Analysing multivariate ecological data with Generalized Linear Latent Variable Models

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Exercise material and package installation

https://github.com/BertvanderVeen/IRSAE2021GLLVMworkshop

Questions

In chat or "raise" your hand

On twitter: #**GLLVMs**, @**vdVeenB** or @**J__Niku** or @**samperrinNTNU**
On github: https://github.com/BertvanderVeen/IRSAE2021GLLVMworkshop/discussions

Installation

Ask in chat if you have issues

Welcome! 😄

Who	Affiliation	Expertise
Bert van der Veen PhD candidate	Norwegian institute of Bioeconomy research & Norwegian university of Science and Technology	- Statistical ecology - Ordination - Species distribution modeling

Jenni Niku Postdoc	University of Jyväskylä	- Statistical ecology - Species distribution modeling

Sam Perrin PhD	Norwegian university of Science and Technology Ducky AS	- Fresh water ecology - Invasion ecology - Species distribution modeling

Program

Topic

- Basics of Multivariate analysis
- Latent variables
- Generalized Linear Latent Variable models

Who

Questions / Break

- `gllvm` R-package (Niku et al. 2019)
- How to: model-based ordination with GLLVMs

Questions / Break

- Some ecology with species associations

Finish

- Model-based quadratic ordination
- Model-based constrained ordination
- Wrap-up

What are these GLLVMs?

Generalized Linear Latent Variable Models

- Model-based multivariate analysis
- Mixed-effects model
- Joint Species Distribution Model Ovaskainen et al. 2017
- Unconstrained ordination Hui et al. 2015
- Constrained ordination
- "Factor analytic approach"

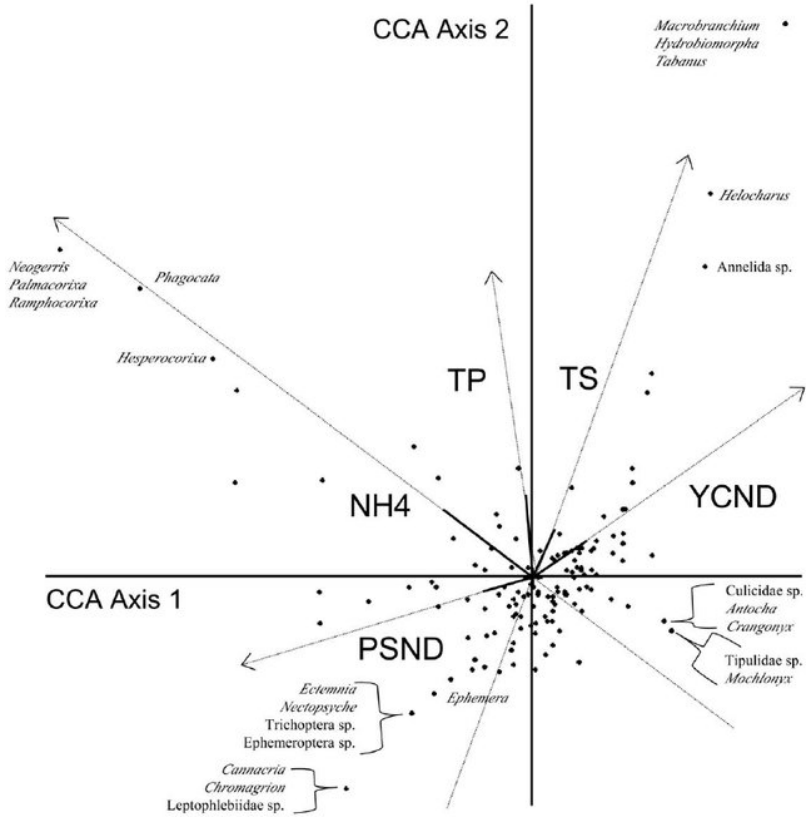
But in general, for the analysis of species (co-)occurrence patterns.

- **GLLVMs are flexible**

Classical multivariate analysis

E.g., PCA, CA, DCA, NMDS

With **eigenvectors** and using **distance metrics**



Maul et al. 2004

Classical multivariate analysis

Here we go model-based!

Plant Ecol (2015) 216:669–682
DOI 10.1007/s11258-014-0366-3

CrossMark

Model-based thinking for community ecology

David I. Warton · Scott D. Foster ·
Glenn De'ath · Jakub Stoklosa · Piers K. Dunstan

Received: 29 January 2014 / Accepted: 30 May 2014 / Published online: 19 November 2014

Gathering data

We go out, register species at multiple sites

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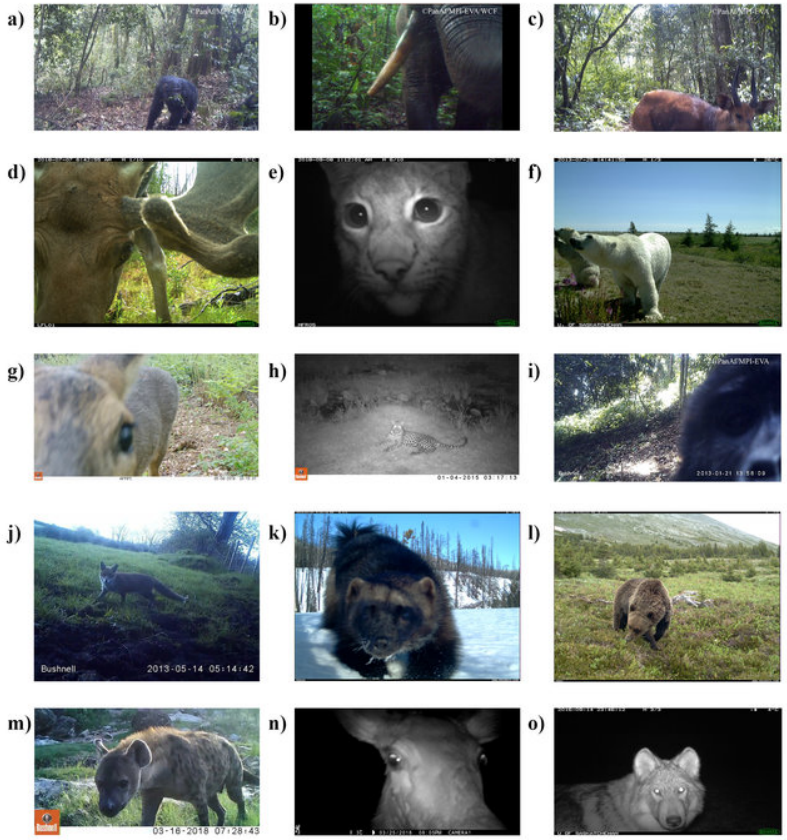
"Multivariate"

- What does multivariate mean?
- Multivariate: multiple **responses**
- E.g. counts of species at sites

	Species 1	Species 2	Species 3	Species 4	Species 5
Site 1	25	10	0	0	0
Site 2	0	2	0	0	0
Site 3	15	20	2	2	0
Site 4	2	6	0	1	0
Site 5	1	20	0	2	0

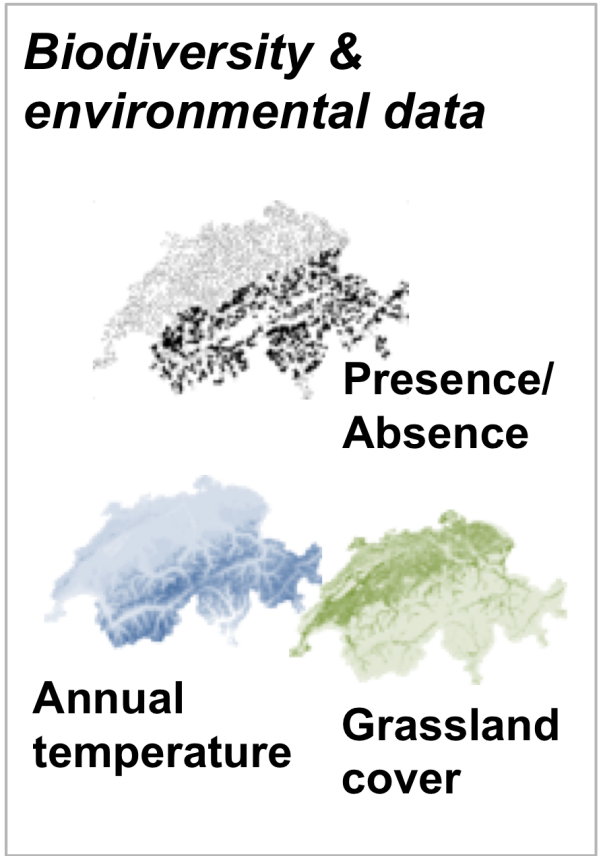
e.g., camera trap data



Caravaggi et al. 2020

"Multivariable"

Multiple **predictors** that represent the environment



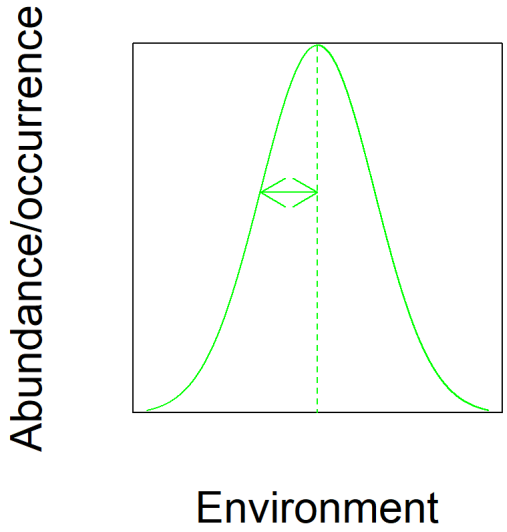
https://damariszurell.github.io/SDM-Intro/

To summarise

- Both data and method can be univariate or multivariate
- Multivariate data can be analysed with both multivariate and univariate methods (SDM, CA)
- Multivariable data can be used in multivariate or univariate analysis
    - Generally the same for all responses
    - (But, note that the model can of course set terms to zero)

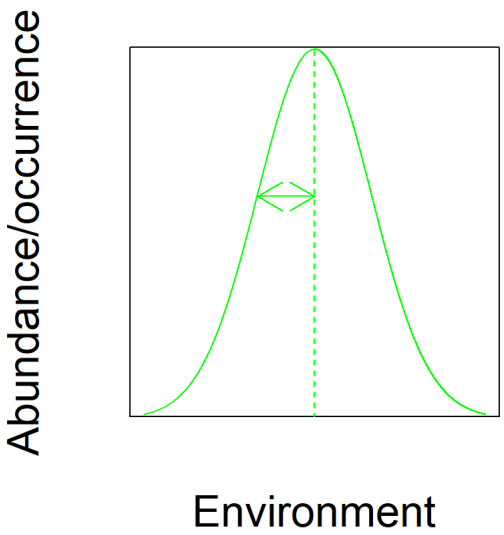
Why analyse multivariate data?

- Interest in **co**-occurrence patterns
  - In contrast to only **occurrence** patterns (a species distribution)
- Why do species co-occur?
  - Similar environmental preferences
  - Similar history in the environment
  - Might result in **Interactions**
- Multiple species form a **community**

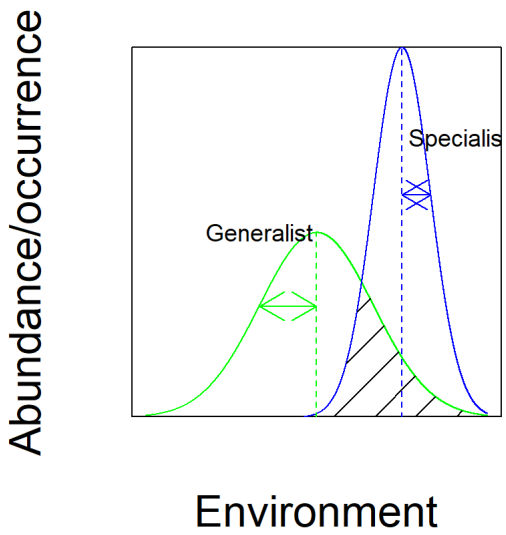


Why analyse multivariate data?

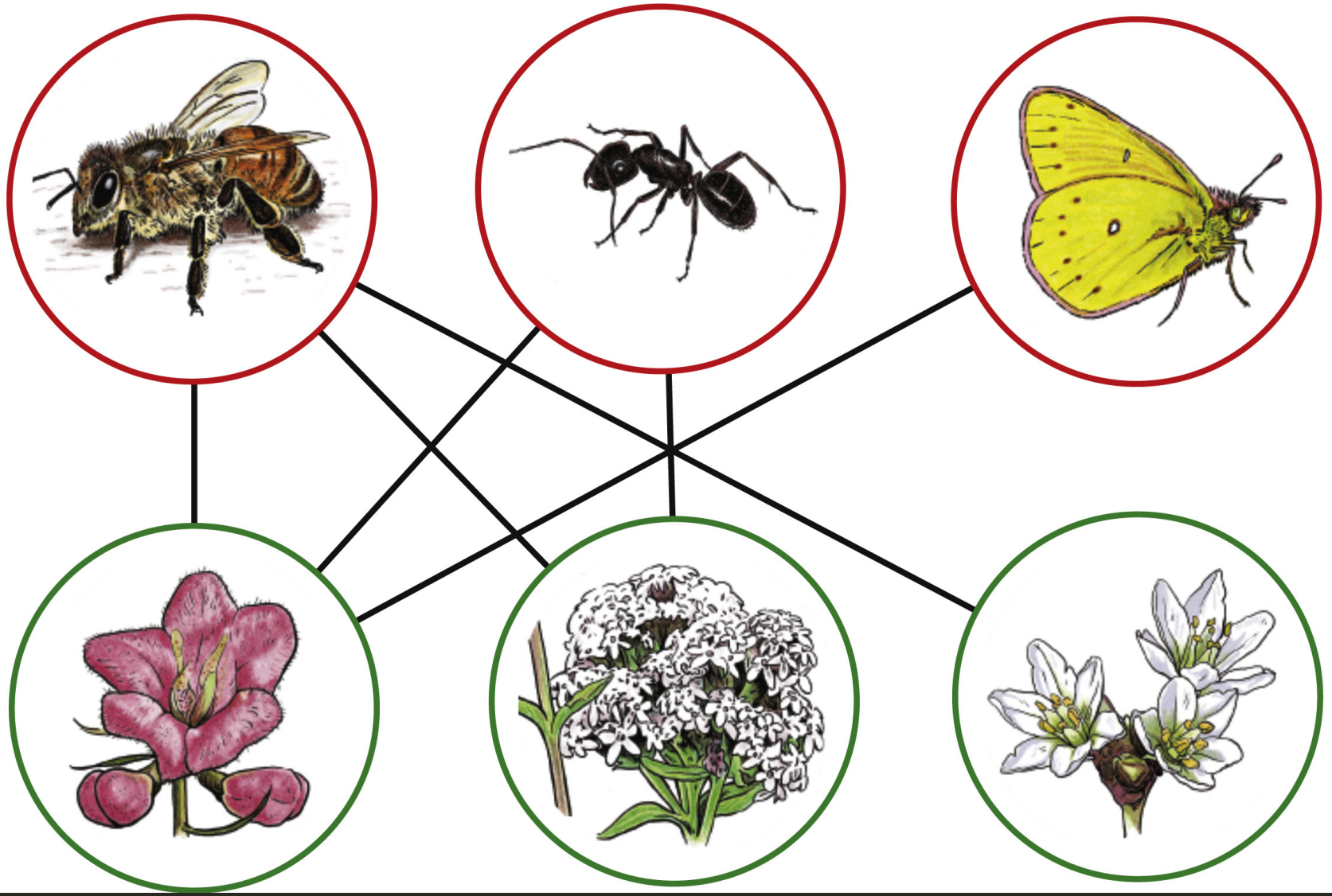
Occurrence pattern



Co-occurrence pattern



But then for more species



Examples

- - - -

Joint modeling with latent variables

- Accounts for correlation between taxa
- "Borrows" information from other species for estimation

- Provides species associations

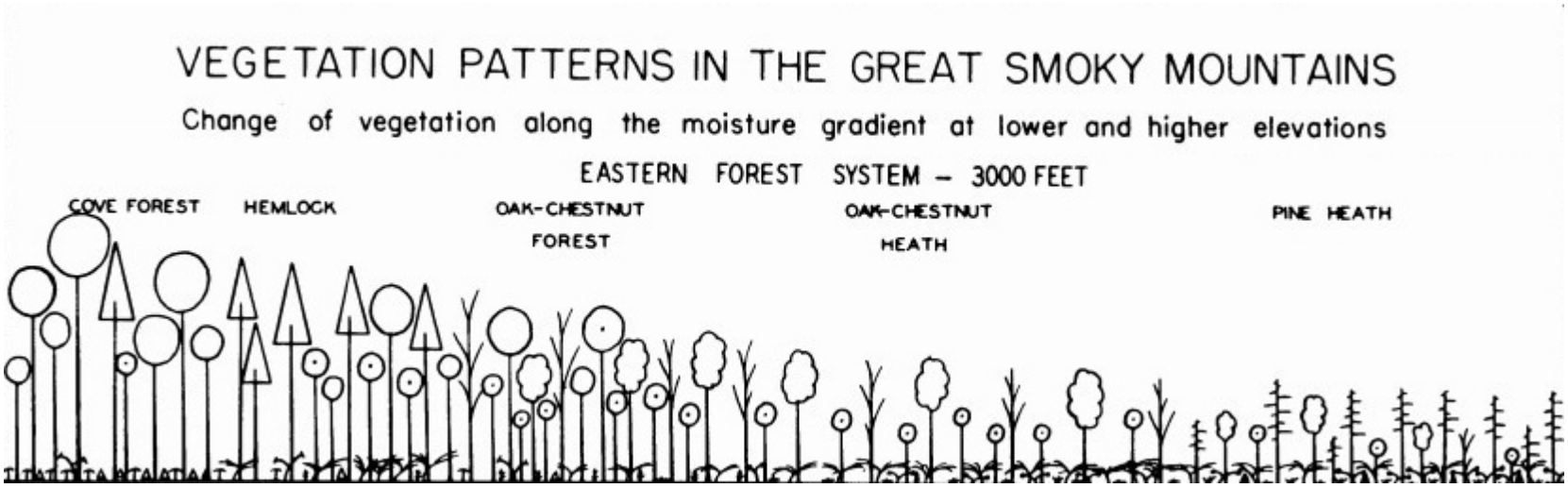
- Concept: fit a single model for all species

- I.e., a "Joint Species Distribution Model"
  - Faster
  - Less tedious
  - Explicitly model species co-occurrence
  - Etc.

Key references

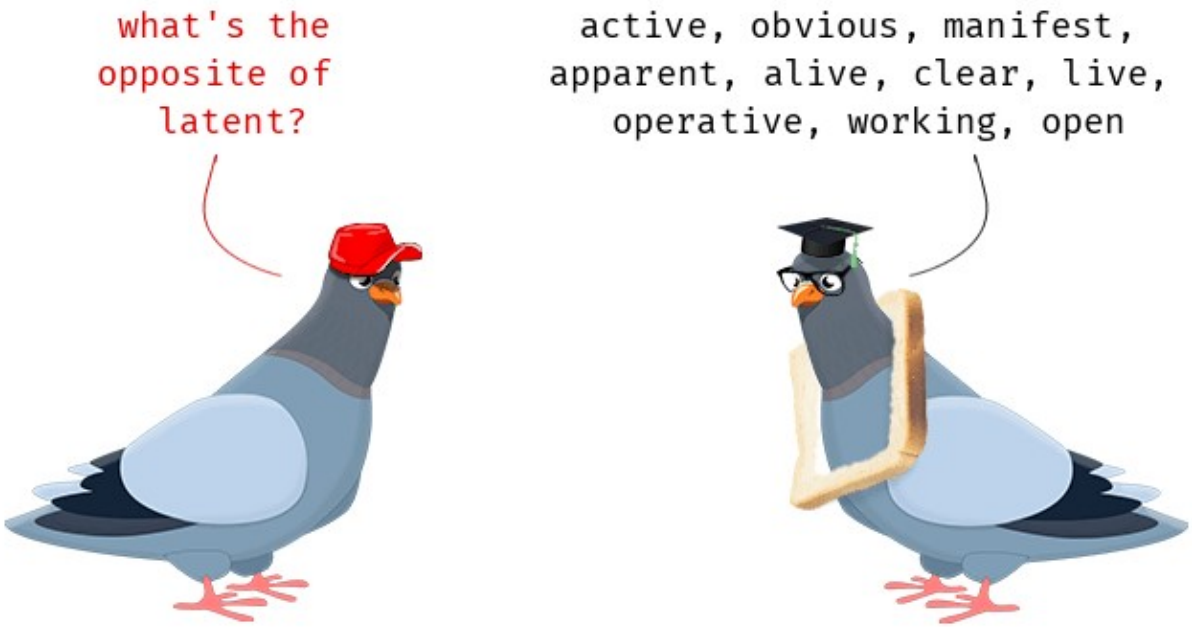
- Warton et al. 2015: "So many variabes: Joint modeling in community ecology"
- Blanchet et al. 2020: "Co-occurrence is not evidence of ecological interactions"
- Poggiato et al. 2021: "On the interpretations of joint modeling in community ecology"

Latent variables?



Whittaker 1967

Variables can be **observed** or **latent**



If not measured, it is latent, like a random-effect.

Ecological gradient analysis

"Gradient analysis is a research approach for the study of spatial patterns of species." Whittaker 1967

Our sites describe the environment. Multiple environmental gradients can form a **complex** gradient.

	Predictor 1	Predictor 2	Predictor 3	Predictor 4	Predictor 5
Site 1	**2.3321**	**3.0445**	0.0000	3.0445	4.4543
Site 2	**3.0493**	**3.2581**	1.7918	1.0986	4.5643
Site 3	**2.5572**	**3.5835**	0.0000	2.3979	4.6052
Site 4	**2.6741**	**4.5109**	0.0000	2.3979	4.6151
Site 5	**3.0155**	**2.3979**	0.0000	0.0000	4.6151

Ecological gradients

1) Ecological gradient: gradual change in the environment

- e.g. temperature

2) Complex gradient: change in several ecological gradients

- e.g., soil moisture and acidity on an elevation gradient
- e.g., a gradual urban to rural change in the landscape
- Can be represented as a single factor, covariate, predictor, latent variable, ordination axis

So a latent variable is an ecological gradient or ordination axis representing one, or multiple, missing predictors.

Latent variables

"Few major complex ecological gradients normally account for most of the variation in species composition." Halvorsen 2012

In essence:

Community structure is generally low-dimensional.

At this point you might think:

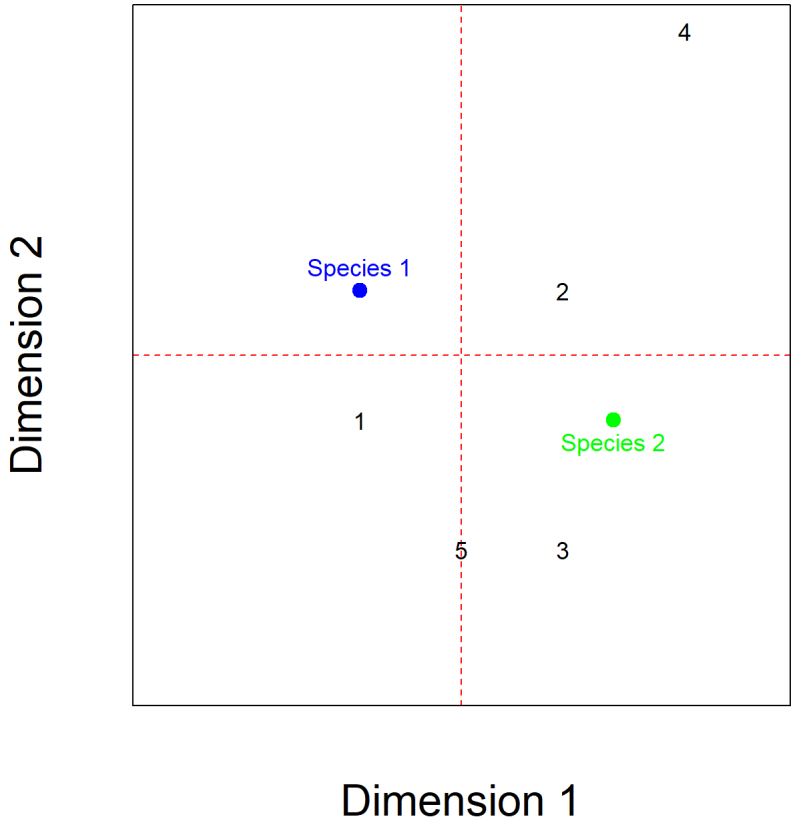
- Community ecology has been doing it for a hundred years!
- e.g. Forbes (1907)
- Ordination:
  - Principal Component Analysis Pearson 1901
  - Correspondence analysis Hirschfeld 1934
  - NMDS Kruskal 1964a,b
- Niche overlap

Analysing multivariate data: ordination

- Termed by David Goodall in 1954: "An essay in the use of factor analysis"
- Applied factor analysis For the analysis of data on a plant community
- Reducing dimension of data
- ordering species or samples along an ecological gradient
- classically e.g.,
    - Principal Component Analysis (PCA; `prcomp()`)
    - Correspondence Analysis (CA; `cca()` in **vegan**)
    - Multidimensional scaling (PCoA; `cmdscale()`, NMDS; `metaMDS()` in **vegan**)
    - **Factor analysis**: Precursor to GLLVMs (FA; `factanal()`)
- *Treats latent variables as fixed-effects*
- So a multivariate Generalized Linear Model (kind of), i.e., a joint model

Ordination: visual inspection

- Most common tool is the biplot Gabriel 1971
- Distance between species indicates dissimilarity
- Distance between sites indicates dissimilarity



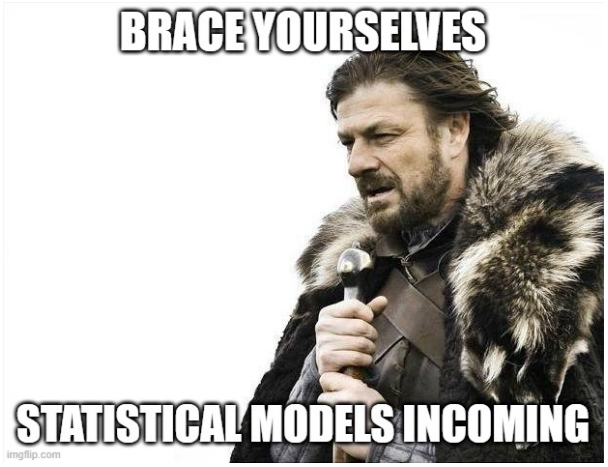
Classical methods have some issues..

- Ordination axis (ecological gradient) treated as fixed (parameter)
- Horseshoe or arch effect (PCA, CA)
- Difficult (near to impossible) to check any assumptions
- Mean-variance relationships Warton and Hui 2017

In general, not very flexible.

Model-based thinking

- Concept: apply regression concepts to multivariate analysis Warton et al. 2015
  - Explicit statistical models
  - Residual diagnostics
  - Model selection
  - et cetera



Specifying a multivariate statistical model

- β_{0j} intercept per species
- $\boldsymbol{x}_{ik}$ site-specific predictors
- $\boldsymbol{\beta_j}$ species-specific slopes

$$g(E(\boldsymbol{y}_{ij}|\boldsymbol{x}_i)) = \beta_{0j} + \boldsymbol{x}_i^\top \boldsymbol{\beta}_j \quad (1)$$

- Stacked SDM (fit with `glm(.)` function)
- No random-effects

A Multivariate Mixed-effects model

- Add residual for $i = 1 \dots n$ sites and $j = 1 \dots p$ species

$$g(\mathrm{E}(y_{ij}|\boldsymbol{x}_i)) = \beta_{0j} + \boldsymbol{x}_i^\top \boldsymbol{\beta}_j + u_{ij}, \qquad \boldsymbol{u}_i \sim \mathcal{N}(0, \Sigma) \tag{2}$$

- Structure $\boldsymbol{u}_{ij}$ with Σ by species
- Σ are species covariances or *associations*
- A "joint species distribution model" Pollock et al. 2014
- Can be fit using standard mixed-effects modeling software.

In `lme4`:

```
glmer(abundance~species+x:species+
(0+species|sites),family="poisson",data=data)
```

- Too many parameters in Σ
- Number of parameters increases rapidly
- Often not feasible to fit

Model-based ordination to the rescue!

- Ordination = dimension reduction
- Represent the latent complex ecological gradient
- A model like in regression
- Represent species associations with latent variables
- So JSDM = ordination? Yes! (for GLLVMs)

- "Model-based approaches to unconstrained ordination" Hui et al. 2015

All the benefits from regression and ordination!, e.g.:

- Procrustus analysis
- Biplots
- Model-selection
- Residual diagnostics
- Appropriate mean-variance relationships
- Hypothesis testing
- No distance metrics

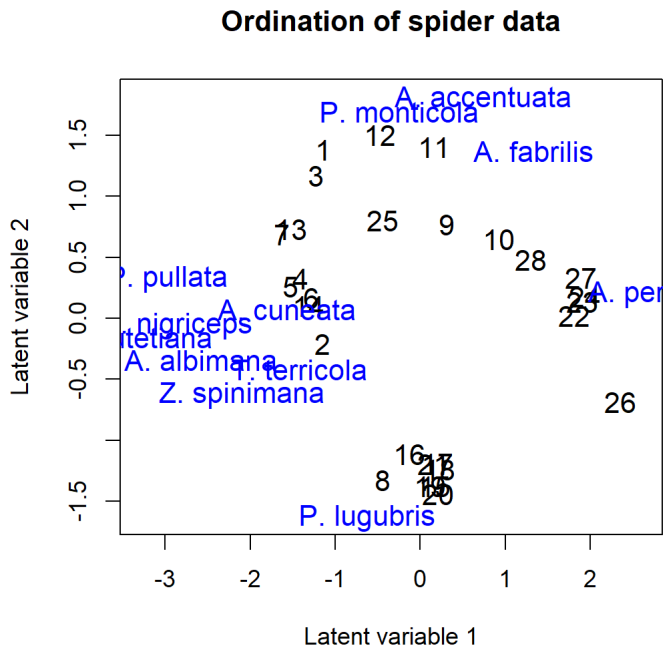
Generalized Linear Latent Variable Models

- GLLVM for short
- Add factor analytic structure to Σ
- Ordination = dimension reduction
- $u_{ij} = \boldsymbol{\epsilon}_i^\top \boldsymbol{\theta}_j$
  - i.e. $\boldsymbol{\epsilon}_i \sim \mathcal{N}(0, \boldsymbol{\theta}_j \boldsymbol{\theta}_j^\top)$
- Faster and fewer parameters:
  - Number of parameter doesn't grow so fast
  - More latent variables, better estimation of Σ
- So we are estimating residual covariances!

$$\Sigma = \begin{bmatrix} \theta_{11} & 0 & 0 \\ \theta_{12} & \theta_{22} & 0 \\ \vdots & \ddots & \vdots \\ \theta_{1j} & \cdots & \theta_{dj} \end{bmatrix} \begin{bmatrix} \theta_{11} & \theta_{12} & \cdots & \theta_{1j} \\ 0 & \theta_{22} & \ddots & \vdots \\ 0 & 0 & \cdots & \theta_{dj} \end{bmatrix} \tag{3}$$

Generalized Linear Latent Variable Models

- Still a mixed-effects model
- d latent variables treated as random-effect
- Produces ordination
  - "site scores" : $\boldsymbol{\epsilon}_i$
  - "species scores" or "loadings": $\boldsymbol{\theta}_j$
- Species and sites far apart are dissimilar
- E.g., because species prefer different environments



$$g(\mathrm{E}(y_{ij}|\boldsymbol{x}_i, \boldsymbol{\epsilon}_i)) = \beta_{0j} + \boldsymbol{x}_i^\top \boldsymbol{\beta}_j + \boldsymbol{\epsilon}_i^\top \boldsymbol{\theta}_j, \qquad \boldsymbol{\epsilon}_i \sim \mathcal{N}(0, \boldsymbol{I}) \tag{4}$$

gllvm R-package

Methods in Ecology and Evolution | BRITISH ECOLOGICAL SOCIETY

APPLICATION | Free Access

gllvm: Fast analysis of multivariate abundance data with generalized linear latent variable models in R

Jenni Niku ✉, Francis K. C. Hui, Sara Taskinen, David I. Warton

First published: 21 September 2019 | https://doi.org/10.1111/2041-210X.13303 | Citations: 4

Break / Questions

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Or in the chat.