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- R package gllvm fits Generalized linear latent variable models (GLLVM) for multivariate data (Niku et al., 2017).
- · Developed by J. Niku, W.Brooks, R. Herliansyah, F.K.C. Hui, S. Taskinen, D.I. Warton, B. van der Veen.
- GitHub: https://github.com/JenniNiku/gllvm
- CRAN: https://cran.r-project.org/web/packages/gllvm/index.html

- GLLVMs are computationally intensive to fit.
- · Often such models have been fitted using MCMC approach, which is very time consuming.
- **gllvm** package overcomes computational problems by applying closed form approximations to log-likelihood and using automatic differentiation in C++ to accelerate computation times (TMB).
- Estimation is performed using either variational approximation (VA) or Laplace approximation (LA) method implemented via **R** package **TMB**.
- VA method is faster and more accurate than LA, but not applicable for all distributions and link functions.

Using **gllvm** we can fit

- GLLVM without covariates gives model-based ordination and biplots
- GLLVM with environmental covariates for studying factors explaining species abundance
- Fourth corner models with latent variables for studying environmentaltrait interactions
- GLLVM without latent variables fits basic multivariate GLMs

Additional tools: model checking, model selection, inference, visualization.

Distributions

| Response | Distribution | Method | Link |
|-------------------------|--------------|--------|----------|
| Counts | Poisson | VA/LA | log |
| | NB | VA/LA | log |
| | ZIP | LA | log |
| Binary | Bernoulli | VA/LA | probit |
| | | LA | logit |
| Ordinal | Ordinal | VA | probit |
| Normal | Gaussian | VA/LA | identity |
| Positive continuous | Gamma | VA/LA | log |
| non-negative continuous | Exponential | VA/LA | log |
| Biomass | Tweedie | LA | log |

Data input

Main function of the **gllvm** package is gllvm(), which can be used to fit GLLVMs for multivariate data with the most important arguments listed in the following:

```
gllvm(y = NULL, X = NULL, TR = NULL, family, num.lv = 2,
formula = NULL, method = "VA", row.eff = FALSE, n.init=1, ...)
```

- · y: matrix of abundances
- · X: matrix or data.frame of environmental variables
- TR: matrix or data.frame of trait variables
- family: distribution for responses
- num.lv: number of latent variables
- method: approximation used "VA" or "LA"
- row.eff: type of row effects
- n.init: number of random starting points for latent variables

```
## Loading required package: TMB
## Loading required package: mvabund
```

Example: Spiders

- Abundances of 12 hunting spider species measured as a count at 28 sites.
- Six environmental variables measured at each site.
 - soil.dry: Soil dry mass
 - bare.sand: cover of bare sand
 - fallen.leaves: cover of fallen leaves/twigs
 - moss: cover of moss
 - herb.layer: cover of herb layer
 - reflection: reflection of the soil surface with a cloudless sky

Data fitting

Fit GLLVM without covariates $g(E(y_{ij})) = eta_{0j} + m{u}_i' m{ heta}_j$ with gllvm:

```
library(mvabund)
data("spider")
library(gllvm)
fithb <- gllvm(y = spider$abund, family = "negative.binomial")
fitnb
## Call:
## gllvm(y = spider$abund, family = "negative.binomial")
## family:
## [1] "negative.binomial"
## method:
## [1] "VA"
##
## log-likelihood: -733.6806
## Residual degrees of freedom: 289
## AIC: 1561.361
## AICc: 1335.761
## BIC: 1623.975
```

Residual analysis

- Residual analysis can be used to assess the appropriateness of the fitted model (eg. in terms of mean-variance relationship).
- Function residuals () calculates randomized quantile residuals for the model, and plot () function provides residual plots.
- Randomized quantile/Dunn-Smyth residuals are used in the package, as they provide standard normal distributed residuals, even for discrete responses, in the case of a proper model.

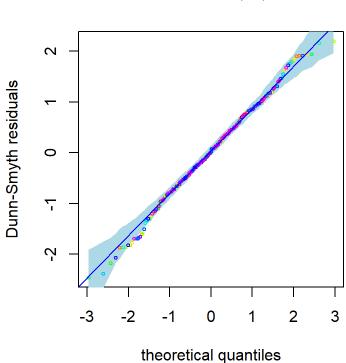
Residual analysis

```
par(mfrow = c(1,2))
plot(fithb, which = 1:2)
```

Residuals vs linear predictors

Sunun-cesiduals -8 -6 -4 -2 0 2 4 linear predictors

Normal Q-Q



Model selection

- Information criterias can be used for model selection.
- For example, compare distributions or choose suitable number of latent variables.

```
fitp <- gllvm(y = spider$abund, family = poisson())
fitnb <- gllvm(y = spider$abund, family = "negative.binomial")
AIC(fitp)
## [1] 1761.655
AIC(fitnb)
## [1] 1561.361</pre>
```

Exercises

For the next 10 minutes, try the package yourself:

- 1. Load spider data from mvabund package and take a look at the dataset.
- 2. Fit GLLVM to spider data with a suitable distribution.
- 3. Explore the fitted model. Where are the estimates for parameters? What about predicted latent variables? Standard errors?
- 4. Fit model with different numbers of latent variables.
- 5. Include environmental variables to the GLLVM and explore the model fit.

If you need help, here you can find the exercises with answers: add link

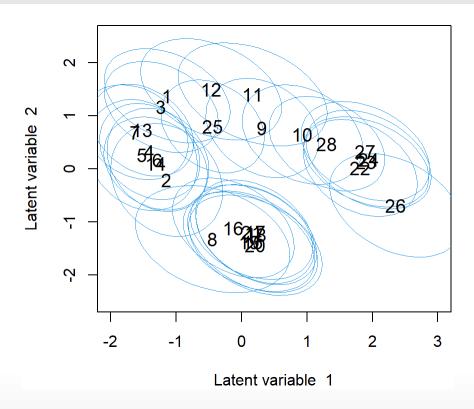
GLLVM as a model based ordination method

- · GLLVMs can be used as a model-based approach to unconstrained ordination by including two latent variables in the model: $g(E(y_{ij})) = \beta_{0j} + \boldsymbol{u}_i' \boldsymbol{\theta}_j$
- The latent variable term try to capture the underlying factors driving species abundances at sites.
- · Predictions for the two latent variables, $\hat{\boldsymbol{u}}_i = (\hat{u}_{i1}, \hat{u}_{i2})$, then provide coordinates for sites in the ordination plot and then provides a graphical representation of which sites are similar in terms of their species composition.

Ordination plot

- · ordiplot() produces ordination plots based on fitted GLLVMs.
- · Uncertainty of the ordination points in model based ordination can be assessed with prediction errors of latent variables.

```
ordiplot(fithb, predict.region = TRUE, ylim=c(-2.5, 2.5), xlim=c(-2,3))
```

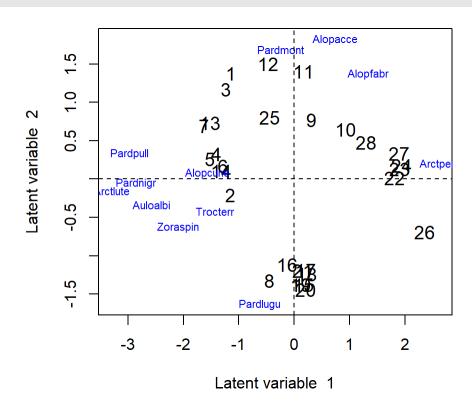


Biplot

- Between species correlations can be visualized with biplot by adding latent variable loadings θ_j to the ordination of sites, by producing a biplot, (argument biplot = TRUE in ordiplot()).
- In a biplot latent variables and their loadings are rotated so that the LV loadings of the species are in the same direction with the sites where they are most abundant.
- The biplots can be used for finding groups of correlated species or finding indicator species common at specific sites.

Biplot

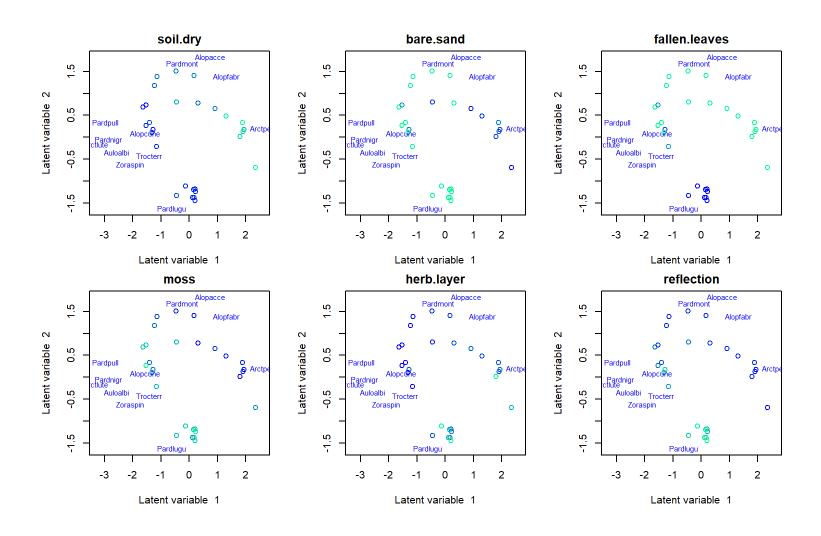
```
ordiplot(fitnb, biplot = TRUE) abline(h = 0, v = 0, lty=2)
```



Environmental gradients

The potential impact of environmental variables on species communities can be viewed by coloring ordination points according to the variables.

Environmental gradients



Environmental gradients

 The next step would be to include covariates to the model to study more precisely the effects of environmental variables:

$$g(E(y_{ij})) = eta_{0j} + oldsymbol{x}_i'oldsymbol{eta}_j + oldsymbol{u}_i'oldsymbol{ heta}_j$$

This topic will be considered closer tomorrow.

More

More information and examples about the usage of the package can be found from the **gllvm** package's website: https://jenniniku.github.io/gllvm/