

1) Consider the circuit shown in Figure 1 below.

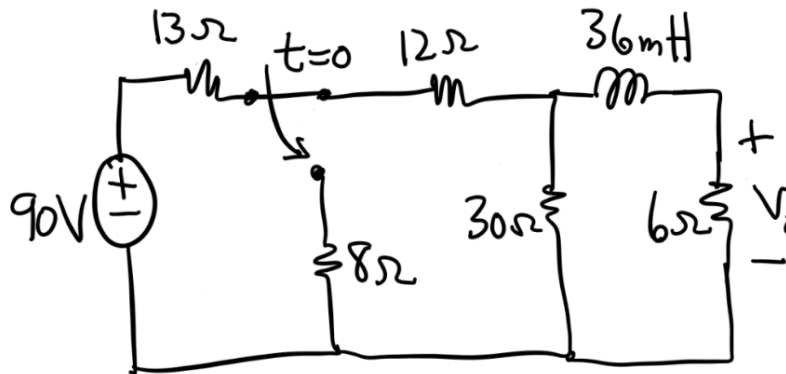


Figure 1. Circuit for Problem 1.

a) The response $V_o(t)$ for $t > 0$ can be written as

$$V_o(t) = A + Be^{-ct},$$

where A and B are in units of volts and c has units of rps (i.e., rad/sec; c is the reciprocal of the time constant). State your by-hand solutions for A , B , and c , and **list your A , B , and c values with appropriate units in proper engineering notation format with two decimal places of precision.**

Also, sketch the response. Label the plot axes on your sketch and otherwise make your sketch neat-looking and easy to comprehend.

b) Use the LTSpice verification testbench which has been provided to you to verify your by-hand answers for A , B , and c . **List the *maxerror* value you attained from the LTSpice verification testbench;** you should ensure that the *maxerror* value listed in the Spice Error Log (ctrl-L) is less than or equal to the value given in the testbench comment. If you do not achieve a *maxerror* less than or equal to the value given in the testbench comment, **something is wrong**, and you should work to resolve the issues with your by-hand solutions for A , B , and c prior to submitting. Attach a screenshot of the Spice Error Log showing the value of *maxerror* that you attained.

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Circuit $t=0^-$



$$V_o(0^-) = V_o(0^+)$$

V_o = Voltage divider

$$V_o = V_s \left(\frac{R_B}{R_A + R_B} \right) \left[\begin{aligned} R_A &= 12\Omega + 12\Omega = 24\Omega \\ R_B &= \frac{20 \cdot 6}{20 + 6} = 5\Omega \end{aligned} \right]$$

$$V_o = 90V \left(\frac{5\Omega}{24\Omega + 5\Omega} \right)$$

$$V_o(0^-) = V_o(0^+) = 15V$$

$$B = 15V$$

Find A, B, c in

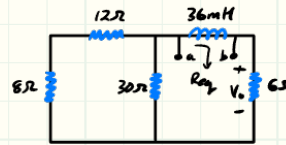
$$V_o(t) = A + B e^{-ct}$$

$$A = V(\infty)$$

$$B = [V(0^+) - V(\infty)]$$

$$c = 1/\tau$$

at $t = \infty$, V_s is disconnected and so $V_o(\infty) = 0$



$$A = 0V$$

$$c = \frac{1}{\tau}$$

$$\tau = \frac{L}{R_{eq}}$$

$$\tau = \frac{36mH}{18.5\Omega} = 0.002s$$

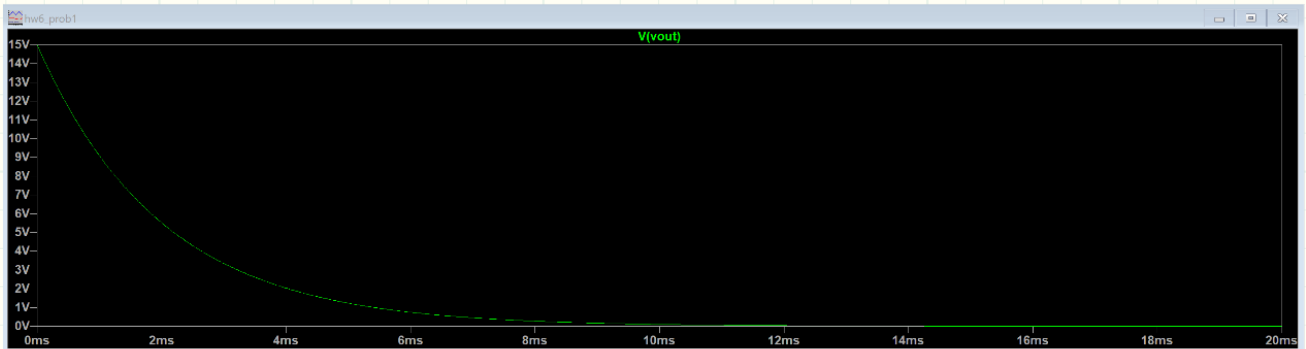
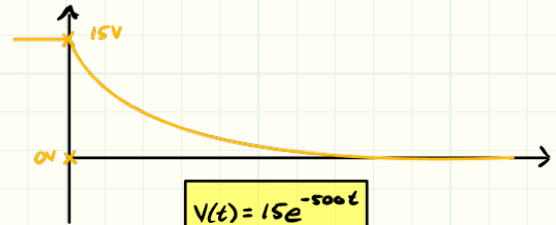
$$c = 1/0.002$$

$$c = 500 \text{ rad/s}$$

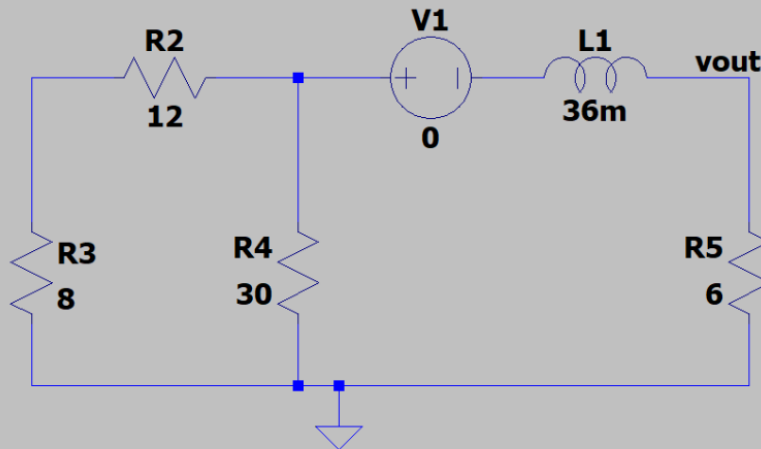


$$R_{eq} = (6\Omega) + \left(\frac{(20+12) \cdot 30}{(20+12) + 30} \right)$$

$$R_{eq} = 18.5\Omega$$



maxerror: MAX(abs(v(vout)-v(voutcheck)))=0.00269952158477 FROM 0 TO 0.02



2) Consider the circuit shown in Figure 2 below.

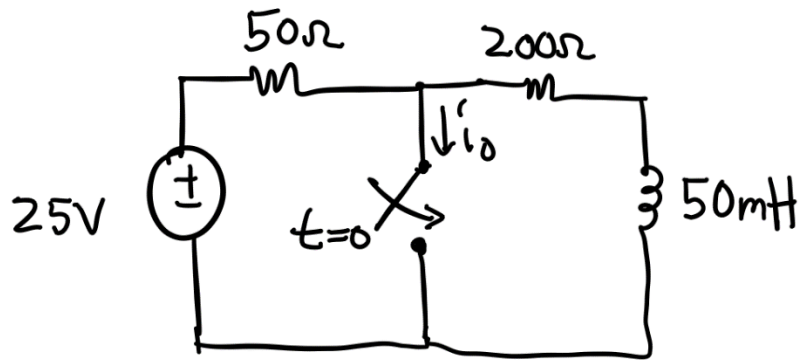


Figure 2. Circuit for Problem 2.

a) The response $i_0(t)$ for $t > 0$ can be written as

$$i_0(t) = A + Be^{-ct},$$

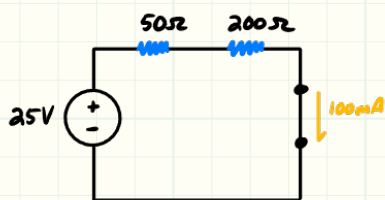
where A and B are in units of amps and c has units of rps (i.e., rad/sec; c is the reciprocal of the time constant). State your by-hand solutions for A , B , and c , and **list your A , B , and c values with appropriate units in proper engineering notation format with two decimal places of precision.**

Also, sketch the response. Label the plot axes on your sketch and otherwise make your sketch neat-looking and easy to comprehend.

b) Use the LTSpice verification testbench which has been provided to you to verify your by-hand answers for A , B , and c . **List the *maxerror* value you attained from the LTSpice verification testbench;** you should ensure that the *maxerror* value listed in the Spice Error Log (ctrl-L) is less than or equal to the value given in the testbench comment. If you do not achieve a *maxerror* less than or equal to the value given in the testbench comment, **something is wrong**, and you should work to resolve the issues with your by-hand solutions for A , B , and c prior to submitting. Attach a screenshot of the Spice Error Log showing the value of *maxerror* that you attained.

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CKT at $t=0^-$



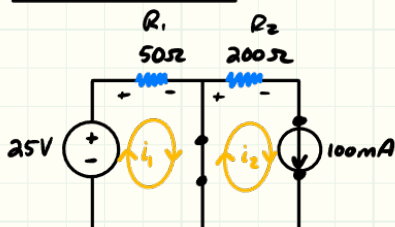
$$i = \frac{V}{R}$$

$$i(0^-) = \frac{V_s}{R_{eq}}$$

$$i(0^-) = \frac{25V}{200\Omega + 50\Omega}$$

$$i(0^-) = 100mA$$

CKT at $t=0^+$



$$i_2 = 100mA$$

$$0 = -V_s + R_1(i_1)$$

$$V = i_1 R_1$$

$$\frac{25V}{50\Omega} = 500mA = i_1$$

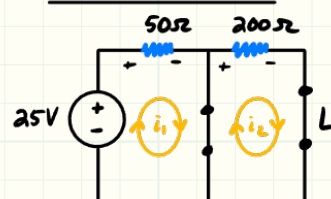
$$i_0 = i_1 - i_2$$

$$i_0 = 500mA - 100mA$$

$$i_0 = 400mA$$

$$B = -100mA$$

CKT at $i(t \rightarrow \infty)$



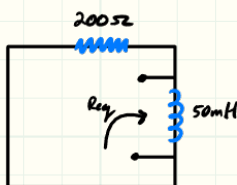
$i_2 = 0$; because current flows the path of least resistance and skip loop 2.

$$i_1 = 500mA$$

$$A = 500mA$$

Finding τ

$$\tau = L/R_{eq}$$



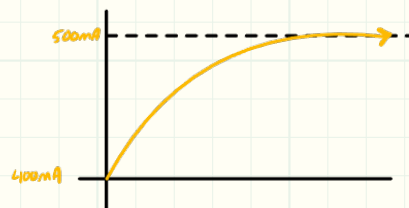
$$R_{eq} = 200\Omega$$

$$\tau = \frac{50mH}{200\Omega} = 0.00025$$

$$C = \frac{1}{\tau}$$

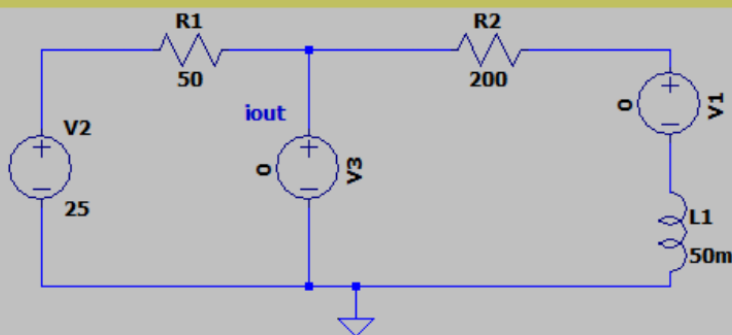
$$C = \frac{1}{0.00025} = 4000 rps$$

$$C = 4000 rps$$

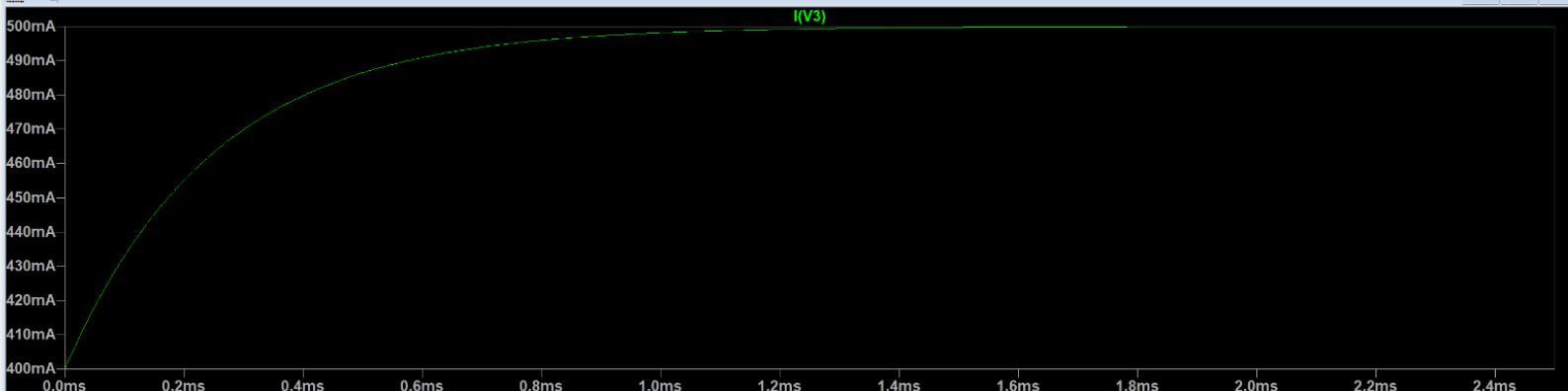


$$i_0(t) = 500 - 100e^{-4000t}$$

maxerror: MAX(abs(i(v3)-i(v4)))=0.000199601196808 FROM 0 TO 0.0025



hw6_prob2



3) Consider the circuit shown in Figure 3 below.

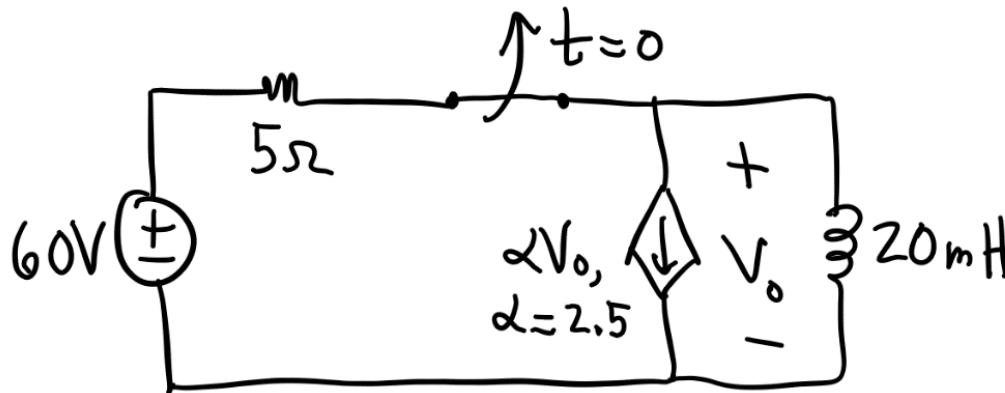


Figure 3. Circuit for Problem 3.

a) The response $V_o(t)$ for $t > 0$ can be written as

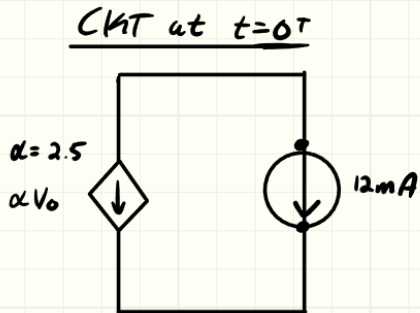
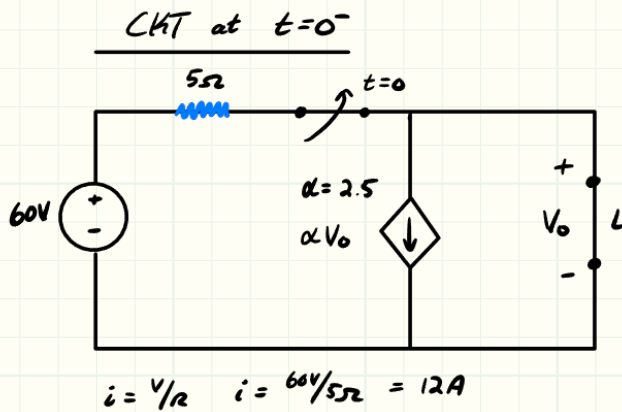
$$V_o(t) = A + Be^{-ct},$$

where A and B are in units of volts and c has units of rps (i.e., rad/sec; c is the reciprocal of the time constant). State your by-hand solutions for A , B , and c , and **list your A , B , and c values with appropriate units in proper engineering notation format with two decimal places of precision.**

Also, sketch the response. Label the plot axes on your sketch and otherwise make your sketch neat-looking and easy to comprehend.

b) Use the LTSpice verification testbench which has been provided to you to verify your by-hand answers for A , B , and c . **List the *maxerror* value you attained from the LTSpice verification testbench;** you should ensure that the *maxerror* value listed in the Spice Error Log (ctrl-L) is less than or equal to the value given in the testbench comment. If you do not achieve a *maxerror* less than or equal to the value given in the testbench comment, **something is wrong**, and you should work to resolve the issues with your by-hand solutions for A , B , and c prior to submitting. Attach a screenshot of the Spice Error Log showing the value of *maxerror* that you attained.

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$$\alpha V_0 + 12mA = 0$$

$$2.5V_0 = -12mA$$

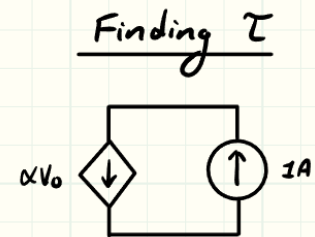
$$V_0 = -\frac{12mA}{2.5}$$

$$V_0 = -4.8V$$

$$\boxed{B = -4.8V}$$

at $t \rightarrow \infty$,
there is no voltage
drop, so $V_0(\infty) = 0$

$$\boxed{A = 0V}$$



$$\alpha V_0 = 1A$$

$$2.5V_0 = 1A$$

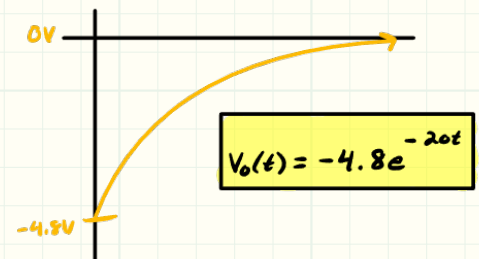
$$V_0 = 1/2.5 = 0.4$$

$$R_{eq} = 0.4$$

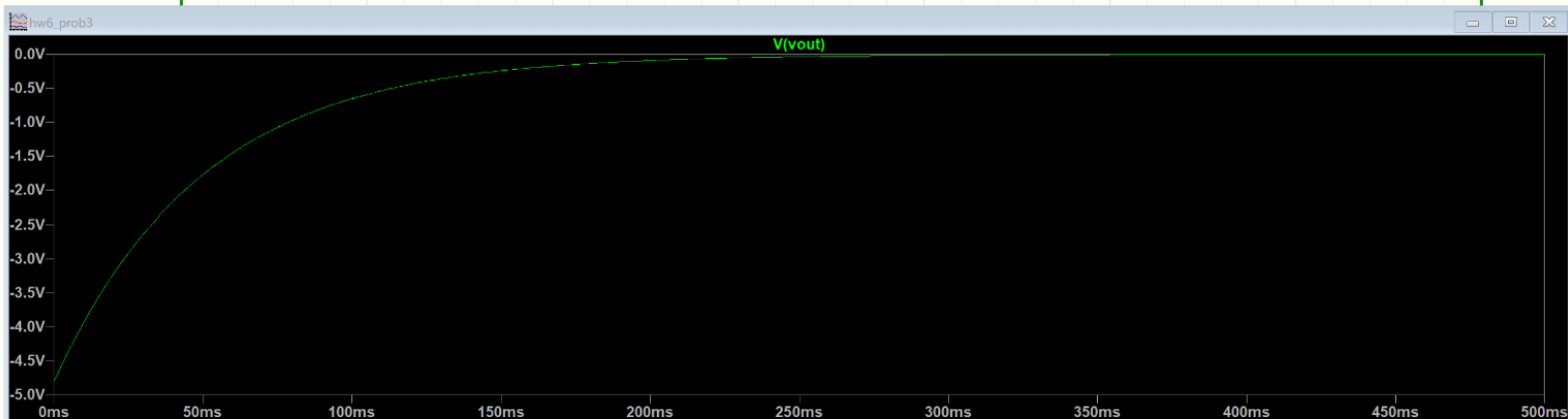
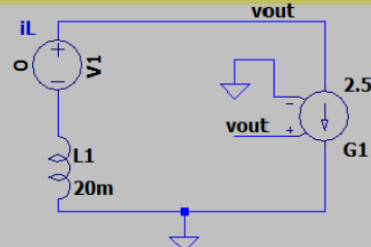
$$\tau = \frac{L}{R_{eq}} = \frac{20mH}{0.4} = 0.05$$

$$C = 1/\tau = 1/0.05 = 20rps$$

$$\boxed{C = 20rps}$$



maxerror: MAX(abs(v(vout)-v(voutcheck)))=0.000112577250486 FROM 0 TO 0.5



4) Consider the circuit shown in Figure 4 below.

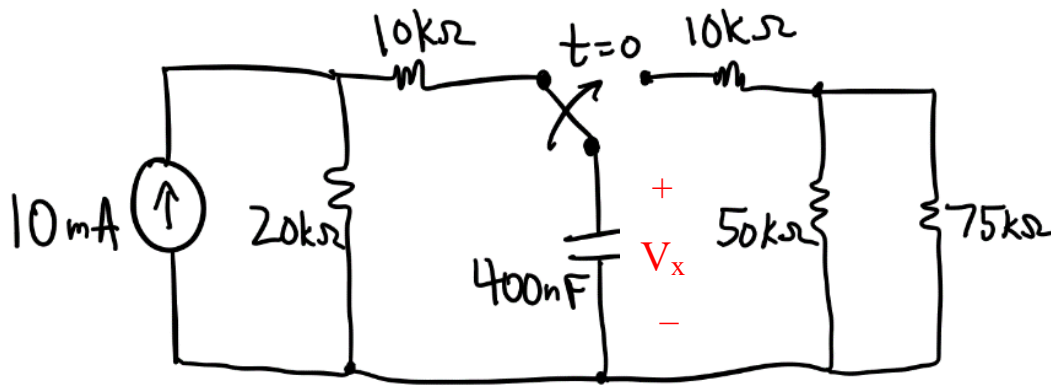


Figure 4. Circuit for Problem 4.

a) The response $V_x(t)$ for $t \geq 0$ can be written as

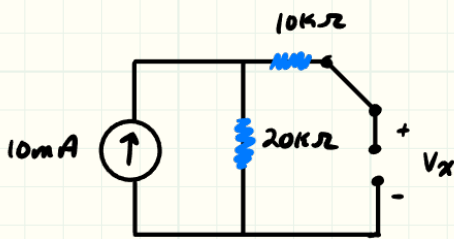
$$V_x(t) = A + Be^{-ct},$$

where A and B are in units of volts and c has units of rps (i.e., rad/sec; c is the reciprocal of the time constant). State your by-hand solutions for A , B , and c , and **list your A , B , and c values with appropriate units in proper engineering notation format with two decimal places of precision.**

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CHT at $t = 0^-$

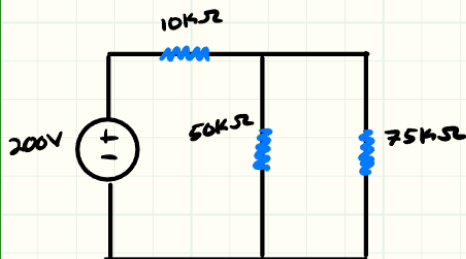


$$V = IR$$

$$V_x = (10mA)(20k\Omega)$$

$$V_x = 200V$$

CHT at $t = 0^+$



$$V_x(0^-) = V_x(0^+)$$

$$B = 200V$$

at $V(\infty)$,

all sources are deactivated
so all voltage goes to zero

$$V_x(\infty) = 0$$

$$A = 0V$$

$$\tau = RC$$

$$\tau = R_{eq} \cdot 400nF$$

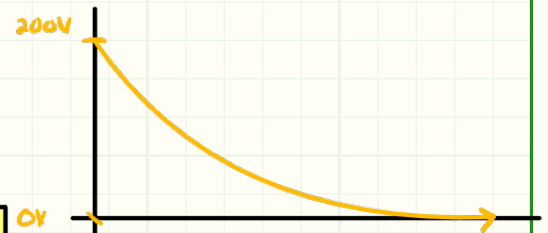
$$\tau = \left[\left(\frac{50k \cdot 75k}{50k + 75k} \right) + 10k \right] \cdot 400nF$$

$$\tau = 0.016$$

$$C = 1/\tau$$

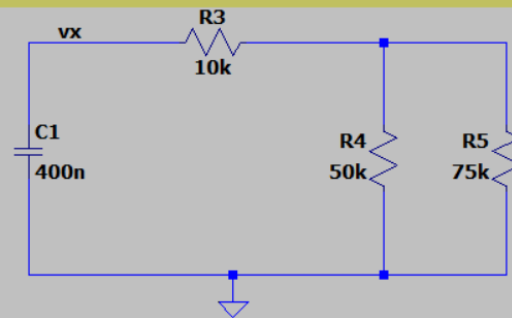
$$C = 1/0.016$$

$$C = 62.5\mu s$$



$$V_x(t) = 200e^{-62.5t}$$

maxerror: MAX(abs(v(vx)-v(vxcheck)))=0.0050673314236 FROM 0 TO 0.16



hw6_prob4

V(vx)

