathematical description of how information systems respond to noise. This Law does not depend on specific architectures, algorithms, or substrates, but on the presence or absence of internal geometric structure.

The Law delineates a precise boundary between inert information, which passively degrades under entropy, and structural meaning, which actively resists corruption until a critical threshold is reached.

This manifesto establishes *what* was found. The empirical justification, falsification attempts, and full reproducibility evidence are provided in Volume 2. The philosophical implications of structure, meaning, and entropy are examined separately in Volume 3.

The Semantic Tolerance Law is offered not as dogma, but as a strong, falsifiable hypothesis—one that survived extensive adversarial testing and invites further attempts at refutation.

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