

Diffusion-based Reinforcement Learning via Q-weighted Variational Policy Optimization

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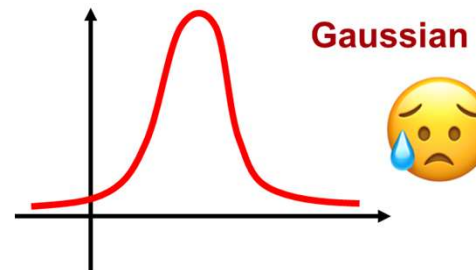
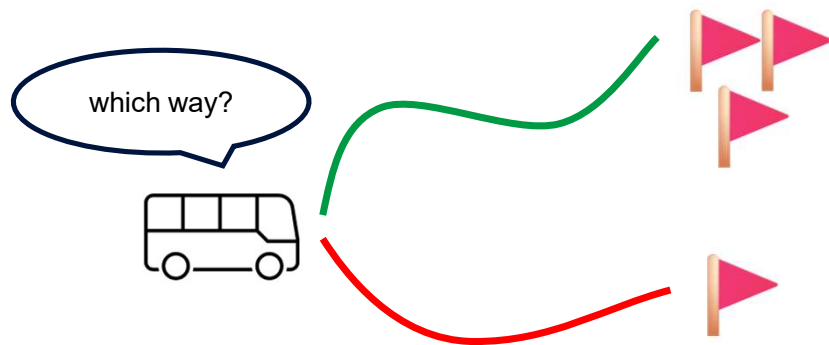


Background: Diffusion in Online RL

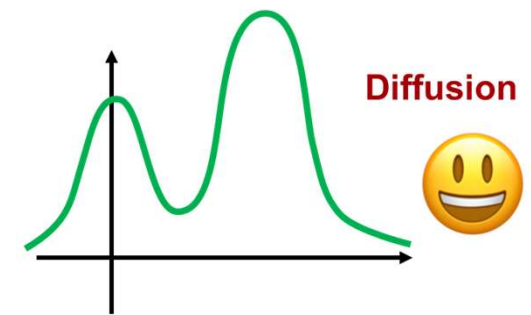


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1. **Exploration capability** of Gaussian policy or deterministic policy is limited
2. **Expressiveness and multimodality** of diffusion avoid policy falling into the local optimality



Gaussian



Diffusion

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Background: Diffusion in Online RL



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Directions of applying diffusion in Online RL:

1. Use the variational loss of diffusion to do policy improvement

$$\mathbb{E}_{t \sim [1, T], \mathbf{x}_0, \epsilon_t} [\|\epsilon_t - \epsilon_\theta(\sqrt{\bar{\alpha}_t} \mathbf{x}_0 + \sqrt{1 - \bar{\alpha}_t} \epsilon_t, t)\|^2].$$

2. Apply deterministic policy loss to train the diffusion model (like Diffusion-QL [1])

$$\pi = \arg \min_{\pi_\theta} \mathcal{L}(\theta) = \mathcal{L}_d(\theta) + \mathcal{L}_q(\theta) = \mathcal{L}_d(\theta) - \alpha \cdot \mathbb{E}_{s \sim \mathcal{D}, a^0 \sim \pi_\theta} [Q_\phi(s, a^0)]$$

[1] Wang Z, Hunt J J, Zhou M. Diffusion policies as an expressive policy class for offline reinforcement learning[J]. arXiv preprint arXiv:2208.06193, 2022..



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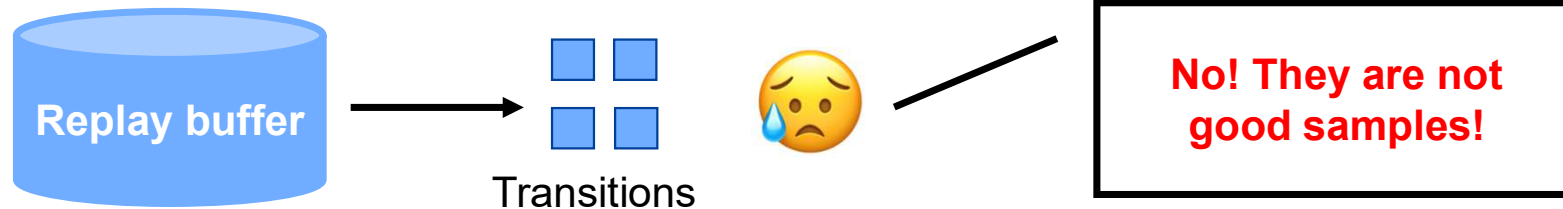
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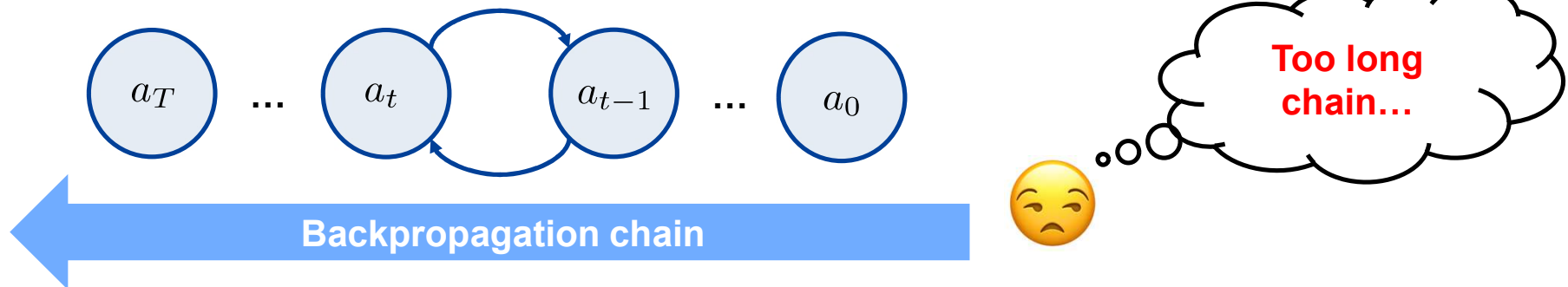
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Difficulties:

Direction 1: Unavailability of **good** actions (not like imitation learning or offline RL)



Direction 2: Too long backpropagation chain (leads to high training cost and training instability)



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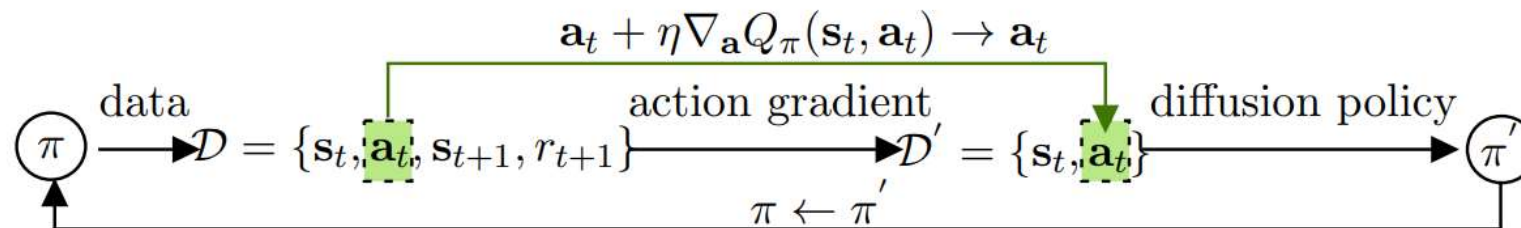
Background: Diffusion in Online RL



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Previous works:

DIPO [1]: Directly perform gradient update on action sample (**affect the multimodality**)



QSM [2]: Do score matching with the gradient of Q function (**Doubled approximation error**)

Update score model:

$$\phi = \operatorname{argmin}_{\phi} N^{-1} \sum (\Psi_{\phi}(x_t, a_t) - \nabla_a Q(x_t, a_t))^2;$$

[1] Yang L, Huang Z, Lei F, et al. Policy representation via diffusion probability model for reinforcement learning[J]. arXiv preprint arXiv:2305.13122, 2023.

[2] Psenka M, Escontrela A, Abbeel P, et al. Learning a diffusion model policy from rewards via q-score matching[J]. arXiv preprint arXiv:2312.11752, 2023.

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Solution: Q-weighted Variational Policy Optimization



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Can we use the variational loss to train diffusion policy?

Distinguish bad and good samples according to their **Q-value**?



But samples from replay buffer are still not good enough!

What if use samples from **current policy**?



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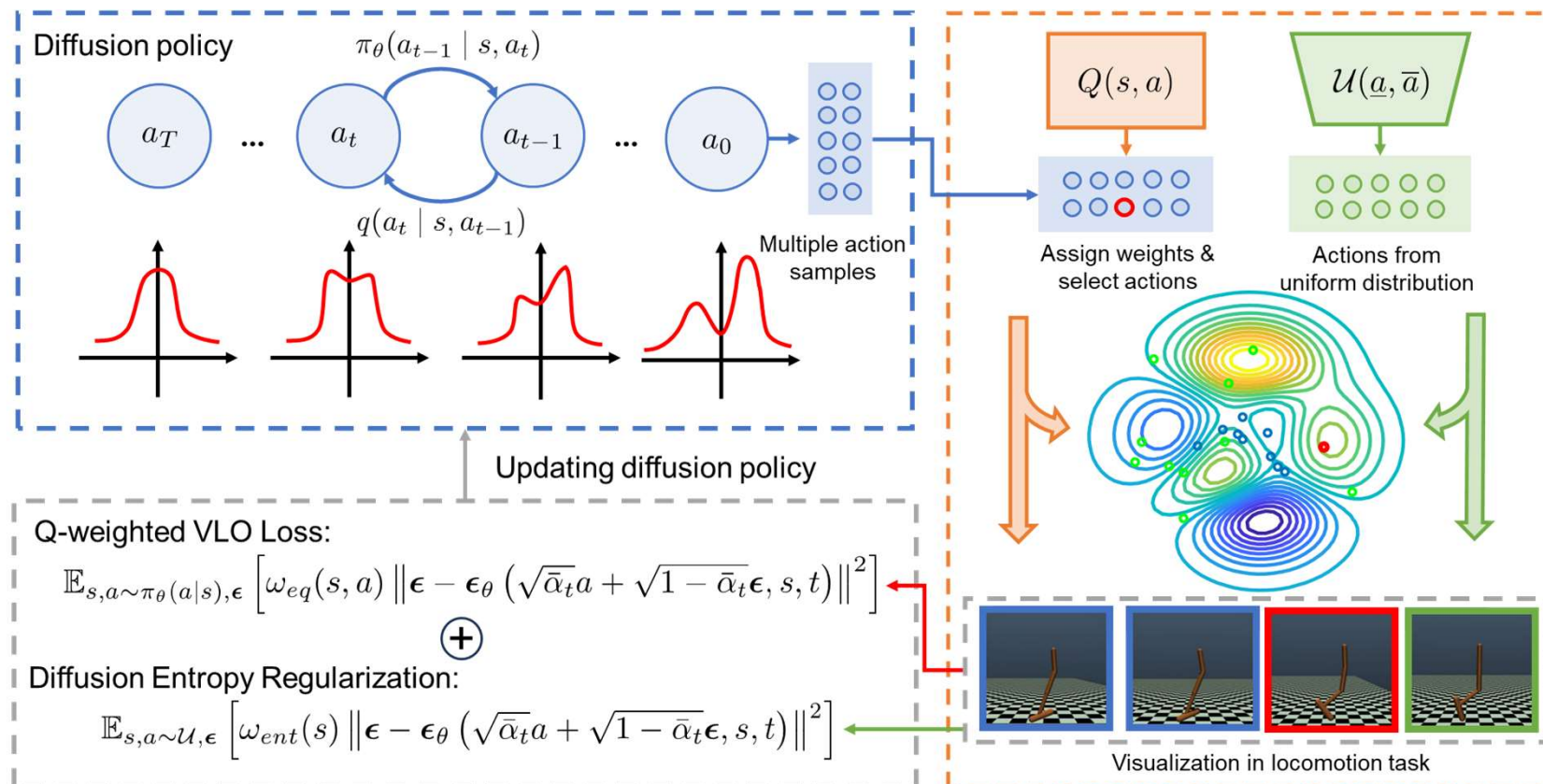
Solution: Q-weighted Variational Policy Optimization



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Motivated by these two ideas, we propose Q-weighted variational policy optimization.

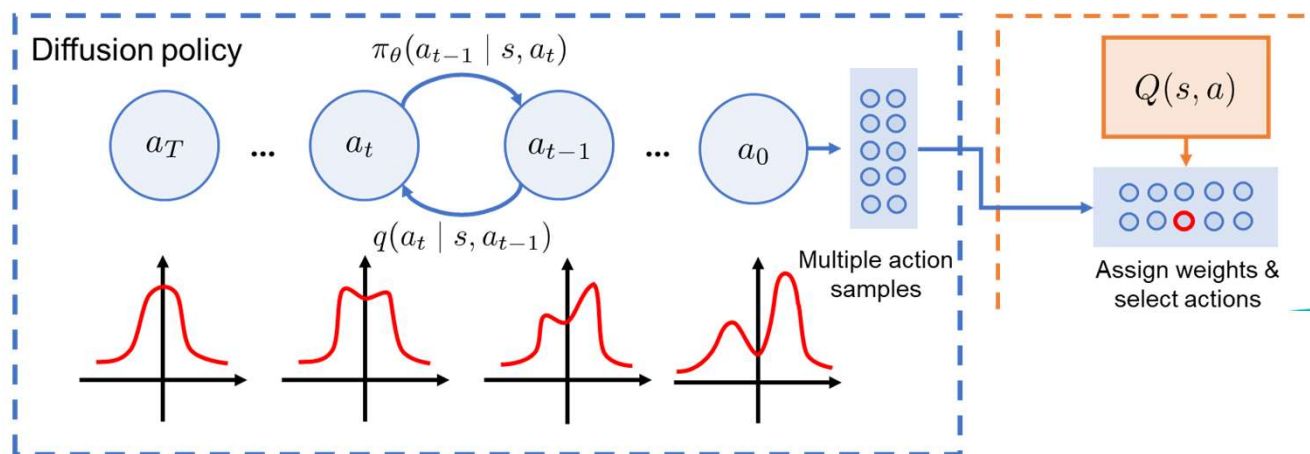


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Q-weighted Variational Loss



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Only choose **the best** generated sample for training.

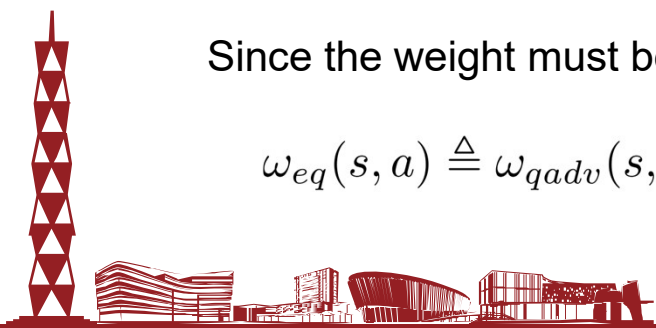
Q-weighted VLO Loss (tight lower bound of RL policy objective):

$$\mathbb{E}_{s, a \sim \pi_{\theta}(a|s), \epsilon} \left[\omega_{eq}(s, a) \left\| \epsilon - \epsilon_{\theta} \left(\sqrt{\bar{\alpha}_t} a + \sqrt{1 - \bar{\alpha}_t} \epsilon, s, t \right) \right\|^2 \right]$$

Since the weight must be nonnegative, we define the weight as

$$\omega_{eq}(s, a) \triangleq \omega_{qadv}(s, a) = \begin{cases} A(s, a), & A(s, a) \geq 0 \\ 0, & A(s, a) < 0 \end{cases},$$

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Diffusion Entropy Regularization

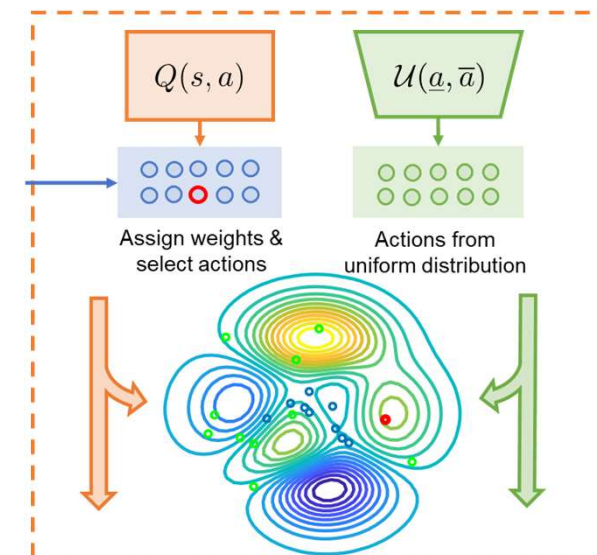


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We also add Diffusion Entropy Regularization term in objective for enhancing exploration capability:

$$\mathbb{E}_{s,a \sim \mathcal{U}, \epsilon} \left[\omega_{ent}(s) \left\| \epsilon - \epsilon_{\theta} \left(\sqrt{\bar{\alpha}_t} a + \sqrt{1 - \bar{\alpha}_t} \epsilon, s, t \right) \right\|^2 \right]$$

- Maximizing entropy can be viewed as **minimizing the distance** between current policy and the **uniform distribution**.
- Hence, we use samples from the uniform distribution to train diffusion policy for maximizing the diffusion entropy.



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Comparison w/ & w/o Entropy Term

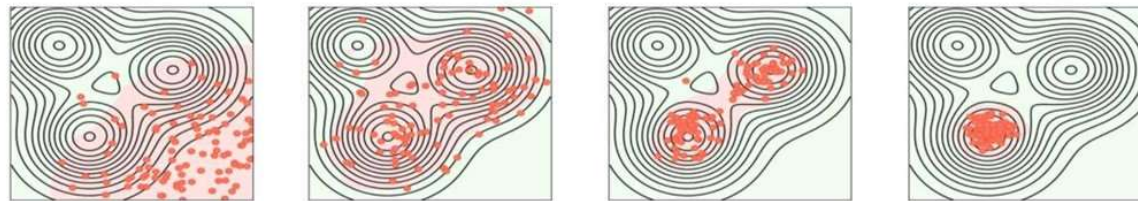


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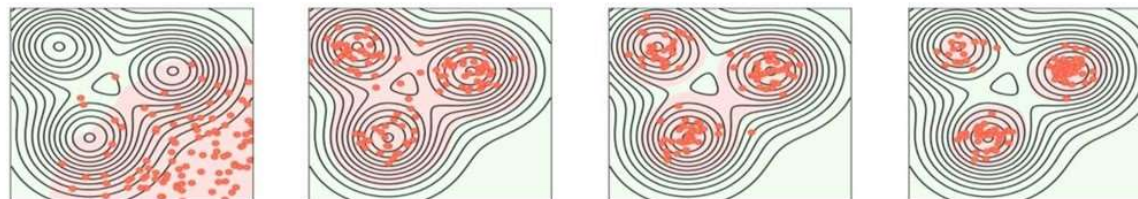
$$\mathbb{E}_{s,a \sim \mathcal{U}, \epsilon} \left[\omega_{ent}(s) \left\| \epsilon - \epsilon_{\theta} \left(\sqrt{\bar{\alpha}_t} a + \sqrt{1 - \bar{\alpha}_t} \epsilon, s, t \right) \right\|^2 \right]$$

Diffusion Policy
w/o entropy term

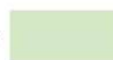


Training Procedure

Diffusion Policy
w/ entropy term



Explorable area of diffusion policy



Unexplorable area



Target objective function

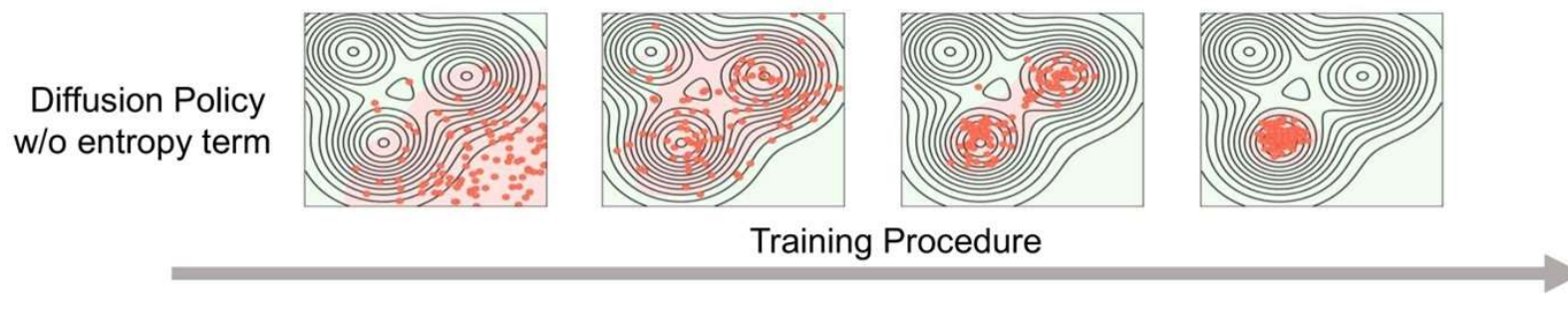
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Reducing Diffusion Policy Variance via Action Selection



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- Diffusion policy has a **large policy variance**
- Reducing this variance can improve **the quality** of collected transitions



We design **efficient behavior policy** via action selection for sample efficiency:

$$\pi_{\theta}^K(a | s) \triangleq \underset{a \in \{a_1, \dots, a_K \sim \pi_{\theta}(a|s)\}}{\operatorname{argmax}} Q(s, a).$$

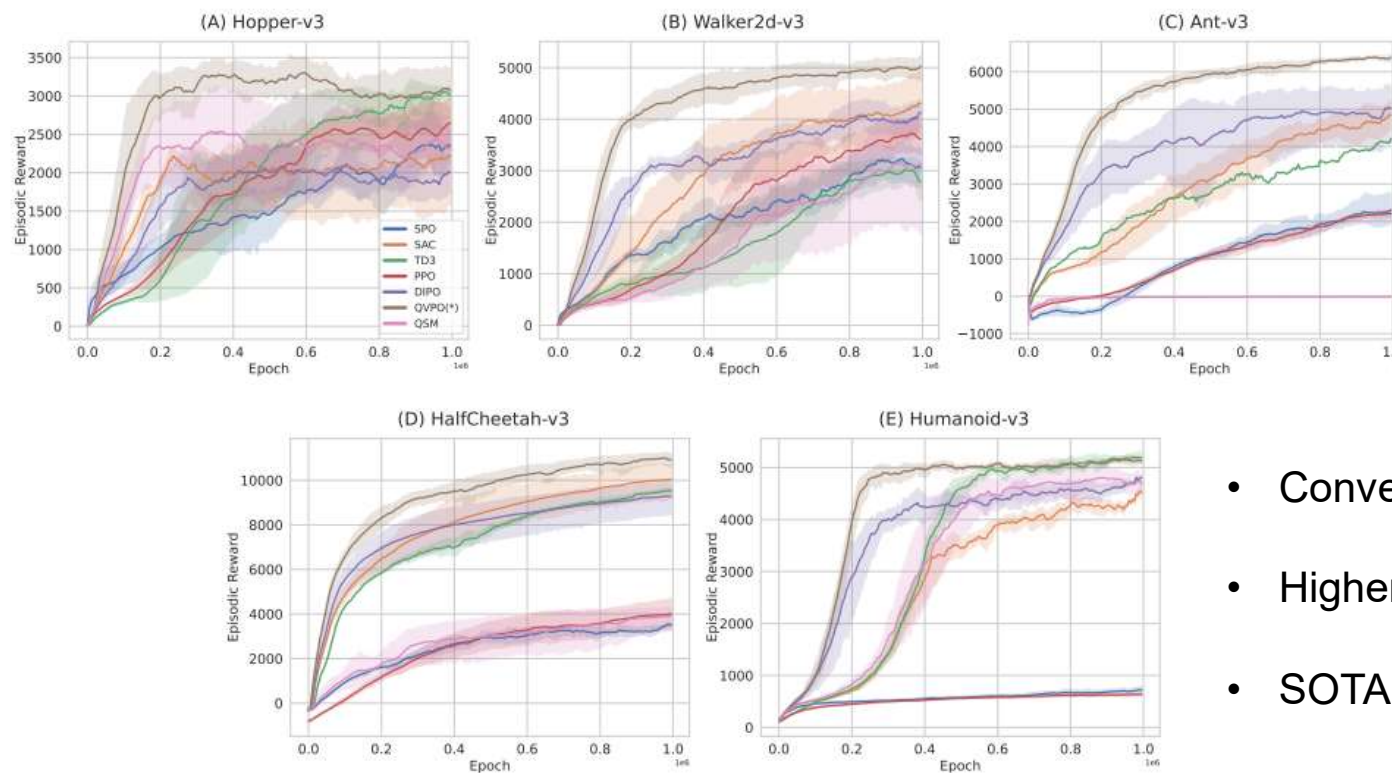


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Results



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- Converge faster (sample efficiency)
- Higher cumulative reward
- SOTA method in online RL

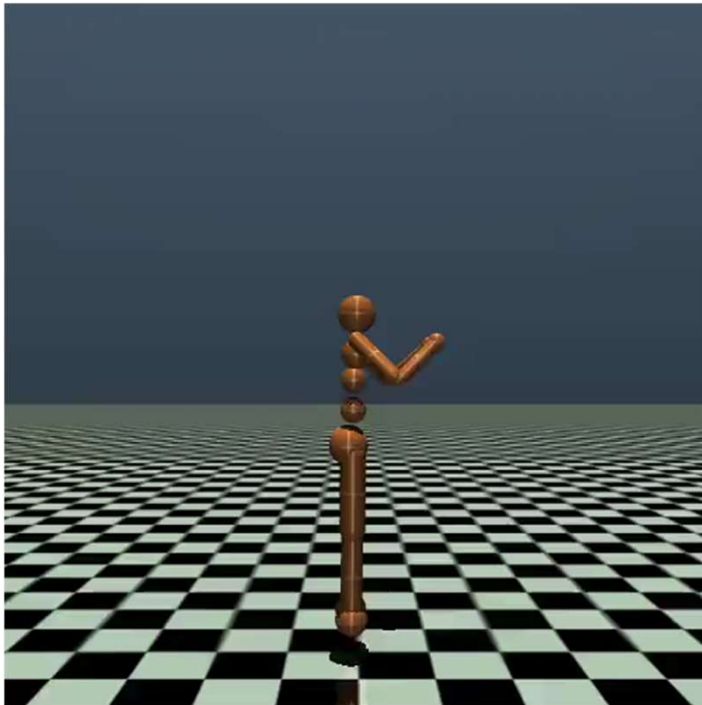
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Comparison with SAC in Humanoid-v3

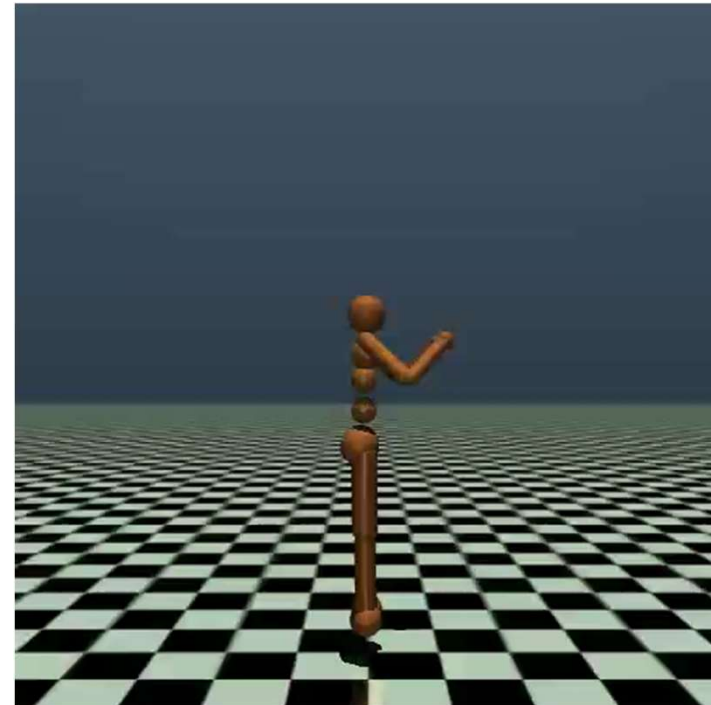


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SAC



our QVPO

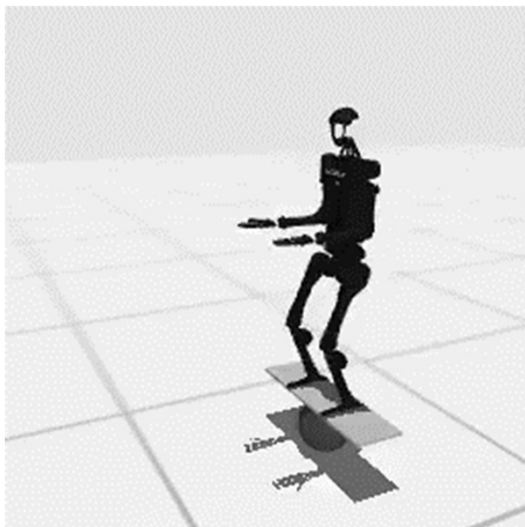


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More Tasks in Unitree Humanoid H1



Balance (TD-MPC2)



Balance (our QVPO)



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More Tasks in Unitree Humanoid H1

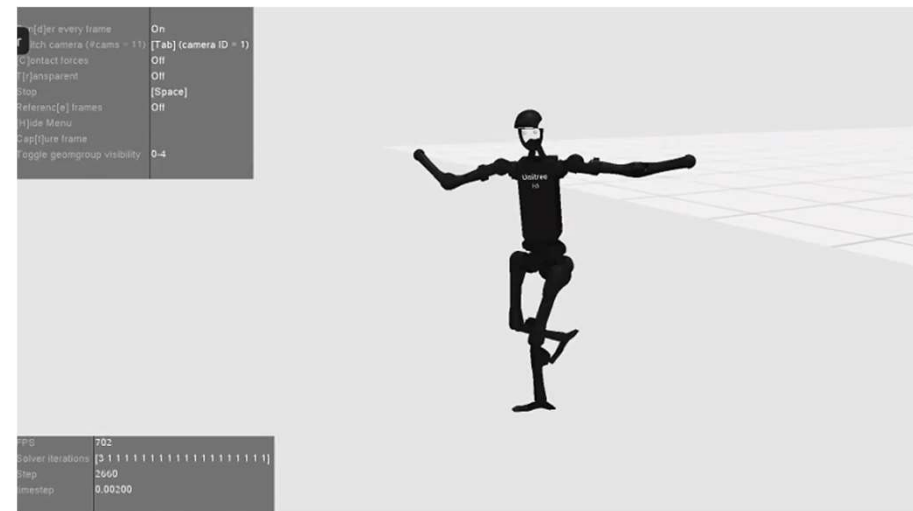


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Walk (QVPO)



Run (QVPO)



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