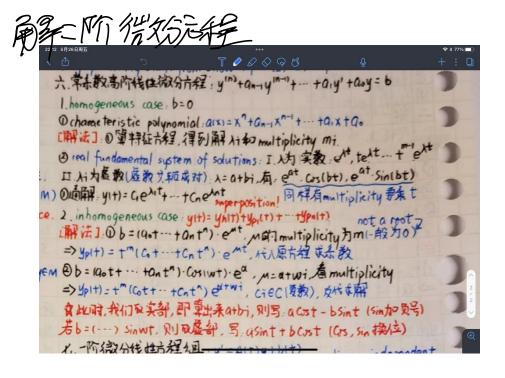
$f(t)$, period $T = \frac{2\pi}{\omega_o}$	Form	Coefficients
$\sum_{n=-\infty}^{\infty} F_n e^{jn\omega_o t}$	Exponential	$F_n = \frac{1}{T} \int_T f(t) e^{-jn\omega_o t} dt$
$\frac{a_o}{2} + \sum_{n=1}^{\infty} a_n \cos(n\omega_o t) + b_n \sin(n\omega_o t)$	Trigonometric	$a_n = F_n + F_{-n}$ $b_n = j (F_n - F_{-n})$
$\frac{c_o}{2} + \sum_{n=1}^{\infty} c_n \cos(n\omega_o t + \theta_n)$	Compact for real $f(t)$	$c_n = 2 F_n $ $\theta_n = \angle F_n$

Table 1: Fourier series forms.

	Name:	Condition:	Property:
1	Scaling	Constant K	$K f(t) \leftrightarrow K F_n$
2	Addition	$f(t) \leftrightarrow F_n, g(t) \leftrightarrow G_n, \dots$	$f(t) + g(t) + \ldots \leftrightarrow F_n + G_n + \ldots$
3	Time shift	Delay t_o	$f(t-t_o) \leftrightarrow F_n e^{-jn\omega_o t_o}$
4	Derivative	Continuous $f(t)$	$\frac{df}{dt} \leftrightarrow jn\omega_o F_n$
5	Hermitian	Real $f(t)$	$F_{-n} = F_n^*$
6	Even function	f(-t) = f(t)	$f(t) = \frac{a_o}{2} + \sum_{n=1}^{\infty} a_n \cos(n\omega_o t)$
7	Odd function	f(-t) = -f(t)	$f(t) = \sum_{n=1}^{\infty} b_n \sin(n\omega_o t)$
8	Average power		$P \equiv \frac{1}{T} \int_{T} f(t) ^{2} dt = \sum_{n=-\infty}^{\infty} F_{n} ^{2}$

Table 2: Fourier series properties



$$Q = \frac{W_0}{B}$$

$$B = W_2 - W_1 = 2\pi t_2 - 2\pi t_1$$

$$W_0 = \frac{1}{J_{LL}} = J_{W_LW_1}$$

$$B = \frac{1}{J_{LL}} = \frac{1}{R_L}$$

$$LIBE \neq LIATZ$$

$$T. H.D. = \frac{2}{L_1^2} \frac{C_1^2}{C_1^2}$$
, $T. H.D. = \frac{P_y - (\frac{C_1^2 + \frac{C_1^2}{2}}{2})}{\frac{1}{2}C_1^2}$

$F(w) = \int_{-\infty}^{\infty} t(t)e^{-jwt}dt$

	Name:	Condition:	Property:
1	Amplitude scaling	$f(t) \leftrightarrow F(\omega)$, constant K	$Kf(t) \leftrightarrow KF(\omega)$
2	Addition	$f(t) \leftrightarrow F(\omega), g(t) \leftrightarrow G(\omega), \cdots$	$f(t) + g(t) + \cdots \leftrightarrow F(\omega) + G(\omega) + \cdots$
3	Hermitian	Real $f(t) \leftrightarrow F(\omega)$	$F(-\omega) = F^*(\omega)$
4	Even	Real and even $f(t)$	Real and even $F(\omega)$
5	Odd	Real and odd $f(t)$	Imaginary and odd $F(\omega)$
6	Symmetry	$f(t) \leftrightarrow F(\omega)$	$F(t) \leftrightarrow 2\pi f(-\omega)$
7	Time scaling	$f(t) \leftrightarrow F(\omega)$, real s	$f(st) \leftrightarrow \frac{1}{ s } F(\frac{\omega}{s})$
8	Time shift	$f(t) \leftrightarrow F(\omega)$	$f(t-t_o) \leftrightarrow F(\omega)e^{-j\omega t_o}$
9	Frequency shift	$f(t) \leftrightarrow F(\omega)$	$f(t)e^{j\omega_o t} \leftrightarrow F(\omega - \omega_o)$
10	Modulation	$f(t) \leftrightarrow F(\omega)$	$f(t)\cos(\omega_o t) \leftrightarrow \frac{1}{2}F(\omega - \omega_o) + \frac{1}{2}F(\omega + \omega_o)$
11	Time derivative	Differentiable $f(t) \leftrightarrow F(\omega)$	$\frac{df}{dt} \leftrightarrow j\omega F(\omega)$
12	Freq derivative	$f(t) \leftrightarrow F(\omega)$	$-jtf(t) \leftrightarrow \frac{d}{d\omega}F(\omega)$
13	Time convolution	$f(t) \leftrightarrow F(\omega), g(t) \leftrightarrow G(\omega)$	$f(t) * g(t) \leftrightarrow F(\omega)G(\omega)$
14	Freq convolution	$f(t) \leftrightarrow F(\omega), g(t) \leftrightarrow G(\omega)$	$f(t)g(t) \leftrightarrow \frac{1}{2\pi}F(\omega) * G(\omega)$
15	Compact form	Real $f(t)$	$f(t) = \frac{1}{2\pi} \int_0^\infty 2 F(\omega) \cos(\omega t + \angle F(\omega)) d\omega$
16	Parseval, Energy W	$f(t) \leftrightarrow F(\omega)$	$W \equiv \int_{-\infty}^{\infty} f(t) ^2 dt = \frac{1}{2\pi} \int_{-\infty}^{\infty} F(\omega) ^2 d\omega$

Table 3: Important properties of the Fourier transform.

	$f(t) \leftrightarrow F(\omega)$		
1	$e^{-at}u(t) \leftrightarrow \frac{1}{a+j\omega}, \ a>0$	14	$\delta(t) \leftrightarrow 1$
2	$e^{at}u(-t) \leftrightarrow \frac{1}{a-j\omega}, \ a>0$	15	$1 \leftrightarrow 2\pi\delta(\omega)$
3	$e^{-a t } \leftrightarrow \frac{2a}{a^2 + \omega^2}, \ a > 0$	16	$\delta(t - t_o) \leftrightarrow e^{-j\omega t_o}$
4	$\frac{a^2}{a^2+t^2} \leftrightarrow \pi a e^{-a \omega }, \ a > 0$	17	$e^{j\omega_o t} \leftrightarrow 2\pi\delta(\omega - \omega_o)$
5	$te^{-at}u(t) \leftrightarrow \frac{1}{(a+j\omega)^2}, \ a>0$	18	$\cos(\omega_o t) \leftrightarrow \pi [\delta(\omega - \omega_o) + \delta(\omega + \omega_o)]$
6	$t^n e^{-at} u(t) \leftrightarrow \frac{n!}{(a+j\omega)^{n+1}}, \ a > 0$	19	$\sin(\omega_o t) \leftrightarrow j\pi[\delta(\omega + \omega_o) - \delta(\omega - \omega_o)]$
7	$\operatorname{rect}(\frac{t}{\tau}) \leftrightarrow \tau \operatorname{sinc}(\frac{\omega \tau}{2})$	20	$\cos(\omega_o t)u(t) \leftrightarrow \frac{\pi}{2} [\delta(\omega - \omega_o) + \delta(\omega + \omega_o)] + \frac{j\omega}{\omega_o^2 - \omega^2}$
8	$\operatorname{sinc}(Wt) \leftrightarrow \frac{\pi}{W}\operatorname{rect}(\frac{\omega}{2W})$	21	$\sin(\omega_o t)u(t) \leftrightarrow j\frac{\pi}{2}[\delta(\omega + \omega_o) - \delta(\omega - \omega_o)] + \frac{\omega_o}{\omega_o^2 - \omega^2}$
9	$\triangle(\frac{t}{\tau}) \leftrightarrow \frac{\tau}{2} \operatorname{sinc}^2(\frac{\omega \tau}{4})$	22	$\operatorname{sgn}(t) \leftrightarrow \frac{2}{j\omega}$
10	$\operatorname{sinc}^2(\frac{Wt}{2}) \leftrightarrow \frac{2\pi}{W} \triangle(\frac{\omega}{2W})$	23	$u(t) \leftrightarrow \pi \delta(\omega) + \frac{1}{j\omega}$
11	$e^{-at}\sin(\omega_o t)u(t) \leftrightarrow \frac{\omega_o}{(a+j\omega)^2+\omega_o^2}, a>0$	24	$\sum_{n=-\infty}^{\infty} \delta(t - nT) \leftrightarrow \frac{2\pi}{T} \sum_{n=-\infty}^{\infty} \delta(\omega - n\frac{2\pi}{T})$
12	$e^{-at}\cos(\omega_o t)u(t) \leftrightarrow \frac{a+j\omega}{(a+j\omega)^2+\omega_o^2}, a>0$	25	$\sum_{n=-\infty}^{\infty} f(t)\delta(t-nT) \leftrightarrow \sum_{n=-\infty}^{\infty} \frac{1}{T}F(\omega - n\frac{2\pi}{T})$
13	$e^{-\frac{t^2}{2\sigma^2}} \leftrightarrow \sigma\sqrt{2\pi}e^{-\frac{\sigma^2\omega^2}{2}}$		

Table 4: Important Fourier transform pairs. The left-hand column includes only "energy signals" f(t),

while the right-hand column includes "power signals" and distributions.

$$t(t)(e^{jw_{c}t} + e^{-jw_{c}t}) = 2 f(t) \cos(w_{c}t) \iff F(w-w_{c}) + F(w+w_{c})$$

$$t(t) \cos(w_{c}t) \iff \frac{1}{2} F(w-w_{c}) + \frac{1}{2} F(w+w_{c})$$

$$\delta(t)^{*} f(t) = f(t)$$

$$\delta(t-t_{o})^{*} f(t) = f(t-t_{o})$$

$$P = V_{o} I_{o} I_{o}$$

卷积的性质

Name	Property
Commutative	h(t) * f(t) = f(t) * h(t)
Distributive	f(t) * (g(t) + h(t)) = f(t) * g(t) + f(t) * h(t)
Associative	f(t) * (g(t) * h(t)) = (f(t) * g(t)) * h(t)
Shift	$h(t) * f(t) = y(t) \Rightarrow h(t - t_0) * f(t) = h(t) * f(t - t_0) = y(t - t_0)$
Derivative	$h(t)*f(t) = y(t) \Rightarrow \left(\frac{d}{dt}h(t)\right)*f(t) = h(t)*\left(\frac{d}{dt}f(t)\right) = \frac{d}{dt}y(t)$
Reversal	$f(t)*h(t) = y(t) \Rightarrow h(-t)*f(-t) = y(-t)$
Start-point	If $h(t) = 0$ for $t < t_{sh}$ and $f(t) = 0$ for $t < t_{sf}$
	then $y(t) = h(t) * f(t) = 0$ for $t < t_{sy} = t_{sh} + t_{sf}$.
End-point	If $h(t) = 0$ for $t > t_{eh}$ and $f(t) = 0$ for $t > t_{ef}$
	then $y(t) = h(t) * f(t) = 0$ for $t > t_{ey} = t_{eh} + t_{ef}$.
Width	$h(t) * f(t) = y(t) \Rightarrow T_y = T_h + T_f$
	where T_h , T_f , and T_y denote the widths of $h(t)$, $f(t)$, and $y(t)$.

Table 5: Convolution properties.

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Name	Impulse properties	Shifted-impulse properties
Convolution	$\delta(t) * f(t) = f(t)$	$\delta(t - t_0) * f(t) = f(t - t_0)$
Sifting	$\int_{-\infty}^{\infty} \delta(t)f(t)dt = f(0) \text{and}$	$\int_{-\infty}^{\infty} \delta(t - t_0) f(t) dt = f(t_0) \text{and}$
	$\int_{a}^{b} \delta(t) f(t) dt = \begin{cases} f(0) & \text{if } a < 0 < b \\ 0, & \text{otherwise} \end{cases}$	$\int_{a}^{b} \delta(t - t_0) f(t) dt = \begin{cases} f(t_0) & \text{if } a < t_0 < b \\ 0, & \text{otherwise} \end{cases}$
Sampling	$f(t)\delta(t) = f(0)\delta(t)$	$f(t)\delta(t-t_0) = f(t_0)\delta(t-t_0)$
Symmetry	$\delta(-t) = \delta(t)$	$\delta(t_0 - t) = \delta(t - t_0)$
Scaling	$\delta(at) = \frac{1}{ a }\delta(t), \ a \neq 0$	$\delta(a(t-t_0)) = \frac{1}{ a }\delta(t-t_0), \ a \neq 0$
Area	$\int_{-\infty}^{\infty} \delta(t)dt = 1 \text{and}$	$\int_{-\infty}^{\infty} \delta(t - t_0) dt = 1 \text{and}$
	$\int_{a}^{b} \delta(t)dt = \begin{cases} 1 & \text{if } a < 0 < b \\ 0, & \text{otherwise} \end{cases}$	$\int_{a}^{b} \delta(t - t_0) dt = \begin{cases} 1 & \text{if } a < t_0 < b \\ 0, & \text{otherwise} \end{cases}$
Definite integral	$\int_{-\infty}^{t} \delta(\tau) d\tau = u(t)$	$\int_{-\infty}^{t} \delta(\tau - t_0) d\tau = u(t - t_0)$ $\frac{d}{dt} u(t - t_0) = \delta(t - t_0)$
Unit-step derivative	$\frac{d}{dt}u(t) = \delta(t)$	$\frac{d}{dt}u(t-t_0) = \delta(t-t_0)$
Derivative	$\left(\frac{d}{dt}\delta(t)\right) * f(t) = \frac{d}{dt}f(t)$	$\left(\frac{d}{dt}\delta(t-t_0)\right)*f(t) = \frac{d}{dt}f(t-t_0)$
Fourier transform	$\delta(t) \leftrightarrow 1$	$\delta(t-t_0) \leftrightarrow e^{-j\omega t_0}$
Graphical symbol	1 δ (t)	$1 + \delta(t - t_0)$ t_0

Table 6: Properties of the impulse and shifted impulse.

1	$\delta(t) \leftrightarrow 1$	7	$\delta'(t) \leftrightarrow s$
2	$e^{pt}u(t)\leftrightarrow \frac{1}{s-p}$	8	$u(t) \leftrightarrow \frac{1}{s}$
3	$te^{pt}u(t)\leftrightarrow \frac{1}{(s-p)^2}$	9	$tu(t) \leftrightarrow \frac{1}{s^2}$
4	$t^n e^{pt} u(t) \leftrightarrow \frac{n!}{(s-p)^{n+1}}$	10	$t^n u(t) \leftrightarrow \frac{n!}{s^{n+1}}$
5	$\cos(\omega_o t)u(t) \leftrightarrow \frac{s}{s^2 + \omega_o^2}$	11	$\sin(\omega_o t)u(t) \leftrightarrow \frac{\omega_o}{s^2 + \omega_o^2}$
6	$e^{-\alpha t}\cos(\omega_d t)u(t) \leftrightarrow \frac{s+\alpha}{(s+\alpha)^2+\omega_d^2}$	12	$e^{-\alpha t}\sin(\omega_d t)u(t) \leftrightarrow \frac{\omega_d}{(s+\alpha)^2 + \omega_d^2}$

Table 7: Laplace transforms pairs $h(t) \leftrightarrow \hat{H}(s)$ involving frequently encountered causal signals — α , ω_o , and ω_d stand for arbitrary real constants, n for non-negative integers, and p denotes for an arbitrary complex constant.

	Name:	Condition:	Property:
1	Multiplication	$f(t) \to \hat{F}(s)$, constant K	$Kf(t) \to K\hat{F}(s)$
2	Addition	$f(t) \to \hat{F}(s), g(t) \to \hat{G}(s) \cdots$	$f(t) + g(t) + \cdots \rightarrow \hat{F}(s) + \hat{G}(s) + \cdots$
3	Time scaling	$f(t) \to \hat{F}(s)$, real $a > 0$	$f(at) \to \frac{1}{a}\hat{F}(\frac{s}{a})$
4*	Time delay	$f(t) \leftrightarrow \hat{F}(s), t_o \ge 0$	$f(t-t_o) \leftrightarrow \hat{F}(s)e^{-st_o}$
5	Frequency shift	$f(t) \to \hat{F}(s)$	$f(t)e^{s_o t} \to \hat{F}(s-s_o)$
6	Time derivative	Differentiable $f(t) \to \hat{F}(s)$	$f'(t) \to s\hat{F}(s) - f(0^{-})$ $f''(t) \to s^{2}\hat{F}(s) - sf(0^{-}) - f'(0^{-})$ \cdots $f^{(n)}(t) \to s^{n}\hat{F}(s) - \cdots - f^{(n-1)}(0^{-})$
7	Time integration	$f(t) \to \hat{F}(s)$	$\int_{0^{-}}^{t} f(\tau)d\tau \to \frac{1}{s}\hat{F}(s)$
8	Freq. derivative	$f(t) o \hat{F}(s)$	$-tf(t) o rac{d}{ds}\hat{F}(s)$
9*	Time convolution	$h(t) \leftrightarrow \hat{H}(s), f(t) \leftrightarrow \hat{F}(s)$	$h(t) * f(t) \leftrightarrow \hat{H}(s)\hat{F}(s)$
10	Freq. convolution	$f(t) \to \hat{F}(s), \ g(t) \to \hat{G}(s)$	$f(t)g(t) \to \frac{1}{2\pi j}\hat{F}(s) * \hat{G}(s)$
11	Poles	$f(t) \to \hat{F}(s)$	Values of s such that $ \hat{F}(s) = \infty$
12	ROC	$f(t) o \hat{F}(s)$	Portion of s – plane to the right of rightmost pole $\neq \infty$
13*	Fourier transform	$f(t) \leftrightarrow \hat{F}(s)$	$F(\omega) = \hat{F}(j\omega)$ if and only if ROC includes $s = j\omega$
14	Final value	Poles of $s\hat{F}(s)$ in LHP	$f(\infty) = \lim_{s \to 0} s\hat{F}(s)$
15	Initial value	Existence of the limit	$f(0^+) = \lim_{s \to \infty} s\hat{F}(s)$

Table 8: Important properties of the one-sided Laplace transform. Properties marked by * in the first column hold only for causal signals.