

Bertinelli_Gabriele_rlab06

June 1, 2023

1 RLab06 - Gabriele Bertinelli (1219907 - tri)

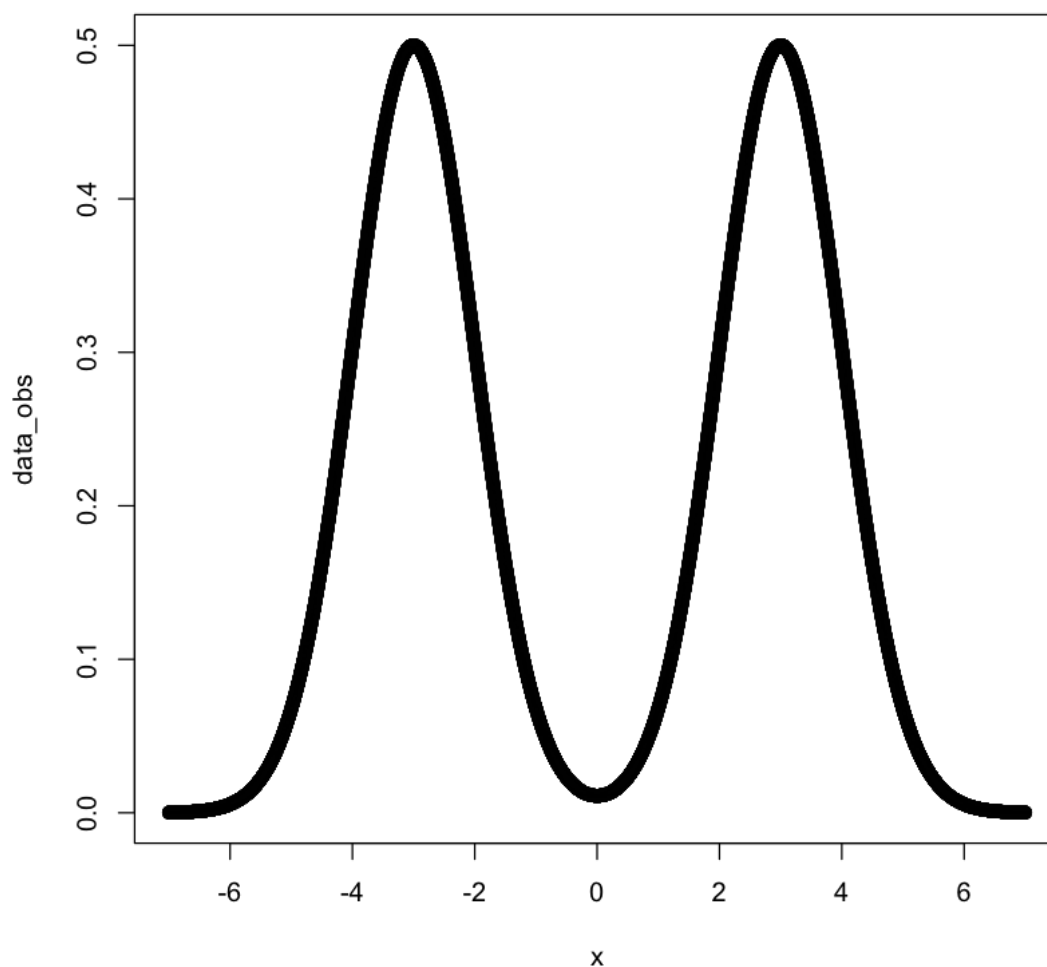
```
[34]: library(tidyverse)
library(emdbook)
library(gridExtra)
library(rjags)
library(tidybayes)
library(emdbook)
```

2 1)

```
[2]: g<-function(t){
  0.5*exp(-(t+3)**2/2))+0.5*exp(-0.5*(t-3)**2)
}
```

```
[3]: data_size <- 1000
x<-seq(-7,7,1/data_size)
data_obs<- g(x)
data <- NULL
data$X <- data_obs
```

```
[4]: plot(x,data_obs)
```



```
[5]: # func : a function whose first argument is a real vector of parameters
# func returns a log10 of the likelihood function
# theta.init : the initial value of the Markov Chain (and of func)
# n.sample: number of required samples
# sigma : standar deviation of the gaussian MCMC sampling pdf

metropolis.1dim <- function(func, theta.init, n.sample , sigma) {

  theta.cur <- theta.init
  func.Cur <- func(theta.cur)

  func.Samp <- matrix(data=NA, nrow=n.sample , ncol=2+1)
```

```

n.accept <- 0
rate.accept <- 0.0

for (n in 1:n.sample) {

  theta.prop <- rnorm(n=1, mean = theta.cur, sigma)
  func.Prop <- func(theta.prop)
  logMR <- func.Prop - func.Cur # Log10 of the Metropolis ratio

  if ( logMR >=0 || logMR>log10(runif(1)) ) {
    theta.cur <- theta.prop
    func.Cur <- func.Prop
    n.accept <- n.accept + 1
  }

  func.Samp[n, 1] <- func.Cur
  func.Samp[n, 2] <- theta.cur

}

return(func.Samp)
}

# - interface for the metropolis function , gets the log10 of test function
testfunc.metropolis <- function(theta) {
  return(log10(g(theta))) }

```

```
[6]: options(repr.plot.width=20, repr.plot.height=6)
```

```

sigma<-c(0.5,1,5,10)

for (i in 1:length(sigma)){

  ### Running parameters
  theta.init <- 3
  sample.sig <- sigma[i]
  n.sample <- 10**5

  chain <- metropolis.1dim(func=testfunc.metropolis ,
                          theta.init = theta.init, n.sample = n.sample ,
                          sigma = sample.sig**2)

```

```

par(mfrow=c(1,2))

x <- seq(-7, 7, length.out=10**4)
y <- g(x)
ymax <- 1.05 * max(y)

# Compute normalization function: used later to put on same as histogram
Zfunc <- sum(y)*diff(range(x))/(length(x))

plot(x, y, ylim=c(0,max(y)*1.10), type='l', lwd=2, col='firebrick3')

plot(x, y, type="n" , yaxs="i" , ylim=c(0,1.05*max(y)))

sa <- which(chain[,2]>=min(x) & chain[,2]<=max(x))

hist <- hist(chain[sa,2], breaks=seq(from=min(x), to=max(x),length.out=100),
  ↪plot=FALSE)
Zhist <- sum(hist$counts)*diff(range(hist$breaks))/(length(hist$counts))
lines(hist$breaks , c(hist$counts*Zfunc/Zhist,0), col='navy', type="s" , lwd=2,
  ↪lty=5)

lines(x, y, lwd=1, lty=1)

leg.labels = c('analytical', 'MCMC')
leg.ltype = c(1, 5)
leg.colors = c('firebrick3','navy')
legend("topleft" , inset=.05, bty='n', legend = leg.labels, lty=leg.ltype,
  ↪col=leg.colors,lwd = 2)

c.chain1 <- as.mcmc(chain[,2])

my.lags = seq(0,500,10)

y1 <- autocorr(c.chain1, lags=my.lags)

thin<-1
plot(my.lags, y1, ylim=c(0,1), pch=12, col='navy', xlab='lag', ylab='ACF',
  ↪cex=1.3)
text(400,0.9, sprintf('sigma:%.2f',sample.sig))
text(400,0.85,sprintf(" effective size: %.2f" , effectiveSize(c.chain1)))
text(400,0.95, sprintf('thinning:%.2f',thin))

allSamp<-chain
thin<-10
thinSel <- seq(from=1, to=nrow(allSamp), by=thin) # thin by factor 25

```

```

postSamp <- allSamp[thinSel ,]

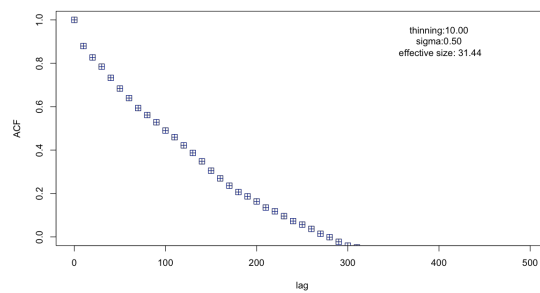
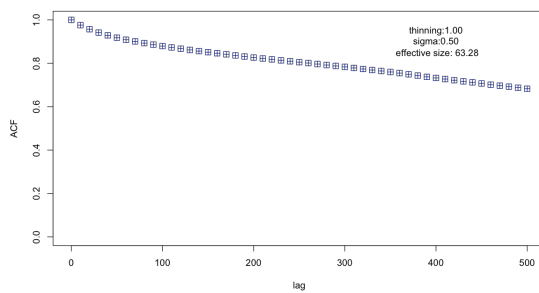
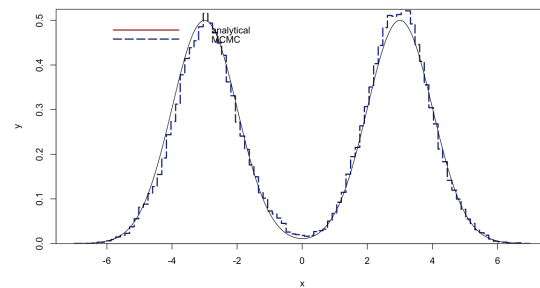
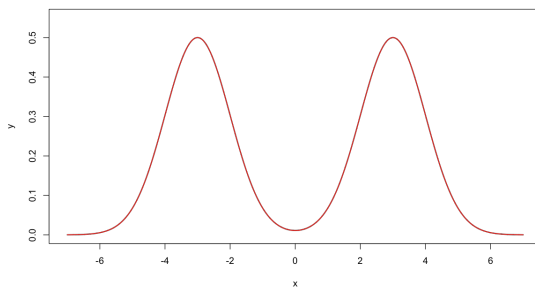
c.chain1 <- as.mcmc(postSamp[,2])

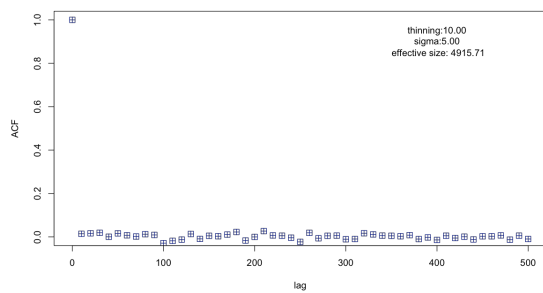
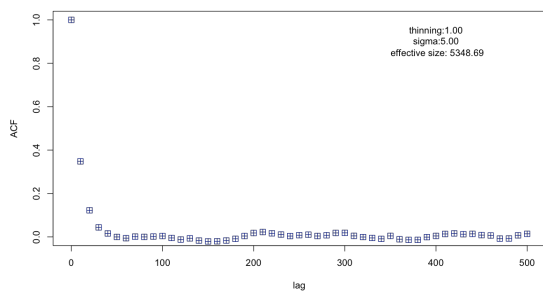
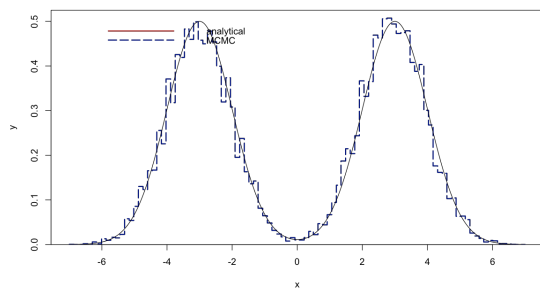
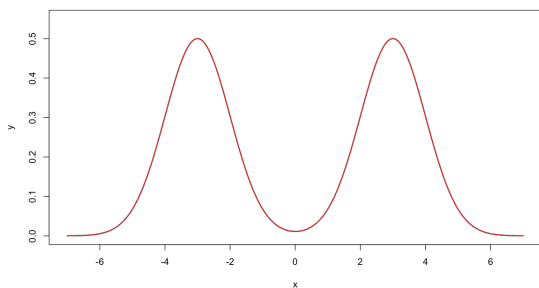
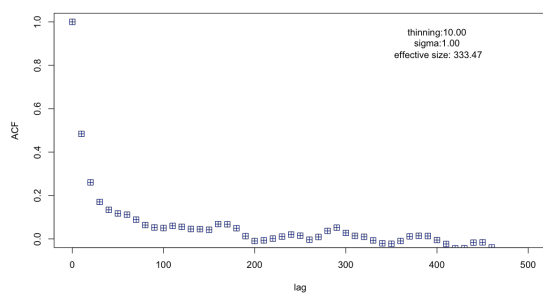
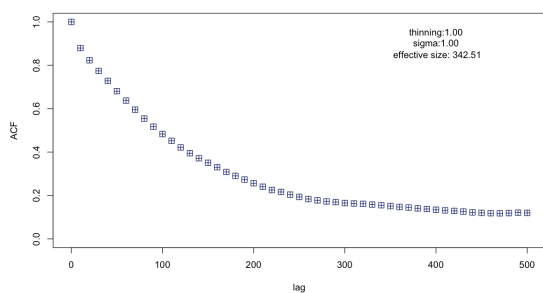
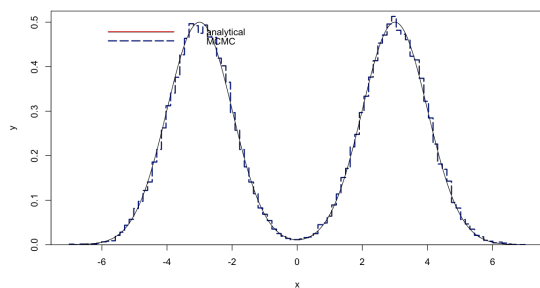
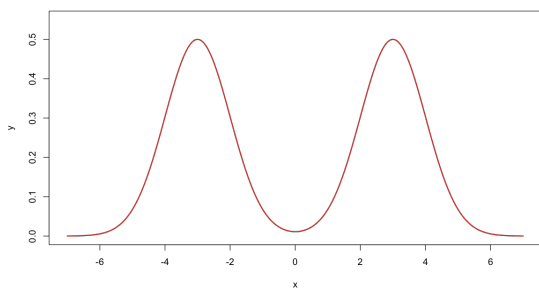
my.lags = seq(0,500,10)

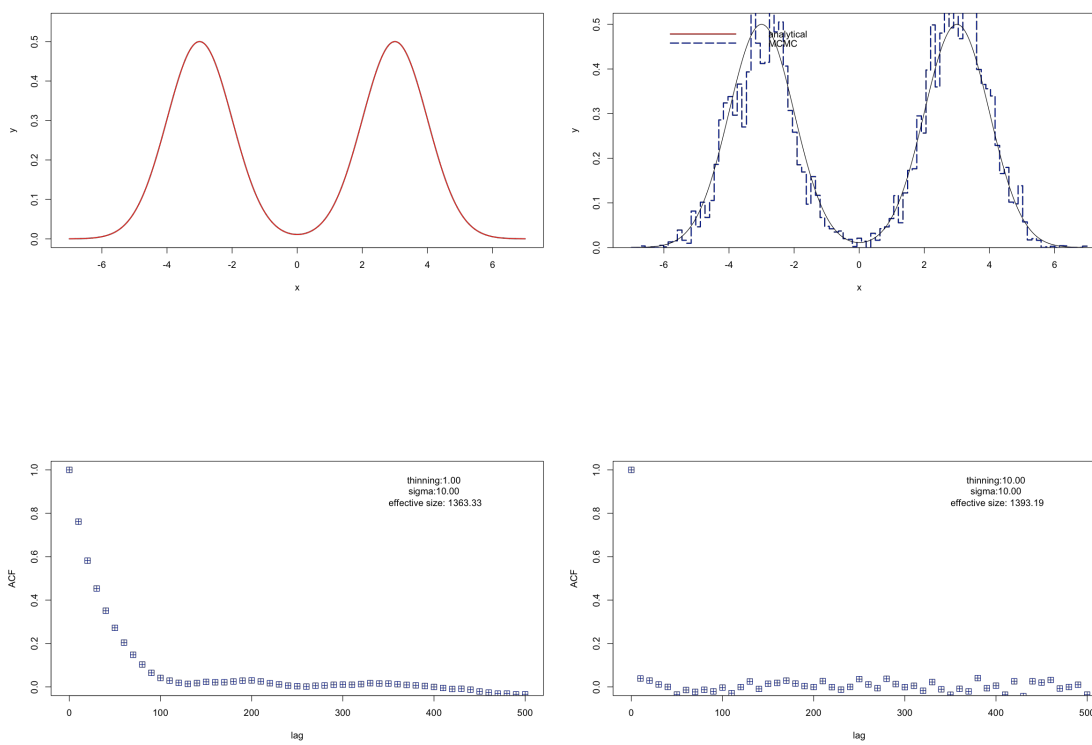
y1 <- autocorr(c.chain1, lags=my.lags)

plot(my.lags, y1, ylim=c(0,1), pch=12, col='navy', xlab='lag', ylab='ACF',
      cex=1.3)
text(400,0.9, sprintf('sigma: %.2f', sample.sig))
text(400,0.85, sprintf(" effective size: %.2f" , effectiveSize(c.chain1)))
text(400,0.95, sprintf('thinning: %.2f', thin))
}

```







3 2)

[107]: *#janssen and Jcovden -> same vaccines*

```
tot_vaccine <- 19630
tot_placebo <- 19691

patient <- c(rep(" Vaccine" , tot_vaccine), rep(" Placebo" , tot_placebo))

# Number of patients tested postive after RCT:

pos_vaccine <- 116
pos_placebo <- 348
tested <- c(rep(" Pos" , pos_vaccine),
            rep(" Neg" , tot_vaccine - pos_vaccine),
            rep(" Pos" , pos_placebo),
            rep(" Neg" , tot_placebo - pos_placebo))

janssen.tb <- tibble(tested = tested, patient=patient)
```

```
table(janssen.tb[[2]], janssen.tb[[1]])
head(janssen.tb)
```

	Neg	Pos
Placebo	19343	348
Vaccine	19514	116

	tested <chr>	patient <chr>
	Pos	Vaccine
	Pos	Vaccine
	Pos	Vaccine
	Pos	Vaccine
	Pos	Vaccine
	Pos	Vaccine

A tibble: 6 × 2

```
[108]: dataList = list(tested = ifelse(janssen.tb$tested == " Neg" , 0, 1),
                        patient = as.integer(factor(janssen.tb$patient)),
                        Ntot = nrow(janssen.tb) ,
                        Nclass = nlevels(factor(janssen.tb$patient))
                      )

#model
model_bugs <- "model{
  for ( i in 1:Ntot ){
    tested[i] ~ dbern( theta[patient[i]] )
  }

  for ( k in 1:Nclass ) {
    theta[k] ~ dbeta(3 , 100) } }"

jm <- jags.model(textConnection(model_bugs), data=dataList)
```

Compiling model graph


```

Resolving undeclared variables
Allocating nodes
Graph information:
  Observed stochastic nodes: 39321
  Unobserved stochastic nodes: 2
  Total graph size: 78648

```

Initializing model

```

[109]: # Update the Markov chain (Burn -in)
update (jm , 10000)
chain <- coda.samples(jm , c("theta"), n.iter=10000)
summary(chain)

```

```

Iterations = 10001:20000
Thinning interval = 1
Number of chains = 1
Sample size per chain = 10000

```

1. Empirical mean and standard deviation for each variable,
plus standard error of the mean:

	Mean	SD	Naive SE	Time-series SE
theta[1]	0.017744	0.0009314	9.314e-06	9.314e-06
theta[2]	0.006034	0.0005521	5.521e-06	5.521e-06

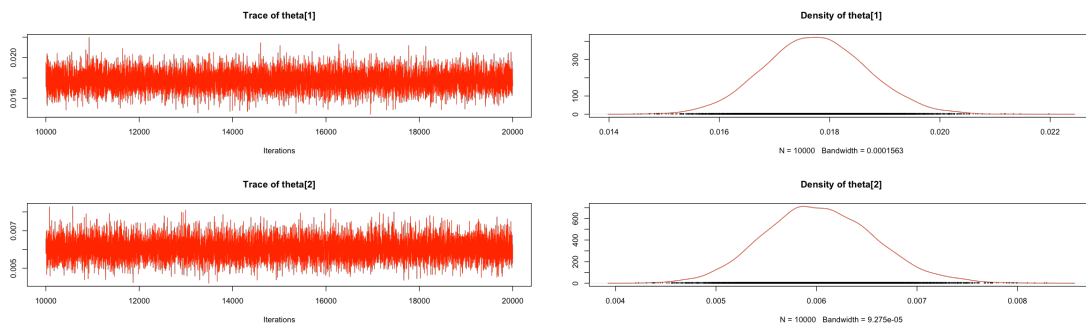
2. Quantiles for each variable:

	2.5%	25%	50%	75%	97.5%
theta[1]	0.01594	0.017119	0.017735	0.018366	0.019589
theta[2]	0.00500	0.005656	0.006016	0.006401	0.007173

```

[110]: plot(chain, col="red")

```



```
[111]: janssen_res<- tidybayes::tidy_draws(chain) %>%
      select('theta[1]':'theta[2]') %>%
      rename(Placebo = 'theta[1]', Vaccine = 'theta[2]') %>%
      mutate(diff_rate = (Placebo - Vaccine) / Placebo * 100,
             Placebo_perc = Placebo * 100, Vaccine_perc = Vaccine * 100)

allmcmc2 <- as.mcmc(janssen_res, vars="diff_rate" )

df<-as.data.frame(allmcmc2)

rates<-as_tibble(janssen_res$diff_rate)

ci<-summarise_draws(rates, mean,~quantile(.x,probs = c(0.025, 0.975)))

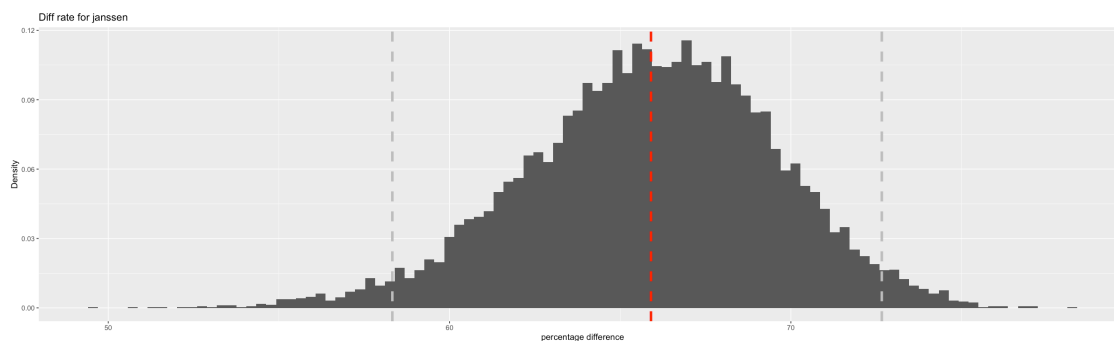
print(ci)

a <- ggplot() +
  geom_histogram(aes(df$diff_rate, y=after_stat(density)), bins=100) +
  geom_vline(xintercept =ci[[3]],linetype='dashed',
  ↪color='grey',linewidth=1.5)+
  geom_vline(xintercept=
  ↪ci[[4]],linetype='dashed',color='grey',linewidth=1.5)+
  geom_vline(xintercept=
  ↪ci[[2]],linetype='dashed',color='red',linewidth=1.5)+

  labs(title='Diff rate for janssen', x='percentage difference',
        y='Density')

a
```

```
# A tibble: 1 × 4
  variable mean `2.5%` `97.5%`
  <chr>    <num> <num>
<num>
1 value      65.9  58.3   72.7
```



```
[103]: #Spikevax

tot_vaccine <- 14134
tot_placebo <- 14073

patient <- c(rep(" Vaccine" , tot_vaccine), rep(" Placebo" , tot_placebo))

# Number of patients tested postive after RCT:

pos_vaccine <- 11
pos_placebo <- 185
tested <- c(rep(" Pos" , pos_vaccine),
            rep(" Neg" , tot_vaccine - pos_vaccine),
            rep(" Pos" , pos_placebo),
            rep(" Neg" , tot_placebo - pos_placebo))

spikevax.tb <- tibble(tested = tested, patient=patient)

table(spikevax.tb[[2]], spikevax.tb[[1]])
head(spikevax.tb)
```

	Neg	Pos
Placebo	13888	185
Vaccine	14123	11

	tested <chr>	patient <chr>
	Pos	Vaccine
	Pos	Vaccine
	Pos	Vaccine
	Pos	Vaccine
	Pos	Vaccine
	Pos	Vaccine

A tibble: 6 × 2

```
[104]: dataList = list(tested = ifelse(spikevax.tb$tested == " Neg" , 0, 1),
                      patient = as.integer(factor(spikevax.tb$patient)),
                      Ntot = nrow(spikevax.tb) ,
                      Nclass = nlevels(factor(spikevax.tb$patient))

)

#model
model_bugs <- "model{
```

```

for ( i in 1:Ntot ){
  tested[i] ~ dbern( theta[patient[i]] )
}

for ( k in 1:Nclass ) {
  theta[k] ~ dbeta(3 , 100) } }"

jm <- jags.model(textConnection(model_bugs), data=dataList)

```

Compiling model graph
 Resolving undeclared variables
 Allocating nodes
 Graph information:
 Observed stochastic nodes: 28207
 Unobserved stochastic nodes: 2
 Total graph size: 56420

Initializing model

```

[105]: # Update the Markov chain (Burn -in)
update (jm , 10000)
chain <- coda.samples(jm , c("theta"), n.iter=10000)
summary(chain)
plot(chain, col="red")

```

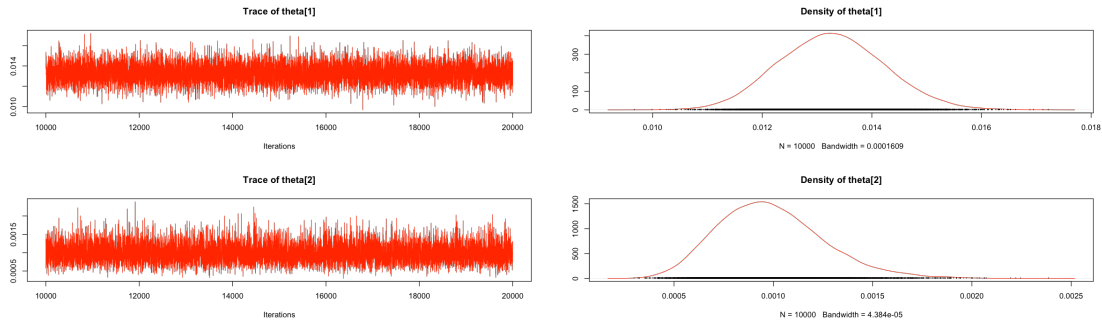
Iterations = 10001:20000
 Thinning interval = 1
 Number of chains = 1
 Sample size per chain = 10000

1. Empirical mean and standard deviation for each variable,
 plus standard error of the mean:

	Mean	SD	Naive SE	Time-series SE
theta[1]	0.0132698	0.0009578	9.578e-06	9.435e-06
theta[2]	0.0009881	0.0002653	2.653e-06	2.653e-06

2. Quantiles for each variable:

	2.5%	25%	50%	75%	97.5%
theta[1]	0.0114572	0.01261	0.0132538	0.01391	0.015202
theta[2]	0.0005394	0.00080	0.0009665	0.00115	0.001576



```
[106]: spikevax_res<- tidybayes::tidy_draws(chain) %>%
  select('theta[1]':'theta[2]') %>%
  rename(Placebo = 'theta[1]', Vaccine = 'theta[2]') %>%
  mutate(diff_rate = (Placebo - Vaccine) / Placebo * 100,
         Placebo_perc = Placebo * 100, Vaccine_perc = Vaccine * 100)

allmcmc2 <- as.mcmc(spikevax_res, vars="diff_rate" )

df<-as.data.frame(allmcmc2)

rates<-as_tibble(spikevax_res$diff_rate)

ci<-summarise_draws(rates, mean,~quantile(.x,probs = c(0.025, 0.975)))

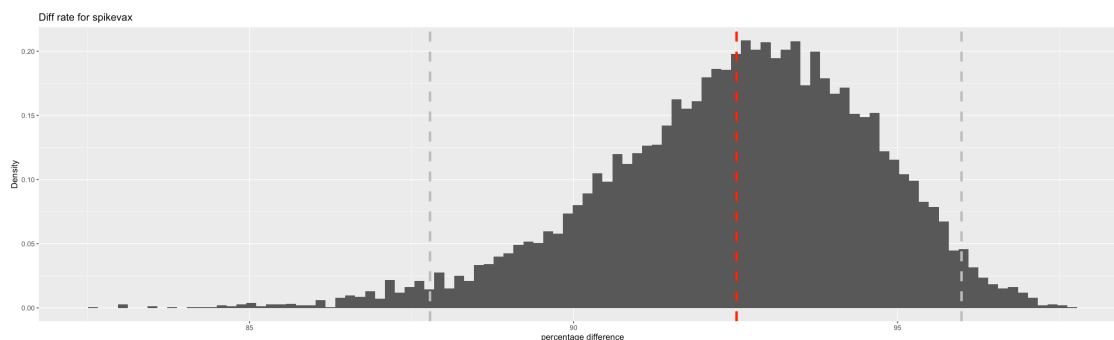
print(ci)

a <- ggplot() +
  geom_histogram(aes(df$diff_rate, y=after_stat(density)), bins=100) +
  geom_vline(xintercept =ci[[3]],linetype='dashed',
  ↪color='grey',linewidth=1.5)+
  geom_vline(xintercept=
  ↪ci[[4]],linetype='dashed',color='grey',linewidth=1.5)+
  geom_vline(xintercept=
  ↪ci[[2]],linetype='dashed',color='red',linewidth=1.5)+

  labs(title='Diff rate for spikevax', x='percentage difference',
        y='Density')

a
```

```
# A tibble: 1 × 4
  variable mean `2.5%` `97.5%`
  <chr>     <num> <num>
<num>
1 value      92.5   87.8   96.0
```



```
[95]: #astrazeneca
tot_vaccine <- 5258
tot_placebo <- 5210

patient <- c(rep(" Vaccine" , tot_vaccine), rep(" Placebo" , tot_placebo))

# Number of patients tested postive after RCT:

pos_vaccine <- 64
pos_placebo <- 154
tested <- c(rep(" Pos" , pos_vaccine),
            rep(" Neg" , tot_vaccine - pos_vaccine),
            rep(" Pos" , pos_placebo),
            rep(" Neg" , tot_placebo - pos_placebo))

astrazeneca.tb <- tibble(tested = tested, patient=patient)

table(astrazeneca.tb[[2]], astrazeneca.tb[[1]])
head(astrazeneca.tb)
```

	Neg	Pos
Placebo	5056	154
Vaccine	5194	64

	tested	patient
	<chr>	<chr>
	Pos	Vaccine
	Pos	Vaccine
	Pos	Vaccine
	Pos	Vaccine
	Pos	Vaccine
	Pos	Vaccine

A tibble: 6 × 2

```
[96]: dataList = list(tested = ifelse(astrazeneca.tb$tested == " Neg" , 0, 1),
                        patient = as.integer(factor(astrazeneca.tb$patient)),
                        Ntot = nrow(astrazeneca.tb) ,
                        Nclass = nlevels(factor(astrazeneca.tb$patient))

)

#model
model_bugs <- "model{

for ( i in 1:Ntot ){
    tested[i] ~ dbern( theta[patient[i]] )
}

for ( k in 1:Nclass ) {
    theta[k] ~ dbeta(3 , 100) } }"

jm <- jags.model(textConnection(model_bugs), data=dataList)
```

Compiling model graph
 Resolving undeclared variables
 Allocating nodes
 Graph information:
 Observed stochastic nodes: 10468
 Unobserved stochastic nodes: 2
 Total graph size: 20942

Initializing model

```
[97]: # Update the Markov chain (Burn -in)
update (jm , 10000)
chain <- coda.samples(jm , c("theta"), n.iter=10000)
summary(chain)
plot(chain, col="red")
```

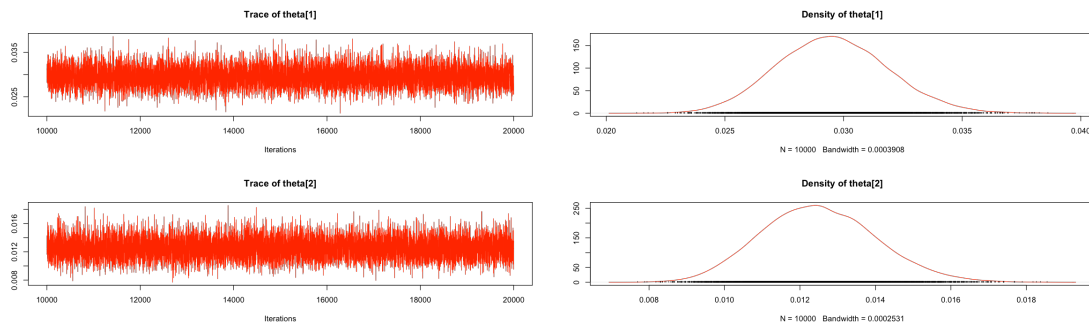
Iterations = 10001:20000
 Thinning interval = 1
 Number of chains = 1
 Sample size per chain = 10000

1. Empirical mean and standard deviation for each variable,
 plus standard error of the mean:

	Mean	SD	Naive SE	Time-series SE
theta[1]	0.02955	0.002326	2.326e-05	2.326e-05
theta[2]	0.01250	0.001507	1.507e-05	1.464e-05

2. Quantiles for each variable:

	2.5%	25%	50%	75%	97.5%
theta[1]	0.025156	0.02794	0.02950	0.03109	0.03423
theta[2]	0.009735	0.01144	0.01245	0.01350	0.01559



```
[102]: astrazeneca_res<- tidybayes::tidy_draws(chain) %>%
  select('theta[1]':'theta[2]') %>%
  rename(Placebo = 'theta[1]', Vaccine = 'theta[2]') %>%
  mutate(diff_rate = (Placebo - Vaccine) / Placebo * 100,
         Placebo_perc = Placebo * 100, Vaccine_perc = Vaccine * 100)

allmcmc2 <- as.mcmc(astrazeneca_res, vars="diff_rate" )

df<-as.data.frame(allmcmc2)

rates<-as_tibble(astrazeneca_res$diff_rate)

ci<-summarise_draws(rates, mean,~quantile(.x,probs = c(0.025, 0.975)))

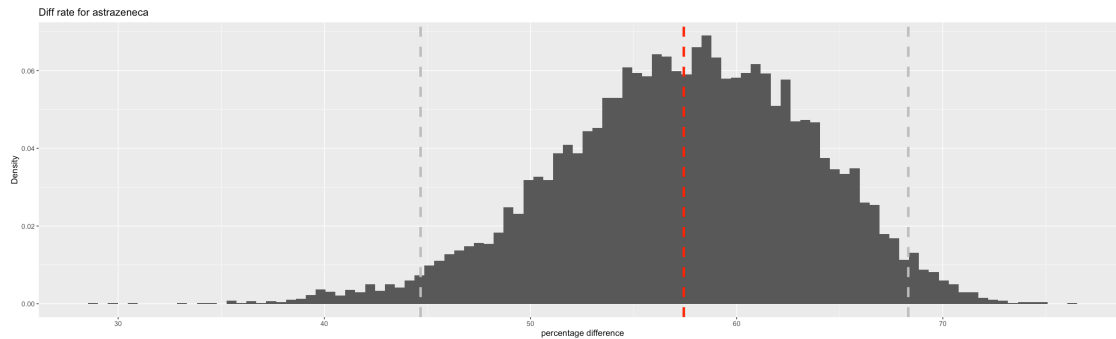
print(ci)

a <- ggplot() +
  geom_histogram(aes(df$diff_rate, y=after_stat(density)), bins=100) +
  geom_vline(xintercept =ci[[3]],linetype='dashed',
  ↪color='grey',linewidth=1.5)+
  geom_vline(xintercept=
  ↪ci[[4]],linetype='dashed',color='grey',linewidth=1.5)+
  geom_vline(xintercept=
  ↪ci[[2]],linetype='dashed',color='red',linewidth=1.5)+

  labs(title='Diff rate for astrazeneca', x='percentage difference',
       y='Density')
```


a

```
# A tibble: 1 × 4
  variable mean `2.5%` `97.5%`
  <chr>     <num> <num>
<num>
1 value      57.4  44.7   68.3
```



4 3

```
[167]: covid <- read.delim("owid-covid-data.csv", header = TRUE, sep = ",",)
```

```
[168]: colnames(covid)
```

```
1. 'iso_code' 2. 'continent' 3. 'location' 4. 'date' 5. 'total_cases'
6. 'new_cases' 7. 'new_cases_smoothed' 8. 'total_deaths' 9. 'new_deaths'
10. 'new_deaths_smoothed' 11. 'total_cases_per_million' 12. 'new_cases_per_million'
13. 'new_cases_smoothed_per_million' 14. 'total_deaths_per_million'
15. 'new_deaths_per_million' 16. 'new_deaths_smoothed_per_million'
17. 'reproduction_rate' 18. 'icu_patients' 19. 'icu_patients_per_million'
20. 'hosp_patients' 21. 'hosp_patients_per_million' 22. 'weekly_icu_admissions'
23. 'weekly_icu_admissions_per_million' 24. 'weekly_hosp_admissions'
25. 'weekly_hosp_admissions_per_million' 26. 'total_tests' 27. 'new_tests' 28. 'total_tests_per_thousand'
29. 'new_tests_per_thousand' 30. 'new_tests_smoothed'
31. 'new_tests_smoothed_per_thousand' 32. 'positive_rate' 33. 'tests_per_case' 34. 'tests_units'
35. 'total_vaccinations' 36. 'people_vaccinated' 37. 'people_fully_vaccinated' 38. 'total_boosters'
39. 'new_vaccinations' 40. 'new_vaccinations_smoothed' 41. 'total_vaccinations_per_hundred'
42. 'people_vaccinated_per_hundred' 43. 'people_fully_vaccinated_per_hundred'
44. 'total_boosters_per_hundred' 45. 'new_vaccinations_smoothed_per_million'
46. 'new_people_vaccinated_smoothed' 47. 'new_people_vaccinated_smoothed_per_hundred'
48. 'stringency_index' 49. 'population_density' 50. 'median_age' 51. 'aged_65_older'
52. 'aged_70_older' 53. 'gdp_per_capita' 54. 'extreme_poverty' 55. 'cardiovasc_death_rate'
56. 'diabetes_prevalence' 57. 'female_smokers' 58. 'male_smokers' 59. 'handwashing_facilities'
60. 'hospital_beds_per_thousand' 61. 'life_expectancy' 62. 'human_development_index'
```

63. 'population' 64. 'excess_mortality_cumulative_absolute' 65. 'excess_mortality_cumulative'
 66. 'excess_mortality' 67. 'excess_mortality_cumulative_per_million'

Columns used: - new_vaccinations: New COVID-19 vaccination doses administered (only calculated for consecutive days) - total_vaccinations: Total number of COVID-19 vaccination doses administered - new_deaths: New deaths attributed to COVID-19. Counts can include probable deaths, where reported. - total_deaths: Total deaths attributed to COVID-19. Counts can include probable deaths, where reported.

<https://github.com/owid/covid-19-data/tree/master/public/data>

```
[333]: deaths<-data.frame(covid$date,covid$new_deaths,covid$total_deaths)

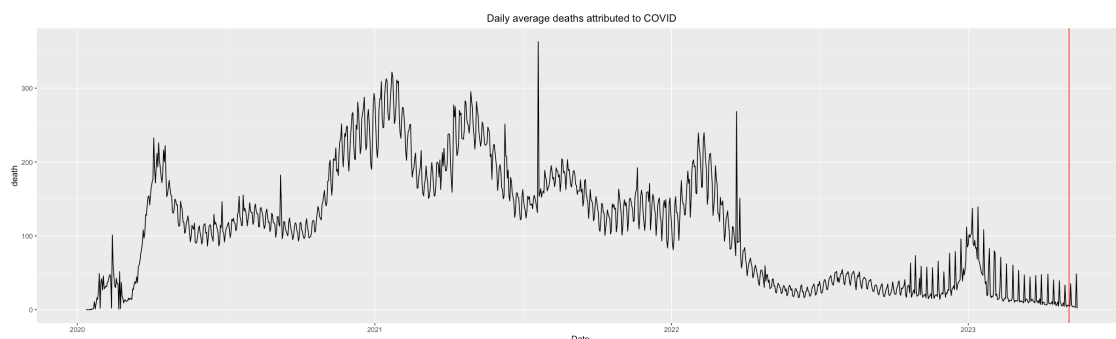
deaths$covid.date <- as.Date(deaths$covid.date, "%Y-%m-%d")

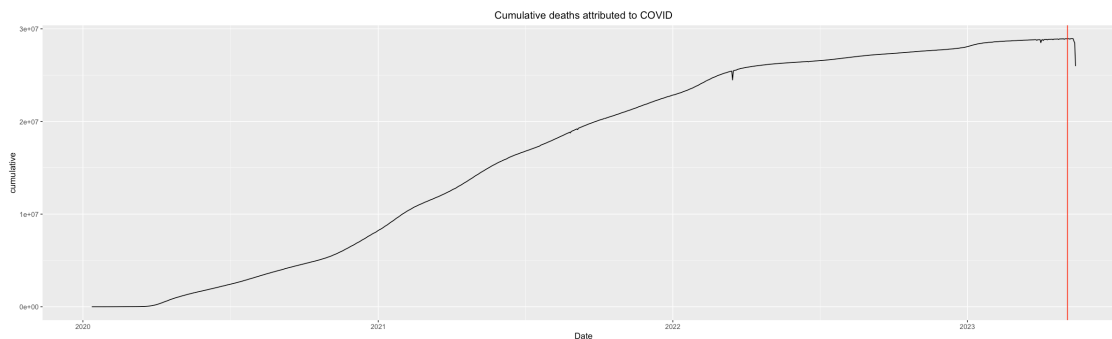
deaths<-as_tibble(deaths)

tda<-deaths$covid.date
deaths$week <- (interval(min(tda), tda) %/% weeks(1)) + 1

a<-deaths %>% drop_na() %>% group_by(covid.date)%>%
  summarise(death = mean(covid.new_deaths),
            cumulative=sum(covid.total_deaths))
a<-slice(a, 1:(n() - 2))

ggplot(data=a,aes(x=covid.date,y=death))+geom_line(aes(y=death))+
  ↪geom_vline(xintercept =as.Date('2023-05-05',"%Y-%m-%d"),color='red')+
  ggtitle("Daily average deaths attributed to COVID") +
  theme(plot.title = element_text(hjust = 0.5)) +
  xlab("Date ")
ggplot(data=a,aes(x=covid.date,y=cumulative))+geom_line(aes(y=cumulative))+
  ↪geom_vline(xintercept =as.Date('2023-05-05',"%Y-%m-%d"),color='red')+
  ggtitle("Cumulative deaths attributed to COVID") +
  theme(plot.title = element_text(hjust = 0.5)) +
  xlab("Date")
```

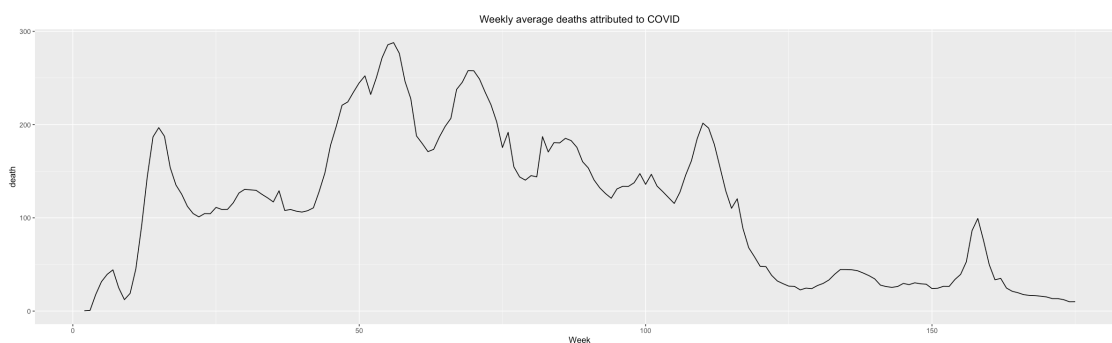


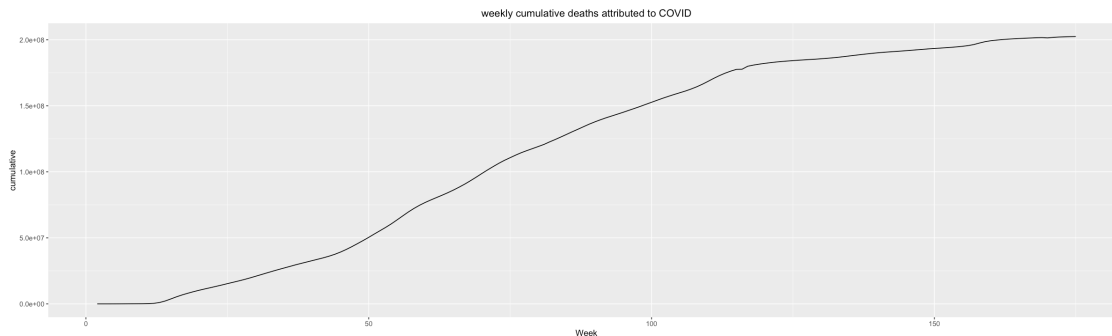


On 2023-05-05 WHO declared the end of the covid pandemic (red line).

```
[334]: a<-deaths %>% drop_na() %>% group_by(week)%>%
      summarise(death = mean(covid.new_deaths),
                 cumulative=sum(covid.total_deaths))
a<-slice(a, 1:(n() - 2))

ggplot(data=a,aes(x=week,y=death))+geom_line(aes(y=death))+ ggtitle("Weekly_
↳average deaths attributed to COVID") +
  theme(plot.title = element_text(hjust = 0.5)) +
  xlab("Week")
ggplot(data=a,aes(x=week,y=cumulative))+geom_line(aes(y=cumulative))+ggtitle("weekly_
↳cumulative deaths attributed to COVID") +
  theme(plot.title = element_text(hjust = 0.5)) +
  xlab("Week")
```





```
[335]: vax<-data.frame(covid$date,covid$new_vaccinations,covid$total_vaccinations)

vax$covid.date <- as.Date(vax$covid.date, "%Y-%m-%d")

vax<-as_tibble(vax)

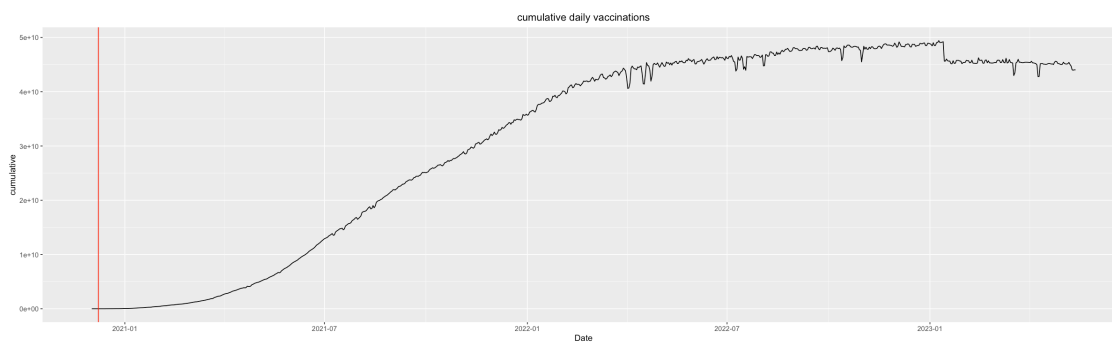
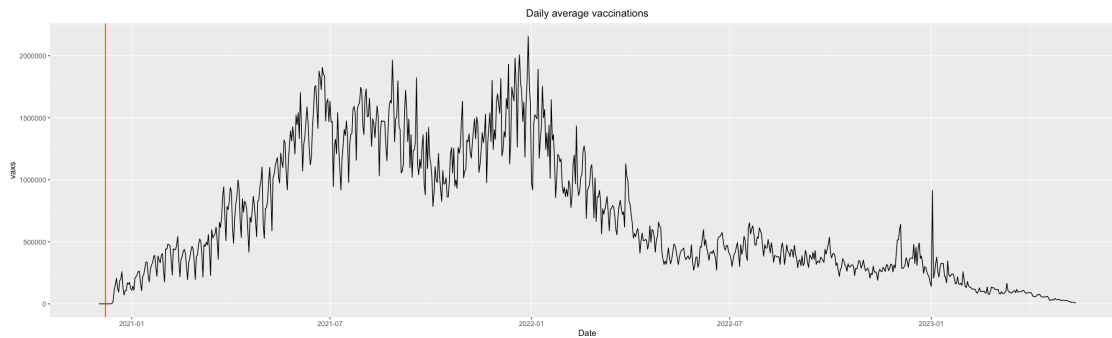
tda<-vax$covid.date
vax$week <- (interval(min(tda), tda) %/% weeks(1)) + 1


a<-vax %>% drop_na() %>% group_by(covid.date)%>%
  summarise(vaxs = mean(covid.new_vaccinations),
            cumulative=sum(covid.total_vaccinations))

a<-slice(a, 1:(n() - 6)) #discarded last six rows


ggplot(data=a,aes(x=covid.date,y=vaxs))+geom_line(aes(y=vaxs))+
  ↪geom_vline(xintercept =as.Date('2020-12-8',"%Y-%m-%d"),color='red')+
  ggtitle("Daily average vaccinations") +
  theme(plot.title = element_text(hjust = 0.5)) +
  xlab("Date")

ggplot(data=a,aes(x=covid.
  ↪date,y=cumulative))+geom_line(aes(y=cumulative))+geom_vline(xintercept =as.
  ↪Date('2020-12-8',"%Y-%m-%d"),color='red')+
  ggtitle("cumulative daily vaccinations") +
  theme(plot.title = element_text(hjust = 0.5)) +
  xlab("Date")
```



On 2020-12-8 (red line) the first person had received the vaccine.

```
[336]: a<-vax %>% drop_na() %>% group_by(week)%>%
      summarise(vaxs = mean(covid.new_vaccinations),
                 cumulative=sum(covid.total_vaccinations))
a<-slice(a, 1:(n() - 6)) #removing last six weeks for plotting purposes, data
  ↳ is not updated correctly and cumulative drops to zero

ggplot(data=a,aes(x=week,y=vaxs))+geom_line(aes(y=vaxs))+ ggtitle("Weekly
  ↳ average vaccinations") +
  theme(plot.title = element_text(hjust = 0.5)) +
  xlab("Week")

ggplot(data=a,aes(x=week,y=cumulative))+geom_line(aes(y=cumulative))+
  ↳ ggtitle("Weekly cumulative vaccinations") +
  theme(plot.title = element_text(hjust = 0.5)) +
  xlab("Week")
```

