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- R package gllvm fits Generalized linear latent variable models (GLLVM) for multivariate data (Niku et al., 2017).
- · Developed by J. Niku, W.Brooks, R. Herliansyah, F.K.C. Hui, S. Taskinen, D.I. Warton, B. van der Veen.
- GitHub: https://github.com/JenniNiku/gllvm
- CRAN: https://cran.r-project.org/web/packages/gllvm/index.html

- GLLVMs are computationally intensive to fit.
- · Often such models have been fitted using MCMC approach, which is very time consuming.
- **gllvm** package overcomes computational problems by applying closed form approximations to log-likelihood and using automatic differentiation in C++ to accelerate computation times (TMB).
- Estimation is performed using either variational approximation (VA) or Laplace approximation (LA) method implemented via **R** package **TMB**.
- VA method is faster and more accurate than LA, but not applicable for all distributions and link functions.

Using **gllvm** we can fit

- GLLVM without covariates gives model-based ordination and biplots
- GLLVM with environmental and/or trait covariates for studying factors explaining species abundance
- Fourth corner models with latent variables for studying environmentaltrait interactions
- GLLVM without latent variables fits basic multivariate GLMs

Additional tools: residuals, information criterias, confidence intervals, visualization.

Distributions

Response	Distribution	Method	Link
Counts	Poisson	VA/LA	log
	NB	VA/LA	log
	ZIP	LA	log
Binary	Bernoulli	VA/LA	probit
		LA	logit
Ordinal	Ordinal	VA	probit
Normal	Gaussian	VA/LA	identity
Positive continuous	Gamma	VA/LA	log
non-negative continuous	Exponential	VA/LA	log
Biomass	Tweedie	LA	log

Data input

Main function of the **gllvm** package is gllvm(), which can be used to fit GLLVMs for multivariate data with the most important arguments listed in the following:

```
gllvm(y = NULL, X = NULL, TR = NULL, family, num.lv = 2,
formula = NULL, method = "VA", row.eff = FALSE, n.init=1, ...)
```

- · y: matrix of abundances
- · X: matrix or data.frame of environmental variables
- TR: matrix or data.frame of trait variables
- family: distribution for responses
- num.lv: number of latent variables
- method: approximation used "VA" or "LA"
- row.eff: type of row effects
- n.init: number of random starting points for latent variables

```
## Loading required package: TMB
## Loading required package: mvabund
```

Example: Spiders

- Abundances of 12 hunting spider species measured as a count at 28 sites.
- Six environmental variables measured at each site.
 - soil.dry: Soil dry mass
 - bare.sand: cover of bare sand
 - fallen.leaves: cover of fallen leaves/twigs
 - moss: cover of moss
 - herb.layer: cover of herb layer
 - reflection: reflection of the soil surface with a cloudless sky

Data fitting

Fit GLLVM without covariates $g(E(y_{ij})) = eta_{0j} + m{u}_i'm{ heta}_j$ with <code>gllvm</code>:

```
library(mvabund)
data("spider")
library(gllvm)
fithb <- gllvm(y = spider$abund, family = "negative.binomial")
fitnb
## Call:
## gllvm(y = spider$abund, family = "negative.binomial")
## family:
## [1] "negative.binomial"
## method:
## [1] "VA"
##
## log-likelihood: -733.6806
## Residual degrees of freedom: 289
## AIC: 1561.361
## AICc: 1335.761
## BIC: 1623.975
```

Residual analysis

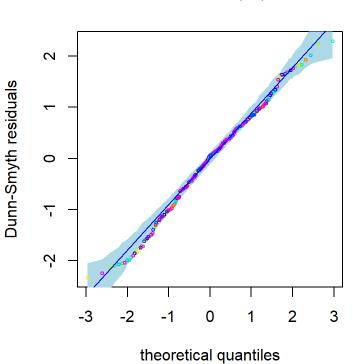
- Residual analysis can be used to assess the appropriateness of the fitted model (eg. in terms of mean-variance relationship).
- Function residuals () calculates randomized quantile residuals for the model, and plot () function provides residual plots.
- · Randomized quantile/Dunn-Smyth residuals are used in the package, as they provide standard normal distributed residuals, even for discrete responses, in the case of a proper model.

Residual analysis

```
par(mfrow = c(1,2))
plot(fithb, which = 1:2)
```

Residuals vs linear predictors

Normal Q-Q



Model selection

- Information criterias can be used for model selection.
- For example, compare distributions or choose suitable number of latent variables.

```
fitp <- gllvm(y = spider$abund, family = poisson())
fitnb <- gllvm(y = spider$abund, family = "negative.binomial")
AIC(fitp)
## [1] 1761.655
AIC(fitnb)
## [1] 1561.361</pre>
```

Exercises

- 1. Load spider data from mvabund package and take a look at the dataset.
- 2. Fit GLLVM to spider data with a suitable distribution.
- 3. Explore the fitted model. Where are the estimates for parameters? What about predicted latent variables? Standard errors?
- 4. Fit model with different numbers of latent variables.
- 5. Include environmental variables to the GLLVM and explore the model fit.

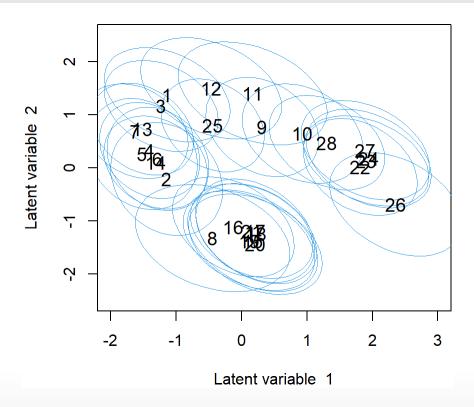
GLLVM as a model based ordination method

- · GLLVMs can be used as a model-based approach to unconstrained ordination by including two latent variables in the model: $g(E(y_{ij})) = \beta_{0j} + \boldsymbol{u}_i' \boldsymbol{\theta}_j$
- · Predictions for the two latent variables, $\hat{\boldsymbol{u}}_i = (\hat{u}_{i1}, \hat{u}_{i2})$, then provide coordinates for sites in the ordination plot and then provides a graphical representation of which sites are similar in terms of their species composition.
- The corresponding ordination plot then provides a graphical representation of which sites are similar in terms of their species composition.

Ordination plot

- · ordiplot() produces ordination plots based on fitted GLLVMs.
- · Uncertainty of the ordination points in model based ordination can be assessed with prediction errors of latent variables.

```
ordiplot(fitnb, predict.region = TRUE, ylim=c(-2.5, 2.5), xlim=c(-2,3))
```

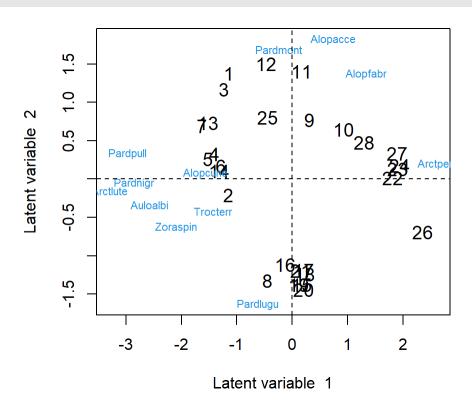


Biplot

- Between species correlations can be visualized with biplot by adding latent variable loadings θ_j to the ordination of sites, by producing a biplot, (argument biplot = TRUE in ordiplot()).
- In a biplot latent variables and their loadings are rotated so that the LV loadings of the species are in the same direction with the sites where they are most abundant.
- Biplot can be used for finding indicator species corresponding to specific sites, or finding groups of correlated species.

Biplot

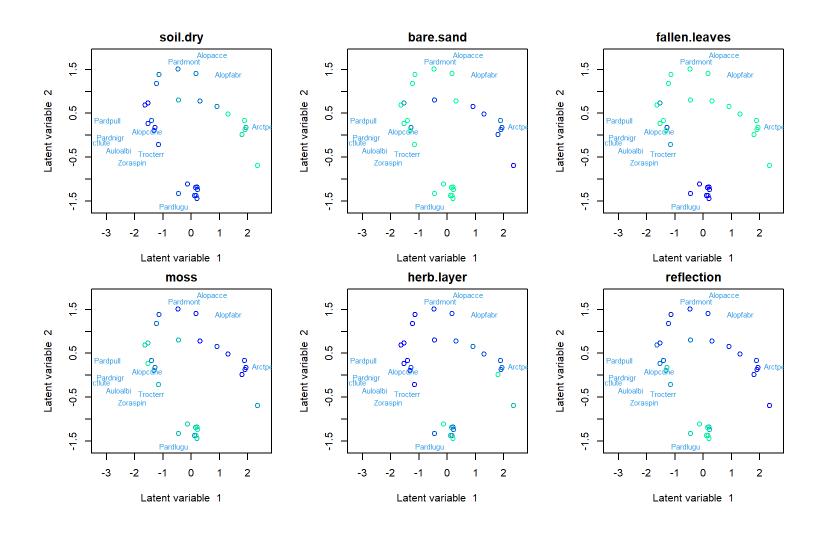
```
ordiplot(fitnb, biplot = TRUE) abline(h = 0, v = 0, lty=2)
```



Environmental gradients

The potential impact of environmental variables on species communities can be viewed by coloring ordination points according to the variables.

Environmental gradients



Environmental gradients

• The next step would be to include covariates to the model and this matter will be dealt with tomorrow.