

ECS763U/P Natural Language Processing

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Week 2: Language

Models

## OUTLINE

- 1) The need for a probabilistic approach to NLP
- 2) Probability introduction
- 3) Language Models: motivation
- 4) Language Models: ngram models
- 5) Language Models: evaluation
- 6) Smoothing

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## Why Probability?

- Building a chatbot- what were the problems with 'intents'?
- You can define an input->output mapping like a database look-up....
- But what if the user doesn't say what you manually defined in the input examples?
- It 'breaks' with unseen input- we need something more robust which accepts things close to what is in its database, but not exact string matches.
- The system should be able to make a good guess at which intent the user's contribution refers to. i.e. 'A Hawaiwan with extra cheese please' **probably means** #UserRequestPizza.

- The measure of the likelihood that an event will occur or that a given proposition is the case. A value between 0 (impossible) and 1 (certain). E.g.:
  - The probability that the earth is flat: close to 0
  - The probability that 1 + 1 = 3: **0**
  - The probability that the sun will set today: close to 1
  - The probability that 1 + 1 = 2: **1**
  - The probability that 6 is thrown in a fair die: 1/6

- Complex probabilities with more than one event/state of affairs in question can be cashed out in terms of ANDs and ORs over single outcomes:
  - probability it will rain and be warm?
  - probability it will rain or snow?

 AND: The probability of two 6's being thrown in a fair die one after each other, i.e. the probability of one independent throw being a 6 <u>and</u> another independent throw being 6, just multiply the probabilities:

```
p(6 thrown) x p(6 thrown) = 1/6 \times 1/6 = 1/36
```

(conjunctive probability of independent events)

• **OR:** The probability of either a 6 <u>or</u> a 3 being thrown in a fair die for a given throw, just **add** the probabilities :

```
p(6 \text{ thrown}) + p(3 \text{ thrown}) = 1/6 + 1/6 = 1/3
```

(disjunctive probability of independent events)

- Also what GIVEN we know that one event has happened, THEN want to know the probability another event has happened, i.e. conditional probability.
- Given I know I have thrown an even numbered die ({2,4,6}), then what's the probability of me having thrown a 6?
  - Originally when there were 6 possible outcomes {1,2,3,4,5,6}, the probability was 1/6.
  - Now, given the new condition, this has changed, as there are only 3 possible outcomes {2,4,6} we need to be concerned with- so the likelihood changes to 1/3.
  - We narrow the denominator from all events in the event space to a subset of that space given the information we have.

- However, not everything is a die. For potentially dependent events, you can't just multiply for conjunction and add for disjunction. We need general rules.
- A and B can also be calculated in terms of A given B and B given A, so we have the product rule:

$$p(A \land B) = p(A \mid B) \times p(B) = p(B \mid A) \times p(A)$$

• For A or B, you have to factor out the probability of A and B, so in general we have the sum rule:

$$p(A \lor B) = p(A) + p(B) - p(A \land B)$$

 You can formulate conditional probability (i.e. A is the case, given B is the case) in terms of the probability of and A and B being the case over the probability B is the case:

$$p(A \mid B) = \frac{p(A \land B)}{P(B)}$$

 Using the product rule for the numerator, conditional probability can be formulated in terms of Bayes rule:

$$p(A \mid B) = \frac{p(B \mid A)p(A)}{p(B)}$$

- This is one of the most important equations in probability theory (and NLP)
- It allows estimation of p(A|B), using p(B|A), p(A) and p(B) without necessarily having full access to the full joint distribution p(A,B), which is often very large.

Bayes rule:

$$p(A \mid B) = \frac{p(B \mid A)p(A)}{p(B)}$$

- We can think of this in terms of set theory where a possible outcome can be seen as a set.
- The probability of an outcome, e.g. *throws 6*, is a function of the **cardinality** (size) of the set of all instances with that outcome and the number of *all* events in the **event space** *U*.
- This means any probability is between 0 and 1.

$$p(throws6) = \frac{|throws6|}{|U|}$$
 i.e. for any event A,  $p(A) = \frac{|A|}{|U|}$ 

 We can use the analogues of conjunction (and) and disjunction (or) for set intersection and set union:

$$p(A \wedge B) = \frac{|A \cap B|}{|U|}$$

$$p(A \vee B) = \frac{|A \cup B|}{|U|}$$

• And Bayes rule can be formulated as:  $p(A|B) = \frac{|A \cap B|}{|B|}$ 

U

$$p(A) = \frac{|A|}{|U|} = \frac{3}{4}$$
$$p(B) = \frac{|B|}{|U|} = \frac{2}{4}$$

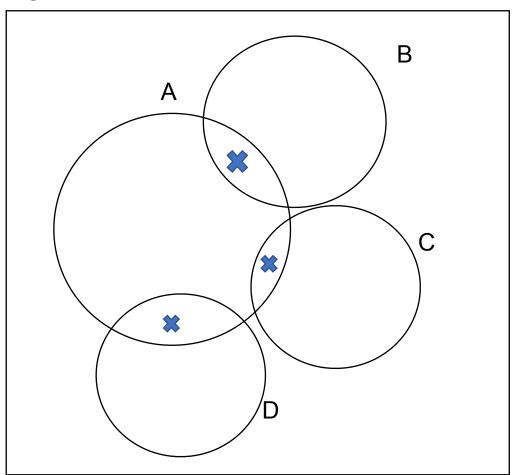
$$p(A \land B) = \frac{\left|A \cap B\right|}{\left|U\right|} = \frac{1}{4}$$
$$p(A \lor B) = \frac{\left|A \cup B\right|}{\left|U\right|} = \frac{4}{4} = 1$$

$$p(A \mid B) = \frac{|A \cap B|}{|B|} = \frac{1}{2}$$

$$p(B \mid A) = \frac{|A \cap B|}{|A|} = \frac{1}{3}$$

# What is a Discrete Probability Distribution?

U

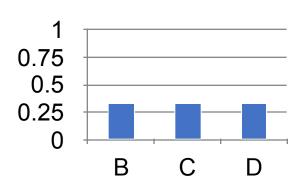


$$p(X = ? | A)$$

$$p(B \mid A) = \frac{|A \cap B|}{|A|} = \frac{1}{3}$$

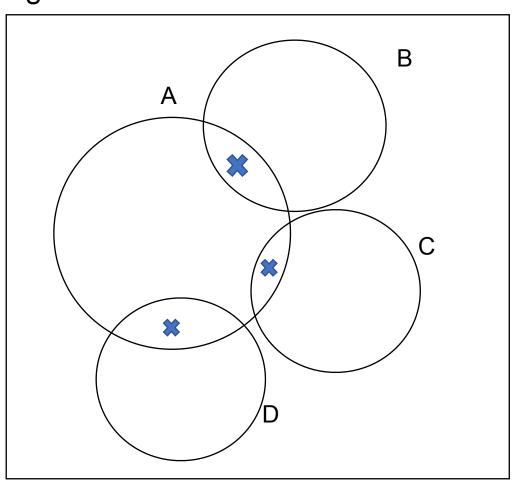
$$p(C \mid A) = \frac{|A \cap C|}{|A|} = \frac{1}{3}$$

$$p(D \mid A) = \frac{|A \cap D|}{|A|} = \frac{1}{3}$$



# What is a Discrete Probability Distribution?

J

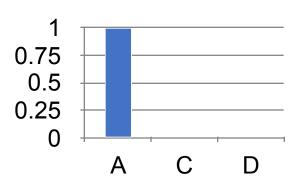


$$p(X = ? | B)$$

$$p(A \mid B) = \frac{|B \cap A|}{|B|} = \frac{1}{1} = 1$$

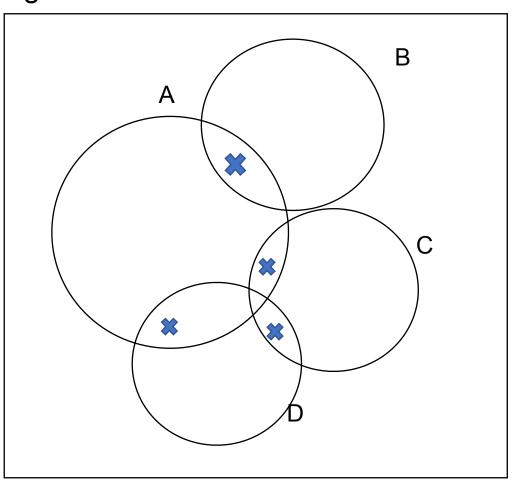
$$p(C|B) = \frac{|B \cap C|}{|B|} = \frac{0}{1} = 0$$

$$p(D \mid B) = \frac{|B \cap D|}{|B|} = \frac{0}{1} = 0$$



# What is a Discrete Probability Distribution?

J

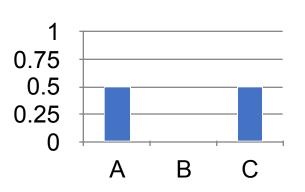


$$p(X = ? \mid D)$$

$$p(A | D) = \frac{|D \cap A|}{|D|} = \frac{1}{2}$$

$$p(B|D) = \frac{|D \cap B|}{|D|} = \frac{0}{2} = 0$$

$$p(C|D) = \frac{|D \cap C|}{|D|} = \frac{1}{2}$$



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## Sequence Modelling Tasks

- We considered a classification task last week (sentiment analysis) d → c
- Many problems are about modelling (labelling, characterising, evaluating) sequences:
  - Part-of-speech tagging
  - Dialogue act tagging
  - Named entity recognition
  - Speech recognition
  - Spelling correction
  - Machine translation

•

#### Sequence Likelihood Tasks

Speech recognition

```
I saw a van eyes awe of an
```

Spelling correction

```
It's about fifteen minuets from my house It's about fifteen minutes from my house
```

Machine translation

```
vjetar će biti noćas jak:
the wind tonight will be strong
the wind tonight will be powerful
the wind tonight will be a yak
```

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- To do effective sequence prediction we want to know the likelihood of different sequences (of words).
- Language models are designed to do this and are machines which play the Shannon Game (1951), reframing the challenge as:

 How well can we predict the next word given the history of previous words?

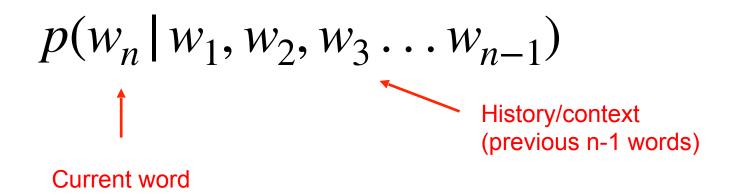
		mushrooms 0.1
		pepperoni 0.1
I always order pizza with cheese and<	) \	anchovies 0.01
The 33rd President of the US was		fried rice 0.0001
I saw a		
		and 1e-100

- Answering the following questions would be useful for assigning probabilities to sequences:
  - What is the probability of observed sequence O?  $p(O) = p(o_1, o_2, o_3, ...o_n)$
  - Given observed sequence  $O = o_1 ... o_{n-1}$ , what is the probability of observing symbol  $o_n$  next?

$$p(o_n|o_1,o_2,o_3,...o_{n-1})$$

- i.e. What is p("john likes mary") or p("john likes") or p("john likes"|"john")?
- A model which computes these is a language model.

• A language model estimates the probability function *p*:



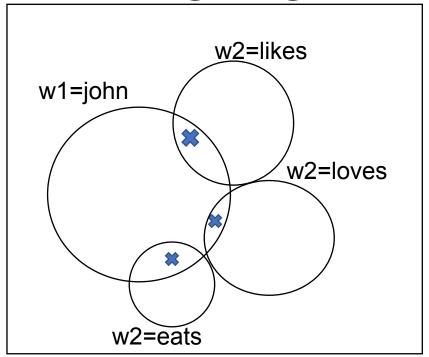
- For each context it gives a discrete probability distribution over all words in the vocabulary.
- It assigns a probability value for a given word observed at position w<sub>n</sub> given the context observed at w<sub>1</sub> ...w<sub>n-1</sub>

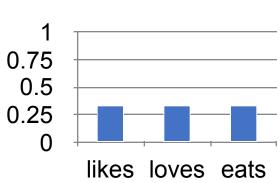
 The probability of the next word being a given value, (e.g. 'loves') independent of the previous words is the unigram probability. In event terms:

$$p(w_i = loves) = \frac{\left| w_i = loves \right|}{\sum_{x \in vocab} \left| w_i = x \right|}$$

• Using the probability of the next word given the previous one i.e. the conditional probability  $p(w_i|w_{i-1})$  (e.g. for 'john loves') is the **bigram** probability. In event terms:

$$p(w_i = loves | w_{i-1} = john) = \frac{|w_{i-1} = john \cap w_i = loves|}{|w_{i-1} = john|}$$





$$p(w2 = loves \mid w1 = john) = \frac{\left|w1 = john \cap w2 = loves\right|}{\left|w1 = john\right|} = \frac{1}{3}$$

$$p(w2 = likes \mid w1 = john) = \frac{\left|w1 = john \cap w2 = likes\right|}{\left|w1 = john\right|} = \frac{1}{3}$$

$$p(w2 = eats \mid w1 = john) = \frac{\left|w1 = john \cap w2 = eats\right|}{\left|w1 = john\right|} = \frac{1}{3}$$

#### The Chain Rule

- In ngram models, how do we assign probabilities to an entire sequence of words, or the probability of a word given the words so far?
- We can address both via the chain rule
- Recall the definition of conditional probabilities (through the product rule)

Rewriting: P(A,B) = P(A)P(B|A)

More variables:

$$P(A,B,C,D) = P(A)P(B|A)P(C|A,B)P(D|A,B,C)$$

The Chain Rule in General

$$P(x_1, x_2, x_3, ..., x_n) = P(x_1)P(x_2|x_1)P(x_3|x_1, x_2)...P(x_n|x_1, ..., x_{n-1})$$

## Using the chain rule

- How do we estimate probabilities? E.g. for the sentence 'Its water is so transparent'
- Count and divide:

```
p(its\ water\ is\ so\ transparent) = p(transparent\ |\ its\ water\ is\ so) = \frac{C(its\ water\ is\ so\ transparent)}{C(its\ water\ is\ so)}
```

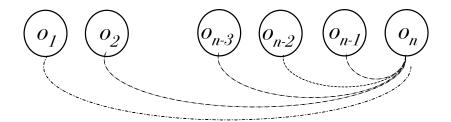
According to the chain rule:

```
p("its water is so transparent") = \\ p(its) \times \\ p(water|its) \times \\ p(is|its water) \times \\ p(so|its water is) \times \\ p(transparent|its water is so)
```

• We'll never see enough data, so use the **Markov Assumption**probability of next word only depends on a fixed number of words back, e.g. for a bigram, only depends on previous word:

## Markov Assumption

Instead of:



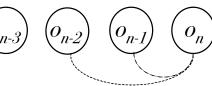
- We approximate by:
  - "n-gram model of length k" (where k = n-1)

trigram model (k=2):



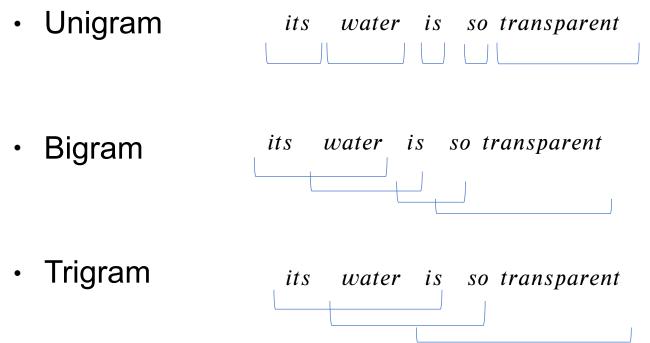






- In general not sufficient but often good approximation for high k.
  - Ignores long-distance dependencies:
    - "the computer I just put into the machine room on the fifth floor crashed"

- This can go up to any arbitrary length (or 'order'), e.g. unigram, bigram, trigram, 4-gram....7-gram... etc.
- In general n-gram models (Shannon, 1948).



4-gram etc.

- General method when processing sequences is to extract the relevant n-grams (word sequences) according of order n.
- In training count the frequency of the ngrams occurring in the training data and store the counts.
- In testing use those counts to get probabilities of sequences of unseen data.
- Deriving the probabilities can be done with a variety of methods!

 After training a Maximum Likelihood Estimation (MLE) bigram model from counting function C from a corpus:

$$p(w_i \,|\, w_{i-1}) = \frac{C(w_{i-1}, w_i)}{C(w_{i-1})}$$
 context (previous n-1 words)

$$p(w_i | w_{i-1}) = \frac{C(w_{i-1}, w_i)}{C(w_{i-1})}$$

 Example corpus (note beginning (<s>) and end-of-sentence (</s>) markers):

<s>I am Sam </s>

<s> Sam I am </s>

<s> I do not like green eggs and ham </s>

#### Exercise: what is the MLE estimate for:

$$p(||~~) =~~$$

$$p(||Sam|) =$$

$$p(|Sam) = p(do|I) = p(do|I) = p(do|I)$$

$$p(do|I) = \blacksquare$$

$$p(w_i | w_{i-1}) = \frac{C(w_{i-1}, w_i)}{C(w_{i-1})}$$

Example corpus
 (note beginning (<s>) and end-of-sentence (</s>)
markers):

<s> I am Sam </s>

<s> Sam I am </s>

<s> I do not like green eggs and ham </s>

#### Exercise: what is the MLE estimate for:

$$p(||~~) = 2/3~~$$
  $p(Sam||~~) = 1/3~~$   $p(am||) = 2/3$   $p(|Sam) = 1/2$   $p(Sam|am) = 1/2$   $p(do||) = 1/3$ 

(Real corpus) Berkeley Restaurant Project sentences:

- can you tell me about any good cantonese restaurants close by
- mid priced thai food is what i'm looking for
- tell me about chez panisse
- can you give me a listing of the kinds of food that are available
- i'm looking for a good place to eat breakfast
- when is caffe venezia open during the day

• Bigram counts from 9222 sentences

Word (cont		Word 2 (the bigram is Word 1,Word2) t)							
		i	want	to	eat	chinese	food	lunch	spend
i		5	827	0	9	0	0	0	2
wa	nt	2	0	608	1	6	6	5	1
to		2	0	4	686	2	0	6	211
eat		0	0	2	0	16	2	42	0
chi	inese	1	0	0	0	0	82	1	0
foo	od	15	0	15	0	1	4	0	0
lur	nch	2	0	0	0	0	1	0	0
spe	end	1	0	1	0	0	0	0	0

$$p(w_i | w_{i-1}) = \frac{C(w_{i-1}, w_i)}{C(w_{i-1})}$$

- Bigram MLE estimates:
- Normalize by unigram counts:

i	want	to	eat	chinese	food	lunch	spend
2533	927	2417	746	158	1093	341	278

Result:

	i	want	to	eat	chinese	food	lunch	spend
i	0.002	0.33	0	0.0036	0	0	0	0.00079
want	0.0022	0	0.66	0.0011	0.0065	0.0065	0.0054	0.0011
to	0.00083	0	0.0017	0.28	0.00083	0	0.0025	0.087
eat	0	0	0.0027	0	0.021	0.0027	0.056	0
chinese	0.0063	0	0	0	0	0.52	0.0063	0
food	0.014	0	0.014	0	0.00092	0.0037	0	0
lunch	0.0059	0	0	0	0	0.0029	0	0
spend	0.0036	0	0.0036	0	0	0	0	0

# Language Models

 Bigram MLE estimates (example knowledge of the model after counts):

- p(english|want) = .0011
- p(chinese|want) = .0065
- p(to|want) = .66
- p(eat|to) = .28
- p(food|to) = 0
- p(want|spend) = 0
- p(i|<s>) = .25

# Language Models

 Bigram MLE probability estimates of full sentences/ multiple contiguous ngrams- use multiplication of probabilities assuming independence of bigrams:

```
p(<s> I want english food </s>) =
 p(I|<s>)
  × p(want|I)
  × p(english|want)
  × p(food|english)
  × p(</s>|food)
  = .000031
```

## Language Models

- Practical reality: we do everything in log space
  - Avoids underflow
  - Adding is faster than multiplying.

$$log(p(w_1) \times p(w_2) \times p(w_3)) = log(p(w_1)) + log(p(w_2)) + log(p(w_3))$$

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#### How do we evaluate a LM?

- Gather a corpus.
- Divide it into 3 standard sections:

## **Training Data**



Test Data

- Gather all the counts/estimations from the training data
- Iteratively develop by assigning probability to the heldout (not the test!) data.
- Experiment with value of n and other parameters like discounts (more later).
- Get the **Perplexity** score on the Test data (measure of how confused the model is by the unseen corpus).

### How do we evaluate a LM?

- Though, don't forget the preprocessing first!
  - Tokenizing raw text.
  - Spelling normalization (including capitalization).
  - Removal of punctuation (though possibly not all!)
- What about words not in the training data but which appear at testing time (remember language is Zipfian!)
- These could give a zero and mess up the model/ perplexity!
- How do we estimate how many unknown or 'out of vocabulary' (OOV) words we're likely to encounter at testing?

#### How do we evaluate a LM?

- Several approaches to unknown/OOV words:
  - 1. Set a minimum document frequency for words across the training data. Any words appearing less than that, replace with an unknown word token <unk/>
  - 2. Set some heldout training data aside, and any words appearing in that which are not in the training data, set as <unk/>
- At test time, replace all unknown words to the model with <unk/>.
- Warning- for a fair comparison of different models' perplexities, the same vocab must be used!

## 1. OOV words with minimum doc frequency

## Training Data- pass 1

John likes Mary John adores Mary John adores Bill Get counts only for the vocab selection.

Vocab counts: John: 3, likes:1, adores: 2, Mary: 2, Bill: 1

Min. Doc. freq = 2, Vocab = {John, adores, Mary}

## Training Data pass 2

John likes Mary
John adores Mary
John adores Bill

Replace OOV words with <unk/>, then get counts for the language model.

John **<unk/>** Mary John adores Mary John adores **<unk/>** 

Counts: John: 3, adores: 2,

Mary: 2, <unk/>: 2

#### **Test Data**

John despises Mary Bill adores John



John <unk/> Mary <unk/> adores John

## 2. OOV words from heldout training data

## **Training Data**

John likes Mary John adores Mary John adores Bill Do the counts for all words without replacement and define vocab as all words observed in this data.

Counts: John: 3, likes:1, adores: 2, Mary: 2, Bill: 1

Vocab = {John, likes, Mary, adores, Bill}

#### Held-Out Training Data

John hates Mary Bill adores Mary Replace OOV words with <unk/>, then keep adding to the model counts

John **<unk/>** Mary Bill adores Mary

Counts: John: 4, likes:1, adores: 3,

Mary: 4, Bill: 2, <unk/>: 1

#### **Test Data**

John despises Mary Bill adores John



John **<unk/>** Mary Bill adores John

# Perplexity

- The Shannon Game:
  - How well can we predict the next word?

I always order pizza with cheese and \_\_\_\_\_

The 33rd President of the US was \_\_\_\_\_

I saw a \_\_\_\_

mushrooms 0.1
pepperoni 0.1
anchovies 0.01
....
fried rice 0.0001
....
and 1e-100

- Unigrams are terrible at this game. (Why?)
- A better model of a text
  - is one which assigns a higher probability to the word that actually occurs!

# Perplexity

- The best language model is one that best predicts an unseen test data W, i.e. the one that gives the highest probability for those sentences.
- Perplexity is the inverse probability of the test set, normalised by the number of words:

$$PP(W) = P(w_1 w_2 \dots w_N)^{-\frac{1}{N}}$$
$$= \sqrt[N]{\frac{1}{P(w_1 w_2 \dots w_N)}}$$

Chain rule: 
$$PP(W) = \sqrt[N]{\prod_{i=1}^{N} \frac{1}{P(w_i|w_1...w_{i-1})}}$$

For bigrams: 
$$PP(W) = \sqrt[N]{\prod_{i=1}^{N} \frac{1}{P(w_i|w_{i-1})}}$$

Minimising perplexity is the same as maximising probability

# Perplexity

- Cross-entropy is another metric used for evaluating the confusion of the language model on a test corpus.
- Practically, it is easy to calculate as just the negative sum of the log probabilities divided by the length of the corpus:

$$H(W) = -\frac{1}{N}\log P(w_1w_2...w_N)$$

 Perplexity can be calculated from cross-entropy as it's 2 (or whatever log base you're using) to the power of the cross-entropy:

Perplexity(W) = 
$$2^{H(W)}$$

So, minimising cross-entropy is also the same as maximising probability

## Lower perplexity, better model

 Training 38 million words, test 1.5 million words, Wall St. Journal

N-gram Order	Unigram	Bigram	Trigram
Perplexity	962	170	109

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# The danger of overfitting!

- N-grams only work well for word prediction if the test corpus looks like the training corpus
  - In real life, it often doesn't
  - We need to train robust models that generalize!
- One kind of generalization: ngrams with 0 counts!
  - Things that don't ever occur in the training set
  - But occur in the test set

## Zeros!

- Training set:
  - ... denied the allegations
  - ... denied the reports
  - ... denied the claims
  - ... denied the request

- Test set
  - •... denied the offer
  - •... denied the loan

$$p(offer \mid denied the) = 0$$

- ngrams with zero probability
  - mean that we will assign 0 probability to the test set!
- And hence we cannot compute perplexity (can't divide by 0)!

### What can we do about this?

Three main approaches:

#### Smoothing

Hold back some probability mass for unseen events

#### Backoff & Interpolation

Estimate n-gram probability from (n-1)-gram probability

#### Class-based models

Group words together, estimate class n-gram probability

# **Smoothing**

When we have sparse statistics from the counts:

```
C(denied the, w)
3 allegations
2 reports
1 claims
1 request
7 total
```

 'Steal'/spread around probability mass to generalize better. I.e. **Discount** some of the seen counts and add that discount to unseen counts:

```
C(denied the, w)
2.5 allegations
1.5 reports
0.5 claims
0.5 request
2 other
7 total
```

- Also called Laplace smoothing
- Pretend we saw each word one more time than we did
- Just add one to all the counts!

• MLE estimate: 
$$p(w_i | w_{i-1}) = \frac{C(w_{i-1}, w_i)}{C(w_{i-1})}$$

Add-1 estimate:

$$p^{add-one}(w_i \mid w_{i-1}) = \frac{C(w_{i-1}, w_i) + 1}{C(w_{i-1}) + V}$$
 Vocab size

Add one to all counts (can be done during testing too).
 New counts will look like this:

	i	want	to	eat	chinese	food	lunch	spend
i	6	828	1	10	1	1	1	3
want	3	1	609	2	7	7	6	2
to	3	1	5	687	3	1	7	212
eat	1	1	3	1	17	3	43	1
chinese	2	1	1	1	1	83	2	1
food	16	1	16	1	2	5	1	1
lunch	3	1	1	1	1	2	1	1
spend	2	1	2	1	1	1	1	1

 Results in a discount (reduction) of the seen counts, but adding to the unseen ones to give the smoothed probabilities.

	i	want	to	eat	chinese	food	lunch	spend
i	0.0015	0.21	0.00025	0.0025	0.00025	0.00025	0.00025	0.00075
want	0.0013	0.00042	0.26	0.00084	0.0029	0.0029	0.0025	0.00084
to	0.00078	0.00026	0.0013	0.18	0.00078	0.00026	0.0018	0.055
eat	0.00046	0.00046	0.0014	0.00046	0.0078	0.0014	0.02	0.00046
chinese	0.0012	0.00062	0.00062	0.00062	0.00062	0.052	0.0012	0.00062
food	0.0063	0.00039	0.0063	0.00039	0.00079	0.002	0.00039	0.00039
lunch	0.0017	0.00056	0.00056	0.00056	0.00056	0.0011	0.00056	0.00056
spend	0.0012	0.00058	0.0012	0.00058	0.00058	0.00058	0.00058	0.00058

- Add-1 estimation is a blunt instrument
- So add-1 isn't used very much for language modelling:
  - We'll have a look at a couple of better methods!
- But add-1 is used to smooth other NLP models
  - For text classification.
  - In domains where the number of zeros isn't so huge.

# Add-k smoothing (generalized additive smoothing)

- Also additive Laplace smoothing, though sometimes 'Lidstone' smoothing
- Pretend we saw each word a value k more than we did.
- MLE estimate:  $p(w_i | w_{i-1}) = \frac{C(w_{i-1}, w_i)}{C(w_{i-1})}$
- Add-k estimate:

$$p^{add-k}(w_i | w_{i-1}) = \frac{C(w_{i-1}, w_i) + k}{C(w_{i-1}) + kV}$$

• Add-1 smoothing a special case where *k*=1.

# **Backoff and Interpolation**

- Sometimes it helps to use less context
  - Condition on less context for contexts you haven't learned much about

#### Backoff:

- use trigram if you have good evidence,
- · otherwise bigram, otherwise unigram

#### Interpolation (with lower orders):

- mix unigram, bigram, trigram
- Interpolation tends to work better in general.

# **Backoff and Interpolation**

Simple interpolation

where:

$$\hat{P}(w_n|w_{n-2}w_{n-1}) = \lambda_1 P(w_n|w_{n-2}w_{n-1}) + \lambda_2 P(w_n|w_{n-1}) + \lambda_3 P(w_n)$$

$$\sum_{i} \lambda_{i} = 1$$

Lambdas conditional on context:

$$\hat{P}(w_n|w_{n-2}w_{n-1}) = \lambda_1(w_{n-2}^{n-1})P(w_n|w_{n-2}w_{n-1}) 
+ \lambda_2(w_{n-2}^{n-1})P(w_n|w_{n-1}) 
+ \lambda_3(w_{n-2}^{n-1})P(w_n)$$

## Backoff and Interpolation

Use a held-out corpus to get the right λs

**Training Data** 



Test Data

- Choose λs to maximize the probability of held-out data:
  - Fix the N-gram probabilities (on the training data)
  - Then search for λs that give largest probability to held-out set
- Advanced interpolation + backoff technique- Kneser-Ney smoothing. Uses absolute discounting and the lowerorder models. See Goodman (2001).

## Summary

- Language models offer a way to assign a probability to a sentence or other sequence of words, and to predict a word from preceding words.
- n-gram models are Markov models that estimate words from a fixed window of previous words. n-gram probabilities can be estimated by counting in a corpus and normalizing (the maximum likelihood estimate).
- n-gram language models are evaluated extrinsically in some task, or intrinsically using perplexity.
- The perplexity of a test set according to a language model is the geometric mean of the inverse test set probability computed by the model.

## Summary

- Smoothing algorithms provide a more sophisticated way to estimate the probability of n-grams. Commonly used smoothing algorithms for n-grams rely on lowerorder n-gram counts through backoff or interpolation.
- Both backoff and interpolation require discounting to create a probability distribution.
- <u>Lab: Implement Add-one smoothing, generalised additive smoothing and Kneser-Ney smoothing.</u>
   The interpolated Kneser-Ney smoothing algorithm mixes a discounted probability with a lower-order continuation probability.

# Reading

- Manning and Schuetze (1999) Chapters 2 and 6
- Jurafsky and Martin (3<sup>rd</sup> Ed) Chapter 3
- Goodman (2001)- "A bit of Progress in Language Modeling"