

$$\frac{d}{dx} \frac{1}{1+e^{-x}} = -(1+e^{-x})^{-2} \times (-e)^{-x}$$

$$= \frac{e^{-x}}{(1+e^{-x})^2} = \frac{1+e^{-x}-1}{(1+e^{-x})^2} = \frac{1}{1+e^{-x}} - \frac{1}{(1+e^{-x})^2}$$

$$= \delta(2)(1-\delta(2))$$

2. $W_0 = 0.5$, $W_1 = -0.6$, $b = 0.2$

x_1	x_0	y
0	1	0
0	0	1
1	1	1
1	0	1

① $0.5 \times 0 + (-0.6) \times 1 + 0.2 = -0.4$
 ② $0.5 \times 0 + (-0.6) \times 0 + 0.2 = 0.2$
 ③ $0.5 \times 1 + (-0.6) \times 1 + 0.2 = 0.1$
 ④ $0.5 \times 1 + (-0.6) \times 0 + 0.2 = 0.7$

2-2 $\eta = 0.05$ 설정

재분류

$$b = 0.2 + 0.05(1-0) \cdot 1 = 0.25$$

$$① (0,1) \quad -0.55 + 0.2 = -0.35 \quad P(-0.35) = 0$$

$$W_0 = 0.5 + 0.05(1-0) \cdot 1 = 0.55$$

$$(0,0) \quad 0.25 \quad P(0.25) = 1$$

$$W_1 = (-0.6) + 0.05(1-0) \cdot 1 = -0.55$$

$$(1,1) \quad 0.55 - 0.55 + 0.25 \quad P(0.25) = 1$$

$$(1,0) \quad 0.55 + 0.25 = 0.75 \quad P(0.75) = 1$$

∴ 모든 예외

3. $\eta = 0.05$ 설정

$$① = 0.5 \times 0.1 + 0.5 \times 0.2 \quad z_1(2) = 0.15$$

$$= 0.05 + 0.1 = 0.15$$

$$② \quad a_1(2) = \frac{1}{1+e^{-0.15}} = 0.54$$

$$③ \quad z_1(3) = 0.54 \times 0.4 + 0.54 \times 0.15 = 0.3$$

$$④ \quad a_1(3) = 0.57$$

$$⑤ \quad z_2(3) = 0.3 \times 0.4 + 0.3 \times 0.2 = 0.18$$

$$⑥ \quad a_2(3) = 0.54$$

$$⑦ \quad z_2(4) = 0.54 \times 0.45 + 0.54 \times 0.35 = 0.43$$

$$⑧ \quad a_2(4) = 0.61$$

$$3-2. \quad J_1 = \frac{1}{2}(0.57 - 0.5)^2 = 0.00245$$

$$J_2 = \frac{1}{2}(0.61 - 0.8)^2 = 0.01805$$

$$3-3) \eta = 0.1$$

$$\boxed{1} W_{2,1}^{(1)}$$

$$\frac{\partial J_{total}}{\partial W_{2,1}^{(1)}} = \left(\frac{\partial J_1}{\partial a_1^{(2)}} + \frac{\partial J_2}{\partial a_1^{(2)}} \right) \cdot \frac{\partial a_1^{(2)}}{\partial W_{2,1}^{(1)}} \cdot W_{1,2}^{(1)}$$

$$\boxed{2} W_{2,2}^{(2)} = \frac{\partial J_2}{\partial a_2^{(3)}} \times \frac{\partial a_2^{(3)}}{\partial z_2^{(3)}} \times \frac{\partial z_2^{(3)}}{\partial W_{2,2}^{(2)}}$$

$$\boxed{1} \frac{\partial J_1}{\partial a_1^{(2)}} \times \frac{\partial a_1^{(2)}}{\partial z_1^{(2)}} \times \frac{\partial z_1^{(2)}}{\partial a_2^{(2)}} \times \frac{\partial a_2^{(2)}}{\partial z_2^{(2)}} \times \frac{\partial z_2^{(2)}}{\partial W_{2,1}^{(1)}} + \frac{\partial J_2}{\partial a_2^{(3)}} \times \frac{\partial a_2^{(3)}}{\partial z_2^{(3)}} \times \frac{\partial z_2^{(3)}}{\partial a_2^{(2)}} \times \frac{\partial a_2^{(2)}}{\partial z_2^{(2)}} \times \frac{\partial z_2^{(2)}}{\partial W_{2,1}^{(1)}}$$

$$\textcircled{1} \frac{\partial J_1}{\partial a_1^{(2)}} = \frac{\partial}{\partial a_1^{(2)}} (a_1^{(2)} - y_1)^2 = (a_1^{(2)} - y_1) \quad 0.57 - 0.5 = 0.07$$

$$\textcircled{2} \frac{\partial a_1^{(2)}}{\partial z_1^{(2)}} = \sigma'(z_1^{(2)}) (1 - \sigma(z_1^{(2)})) = a_1^{(2)} (1 - a_1^{(2)})$$

$$= 0.57(1 - 0.57)$$

$$= 0.57(0.43)$$

$$= 0.245$$

$$\textcircled{3} z_1^{(2)} = a_1^{(1)} \times W_{1,1}^{(2)} + a_2^{(1)} \times W_{1,2}^{(2)}$$

$$\textcircled{4} = 0.54 \times 0.4 + 0.54 \times 0.15 = 0.3 \quad \text{and} \quad \frac{\partial z_1^{(2)}}{\partial a_2^{(1)}} = W_{1,2}^{(2)} = 0.15$$

$$\textcircled{5} \frac{\partial a_2^{(2)}}{\partial z_2^{(2)}} \times \frac{\partial z_2^{(2)}}{\partial a_2^{(1)}} = 0.124$$

$$\textcircled{6} a_2^{(2)} - y_2 = 0.61 - 0.8 = -0.19$$

$$\textcircled{7} 0.61 \times 0.39 = 0.24$$

$$\textcircled{8} 0.45$$

$$\textcircled{9} 0.54 \times 0.46 \times \frac{1}{2} = 0.124$$

$$\frac{\partial E_t}{\partial W_{2,1}^{(1)}} = 0.0003 + (-0.0003) = 0$$

$$\therefore W_{2,1}^{(1)} = 0.2 - 0.1(0) = 0.2$$

$$\textcircled{2} = \textcircled{5} \times \textcircled{6} \times 0.54 = -0.025$$

$$W_{2,2}^{(1)} = 0.45 - 0.1(-0.025) = 0.453$$