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Hyperparameter Optimization Methods for the H-SPPBO Metaheuristic

Applied to the Dynamic Traveling Salesperson Problem

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2. Theoretical Background
3. Implementation
4. Experimental Design
5. Results
6. Conclusion
7. Demo

1. Motivation, Problem, Approach

WHY, WHAT AND HOW?

MOTIVATION

- **Combinatorial problems** everywhere:
 - Transporting, logistics, digital traffic routing
 - Complex problems (NP-hard) need metaheuristics
- No free lunch theorem → No single metaheuristic is the best for all problems
- **Metaheuristic Frameworks:** Streamlining algorithm design
 - Simple Probabilistic Population-Based Optimization (SPPBO)
 - Adaptable to many problems through parameters

MOTIVATION



?

PROBLEM

- **Problem 1:** Feature- and parameter-rich metaheuristic frameworks
 - Not feasibly tuned by hand
 - Only **optimal parameters** yield **optimal solutions**
- **Problem 2:**
Real world rarely static, **dynamic problems needed**
 - TSP → DTSP

APPROACH

- **Solution 1:** Hyperparameter Optimization (HPO)
 - Methods from **Machine Learning**
 - Applied to Parameter Tuning of Metaheuristics
- **Solution 2:** Hierarchical Simple Probabilistic Population-Based Optimization
 - Designed using SPPBO and H-PSO
 - Solution construction using **tree hierarchy**
 - Solves the DTSP and **detects change**

RESEARCH QUESTIONS

What is the ideal HPO method for the H-SPPBO algorithm?



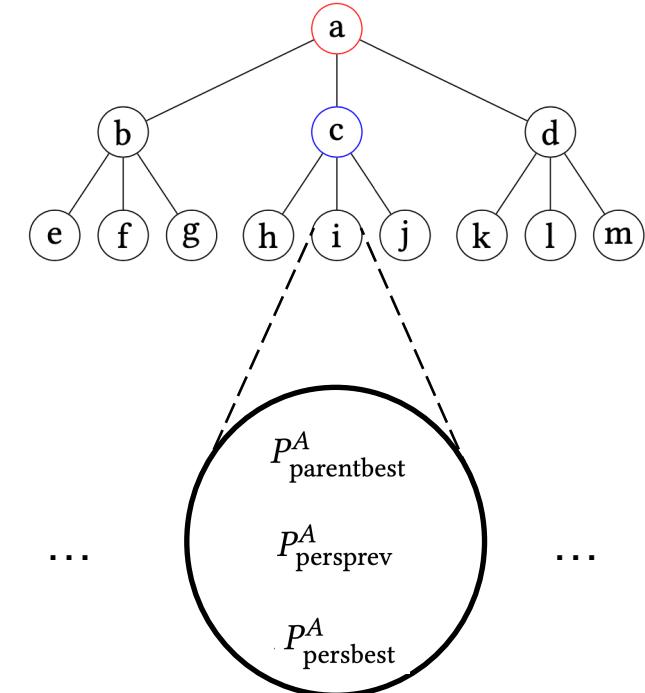
Which sets of parameters yield the best results for a given DTSP instance?

2. Theoretical Background

WHAT DO I NEED TO KNOW?

HIERARCHICAL SIMPLE PROBABILISTIC POPULATION-BASED OPTIMIZATION (H-SPPBO)

- SCEs: Solution creating entities (\approx particles, ants)
 - Organized in a **hierarchical m-ary tree**
 - Defines **neighborhood relation** (range)
- **Three populations** influence solutions
 - Personal previous solution P_{persprev}^A
 - Personal best solution P_{persbest}^A
 - Parent best solution $P_{\text{parentbest}}^A$



HIERARCHICAL SIMPLE PROBABILISTIC POPULATION-BASED OPTIMIZATION (H-SPPBO)

- Solutions created using **probabilistic term** τ

- Start at random city node i
- Set of unvisited cities U , iterate for: $k \in U$

$$\begin{aligned}\tau_{ik}(A) = & \left[w_{\text{rand}} + w_{\text{persprev}} \cdot s_{ik}(P_{\text{persprev}}) \right. \\ & + w_{\text{persbest}} \cdot s_{ik}(P_{\text{persbest}}) \\ & \left. + w_{\text{parentbest}} \cdot s_{ik}(P_{\text{parentbest}}) \right]^{\alpha} \cdot \eta_{ik}^{\beta}\end{aligned}$$



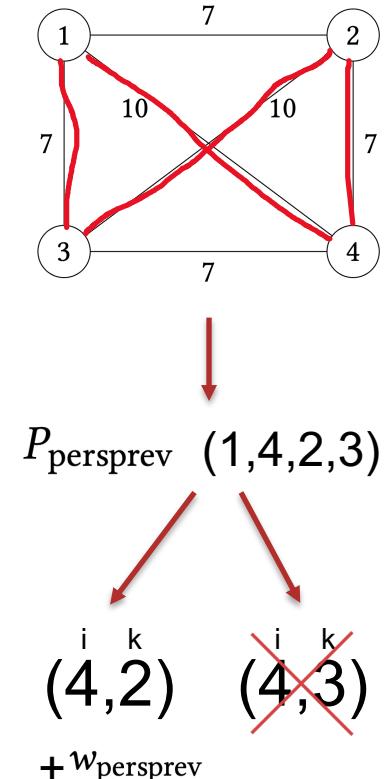
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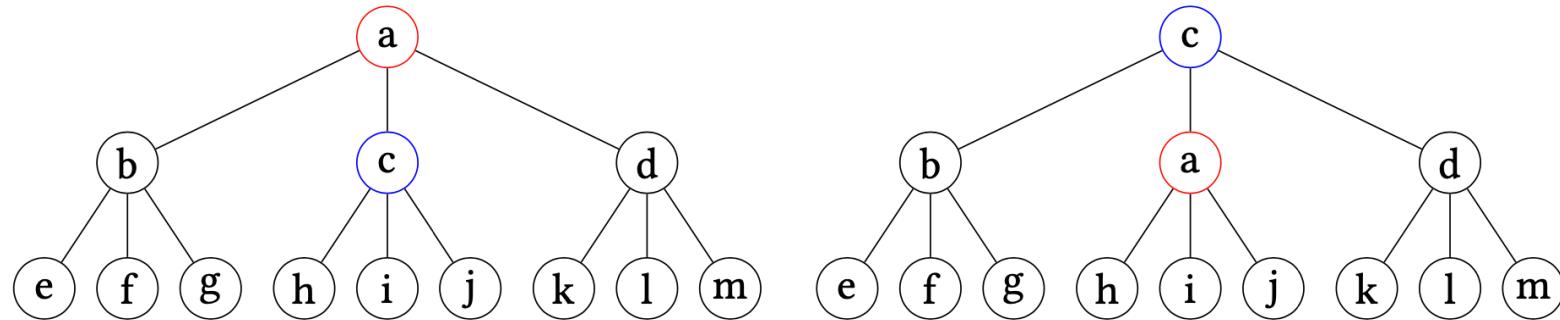
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Stochastic Heuristic



HIERARCHICAL SIMPLE PROBABILISTIC POPULATION-BASED OPTIMIZATION (H-SPPBO)

- SCE tree updated with new solutions: **Top-Down, Breadth-First**

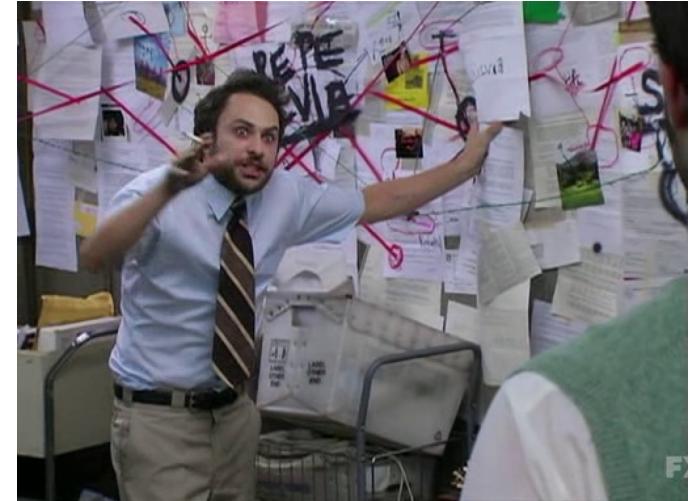


HIERARCHICAL SIMPLE PROBABILISTIC POPULATION-BASED OPTIMIZATION (H-SPPBO)

- Detect changes using **tree swaps**
 - Percentage of SCEs swapped per iteration $\theta \in [0, 1]$
- Threshold triggers **change handling procedure**: two strategies
 1. **Full** reset of all personal best solutions
 2. **Partial** reset of personal best solutions (from third tree level down)

PARAMETER OPTIMIZATION FOR METAHEURISTICS

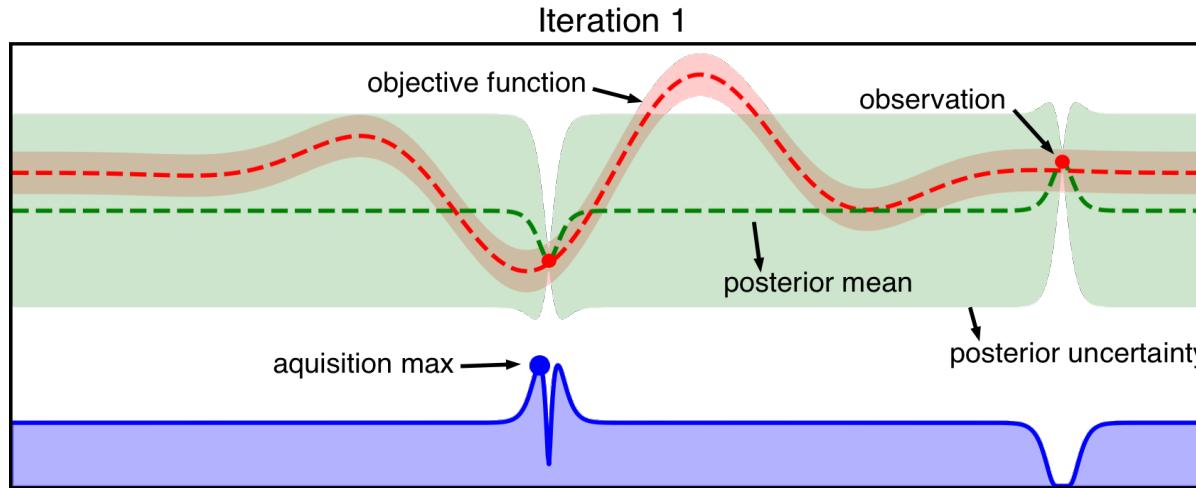
- H-SPPBO has many parameters:
 - $w_{persprev}, w_{persbest}, w_{parentbest} \geq 0$
 - $\alpha, \beta \geq 0$
 - $\theta \in [0, 1]$
 - change handling procedure (full/partial)
- Performance relies on **good parameters**
 - Solution: Manual Parameter Tuning
 - Better Solution: HPO

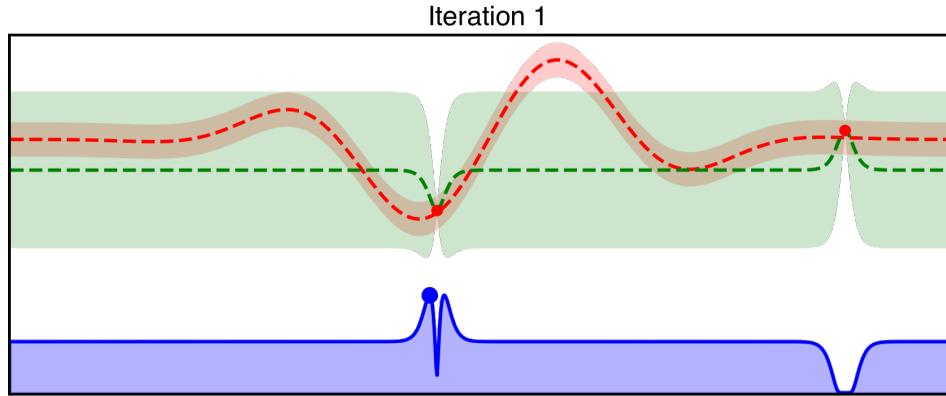


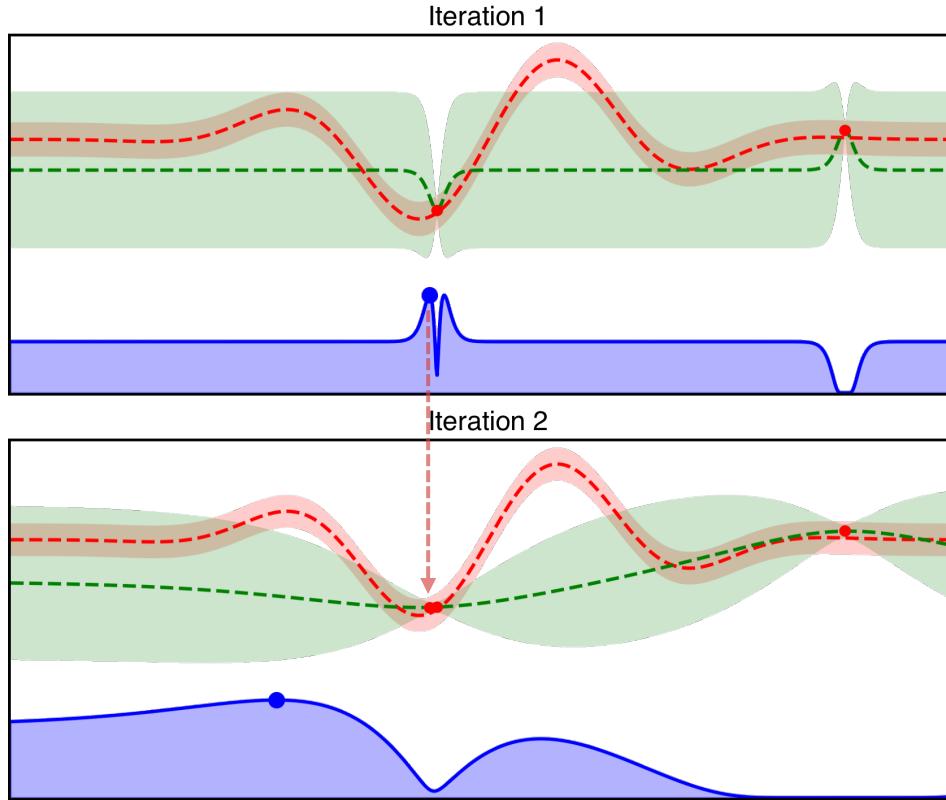
HPO: METHODS

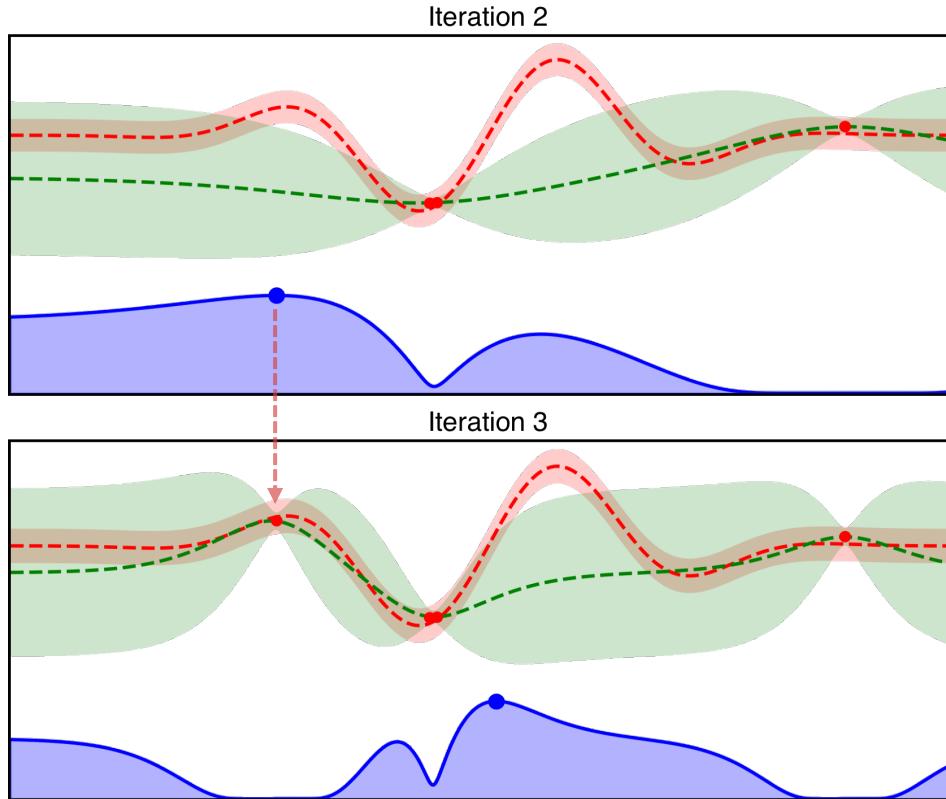
- Model-Free: Random Search (RS)
 - Randomized Brute Force approach (uniform samples)
- Model-Based: Bayesian Optimization (BO)
 - Algorithm framework for global optimization
 - **Bayes' theorem:** Incorporates **prior knowledge** into search
 - Two key components: **Surrogate Model** and **Acquisition Function**

BAYESIAN OPTIMIZATION (BO): ALGORITHM









3. Implementation

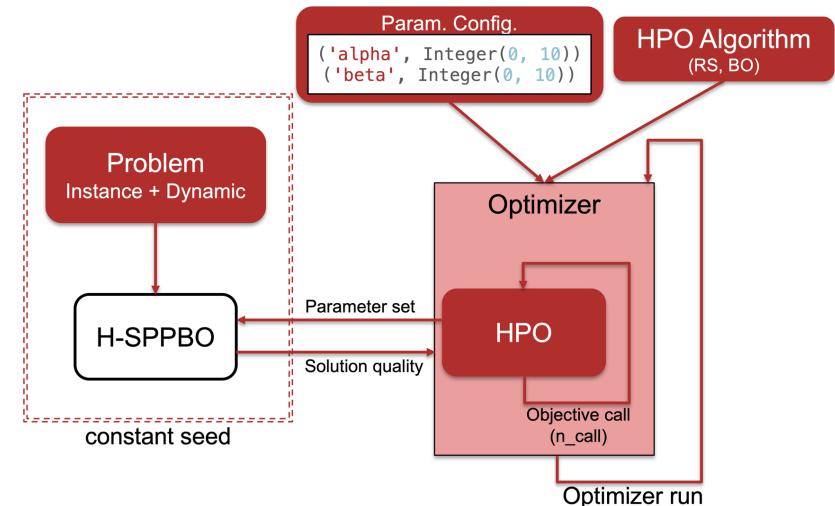
HOW IS THIS REALIZED?

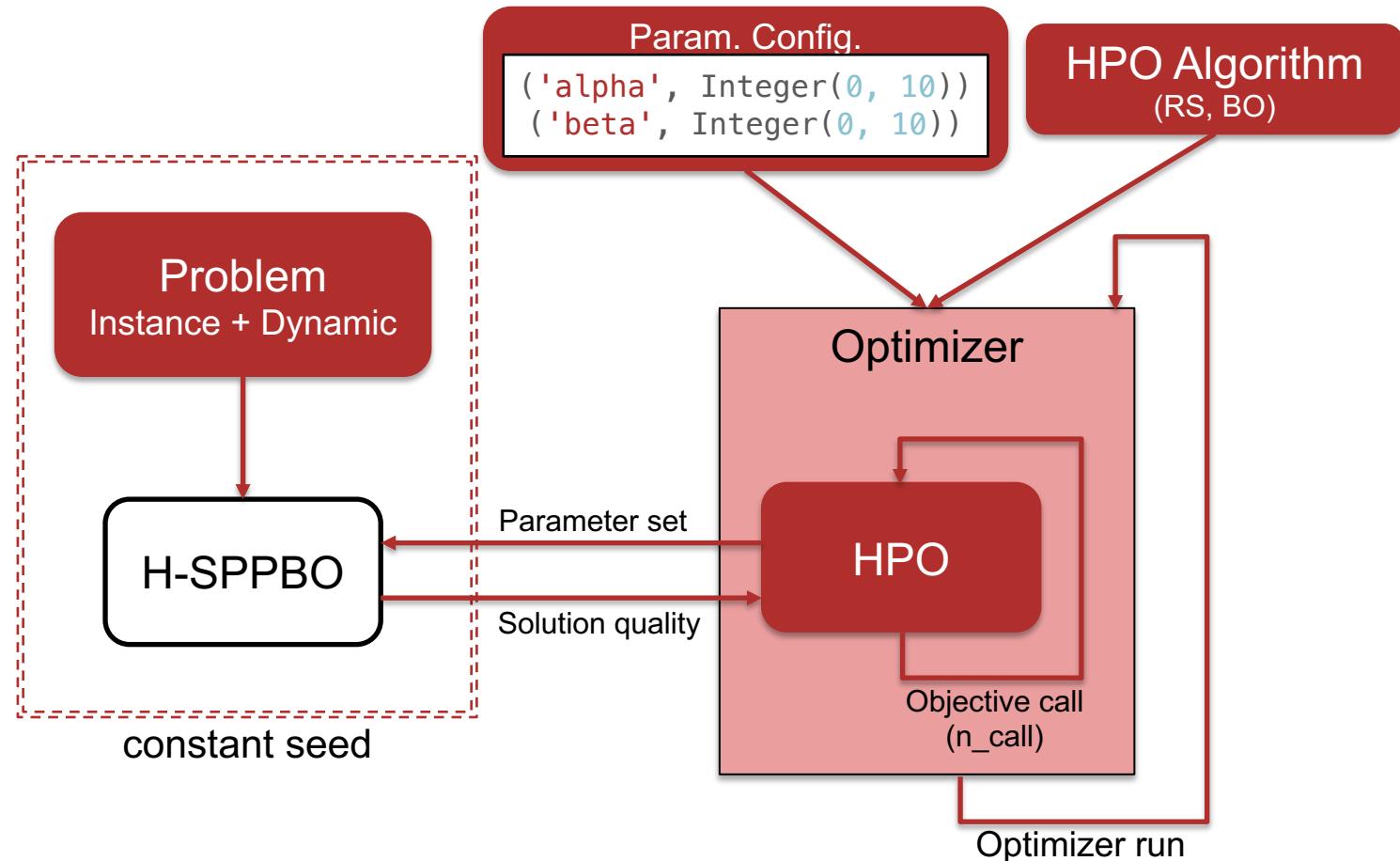
IMPLEMENTATION

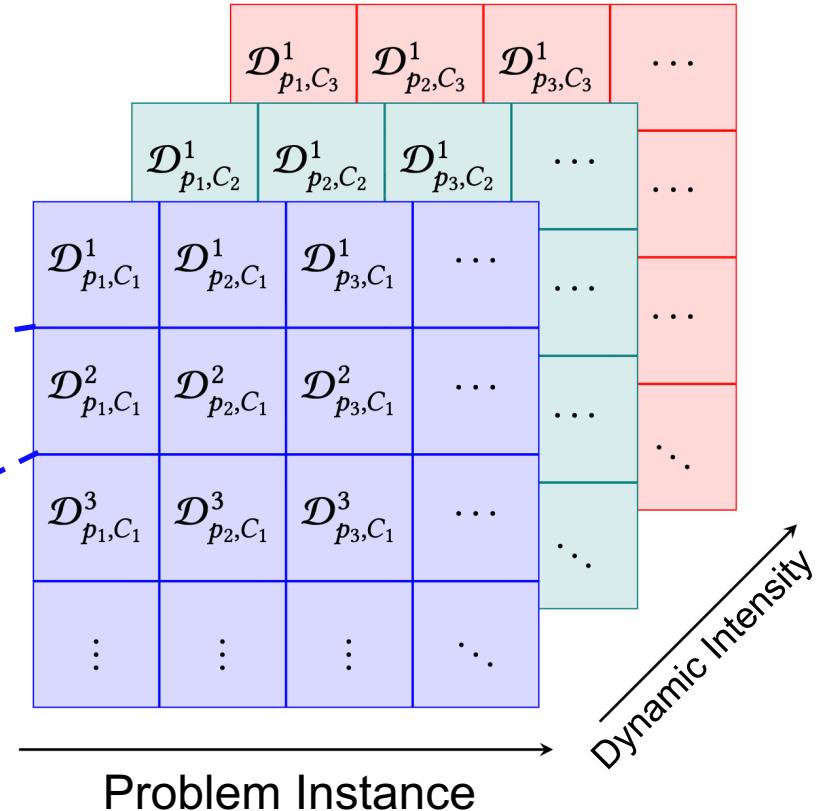
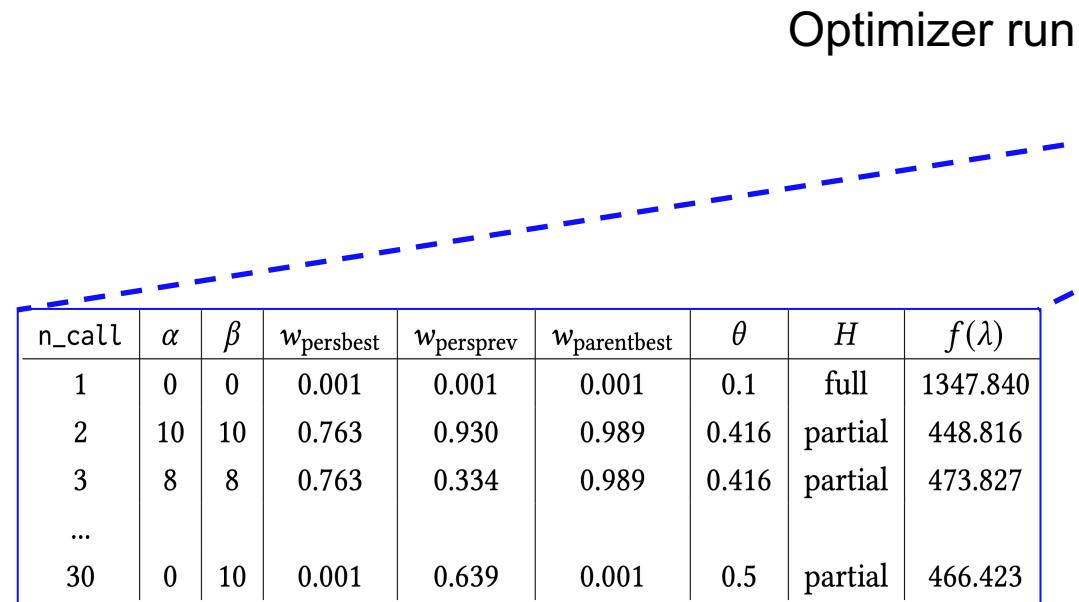
- **EXperimentation Framework and (Hyper-)Parameter Optimization for Metaheuristics (XF-OPT/META)**
 - Python 3.10 or newer
 - Modular, expandable and object-oriented
- Three major, custom modules
 - Problem Interface + TSP Module
 - H-SPPBO Module
 - Optimizer Module

OPTIMIZER MODULE

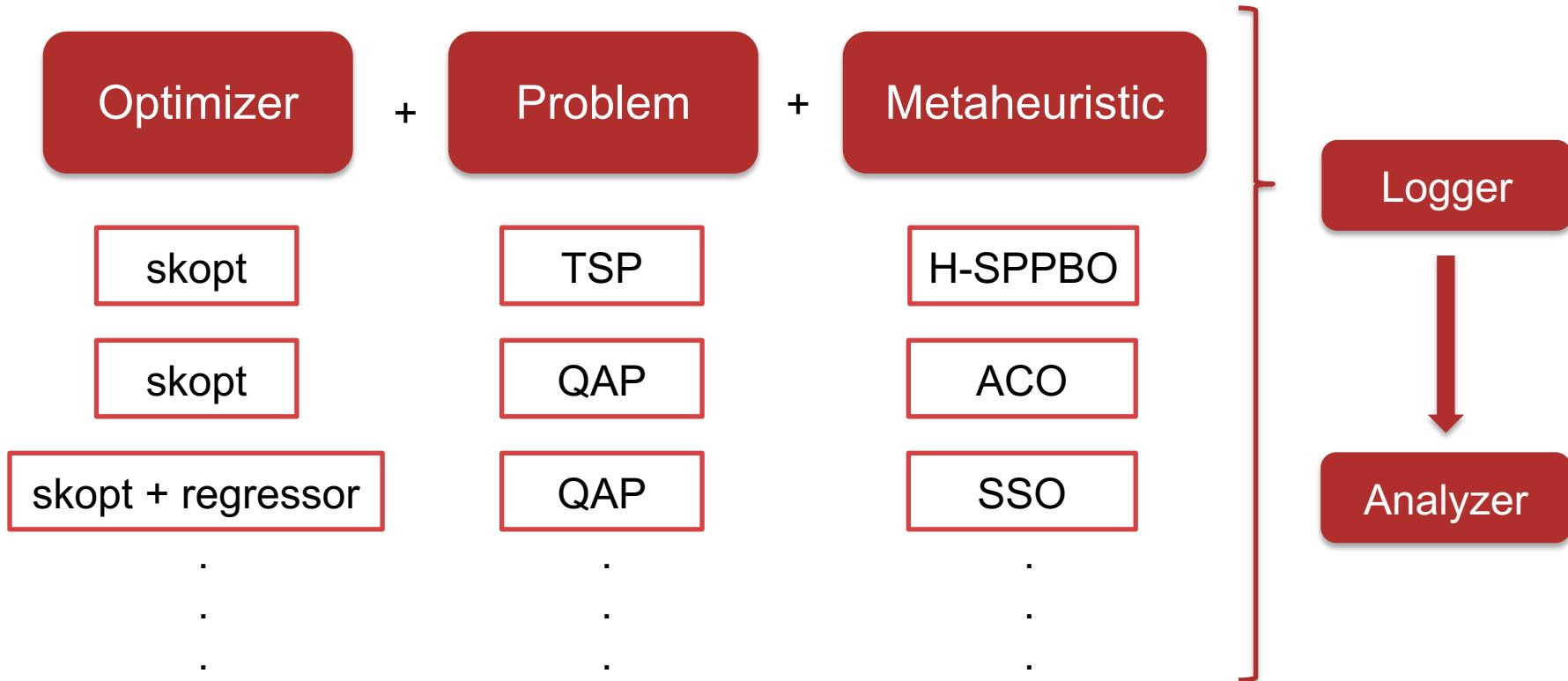
- HPO based on *scikit-optimize (skopt)* library
 - Relies on popular *scikit-learn* package
- Deterministically **repeatable** optimizer runs
 - RNG seed fixed for all modules







FRAMEWORK VIEW AND WORKFLOWS



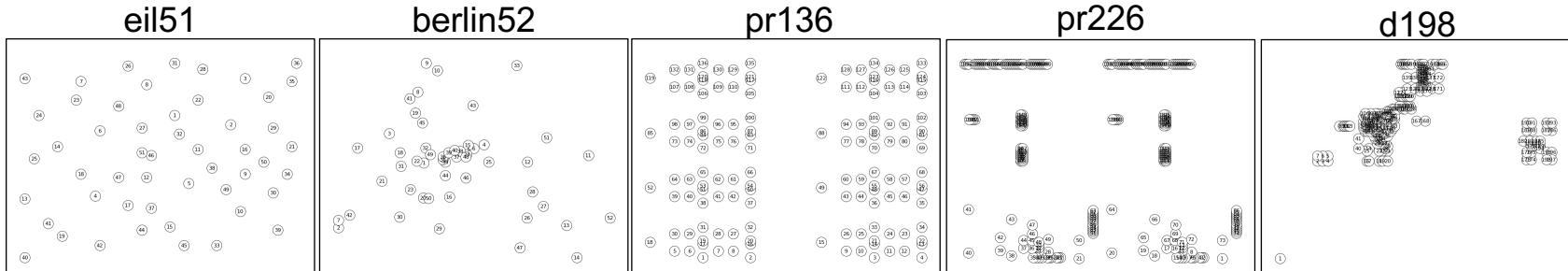
4. Experimental Design

WHAT DATA DO I NEED AND HOW DO I GET IT?

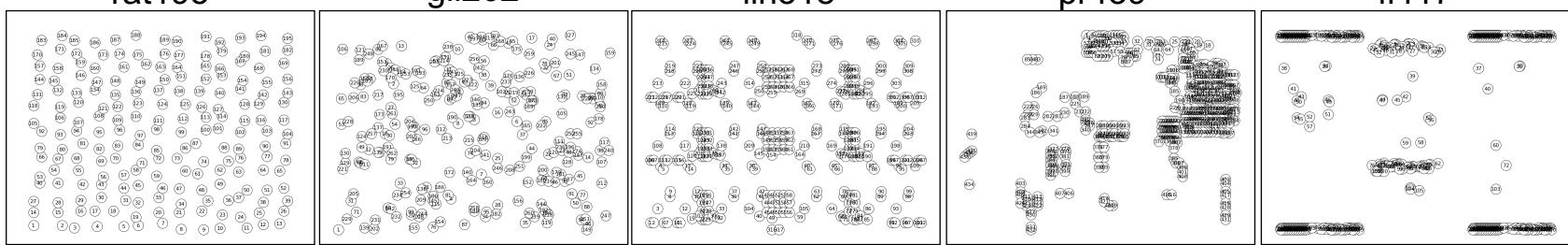
CHOICE OF PROBLEM INSTANCES

- Goal: **meaningful, disjoint subset** of problem instances from TSPLIB
- Two decision metrics: **Dimension & Placement characteristics**
- Dimension: Time as decision factor → smaller than 450 nodes
 - **Smaller** instances [50, 250]
 - **Larger** instances [250, 450]

smaller



larger



Group

1.

2.

3.

4.

5.

random, nearly
regularslightly clustered,
otherwise randomartificial pattern,
many medium
clustersfew highly
clustereddispersed, highly
clustered

CHOICE OF OPTIMIZATION METHODS

- Random Search & Bayesian Optimization

→ Four distinct HPO methods:

- 1. Random Search (**RS**)
 - 2. Bayesian Optimization using Gaussian Process (**BO-GP**)
 - 3. Bayesian Optimization using Extra Tress (**BO-ET**)
 - 4. Bayesian Optimization using Gradient Boosted Regression Trees (**BO-GBRT**)
- 
- Surrogate Models

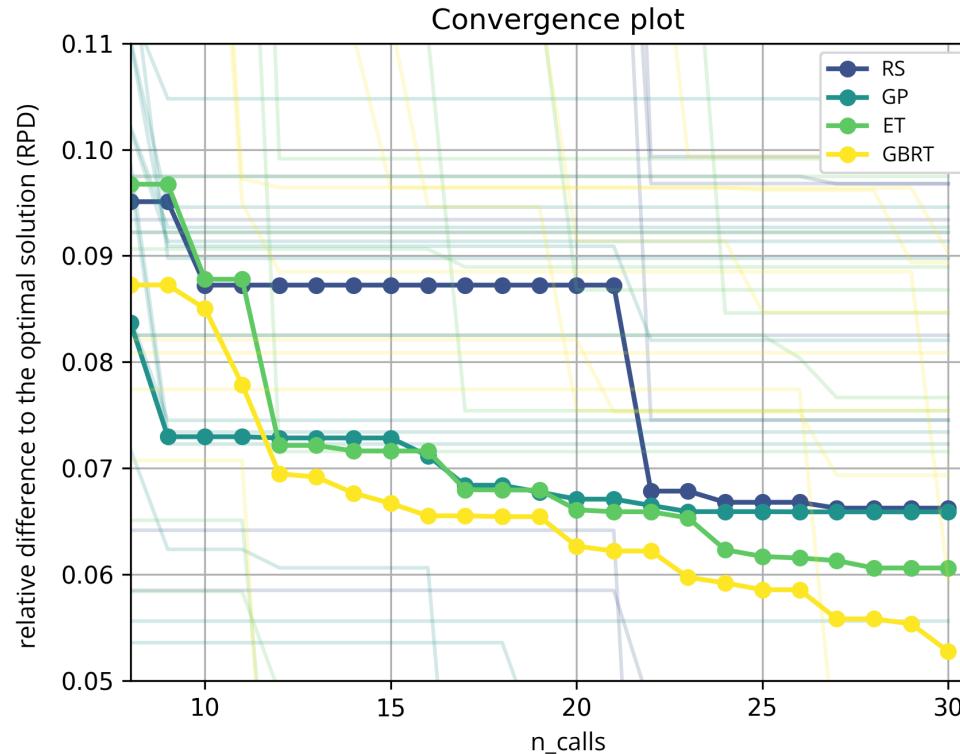
TESTING PROCEDURE

- Three test parts
 1. Find most appropriate HPO method for H-SPPBO
→ 1800 H-SPPBO executions
 2. Find optimal parameter sets for each problem instance
→ 5400 H-SPPBO executions
 3. Evaluate and compare HPO parameters with standard choices
→ 1200 H-SPPBO executions
- Two servers (16/36 threads), taking ~3 months

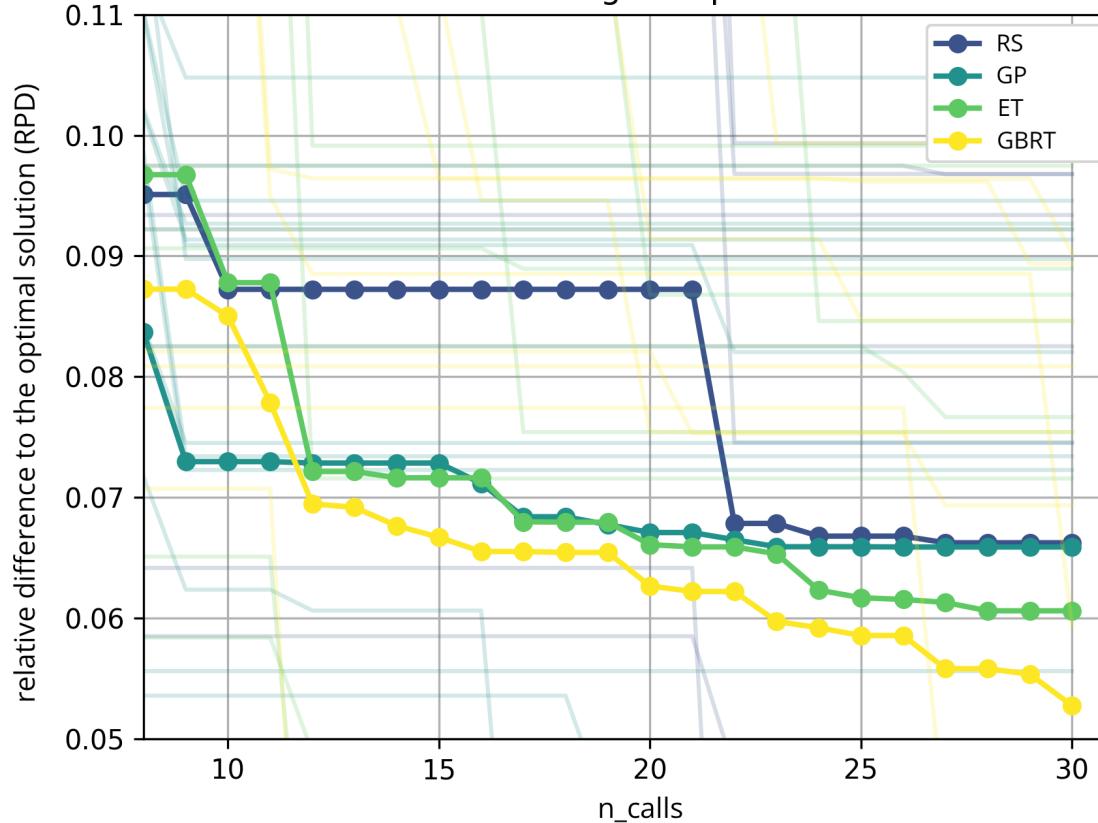
5. Results

WHAT DOES THE DATA SAY?

RESULTS: PART 1 - CONVERGENCE BEHAVIOR



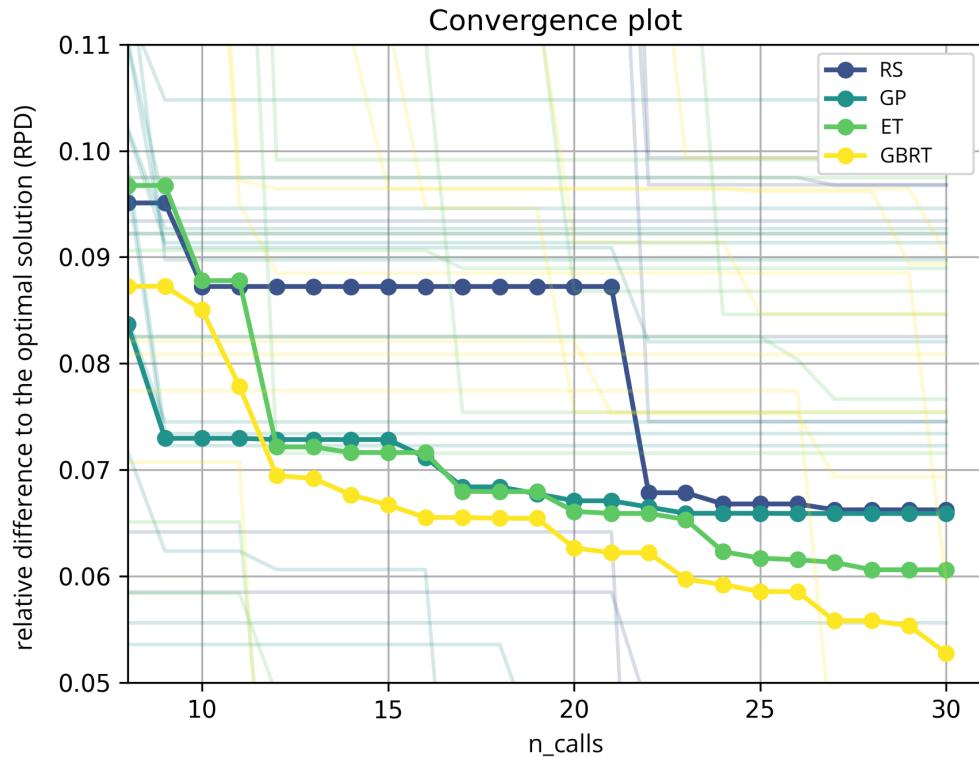
Convergence plot



RESULTS: PART 1

CONVERGENCE BEHAVIOR

	RS	GP	ET	GBRT
AUC	1.484	1.298	1.268	1.190
min	0.058	0.060	0.051	0.045

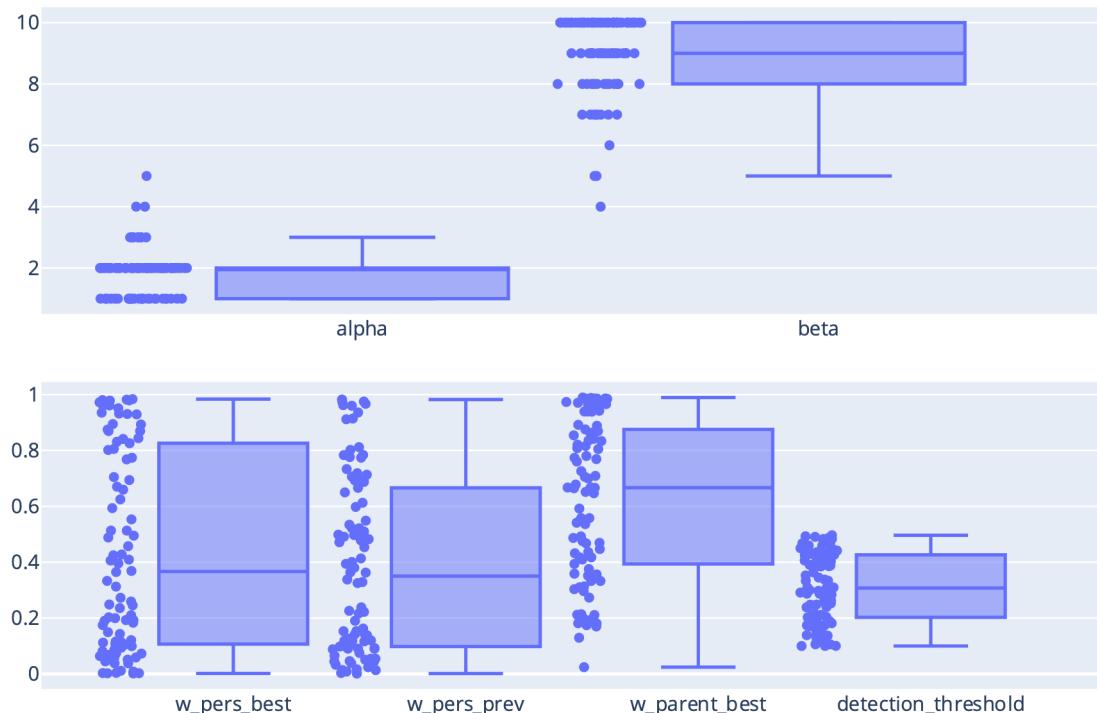


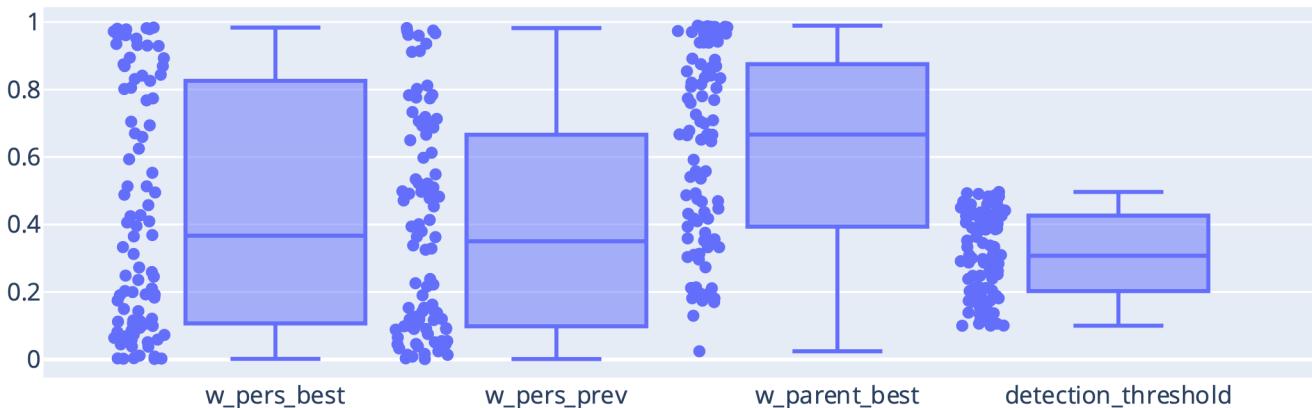
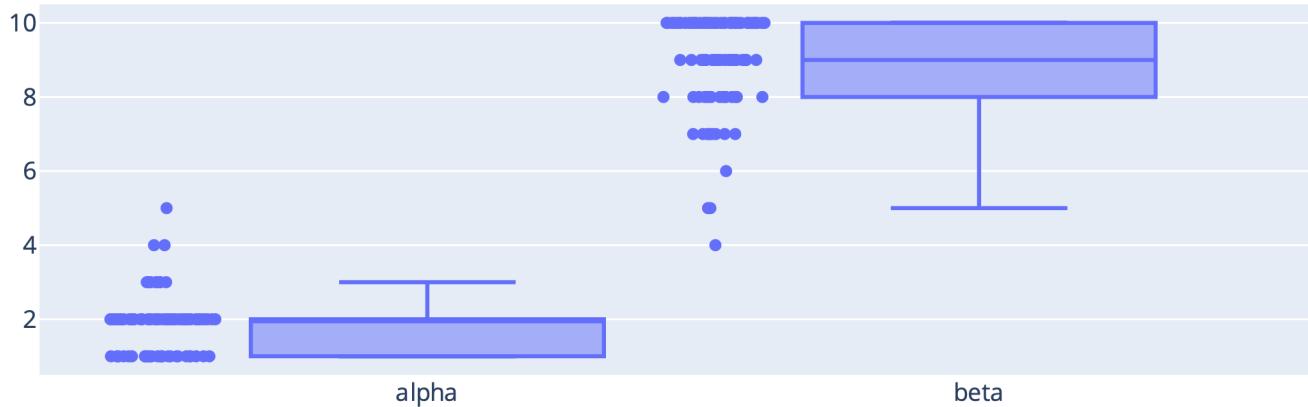
RESULTS: PART 1 - CONCLUSION

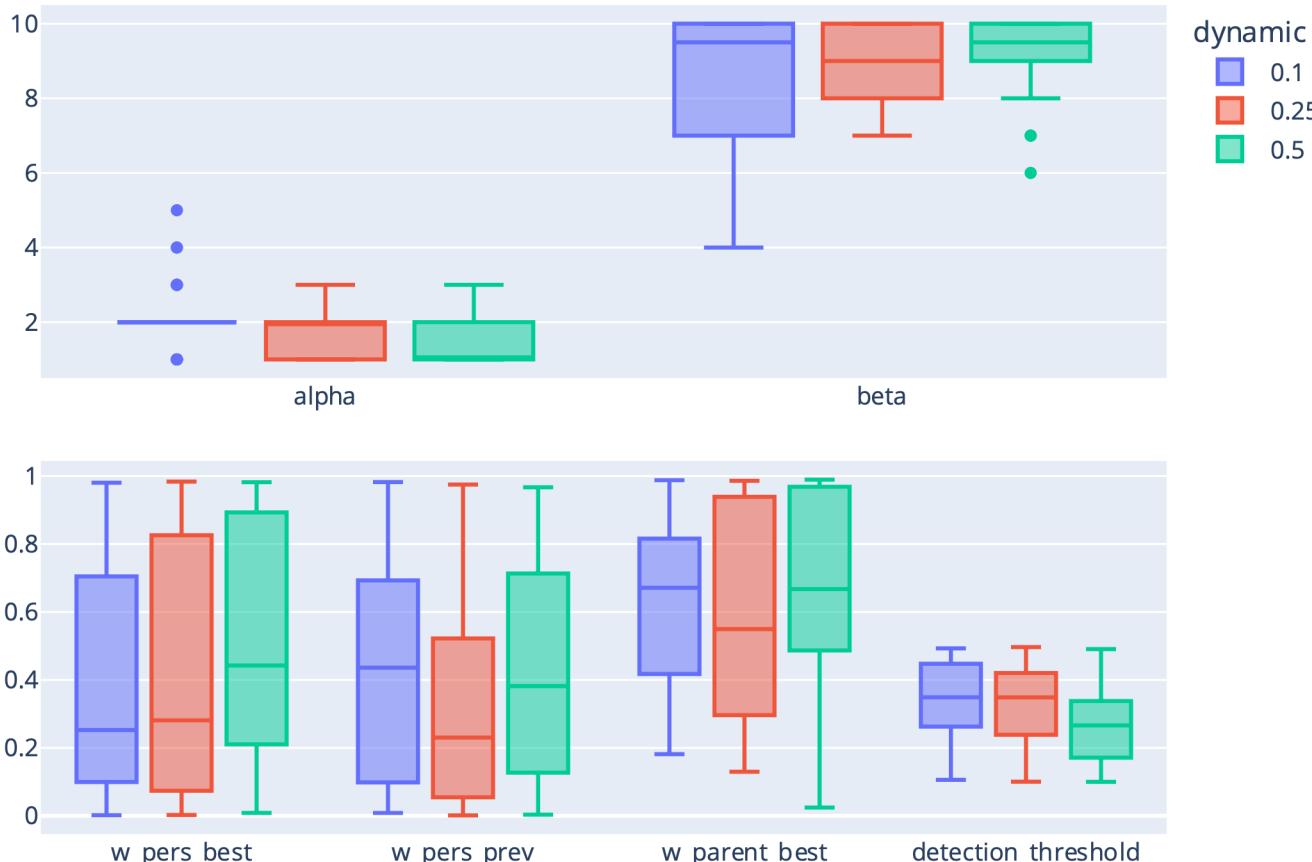
- GBRT performs best
 - Fastest convergence
 - Best solutions
 - Bonus: Parameter Importance through model
- GP: Good performance on larger instances
 - Narrow performance variance → reliable
- GBRT chosen: convergence (speed) → shorter runtime

RESULTS: PART 2 – ROBUSTNESS

- Best parameter sets
 - 5 instances
 - 3 dynamics
 - 6 runs for each instance + dynamic
- 90 data points







6. Conclusion

WHAT HAVE WE LEARNED?

CONCLUSION

- **HPO suitable** for H-SPPBO
 - Good performance without deep algorithm knowledge
- Gradient Boosted Regression Trees (**GBRT**):
 - Top-performing HPO algorithm
- **No single best parameter set** or preferred parameter choices
 - One set per problem description

7. DEMO

SHOW ME!



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THANK YOU!

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