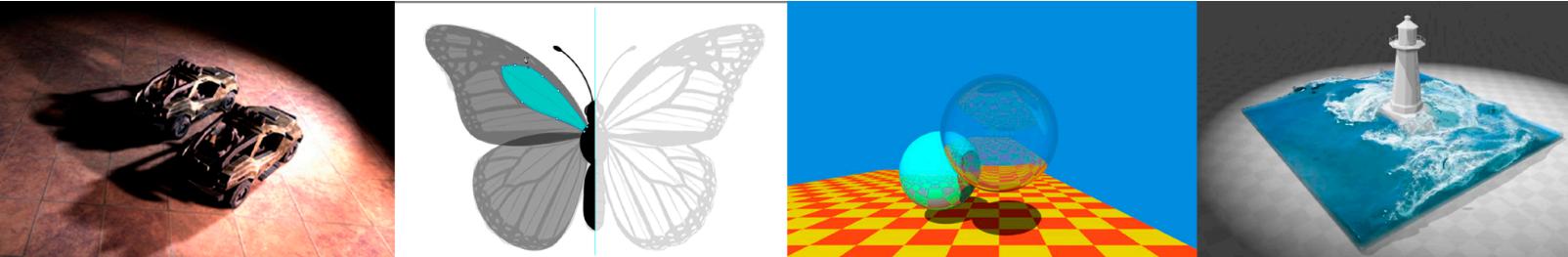


# Introduction to Computer Graphics

GAMES101, Lingqi Yan, UC Santa Barbara

## Lecture 5: Rasterization 1 (Triangles)

光栅化.



# Announcements

- Homework 0 – 188 submissions
  - No worries if you did not submit
- Homework 1 will be released today
  - Containing basic and advanced requirements (graded separately)
  - Pass or not pass depends on basic requirements only
- Asking on BBS
  - Please try to describe your question more clearly
- Today's lecture is pretty easy

# Last Lecture

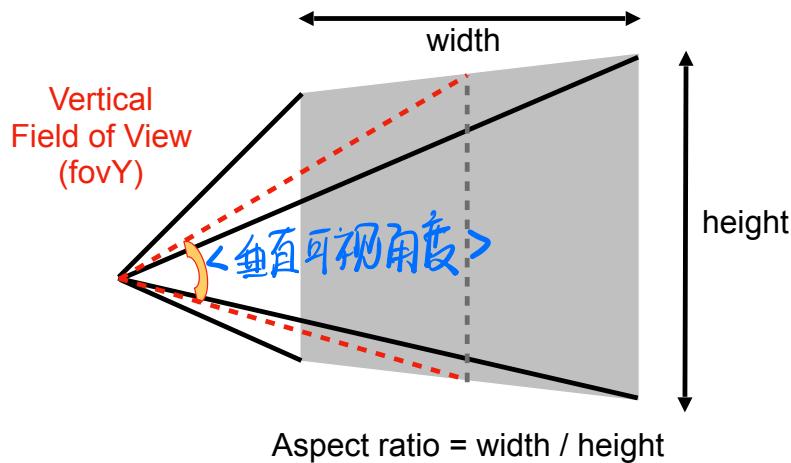
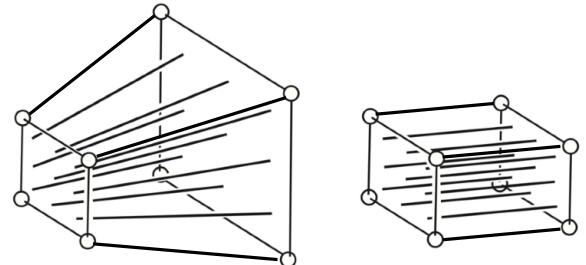
- Viewing (观测) transformation
  - View (视图) / Camera transformation
  - Projection (投影) transformation
    - Orthographic (正交) projection
    - Perspective (透视) projection

# Today

- Finishing up Viewing
  - Viewport transformation
- Rasterization
  - Different raster displays
  - Rasterizing a triangle
- Occlusions and Visibility

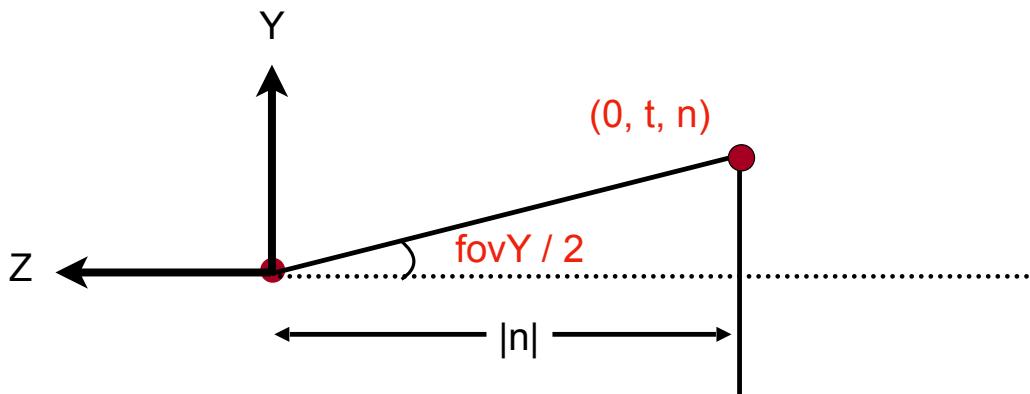
# Perspective Projection

- What's near plane's l, r, b, t then?
  - If explicitly specified, good
  - Sometimes people prefer:  
vertical **field-of-view** (fovY) and  
**aspect ratio** <垂直可视角度>  
(assume symmetry i.e. l = -r, b = -t)



# Perspective Projection

- How to convert from  $\text{fovY}$  and aspect to  $l, r, b, t$ ?
  - Trivial



$$\tan \frac{\text{fovY}}{2} = \frac{t}{|n|}$$

$$\text{aspect} = \frac{r}{t}$$

# What's after MVP?

- Model transformation (placing objects)
- View transformation (placing camera)
- Projection transformation
  - Orthographic projection (cuboid to “canonical” cube  $[-1, 1]^3$ )
  - Perspective projection (frustum to “canonical” cube)
- Canonical cube to ?

标准立方体到屏幕

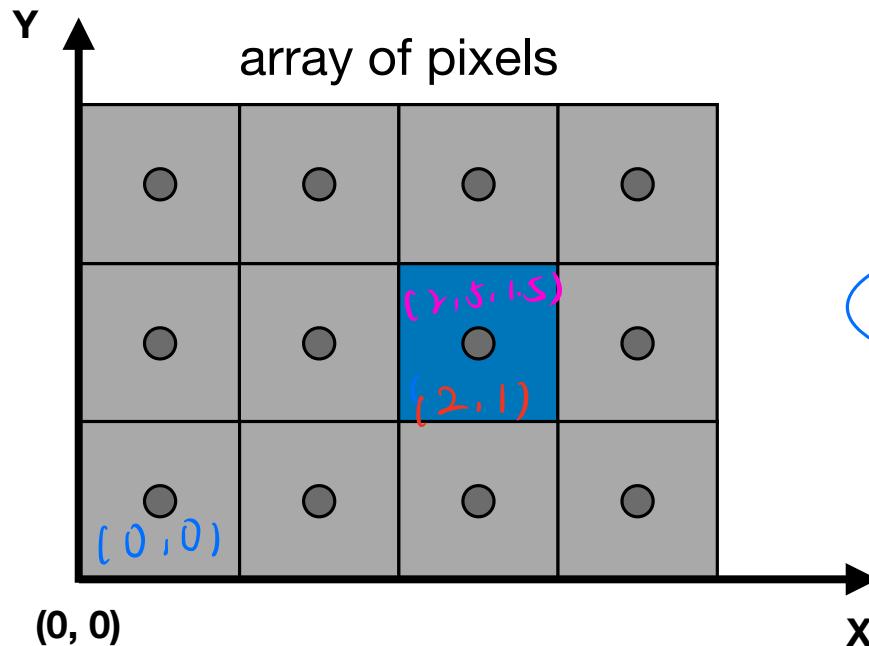
# Canonical Cube to Screen

- What is a screen?
  - An array of pixels
  - Size of the array: resolution
  - A typical kind of raster display
- Raster == screen in German
  - Rasterize == drawing onto the screen
- Pixel (FYI, short for “picture element”)
  - For now: A pixel is a little square with uniform color
  - Color is a mixture of (red, green, blue)

# Canonical Cube to Screen

从 Canonical Cube 到 Screen Space

- Defining the screen space
  - Slightly different from the “tiger book”



Pixels' indices are in the form of  $(x, y)$ , where both  $x$  and  $y$  are integers

像素坐标

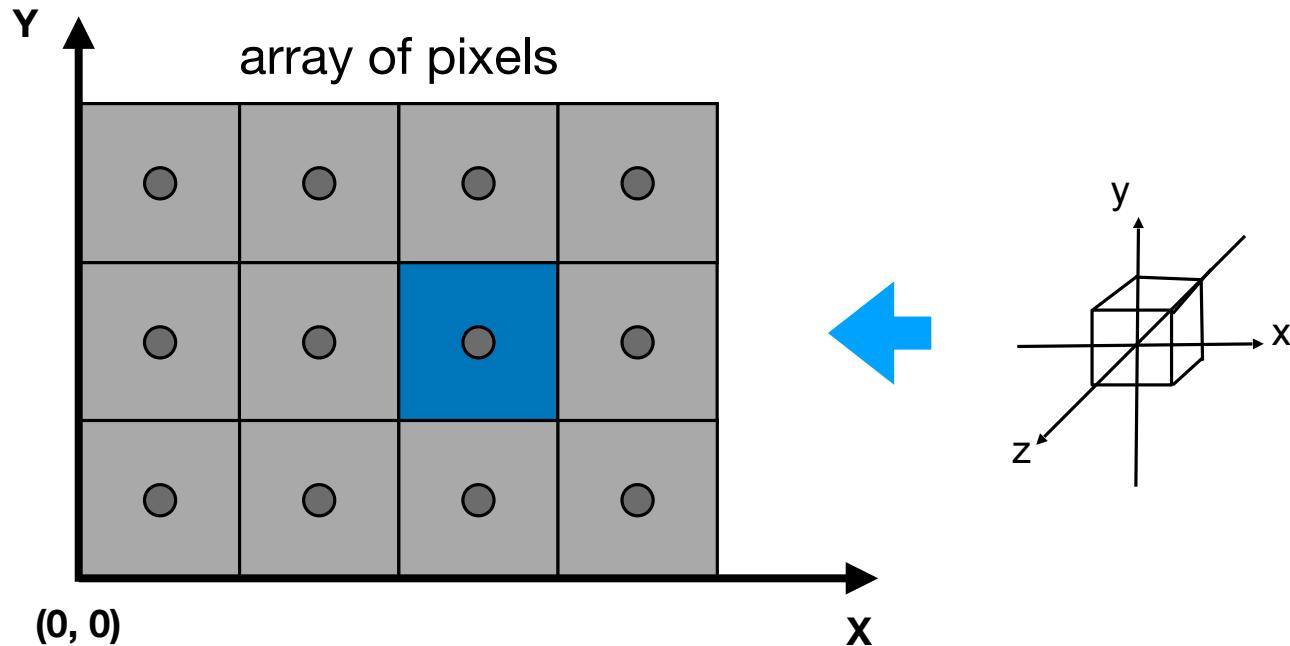
Pixels' indices are from  $(0, 0)$  to  $(\text{width} - 1, \text{height} - 1)$

Pixel  $(x, y)$  is centered at  $(x + 0.5, y + 0.5)$

The screen covers range  $(0, 0)$  to  $(\text{width}, \text{height})$

# Canonical Cube to Screen

- Irrelevant to z *(忽略 z)*
- Transform in xy plane:  $[-1, 1]^2$  to  $[0, \text{width}] \times [0, \text{height}]$



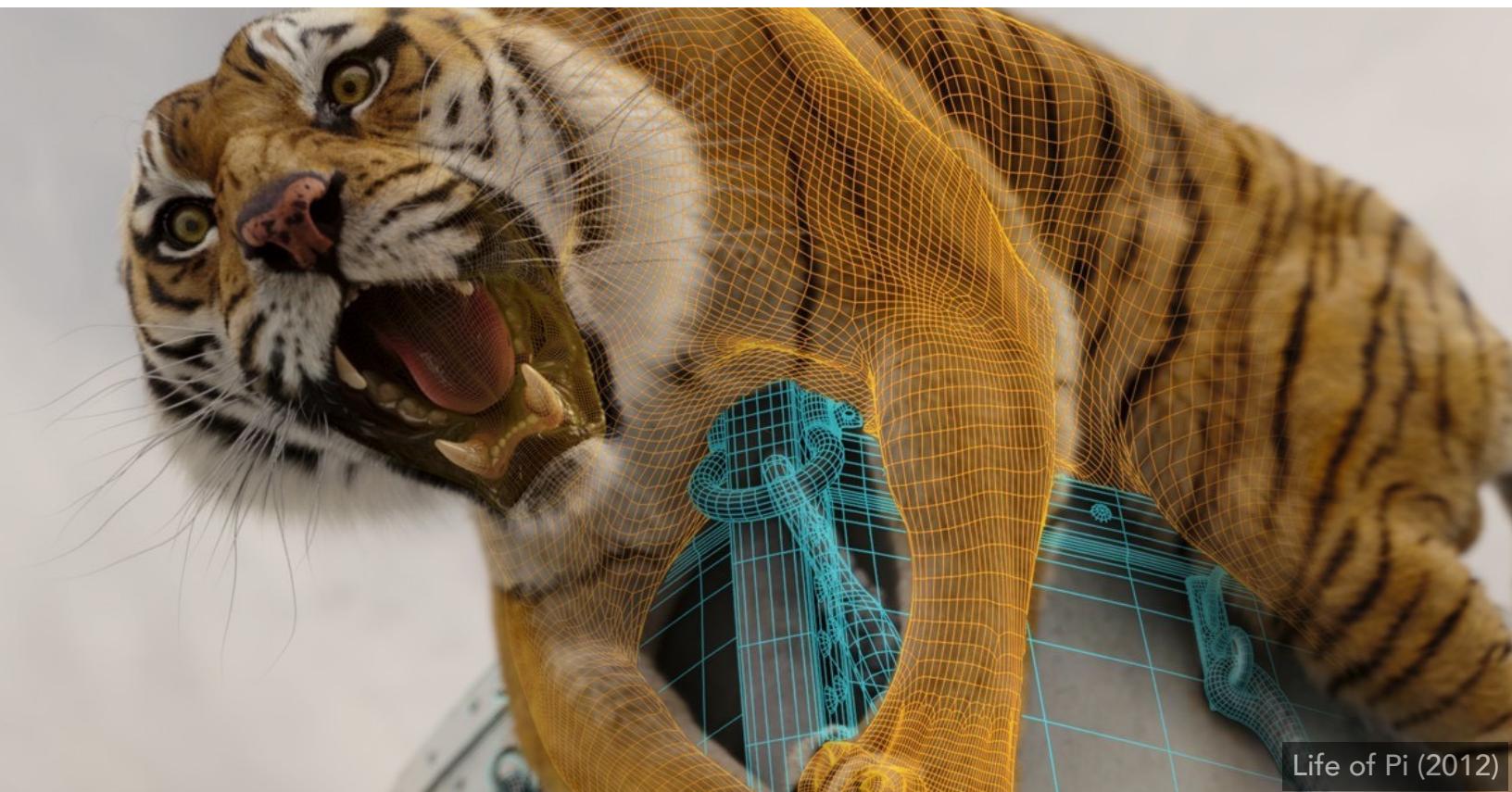
# Canonical Cube to Screen

- Irrelevant to z
- Transform in xy plane:  $[-1, 1]^2$  to  $[0, \text{width}] \times [0, \text{height}]$   
*不用做很多矩阵.*
- Viewport transform matrix:

*从 scale 到 translate*

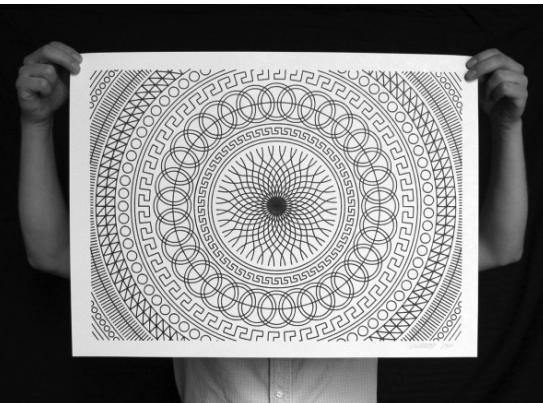
$$M_{viewport} = \begin{pmatrix} \frac{\text{width}}{2} & 0 & 0 & \frac{\text{width}}{2} \\ 0 & \frac{\text{height}}{2} & 0 & \frac{\text{height}}{2} \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

# Next: Rasterizing Triangles into Pixels



# Drawing Machines

# CNC Sharpie Drawing Machine



Aaron Panone with Matt W. Moore

<http://44rn.com/projects/numerically-controlled-poster-series-with-matt-w-moore/>

# Laser Cutters

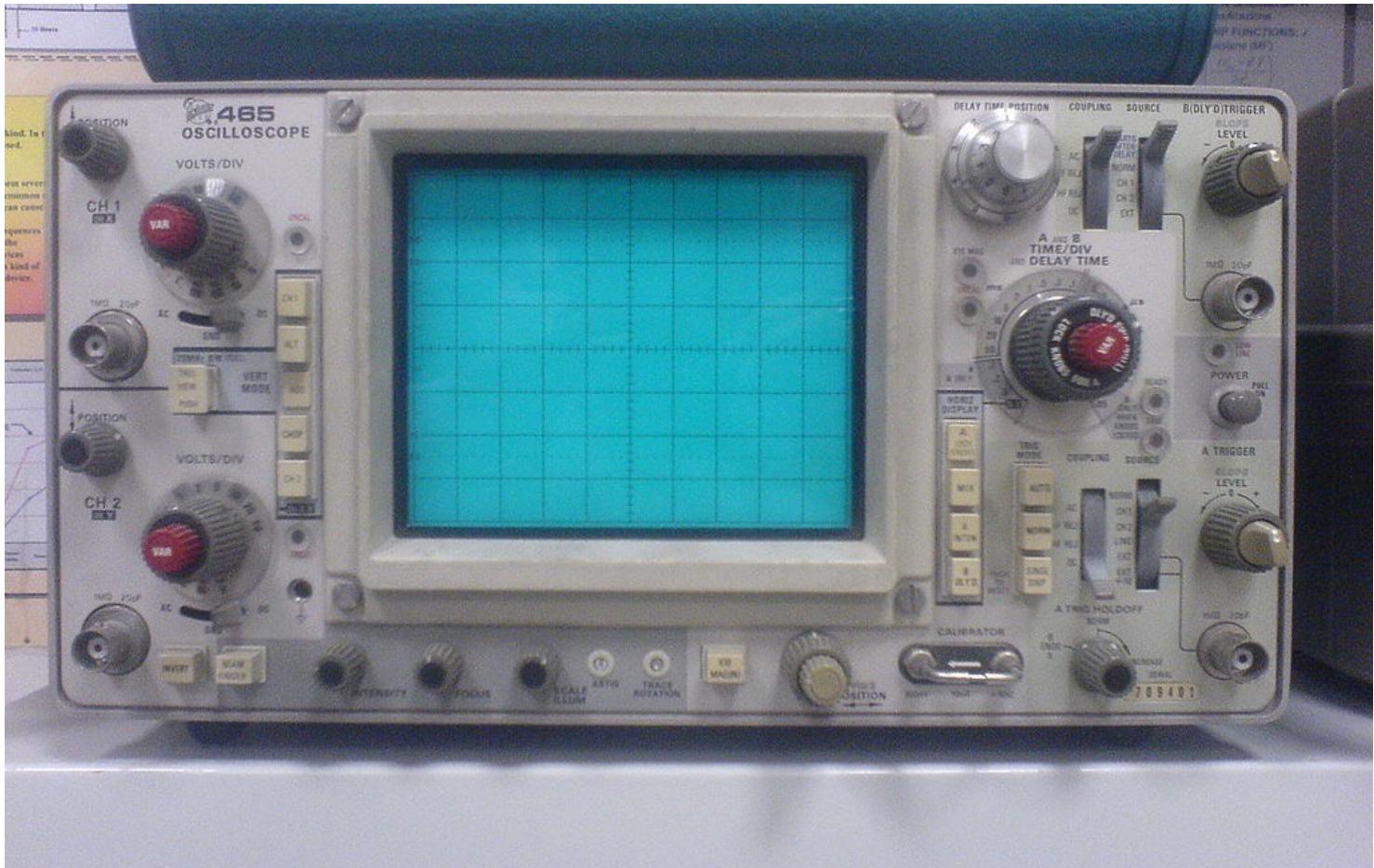


JACOBS HALL  
**WALL PANEL**  
CONCEPT COMPETITION

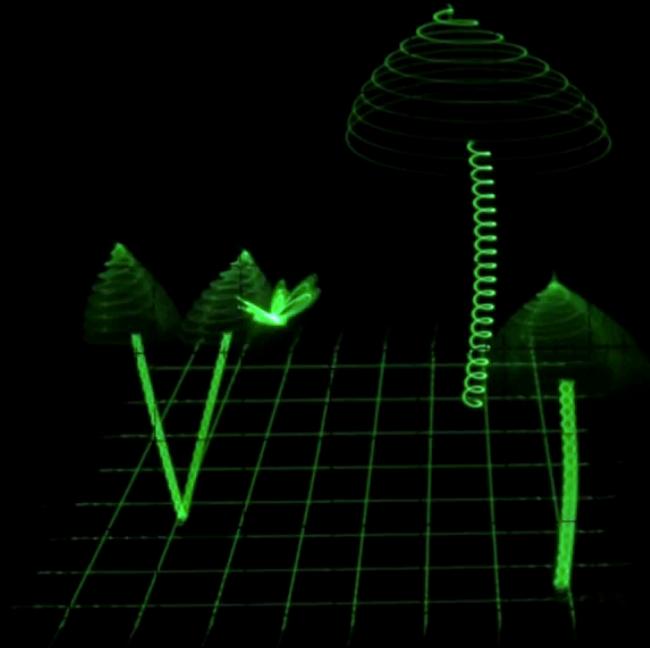


# Different Raster Displays

# Oscilloscope



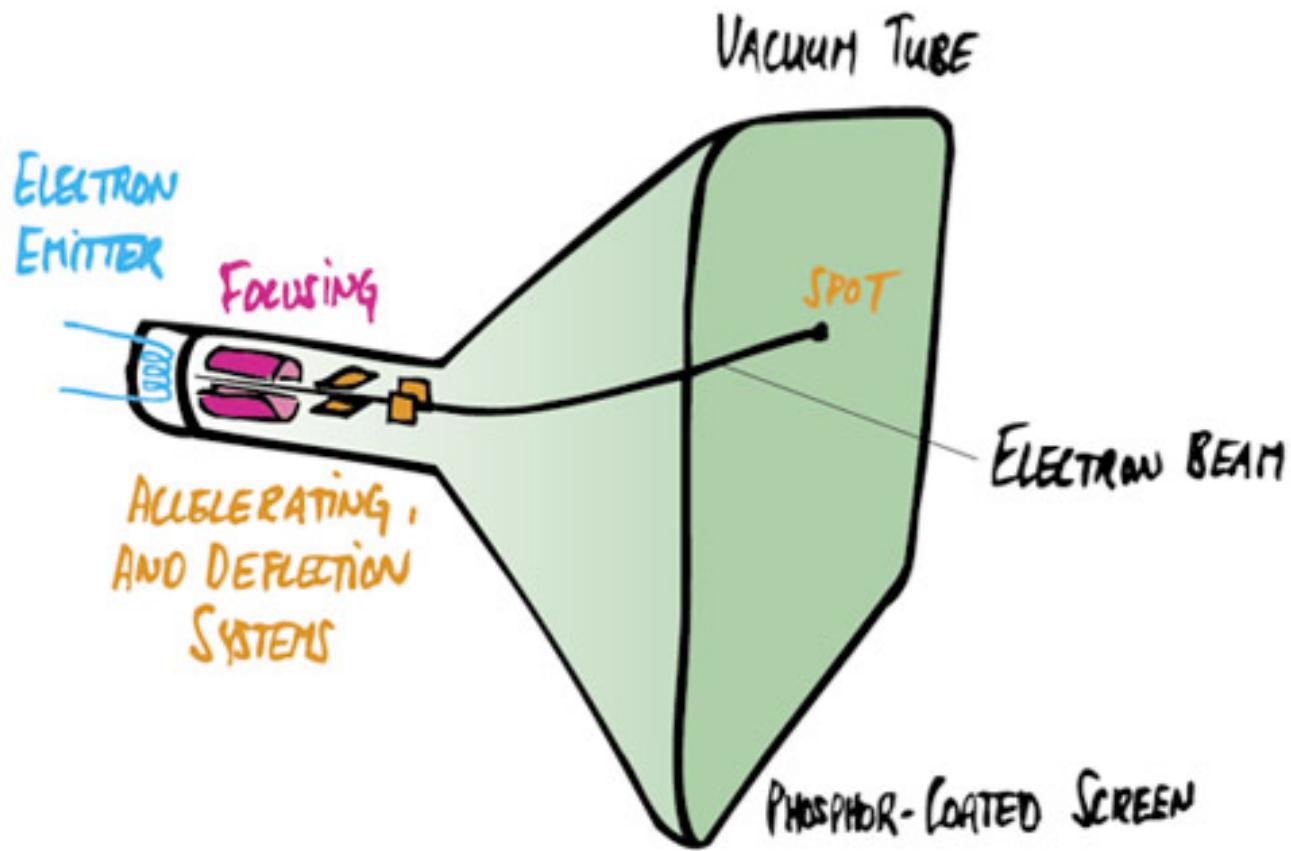
# Oscilloscope Art



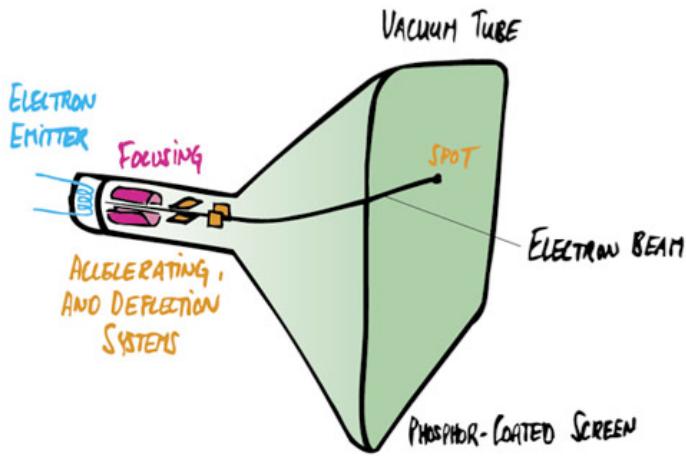
Jerobeam Fenderson

<https://www.youtube.com/watch?v=rtR63-ecUNo>

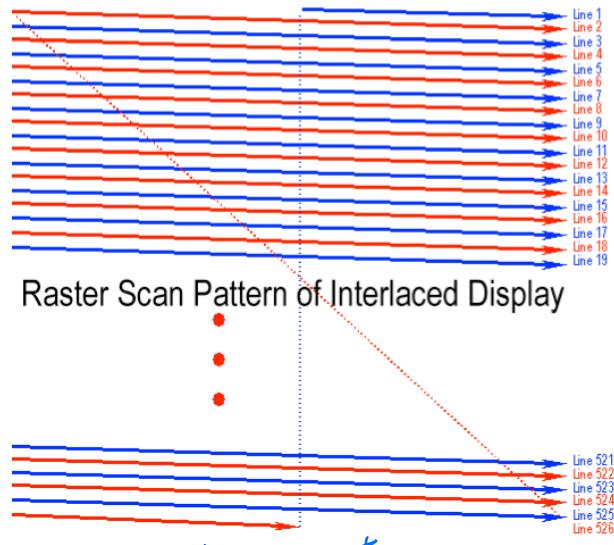
# Cathode Ray Tube



# Television - Raster Display CRT



阴极射线管  
Cathode Ray Tube



光栅扫描  
Raster Scan  
(modulate intensity)

# Frame Buffer: Memory for a Raster Display

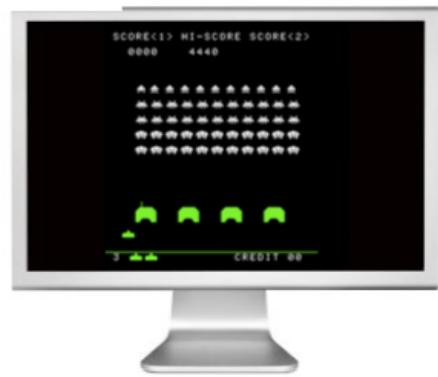


**DAC =  
Digital to Analog Convertors**

**Analog**



**Digital**



**Image = 2D array of colors**

# Flat Panel Displays



Low-Res LCD Display



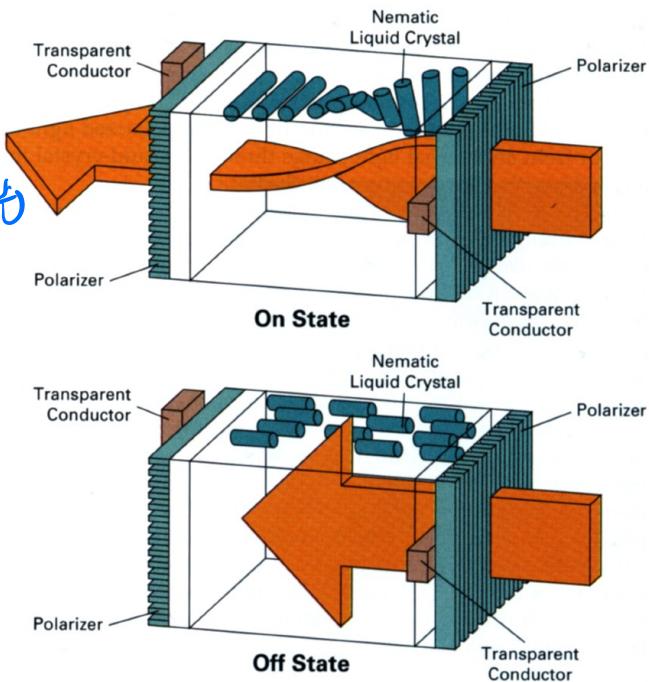
Color LCD, OLED, ...

# LCD (Liquid Crystal Display) Pixel

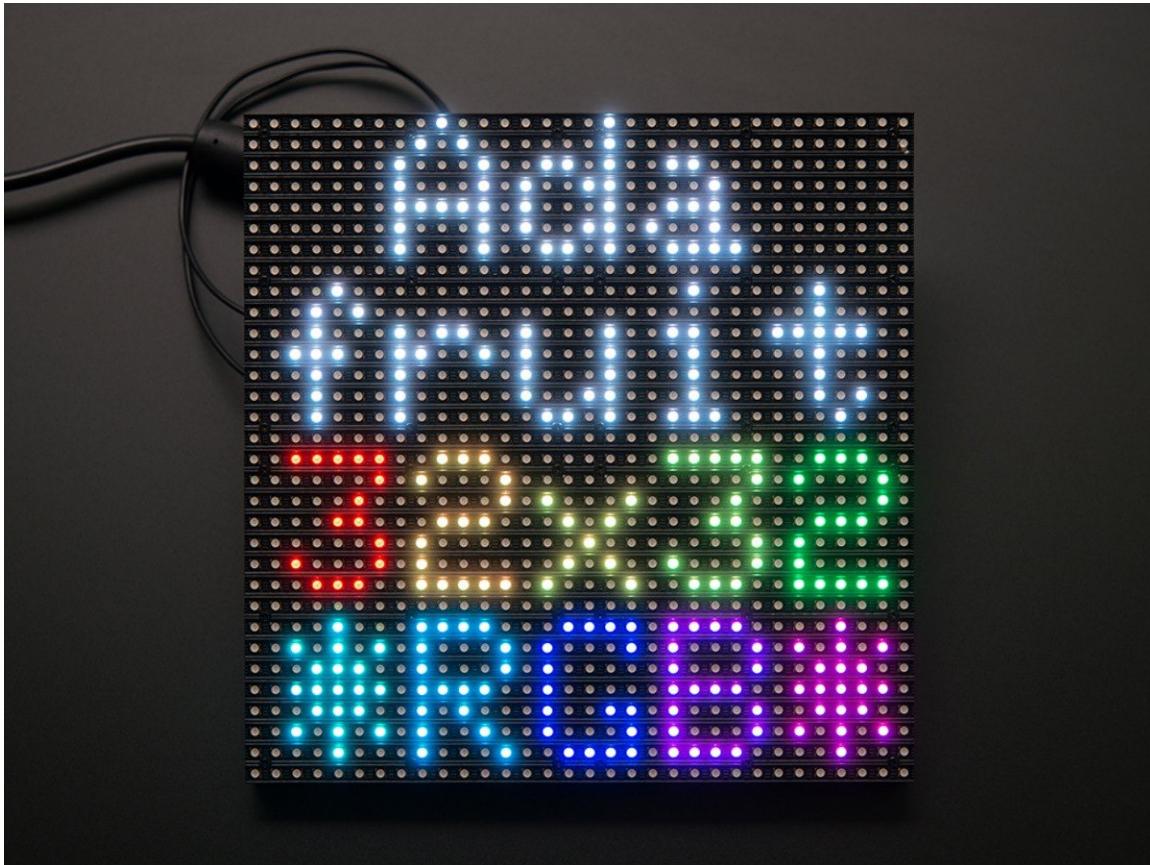
Principle: block or transmit light by twisting polarization  
扭曲偏振光

Illumination from backlight  
 (e.g. fluorescent or LED)

Intermediate intensity levels by partial twist



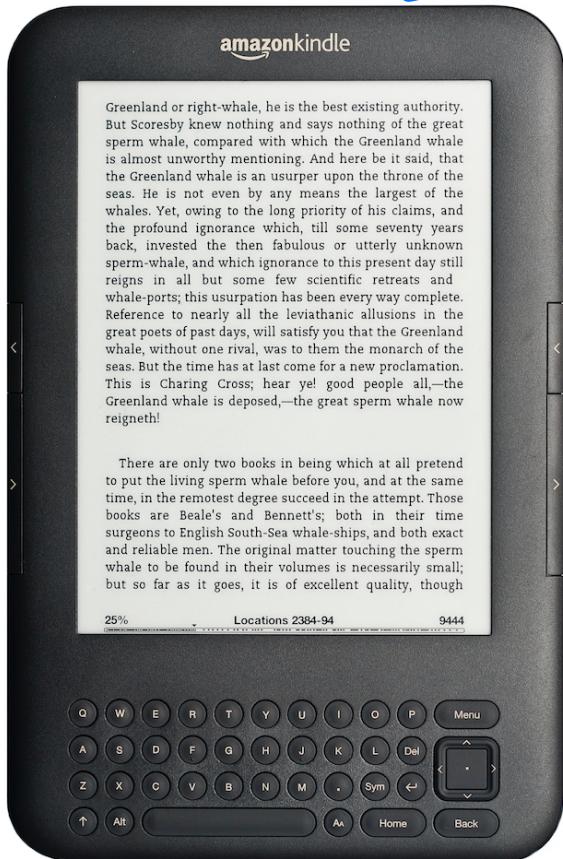
# LED Array Display



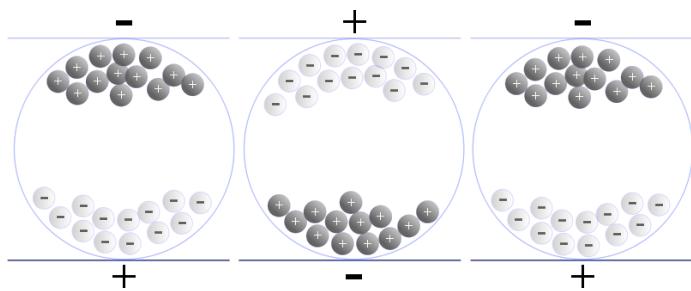
Light emitting diode array  
发光二极管阵列

# Electrophoretic (Electronic Ink) Display

电泳(电子墨水)显示.



电泳：刷新率很快。



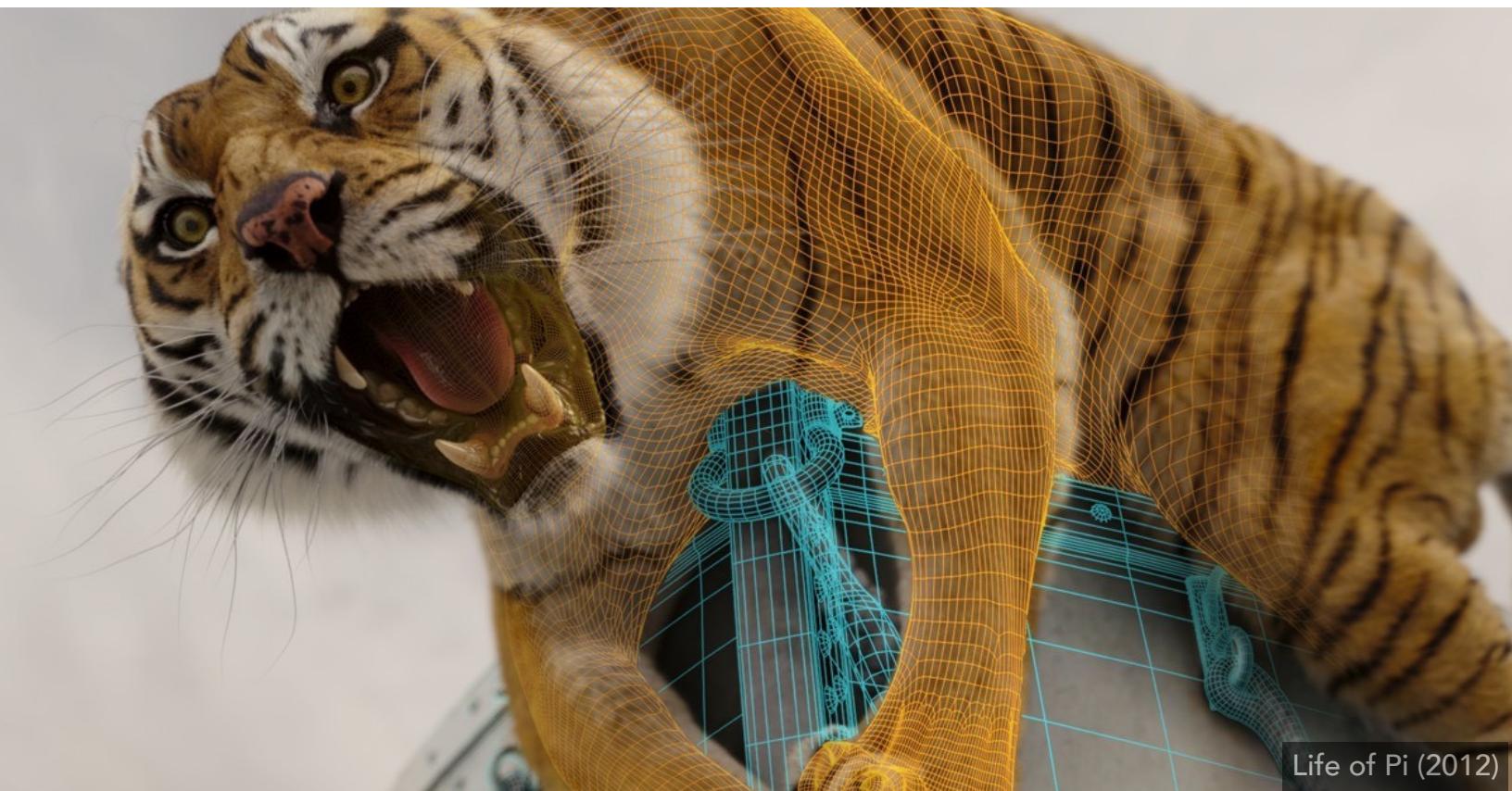
光栅化

Rasterization:

Drawing to Raster Displays

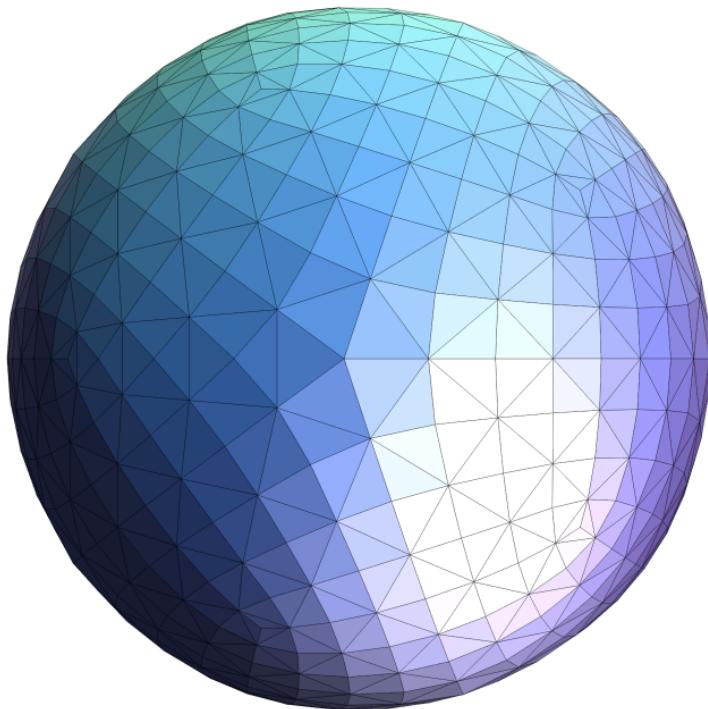
绘制到光栅显示

# Polygon Meshes 多边形网格



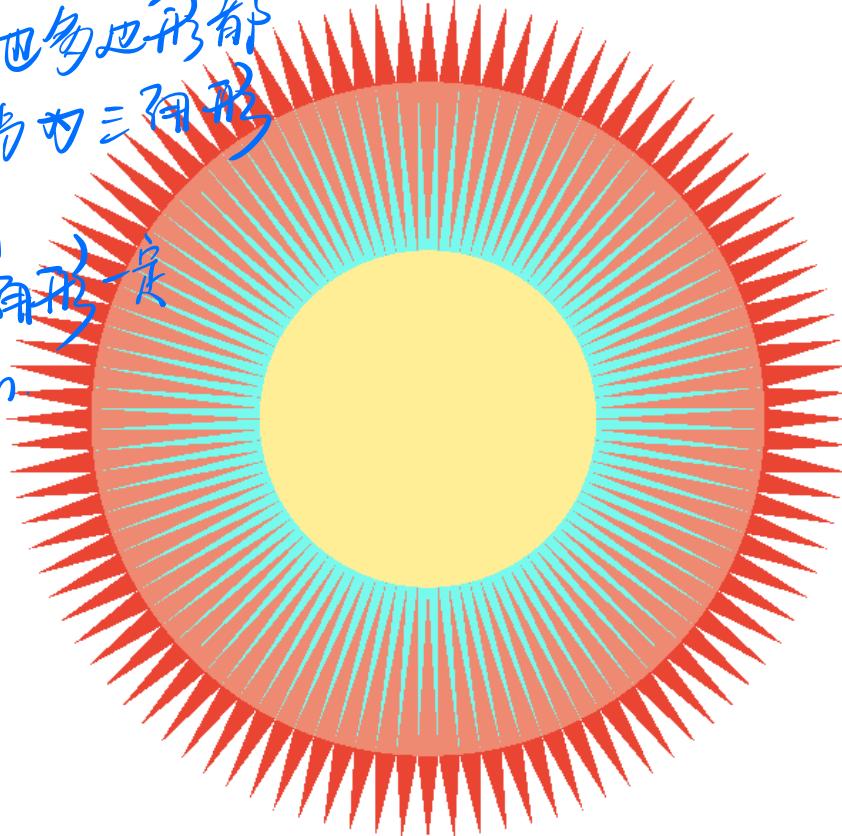
# Triangle Meshes

三角形网格.



# Triangle Meshes

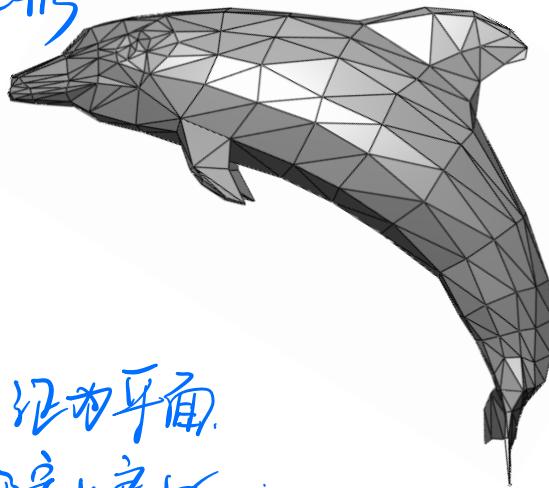
1. 最基础的多边形
2. 经何其他多边形都可以拆分为三角形
3. 给定3个点  
连成的三角形一定是平面的



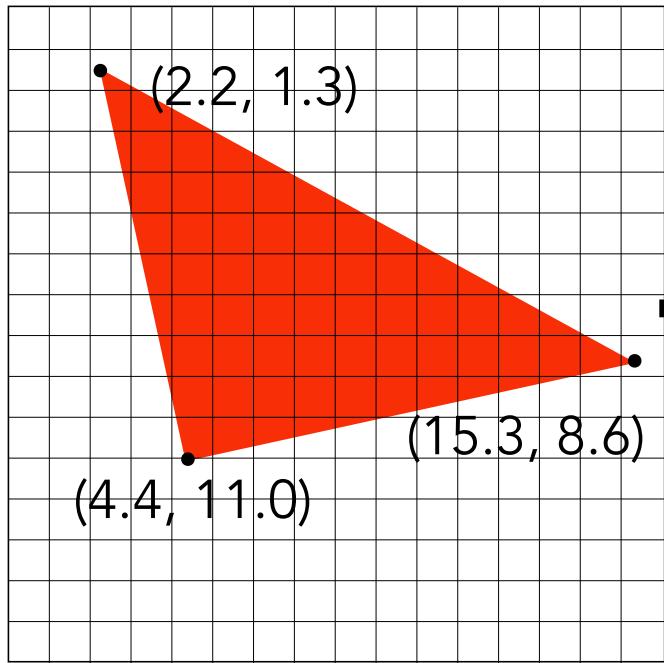
# Triangles - Fundamental Shape Primitives

Why triangles?

- Most basic polygon  
最基础多边形
- Break up other polygons  
分解其他多边形
- Unique properties
  - Guaranteed to be planar  
保证为平面.
  - Well-defined interior  
内/外部定义良好
  - Well-defined method for interpolating values at vertices over triangle (barycentric interpolation)  
重心插值

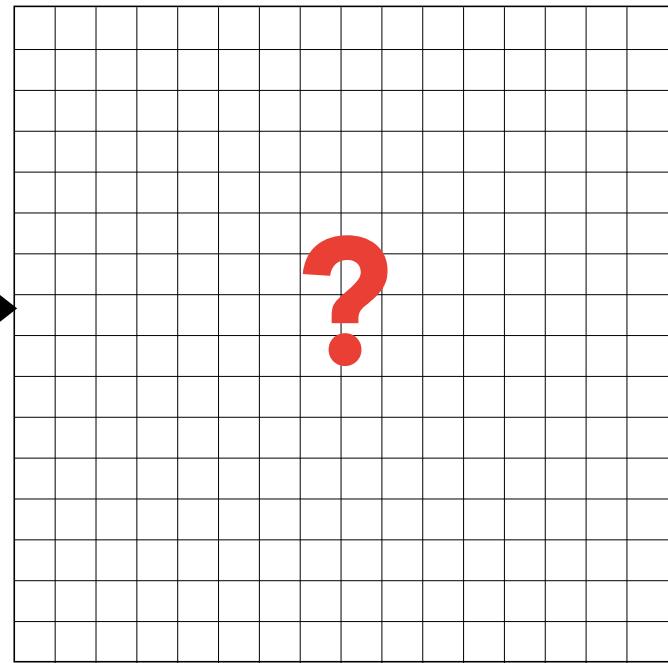


# What Pixel Values Approximate a Triangle?



Input: position of triangle  
vertices projected on screen

投影在屏幕上的一组三角形顶点位置。



Output: set of pixel values  
approximating triangle

近似三角形的像素值集

# A Simple Approach: Sampling

采样

# Sampling a Function

Evaluating a function at a point is sampling.

We can **discretize** a function by sampling.

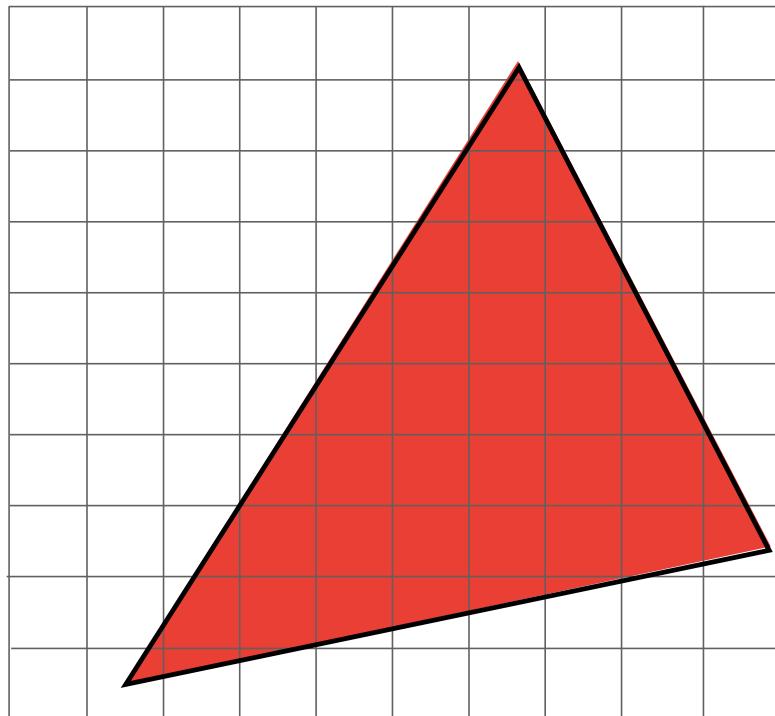
离散化

```
for (int x = 0; x < xmax; ++x)  
    output[x] = f(x);
```

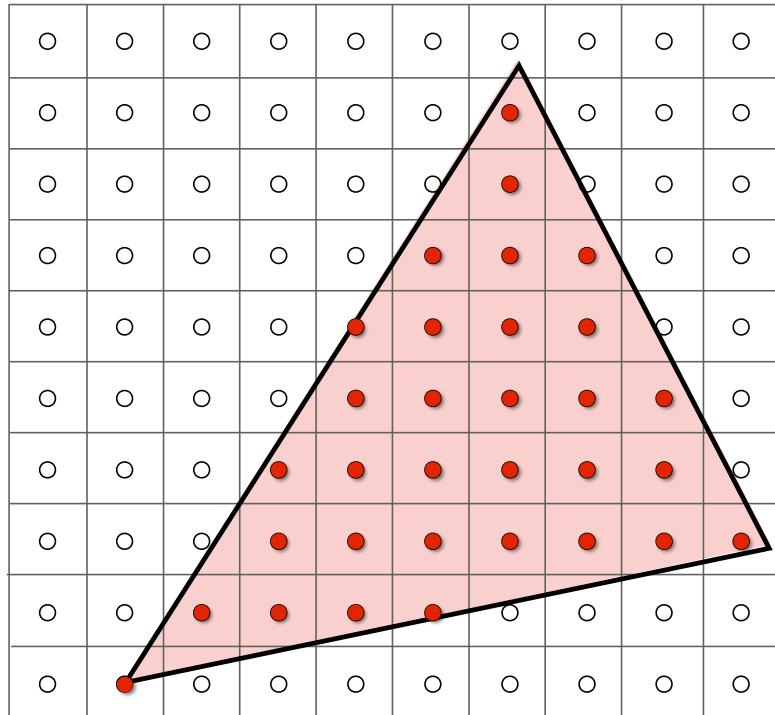
Sampling is a core idea in graphics.

We sample time (1D), area (2D), direction (2D), volume (3D) ...

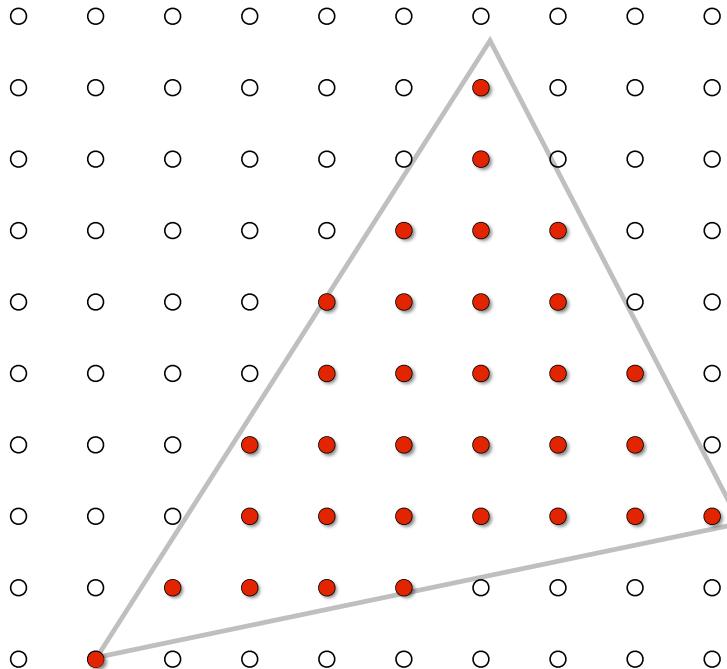
# Rasterization As 2D Sampling



# Sample If Each Pixel Center Is Inside Triangle

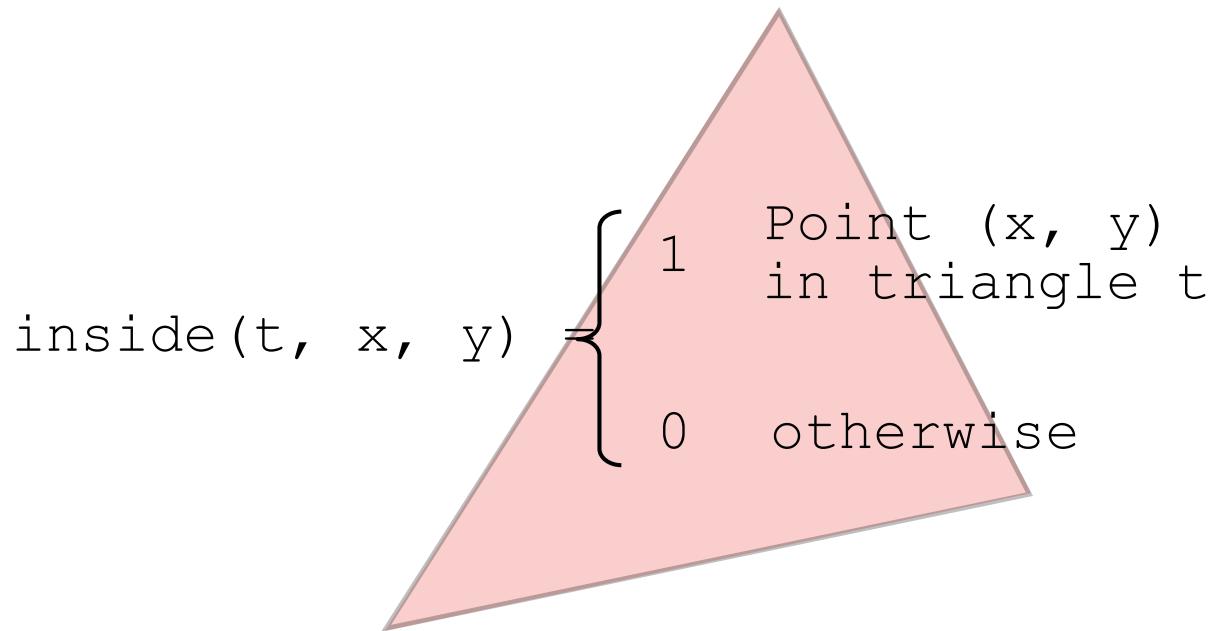


# Sample If Each Pixel Center Is Inside Triangle



# Define Binary Function: `inside(tri, x, y)`

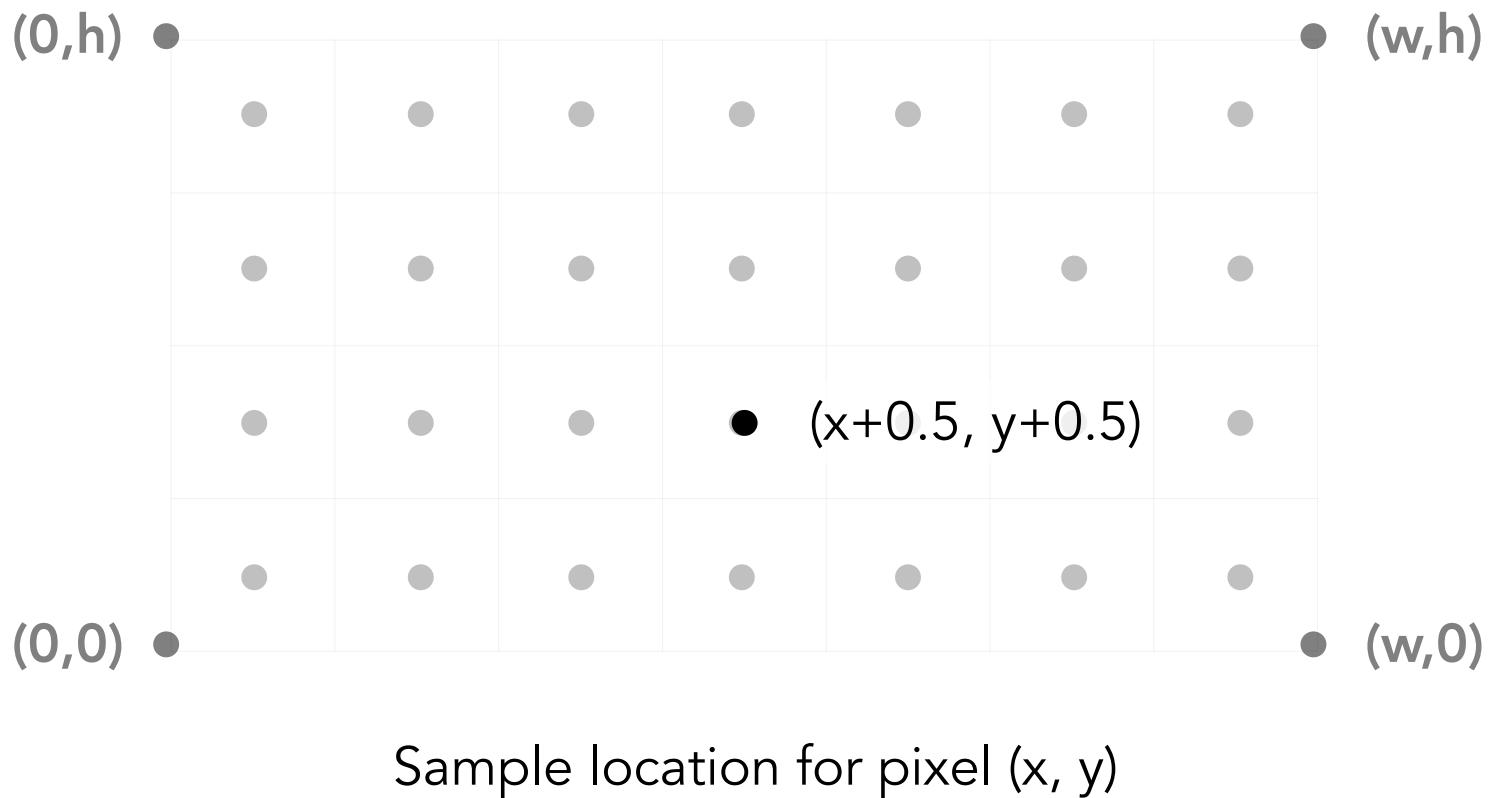
$x, y$ : not necessarily integers



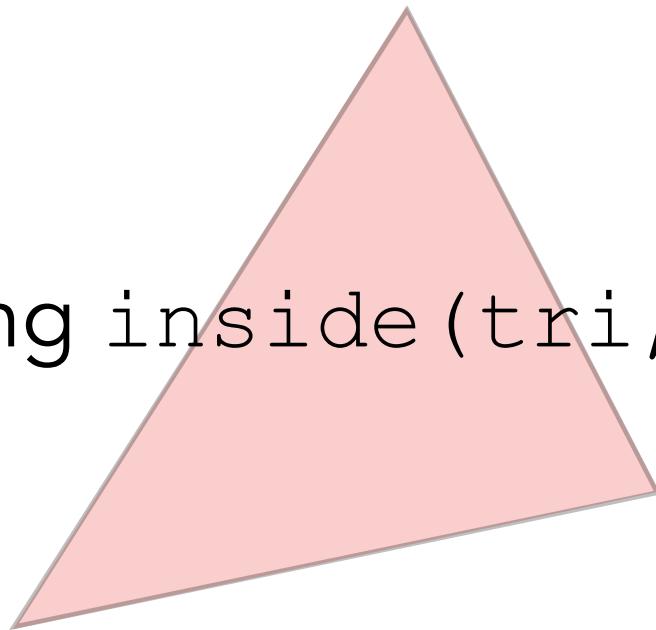
# Rasterization = Sampling A 2D Indicator Function

```
for (int x = 0; x < xmax; ++x)
    for (int y = 0; y < ymax; ++y)
        image[x][y] = inside(tri,
                             x + 0.5,
                             y + 0.5);
```

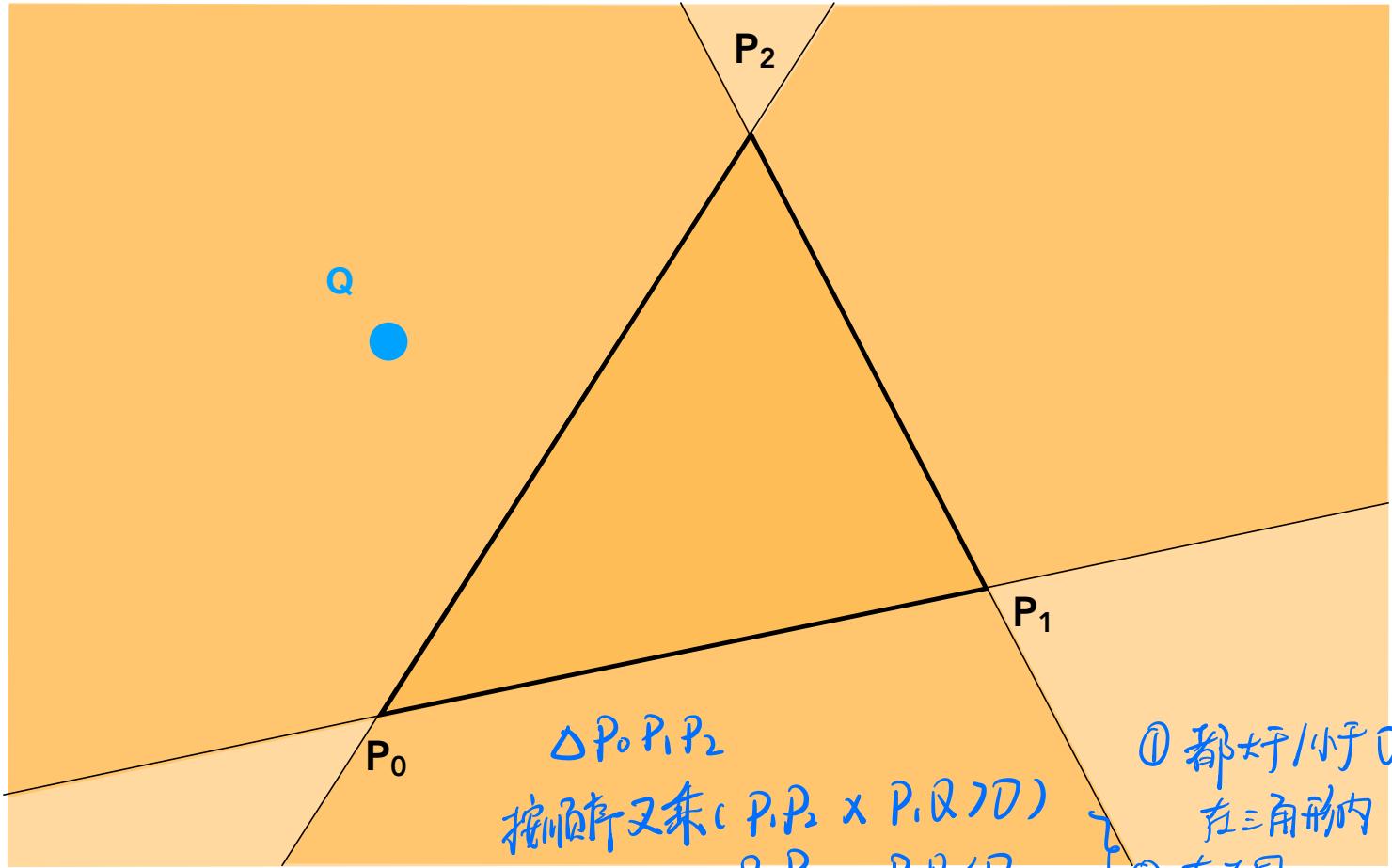
# Recall: Sample Locations



Evaluating `inside(tri, x, y)`



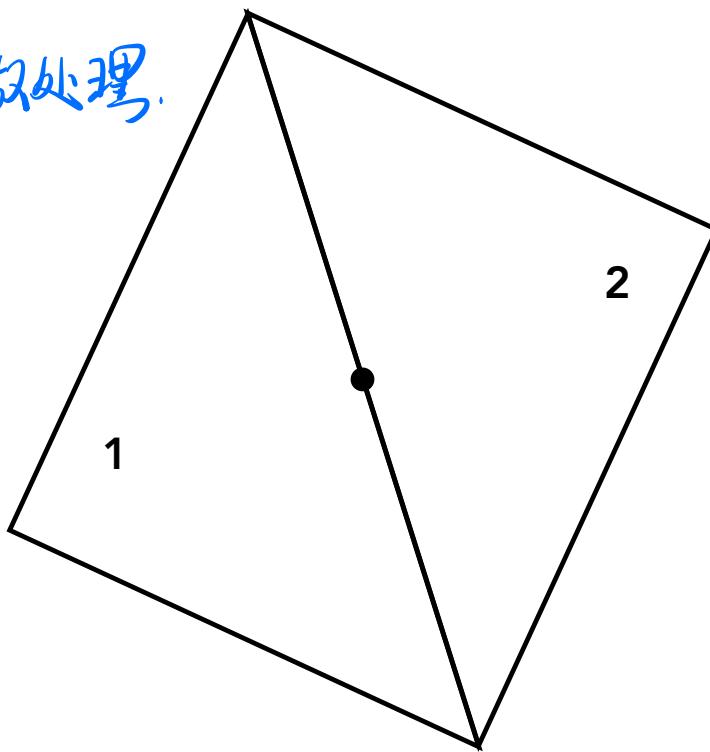
# Inside? Recall: Three Cross Products!



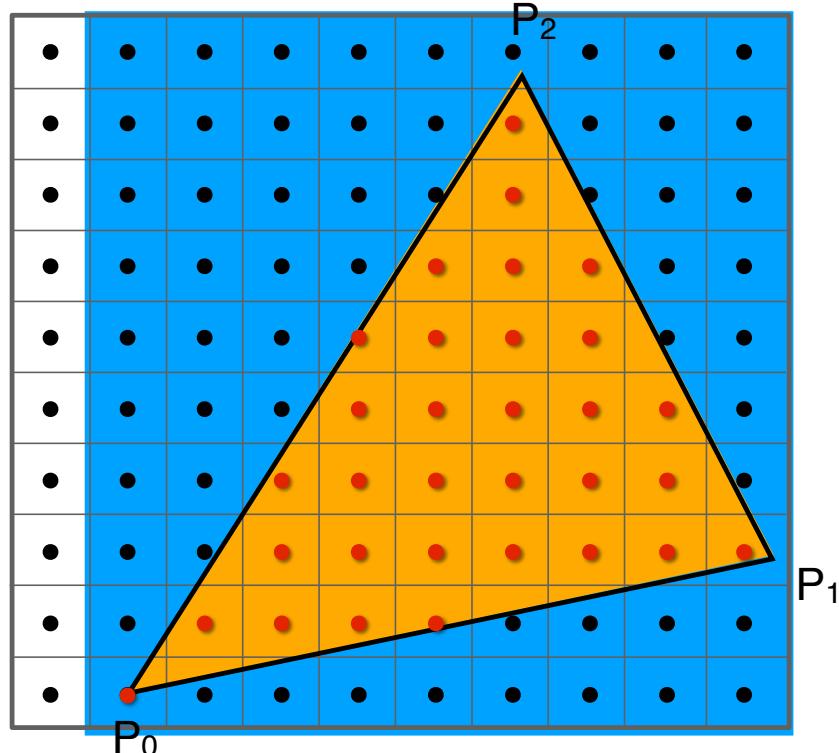
# Edge Cases (Literally)

Is this sample point covered by triangle 1, triangle 2, or both?

X 界点我们不做处理.



# Checking All Pixels on the Screen?

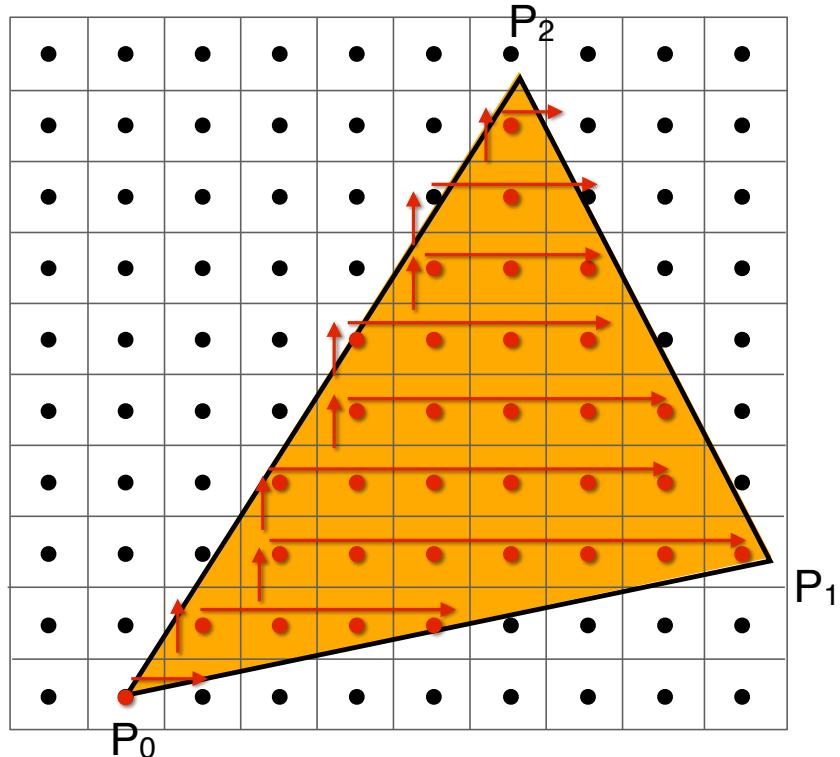


Use a **Bounding Box!**

包围盒(轴向)  $AABB$ .

增量三角形遍历

# Incremental Triangle Traversal (Faster?)



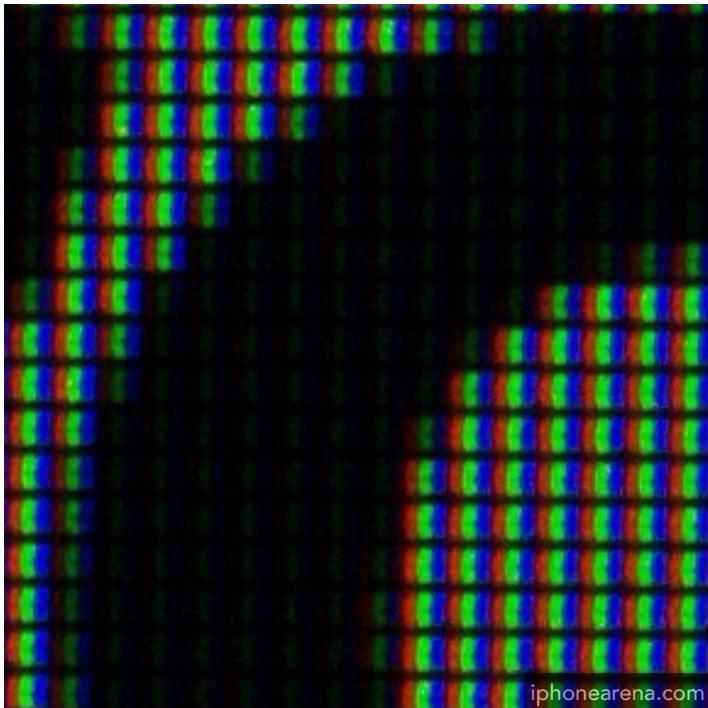
suitable for thin and rotated triangles

适用于薄且旋转的三角形

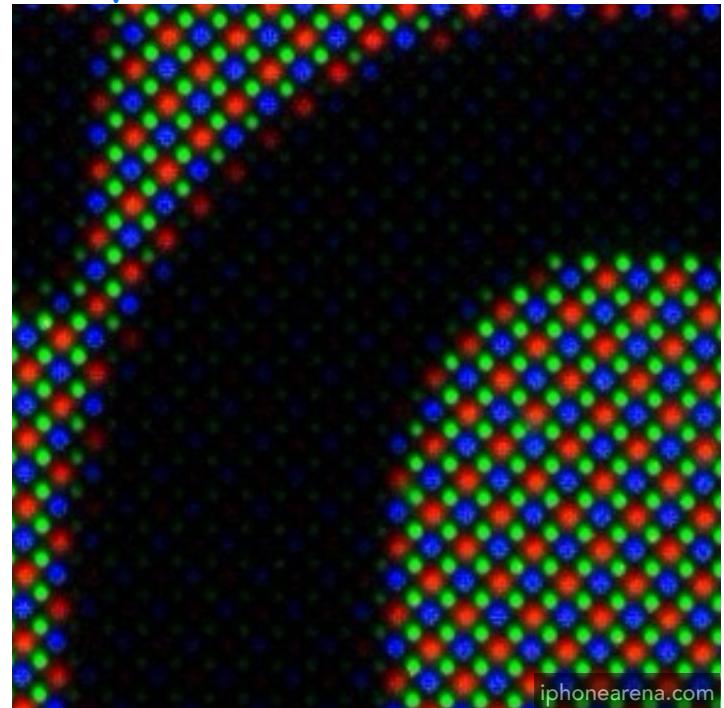
# Rasterization on Real Displays

# Real LCD Screen Pixels (Closeup)

Bayer pattern



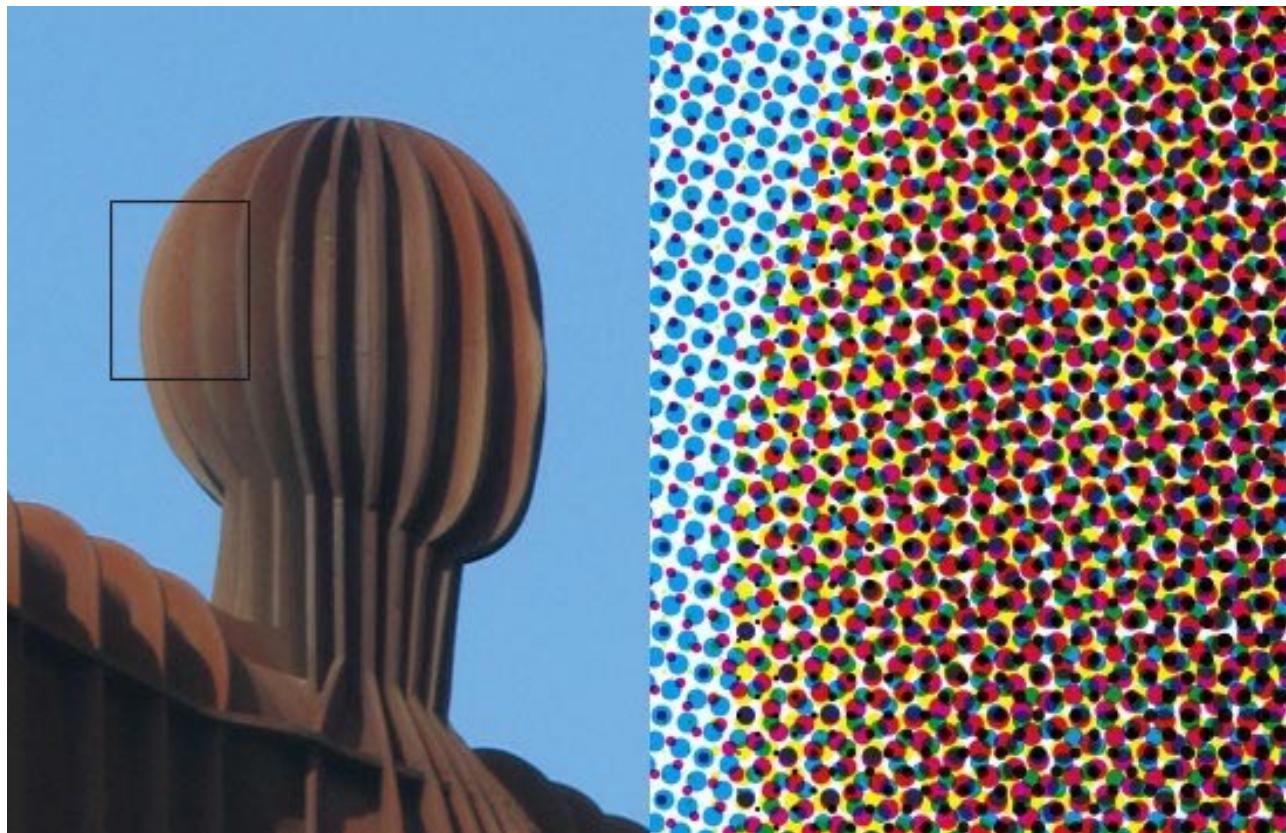
iPhone 6S



Galaxy S5

Notice R,G,B pixel geometry! But in this class, we will assume a colored square full-color pixel.

# Aside: What About Other Display Methods?



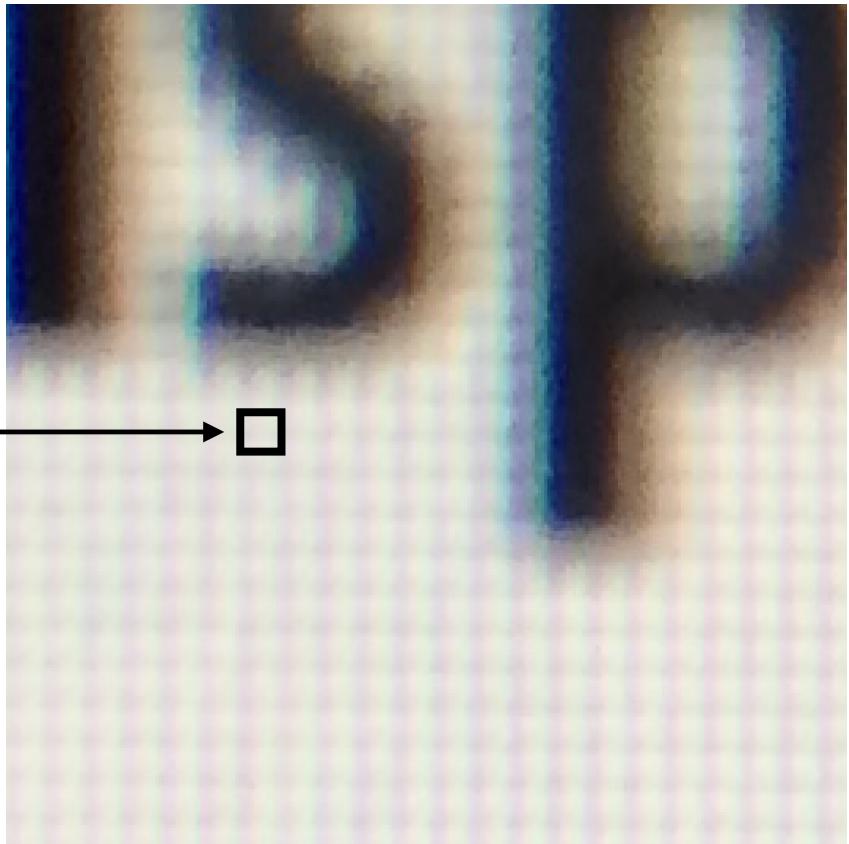
Color print: observe half-tone pattern

# Assume Display Pixels Emit Square of Light

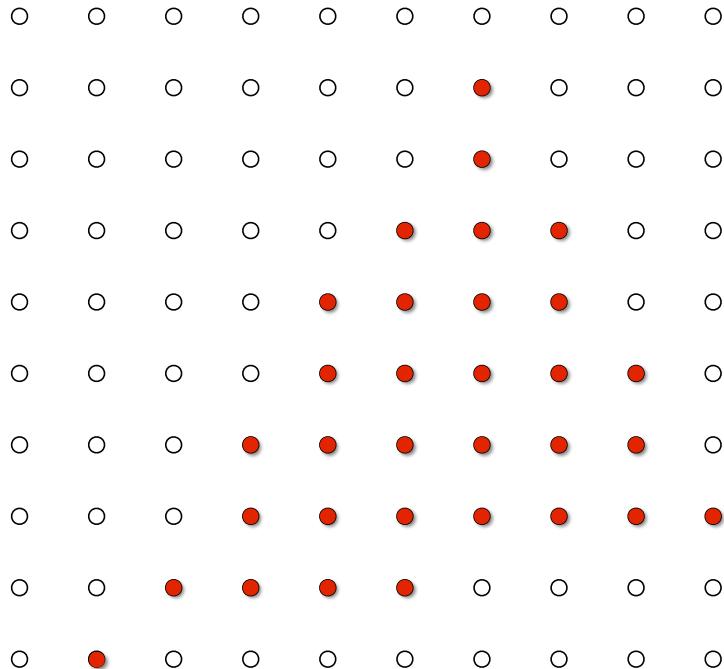
LCD pixel  
on laptop



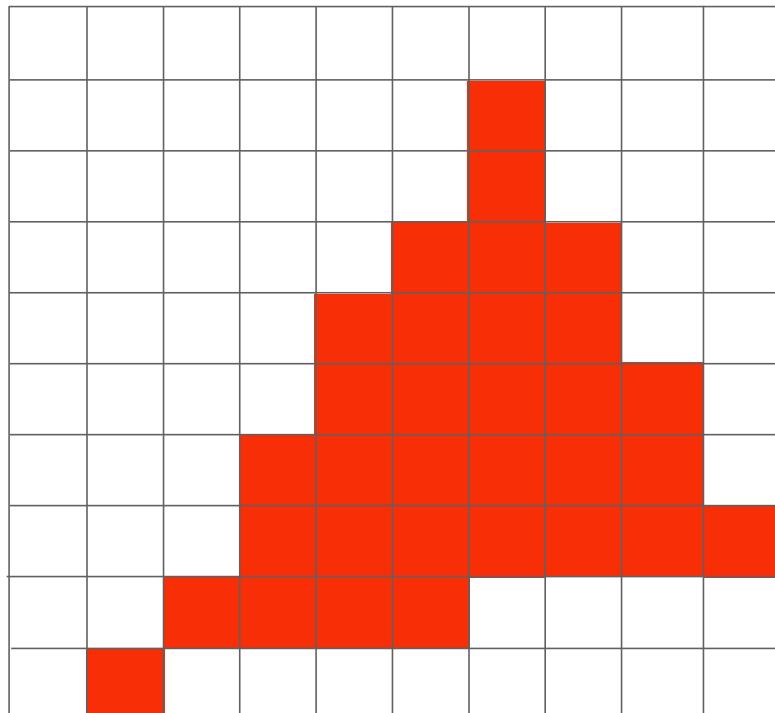
\* LCD pixels do not actually emit light in a square of uniform color, but this approximation suffices for our current discussion



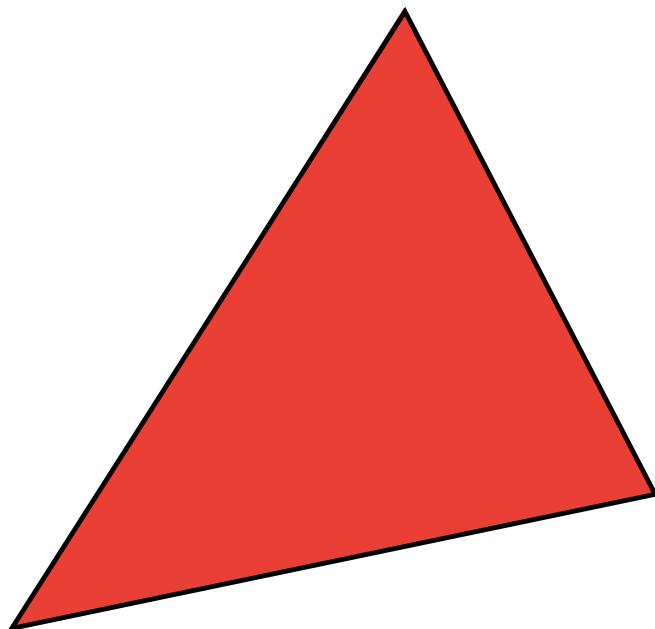
# So, If We Send the Display the Sampled Signal



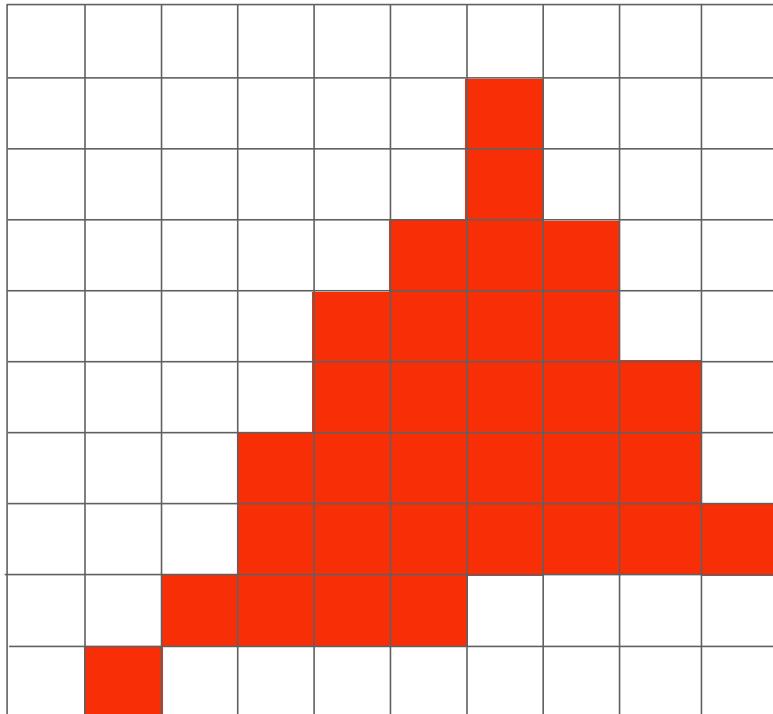
# The Display Physically Emits This Signal



# Compare: The Continuous Triangle Function

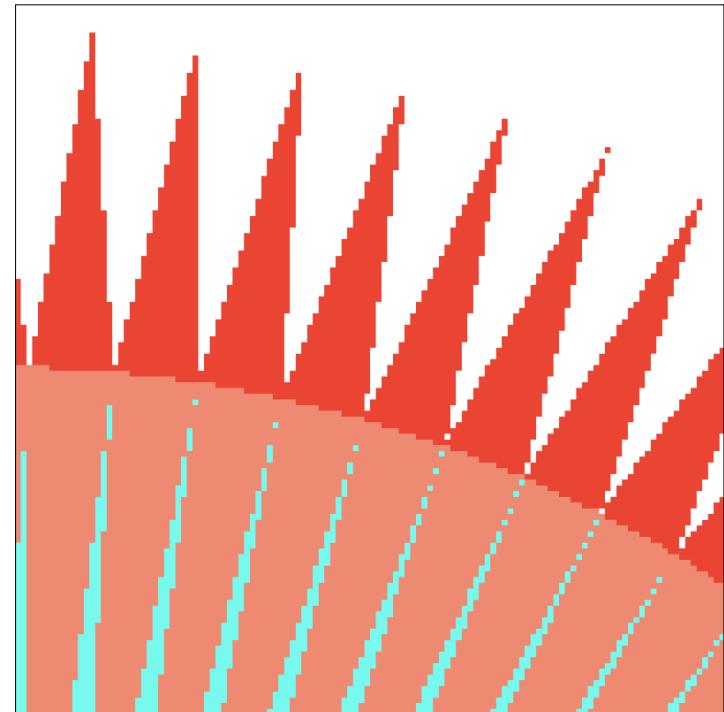
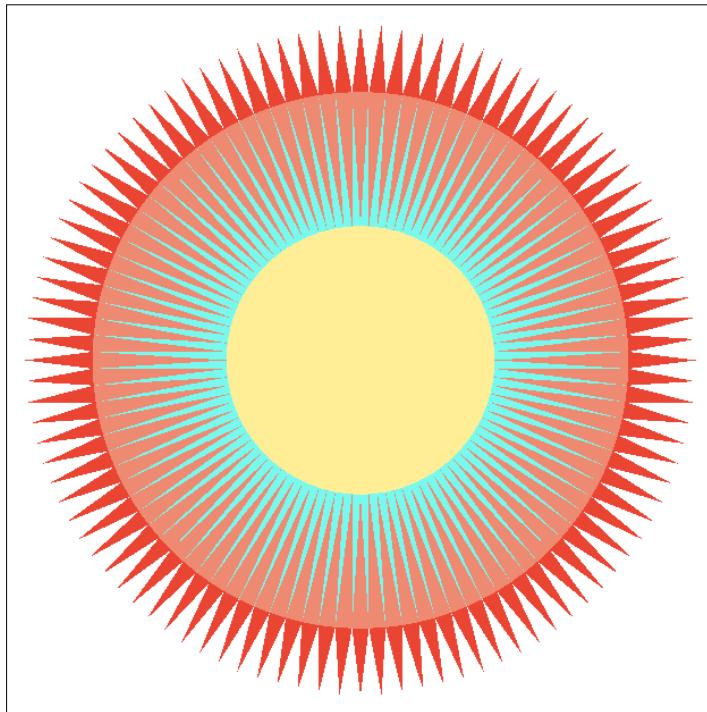


# What's Wrong With This Picture?



# 锯齿边 Jaggies!

# Aliasing (Jaggies)



Is this the best we can do?

# Thank you!

(And thank Prof. Ravi Ramamoorthi and Prof. Ren Ng for many of the slides!)