

# Real-Time High Quality Rendering

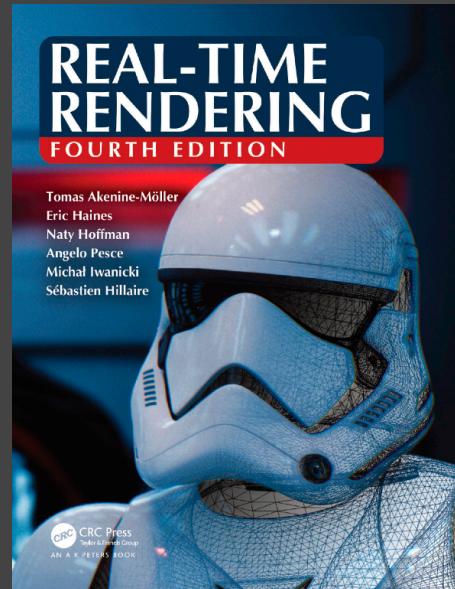
GAMES202, Lingqi Yan, UC Santa Barbara

## Lecture 3: Real-Time Shadows 1



# Announcement

- Enjoying assignment 0?
- Assignment 1 will be released this week
  - Ideally together with Lecture 4
- Adjusted orders of some contents
- The RTR book



# Last Lecture

- Recap of CG Basics
  - Basic GPU hardware pipeline
  - OpenGL
  - OpenGL Shading Language (GLSL)
  - The Rendering Equation
  - Calculus

# Today

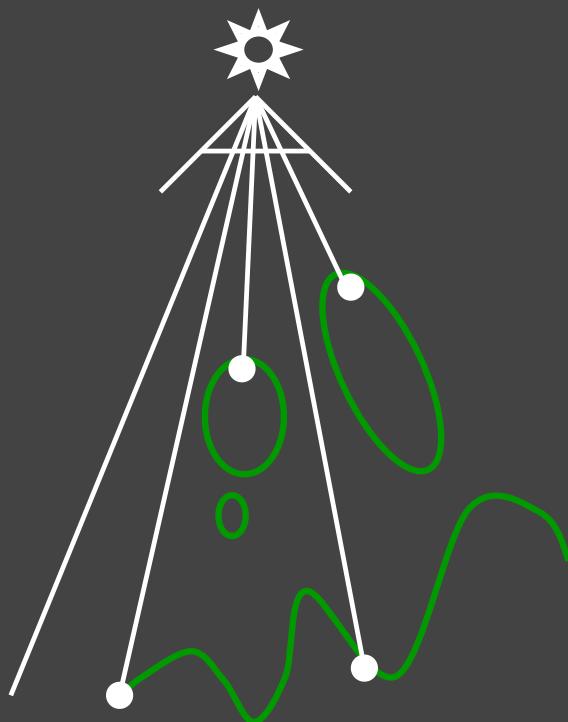
- Recap: shadow mapping  
[slides courtesy of Prof. Ravi Ramamoorthi]
  - Issues from shadow mapping and solutions
- The math behind shadow mapping
- Percentage closer soft shadows
- Basic filtering techniques

# Shadow Mapping

- A 2-Pass Algorithm
  - The light pass generates the SM
  - The camera pass uses the SM (recall last lecture)
- An image-space algorithm
  - Pro: no knowledge of scene's geometry is required
  - Con: causing self occlusion and aliasing issues
- Well known shadow rendering technique
  - Basic shadowing technique even for early offline renderings, e.g., Toy Story

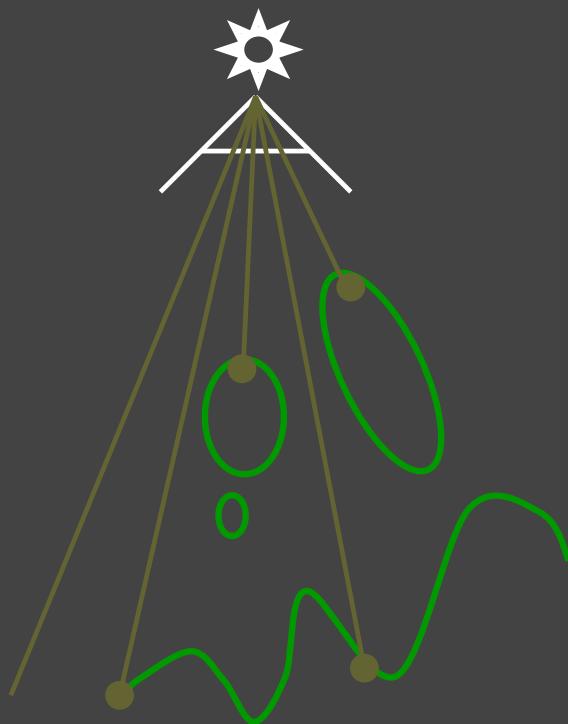
# Pass 1: Render from Light

- Output a “depth texture” from the light source



# Pass 1: Render from Light

- Output a “depth texture” from the light source



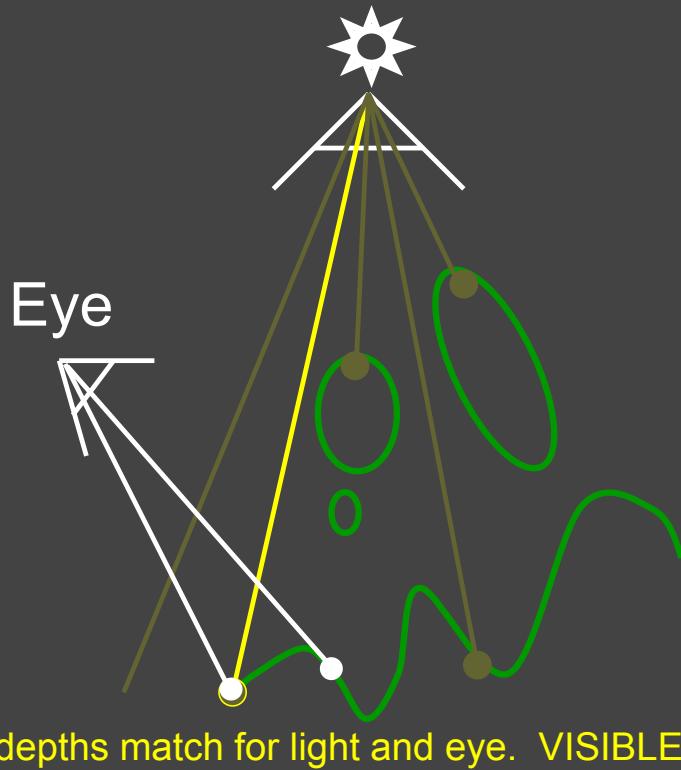
# Pass 2: Render from Eye

- Render a standard image from the eye



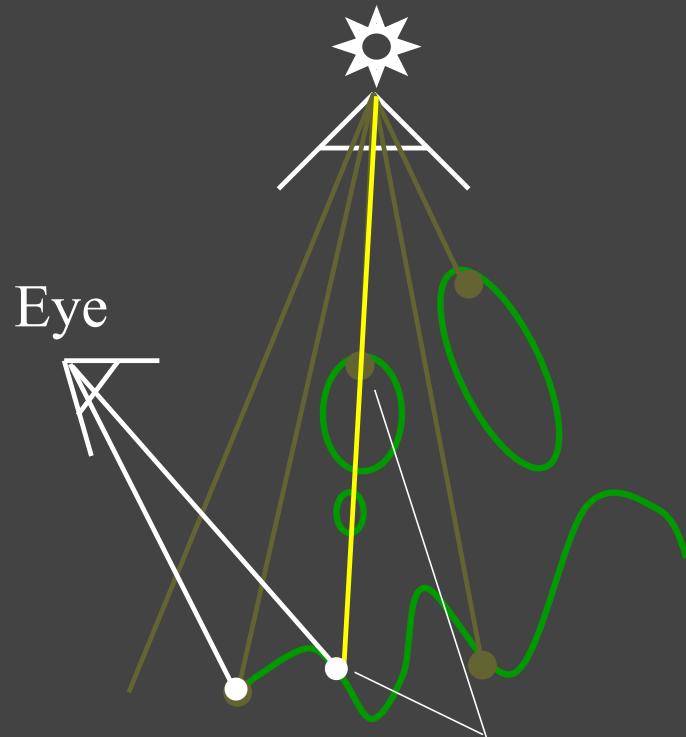
# Pass 2: Project to light for shadows

- Project visible points in eye view back to light source



# Pass 2: Project to light for shadows

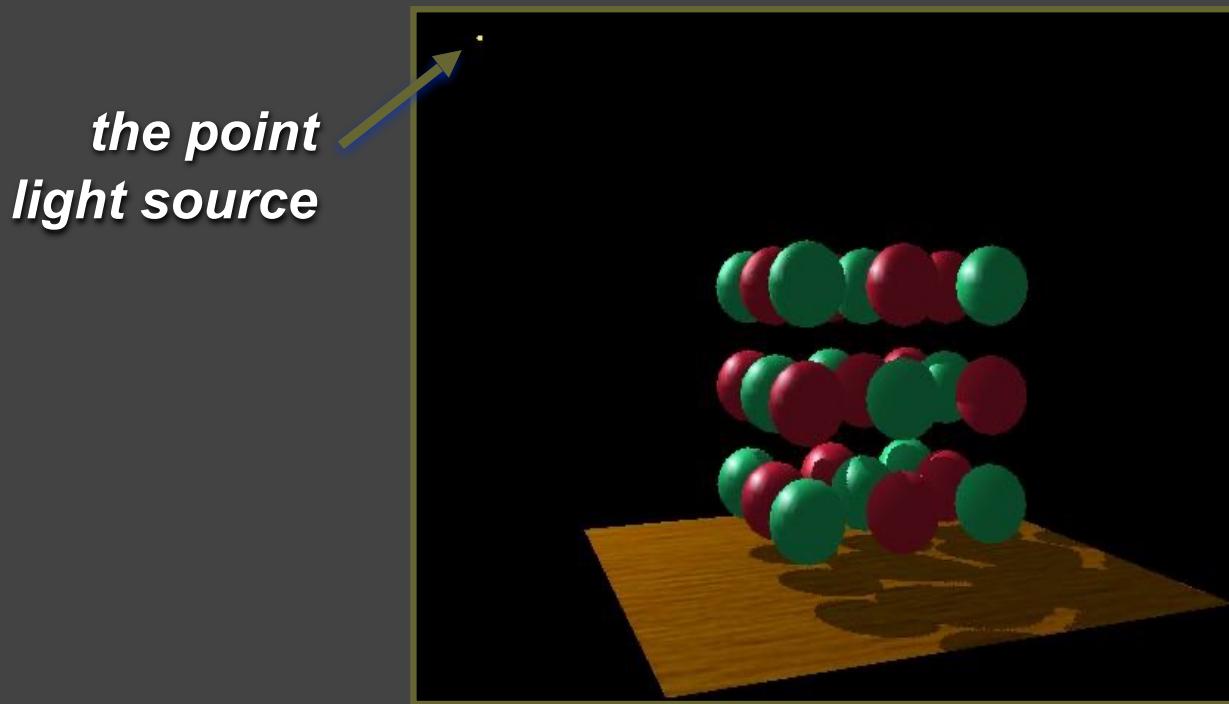
- Project visible points in eye view back to light source



(Reprojected) depths from light, eye not the same. **BLOCKED!!**

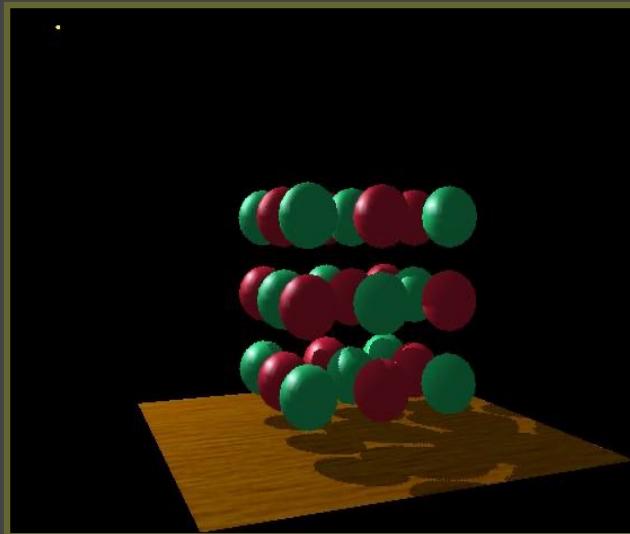
# Shadow Mapping Results

- A fairly complex scene with shadows

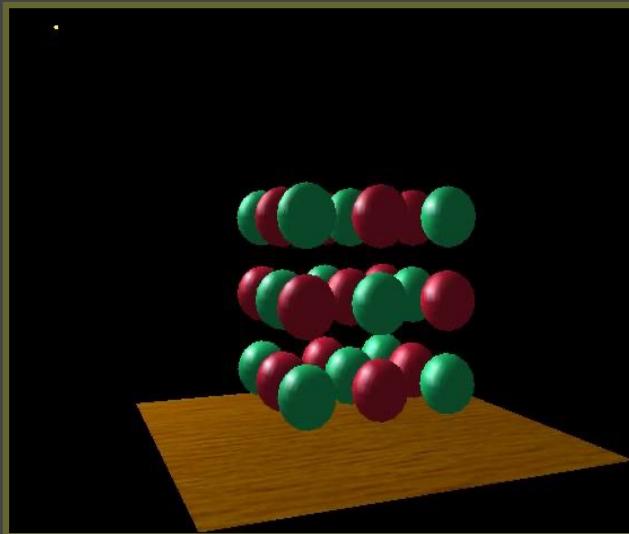


# Shadow Mapping Results

- Compare with and without shadows



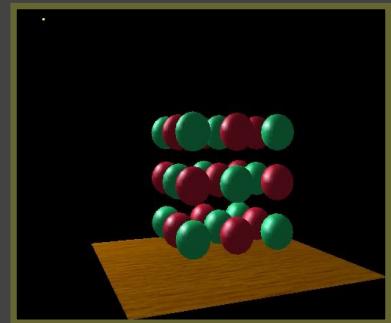
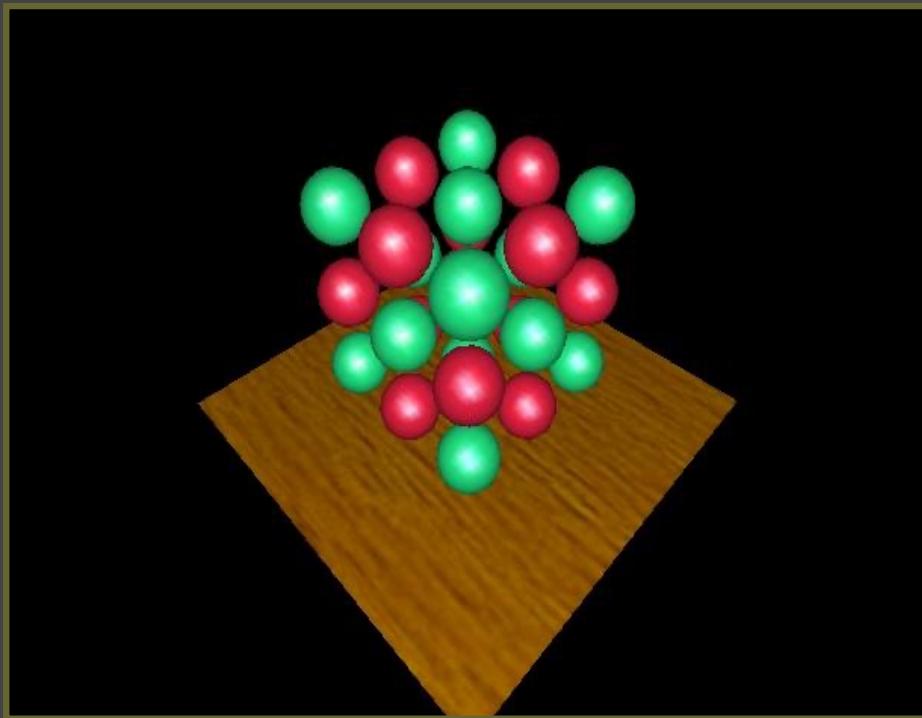
*with shadows*



*without shadows*

# Visualizing Shadow Mapping

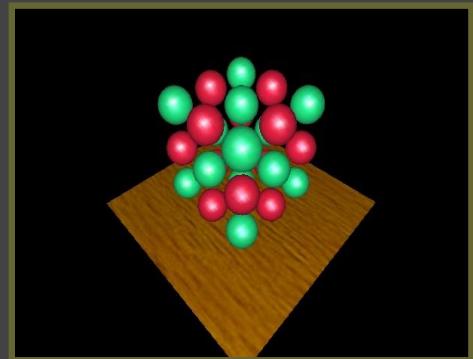
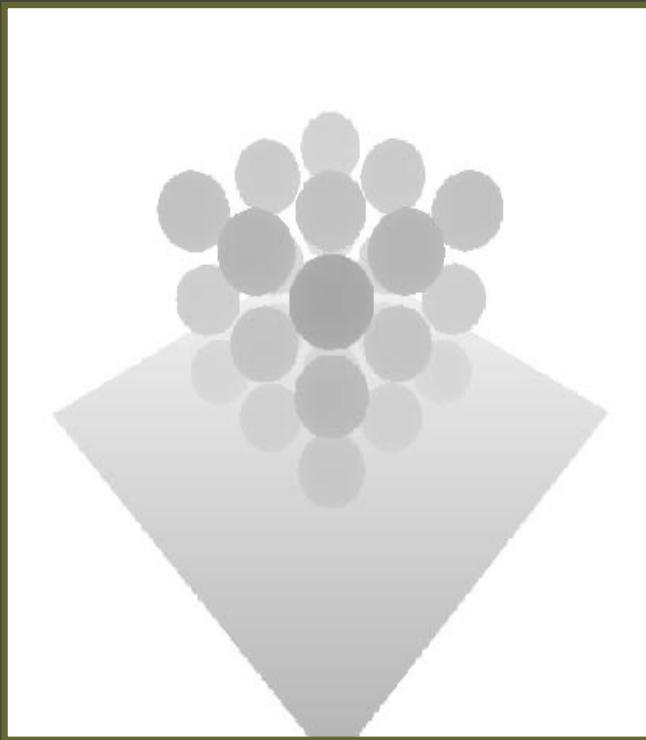
- The scene from the light's point-of-view



*FYI: from the  
eye's point-of-view  
again*

# Visualizing Shadow Mapping

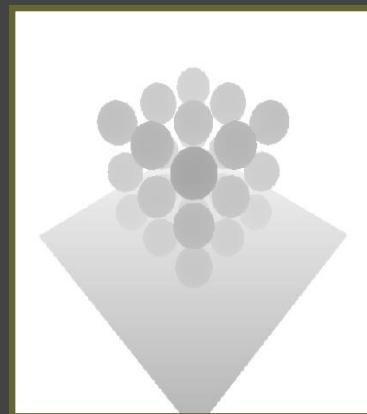
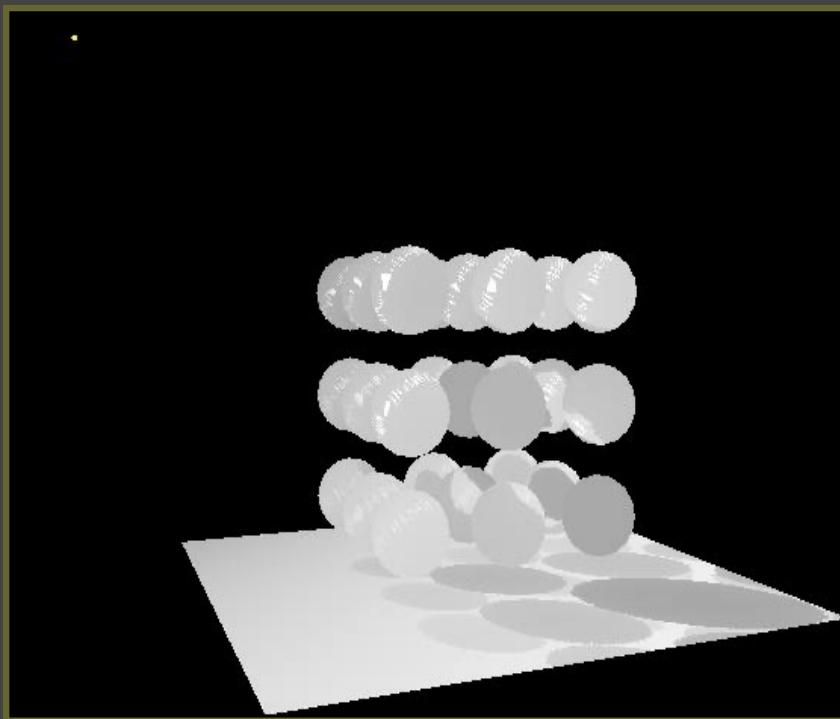
- The depth buffer from the light's point-of-view



*FYI: from the  
light's point-of-view  
again*

# Visualizing Shadow Mapping

- Projecting the depth map onto the eye's view

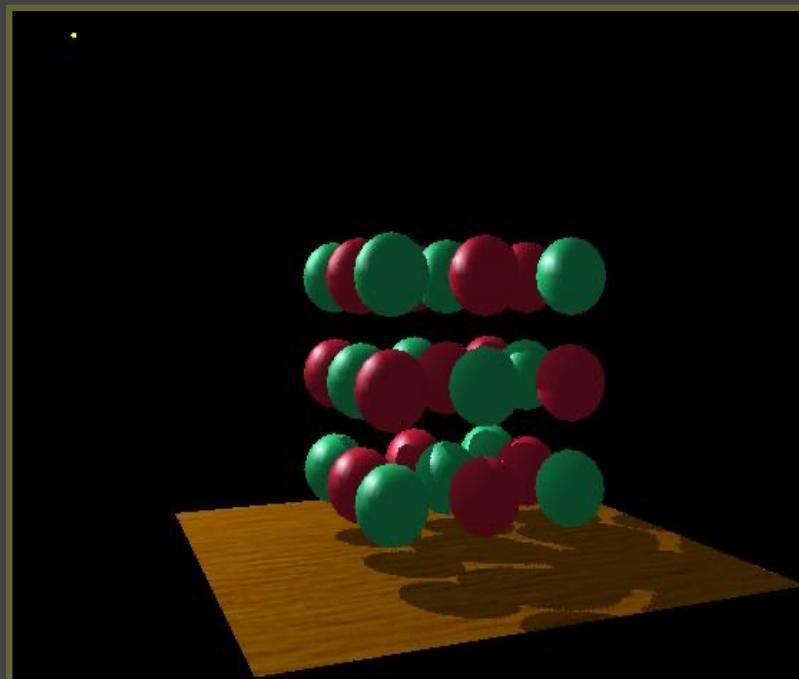


*FYI: depth map for  
light's point-of-view  
again*

# Visualizing Shadow Mapping

- Scene with shadows

*Notice how  
specular  
highlights  
never appear  
in shadows*



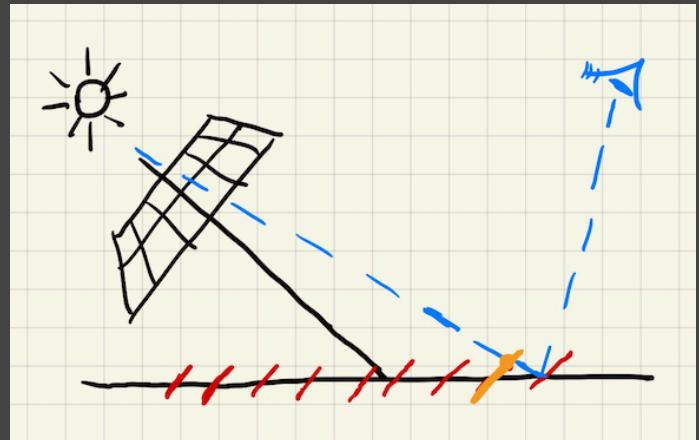
*Notice how  
curved  
surfaces cast  
shadows on  
each other*

# Issues in Shadow Mapping

- Self occlusion
  - When is it most severe?



[Image from RTR4]

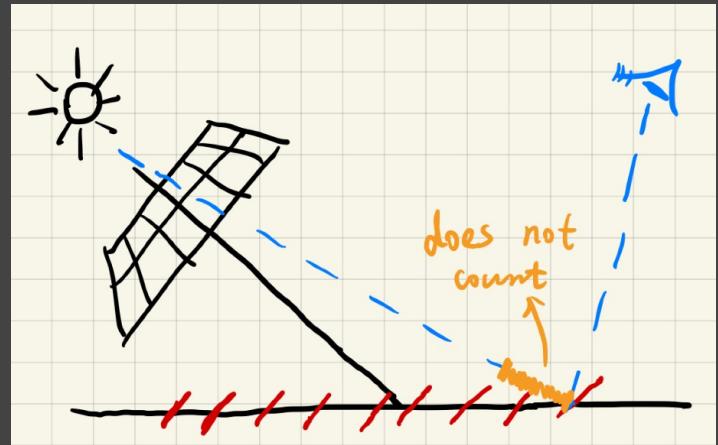


# Issues in Shadow Mapping

- Adding a (variable) bias to reduce self occlusion
  - But introducing detached shadow issue



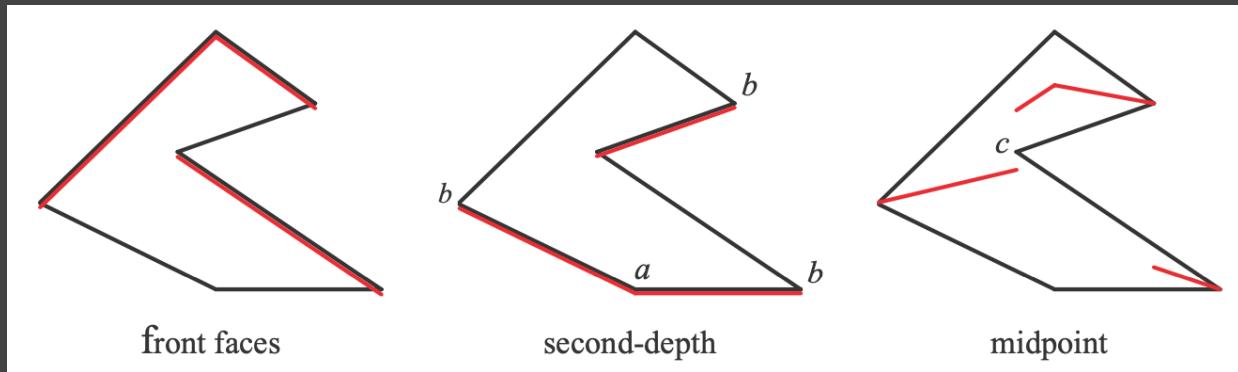
[Image from RTR4]



# Issues in Shadow Mapping

- Second-depth shadow mapping\*

  - Using the midpoint between first and second depths in SM
  - Unfortunately, requires objects to be watertight
  - And the overhead may not worth it

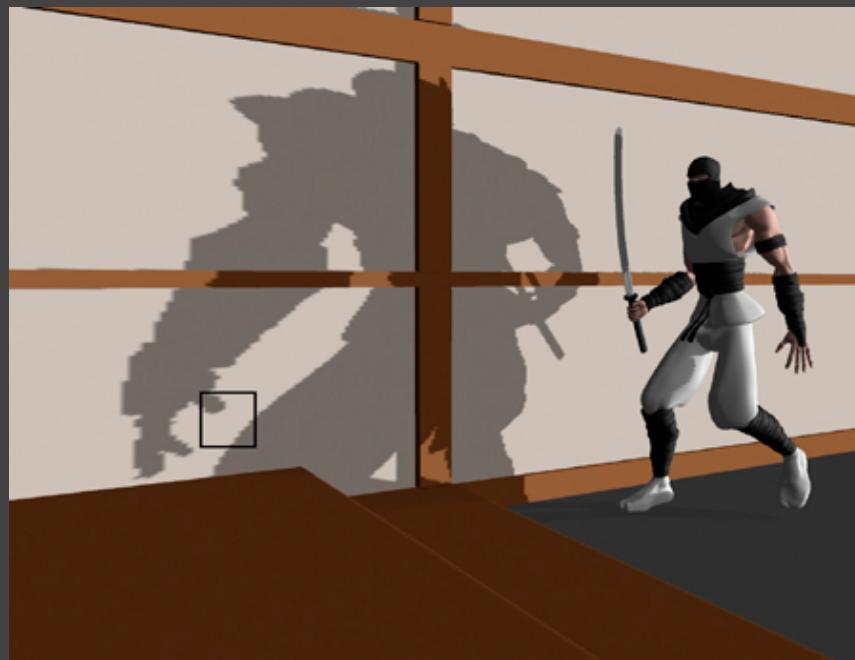


[Image from RTR4]

RTR does not trust in  
COMPLEXITY

# Issues in Shadow Mapping

- Aliasing



[[https://developer.download.nvidia.com/books/HTML/gpugems/gpugems\\_ch11.html](https://developer.download.nvidia.com/books/HTML/gpugems/gpugems_ch11.html)]

# Questions?

# Today

- Recap: shadow mapping
  - Issues from shadow mapping and solutions
- The math behind shadow mapping
- Percentage closer soft shadows
- Basic filtering techniques

# Inequalities in Calculus

- There are a lot of useful inequalities in calculus

12. 设  $f(x)$  和  $g(x)$  在  $[a, b]$  上都可积, 证明不等式:

(1) (Schwarz 不等式)  $\left[ \int_a^b f(x) g(x) dx \right]^2 \leq \int_a^b f^2(x) dx \cdot \int_a^b g^2(x) dx;$

(2) (Minkowski 不等式) <http://blog.csdn.net/>

$$\left\{ \int_a^b [f(x) + g(x)]^2 dx \right\}^{\frac{1}{2}} \leq \left\{ \int_a^b f^2(x) dx \right\}^{\frac{1}{2}} + \left\{ \int_a^b g^2(x) dx \right\}^{\frac{1}{2}}.$$

# Approximation in RTR

近似相等

- But in RTR, we care more about “approximately equal”
- An important approximation throughout RTR

$$\int_{\Omega} f(x)g(x) \, dx \approx \underbrace{\frac{\int_{\Omega} f(x) \, dx}{\int_{\Omega} \, dx}}_{\text{归一化, 使效率不变.}} \cdot \int_{\Omega} g(x) \, dx$$

- When is it (more) accurate?

1. 积分域  $\Omega$  较小且简单
2.  $g(x)$  光滑 smooth 变化不大.

# In Shadow Mapping

- Recall: the rendering equation with explicit visibility

$$L_o(p, \omega_o) = \int_{\Omega^+} [L_i(p, \omega_i) f_r(p, \omega_i, \omega_o) \cos \theta_i V(p, \omega_i)] d\omega_i$$

- Approximated as

$$L_o(p, \omega_o) \approx \frac{\int_{\Omega^+} V(p, \omega_i) d\omega_i}{\int_{\Omega^+} d\omega_i} \cdot \int_{\Omega^+} L_i(p, \omega_i) f_r(p, \omega_i, \omega_o) \cos \theta_i d\omega_i$$

*visibility*       $\times$       *<# shading>*

# In Shadow Mapping

$$L_o(p, \omega_o) \approx \frac{\int_{\Omega^+} V(p, \omega_i) d\omega_i}{\int_{\Omega^+} d\omega_i} \cdot \int_{\Omega^+} L_i(p, \omega_i) f_r(p, \omega_i, \omega_o) \cos \theta_i d\omega_i$$

- When is it accurate?

- Small support  
(point / directional lighting)
- Smooth integrand  
(diffuse bsdf / constant radiance area lighting)

其子之前称为半物理方法。

1. 当使用点光源 / 方向光源是准确的  
<此时区域很小，只有一个点或线>

g<sub>in</sub> 细颗粒。 g<sub>in</sub>: 光源。 BRDF.

面光源。光源有几何意义。  
uniform 光源  
shadow point  
是 diffuse.

- We'll see it again in Ambient Occlusions, etc.

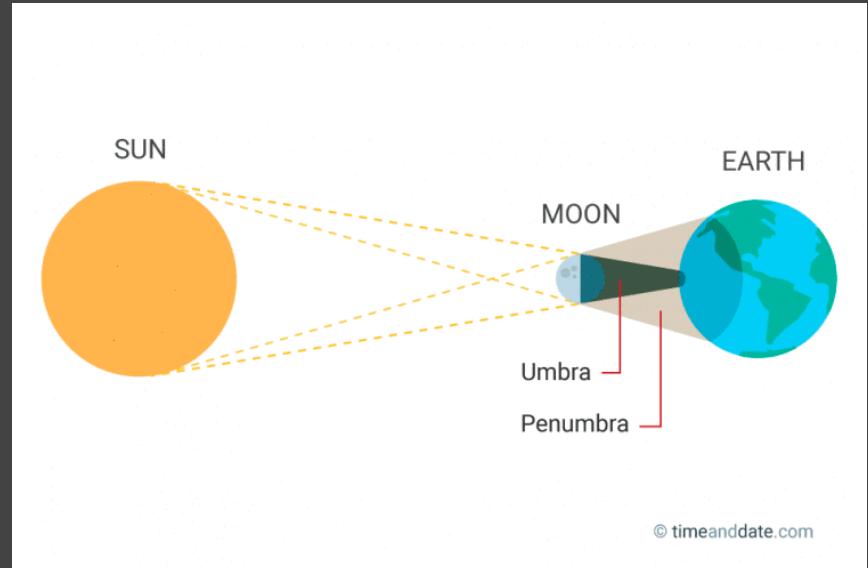
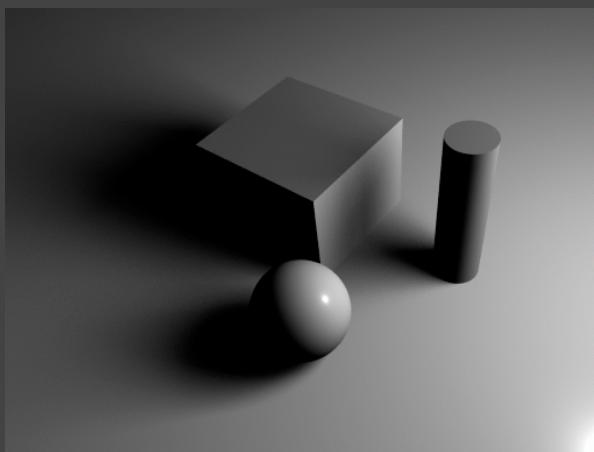
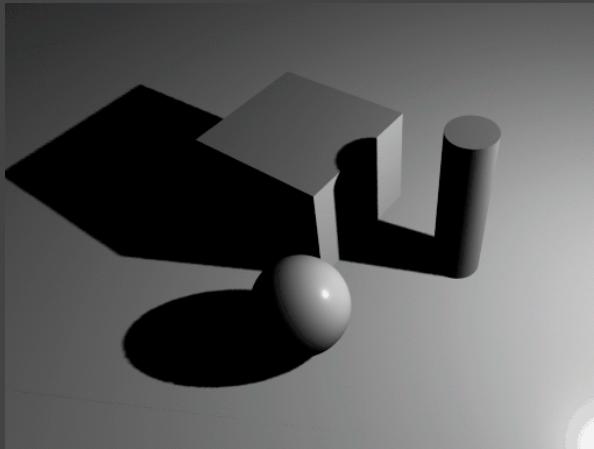
环境遮挡

# Questions?

# Today

- Recap: shadow mapping
  - Issues from shadow mapping and solutions
- The math behind shadow mapping
- Percentage closer soft shadows *PCSS*
- Basic filtering techniques

# From Hard Shadows to Soft Shadows



[<https://www.timeanddate.com/eclipse/umbra-shadow.html>]

# Percentage Closer Filtering (PCF)

反锯齿

在阴影边缘

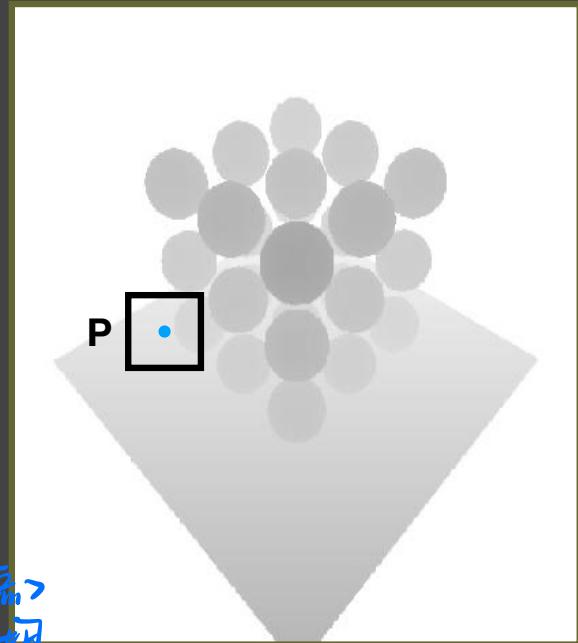
- Provides **anti-aliasing** at shadows' edges
  - Not for soft shadows (PCSS is, introducing later)
  - Filtering the results of shadow comparisons
- Why not filtering the shadow map?
  - Texture filtering just averages color components, i.e. you'll get blurred shadow map first
  - Averaging depth values, then comparing, you still get a **binary** visibility

1. 在做阴影判断时进行 filtering  
而非已得到 shadow map.  
对其进行模糊.
2. 不是纹理过滤, 而只是对颜色过滤  
进行平均|会得到模糊的阴影  
贴图. <已扭曲锯齿的阴影>

# Percentage Closer Filtering (PCF)

- Solution [Reeves, SIGGRAPH 87]
  - Perform multiple (e.g. 7x7) depth comparisons for each fragment
  - Then, averages **results of** comparisons
  - e.g. for point P on the floor,
    - (1) compare its depth with all pixels in the red box, e.g. 3x3
    - (2) get the compared results, e.g.  
1, 0, 1,  
1, 0, 1,  
1, 1, 0,
    - (3) take avg. to get visibility, e.g. 0.667

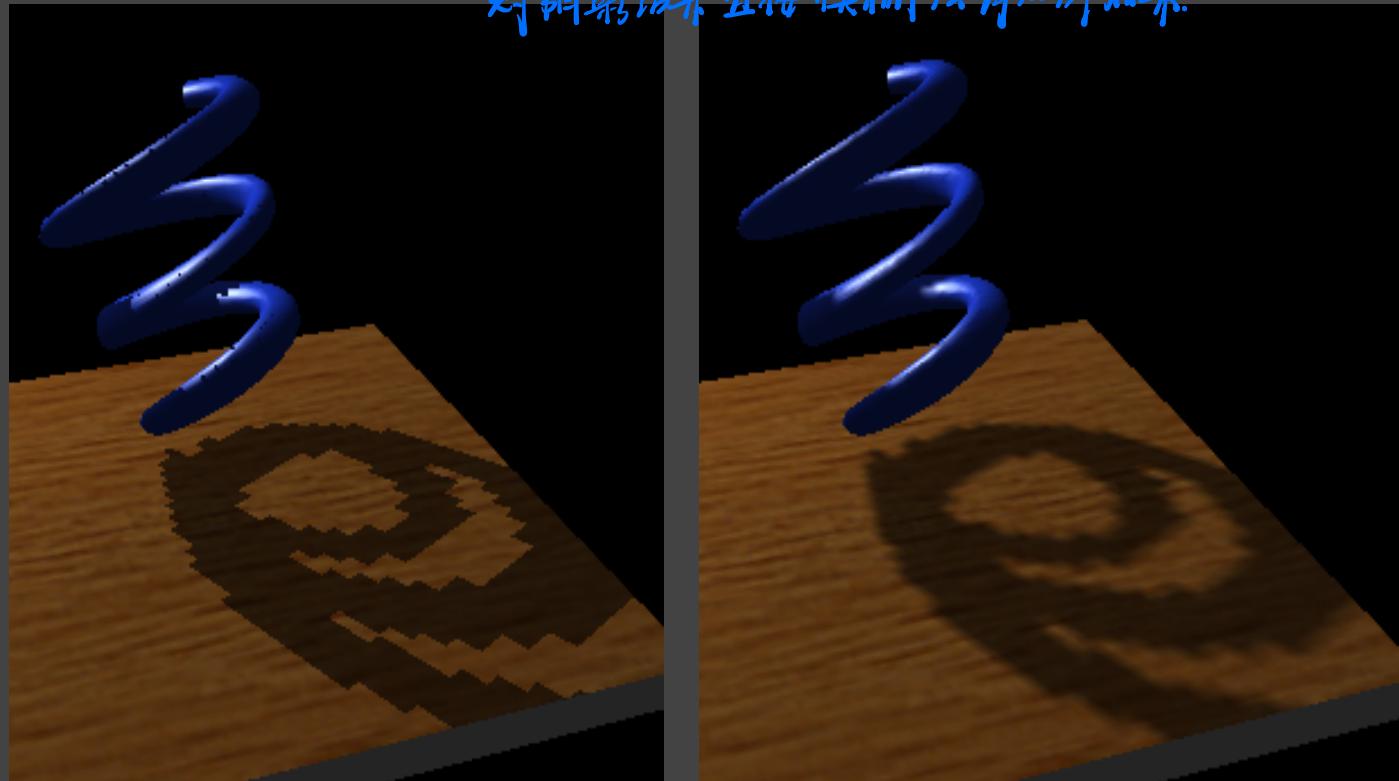
对某点深度值进行采样，映射到 shadow map 上。  
对周围 7 个像素进行比较，并对结果进行平均。



# Percentage Closer Filtering

Again, not soft shadows in the umbra/penumbra sense

对阴影场景直接模糊法有类似效果.



# Percentage Closer Filtering

<PCF>

锯齿消失. ✓



[[https://developer.nvidia.com/gpugems/GPUGems3/gpugems3\\_ch08.html](https://developer.nvidia.com/gpugems/GPUGems3/gpugems3_ch08.html)]

# Percentage Closer Filtering

- Does filtering size matter?
  - Small -> sharper
  - Large -> softer
- Can we use PCF to achieve soft shadow effects?
- Key thoughts
  - From hard shadows to soft shadows
  - What's the correct size to filter?
  - Is it uniform?

# Percentage Closer Soft Shadows

- Key observation [Fernando et al.]
  - Where is sharper? Where is softer?



[<https://graphicdesign.stackexchange.com/questions/71734/transfer-the-shadow-of-an-object-on-white-paper-to-ruled-paper>]

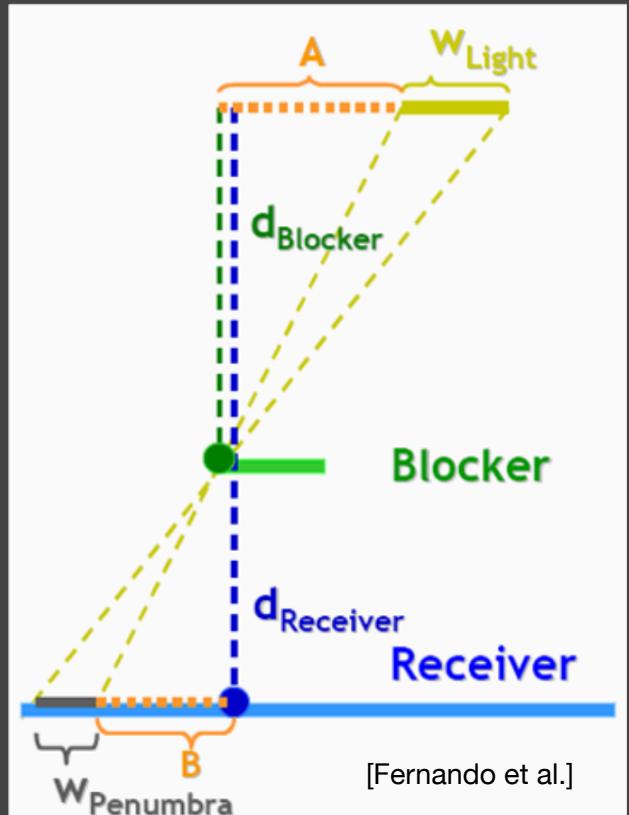
# Percentage Closer Soft Shadows

- Key conclusion
  - Filter size <-> blocker distance
  - More accurately, **relative average** projected blocker depth!  
相对平均投影拦截深度.
- A mathematical “translation”

$$w_{Penumbra} = (d_{Receiver} - d_{Blocker}) \cdot w_{Light} / d_{Blocker}$$

半影

“越小越强  
越大越弱”

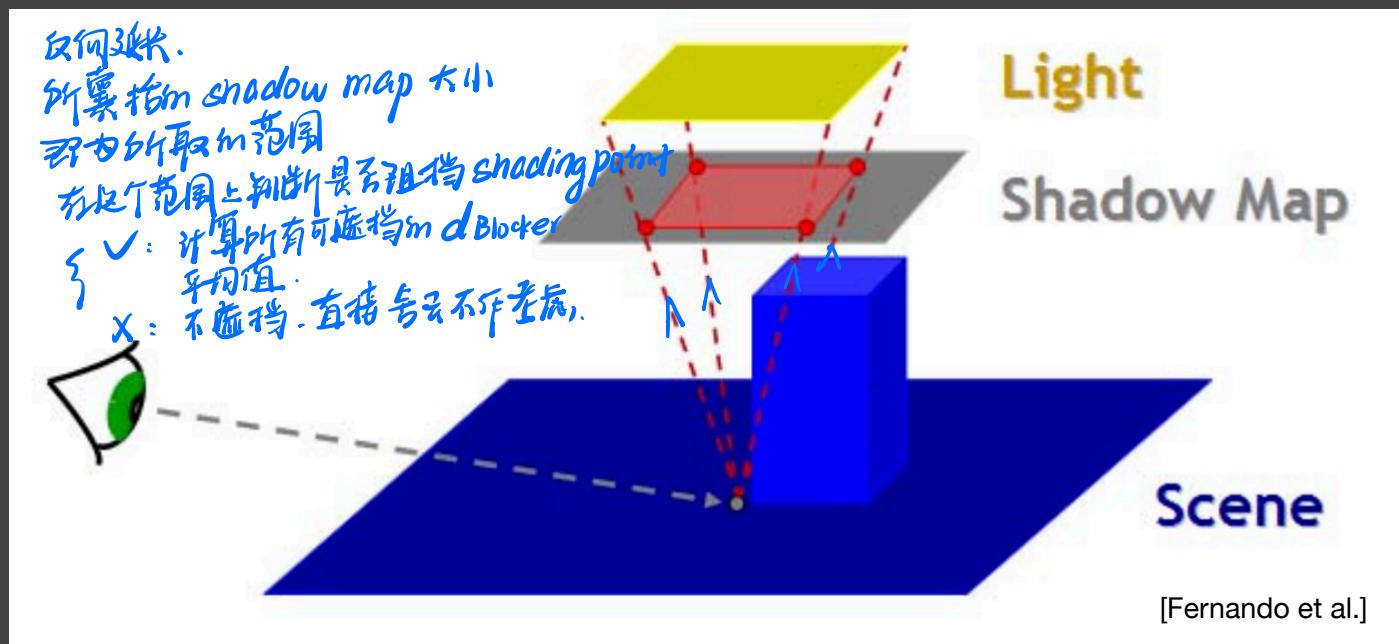


# Percentage Closer Soft Shadows

- Now the only question:
  - What's the blocker depth  $d_{\text{Blocker}}$
- The complete algorithm of PCSS
  - Step 1: Blocker search  
(getting the average blocker depth in a certain region)
  - Step 2: Penumbra estimation  
(use the average blocker depth to determine filter size)  $\omega_{\text{penumbra}}$
  - Step 3: Percentage Closer Filtering "PCF"
- Which region to perform blocker search?
  - Can be set constant (e.g. 5x5), but can be better with heuristics

# Percentage Closer Soft Shadows

- Which region (on the shadow map) to perform blocker search?
  - depends on the light size
  - and receiver's distance from the light



# Percentage Closer Soft Shadows

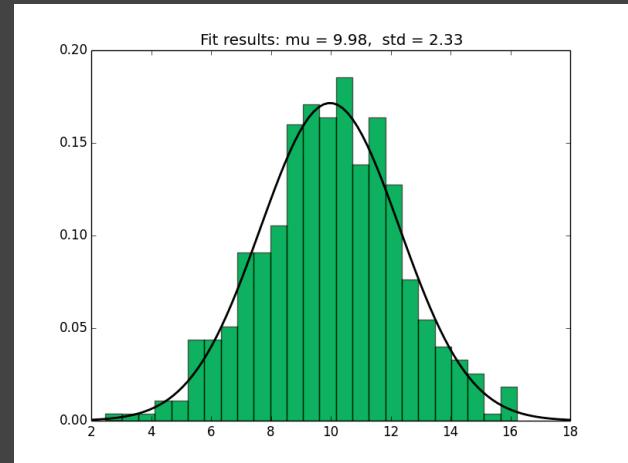


Video game: Dying Light

# Questions?

# Next Lecture

- Basic filtering techniques
- Variance soft shadow mapping
- MIPMAP and Summed-Area Variance Shadow Maps
- Moment shadow mapping



Thank you!