Ex1:

SoitzeR

$$\forall n \in \mathbb{N} \quad f(x) = f(x + n\tau)$$

SoitneR

$$\forall n \in \mathbb{N}$$
 $f(x) = f(x + nT)$

Donc
$$f(n) = +\infty$$
 Absurde

Ex3:

$$\mathbb{D}_{f} = \{ x \in \mathbb{R}, \tan x > 0 \} = \bigcup_{k \in \mathbb{Z}} \mathbb{J}_{k\pi} / \frac{\pi}{2} + k\pi [$$

$$\frac{\cos n - 1}{\sqrt{\tan n}} \sim \frac{-\frac{n^2}{2}}{\sqrt{n}} = -\frac{1}{2} n^{\frac{3}{2}}$$

2)
$$f: n \mapsto \ln (1+e^n) - \ln 2$$

$$Df = \left\{ x \in \mathbb{R} : 1 + e^n > 0 \right\} = \mathbb{R}$$

$$\ln (1+e^n) - \ln 2 = \ln \left(\frac{1+e^n}{2} \right)$$

$$\ln (1+h) \int_{h>0} h$$

$$\ln (g) \int_{g>0} g - 1 \text{ then the raniable}$$

$$\ln \left(\frac{1+e^n}{2} \right) \sim \frac{1+e^n}{2} - 1 = \frac{e^n - 1}{2}$$

$$\ln \left(\frac{1+e^n}{2} \right) = \ln \left(1 + \frac{e^n - 1}{2} \right) \sim \frac{e^n - 1}{2} \sim \frac{m}{2}$$
3) $f: n \mapsto \frac{1 - \sin \left(\frac{\pi}{2} \right)}{n - \sqrt{n^2 + 2n}}$

$$Df = \left\{ x \in \mathbb{R} \text{ ty } \left\{ \frac{n^2 + 2n \ge 0}{n + \sqrt{n^2 + 2n}} \right\}$$
Soit $n \in \mathbb{R}$

$$n^2 + 2n - n (n + 2)$$

$$dne \quad n^2 + 2n \ge 0 \iff n \in] - \infty; -2] \cup \{0; + \infty[$$

$$n \ge \sqrt{n^2 + 2n^2} \iff n \ge n \le] - \infty; -2] \cup \{0; + \infty[$$

$$n \ge \sqrt{n^2 + 2n^2} \iff n \ge n \le] - \infty; -2] \cup \{0; + \infty[$$

Done
$$Df =]-\omega; -2] \cup]0; +\omega[$$

$$1-\sin\left(\frac{\pi(1-x)}{2}\right) = 1-\sin\left(\frac{\pi}{2} + \frac{\pi\pi}{2}\right) = 1-\cos\left(\frac{\pi x}{2}\right) \sim \frac{1}{2}\left(\frac{\pi x}{2}\right)^2 = \frac{\pi^2}{8}x^2$$

$$\pi - \sqrt{n^2 + 2x^2} \sim -\sqrt{2\pi}$$

$$= \sqrt{2\pi}$$

Done
$$f(n) \sim \frac{\frac{\pi^2}{8} n^2}{-\sqrt{2\pi^2}} = -\frac{\pi^2}{8\sqrt{27}} n^{3/2}$$

Rg:
$$n - \sqrt{n^2 + 2n^2} \approx ?$$
 Methe en facteur les termes dominants $\varkappa \left(\Lambda - \sqrt{1 + \frac{2}{n^2}} \right) \sim \varkappa \times \left(\frac{-1}{2} \right) \times \frac{2}{\varkappa} = -1$

4)
$$f: n \mapsto \frac{\tan^2 n}{1 + \frac{1}{n^2}}$$

$$\mathcal{D}_{f} = \left\{ \kappa \in \mathcal{D}_{tan} \mid \kappa \neq 0 \right\} = \mathcal{D}_{tan} \setminus \left\{ 0 \right\} = \left(\bigcup_{k \in \mathbb{Z}} \left[-\frac{\pi}{2} + k\pi \right] + k\pi \left[\right] \setminus \left\{ 0 \right\}$$

$$\frac{\tan^2 n}{1 + \frac{1}{n^2}} \sim \frac{n^2}{\frac{1}{n^2}} = n^4 \frac{1}{n \rightarrow 0}, \quad 0$$

5)
$$f: n \mapsto \frac{\sqrt[3]{n^3 - 2}}{\sqrt{n^2 + n^2}}$$

$$\mathcal{D}_{f} = \left\{ n \in \mathbb{R} : n^{2} + n > 0 \right\} = \left[-\infty; -1 \left[U \right] o; + \infty \right[n \in \mathbb{R}$$

$$\sqrt[3]{x^3-2} \sim \sqrt[3]{-n}$$

$$\sqrt{x^2+x} \sim \sqrt{x}$$

$$\operatorname{Donc} \int (x) \sim \frac{\sqrt[3]{-x}}{\sqrt{n^{7}}} = \frac{-x^{\frac{1}{3}}}{x^{\frac{1}{2}}} = -x^{\frac{1}{6}} \xrightarrow{n \to 0} -\infty$$

6)
$$\int : n \mapsto \sqrt{\frac{1}{n} + \sqrt{\frac{1}{n} + \sqrt{\frac{1}{n}}}} - \sqrt{\frac{1}{n}}$$

$$\frac{1}{n} + \sqrt{\frac{1}{n}} \sim \frac{1}{n}$$

$$\sqrt{\frac{1}{\varkappa}} + \sqrt{\frac{1}{n}} \sim \sqrt{\frac{1}{\varkappa}}$$

$$\frac{1}{n} + \sqrt{\frac{1}{n}} + \sqrt{\frac{1}{n}} \sim \frac{1}{n}$$

$$\sim \sqrt{\frac{1}{n}} = o\left(\frac{1}{n}\right)$$

$$\sqrt{\frac{1}{n}} + \sqrt{\frac{1}{n}} + \sqrt{\frac{1}{n}} \sim \sqrt{\frac{1}{n}}$$

$$\int_{0}^{1} (n) - \sqrt{\frac{1}{n}} \left(\sqrt{1 + n \sqrt{\frac{1}{n}} + \sqrt{\frac{1}{n}}} - 1 \right)$$

$$\sim \sqrt{\frac{1}{n}} \times \frac{1}{2} \sqrt{n} = \frac{1}{2}$$

7)
$$\int : n \mapsto \sqrt[3]{\frac{1}{n^3} + \frac{1}{n}} + 1 - \sqrt{1 + \frac{1}{n^2}}$$

$$D \int_{1}^{\infty} = \mathbb{R}^{+}$$

$$\begin{cases} \binom{n}{n} = \frac{1}{n} + o\left(\frac{1}{n}\right) + \frac{1}{n} + o\left(\frac{1}{n}\right) \sim \frac{2}{n}
\end{cases}$$

$$\int (n) = \frac{1}{n^3} \left(\sqrt[3]{1 + n^2 + n^3} - \sqrt{1 + n^2} \right) \\
= \frac{1}{n^3} \left(\sqrt[3]{1 + n^2 + n^3} + 1 - \sqrt{1 + n^2} \right) \sim \frac{-n}{6} \\
\sim \frac{1}{3} n^2 \qquad \sim -\frac{1}{2} n^2$$