

Recovery controller for ANYmal on various terrains

Kyoungyeon Choi

15 credits project

Supervisor: Joonho Lee, Takahiro Miki

Intro: Motivation



Backflipping MIT Mini Cheetah

<https://www.youtube.com/watch?v=xNeZWP5Mx9s>

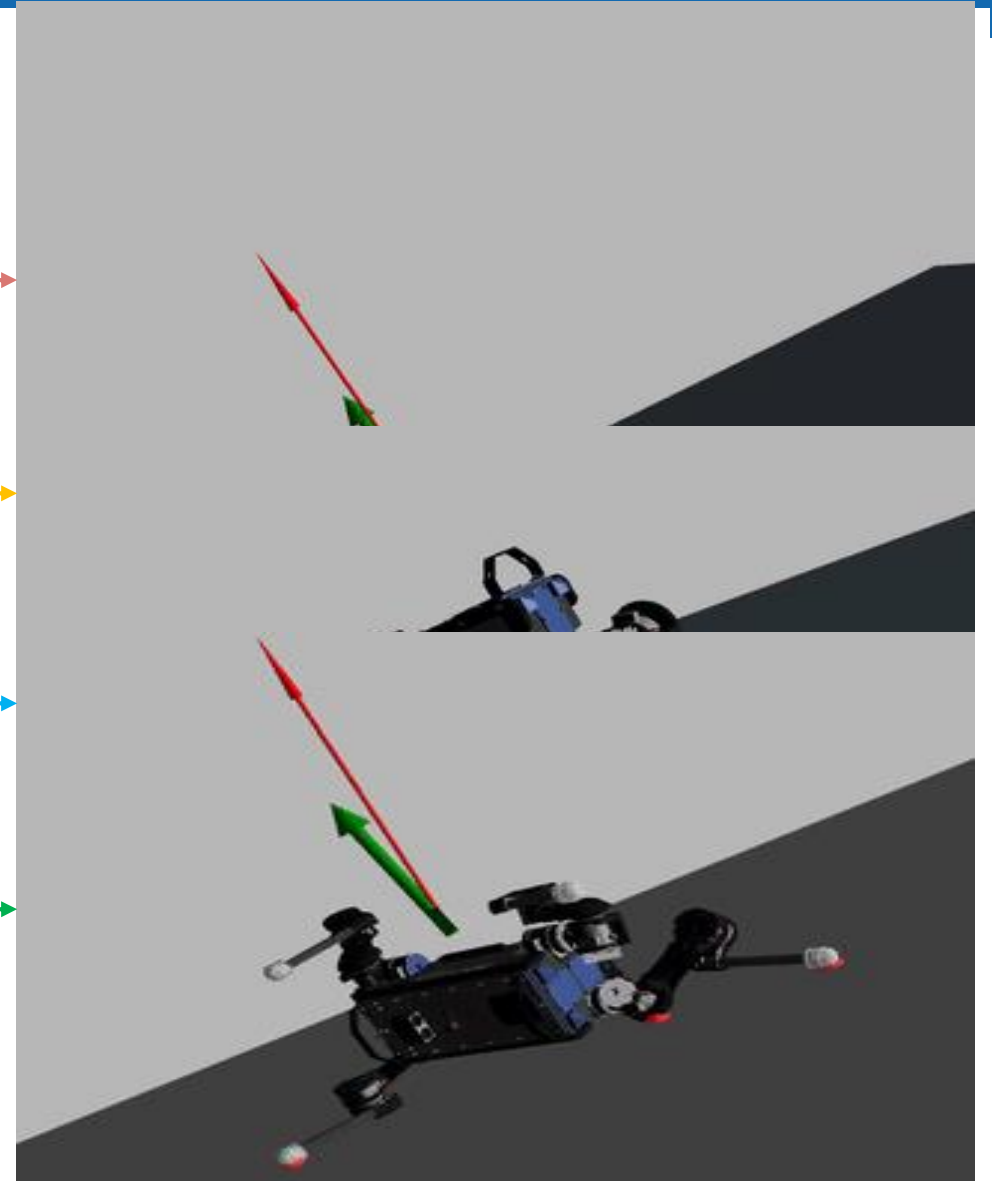
Intro: Approach & Contributions

1. Recovery controller

2. Terrain normal estimation

3. Standing up controller

4. Finite state machine



Method: Recovery Controller

I : inertial frame

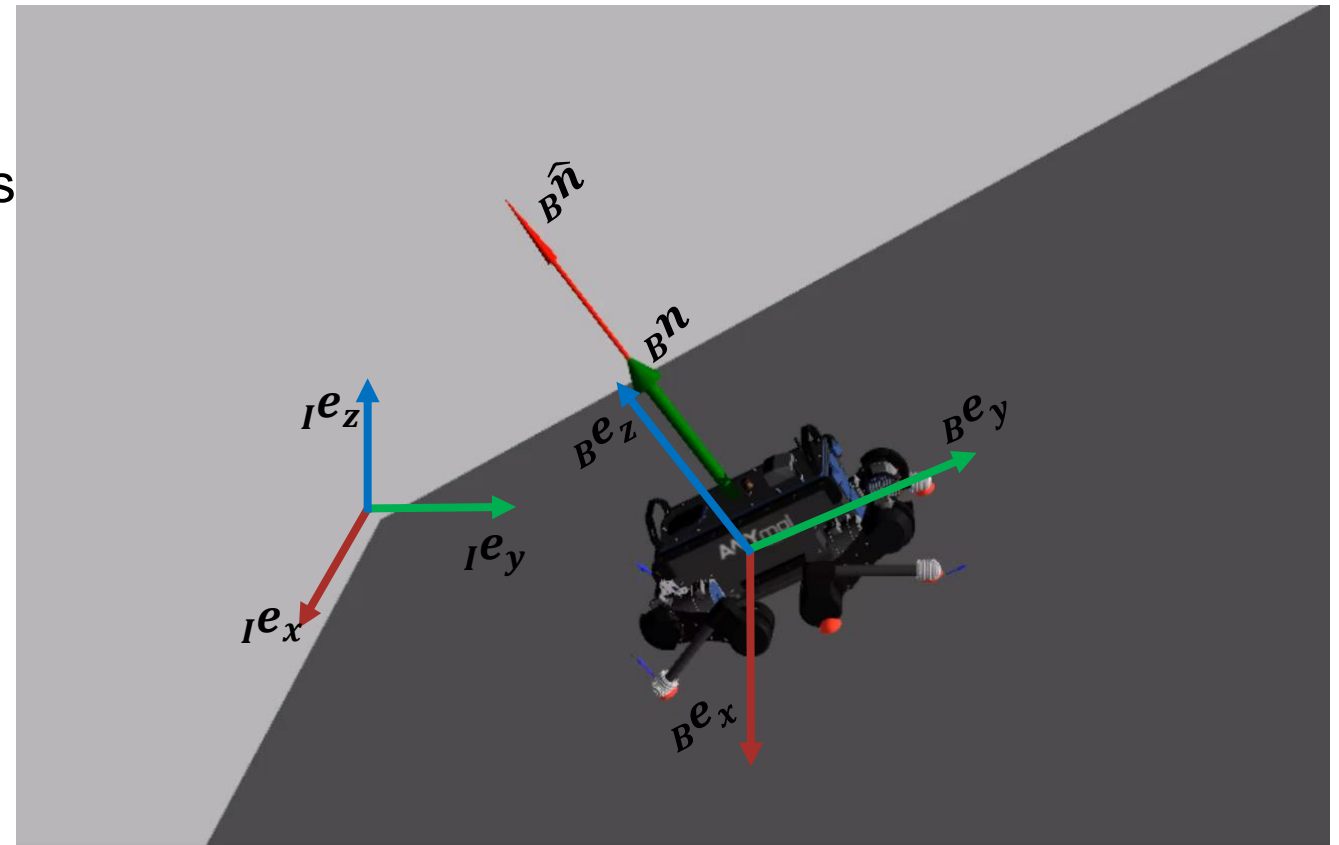
B : Body frame

${}_B n$: terrain normal vector expressed in B

${}_B \hat{n}$: normal vector observation expressed in B

Task Objective :

Recover from arbitrary falling configurations and sit with a stable position.
(on flat and slope(0~36deg) terrains)



Method: Recovery Controller

MDP observation space O_t :

$$\langle e_g, {}_B v_{IB}, {}_B \omega_{IB}, \psi, \dot{\psi}_{t_k}, \dot{\psi}_{t_k - 0.01}, \dot{\psi}_{t_k - 0.02}, a_{k-1} \rangle \in R^{69} [1,2]$$

Gravity vector : $e_g \in R^3$

Linear velocity : ${}_B v_{IB} \in R^3$

Angular velocity : ${}_B \omega_{IB} \in R^3$

Joint positions : $\psi \in R^{12}$

Joint velocity history : $\dot{\psi}_{t_k}, \dot{\psi}_{t_k - 0.01}, \dot{\psi}_{t_k - 0.02} \in R^{36}$

Previous action: $a_{k-1} \in R^{12}$

MDP action space a_t :

$$\psi_d = \psi_t + k a_t \quad (k = 0.1), \quad a_t \in R^{12}$$

Current joint positions : $\psi_t \in R^{12}$

Desired joint positions : $\psi_d \in R^{12}$

Cost terms :

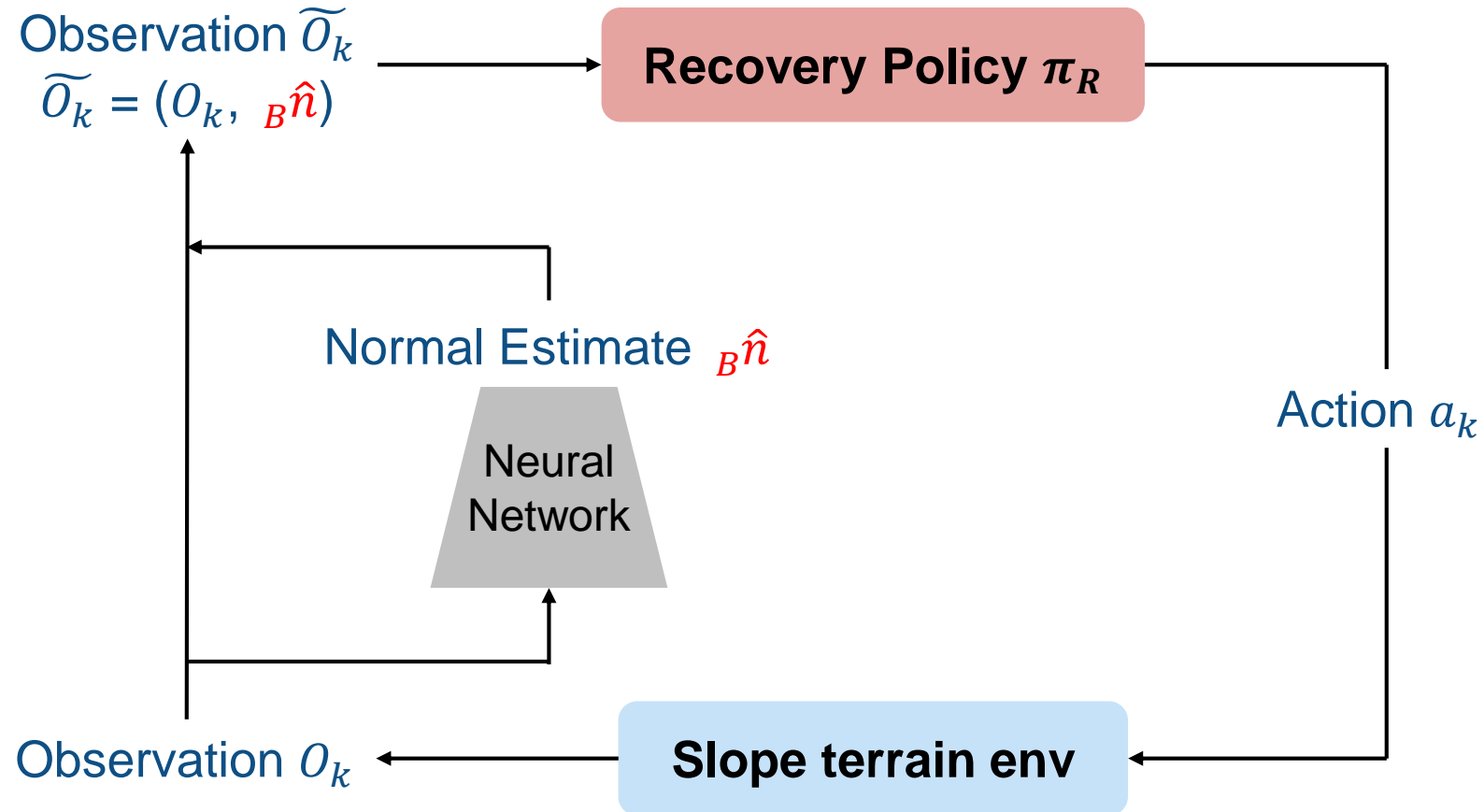
Orientation, Joint position, Self collision,
Joint acceleration, Joint velocity, Torque

Orientation Cost : $({}_B \hat{n} \cdot {}_B e_z - 1)^2$

Terrain normal vector exp in body frame: ${}_B \hat{n} \in R^3$

Body z axis exp in body frame: ${}_B e_z \in R^3$

Method: Normal Estimator



Method: Normal Estimator

Input observations:

$$\langle e_g, \psi \rangle \in R^{15}$$

Gravity vector : $e_g \in R^3$

Joint positions : $\psi \in R^{12}$

Output representation :

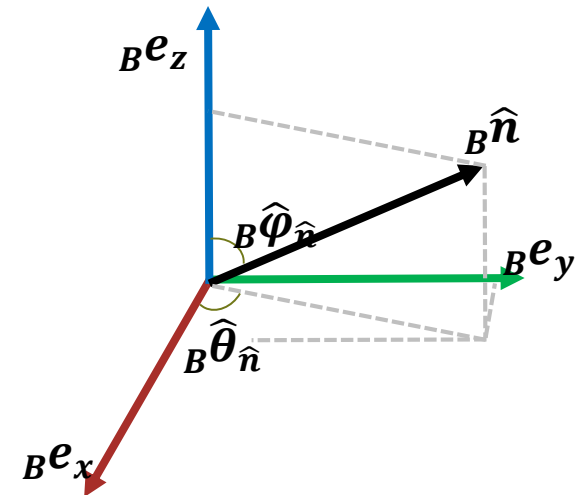
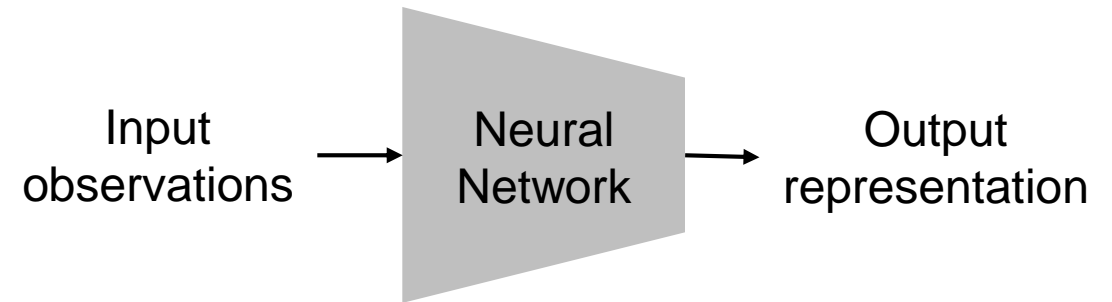
$$\langle \cos {}_B\theta_n, \sin {}_B\theta_n, \cos {}_B\varphi_n, \sin {}_B\varphi_n \rangle \in R^4 [3]$$

Spherical representation of ${}_B\hat{n}$: ${}_B\hat{\varphi}_{\hat{n}}, {}_B\hat{\theta}_{\hat{n}}$

Network architecture:

Size : 128×128×128

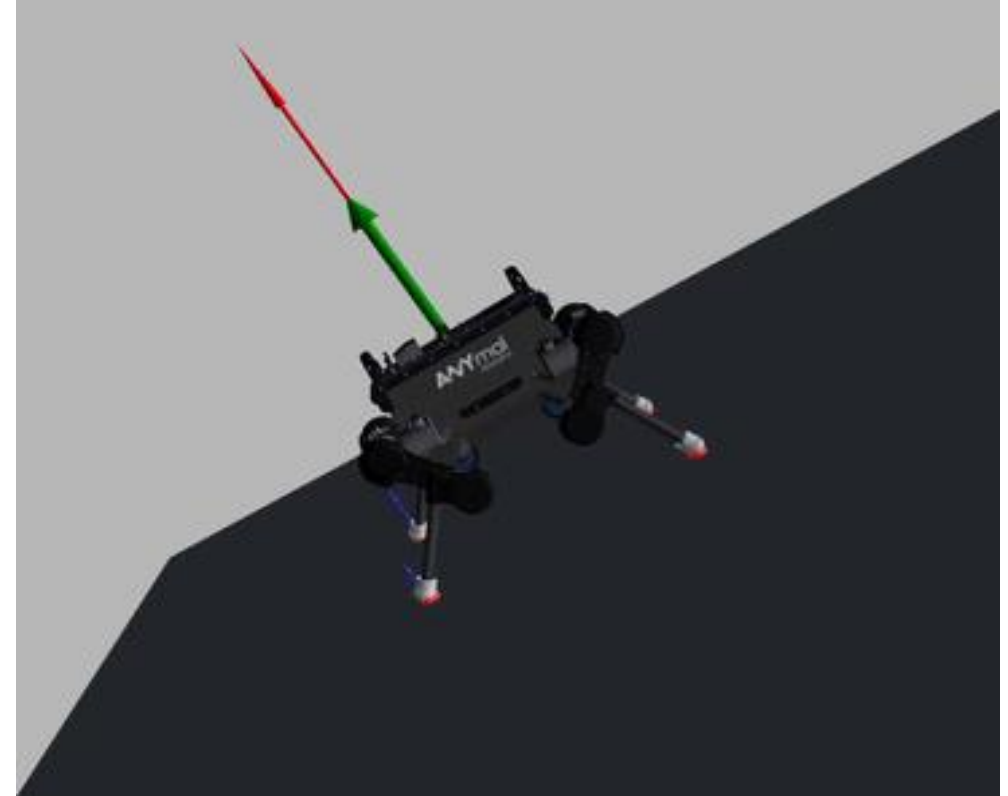
Activation : ReLu



Method: Standing up Controller

Task Objective :

Stand up from near sitting configuration and balance with a stable position.
(on flat and slope(0~36deg) terrains)



Method: Standing up Controller

MDP observation space O_t :

$$\langle e_g, {}_B v_{IB}, {}_B \omega_{IB}, \psi, \dot{\psi}_{t_k}, \dot{\psi}_{t_k - 0.01}, \dot{\psi}_{t_k - 0.02}, a_{k-1} \rangle_{[1,2]}$$

Gravity vector : $e_g \in R^3$

Linear velocity : ${}_B v_{IB} \in R^3$

Angular velocity : ${}_B \omega_{IB} \in R^3$

Joint positions : $\psi \in R^{12}$

Joint velocity history : $\dot{\psi}_{t_k}, \dot{\psi}_{t_k - 0.01}, \dot{\psi}_{t_k - 0.02} \in R^{36}$

Previous action: $a_{k-1} \in R^{12}$

MDP action space a_t :

$$\psi_d = \psi_t + k a_t \quad (k = 0.1), \quad a_t \in R^{12}$$

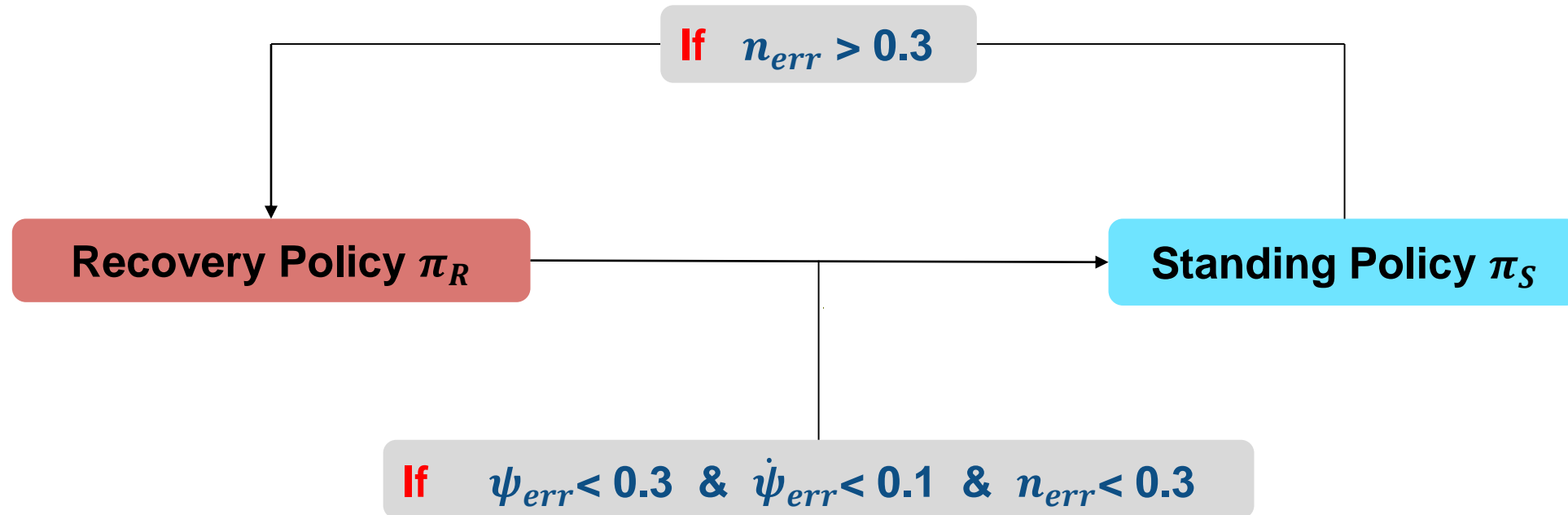
Current joint positions : $\psi_t \in R^{12}$

Desired joint positions : $\psi_d \in R^{12}$

Cost terms :

Joint position, Height, Slip, Orientation, Self collision,
Joint acceleration, Joint velocity, Torque

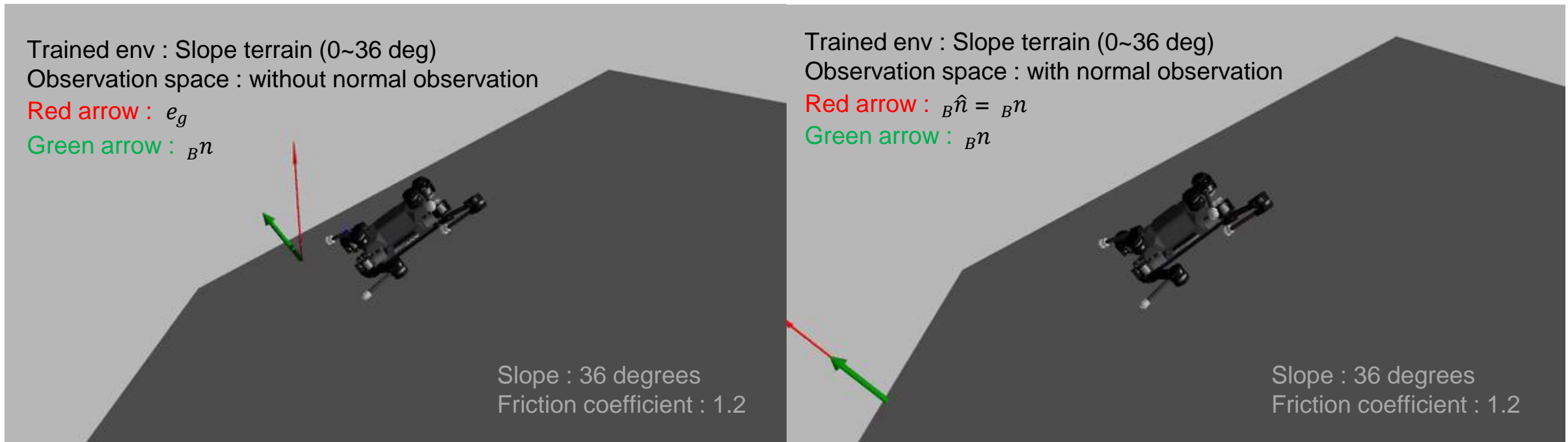
Method: Finite state machine



Results: Recovery Controller simulation results (flat terrain)



Results: Recovery Controller simulation results (slope terrain)



Results: Normal estimator error

1) No history

Input : Gravity vector $e_g \in R^3$, Joint position $\psi \in R^{12}$

Output : $\cos {}_B\theta_n$, $\sin {}_B\theta_n$, $\cos {}_B\varphi_n$, $\sin {}_B\varphi_n$

Hidden layer size : $128 \times 128 \times 128$

Activation : ReLu

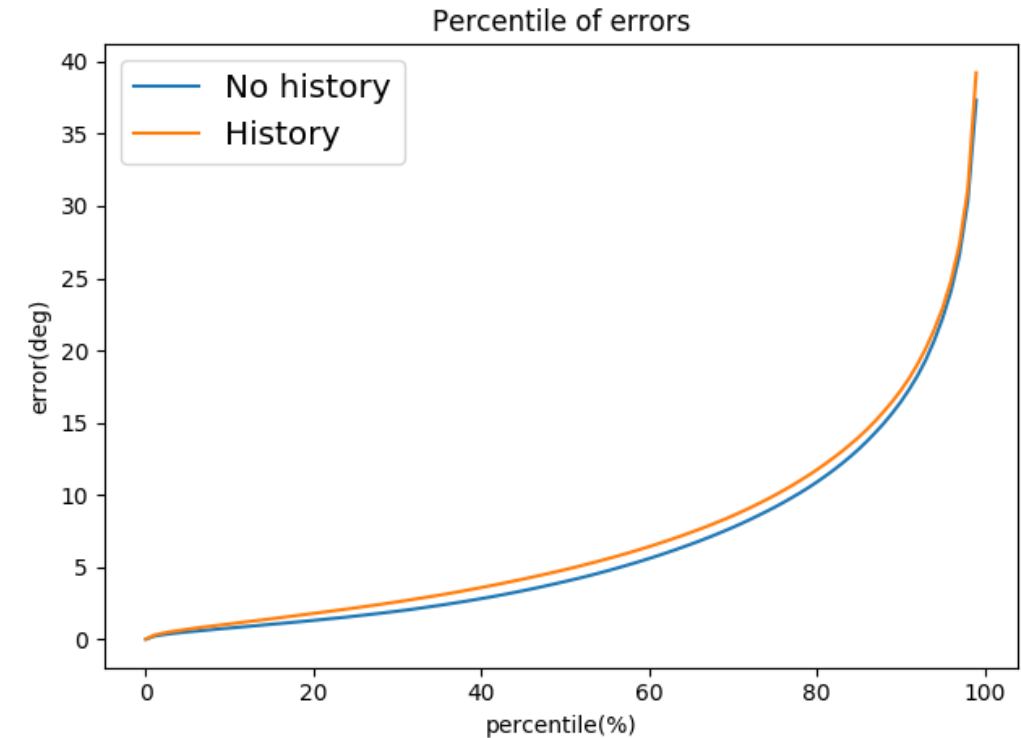
2) History input

Input : $(o_{k-4}, a_{k-4}, o_{k-3}, a_{k-3} \dots, o_k, a_k)$, $o_k = (e_g, \psi)$

Output : $\cos {}_B\theta_n$, $\sin {}_B\theta_n$, $\cos {}_B\varphi_n$, $\sin {}_B\varphi_n$

Hidden layer size : $128 \times 128 \times 128$

Activation : ReLu



	Mean(deg)	Std(deg)
No history	6.806	8.17
History input	7.544	8.69

Table 1. Model validation L1 loss (1600000 time steps)

Results: Policy comparison

		Observation		
		No normal	Normal(truth)	Normal(estimate)
Env	flat_without_normal (fwn)	Train(flat)/Test(slope)		
	slope_without_normal (swn)	Train(slope)/Test(slope)		
	slope_normal(Explicit) (snE)		Train(slope)/Test(slope)	
	slope_normal_Predicted (snP)		Train(slope)	Test(slope)
	slope_normal(Implicit) (snI)	Test(slope)	Train(slope)	

Table 2. Policies trained with different observations

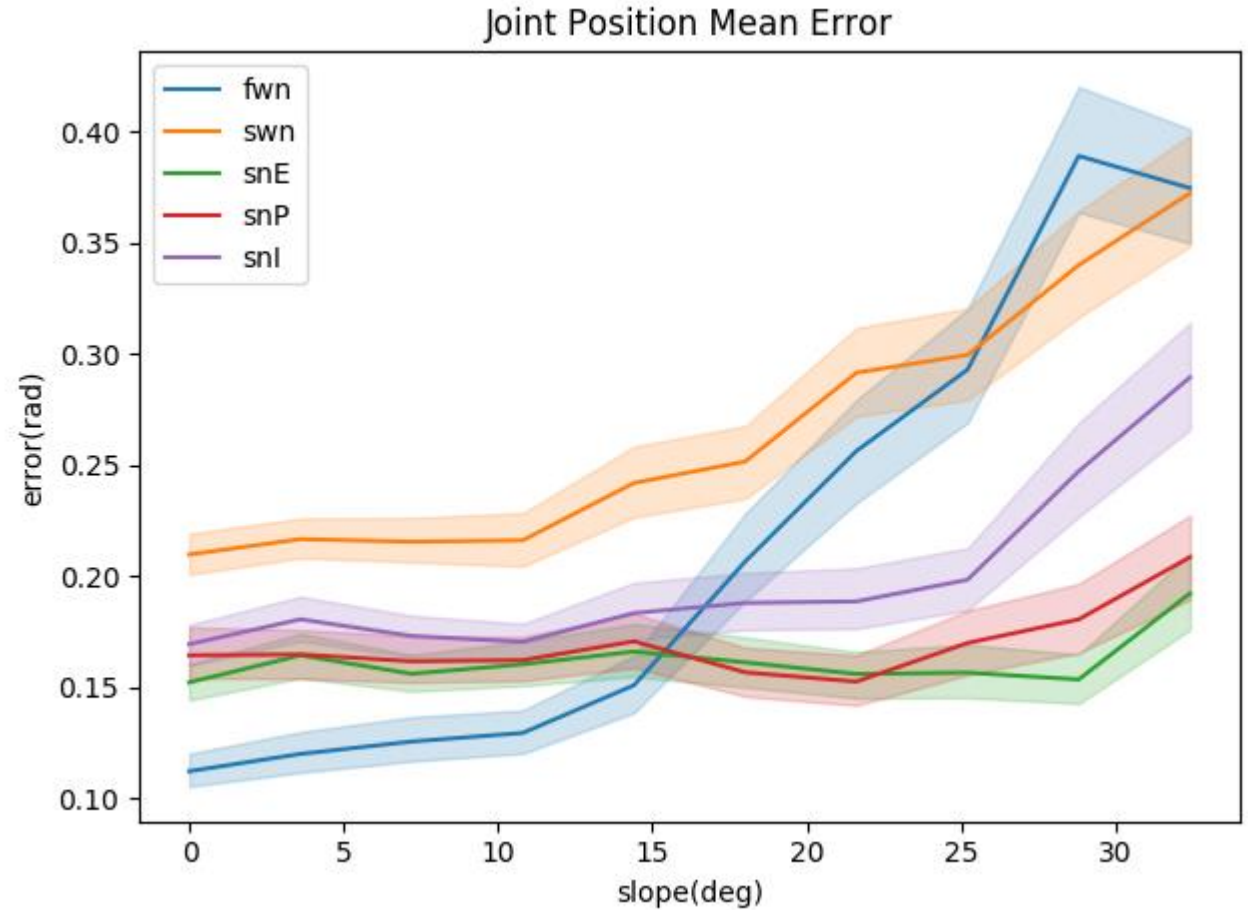
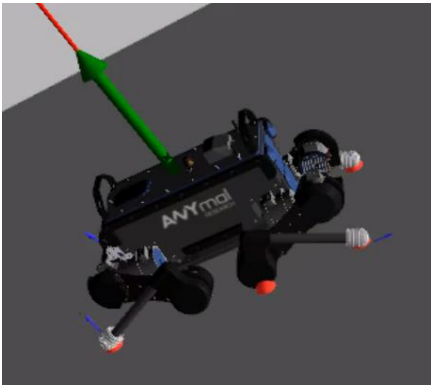
Results: Joint position error

1000 test episodes per slope (0, 6, 12, ..., 36deg)

Last time step observation : Joint positions $\psi \in R^{12}$

Desired position (sit) : $\psi_{des} \in R^{12}$

Joint position error : $|\psi_{des} - \psi|$

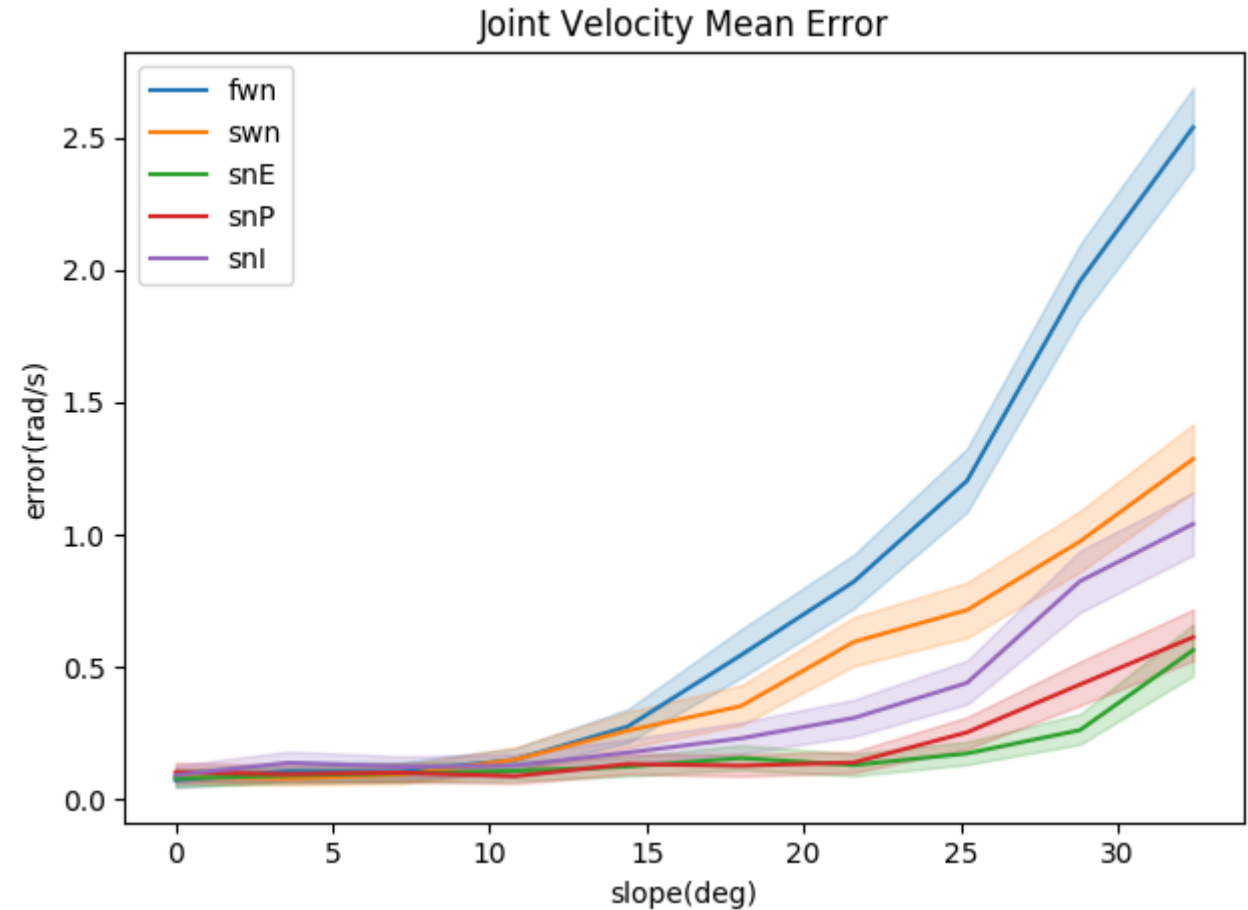


Results: Joint velocity error

Last time step observation : Joint velocities $\dot{\psi} \in R^1$

Desired velocity : $\psi_{des} \in R^{12}$, $\dot{\psi}_{des} = 0$

Joint velocity error : $|\dot{\psi}_{des} - \dot{\psi}|$

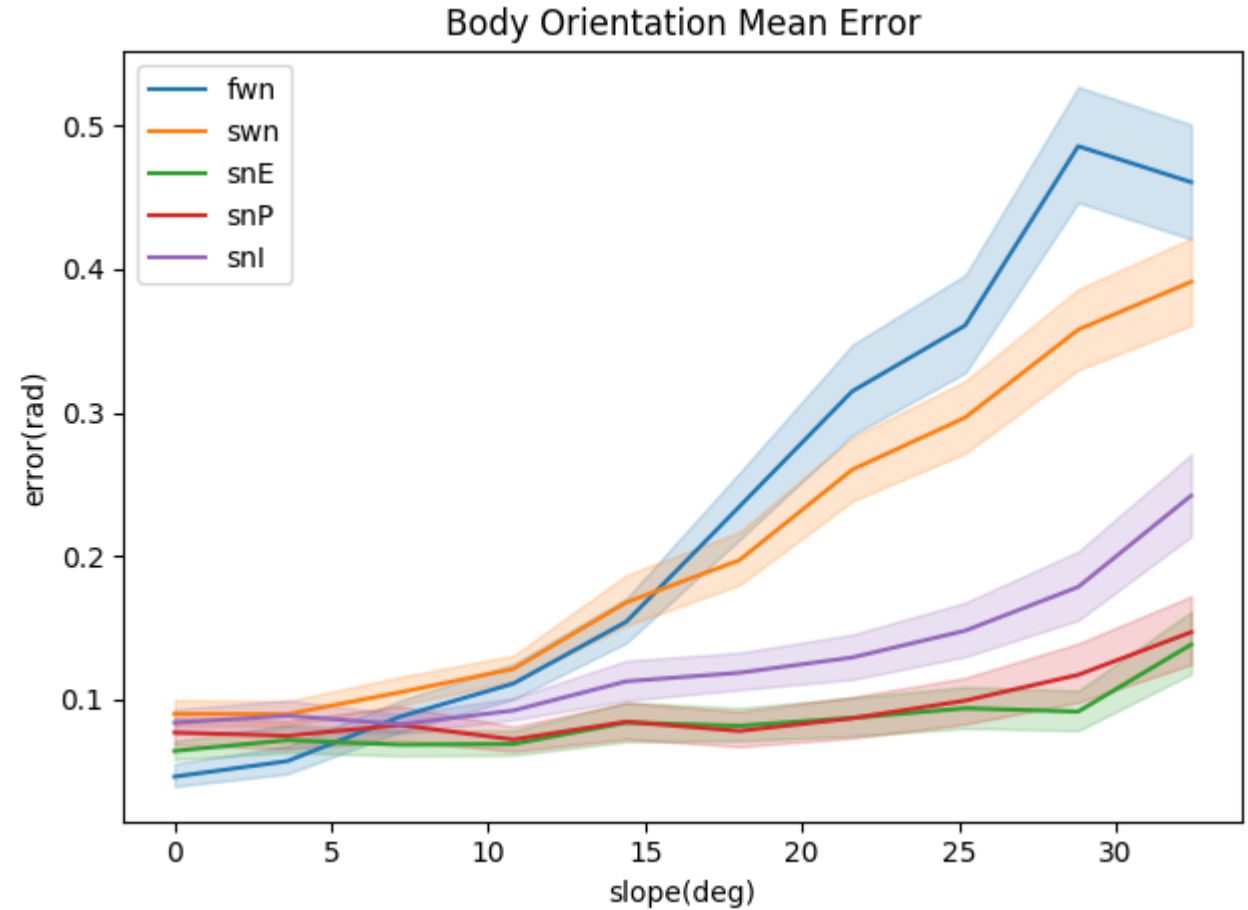
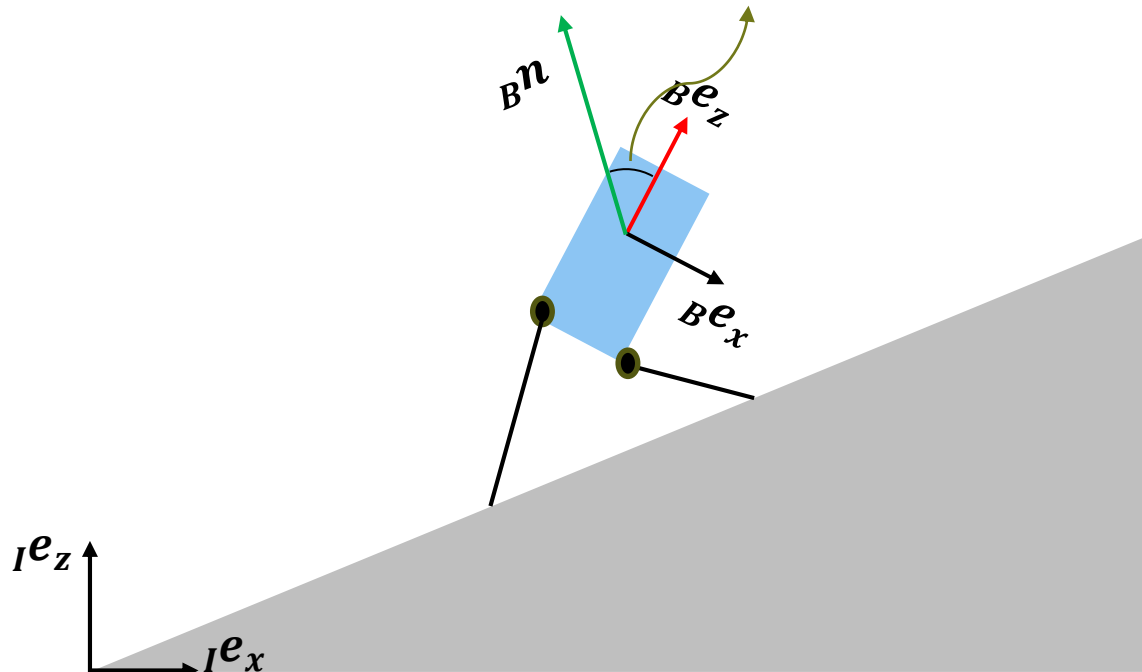


Results: Body orientation error

Last time step observation : Base z axis ${}_B e_z \in R^3$

Desired orientation : ${}_B e_{des} = {}_B n$

Body orientation error : $\cos^{-1}({}_B n \cdot {}_B e_z)$



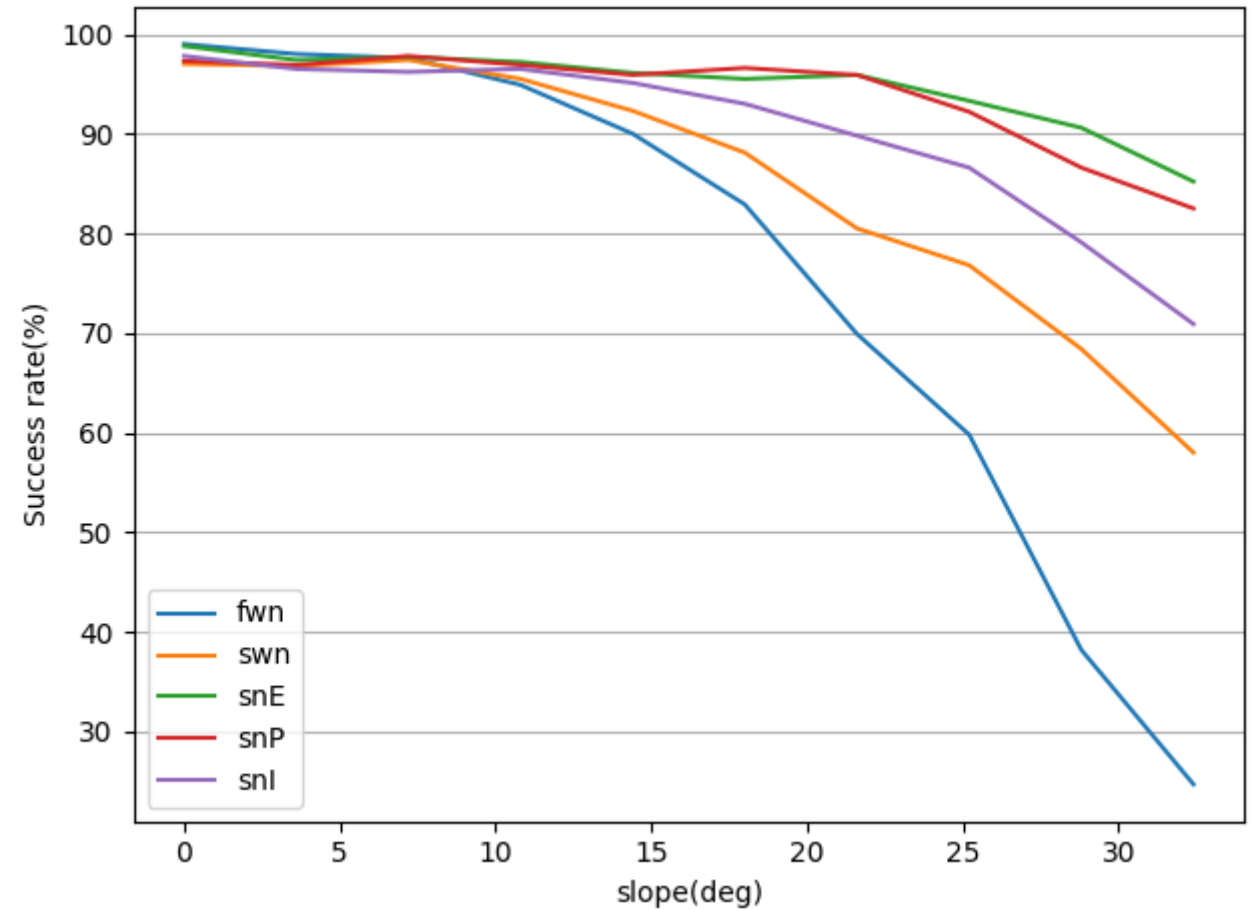
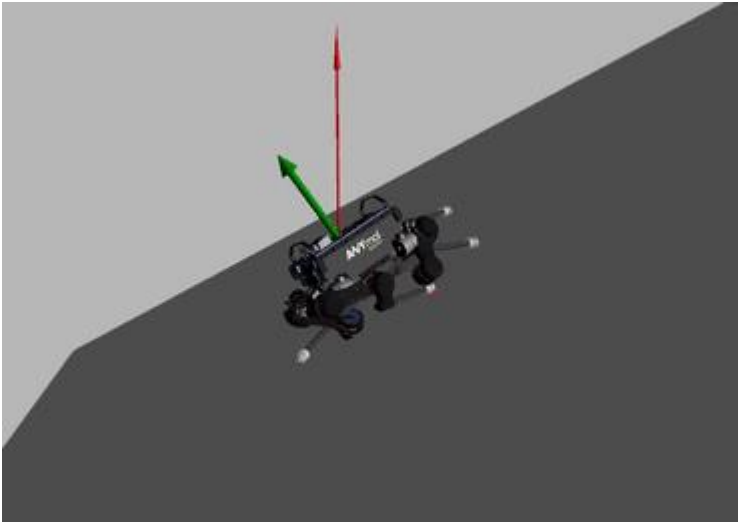
Results: Success rate

Success definition :

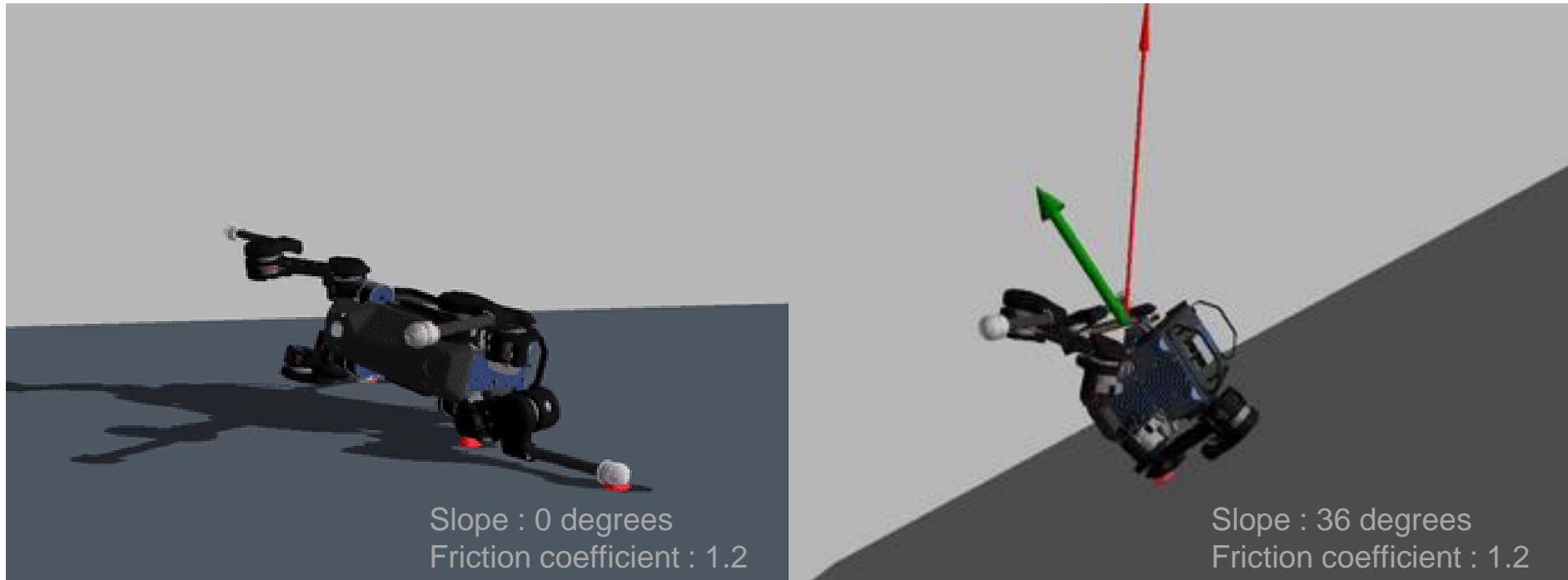
Joint position error $< 0.5(\text{rad})$

Joint velocity error $< 0.1(\text{rad/s})$

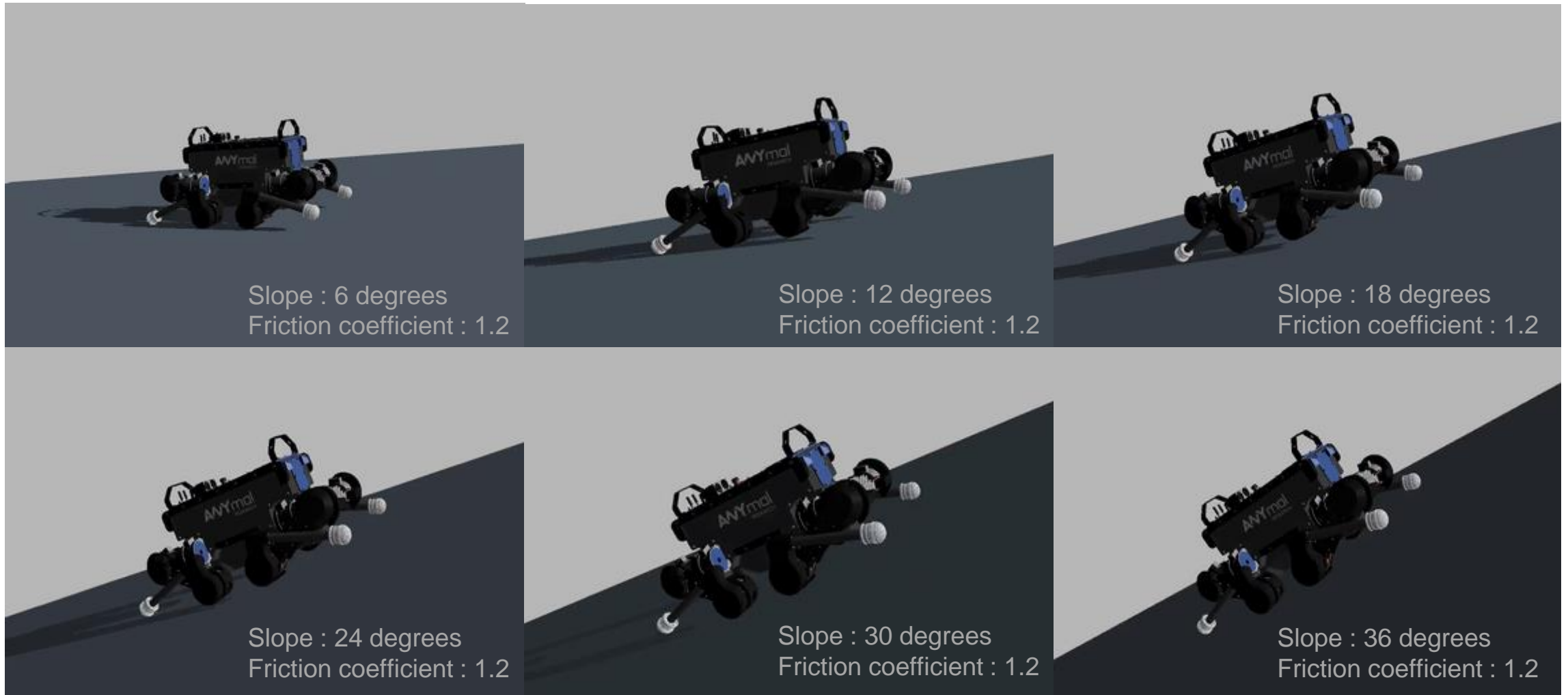
Body orientation error $< 1.0(\text{rad})$



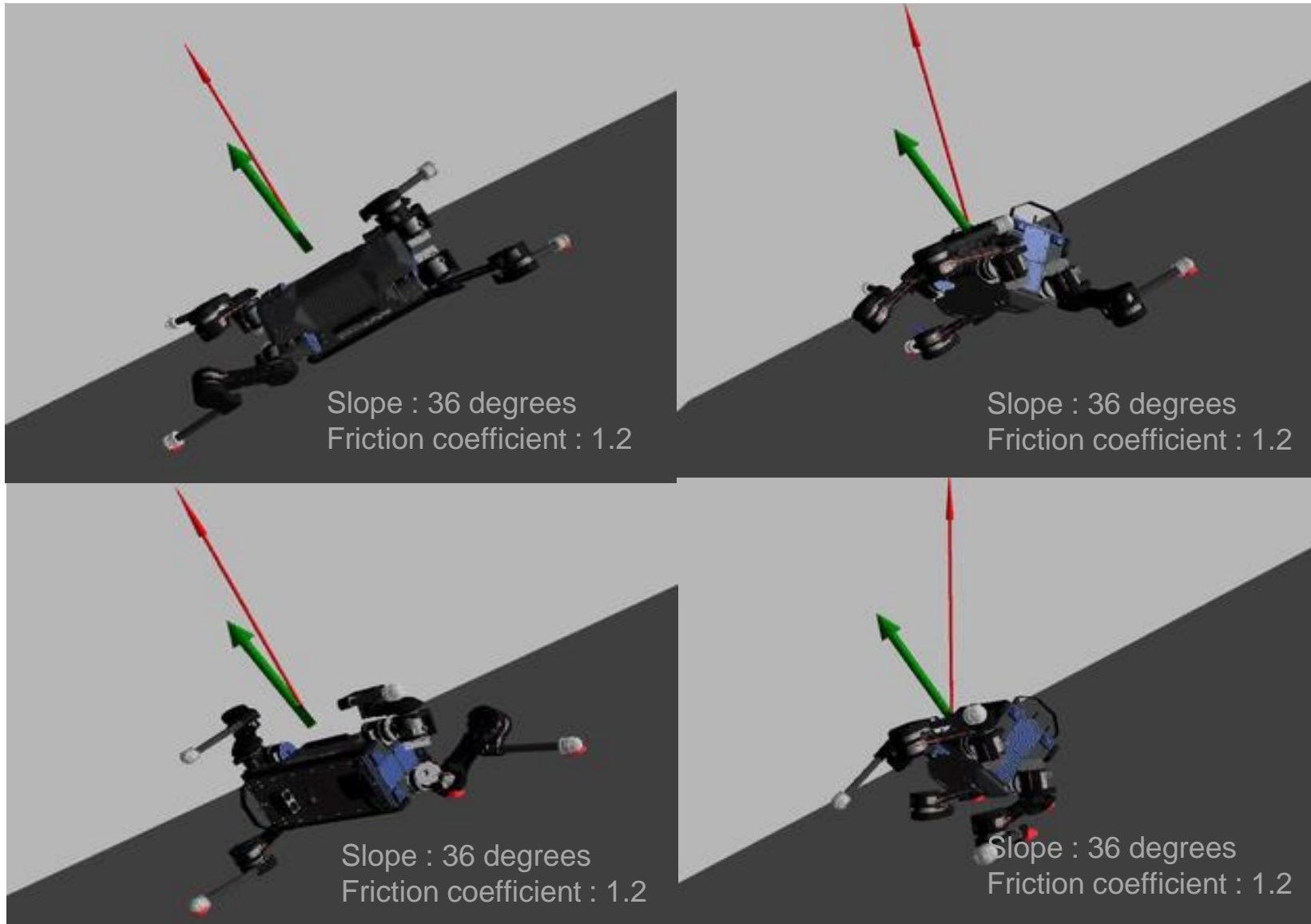
Results: Different behaviors on slope



Results: Standing up Controller simulation results



Results: Finite state machine simulation results



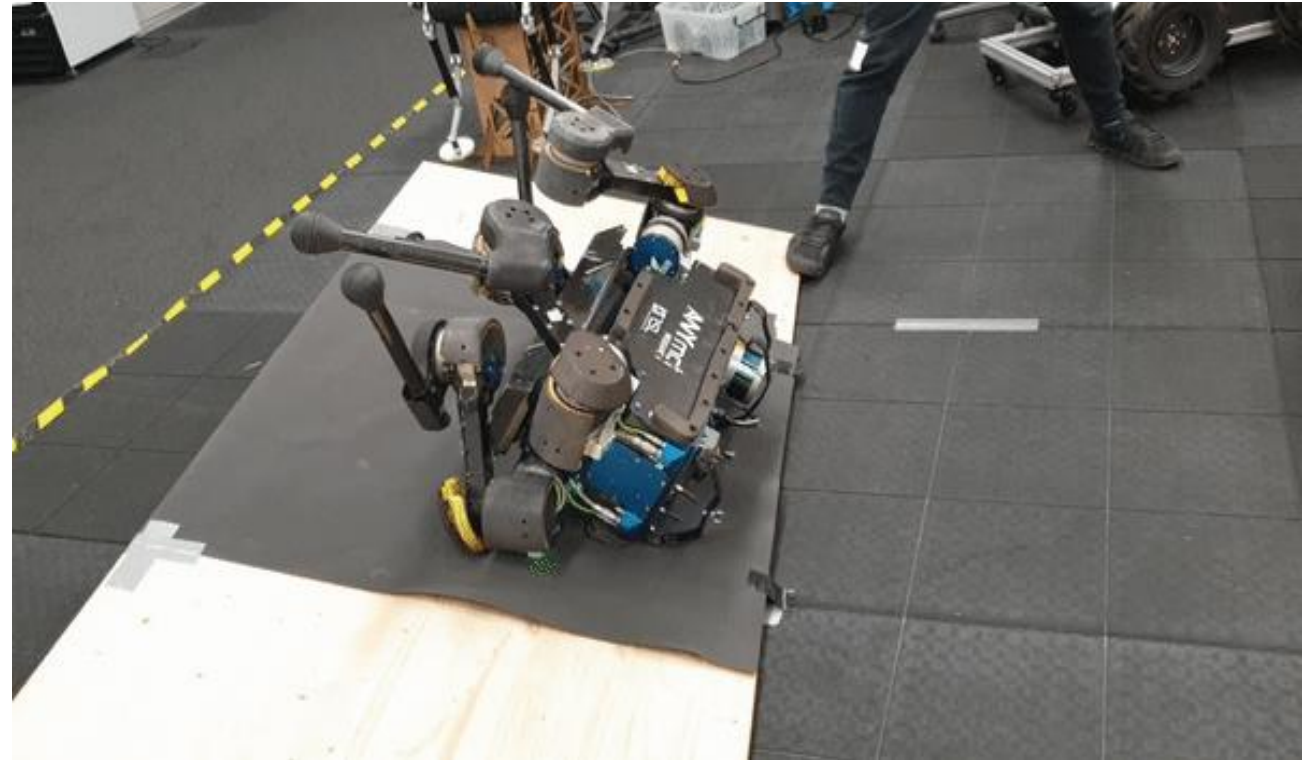
Results: Real-world experiments(flat terrain)



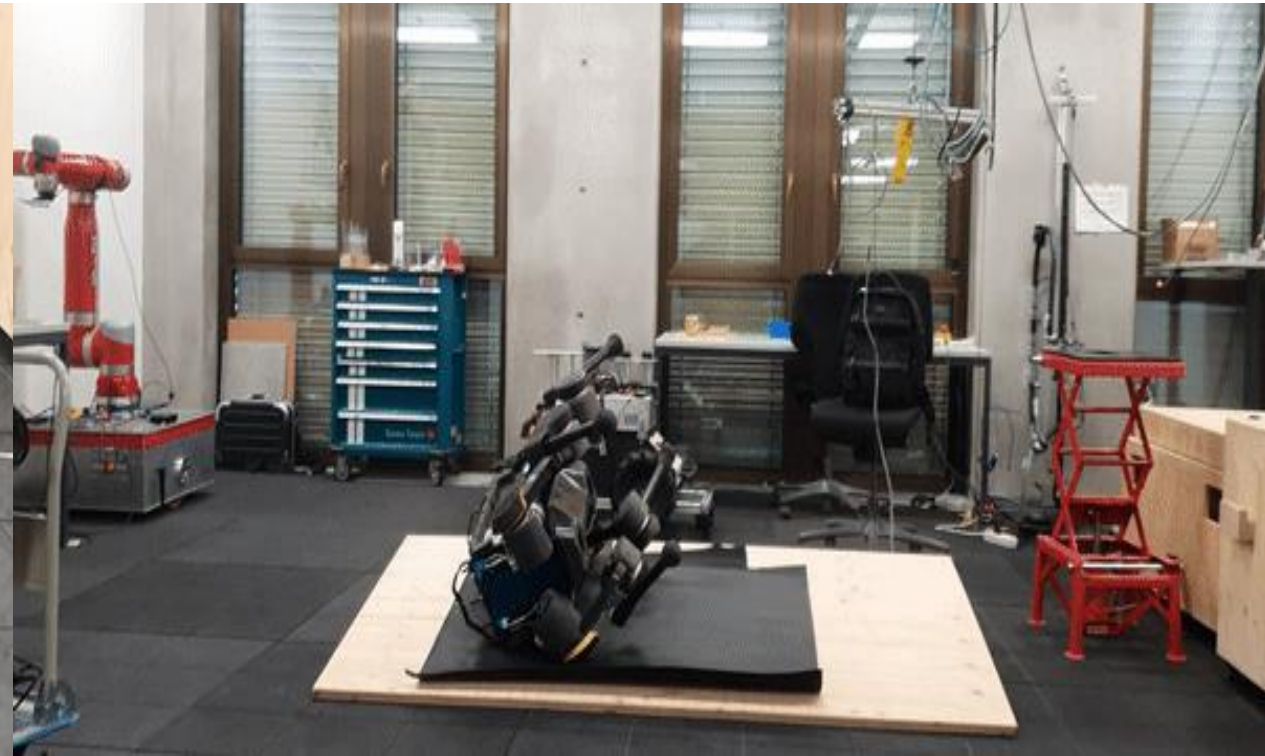
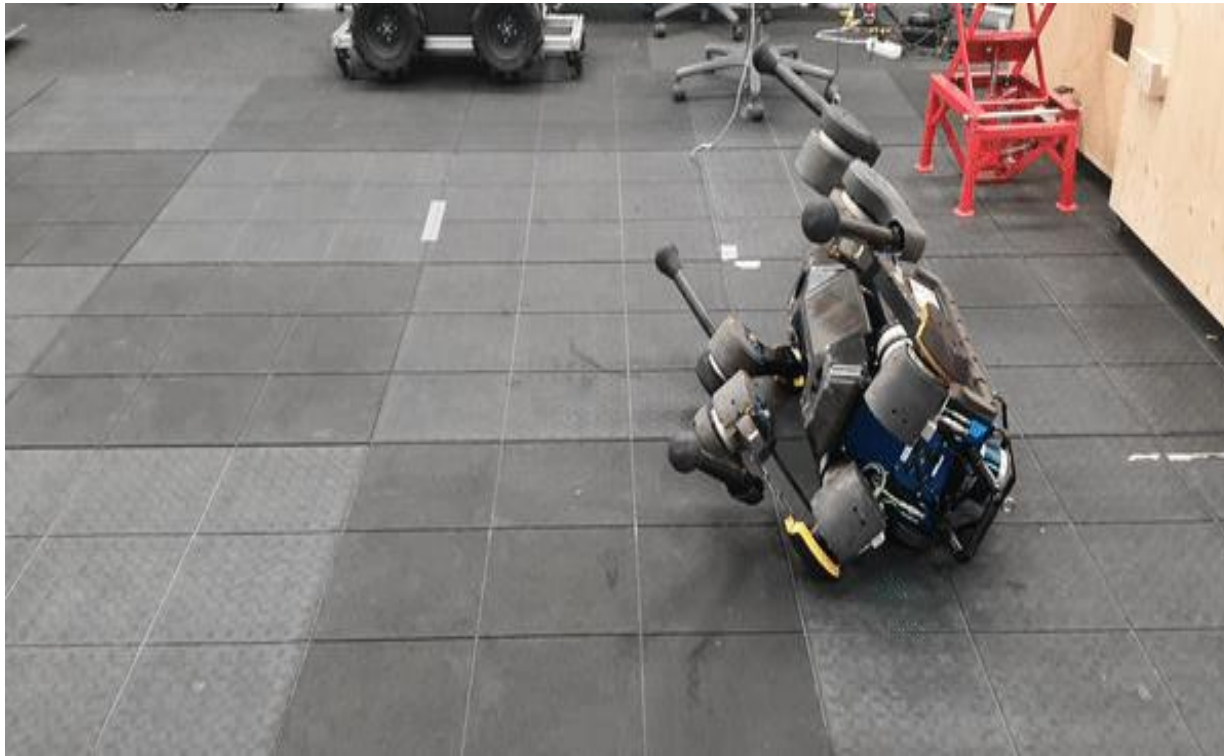
Results: Real-world experiments(slope terrain)

Problem : Linear velocity, Height drift
State drift leads to abnormal behaviors

Solution : Exclude states that have drift issues



Results: Real-world experiments(finite state machine)



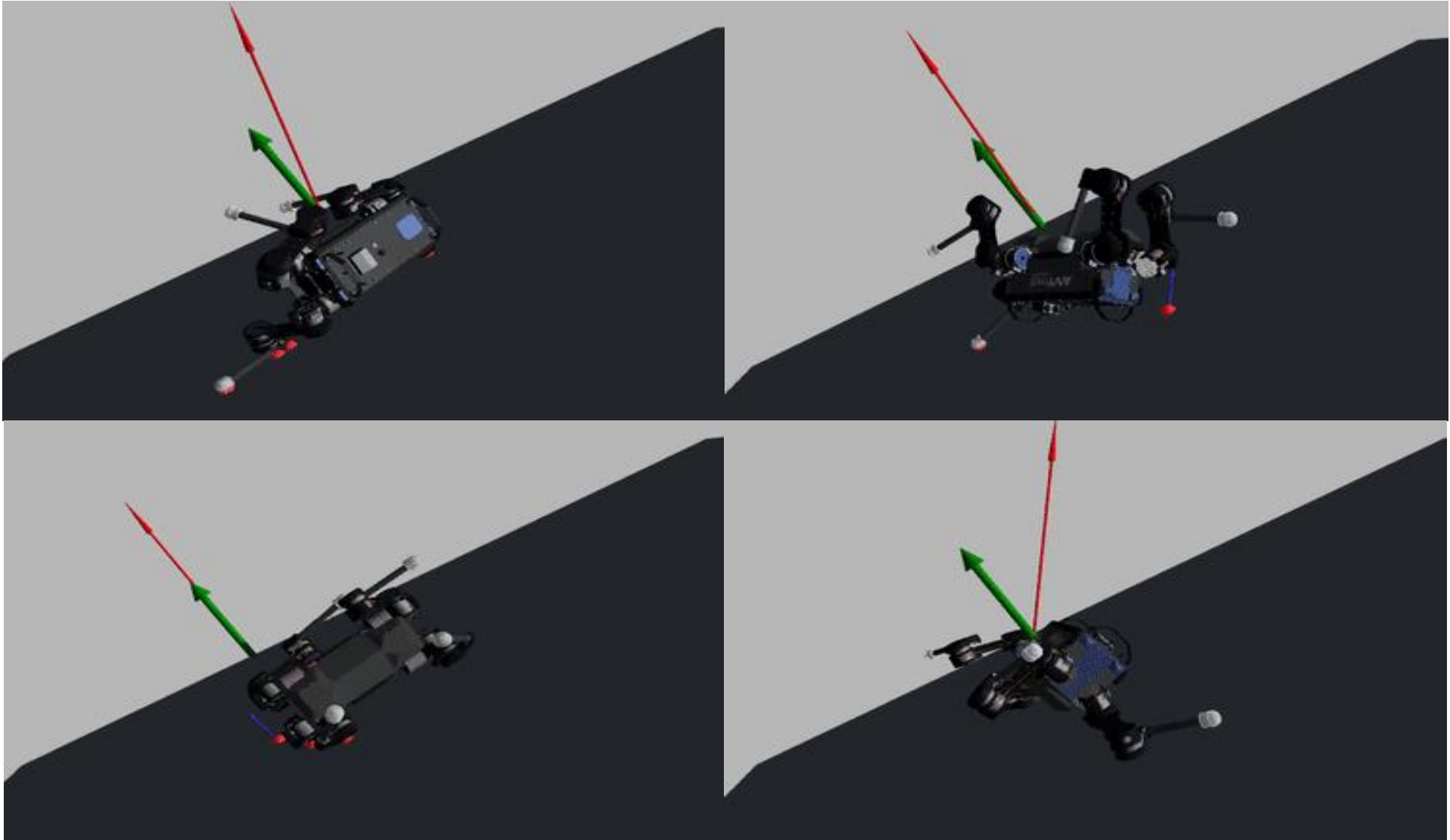
Results: Real-world experiments(finite state machine)

Problem : Normal estimation noise
Policy trained only with ground truth normal

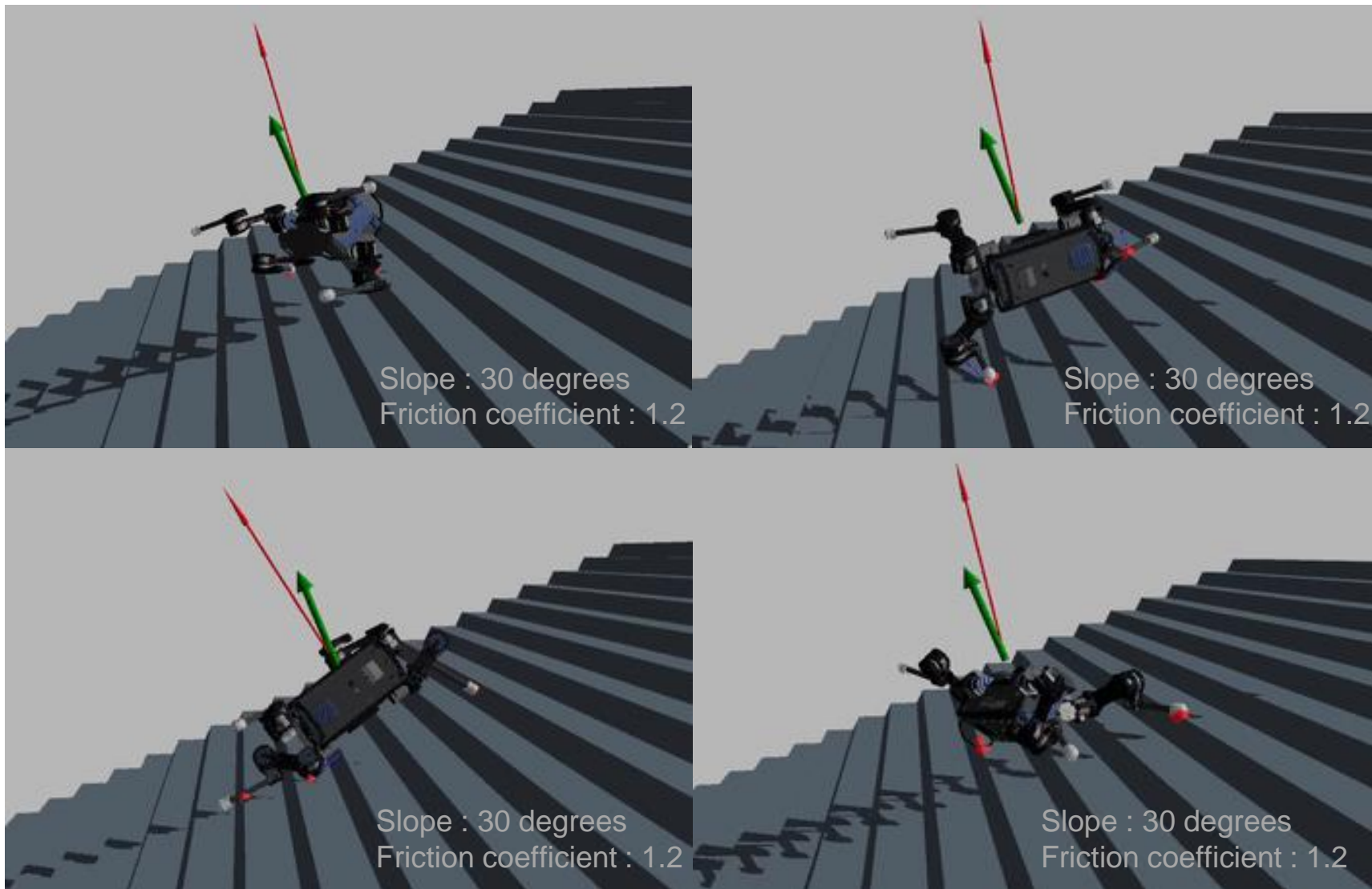
Solution : Train policy with normal estimator

		Observation		
		No normal	Normal(truth)	Normal(estimate)
Env	Train(slope)			✓
	Test(slope)			✓

Results: Simulation results(trained with estimator)



Thank you

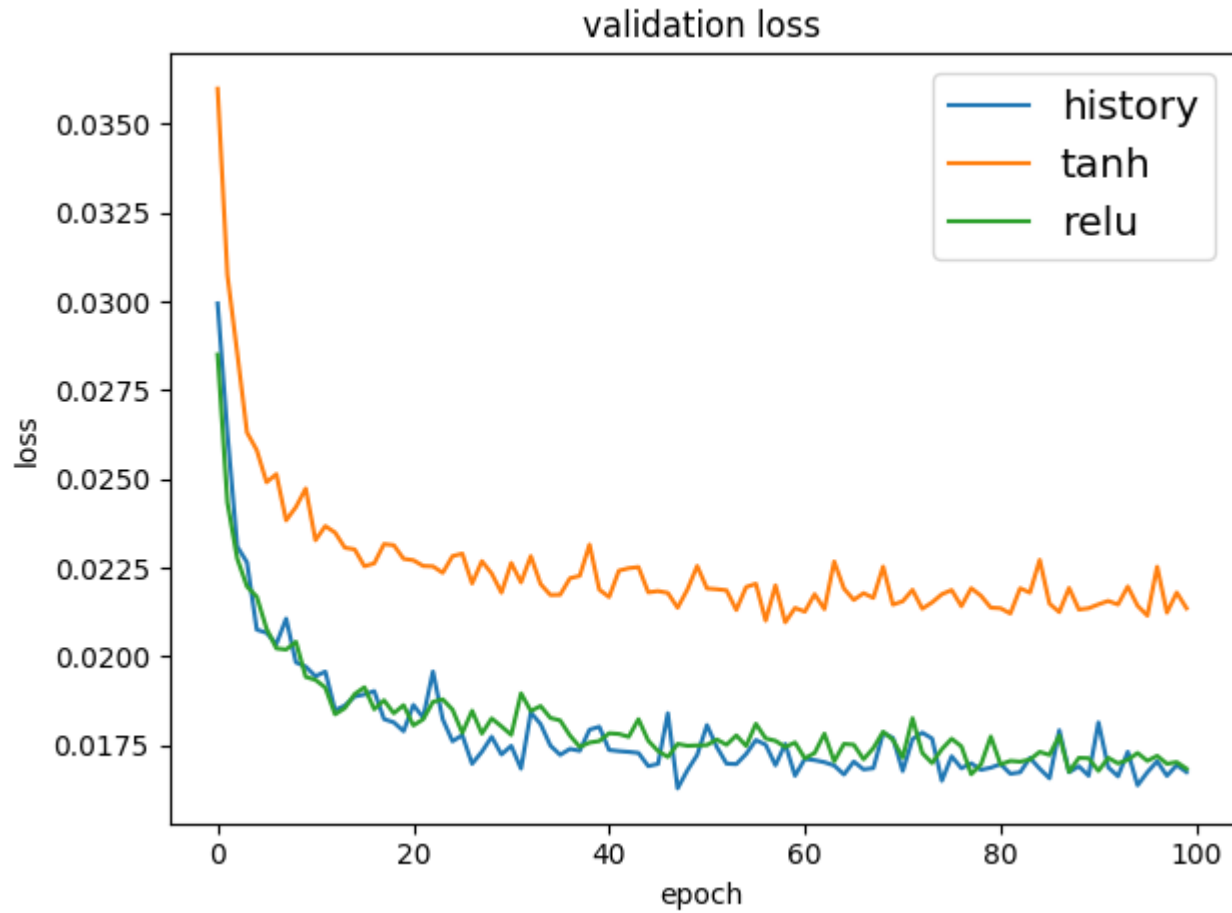


References

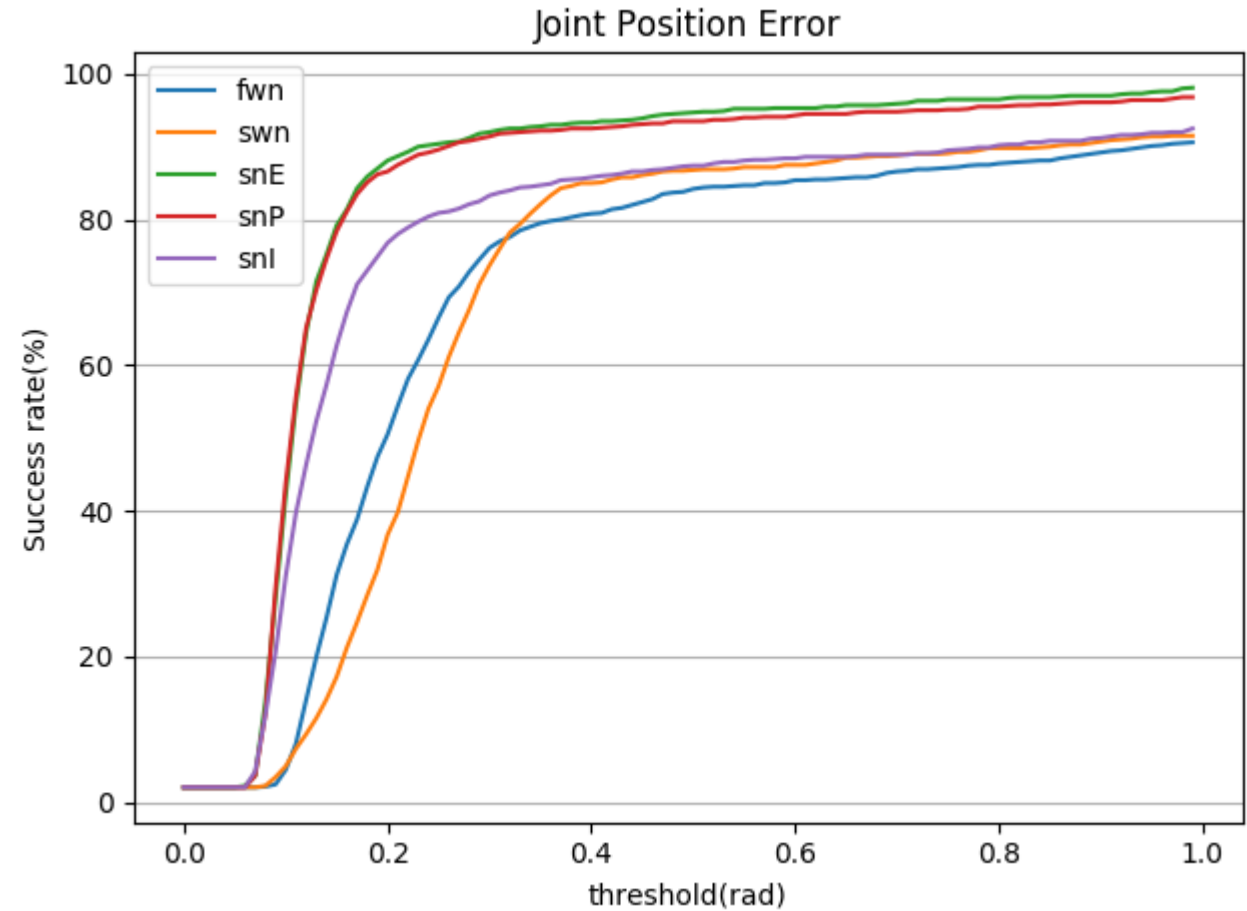
1. J. Lee, J. Hwangbo, and M. Hutter, “Robust recovery controller for a quadrupedal robot using deep reinforcement learning,” arXiv preprint arXiv:1901.07517, 2019.
2. Hwangbo, Jemin et al. “Learning Agile and Dynamic Motor Skills for Legged Robots.” Science Robotics 4.26 (2019)
3. Yi Zhou, Connelly Barnes, Jingwan Lu, Jimei Yang, and Hao Li. On the continuity of rotation representations in neural networks. arXiv preprint arXiv:1812.07035, 2018.

Q&A

appendix

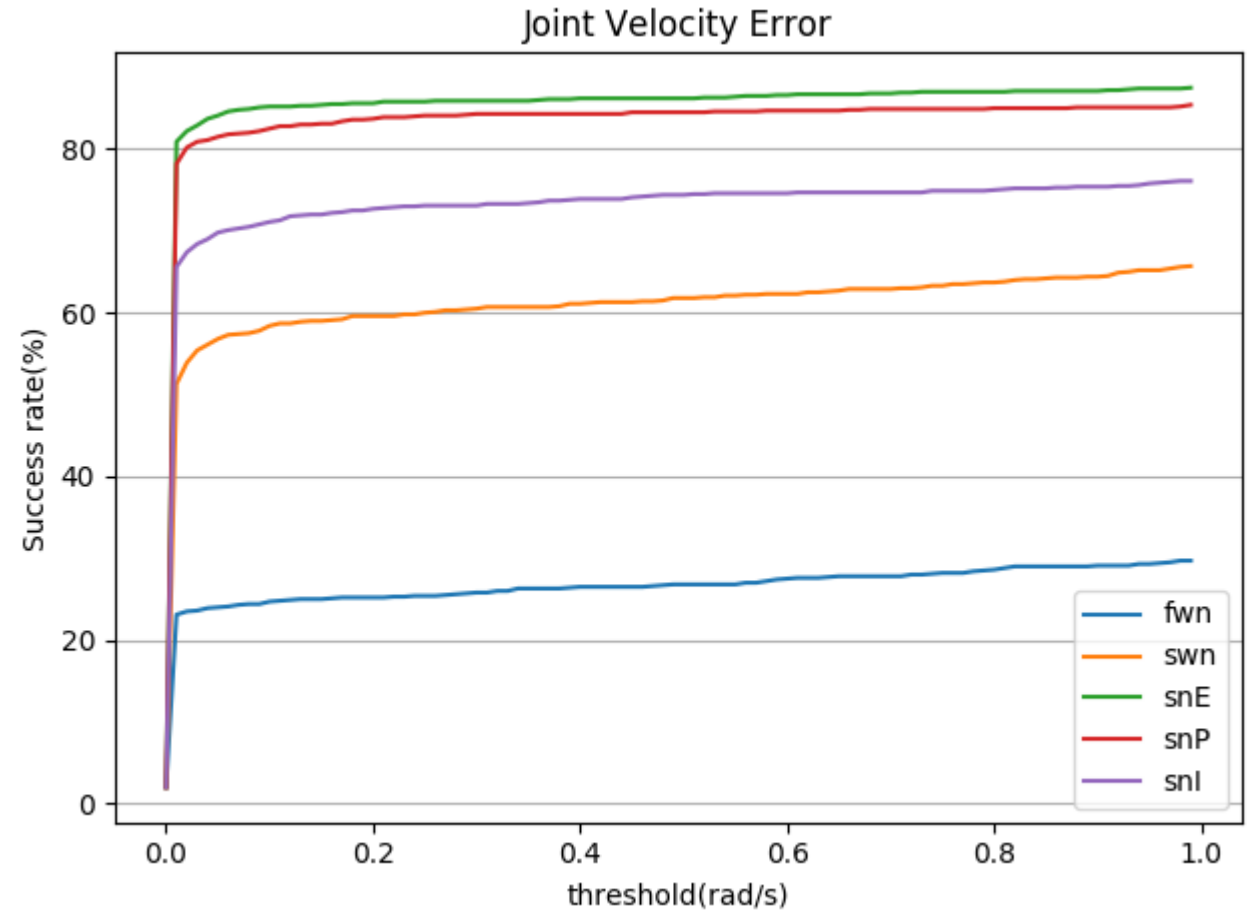


appendix

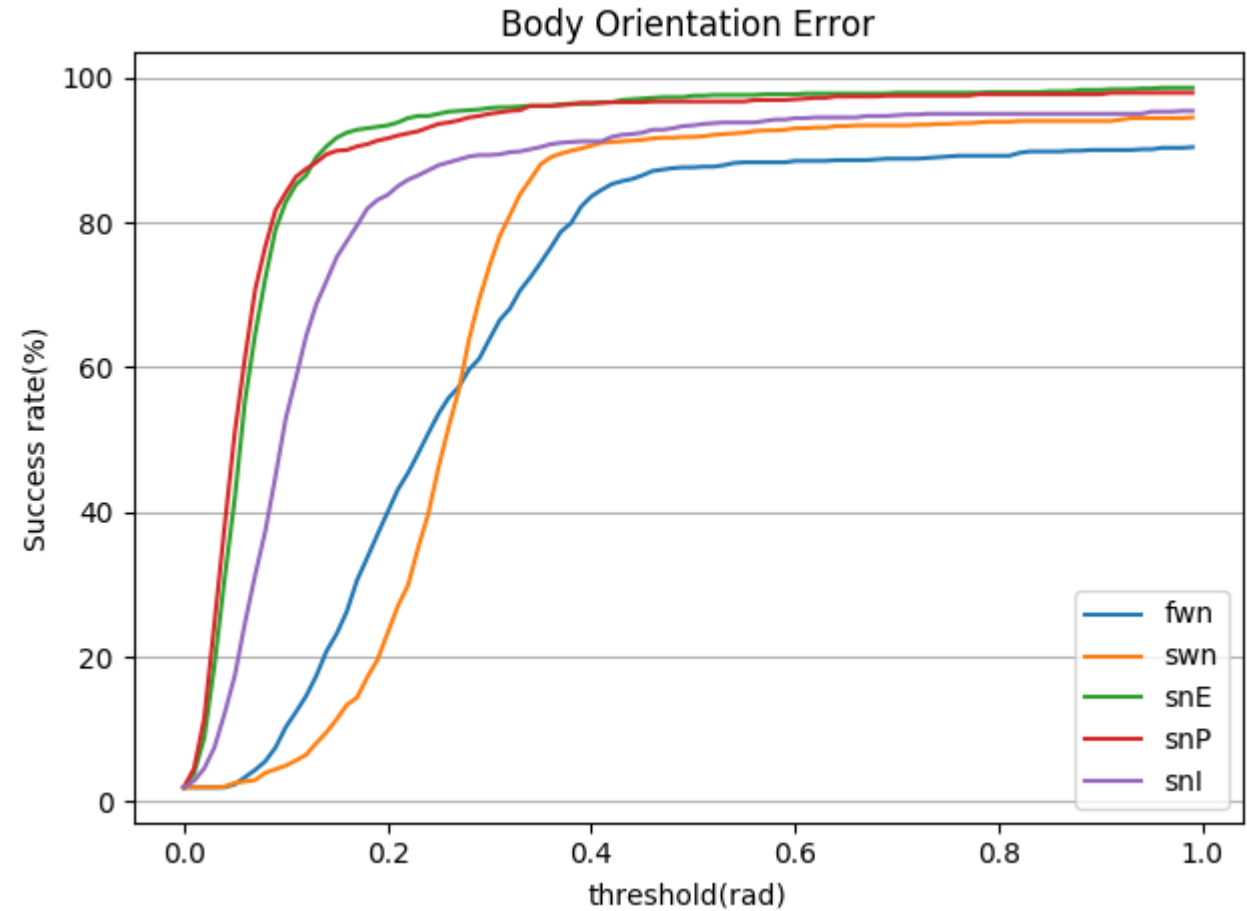


Slope : 36 degrees

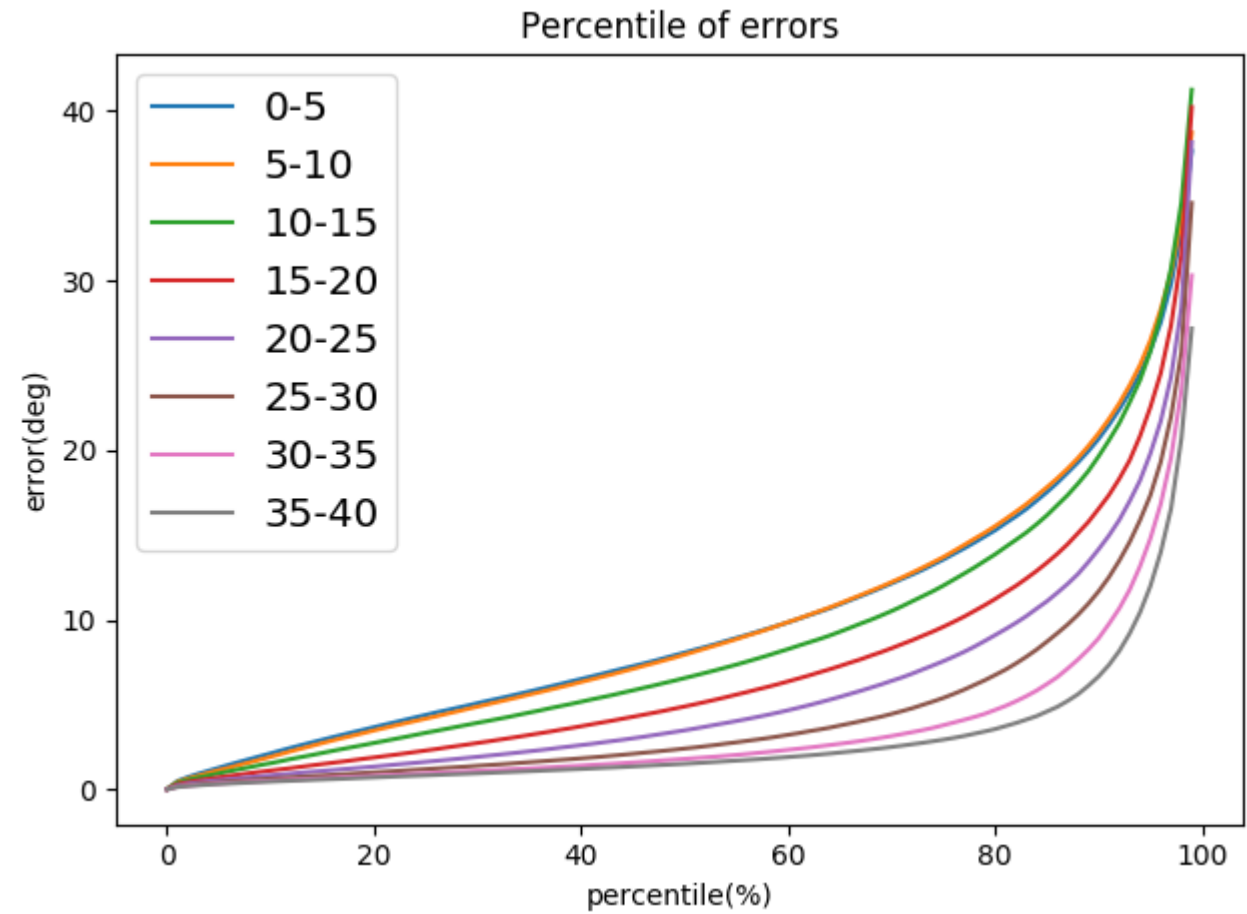
appendix



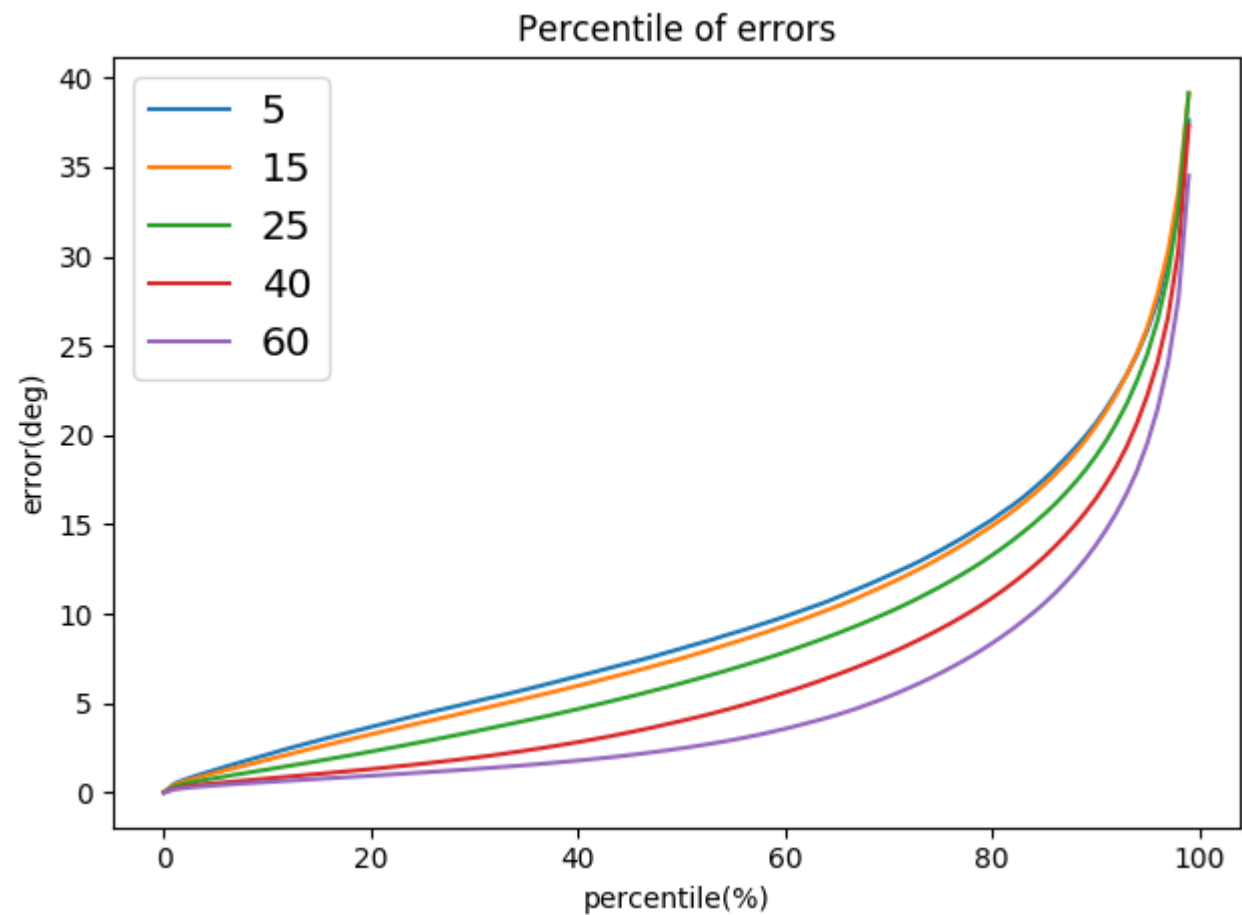
appendix



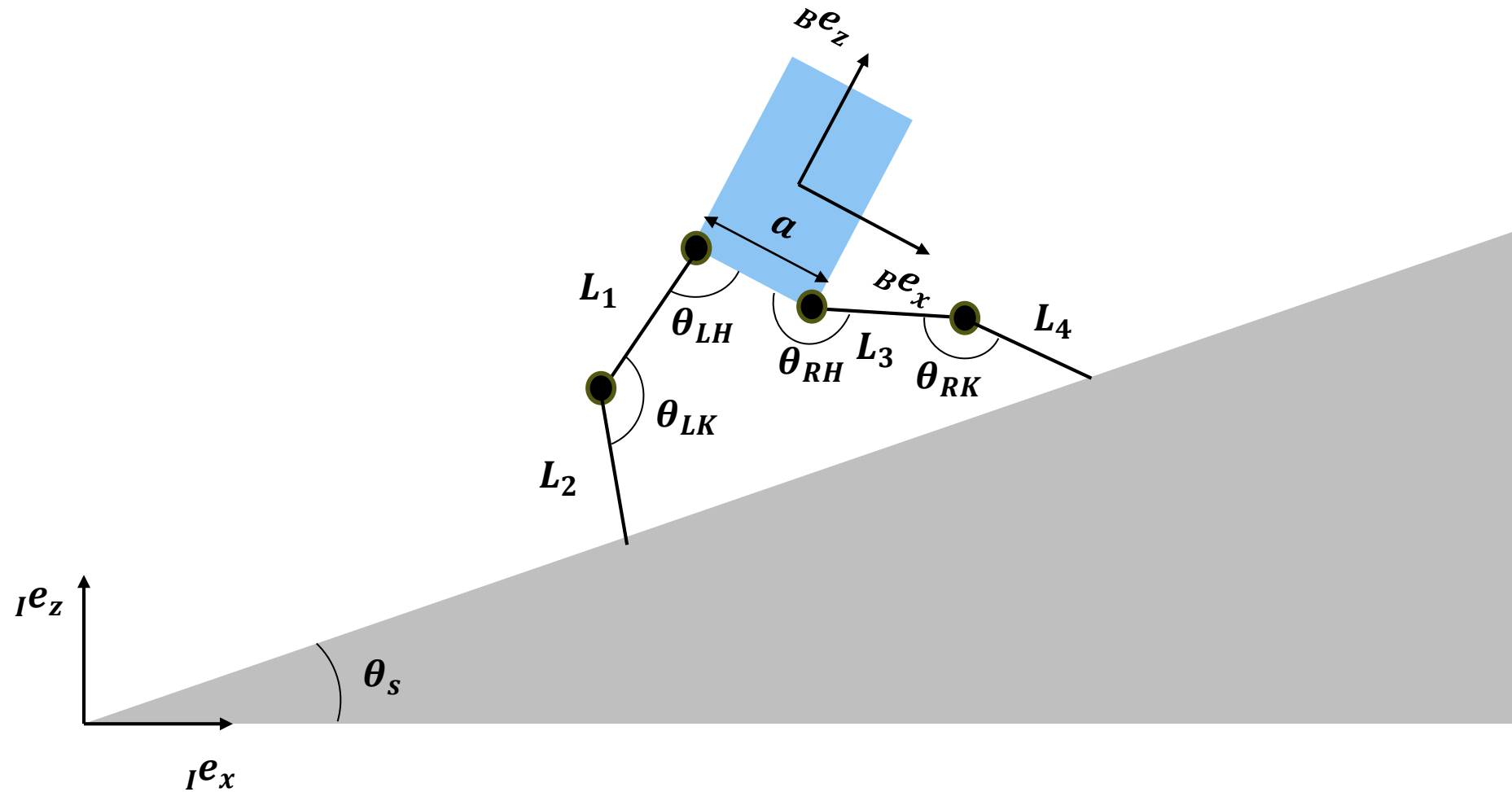
appendix



appendix



Normal estimation



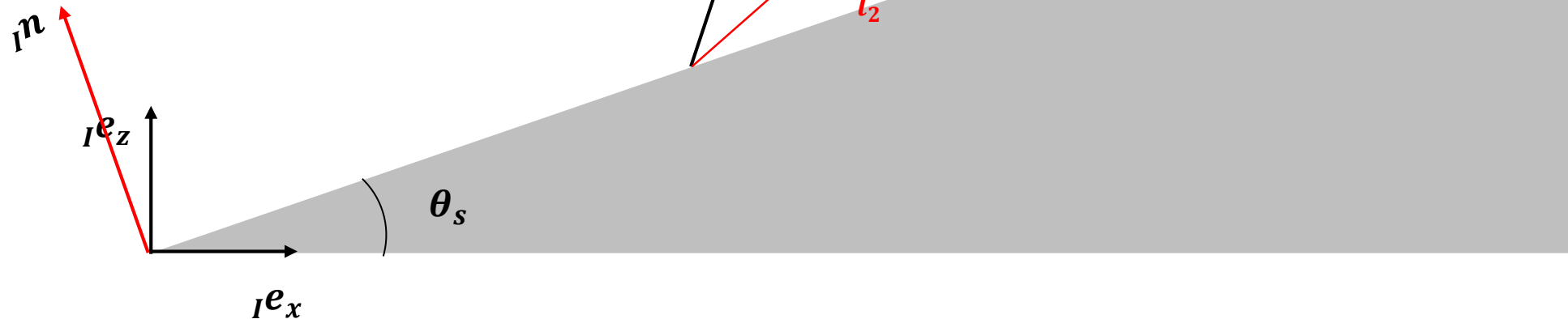
Normal estimation

$$l_1^2 = L_1^2 + a^2 - 2aL_1 \cos\theta_{LH}$$

$$\sin\beta = \frac{L_1 \sin\theta_{LH}}{l_1}$$

$$l_2^2 = L_2^2 + l_1^2 - 2L_2 l_1 \cos(\theta_{RH} - \beta)$$

$$\sin\alpha = \frac{l_1 \sin(\theta_{RH} - \beta)}{l_2}$$

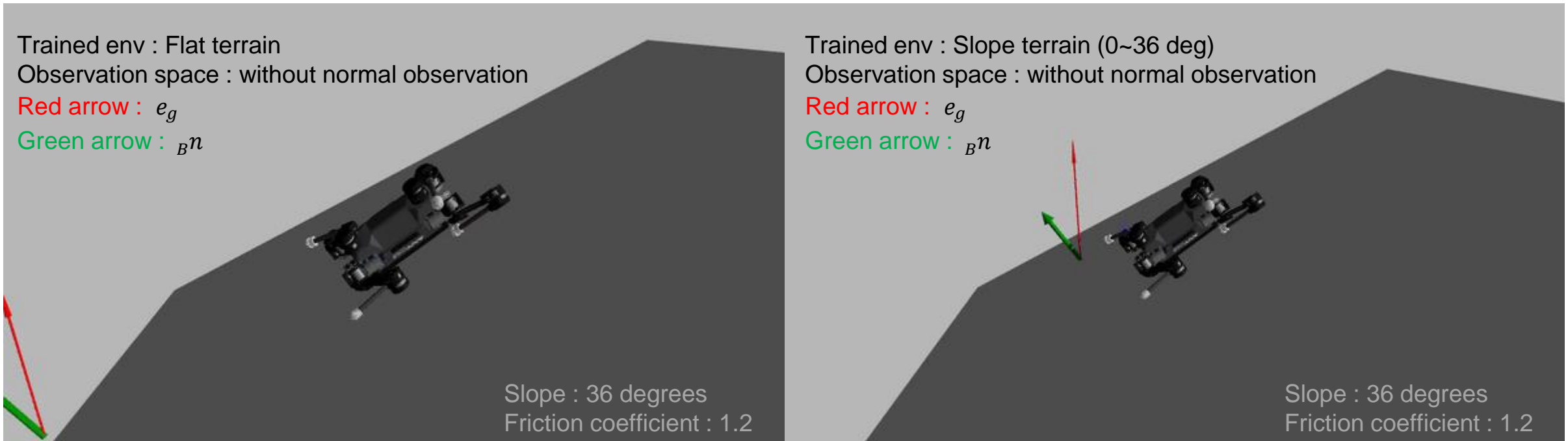


$$\theta_{slope} = \alpha + \theta_{RH} - \theta_g - \frac{\pi}{4}$$

$${}_B n = C_{BI} {}_I n = \begin{pmatrix} \cos\theta_g & -\sin\theta_g \\ \sin\theta_g & \cos\theta_g \end{pmatrix} {}_I n$$

$${}_B n = (-\cos\theta_g \sin\theta_s - \sin\theta_g \cos\theta_s, -\sin\theta_g \sin\theta_s + \cos\theta_g \cos\theta_s)^T$$

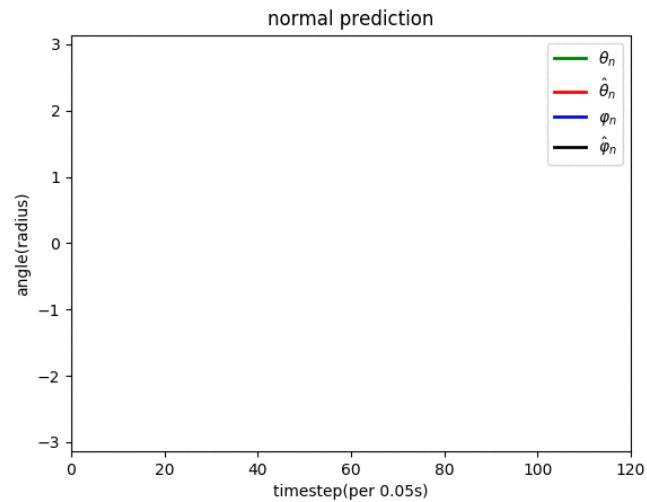
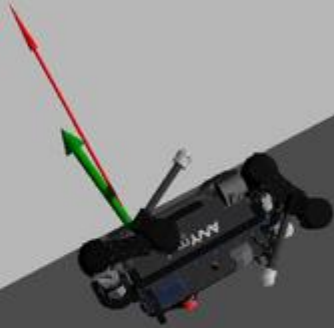
Policy without normal observation



Estimation error comparison

Estimator Output : ${}_B\hat{\varphi}_{\hat{n}}$, ${}_B\hat{\theta}_{\hat{n}}$

Slope : 36 degrees



Estimator Output : $\cos {}_B\hat{\varphi}_{\hat{n}}$, $\sin {}_B\hat{\varphi}_{\hat{n}}$, $\cos {}_B\hat{\theta}_{\hat{n}}$, $\sin {}_B\hat{\theta}_{\hat{n}}$

Slope : 36 degrees

