

Level 1 Questions ; Bird that hit king Pig \rightarrow Black. Proof;

\rightarrow Yellow bird $\rightarrow y = -2x^2 + 12x - 10$

Vertex = $x = \frac{-b}{2a}$ $b = 12$ $a = -2$

$$\frac{-12}{2(-2)} = \frac{-12}{-4} = 3$$

$$x = 3$$

$$y = -2(3)^2 + 12(3) - 10 = 8$$

$$y = 8 \quad \text{peak} \rightarrow (3, 8)$$

Pig (11, 8)

$x = \frac{-b}{2a}$ Make a the subject.

$$\frac{2a}{2} = \frac{-b}{2x}$$

$$a = \frac{-b}{2x}$$

$$a = \frac{-12}{2(11)}$$

$$a = \frac{-12}{22}$$

$$a = \frac{-6}{11}$$

$a \rightarrow$ is the direction of the parabola and should be the same.

OR substitute

Pig (11, 8) $y = -2x^2 + 12x - 10$

$$8 = -2(11)^2 + 12(11) - 10 = 100 \quad \text{Not equal}$$

Hence the yellow bird won't hit king Pig at (11, 8)

\rightarrow Blue starts (0, 0) 5 yards lands (20, 0)

Vertex = $\frac{0+20}{2} = 10 \rightarrow x$ $y \rightarrow 5$ (10, 5)

$$y = a(x-h)^2 + k$$

$$0 = a(0-10)^2 + 5 \rightarrow -5 = a(-10)^2 \rightarrow \frac{100a}{100} = \frac{-5}{100} \rightarrow a = -\frac{1}{20}$$

$$y = -\frac{1}{20}(x-10)^2 + 5$$

Pig (11, 8) to find a

$$8 = a(11-10)^2 + 5 \rightarrow 8-5 = a(1)^2 \rightarrow a = 3; a \text{ should be } -\frac{1}{20}$$

Hence blue doesn't hit Pig at (11, 8)

→ Black

$$y = -0.25(x-9)^2 + 9$$

$$y = a(x-h)^2 + k \quad \text{vertex} = (9, 9)$$

Pig(11, 8)

$$8 = a(11-9)^2 + 9$$

$$8 - 9 = a(2)^2$$

$$\frac{4}{4}a = \frac{-1}{4} \rightarrow a = -0.25, \text{ } a \text{ is the same in both.}$$

Hence the Black bird hits king Pig at (11, 8)
through a turning point of (9, 9)

→ Bird that reached the highest altitude was the Black bird
at a maximum height of 9 yards.

→ This was 4 yards higher than the lowest altitude
(5yds)

→ The blue bird was in the air the longest and it was there
for 20 seconds.

→ It took 10 seconds before it started to descend.