

# Analysing multivariate ecological data with Generalized Linear Latent Variable Models

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# Exercise material and package installation

<https://github.com/BertvanderVeen/IRSAE2021GLLVMworkshop>

## Questions

In zoom chat or "raise" your hand

 On twitter: **#GLLVMs**, **@vdVeenB** or **@J\_\_Niku** or **@samperrinNTNU**

 On github: <https://github.com/BertvanderVeen/IRSAE2021GLLVMworkshop/discussions>

# Welcome! 😊



## Who

Bert van der Veen  
PhD candidate

## Affiliation

Norwegian insitute of  
Bioeconomy research &  
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Science and Technology

## Expertise

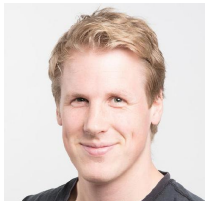
- Statistical ecology
- Ordination
- Species distribution modeling



Jenni Niku  
Postdoc

University of Jyväskylä

- Statistical ecology
- Species distribution modeling



Sam Perrin  
PhD

Norwegian university of  
Science and Technology

- Fresh water ecology
- Invasion ecology
- Species distribution modeling

# Program

## Topic

- Basics of Multivariate analysis
- Latent variables
- Generalized Linear Latent Variable models

## Who



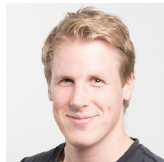
## Questions / Break

- **gllvm** R-package (Niku et al. 2019)
- How to: model-based ordination with GLLVMs



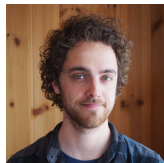
## Questions / Break

- Some ecology with species associations



## Finish

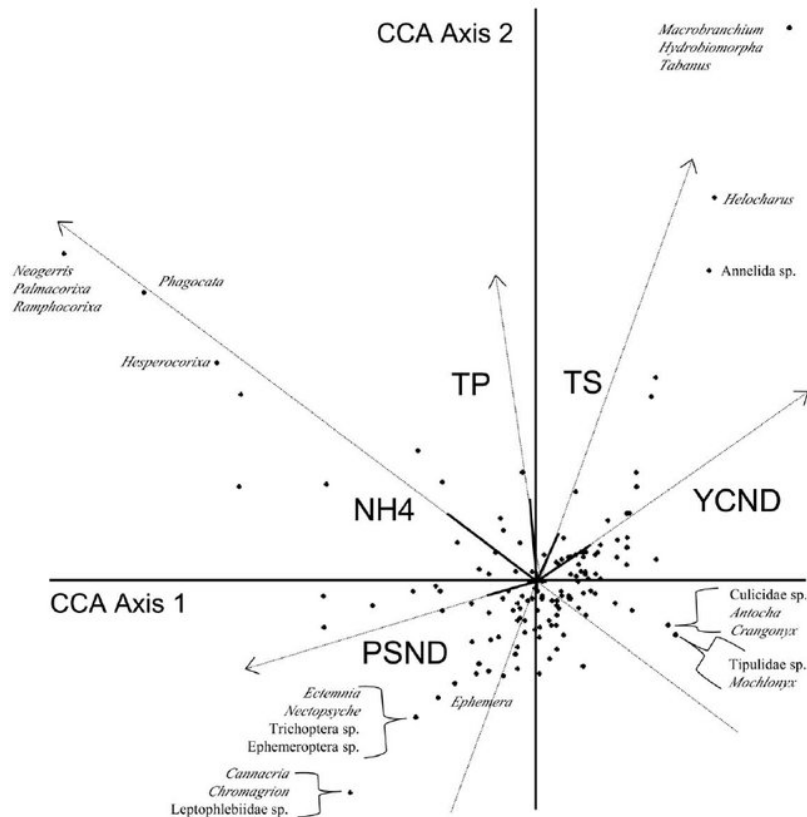
- Model-based quadratic ordination
- Model-based constrained ordination
- Wrap-up



# Classical multivariate analysis

E.g., PCA, CA, DCA, NMDS

With **eigenvectors** and using **distance metrics**



Maul et al. 2004

# Classical multivariate analysis

Here we go model-based!

Plant Ecol (2015) 216:669–682  
DOI 10.1007/s11258-014-0366-3



## **Model-based thinking for community ecology**

**David I. Warton · Scott D. Foster ·  
Glenn De'ath · Jakub Stoklosa · Piers K. Dunstan**

Received: 29 January 2014 / Accepted: 30 May 2014 / Published online: 19 November 2014  
© Springer Science+Business Media Dordrecht 2014

# Gathering data

We go out, register species at multiple sites



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e.g., camera trap data



Caravaggi et al. 2020



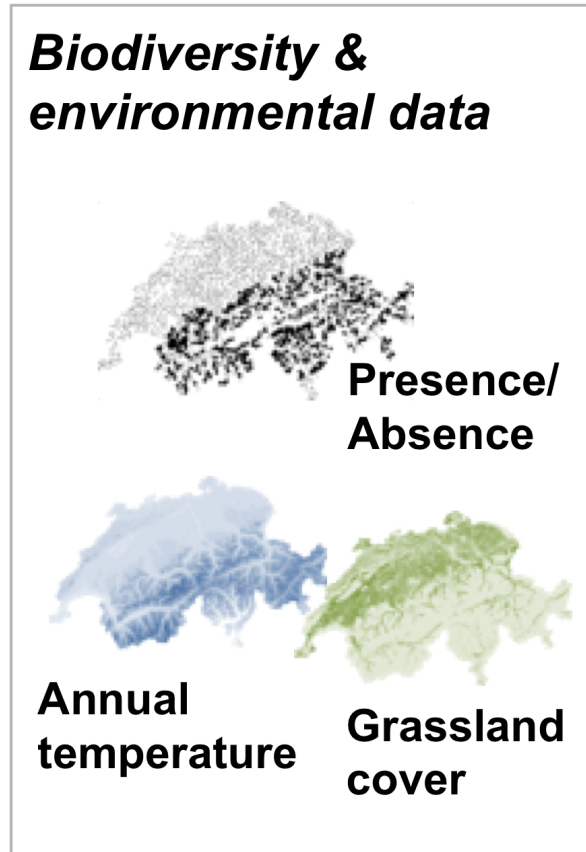
# "Multivariate"

- What does multivariate mean?
- Multivariate: multiple **responses**
- E.g. counts of species at sites

	Species 1	Species 2	Species 3	Species 4	Species 5
Site 1	25	10	0	0	0
Site 2	0	2	0	0	0
Site 3	15	20	2	2	0
Site 4	2	6	0	1	0
Site 5	1	20	0	2	0

# "Multivariable"

Multiple **predictors** that represent the environment



<https://damarisurell.github.io/SDM-Intro/>

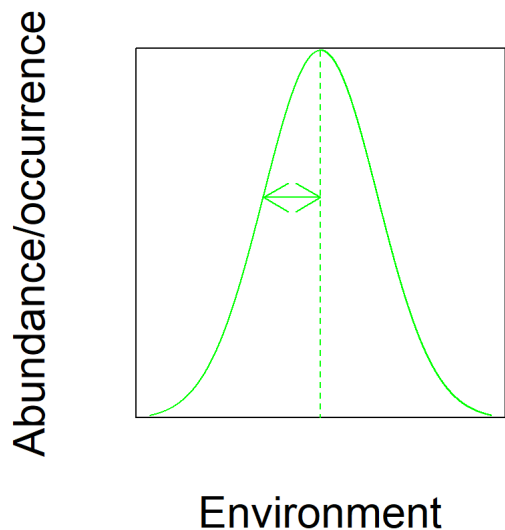
# To clarify

- Both data and method can be univariate or multivariate
- Multivariate data can be analysed with both multivariate and univariate methods (SDM, CA)
- Multivariable data can be used in multivariate or univariate analysis
  - Generally the same for all responses
  - (But, note that the model can of course set terms to zero)

# Why analyse multivariate data?

- Interest in **co**-occurrence patterns
  - In contrast to only **occurrence** patterns (a species distribution)
- Why do species co-occur?
  - Similar environmental preferences
  - Similar history in the environment
  - Might result in **Interactions**
- Multiple species form a **community**

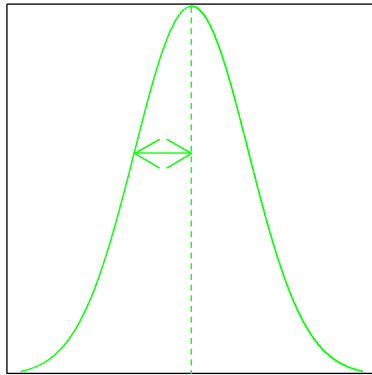
Occurrence pattern



# Why analyse multivariate data?

Occurrence pattern

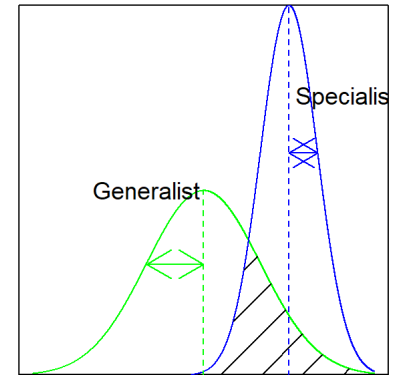
Abundance/occurrence



Environment

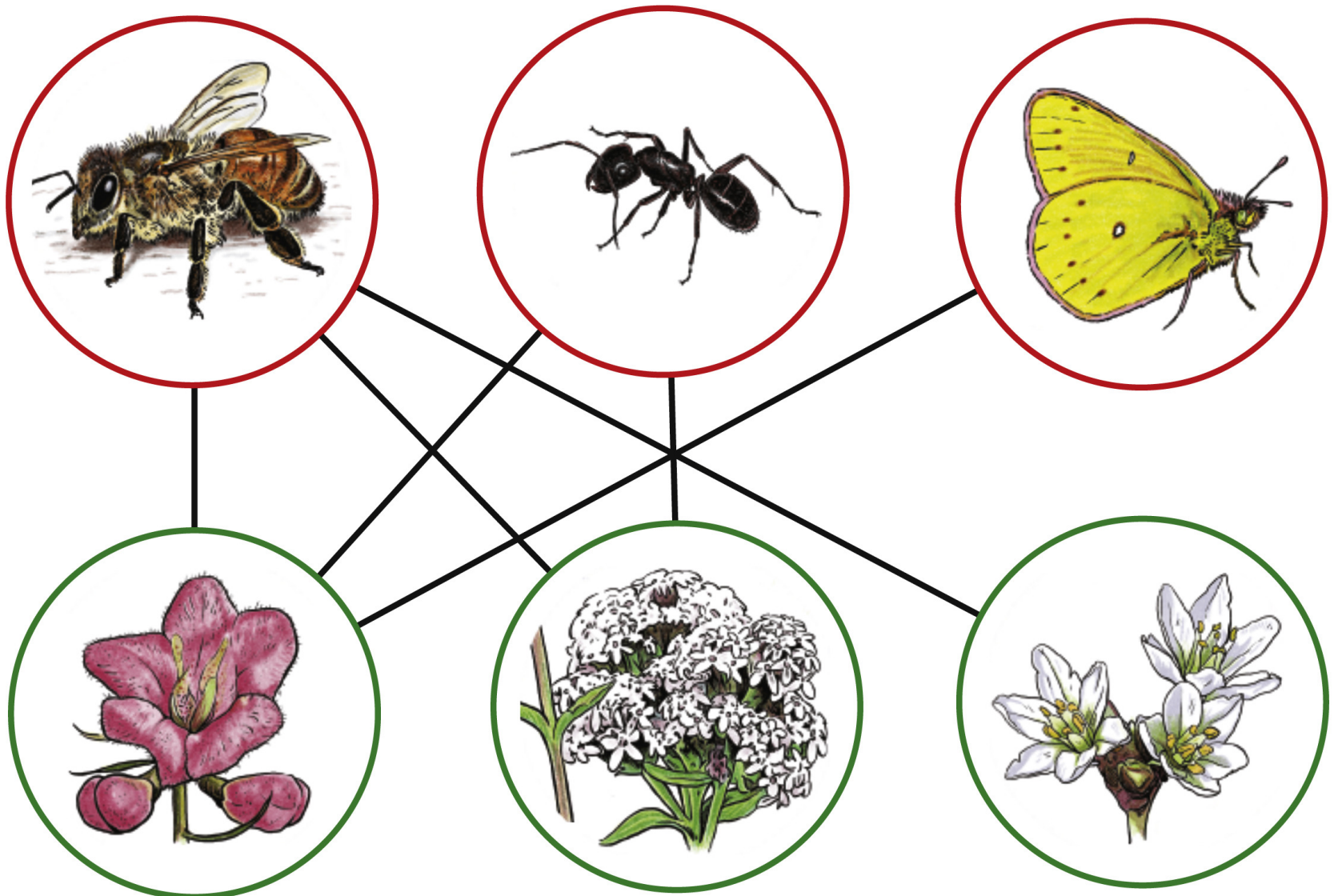
Co-occurrence pattern

Abundance/occurrence



Environment

# But then for more species



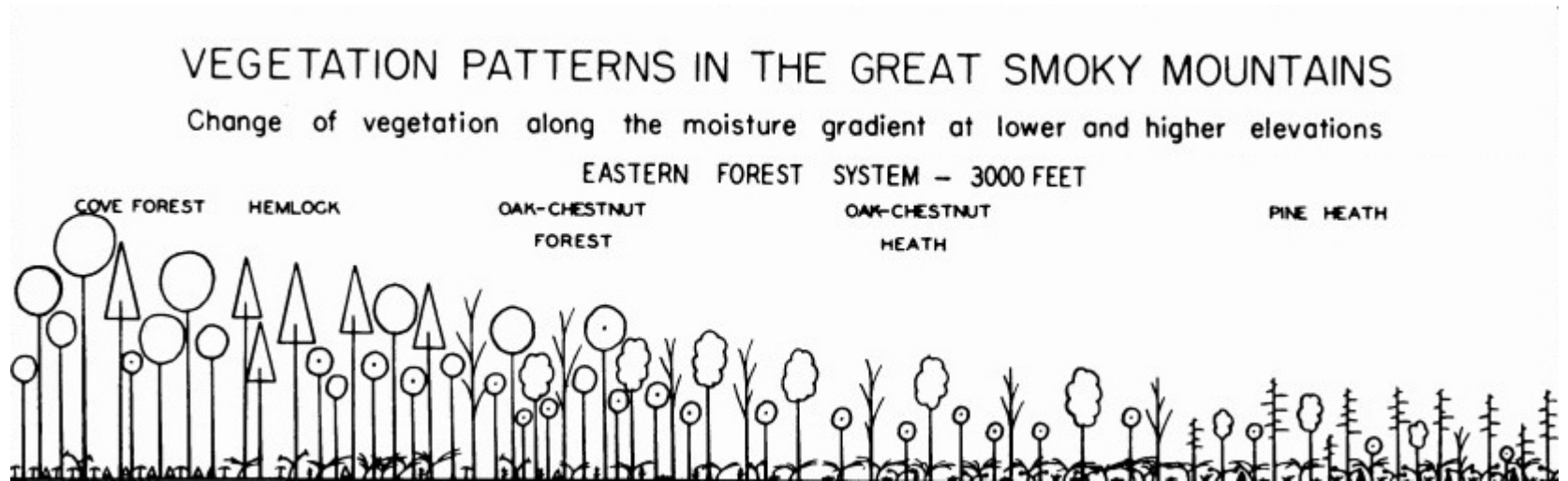
# Joint modeling with latent variables

- Accounts for correlation between taxa
- "Borrows" information from other species for estimation
- Provides species associations
- Concept: fit a single model for all species
- I.e., a "Joint Species Distribution Model"
  - Faster
  - Less tedious
  - Explicitly model species co-occurrence
  - Etc.

## Key references

- Warton et al. 2015: "So many variables: Joint modeling in community ecology"
- Poggiato et al. 2021: "On the interpretations of joint modeling in community ecology"
- Blanchet et al. (2020): "Co-occurrence is not evidence of ecological interactions"

# Latent variables?



Whittaker 1967



Variables can be **observed** or **latent**

what's the  
opposite of  
latent?



active, obvious, manifest,  
apparent, alive, clear, live,  
operative, working, open



*If not measured, it is latent, like a fixed versus a random-effect.*

# Ecological gradient analysis

"Gradient analysis is a research approach for the study of spatial patterns of species." Whittaker 1967

Our sites describe the environment. Multiple environmental gradients can form a **complex** gradient.

	Predictor 1	Predictor 2	Predictor 3	Predictor 4	Predictor 5
Site 1	2.3321	3.0445	0.0000	3.0445	4.4543
Site 2	3.0493	3.2581	1.7918	1.0986	4.5643
Site 3	2.5572	3.5835	0.0000	2.3979	4.6052
Site 4	2.6741	4.5109	0.0000	2.3979	4.6151
Site 5	3.0155	2.3979	0.0000	0.0000	4.6151

# Ecological gradients

1) Ecological gradient: gradual change in the environment

- e.g. temperature

2) Complex gradient: change in several ecological gradients

- e.g., soil moisture and acidity on an elevation gradient
- e.g., a gradual urban to rural change in the landscape
- Can be represented as a single factor, covariate, predictor, latent variable, ordination axis

*So a latent variable is an ecological gradient or ordination axis representing one, or multiple, missing predictors.*

# Latent variables

"Few major complex ecological gradients normally account for most of the variation in species composition." Halvorsen 2012

## In essence:

Community structure is generally low-dimensional.

# Analysing co-occurrence patterns

## At this point you might think:

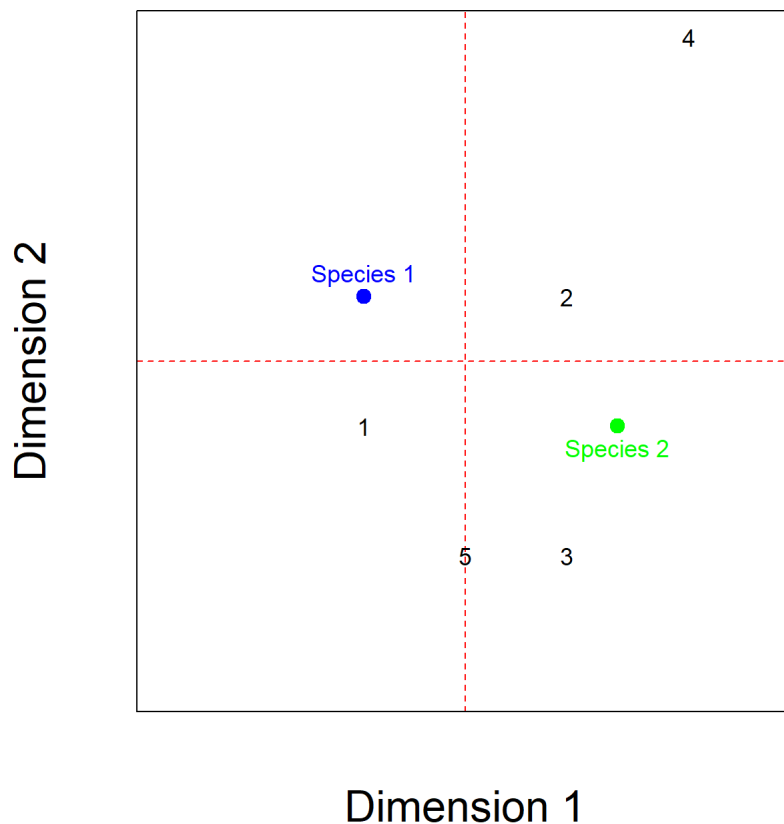
- Community ecology has been doing it for a hundred years!
- e.g. Forbes (1907)
- Ordination: Principal Component Analysis Pearson 1901, Correspondence analysis Hirschfeld 1934, NMDS (Kruskal 1964a,b)
- Niche overlap

# Analysing multivariate data: ordination

- Termed by David Goodall in 1954: "An essay in the use of factor analysis"
- Applied factor analysis For the analysis of data on a plant community
- Reducing dimension of data
- ordering species or samples along an ecological gradient
- classically e.g.,
  - Principal Component Analysis (PCA; `prcomp()`)
  - Correspondence Analysis (CA; `cca()` in **vegan**)
  - Multidimensional scaling (PCoA; `cmdscale()`, NMDS; `metaMDS()` in **vegan**)
  - **Factor analysis**: Precursor to GLLVMs (FA; `factanal()`)
- *Treats latent variables as fixed-effects*
- So a multivariate Generalized Linear Model (kind of), i.e., a joint model

# Ordination: visual inspection

- Most common tool is the biplot Gabriel 1971
- Distance between species indicates dissimilarity
- Distance between sites indicates dissimilarity



# Classical methods have some issues..

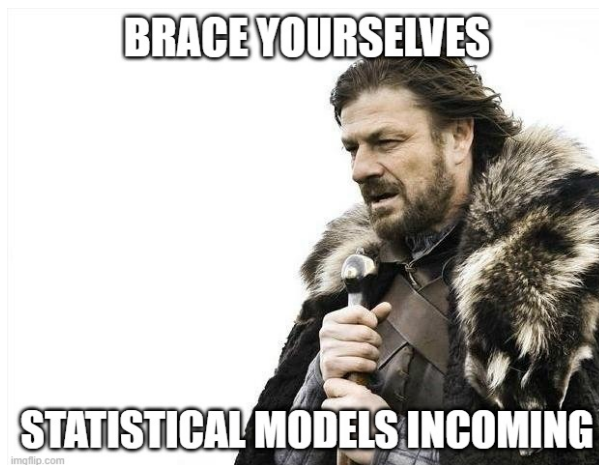
- Ordination axis (ecological gradient) treated as fixed (parameter)
- Horseshoe or arch effect (PCA, CA)
- Difficult (near to impossible) to check any assumptions
- Mean-variance relationships Warton and Hui 2017

**In general, not very flexible.**



# Model-based thinking

- Concept: apply regression concepts to multivariate analysis Warton et al. 2015
  - Explicit statistical models
  - Residual diagnostics
  - Model selection
  - et cetera



# Specifying a multivariate statistical model

- $\beta_{0j}$  intercept per species
- $x_{ik}$  site-specific predictors
- $\beta_j$  species-specific slopes

$$g(E(y_{ij}|\mathbf{x}_i)) = \beta_{0j} + \mathbf{x}_i^\top \beta_j \quad (2)$$

- Stacked SDM or `glm(.)` function
- Without random-effects

# A Multivariate Mixed-effects model

- Add residual for  $i = 1 \dots n$  sites and  $j = 1 \dots p$  species
- Structure  $\Sigma$  by species
- $\Sigma$  are species covariances or *associations*
- A "joint species distribution model" Pollock et al. 2014

$$g(\mathbb{E}(y_{ij}|\mathbf{x}_i)) = \beta_{0j} + \mathbf{x}_i^\top \boldsymbol{\beta}_j + \epsilon_{ij}, \quad \boldsymbol{\epsilon}_i \sim \mathcal{N}(0, \Sigma) \quad (3)$$

- Can be fit using standard mixed-effects modeling software.

In `lme4`:

```
glmer(abundance~species+x:species+  
(0+species|sites),family="poisson",data=data)
```

- $\Sigma$  has  $p(p + 1)/2$  parameters (which increases quadratically with # species)

# Model-based ordination to the rescue!

- Ordination = dimension reduction
- Represent the latent complex ecological gradient
- A model like in regression
- Represent species associations with latent variables
- So JSMD = ordination? Yes! (for GLLVMs)
- "Model-based approaches to unconstrained ordination" Hui et al. 2015

## **All the benefits from regression and ordination!, e.g.:**

- Procrustes analysis
- Biplots
- Model-selection
- Residual diagnostics
- Appropriate mean-variance relationships
- Hypothesis testing
- No distance metrics



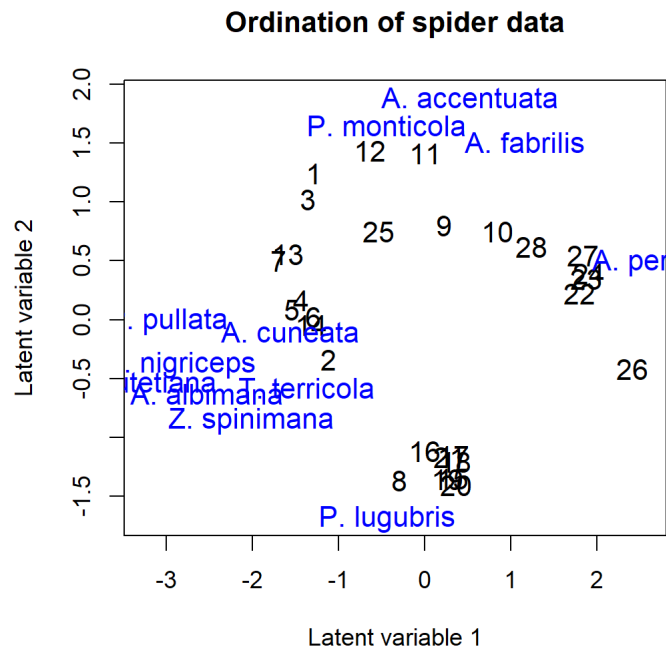
# Generalized Linear Latent Variable Models

- GLLVM for short
- Add factor analytic structure to  $\Sigma$
- Ordination = dimension reduction
- $\epsilon_{ij} = \mathbf{u}_i^\top \boldsymbol{\theta}_j$ 
  - i.e.  $\boldsymbol{\epsilon}_i \sim \mathcal{N}(0, \boldsymbol{\theta}_j \boldsymbol{\theta}_j^\top)$
- Faster and fewer parameters:
  - Number of parameter doesn't grow so fast
  - More latent variables, better estimation of  $\Sigma$

$$\Sigma = \begin{bmatrix} \theta_{11} & 0 & 0 \\ \theta_{12} & \theta_{22} & 0 \\ \vdots & \ddots & \vdots \\ \theta_{1j} & \cdots & \theta_{dj} \end{bmatrix} \begin{bmatrix} \theta_{11} & \theta_{12} & \cdots & \theta_{1j} \\ 0 & \theta_{22} & \ddots & \vdots \\ 0 & 0 & \cdots & \theta_{dj} \end{bmatrix} \quad (4)$$

# Generalized Linear Latent Variable Models

- Still a mixed-effects model
- $d$  latent variables treated as random-effect
- Produces ordination
  - "site scores" :  $\mathbf{u}_i$
  - "species scores" or "loadings":  $\boldsymbol{\theta}_j$
- Species and sites far apart are dissimilar
- E.g., because species prefer different environments



$$g(\mathbb{E}(y_{ij}|\mathbf{x}_i, \mathbf{u}_i)) = \beta_{0j} + \mathbf{x}_i^\top \boldsymbol{\beta}_j + \mathbf{u}_i^\top \boldsymbol{\theta}_j, \quad \mathbf{u}_i \sim \mathcal{N}(\mathbf{0}, \mathbf{I}) \quad (5)$$

# Compared to (unconstrained) classical ordination

So GLLVMs can be used as, e.g.,

- Joint species distribution model (with reduced-rank residual covariance matrix),
- Multivariate GLM (no random-effects),
- Unconstrained Ordination
- Constrained ordination (see last part)

*But in general, for the analysis of species (co-)occurrence patterns.*

- **GLLVMs are flexible**
- **Because the statistical model can be extended**



# gllvm R-package

## Methods in Ecology and Evolution



APPLICATION |  Free Access |

**gllvm: Fast analysis of multivariate abundance data with generalized linear latent variable models in R**

Jenni Niku , Francis K. C. Hui, Sara Taskinen, David I. Warton

First published: 21 September 2019 | <https://doi.org/10.1111/2041-210X.13303> | Citations: 4



# Break / Questions

 On twitter: #**GLLVMs**, @**vdVeenB** or @**J\_\_Niku** or @**samperrinNTNU**

 On github: <https://github.com/BertvanderVeen/IRSAE2021GLLVMworkshop/discussions>

Or on zoom.